Direct Observation of the Quantum Critical Point in Heavy Fermion CeRhSi$_3$


DOI: [10.1103/PhysRevLett.108.177204](http://dx.doi.org/10.1103/PhysRevLett.108.177204)
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We report on muon spin rotation ($\mu$SR) studies of the noncentrosymmetric heavy fermion antiferromagnet CeRhSi$_3$. A drastic and monotonic suppression of the internal fields, at the lowest measured temperature, was observed upon increase of external pressure. Our data suggest that the ordered moments are gradually quenched with increasing pressure, in a manner different from the pressure dependence of the Néel temperature. At 23.6 kbar the ordered magnetic moments are fully suppressed via a second order phase transition and $T_N$ is zero. Thus, we directly observed the quantum critical point at 23.6 kbar hidden inside the superconducting phase of CeRhSi$_3$.

PACS numbers: 76.75.+i, 75.50.Ee, 75.30.Mb, 75.40.Cx

The role of magnetism in many superconducting materials is a topic of intense research. Often, these materials display a quantum critical point (QCP) that separates a nonmagnetic from a magnetic metallic phase [1–3]. This usually leads to the formation of new phases of matter, whose properties are dominated by quantum fluctuations. These fluctuations can be fine-tuned by an external parameter, such as chemical substitution, magnetic field or external pressure. The location and nature of QCPs are central to the understanding of the interplay between superconductivity and magnetism in these systems. In a number of heavy fermion (HF) compounds such as CePd$_2$Si$_2$, CeIn$_3$, and CeIrSi$_3$, the QCP is buried deep inside of a superconducting phase in the pressure-temperature phase diagram [2, 4, 5]. In these cases it is challenging to establish the presence of a QCP and to study the microscopic magnetic properties coexisting with superconductivity. In this $\mu$SR study on the HF CeRhSi$_3$, we uncovered the previously conjectured QCP hidden inside the superconducting phase. We directly observed the disappearance of the ordered magnetic moments at the critical pressure $p^* = 23.6$ kbar deep inside the superconducting phase. This suppression of the ordered moments was found to be accompanied by a zeroing of the Néel temperature at $p^*$ suggesting that this QCP is of magnetic nature.

CeRhSi$_3$ is a noncentrosymmetric HF system [6–8], suspected to display a QCP [6, 9, 10] at pressures of the order of 26 kbar. The compound features an intriguing phase diagram. It displays an AFM phase at ambient and applied pressure and a superconducting phase for pressures $p > 12$ kbar [6, 11]. Measurements of the de Haas-van Alphen effect at ambient and applied pressure show that the f-electrons are itinerant up to at least 30 kbar [9]. Neutron diffraction at ambient pressure showed that the magnetic order is incommensurate, with ordered moments of the order of 0.1 $\mu_B$/Ce [12]. From previous results of thermal and transport properties it was established that the antiferromagnetic ordering temperature $T_N \approx 1.6$ K at ambient pressure, initially increases with increasing pressure, and then decreases towards the superconducting transition temperature $T_c \sim 1$ K for $p \approx 20$ kbar. The nature of the magnetism above this pressure across the proposed QCP inside the superconducting phase is unclear.

Single crystal CeRhSi$_3$ platelets were grown via a standard metal flux technique [13] with initial molar ratios of 1:1:3:30 (Ce:Rh:Si:Sn). The high quality of our single crystal samples was verified by the results of X-ray Laue diffraction and by measurements of the residual resistance ratio $\rho_{300}$/$\rho_0$ which was found to be of the order of 110.

$\mu$SR measurements at ambient pressure were performed using the Low Temperature Facility spectrometer (LTF) at the Paul Scherrer Institut (PSI). Measurements under pressure were conducted on the General Purpose Decay-Channel spectrometer (GPD). For zero-field (ZF) and longitudinal-field (LF) measurements we typically counted 6 × 10$^6$ positron events per spectrum and 0.5 × 10$^6$ for transverse-field (TF) measurements, respectively.

The single crystal sample consisted of platelets with an average thickness of 0.1 mm. For the measurement on LTF they were attached to a silver plate, with the crystal c-axis perpendicular to the plate and parallel to the muon beam covering an area of $\sim 1$ cm$^2$. For pressure measurements they were stacked in a cylindrical volume.
A muon stops at a site with an internal field components, which are proportional to the probability that applied pressures on LTF ($p = 0$ kbar) and GPD ($p = 6.8$ and 16.9 kbar) from single crystal and polycrystalline CeRhSi$_3$ samples. (a) The time spectra at different pressures at base temperature (0.02 and 0.27 K, respectively) and their corresponding fits (black lines) according to Eq. (1). (b) FFTs of the time spectra shown in (a). Both the spectra in (a) and the FFTs in (b) are vertically shifted for better illustration.

of 1 cm$^3$ (mass $\sim 500$ mg). In addition, a 1 g polycrystalline sample of CeRhSi$_3$ was measured under pressure.

In Fig. 1 ZF time spectra and the corresponding fast Fourier transforms FFTs for several pressures at a base temperature (0.02 K and 0.27 K for LTF and GPD, respectively) are shown for single crystal and polycrystalline samples. The signal from the Ag plate and the pressure cell, respectively, has been subtracted, (see Supplemental Material for details). The signals shown in Fig. 1 reveal a fast decay and a characteristic time structure, expected in the case of a signal containing several oscillatory components. The fast Fourier transform (FFT) of the time spectrum at $p = 0$ kbar (see Fig. 1(b)), displays three well-defined distributions of internal magnetic fields centered at $\sim 0$, 45 and 120 G. Therefore, the ZF sample asymmetry function is described here by three terms:

$$A_{\text{CeRhSi}}(t) = \sum_{i=1}^{3} A_i \cdot g_i(t),$$  

$$g_i(t) = \alpha \cdot \cos(\gamma_{\mu} B_i t) \cdot e^{-\lambda_T t} + (1 - \alpha) \cdot e^{-\lambda_L t},$$

where $\gamma_{\mu}/2\pi = 135.5$ MHz/T with $\gamma_{\mu}$ the muon gyromagnetic ratio. $B_i$ denote the average internal magnetic fields at the muon stopping sites in the sample. $\alpha$ was found to be $\frac{2}{3}$, which is not a priory evident for single crystals, but is always the case for polycrystalline samples. $A_i$ are the asymmetries at time 0 of the individual components, which are proportional to the probability that a muon stops at a site with an internal field $B_i$. We find: $A_1 = A_2$ and $A_3 = 1.5 \cdot A_1$. $\lambda_T$ and $\lambda_L$ are the transverse and longitudinal muon relaxation rates, respectively. $B_i$, $\lambda_T$ and $\lambda_L$ are temperature dependent. The relations $B_1/B_2 \approx 2.6$ and $\lambda_T/\lambda_L \approx 2.6$ were found experimentally: $B_3$ was found to be roughly 0 for all temperatures and pressures.

The weights of the spectra in Fig. 1(b) shift to lower fields with increasing pressure, that is, the quasi-static internal fields are increasingly suppressed with pressure. Since the AFM structure is incommensurate, one might expect that the quality of the fits would improve by replacing the cosine terms in Eq. (1) by Bessel functions, as in the case of UNi$_2$Al$_3$ [14, 15], CeAl$_3$ [15] or CeCu$_5$Au [16]. This replacement, however, leads to fits of lower quality, and will not be considered further here.

High-pressure data at low and high temperatures are shown in Fig. 2. In the time spectrum at 20.4 kbar and $T = 0.27$ K $\ll T_N$ we observe a fast relaxation and slow oscillations. Both of these features are absent at $T = 1.76$ K $> T_N$ showing that the low-temperature data reflects the presence of internal magnetic fields arising from magnetic order. For the data at 23.6 kbar, the fast relaxation and the oscillations are absent and there is no significant change from the high temperature to the low temperature signal at $T = 0.27$ K. This demonstrates the absence of magnetic order down to at least 0.27 K, the lowest temperature of these experiments. Since at this pressure the internal magnetic fields are zero, $T_N$ is most likely zero.

In the results of resistivity and specific heat measurements CeRhSi$_3$ was found to be superconducting for $p > 12$ kbar and low $T$, our results therefore demonstrate that over the pressure region 12 kbar $< p < 23.6$ kbar superconductivity and AFM order coexist, as indicated in earlier measurements [6].

FIG. 1. (Color online) ZF measurements at various applied pressures on LTF ($p = 0$ kbar) and GPD ($p = 6.8$ and 16.9 kbar) from single crystal and polycrystalline CeRhSi$_3$ samples. (a) The time spectra at different pressures at base temperature (0.02 and 0.27 K, respectively) and their corresponding fits (black lines) according to Eq. (1). (b) FFTs of the time spectra shown in (a). Both the spectra in (a) and the FFTs in (b) are vertically shifted for better illustration.

FIG. 2. (Color online) ZF data from the polycrystalline sample at (a) 20.4 kbar and (b) 23.6 kbar at two different temperatures. The time spectra were fitted using Eq. (1). The signal of the pressure cell was subtracted.
Eq. (1) are depicted in Fig. 4 as a function of pressure. Above \( p = 16.3 \text{kbar} \) the field distribution is very broad. Still, over the entire antiferromagnetically ordered region one observes a pressure independent ratio \( B_1/B_2 \). This implies that the magnetic structure does not change appreciably with pressure. In addition, our data show that near \( p^* \) the fast relaxation characterizing the ZF data in the AFM state vanishes.

The ZF data in the AFM state shows, in addition to the tiny ordered moments, a fast initial relaxation. As we shall see, the fast relaxation is not caused by fluctuating (large) moments, as it would be in the case where Kondo screening were destroyed and the local Ce moments were restored. The results of \( \mu \)SR measurements at longitudinal fields at \( p = 16.3 \text{kbar} \) (see Fig. 3) showed that at modest external fields of 200 gauss (of the order of the internal quasi-static fields) the muon relaxation is substantially suppressed. That means that the \( \mu^+ \) spin is fully decoupled from the internal magnetic field, demonstrating that the weak internal fields are static rather than dynamic and supporting the quasi static origin of the relaxation at the pressure 16.3 kbar. We find no evidence for dynamical relaxation at any pressure in the low-temperature region of the AFM phase. Above \( T_N \) at \( p = 0 \text{kbar} \) an LF measurement was also conducted and complete decoupling from internal fields was observed at an applied field of \( \sim 200 \text{G} \), showing the absence of appreciable dynamical relaxation above \( T_N \). Thus, our data supports a scenario where the Ce moments are quenched at all pressures below \( p^* \), and where the Kondo screening remains largely intact.

The normalized static internal fields \( B_1/B_1(0)(p) \) (equivalent to \( B_2/B_2(0)(p) \)) extracted from the fits using Eq. (1) are depicted in Fig. 4 as a function of pressure (circles). \( B_1(0) \) denotes the internal field at the lowest measured pressure \( p = 0 \text{kbar} \). \( B_1 \) decreases monotonically with pressure and vanishes near \( p^* \sim 23.6 \text{kbar} \), showing that magnetic order is suppressed at \( p^* \). For the two highest measured pressures the field distribution is very broad. Still, over the entire antiferromagnetically ordered region one observes a pressure independent ratio \( B_1/B_2 \). This implies that the magnetic structure does not change appreciably with pressure. In addition, our data show that near \( p^* \) the fast relaxation characterizing the ZF data in the AFM state vanishes.

The Néel temperature as a function of pressure was obtained with \( \mu \)SR measurements in transverse fields of 50 and 300 gauss, respectively. Below the Néel temperature the magnetic order leads to an extra fast relaxation so that the total asymmetry after some time, \( t > 1 \mu s \), in our case, is smaller than the corresponding amplitude above \( T_N \). The time spectra for \( t > 1 \mu s \) were fitted using

\[
A(t) = A_{1\mu s} \cdot \exp \left( -\frac{1}{2}(\sigma t)^2 \right) \cdot \cos(\gamma_B t),
\]

where \( A_{1\mu s} \) is the asymmetry at 1 \( \mu s \) after the muon is implanted. \( B \) represents the local field and is a fit parameter. Upon cooling, one observes a rapid decrease of \( A_{1\mu s} \), as the system enters the AFM state. The Néel temperature is associated with the onset of the drastic steplike reduction of \( A_{1\mu s}(T) \) with decreasing temperature. One example of \( A_{1\mu s}(T) \) for \( p = 20.4 \text{kbar} \) is shown in the inset of Fig. 4.

The results for \( T_N \) at different pressures are shown in Fig. 4 as diamonds. \( T_N(p) \) shows a maximum at around 7 kbar, consistent with the results of resistivity [6, 11] and specific heat [17] measurements. By contrast, the internal fields and, therefore, the ordered magnetic moments decrease monotonically. We find that the internal fields and \( T_N \) vanish at the critical pressure of \( p^* = 23.6 \text{kbar} \) and magnetic order disappears. Our data show that the AFM order is completely suppressed for \( p \geq p^* \), and that there is a continuous tuning of the AFM phase with pressure. All this indicates the presence of a magnetic QCP.

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**Fig. 3.** (Color online) \( \mu \)SR time spectra of the single crystal sample in zero and longitudinal field at \( T = 0.27 \text{K} \) and \( p = 16.3 \text{kbar} \). The pressure cell signal (background) was subtracted.

**Fig. 4.** (Color online) Comparison of the pressure dependence of the Néel temperature (diamonds) and the normalized internal field \( B_1/B_1(0) \) (circles). The lines are guides to the eye. The inset shows the asymmetry \( A \) at 1 \( \mu s \) after the muon is implanted. \( B \) represents the local field and is a fit parameter. Upon cooling, one observes a rapid decrease of \( A_{1\mu s} \), as the system enters the AFM state. The Néel temperature is associated with the onset of the drastic steplike reduction of \( A_{1\mu s}(T) \) with decreasing temperature. One example of \( A_{1\mu s}(T) \) for \( p = 20.4 \text{kbar} \) is shown in the inset of Fig. 4.
at $p^*$. The different pressure dependencies of the Néel temperature and that of the internal fields may be understood using the simplified, but widely used, one-dimensional Kondo lattice model described by S. Doniach [18]. The model considers the competing effects of the Kondo screening and the exchange interaction between Ce moments which tend to stabilize the magnetic moments leading to magnetic order. The results are summarized in the so-called Doniach phase diagram, displaying the Néel temperature $T_N$ as a function of the product $|JN_F|$ of the exchange coupling $J$ and the density of states of the conduction electrons at the Fermi level $N_F$. For low values of $|JN_F|$ the system is magnetically ordered and $T_N$ increases with increasing $|JN_F|$. Further increase of $|JN_F|$ yields a maximum of $T_N$ and a subsequent decrease (observed, for instance in CeAg [19]). $T_N$ eventually reaches zero, and further increase in $|JN_F|$ yields a nonmagnetic (Fermi liquid) system.

In our case, the product $|JN_F|$ is tuned with external pressure. The observation of the maximum of $\langle T_N(p) \rangle$ and the subsequent suppression of $T_N$ to zero, suggests that the application of rather modest pressures leads to substantial changes of $|JN_F|$. At the same time, the Doniach model predicts a monotonic decrease of the ordered moments with increasing $J$ according to [18] $\langle S^x \rangle = \sqrt{1-(J/W)^2}$, where $W$ is the conduction electron bandwidth and $S^x$ is the $x$-component of a spin $S$. These predictions match qualitatively our experimental observations.

We emphasize that the order parameter, i.e., the sublattice magnetization (or more precisely the amplitude of the spin density wave), represented here by the internal fields, displays a continuous phase transition with pressure and the Néel temperature goes to zero at $p^*$. This clearly reveals the presence of a QCP. In our case, it lies deep in the superconducting phase, and its bulk properties are masked by superconductivity. Nevertheless, it has been reported that between 20 – 26 kbar and $T > 1$ K, non-Fermi-liquid behavior [6] is observed in the temperature dependence of the electrical resistivity, adding support to our claim. Further indications for a QCP may be extracted from the extremely high upper critical field $H_{c2}$ ($H_{c2}(T)$) and its sensitivity to pressure for $p > 26$ kbar [20]. Both the behavior of the resistivity and that of $H_{c2}$ may be explained theoretically in terms of antiferromagnetic spin fluctuations in three dimensions close to the QCP [10]. From the results of transport measurements, it was not clear what the critical pressure should be. Nevertheless, the authors suggest that $p^*$ is about 26 kbar [20], a value not compatible with our findings. In the results of de Haas-van Alphen measurements no change in the size of the Fermi surface across $p^*$ was observed [9]. That is, the Kondo screening of the Ce moments is active at pressures on both sides of $p^*$. All this hints at a SDW type QCP [1, 2], consistent with our findings. This type of QCP is driven by quantum fluctuations of the magnetic order parameter, as opposed to the so called local QCP where the Kondo screening is destroyed and the local moments are restored in the magnetically ordered phase, i.e. $p < p^*$.

In summary, we have measured the pressure evolution of the internal fields of the AFM phase of CeRhSi$_3$ with the μSR technique. As a function of pressure the internal fields diminish continuously with increasing pressure, in clear contrast to the complex behavior of the Néel temperature which shows a maximum at around 7 kbar. Our observations may be understood in the framework of the Doniach phase diagram. This analysis reveals a strong sensitivity of $|JN_F|$ to the externally applied pressure for CeRhSi$_3$. At $p^* \approx 23.6$ kbar the system becomes nonmagnetic and signals the presence of a magnetic QCP, masked by the superconducting phase. We find no evidence for a breakdown of the Kondo screening across the QCP.

This work was performed at the Swiss Muon Source (SμS), Paul Scherrer Institut (PSI Villigen, Switzerland). We thank A. Amato and H. Luetkens for helpful discussions and M. Elender for technical support. We acknowledge the financial support of the Swiss National Science Foundation. D. A. acknowledges financial support from the Romanian UEFISCDI Project PN-II-ID-CE-2011-3-0583 (85/2011). A. D. B. received support from the Natural Sciences and Engineering Research Council of Canada (Canada), Fonds Québécois de la Recherche sur la Nature et les Technologies (Québec), and the Canada Research Chair Foundation. Work at UC Riverside was supported by U.S. NSF Grant 0801407.

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