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Fragility of surface states and robustness of topological order in 

$\text{Bi}_2\text{Se}_3$ against oxidation

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Topological surface states are protected against local perturbations, but this protection does not extend to chemical reaction over the whole surface, as demonstrated by theoretical studies of the oxidation of $\text{Bi}_2\text{Se}_3$ and its effects on the surface spin polarization and current. While chemisorption of $\text{O}_2$ largely preserves the topological surface states, reaction with atomic $\text{O}$ removes the original surface states and yields two new sets of surface states. One set forms a regular Dirac cone but is topologically trivial. The other set, while topologically relevant, forms an unusual rounded Dirac cone. The details are governed by the hybridization interaction at the interface.

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Surface states in topological insulators [1-4] are of great interest for spin information technology applications. These states are protected by time-reversal symmetry against local perturbations and are therefore quite tolerant to system imperfections and minor environmental effects [1, 5-8]. This Letter addresses a key issue: Can they be robust against oxidation, which can affect all air-exposed samples? Oxidation is also a processing step often employed in device fabrication, and its effects on the surface electronic and spin structure of topological materials are of great interest. It should be stressed that topological order, being a bulk property, is independent of the surface conditions, but the surface states and their spin properties can undergo drastic changes. We have chosen to perform a theoretical study of the oxidation of Bi$_2$Se$_3$.

Among the known topological insulators [9-12], Bi$_2$Se$_3$ is one of the most technologically promising because of its wide band gap, a single Dirac cone, a simple structure, a natural cleavage plane, and its ease of preparation by molecular beam epitaxy [13]. However, its surface is prone to adsorption by residual gas [14], air [15], carbon monoxide [16], and oxygen [17], making it an excellent model system for the present study.

We perform first-principles calculations to determine the electronic structure of Bi$_2$Se$_3$ upon adsorption by molecular O$_2$ or atomic O, with an emphasis on the spin polarization and current that are relevant to applications. The nature of the chemical transformation is elucidated by following the parentage and heritage of the old and new surface states. While chemisorption of O$_2$ largely preserves the topological surface states, reaction with atomic O removes the original surface states and yields two new sets of surface states with unusual features. Although the topological constraint of the substrate guarantees that one (and only one) of the two sets must be topologically relevant, the surface spin current is very much reduced. This finding shows that air
exposure can be a serious concern for such materials, and surface states of pristine topological insulators are not necessarily relevant to applications.

Our calculations were performed using a density functional approach within the local density approximation. The wave functions and eigenvalues are evaluated using the Abinit package [18, 19], from which we compute the charge separation, spin polarization, spin current, and other quantities of interest. The computation was based on a plane-wave basis, with the cutoff energy set at 400 eV. Reciprocal space sampling was carried out with a 4×4×1 grid. The HGH pseudopotential used in the computation is fully relativistic, but the spin-orbit coupling can be manually turned off. We employed the experimental lattice constants for the lattice structure of Bi$_2$Se$_3$.

The structure of Bi$_2$Se$_3$ consists of a periodic stacking of quintuple layers (QLs) [9], with each QL made of three Se atomic layers intercalated by two Bi atomic layers [20]. The inter-QL bonding is weak, and the stable surface is an outer Se atomic plane of a QL. Calculations for various slab thicknesses were performed. The surface states of bare slabs thicker than about 6 QLs were essentially independent of the slab thickness, implying that the interaction or overlap of the surface states associated with the two faces of the slab could be ignored for the thicker slabs [21]. We employed a slab thickness of 10 QL in the final calculations in order to be well above this limit. A supercell geometry was employed, with the spacing between neighboring slabs set at 15 Å. The equilibrium adsorption geometries of O$_2$ and O on the surface were determined by minimizing the forces to less than 1×10$^{-6}$ Ha/Bohr.

Reaction of Bi$_2$Se$_3$ with oxygen gas initiates with the adsorption of molecular O$_2$. Calculations show that O$_2$ adsorbs on a surface Se atom in a linear straight-up configuration. The
O-O bond is slightly elongated (1.37 vs. 1.21 Å), suggesting a weakened molecular bond. The chemisorption bond, with a bond energy of 0.12 eV, is weak [22]. For reference, the band structure of a pristine 10-QL slab of Bi$_2$Se$_3$, shown in Fig. 1(a), shows two topological surface bands, A$_{1,2}$. The other bands are quantum-well states. The shading indicates the projected bulk band regions. Bands A$_{1,2}$ intersect at the Dirac point DP$_A$ to form a Dirac cone. The band structure after O$_2$ adsorption (Fig. 1(b)) shows a similar Dirac point at DP$_{A'}$. The additional bands in the gap are derived from the $2p_x$, $2p_y$ states of O$_2$. The $2p_z$ bonding states, at lower energies, are outside the display area of the figure. The chemical interaction, though weak, causes A$_{1,2}$ to hybridize with the O$_2$ 2$p$ bands [23], resulting in a small anticrossing gap.

Further oxidation results in the dissociation of O$_2$ [17] and the bonding of each surface Se atom by an O atom directly atop at a Se-O bond length of 1.72 Å. The calculated bond energy is 4.5 eV. With the bond energy of O$_2$ being 5.2 eV [24], oxidation of the surface is highly exothermic with an excess energy of $2 \times 4.5 - 5.2 = 4.2$ eV. The calculated band structure (Fig. 1(c)) reveals two surface state pairs B$_{1,2}$ and C$_{1,2}$, which cross at DP$_B$ and DP$_C$, respectively. DP$_B$ is Dirac-like, but both bands B$_{1,2}$ merge into the valence band region and are topologically trivial. By contrast, bands C$_{1,2}$ are parabolic near the zone center. The result is a highly unusual rounded (rather than pointed) Dirac cone with a finite effective mass. These bands span the bulk gap, and the topological order of the system is preserved. Calculations for the same oxidized slab but with the spin-orbit coupling turned off (Fig. 1(d)) show that the band gap is no longer spanned by surface states, and the system becomes topologically trivial.

The above results (Figs. 1(a) and 1(c)) do not reveal the connection between the original surface states and the new ones. We resolve this question by placing the oxygen atoms far away from the substrate, where the interaction with the substrate is minimal, and then moving the
oxygen atoms gradually to the equilibrium bonding positions. With the O-Se bond stretched by 1.2 Å (Fig. 2(a)), the original surface state pair can be identified with a slightly altered crossing point at DP\(_{A'}\). The other states in the gap are derived from the mostly decoupled oxygen 2\(p\) states. Reducing the O-Se stretch to 0.8 Å (Fig. 2(b)) pushes DP\(_{A'}\) downward, and the oxygen states split and develop more complex shapes. As the O atoms further approach the Se, the original surface states move into the valence band region (Fig. 2(c)). Finally, the oxygen-derived states become the new surface states (Fig. 2(d)). It is interesting to note that when DP\(_{A'}\) merges into the valence band region, DP\(_{C}\) moves into the gap, and the topological order of the system is maintained throughout the process. This Dirac point tuning, however, cannot be (easily) realized experimentally.

The slabs, with or without adsorbed oxygen on both faces, have inversion symmetry. Consequently, all states form spin-degenerate Kramers doublets [25]. The two surface states in a doublet are separately localized near the two faces of the slab [26] in accordance with the Rashba interaction [27, 28]. All bulk-derived doublets should exhibit no such charge and spin separations in the bulk limit, but small separations can occur in thin films. To quantify these properties, we define, for each band along the \(\Gamma \overline{M} (k_x)\) direction, a charge-separation function:

\[
\Delta C(k_x) = \frac{2}{D} \sum_i \langle \Psi_i(k_x) | z \rangle \langle z | \Psi_i(k_x) \rangle - 1,
\]

where \(D\) is the slab thickness, \(z = 0\) is at the midpoint of the slab, and the summation is over the two states in each Kramers doublet. This function ranges from +1 (charge concentrated at the surfaces at \(z = \pm D/2\)), to 0 (uniform distribution), and to –1 (charge concentrated at the mid-plane of the slab). Likewise, we define a spin-polarization (or spin-imbalance) function:
\[ P(k_x) = \frac{1}{\hbar} \sum_i \langle \Psi_i(k_z) | s_y \, \text{sgn}(z) | \Psi_i(k_z) \rangle, \] (2)

where \( \text{sgn}(z) \) is the sign function, and \( s_y \) is the spin operator along \( y \), the only direction yielding a nonzero spin polarization by symmetry. This function equals \( \pm 1 \) if the top (bottom) half of the slab carries an electron with its spin fully polarized along \( \pm y \) (\( \mp y \)). The \( y \)-polarized spin current along the \( x \)-direction is given by

\[ I(k_x) = P(k_x) \frac{v_x(k_x)}{v_0}, \] (3)

where \( v_x \) is the \( x \)-component of the group velocity. \( I \) is normalized to \( \pm 1 \) for a surface state doublet with a full spin imbalance and traveling at the characteristic velocity of \( v_0 = \hbar k_T/m \), where \( m \) is the free electron mass.

The values of \( \Delta C, P, \) and \( I \) for a bare 10-QL slab of \( \text{Bi}_2\text{Se}_3 \) are computed for \( A_{1,2} \) and the two neighboring quantum-well bands \( P \) and \( Q \) (Figs. 3(a)-(d)). Bands \( A_{1,2} \) exhibit large \( \Delta C, P, \) and \( I \) within the band gap. These properties diminish as the surface states disperse away from the zone center, approach, and eventually merge into the bulk region. Bands \( P \) and \( Q \) show little spin polarization near the zone center but have a negative charge separation, meaning that the charge density is suppressed near the slab faces. Because of the tendency toward charge neutrality within the slab, the accumulated surface charge from the surface states must be compensated for by a reduction of charge associated with nearby quantum-well states.

The above results are qualitatively as expected based on the Rashba interaction [27, 28]. The corresponding results for \( \text{Bi}_2\text{Se}_3-\text{O} \) (Figs. 3(e)-(h)) are substantially more complex. States
B_{1,2} and C_{1,2} all show a strong charge separation within the gap. However their charge separations and those of the neighboring quantum-well bands P and Q show complex variations outside the gap (at larger $k_x$). The reason is a strong hybridization of these bands with the O states, resulting in a significant surface charge. The spin-polarization functions also show complex variations for a similar reason. The key quantity of interest to applications, the spin current, is generally much weaker after oxidation. The large reduction for C_{1,2}, which span the bulk gap and would be candidates for surface transport, is partly caused by the smaller group velocities of the bands within the gap. Because of the parabolic dispersions at the zone center, the spin current actually vanishes there.

The characters of B_{1,2} and C_{1,2} are clarified by the calculated charge distributions at a point close to the zone center ($k_x \rightarrow 0$). Fig. 4 presents charge distributions within a $2 \times 2$ surface cell in the oxygen plane (left panels); the dash-dotted lines indicate where $xz$ and $yz$ cuts are made to reveal the vertical distributions (right panels). The charge, strongly concentrated around each O atom, shows the oxygen $2p_{\alpha\beta}$ orbital characters for B_{1,2}, respectively. For C_{1,2}, the orbital characters are $2p_x \pm i2p_y$ with an azimuthally isotropic donut-shaped distribution. All of these oxygen-derived states hybridize with the substrate states, but C_{1,2} involve mostly just the 4p states associated with the top Se atomic layer [20]. The topological states C_{1,2} are thus well isolated from the underlying Bi$_2$Se$_3$ crystal structure that is the source of the global topological order; this nonlocal quantum interaction implies interesting engineering possibilities. The orbital angular momentum along $y$ is effectively quenched for C_{1,2}, and the Rashba splitting vanishes to first order. The splitting away from the zone center is a second-order effect, which accounts for the parabolic dispersions of C_{1,2}. By contrast, states B_{1,2} contain a significant mixture of Bi$_2$Se$_3$ states and have a finite Rashba splitting [20].
For spin information applications, systems with a single spin channel in a large gap would be ideal, as is the case of bare Bi$_2$Se$_3$. However, pristine surfaces are almost never of practical use. Oxidation of Bi$_2$Se$_3$ results in a complex band structure because of hybridization of the O-derived states with the substrate states. While the topological order is preserved, the spin current is much reduced. Thus, the often-cited robustness of the surface states in topological insulators does not imply conserved surface spin properties. Experiments performed on samples exposed to air or otherwise capped could be affected by interactions at the surface. Actual applications of topological materials will require a careful analysis of the effects of surface modification and interface formation in order to control or tailor the features and properties of interest.

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FIG. 1 (color online). Calculated band structures of pristine and O$_2$- and O-adsorbed Bi$_2$Se$_3$. (a) Results for a 10-QL slab of Bi$_2$Se$_3$. The shading indicates the projected bulk band regions. Bands A$_{1,2}$ are spin-polarized surface states; they cross at the Dirac point DP$_A$. (b) Results after surface adsorption of O$_2$. The Dirac point moves slightly to DP$_A'$. The other bands in the gap are derived from the oxygen 2$p$ states. (c) Results after surface adsorption of atomic O. Bands B$_{1,2}$ and C$_{1,2}$ are surface states; they cross at DP$_B$ and DP$_C$, respectively. Pair C$_{1,2}$ spans the band gap. (d) Results for O-adsorbed Bi$_2$Se$_3$ but with the spin-orbit coupling turned off in the calculation.
FIG. 2 (color online). Evolution of the surface states upon O-adsorption of a 10-QL Bi$_2$Se$_3$ slab with both faces terminated by atomic O. The distance of the O to the Se surface atom is stretched from the equilibrium distance by (a) 1.2 Å, (b) 0.8 Å, (c) 0.3 Å, and (d) 0.0 Å. The arrows point to the bands that evolve with the changing distance.
FIG. 3 (color online). Spin and charge properties of the bands in Bi$_2$Se$_3$ and Bi$_2$Se$_3$-O. (a) Band dispersion relations for a 10-QL slab. A$_{1,2}$ are surface bands, and P and Q are the two neighboring quantum-well bands. (b) Charge separation $\Delta C$. (c) Spin polarization $P$. (d) Spin current $I$. (e)-(h) Corresponding results for Bi$_2$Se$_3$-O. The curves are color coded.
FIG. 4 (color online). Charge density distributions for the surface states in Bi₂Se₃-O. The left panels show the charge distributions within the oxygen plane in a 2×2 surface cell. The dash-dotted lines show where a vertical cut is made in each case; the results of the cuts are shown in the right panels. Δx, Δy, and Δz are distances referred to an adsorbed oxygen atom.