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1 **Interaction-induced partitioning and magnetization jumps in**
2 **mixed-spin oxide $\text{FeTiO}_3\text{-Fe}_2\text{O}_3$**

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Abstract

In this study we report jumps in the magnetic moment of the hemo-ilmenite solid solution $(x)\text{FeTiO}_3\text{-(1-x)}\text{Fe}_2\text{O}_3$ above Fe(III) percolation at low temperature ($T < 3$ K). The first jumps appear at 2.5 K, one at each side of the magnetization loop, and their number increases with decreasing temperature and reaches 5 at $T = 0.5$ K. The jumps occur after field reversal from a saturated state and are symmetrical in trigger-field and intensity with respect to the field axis. Moreover, an increase of the sample temperature by 2.8% at $T = 2.0$ K indicates the energy released after the ignition of the magnetization jump, as the spin-currents generated by the event are dissipated in the lattice. The magnetization jumps are further investigated by Monte-Carlo simulations, which show that these effects are a result of magnetic interaction-induced partitioning on a sublattice level.

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12 Keywords: magnetization jump, symmetry breaking, hemo-ilmenite, magnetic frustration

13 Complex magnetic systems that exhibit frustration are a topic of long-standing debate [1–
14 5]. A typical example of the manifestation of magnetic frustration is the spin-glass freezing
15 caused by competing exchange interactions due to their geometry [6–8]. The complex scheme
16 of interactions does not allow the system to reach a ground state, and the system remains
17 trapped in local minima of the energy landscape [6, 9, 10]. Application of an external field
18 can move the system from one minimum to another, whereby the transfer can be either
19 smooth or abrupt, depending on the morphology of the energy landscape. Abrupt effects
20 are manifested in the form of metamagnetic transitions [11–13], which are characterized by
21 sudden changes in the spin structure and thus in the net magnetization. These metamagnetic
22 transitions may appear as single events, such as the spin-glass symmetry breaking along the
23 de Almeida-Thouless (AT) line [14], or as multiple antiferromagnetic spin-flop transitions
24 [15]. Another special case in the context of such phenomena is the occurrence of jumps in the
25 magnetic moment [16–18]. Magnetization jumps have been observed in several materials and
26 have been attributed to various properties, such as cluster formation [19–21] or frustration
27 due to doping [22].

28 Among the systems regarding frustrated magnetism, there is one solid solution with a
29 natural equivalent: hemo-ilmenite $(x)\text{FeTiO}_3-(1-x)\text{Fe}_2\text{O}_3$. Members of this solid solution
30 can be important magnetic carriers in the Earth’s crust and they are likely to be important
31 constituents of other planets. Compositions with $0.50 < x < 0.95$ exhibit ferrimagnetic
32 ordering and spin-glass-like freezing for $0.6 < x < 0.95$ at temperatures below $T < 40$ K
33 [23, 24]. The solid solution crystallizes in the $R\bar{3}c$ and $R\bar{3}$ symmetry, depending on the
34 quenching temperature [25]. In the $R\bar{3}c$ symmetry all cations are distributed evenly on a
35 honeycomb lattice, whereas in the $R\bar{3}$ symmetry Fe(II) and Ti(IV) cations are partitioned
36 in alternating sublattices and Fe(III) are distributed evenly (see inset to Fig. 1). Such
37 distribution of Fe(II) and Fe(III) in the lattice generates a complex scheme of interactions,
38 which also explains the spin-glass-like behavior. Although spin-glass-like freezing has been
39 investigated for both synthetic [23, 24, 26–29] and natural samples [30, 31], the Fe(II)–Fe(III)
40 coupling mechanisms are still ambiguous. Moreover, the hemo-ilmenite system represents
41 an excellent example of a mixed-spin magnetic system with quasi-random interactions, and
42 can be used as a testbed to investigate coupling effects of mixed-spin states. Such coupling
43 effects are enhanced in the absence of thermal fluctuations, i.e., at low temperature. In this
44 study we therefore performed magnetization measurements of hemo-ilmenite solid solutions

45 with $x = 0.7, 0.8,$ and 0.9 deep in the frustrated state at low temperature ($T < 3$ K). For
46 the discussion, the composition $x = 0.8$ is presented.

47 The solid solutions were synthesized by means of solid oxide reaction of the end members
48 at $T = 1400$ K for 48 hrs, and the structure was investigated by powder X-ray diffraction.
49 Rietveld analysis of the diffraction patterns reveals a single-phase hemo-ilmenite solid so-
50 lution with the $R\bar{3}$ symmetry for $x = 0.9$ and $0.8,$ and $R\bar{3}c$ for $x = 0.7.$ Magnetization
51 curves were recorded in a temperature range between 0.5 K $< T < 3.00$ K in a Quantum
52 Design Physical Property Measurement System (PPMS) (for $T > 2.0$ K) and in a Magnetic
53 Property Measurement System (MPMS) (for $T < 2.0$ K). In the PPMS the field-sweep rate
54 was set to 10 Oe/s, whereas in the MPMS the field was stopped for each measurement with
55 the SQUID. In addition, the ac susceptibility was measured in a temperature range from 10
56 K to 300 K in the PPMS at a frequency of 1 kHz and driving-field amplitude of $H_{ac} = 5$ Oe.

57 Measurement of the ac susceptibility (Fig. 1) indicates long-range ferrimagnetic ordering
58 at T_C with a peak in both the in-phase $\chi'(T)$ and out-of-phase component $\chi''(T)$ of the
59 susceptibility. The exact ordering point is defined at the onset of $\chi''(T)$ upon cooling where
60 hysteretic effects appear [32]. The Curie temperature for this solid solution is $T_C = 238(1)$
61 K, consistent with a composition of $x = 0.8$ [33]. Fitting the high-temperature evolution
62 of the inverse susceptibility χ'^{-1} with the Curie-Weiss law provides a Curie constant $C =$
63 $Ng^2\mu_B^2J(J+1)/3k_B = 4.25,$ which gives an effective spin of $S = 2.44$ (considering that
64 $L = 0$), close to the expected value of $5/2$ for Fe(III). From this observation the ferrimagnetic
65 ordering can be attributed to Fe(III).

66 Below 200 K, both components of the susceptibility decrease with decreasing tempera-
67 ture, and below 50 K $\chi'(T)$ exhibits a pronounced decrease, whereas $\chi''(T)$ shows a peak
68 at the freezing temperature $T_f.$ Below T_f both components of $\chi(T)$ decrease with decreas-
69 ing temperature. In addition, $\chi''(T)$ increases linearly with increasing driving field $H_{ac},$
70 indicating the absence of domains [29].

71 Fig. 2 shows a measurement of the magnetic moment deep in the frustrated phase at
72 $T = 2.5$ K, where for small external fields ($H < 3$ kOe) the magnetic moment increases
73 linearly with the external field $H.$ The linear behavior of the total magnetic moment with
74 H indicates spin-glass-like symmetry. However, at a critical trigger field $H_{cr} = 4.5$ kOe an
75 abrupt jump in the magnetic moment, and thus a symmetry breaking, is seen. The jump
76 is very sharp with a width of $h = \Delta H/H_{cr} \approx 0.04,$ and exhibits an intensity $I = \Delta m/m_S$

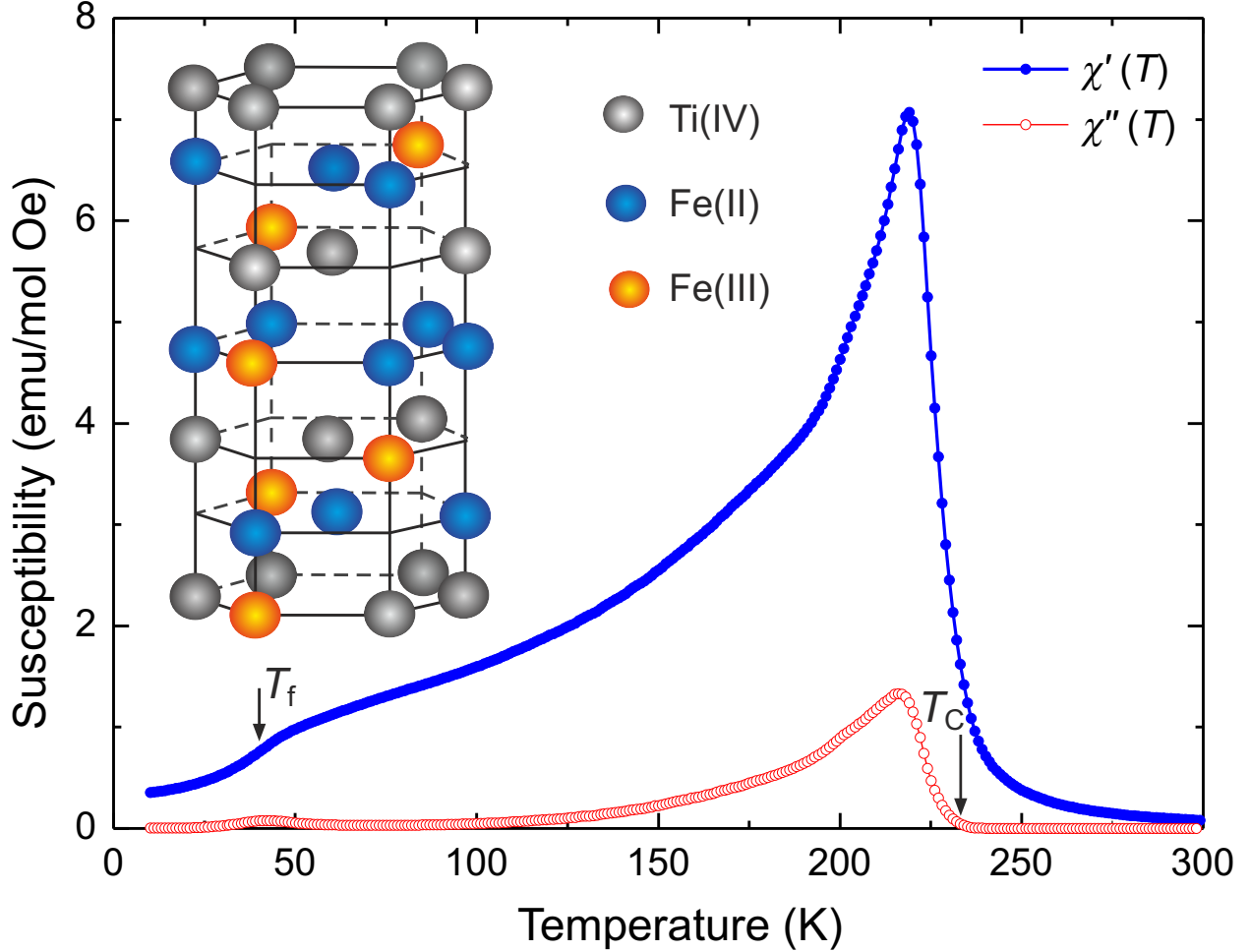


FIG. 1. Dynamic in-phase (full circles) and out-of-phase (open circles) ac susceptibility of the solid solution with $x = 0.8$ indicating the ferrimagnetic ordering at T_C and the spin-glass freezing at T_f . The inset illustrates the cation ordering where the O(II) ions have been omitted.

77 of approximately 25%. After the jump the moment relaxes until the field catches up with
 78 the new state and then with increasing field the magnetic moment increases smoothly and
 79 reaches a pseudosaturation. While the field is reduced to zero the magnetic moment relaxes,
 80 again smoothly, and at $H = 0$ exhibits a relatively high remanence ($m/m_S \approx 60\%$). The
 81 absence of a clear saturation can be attributed to crystallites with their c -axis perpendicular
 82 to the external field, because the layered $R\bar{3}$ structure requires spin alignment along c [34].
 83 Nonetheless, we may define the saturation point to occur at the collapse of the hysteresis
 84 loop, i.e., at $H \approx 20$ kOe.

85 The inset to Fig. 2 shows a comparison of full hysteresis loops at $T = 3.0$, i.e., above the

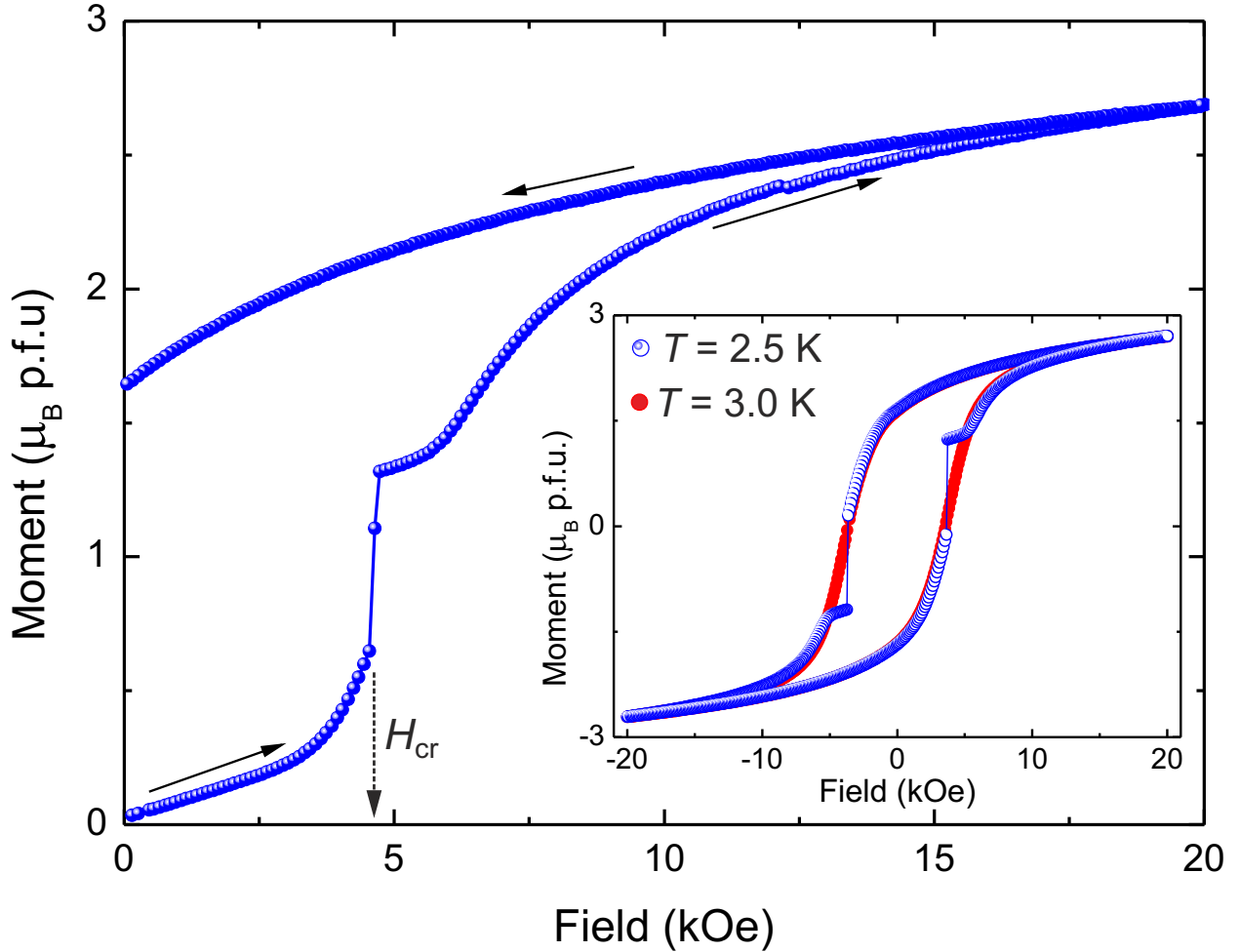


FIG. 2. Virgin line of the magnetization of solid solution with $x = 0.8$ at $T = 2.5$ K. The inset shows full hysteresis loops at $T = 2.5$ K (hollow spheres) and $T = 3.0$ K (full circles) for the same compound.

86 jump occurrence threshold, and at $T = 2.5$ K. At $T = 2.5$ K the hysteresis loop is almost
 87 identical to that at $T = 3$ K, apart from the fact that the reversal of the magnetization
 88 at $T = 2.5$ K occurs in a transition-like manner at the two critical trigger fields $\pm H_{\text{cr}}$.
 89 The events are symmetrical in trigger field and amplitude ($I = \Delta m/m_S \approx 50\%$) with
 90 respect to $H = 0$, and can be associated with the symmetry breaking observed in the virgin-
 91 line, after which the state with $m = 0$ is not favoured anymore. This suggests that the
 92 rapid re-arrangement of the magnetic structure is caused by the fact that the intermediate
 93 configurations (between $H = 3$ kOe and 5 kOe) cost energy.

94 With decreasing temperature the number of jumps increases and the total added intensity

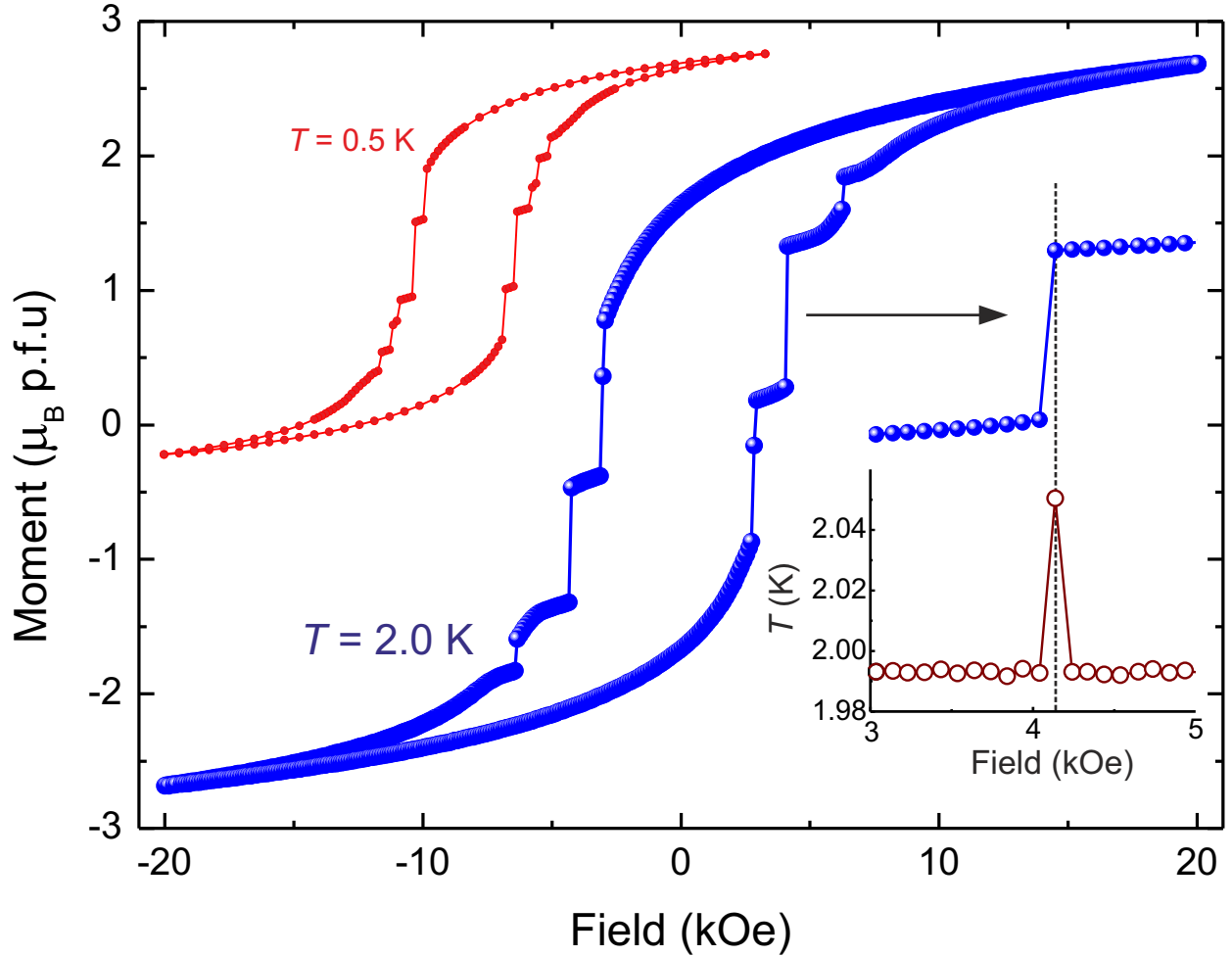


FIG. 3. Magnetization loop of solid solution with $x = 0.8$ at $T = 2.0$ K and blow-up of a jump illustrating temperature rise (lower right). Loop of same compound at $T = 0.5$ K (upper left), not to scale.

95 of the jumps becomes larger. At $T = 2.0$ K three and at $T = 0.5$ K five jumps on either side
 96 of the field axis are observed for solid solutions with $x = 0.8$ (Fig. 3 with inset). For solid
 97 solutions with $x = 0.9$ only two jumps were observed at $T = 2$ K: one large with $I \approx 35\%$
 98 at $H_{\text{cr}} = 4.6$ kOe and one small with $I \approx 6\%$ at $H_{\text{cr}} = 8.5$ kOe (data not shown). These
 99 observations suggest that the number of magnetization jumps will most likely remain finite
 100 at zero-temperature.

101 In the inset of Fig. 3 a close-up of the most intense jump at $T = 2.0$ K and $H_{\text{cr}} = 4.04$ kOe
 102 with intensity $I \approx 39\%$ is seen along with the sample temperature. At the critical field H_{cr}
 103 the magnetic moment jumps in a single motion (within the measurement time-frame of 10 s)

104 and then continues smoothly with increasing field. At the same time, the temperature shows
 105 a spike right after the event, with an increase of 2.8% from the base value of $T = 1.995$ K.
 106 This effect is a direct indicator of energy released by the magnetization jump, as the system
 107 reaches a new energy minimum. The actual energy released during the transition is in fact
 108 the difference in Zeemann energy $\Delta F_Z = g\mu_B HSI$ [16]. The measurable energy (heat),
 109 however, cannot be directly attributed to ΔF_Z but to its aftereffect. This aftereffect can be
 110 explained as follows: while the spin structure is rapidly re-arranging itself during the jump,
 111 the massive reversal results in pulses of spin-currents. These pulses are dissipated in the
 112 lattice, most likely, by means of eddy-currents, which then, in turn, become dissipated, and
 113 release heat.

114 Field-cooling experiments with various fields and field-sweep rate variation do not affect
 115 the occurrence or the features of the jumps. The hysteresis loops are reproducible with the
 116 same number of jumps and same properties, i.e. I and h , at each temperature. Therefore,
 117 we conclude that these effects are intrinsic to the system and are driven by processes on an
 118 atomic level, considering how sharp they appear in these powder samples. These phenomena
 119 occur, however, only for compositions close to, and above, the percolation threshold $x_p \approx$
 120 0.8. We found magnetization jumps for $x = 0.9$ and $x = 0.8$ (both $R\bar{3}$), but not for
 121 $x = 0.7$ ($R\bar{3}c$). This further suggests atomic-scale processes governed by bond-percolation
 122 constraints [19, 20], because in the $R\bar{3}$ symmetry there is clear distinction between Fe-rich
 123 and Fe-deficient sublattices, as opposed to the $R\bar{3}c$ symmetry. Hence, the occurrence of
 124 magnetization jumps can be attributed to collective sublattice reversal, whereas large jumps
 125 correspond to Fe-rich sublattices and small jumps correspond to Fe-deficient sublattices.

126 In order to test this scenario, we performed Monte-Carlo (MC) simulations using the
 127 Ising-like Hamiltonian

$$\mathcal{H} = -\frac{1}{2} \sum_{i,j} J_{ij} S_i S_j - H \sum_i g_i S_i, \quad (1)$$

128 where J_{ij} is the exchange constant between the spins S_i and S_j and g_i the corresponding
 129 spectroscopic splitting factor, and H the external field. The spins take the values $\pm 4/2$
 130 (Fe(II) – $3d^6$) and $\pm 5/2$ (Fe(III) – $3d^5$), whereas g is taken to be 1.5 for Fe(II) and 2.0 for
 131 Fe(III).

132 The presence of the two valence states of Fe requires three different exchange constants,
 133 i.e., $J_{\alpha\alpha}$ for Fe(II)–Fe(II), $J_{\beta\beta}$ for Fe(III)–Fe(III), and $J_{\alpha\beta}$ for Fe(II)–Fe(III) interactions,

134 whereas we assume isotropy ($J_{\alpha\beta} = J_{\beta\alpha}$). The energy and the field used in the calculations
 135 are scaled to $J_{\alpha\alpha}$. Considering the ordering temperature of the end-members (950 K for
 136 Fe_2O_3 and 58 K for FeTiO_3), and the respective number of nearest neighbors, a first estimate
 137 for the Fe(III)–Fe(III) interaction energy yields $J_{\beta\beta} \approx 5.7 \times J_{\alpha\alpha}$. In addition, $J_{\alpha\beta}$ can be
 138 estimated in a first approximation using mean field theory (MFT) predictions for the ordering
 139 temperature of a two-sublattice system by considering the known ordering temperature of the
 140 solid solution with composition $x = 0.66$, where Fe(II) and Fe(III) are in equal parts ($T_C =$
 141 360 K). This results in $J_{\alpha\beta} = 2.3 \times J_{\alpha\alpha}$. In general, the coupling is governed by exchange
 142 and superexchange interactions along the c -axis. However, although the modulation length
 143 of $J_{\alpha\alpha}$ in ilmenite (4 layers) and of $J_{\beta\beta}$ in hematite (2 layers) are known, the modulation
 144 in the mixed state is unknown. Therefore, we use a random distribution of ferromagnetic
 145 (75%) and antiferromagnetic (25%) links.

146 The simulations were performed on a 648-cell superlattice using periodic boundary con-
 147 ditions. Fe(II) and Ti(IV) cations were ordered according to the ilmenite $R\bar{3}$ symmetry and
 148 20% were replaced with Fe(III) at random to generate the composition of the investigated
 149 solid solution. The thermalization was performed by single-site updates and the system was
 150 allowed to thermalize for 1000 cycles per site.

151 Fig. 4 shows magnetization curves simulated using the described model. As seen in the
 152 figure, at $T = 0$ magnetization jumps occur after field reversal and the strongest jumps are
 153 near $m = 0$, similar to the experimental curves. With increasing temperature the effects
 154 disappear. In addition, observation of the spin-structure during the simulations show that
 155 the major moment-rotation during a single jump takes place at the Fe-rich sublattices (see
 156 inset to Fig. 4).

157 Finally, we conclude that the magnetic structure in the presented mixed-spin oxide at low-
 158 temperature is partitioned layer-wise by exchange and superexchange interactions. Strong
 159 coupling within Fe-rich sublattices leads to a collective rotation of their magnetic moment
 160 in an external field, which generates magnetization jumps. Moreover, these observations
 161 demonstrate how the layered structure of the $R\bar{3}$ symmetry imparts a collective behavior to
 162 this quasi-stochastic system above the percolation threshold.

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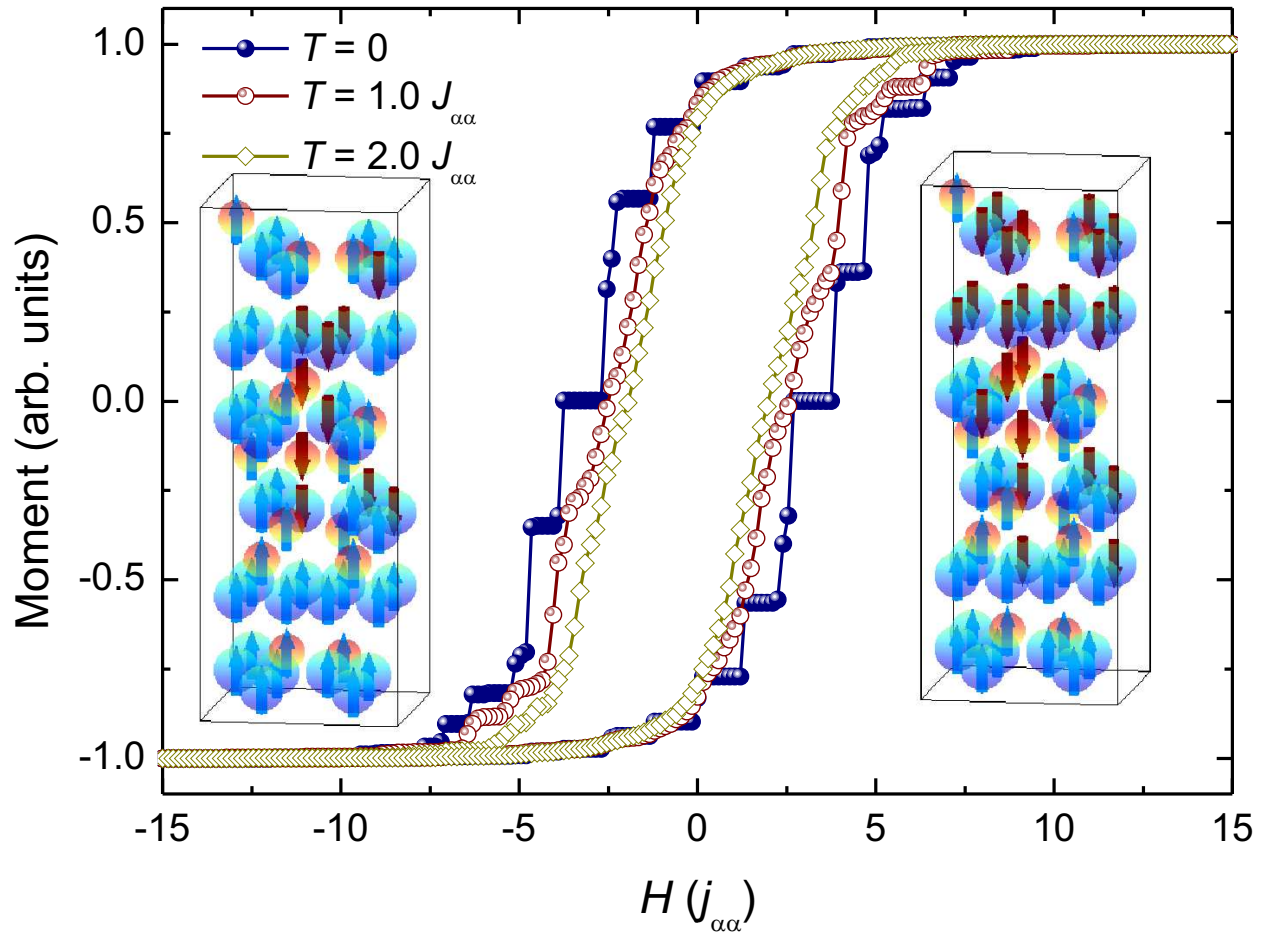


FIG. 4. MC simulation of a magnetization loop at $T = 0$, $T = 1.0 J_{\alpha\alpha}$, and $T = 2.0 J_{\alpha\alpha}$. The insets show a portion of the structure before (left) and after (right) a jump of the magnetic moment during the MC simulation at $T = 0$.

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