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Small fire ant rafts are unstable

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4 Abstract

In this combined experimental and numerical study, we film the formation of fire ant rafts to 5 determine how they cohere together. Surprisingly, we discover that ants prioritize separation and 6 exploration: they flail legs and bounce off neighbors when they collide. Despite the active repulsion, 7 Fire ants cohere by the Cheerios effect, a capillary force that attracts small floating objects such as 8 breakfast cereal. Experiments reveal that rafts consisting of fewer than ten ants disintegrate within 9 minutes. Predictions by a Langevin model reproduce the stability transition and the critical raft 10 size, which emerges from the balance between their mutual repulsion and the Cheerios effect. This 11 work may inspire physically grounded models for the behavior of natural swarms. 12

13 Introduction

Animal groups accomplish tasks that individuals cannot achieve [1, 2, 3]. For example, army ants 14 link their bodies to build bridges over gaps [4]. Slime molds *Dictyostelium discoideum* distribute 15 their spores by building fruiting bodies to grow in height by a factor of 200 [5, 6]. Fish schools 16 reduce energy expenditure and facilitate evasion of predators [7, 8, 9]. One way that we recognize 17 a flock of birds or a school of fish is by its cohesion [10]: members of a swarm remain together 18 despite changes in the swarm's shape and internal structure. Although cohesion in natural swarms 19 is a simple enough concept to recognize, the mechanism by which it arises is still a mystery. 20 Understanding how individuals cohere may inspire new swarm models and guide the designs of 21 artificial systems. The goal of this study is to investigate the origin of cohesion in fire ant rafts. 22

Currently, most models of swarms require a "social force" that attracts individuals towards their 23 neighbors or the center of the swarm [11, 12, 13, 14, 15, 16]. The 1995 Vicsek model [17] does not 24 feature social attraction and thus swarms behave unrealistically: they disperse in the open space 25 [18, 11, 19]. A social attraction force is fundamentally different from physical forces such as drag 26 and thrust. It involves a cascade of internal signals in which the animal senses the distance to its 27 neighbors and propels itself to maintain that distance. Social attraction forces have long been used 28 to rationalize the motion of fish schools [20, 21, 22, 23], bird flocks [24, 25, 26], and insect swarms 29 [27]. Although social attraction enables models to emulate various collective behaviors, Lopez et al. 30 [28] cautioned that this approach increases the number of model parameters to be measured from 31 experiments. Furthermore, as a proxy for complex animal interactions and sensory feedback, social 32 attraction is in itself an emergent property. It may be difficult to justify social attraction forces 33 for insect swarms, for which individuals have limited sensing capabilities and intelligence. Despite 34 years of work, it remains unknown if social attraction forces are legitimate or simply a crutch. In 35 this work, we rationalize the formation of ant rafts without invoking social attraction. 36

We perform experiments with red imported fire ants (*Solenopsis invicta*, **Figure 1**A). Native to the Pantanal wetlands in Brazil [29], this invasive species can now be found on all continents except for Antarctica [30]. Fire ants can link their bodies together to build rafts, towers, and bridges. Ants on the raft perform random walks and expand the raft by accretion of their bodies on the raft edge [31]. Fire ants may also extend pseudopod-like appendages through treadmilling [32] and morph into streamlined airfoil shapes when in flow [33]. Previous studies have focused on large rafts with more than 1000 ants [31, 34, 32] but did not discuss how rafts stayed together. In this study, we

focus on rafts with size 2 to 158 ants to better understand the mechanisms of raft formation.

$_{45}$ Results

⁴⁶ Experimental observations: Small rafts are not stable

We filmed the behavior of balls of ants placed on the water surface (Movie S1). In total, we 47 performed 72 experiments involving groups ranging from 2 to 158 ants. Surprisingly, we find that 48 ant rafts are only stable if they contain at least $N_c \approx 10$ ants. Figure 1C shows a time series of a 49 raft of five ants breaking apart when placed on the water surface. The dense ant ball expands rapidly 50 as it contacts the water surface, and then ants begin to disperse in all directions. Figure 1B shows 51 the relationship between N, the number of ants initially in a raft, and P, the proportion of ants 52 that leave the raft after five minutes. Experimental data are shown by orange triangles. Clearly, 53 larger rafts are more stable, with a stark transition to stability at ten ants. Phenomenologically, 54 such a trend is shown by a logistic function (**Figure 1**B), 55

$$P(N) = \frac{1}{1 + e^{(N - N_c)/\Delta N}},$$
(1)

where N_c is the critical number of ants for stability, and ΔN is the width of the transition interval. 56 Note that when $N = N_c$, half of the ants go astray (P = 0.5). The dashed orange line shows a 57 least-squares fit to our experiments. The best fit yields $N_c = 9.3$ and $\Delta N = 1.5$ $(n = 72, R^2 = 0.66)$. 58 To better understand the factors that lead to the critical raft size, we film the interaction between 59 pairs of ants as they encounter each other on the water surface. Each pair of ants separates after 60 an average interaction time of 77 ± 69 seconds (n = 14). The interaction time is highly variable. 61 ranging from as little as 10 seconds up to four minutes. During this interaction, they flail their 62 legs, intermittently colliding with each other before ultimately departing in opposite directions. 63 This observation contradicts with the naïve assumption that all swarming individuals have social 64 attraction. 65

To determine the dominant forces on the ants, we calculate common dimensionless groups. The 66 Reynolds number Re = $Ul/\nu \sim 10$, where $l \sim 3$ mm is an ant's characteristic body length, $U \sim 10$ 67 4 mm/s its characteristic swimming speed, and ν the kinematic viscosity of water. The Reynolds 68 number suggests that both inertia and viscous force influence an ant's motion. Indeed, when pushed 69 manually, dead ants can drift for tens of body lengths through their inertia. The Reynolds's number 70 remains small if other characteristic length scales are considered such as the body width w = 171 mm, or the leg width $w' = 100 \ \mu m$. The Bond number $Bo = \rho g l^2 / \gamma \sim 1.3$ where ρ is the density of 72 water, g is the gravitational acceleration, and γ is the surface tension of water. The Bond number 73 suggests that both surface tension and buoyancy contribute to the weight support of the ants. 74 Indeed, we see that fire ants maintain their position mostly above the water surface, with just their 75 legs' tips and ventral surfaces wetted. From here on, we will characterize their motion on the water 76 as walking rather than swimming. 77

78 A Langevin model describing fire ant interactions

⁷⁹ We proceed by presenting a model for raft formation that does not rely on social attraction. The ⁸⁰ goal of our model is to rationalize the critical number of ants N_c for raft cohesion as well as the ⁸¹ effect of different parameters such as ant activity level and initial spacing. Newton's law applied ⁸² to a single ant of mass $m \approx 1$ mg states:

$$m\ddot{\boldsymbol{x}}_i = k_a \boldsymbol{\eta}_i - k_f \dot{\boldsymbol{x}}_i - \sum_{i \neq j} k_c \mathrm{K}_1(|\boldsymbol{d}_{ij}|/l_c) \hat{\boldsymbol{d}}_{ij} + \sum_{i \neq j, d_{ij} < 2r} k_r \boldsymbol{d}_{ij}$$
(2)

inertia = propulsion + drag + capillary + repulsion

where x_i is the two-dimensional position of ant i and \ddot{x}_i is its acceleration. The forces experienced by the ants include propulsion, viscous drag, capillary attraction, and ant-to-ant repulsion. These four terms are characterized by their corresponding coefficients h_i , h_i , and h_i

four terms are characterized by their corresponding coefficients k_a , k_f , k_c , and k_r .

86 Active propulsion

In Equation (2), the first term on the right-hand side is the random propulsive force of ants. Dropping the *i* subscript, the propulsive force for an ant may be written as the product of an activity coefficient k_a and η , the two-dimensional standard normal distribution with zero mean and unit standard deviation. Effectively, $k_a \eta$ is the Gaussian distribution with standard deviation k_a . At each time step, and for each ant *i*, we randomly sampled a value from this distribution. To measure activity level k_a , we first describe their trajectories.

Figure 2(A) shows an overlay of ten individual fire ant trajectories on the water surface. These trajectories are characterized by looping circular paths with straight-line distances of less than a few body lengths. Trajectories on water vary significantly from trajectories atop ant rafts, where their straight line distance is on the order of 4 cm, or over 13 body lengths [31]. For simplicity, ants in our model are considered circular discs with no heading.

The velocity distribution of ants on the water surface is qualitatively similar to that of Brownian 98 particles such as pollen. Figure 2(B) shows the probability distribution of an ant's speed U =99 $\sqrt{u^2 + v^2}$, where u and v are the x and y components of the ant's walking velocity $\dot{x}_i = [u, v]$. The 100 two insets of **Figure 2**(B) show that an ant's translational velocity components (u, v) are normally 101 distributed around zero, indicating that ants have no directional bias. The standard deviation 102 σ of velocity in either direction (u, v) is approximately 3.5 mm/s (n = 96). Ants on the water 103 locomote at speeds of $U = 4.2 \pm 2.8$ mm/s (n = 96), a fifth of their walking speed on land, 20 mm/s 104 [35]. Previous work reports that fire ants "showed no directed motion" and categorized them as 105 non-swimmers compared to other tropical ant species [36]. Notably, fire ants are also smaller than 106 other tropical species, which may make their locomotion less effective on water. 107

Following the prediction from statistical mechanics, **Figure 2**B shows the probability distribution of the velocity magnitude U, which is well approximated by the two-dimensional Maxwell-Boltzmann distribution (solid red line),

$$pdf(U) = \frac{1}{2\pi\sigma^2} e^{-\frac{1}{2}(U/\sigma)^2}$$
(3)

where pdf is the probability distribution function, and σ is the standard deviation for u and v. The mean squared displacement (MSD) of ant trajectories is defined as

$$MSD(\Delta t) = \left\langle |\boldsymbol{x}(t + \Delta t) - \boldsymbol{x}(t)|^2 \right\rangle, \tag{4}$$

where $\langle ... \rangle$ denotes the average over all samples and time t. Figure 2C shows the MSD of ant trajectories (n = 96), where MSD is in mm² and the time interval Δt is in seconds. The MSD reveals that the motion is ballistic at short times ($\sim 7.5\Delta t^2$ for $\Delta t < 5$ s, $R^2 = 0.97$) and diffusive at long times ($\sim 30\Delta t$ for $\Delta t > 8$ s, $R^2 = 0.98$). These statistical features confirm that the locomotion of fire ants on the water surface can be modeled by inertial random walkers such as dust particles in plasmas, mini-robots, and Whirligig beetles [37, 38].

The transition between the two regimes is smooth and we could not identify a critical threshold based on the MSD statistics alone. However, though the coasting dead ant experiments that we will introduce below, we calculate a time scale for inertial effects (vertical gray dashed line) that lies in the transition region of MSD.

Fitting the MSD at the early ballistic stage yields the characteristic velocity of 2.7 mm/s ($R^2 = 0.97$), comparable to the average speed in the histograms in **Figure 2B**. From the later diffusive phase, we calculate the diffusion coefficient D of 7.5 mm²/s ($R^2 = 0.98$). This diffusion coefficient suggests that over 22 minutes, an ant's final position on water will be ten centimeters away from its initial position. We can relate the activity coefficient k_a in our model (Equation (2)) to the friction coefficient k_f through $k_a = k_f \sqrt{2D/\delta t}$ [37], where δt is the time step used in our simulations (see the Materials and Methods section).

Although we neglect turning in our model, we briefly explain the looping trajectories observed. Directional bias is absent in our experiments: the mean orientational velocity of the ants, $\dot{\theta}$, is negligible at -0.002 rad/s (n=97). Persistent turning explains the circular trajectories in **Figure 2**A. Fig. S1 shows that orientational MSD has a slope of 1.7 ($R^2 = 0.995$), indicating that ants'

¹³⁴ angular velocities are hyper-diffusive.

135 Fluid drag

The second term in Equation (2) is the fluid drag on an ant. We performed experiments by 136 manually pushing dead ants by hand and recording their deceleration on the water surface due 137 to hydrodynamic drag (Fig. S2). In the intermediate Re regime (Re~ 10), drag involves both 138 pressure drag (~ U^2) and viscous drag (proportional to ~ U). However, we found that viscous 139 drag is sufficient to explain the deceleration. We fit the relationship between fluid drag and the 140 velocity to obtain the coefficient $k_f = 0.24 \text{ mg/s}$ $(n = 14, R^2 = 0.82)$. The time scale of the 141 inertial effect $\tau = m/k_f = 4.3$ s approximately coincides with the transition between the inertial 142 and diffusive regimes in MSD (vertical gray dashed line in **Figure 2**), as predicted by the Langevin 143 model for Brownian particles. Indeed, in the absence of interaction terms, Equation (2) describes 144 Brownian motion [37]. 145

146 Capillary attraction

The last two terms of Equation (2) involve the interaction among individuals and vary with $d_{ij} = x_i - x_j$, the distance between a pair of ants. Small floating objects such as paperclips or Cheerios are drawn together by capillary forces, which act to minimize the deformation of the water surface. Similarly, in both experiments with live and dead ants, we observe attraction sufficient to draw ants together if the initial distance is within a few centimeters. Nicolson et al. derived the attraction force between two floating spheres

$$F_c = k_c \mathcal{K}_1(d/l_c),\tag{5}$$

where k_c is a fitting parameter measured from experiments, K₁ is the modified Bessel function, dis the distance between the two objects, and $l_c = 2.7$ mm is the capillary length of water. The parameter k_c depends on the geometry, contact angle, and density of the object [39, 40, 41]. We account for these effects by fitting the interaction between two dead ants. Although ants are elongated and have a rough surface, we neglect these second-order effects and focus on representing the capillary attraction between ants as floating spheres. Through measuring the attraction between pairs of dead ants (see the method section and Fig. S3), we obtain $k_c = 2.6$ nN (n = 33, $R^2 = 0.83$). Based on the value of k_c , the attraction force between two ants is comparable to the attraction between a pair of small plastic spheres (diameter 1 mm, density 1.1 g/mL, and contact angle 70°).

¹⁶² Short-range repulsion

The last term in Equation (2) is the short-range elastic repulsion force when two ants collide. In simulations, we approximate ants as a 2D discs with radius r = 1 mm, which was chosen to be both comparable to the ant length l and ant width w. Collisions occur when the inter-ant distance $d_{ij} < 2r$. Our simulation results were comparable for most non-zero values of k_r ; therefore we used $k_r = 0.05$ nN/mm.

Our final model, Equation (2), is capable of simulating the trajectories of arbitrary numbers of ants. Except for k_r , which was set to avoid overlapping agents when they came too close, there were no free parameters in our model; all parameters were measured from our experiments on both live and dead ants. In the Materials and Methods section, we detail how we measure the four model parameters (k_a, k_f, k_c, k_r) that characterize the four forces acting on the ants.

¹⁷³ Multi-agent simulations capture the stability transition

¹⁷⁴ In this section, we present simulations of raft destabilization and raft formation, in which we vary ¹⁷⁵ factors that would be difficult to change experimentally.

Raft destabilization simulations begin with ants in a hexagonal lattice, the tightest possible 176 configuration for monodisperse discs. We perform 150 simulations with 15 different raft sizes and 177 10 numerical trials with different values for the random variable η which describes their diffusion. 178 Figure 3A and Movie S2 demonstrate that assemblies of seven agents disintegrate, while rafts of 179 19 agents remain stable, similar to the behavior observed in experiments. Figure 1B shows P, the 180 proportion of stray ants at the end of the trial of five minutes, decreases with the number of ants 181 N in simulations (gray circles). We fit the simulation results to the logistic function, Equation (1), 182 finding that the critical number of ants $N_c = 9.5$ and $\Delta N = 1.1$ $(n = 150, R^2 = 0.88)$, matching 183 the experimental logistic function well. We thus conclude that the stability transition emerges from 184 the agent interactions in our model, the combination of random walks, drag, contact repulsion, and 185 Cheerios effects (Figure 3B). We next use our model to explore the effect of activity levels and 186 the initial spacing of ants. 187

Next, we consider the effect of ant activity on raft stability. In our experiments, we observed 188 that the leg motion of fire ants dwindles over time. Immediately after being placed on water, ants 189 flail their legs at 20.2 ± 4.5 mm/s (n = 6) at their tips. The movement slows down to 10.0 ± 4.5 190 mm/s (n = 6) over a span of ten minutes. This slow down with time is consistent with our previous 191 findings that ants reduce exploration and metabolism with time [42, 33]. Could the decrease in 192 activity improve the stability of the rafts? To answer this question, we simulated ants with activity 193 coefficient k_a ranging from 0.5 to 3.4 nN, where the activity level measured from our experiments 194 was 3.0 nN. Figure 3C shows the stability diagram of the rafts (n = 1200). Larger rafts with 195 less active ants are more stable, as expected. This black dashed curve represents the critical size 196 where half of the ants remain stable in the raft (P = 0.5); by fitting to an exponential, we find this 197 stability criteria correspond to $N_c \approx 0.3 e^{1.2k_a}$. 198

Now that we have identified how ant rafts remain stable, we investigate how rafts are assembled 199 in the first place. These simulations were conducted with ants in a square lattice of centroid-200 to-centroid spacing L. Figure 4a shows the proportion of ants that remain isolated after five 201 minutes as a function of the activity level and initial spacing L. Each data point is an average of 202 ten numerical trials per condition (n = 660). For ants to assemble into a raft from a dispersed 203 state, they must be sufficiently close together. Closely spaced ants with a spacing of L = 16.7 mm 204 condense into rafts if the activity is sufficiently low. Higher activity levels lead to collisions that 205 destabilize the aggregation. Conversely, distant ants with spacing L = 37.5 mm rarely encounter 206 any neighbors within five minutes if their activity is low $(k_a = 0.5 \text{ nN})$. This phenomenon is observed 207 in our experiments: satellite ants a few centimeters away from their neighbors remain isolated if 208 their activity level is too low. Ants must actively locomote on the water surface to encounter 209 neighboring ants. In our experiments, as ant activity levels naturally dwindle with time, sparsely 210 distributed ants have increasing difficulty encountering neighbors. Therefore, the initial spacing is 211 a critical factor for raft formation. 212

Figure 4B-C demonstrate the time series of stray and proportions P for various activity levels 213 and two initial ant-to-ant spacing, L, of 18.75 mm and 30 mm. At small ant-to-ant spacing, 214 L = 18.75 mm, even though the proportion of ants P at t = 5 min is monotonic with activity, 215 the time-scale to achieve 50 percent assembly is nonlinear. Such nonlinearity is due to the pros 216 and cons of increasing activity levels: namely, high activity enables ants to find one another but 217 impedes raft formation upon contact. Conversely, ants of low activity level take longer to find 218 one another but stick together better once in contact. When the activity is low at $k_a = 0.5$ nN, 219 rafts assemble slower because it takes longer for ants to find their neighbors. For large ant-to-ant 220 spacing L = 30 mm, even though low-activity ants assemble more slowly, newly formed rafts rarely 221 break apart. The comparison between **Figure 4**B and **Figure 4**C reveal that for any fixed activity 222 level k_a , the raft is established more rapidly at low initial spacings (**Figure 4C**). At the spacing of 223 L = 18.75 mm, except for when $k_a = 1.5$ nN, the system either quickly converges to the aggregated 224 state $(k_a < 1.5 \text{ nN})$, or maintains the dispersed state $(k_a > 1.5 \text{ nN})$. 225

226 Discussion

²²⁷ Phase-transition analogy of raft stability

Animal swarms can display both behavioral phases (such as Pharaoh ant trail-following [43], and desert locust swarming [44, 45]) and thermodynamical phases [46, 47, 48, 49, 50, 51, 52]. The assembly and disassembly of fire ant rafts is analogous to the phase transition of non-living materials such as water. Here, the raft may be considered the liquid phase; and the dispersed ants, the vapor phase. Subsequently, the proportion of stray ants is analogous to the vapor quality. In this viewpoint, we can readily compare **Figure 4**A to the T-V diagram of the water, where the temperature T corresponds to the ant activity and volume V corresponds to the number of ants.

Following the statistical mechanics' framework and assuming detailed balance, we may also estimate the effective temperature $T_{activity} = 1.4 \times 10^{13}$ K using the Stokes-Einstein relation $D = \frac{k_B T_{activity}}{6\pi\mu l}$, where k_B is the Boltzmann constant, μ the viscosity of water and l the length of the ants. We can estimate the pressure per unit depth $P_{activity}$ by equating the energy scales (ideal gas law) $P_{activity}A = k_B T_{activity}$, where A is the surface area of an ant. We obtain $P_{activity} = 0.2$ mN/m, which is around 1/300 of the water surface tension. Note that the pressure drives ants apart, and surface tension pulls them together.

Fire ant rafts constantly expend energy and are thus out of equilibrium, departing from most traditional physical systems. From previous work, we know that ants slow down and ant rafts shrink on the order of hours [33]. To avoid these fatigue effects, which are difficult to model, we chose five minutes as the time frame to perform our observations and simulations. The numbers calculated will vary with the time frame chosen, but the physical picture should remain the same. Further understanding of the collective dynamics of biological systems calls for a statistical mechanical framework that permits temporal variability as well as individual differences.

²⁴⁹ Biological assemblies on the water surface

Can our model predict if and under what conditions other species can aggregate? Three factors should be considered. Different animals have different physical properties (density, size, hydrophobicity, etc.), and thus different coefficients for the Cheerios effect attraction k_c . While ants are well described by random walks, other organisms may need different models. For example, the locomotion of whirliging beetles resembles "corralled active Brownian particles" [53]. Chirality is critical in describing starfish embryo assemblies [54].

Recently, biologists have identified more ant species that can build rafts, including *Pheidole*, *Formica*, *Wasmannia*, and *Linepthema* spp. [36, 55, 56, 57, 58, 59]. They are often found in habitats prone to inundation. Notably, one common feature of these rafting species is their small body size (< 1 cm), hinting at the potential significance of surface tension and the Cheerios effect in their assembly mechanism. Comparative studies of these species that test the predictive power of our model would be an exciting future direction.

As we focus on the fire ant behaviors on the water surface over a short time scale (five minutes), it can be argued that ants have very limited sensory capabilities. Indeed, we demonstrate that ants walking on the water surface cannot recognize neighboring ants and ricochet off them. The nature of the system calls for stochastic dynamics, where the activity is modeled as white noise that does not require any memory or feedback loop. The lack of memory or feedback is similar for swarms of black soldier larvae as well [60].

Our research coincides with active matter beyond the over-damped limit [61, 38, 62, 53]. Löwen has shown that rich physics can arise from the addition of the inertial term, such as the co-existence of different temperature phases [38]. There has also been increasing interest in active matter at the fluid interfaces [63, 64, 65, 53, 54, 66]. Our model, Equation (2), shares significant similarity with these systems. Through this combined experimental and theoretical study, we present fire ants as a model system for future explorations on these topics.

274 Conclusion

We have shown that fire ants cohere on the water surface through capillary forces. Remarkably, the activity of the ants destabilizes the assembly, causing small rafts to disintegrate. We used a Langevin model to simulate raft breakages and reproduced the stability transition condition we discovered in experiments. Further, we used the model to predict the initial ant spacing required to assemble rafts.

²⁸⁰ Materials and methods

281 Raft experiments

Fire ant colonies were collected from the campus of Georgia Institute of Technology, Atlanta, Georgia. We kept them in plastic trays with access to water and food. In all collected colonies, multiple queens were found. To reduce the effects of the artificial rearing environment in the lab, we only used ants harvested within three months for experiments.

To make rafts, we used previously published protocols [31]: we selected ants from a colony and placed them into a beaker coated with Insect-a-Slip. Then we swirled the beaker to roll the ants into a ball and placed the ball on the water surface. Ants fewer than 30 in number were manually counted before the experiment. For larger numbers, the beaker was weighed and converted to the number of ants using the average weight of one ant, which was around one milligram. For five minutes, we recorded the trajectories of ants and counted the number of stray ants at the end of the film.

²⁹³ Measuring parameters for the Langevin model

We tracked 96 ants to determine their activity level on the water surface. Ants were picked up from the colony using tweezers and transferred to the water surface by gently tapping the tweezers. Occasionally, ants landed on their back and could not flip over due to surface tension. These trials were excluded from further analysis. We recorded the trajectories of ants using an Opti-Tekscope USB microscope placed above the water surface. The recordings were analyzed using a custom MATLAB tracking program. The same system was used to obtain the trajectories in the following experiments.

To measure drag coefficient k_f and the Cheerios effect coefficient k_c , we used recently deceased 301 ants. We euthanized the ants by placing them in the freezer for around ten minutes. We used 302 tweezers to straighten the ants' bodies and legs before placing them on the water surface. We gently 303 pushed the ant so that it started drifting with an initial velocity. We recorded 14 trajectories as they 304 decelerated due to fluid drag. We used Gaussian smoothing and forward difference to calculate the 305 velocity using a time interval of 0.06 s. We find that velocity decreases exponentially with time (Fig 306 S2), suggesting that fluid drag is proportional to the velocity magnitude. We obtain the coefficient 307 for drag k_f from fitting a straight line to the relationship between the logarithm of velocity $\log(U)$ 308 and time t. We measured k_f to be 0.24 mg/s ($n = 14, R^2 = 0.82$, Fig. S2). 309

The activity coefficient k_a depends on both drag coefficient k_f and the time step δt . For intuition, consider the random propulsion term $k_a \eta$ as an average value over a period of δt . The larger the δt , the more smoothed out the random signal becomes in each period, hence the smaller the activity coefficient k_a . To estimate k_a , we used $\delta t = 0.1$ s, the same value that we used for integrating Equation (2) in the simulations. Together, we obtained $k_a = k_f \sqrt{2D/\delta t} = 2.88$ nN. Detailed derivation of this relationship may be found in the supplemental materials.

The Cheerios effect coefficient k_c was measured by placing two dead ants on the water surface. Through the same procedure above, we calculated the relative velocity and acceleration as they attracted each other. The attractive force was calculated as the sum of inertia and fluid drag terms of the Langevin model, Equation (2). Fig. S3 shows that the attraction force decreases monotonically with the distance between the ants. We fit the data to the modified Bessel functions, which we expect from theory [41, 40, 39]. We arrived at $k_c = 2.56$ nN (n = 33, $R^2 = 0.83$).

322 Simulation

We performed 1860 agent-based simulations in MATLAB, consisting of 1200 simulations for raft destabilization and 660 for raft assembly. Raft destabilization simulations were performed with ants initially on a hexagonal lattice, and raft assembly simulations with a square lattice. Circular agents were characterized using four coefficients measured from experiments (m, k_a, k_f, k_c) and one free parameter, the close-range repulsion k_r that had little effect on the results when it was above the chosen value. At each time step, the location and the velocity of each agent were updated according to Equation (2). For raft destabilization simulations, we integrated the equations with a semi-explicit scheme with a time step of $\delta t = 0.1$ s. For each parameter combination, we simulated five minutes of ant motion. The results were averaged over ten trials with different seeds for random number generators.

For raft assembly simulations, we started the simulations from agents on square lattices. The simulation domain was a square that was 150 body radii wide. Periodic boundary condition was imposed in both directions so that the density within the domain remained constant. At the beginning of the simulations, agents were placed in 4x4 to 9x9 square formations. Similar to the raft destabilization trials, we simulated five minutes of ant motion, and results were obtained after averaging over ten realizations.

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Figure 1: Small rafts are unstable. (A) A raft of twenty ants on the surface of water. (Photo credits: Andre L Magyar and Candler Hobbs) (B) Proportion of stray ants P as a function of the raft size N. Orange triangles indicate experimental results (n = 72) and gray circles simulation results (n = 150). Orange and gray dashed lines represent the respective best-fit logistic functions for experiments and simulation. (C) A time series showing the destabilization of raft of five ants over 100 s. Scale bar is 1 cm.



Figure 2: Ants on the water surface behave as inertial random walkers. (A) Ten representative ant trajectories. (B) Probability distribution of the velocity magnitude U. Velocity components u and v are shown in the insets. The red solid line is the two-dimensional Maxwell-Boltzmann distribution with a standard deviation 3.5 mm/s. (C) Mean squared displacement of ant trajectories. The blue dashed line has a slope of 2 and the red a slope of 1, and both are offset from the best fit for clarity. The vertical gray dashed line marks the time scale we obtain through a separate series of experiments $\tau = m/k_f$ 4.3 s. The shaded area represents one standard deviation, which appears distorted under the logarithmic scale. n = 96 for both (B) and (C)



Figure 3: Destabilization of simulated ant rafts. (A) Trajectories of simulated ants as they start from a dense, ordered raft. Initial state of ants shown in red circles and end state shown with black circles. Note that many of the ending states have gone beyond boundaries of the figure. As the number of ants on the raft increases from 7 ants (left) to 9 ants (middle), and to 13 ants (right), rafts become more stable. (B) Schematic of our Langevin model (Equation (2)). (C) Raft stability diagram. Color represents the proportion of stray ants P after five minutes. Black dashed line marks the transition point where half of the ants go astray (P = 0.5).





Figure 4: Assembly of ant rafts from different initial spacings. (A) Proportion of stray ants P as a function of activity level k_a and initial spacing L. Top left inset show the definition of initial ant spacing L. The remaining insets show representative trajectories of ants across a time frame of five minutes. Time series of P for (B) small initial spacing L = 18.75 mm and (C) large initial spacing 30 mm. Color represents the P for all subplots.