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Horizontal Axis Wind Turbine Testing at High Reynolds Numbers

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Abstract

Detailed studies of modern large scale wind turbines represent a significant challenge. The immense length scales characteristic of these machines, in combination with rotational effects, render numerical simulations and conventional wind tunnel tests unfeasible. Field experiments can give us important insight into the aerodynamics and operation, but they are always accompanied by large amounts of uncertainty, due to the changing nature of the inflow, and the lack of accurate control of the test conditions. Here, a series of experiments is presented, using an alternative method that enables us to represent and study much of the physics governing the large scale wind turbines in small scale models. A specialized, compressed-air wind tunnel is used to achieve dynamic similarity with the field-scale, but under accurately controlled conditions of the laboratory. Power and thrust coefficients are investigated as a function of the Reynolds number up to $Re_D = 14 \times 10^6$, at tip speed ratios representative of those typical in the field. A strong Reynolds number dependence is observed in the power coefficient, even at very high Reynolds numbers (well exceeding those occurring in most laboratory studies). We show that for an untripped rotor, the performance reaches a Reynolds number invariant state at $Re_c \geq 3.5 \times 10^6$, regardless of the tip speed ratio. The same model was also tested with scaled tripping devices, with a height of only 9 μm , to study the effect of transition on the rotor performance. In the tripped case, the Reynolds number dependence was eliminated for all tested cases, suggesting that the state of the boundary layer is critical for correct predictions of rotor performance.

I. INTRODUCTION

Modern wind turbine design has been defined by ever-increasing rotor diameters with a ten-fold increase over the last four decades. Larger wind turbines mean a reduction in the total number of individual units requiring installation and maintenance, per kilo-Watt-hour produced, compared to a farm comprised of smaller turbines. The trend towards larger rotors holds whether installation is on- or offshore, with new onshore units exceeding 158 meters and offshore moving past 200 meters [1]. The power that can be extracted from the wind scales linearly with the rotor's swept area, or equivalently with the square of its

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diameter. Furthermore, a larger wind turbine implies access to higher wind speeds higher up in the atmospheric boundary layer. A wind turbine’s ability to convert this available power to useful mechanical power is expressed in the power coefficient:

$$C_p = \frac{P}{\frac{1}{2}\rho U^3 \frac{\pi}{4} D^2} \quad (1)$$

where ρ is the air density, U the wind speed, and D the turbine diameter. The measured power output, P , of a turbine depends on the fluid density, velocity, viscosity (μ), speed of sound, as well as specific turbine geometry and operating conditions. The exact nature between these parameters and the power output is not known, which implies that numerical and experimental simulations, and modeling are necessary to determine the effect these parameters have on the actual turbine performance. Dimensional analysis can inform us that the aerodynamics of a given turbine design is a function of three other non-dimensional parameters. These three parameters are the Reynolds number, the tip speed ratio, and the Mach number, which describe the relative effects of viscosity and rotor rotation to the inertia of the fluid, as well as the compressibility effects.

While these non-dimensional parameters govern the overall rotor response, added complexities in the atmosphere, such as turbulence, wind shear, and buoyancy, as well as structural properties further complicate the problem. For example, Herges *et al.* [2] show a remarkable difference between unstable and stable atmospheric conditions. One of the most common methods for quantifying turbine performance is through field measurements of the power coefficient. This method is complicated by the constantly changing, and challenging to monitor, inflow conditions present at any field site. Factors such as temperature, static pressure, wind shear, turbulence, and wind direction must all be constantly monitored and quantified, as no steady-state conditions exist in the field [3].

Power curves must then be collected over long periods of time, typically requiring months before acceptable convergence is observed in the statistics [4]. Therefore, although important as a validation tool, field experiments are both difficult to perform and expensive to implement while having a large amount of uncertainty in the results. This has driven a decades-long effort by wind turbine manufacturers and researchers to develop engineering design tools and modeling techniques for predicting turbine performance. The reliance on these modeling methods has a long history, with the basic design tool for aerodynamic input

loads (known as blade element momentum or BEM) remaining essentially the same since being developed in 1935 by Glauert [5, 6]. It is widely used in industry due to its low computational cost and the extensive legacy of modeling, validation, and certification efforts on which most of the current iterations of the method are based. However, BEM has a number of inherent deficiencies which must be accounted for through various engineering-type models. Some of the more common corrections attempt to capture three-dimensional and rotational effects, high thrust loading, yawed and turbulent inflow, and many other conditions commonly encountered in the field. These corrections are essential to model the loads accurately, and as such remain an active area of research. One downside of such methods is that limited additional insight can be gained into off-design conditions commonly encountered in the field, such as unsteady or time-varying loads, forcing designs to remain relatively conservative to meet the certification and life-time requirements of the modern turbine.

The dilemma of BEM and field testing has long been known to the research community, and the lack of experimental validation cases was cited as one of the biggest research challenges in a recent review article by van Kuik *et al.* [7]. Attempts at reducing the uncertainty in the power coefficient measurements have been made in two parallel tracks, via numerical simulations using the actuator-line method and laboratory experiments. The challenge for both approaches lies in the large physical scale of the turbine units themselves. This implies that the Reynolds number is very high, which in turn implies that the flows are turbulent:

$$Re_D = \frac{\rho U D}{\mu} \quad (2)$$

Values of Re_D range from $\mathcal{O}(10^5)$ for small-scale turbines with $D \approx 1 - 10$ meters up to $\mathcal{O}(10^8)$ for the largest, offshore units with $D \geq 200$ meters. Unfortunately, the high Reynolds numbers make Direct Numerical Simulations (DNS), where the governing equations are numerically solved at all length and time scales, unfeasible. Instead, Large Eddy Simulation (LES), Reynolds-Averaged Navier Stokes simulations (RANs), or inviscid/vortex-method solvers are used for studying wind turbine flows, where some or all of the turbulence is modeled within the solver. Additionally, except for all but the most advanced LES methods, the flow over the blades and rotors is not resolved, but instead modeled with a distributed forcing on the local numerical grid, in a BEM-like fashion, which requires two-dimensional airfoil data as input, meaning that 3-D and unsteady effects are not directly captured with these methods either.

From an experimental standpoint, few studies have been performed at what can reasonably be considered full-scale Reynolds number values. The underlying issue is the presence of the two non-dimensional parameters in addition to the Reynolds number. The tip speed ratio and Mach number are defined as:

$$\lambda = \frac{\omega R}{U} \qquad Ma = \frac{\omega R}{a} \qquad (3)$$

with ω the angular velocity, and a the sound-speed. Fundamentally, an experimental study seeks to operate with a much smaller diameter than the full-scale, typically two orders of magnitude or more. This means that, if the tests are conducted in conventional wind tunnels, the free-stream velocity must be increased by approximately 100 times or more compared to the field value, to match Re_D . Altering velocity has a domino-like effect on the other non-dimensional parameters, causing λ to decrease unless ω is increased to the rotor scale-ratio squared, or more than four orders of magnitude. Mechanically, this is not feasible due to the centrifugal forces created, and it also creates significant compressibility effects, as can be seen in the equations of 3. For these reasons, many laboratory experiments are performed at reduced Reynolds numbers [8], with only two notable exceptions where the models were physically large (4-10 meters in diameter) and very large wind tunnels were utilized [3, 9]. These studies have provided a number of insights into turbine operation at the full-scale, among them disparities between the BEM and measured loads [3], also clear indication of Reynolds number effects despite the large Re_D tested [10], and even some disparities between the rotationally-driven performance augmentation of both studies [11]. While these works provided some of the clearest insight yet into full-scale operation, there is still a definitive need for additional work concerning Reynolds number effects on turbine performance.

An additional, complicating issue is that experiments (even those performed at large-scale) are typically operated with fixed ω , while the tunnel velocity is altered to affect the tip speed. This means that rotational effects and Reynolds number effects are intermixed, as is also the case in field operation where ω can only vary by a small amount (due to restrictions on the generator, while blade pitch is used to control shaft power). A truly variable speed wind turbine model is required to extensively characterize both Reynolds number and tip speed ratio effects in detail. The lack of prior experimental work in this area again points to a need for additional quantification of these effects in a manner that

independently lends additional physical insight to the problem of scaling behavior for wind turbines.

In this study we aim to address the question of performance scaling with Re and λ for Horizontal Axis Wind Turbines (HAWTs). The challenges associated with wind tunnel tests, as discussed above, have been bypassed by implementing a specialized wind tunnel which uses highly compressed dry air as the working fluid. Increasing the pressure up to 238 bar allows for working fluid densities of over 200 times that of air at atmospheric pressure. Operating at variably densities effectively decouples the Reynolds number from the tip speed ratio, as the density only enters via the Reynolds number. This allows high Reynolds numbers to be achieved without the need for high tunnel velocities, instead they are on the same order as in the field, which avoids compressibility effects, and keeps the time scales relatively large. In this context, Reynolds number and tip-speed-ratio effects can be characterized independently of each other, and without Mach number effects or any assumptions or modeling.

II. EXPERIMENT DESCRIPTION

The experimental facility used in this work is a specialized, compressed air wind tunnel known as the High Reynolds number Test Facility (or HRTF). It is a recirculating-type, low-velocity, high static pressure wind tunnel which uses air as the working fluid. The facility can support up to 24 MPa, and free-stream velocities in the test section of up to 10 m/s. The test section itself is 4.88 m long with an inside diameter of 48.9 cm. This gives a blockage ratio (using the turbine swept area) of $A_{\text{model}}/A_{\text{tunnel}} = 16.7\%$ for the 20 cm rotor. Upstream of the test section is a contraction with an area ratio of 2.43:1 in which a series of flow conditioning screens and honeycomb straighteners are located. Free-stream velocity is measured via a pitot-static tube located upstream of the turbine model using a differential pressure transducer with a range of 3, 447 Pa (Validyne DP-15). This facility has been used previously to study wakes of axisymmetric bodies [12–14], zero-pressure gradient turbulent boundary layers [15], and more recently various wind turbine models of both vertical and horizontal axis varieties [16–18]. The HRTF is shown in figure 1.

In the pressurized test environment, real-gas effects are accounted for via:

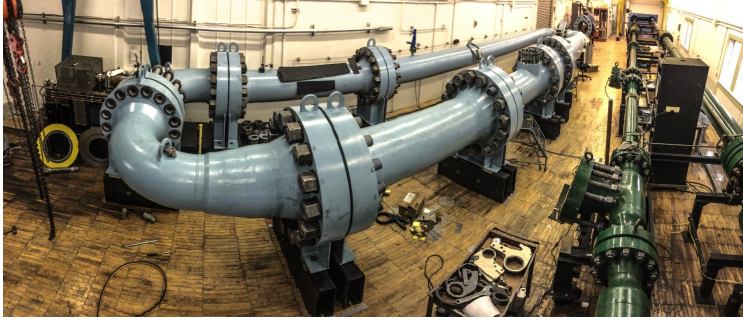


FIG. 1. The High Reynolds number Test Facility (HRTF, in light blue) located at the Princeton Gas Dynamics Laboratory.

$$\rho = p_s / (Z R_a T) \quad (4)$$

where R_a is the specific gas constant for air, T the tunnel temperature, and Z the compressibility factor. For dry air Z changes by only 10% for static pressures in the range 1 - 233 bar, meaning that density changes nearly linearly with static pressure in the test section. For all experimental data sets, the exact density and viscosity of the compressed air are calculated using the real-gas relationship of equation 4 with measurements of p_s and T from the test section [this method is outlined in 19]. The key to high Reynolds number testing using compressed air is that both dynamic viscosity and sound speed are only very weak functions of pressure, meaning that free-stream velocity can remain relatively low and the ω required for λ matching is mechanically feasible.

A. Wind Turbine Model

Challenges of operating in a pressurized environment include large forces and torques acting on the model, which scale linearly with fluid density. For instance, a model tested at the maximum HRTF pressure will see loads which are in excess of 200 times compared to those experienced in an atmospheric wind tunnel at the same velocity. Careful consideration was given to model design so as to minimize rotor deflections during even the most extreme operating conditions.

The rotor model used in these experiments is 20 cm in diameter and attaches to the tower gearbox via a threaded M7 hub. In this series of experiments, the rotor solidity is increased,

TABLE I. Wind Turbine Model Geometry. Between sections 1 and 2 the geometric shape transitions from a circular hub to an airfoil shape. The relative twist of these intermediate sections is set to 13 degrees.

Section	Radius (mm)	Chord (mm)	Twist (degrees)	Airfoil
1	3.704	11.11	13	Circular
2	14.815	28.89	13	NACA 63-235
3	100.0	11.11	0	NACA 63-214

in order to delay the stall tip speed ratio as well as increase the blade Reynolds number and torque. However, the current model operates in the same fashion as a full-scale, slender unit, such as the observed tip speed ratios and power/thrust coefficients are reasonable (i.e. in the lift-producing regime). Lower solidity would likely push the operational tip speed ratio range to larger values and the resulting lower Reynolds numbers (based on chord length) would probably increase the transition effects observed in this study. Future investigations will include studies of the effect of solidity, and allow for investigations of rotors more similar to modern field turbines.

Geometrical details of the three driving sections at hub, root, and tip locations are given in table I. The airfoil geometries, chord, thickness, and twist distribution between the sections were input to a Computer Aided Design (CAD) program. For sections 2 to 3 the extrapolation is straightforward since the airfoils are of the same family, and only the twist, chord, and thickness should be altered. Near the hub, the extrapolation between sections 1 to 2 is more complicated due to the circular hub geometry. It is expected that this has little effect on the performance, however, since it only comprises the inner 15% of the rotor. Three-dimensional CAD files are available upon request if additional information is needed regarding geometrical features of the rotor.

In general, the twist axis of the rotor was located at the quarter-chord of the airfoils, with the exception of the circular hub at section 1 where the twist axis was at the center of the circle. Twist schedule between sections 2 and 3 is nonlinear and was determined with the following equation:

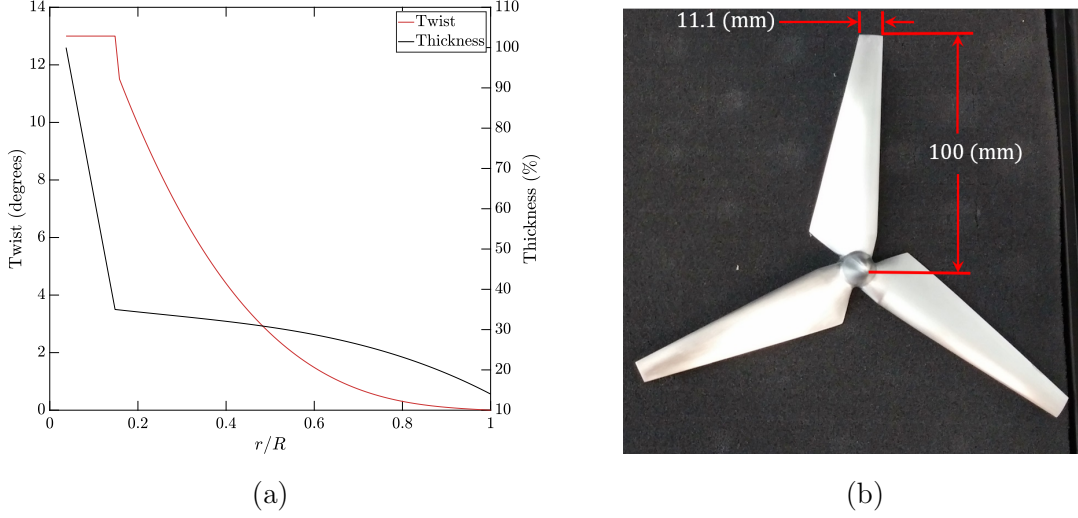


FIG. 2. Twist and thickness schedule for the rotor are shown in plot (a). The finished model rotor is given by the image in (b).

$$\text{Twist } (^{\circ}) = \begin{cases} 13, & \text{if } r/R \leq 4/27 \\ 18.148 \left(\frac{R-r}{R}\right)^3 - 7.698 \left(\frac{R-r}{R}\right)^2 + 8.504 \left(\frac{R-r}{R}\right), & \text{otherwise} \end{cases} \quad (5)$$

Similarly, the thickness has a linear distribution between sections 1 and 2, but is nonlinear between 2 and 3, as given by equation 6. The distribution of both the twist and thickness schedules are shown graphically in figure 2 (a).

$$\text{Thickness } (\%) = \begin{cases} 100 & \text{if } r = 0 \\ 585.01 \frac{R-r}{R} - 463.34 & \text{if } 0 < r/R \leq 4/27 \\ 27.42 \left(\frac{R-r}{R}\right)^3 - 61.41 \left(\frac{R-r}{R}\right)^2 + 57.07 \left(\frac{R-r}{R}\right) + 14, & \text{otherwise} \end{cases} \quad (6)$$

Meanwhile, the chord schedule between locations 2 and 3 is purely linear for any section falling between that given in table I. Rotor pitch is fixed at 5° defined as positive into the oncoming flow from the rotor plane. Yaw, cone and teeter angle have all been set to 0° . The spinner hub geometry was taken directly from Reynolds [20], and consists of a NACA 1 series spinner scaled to the appropriate size for the model. The final rotor is CNC milled from a solid block of aluminum alloy which ensures a high tolerance on the surface finish and

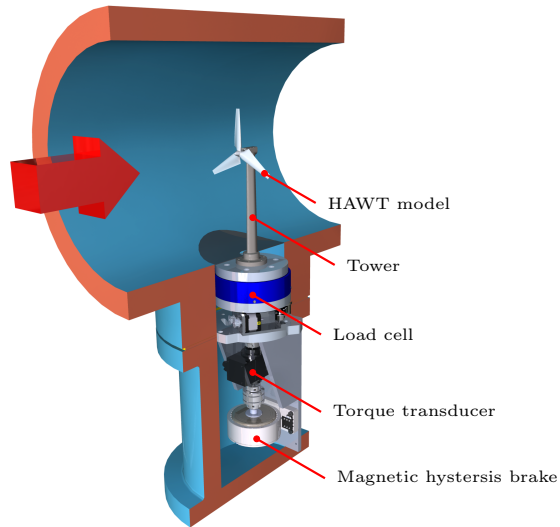


FIG. 3. Sectional view of the HRTF test section with the model wind turbine and measurement stack in place. Red arrow shows direction of flow.

dimensional accuracy. The final model is shown in figure 2 (b). Particular care was given to the surface finish of the model as matching all length-scales is required for full-dynamic similarity. The surface roughness was carefully measured using an Olympus LEXT OLS4000 confocal microscope and the area-averaged, root-mean-square roughness height was found to be $S_q \leq 800$ nm consistently among all three blades. The effect of surface condition on observed rotor performance is discussed in section VI. Section VB details the addition of prescribed tripping devices designed with this same methodology to force transition on the rotor blade surface.

The model tower and nacelle were designed to handle the high loading cases present at maximum tunnel density inside the HRTF. Their design and construction is detailed in Miller *et al.* [16]. The tower cross-section resembles a diamond-shape with rounded edges, so as to support the large aerodynamic thrust and torque imposed by a spinning rotor with minimal deflection and additional drag. Details concerning blockage effects due to the tower and rotor are discussed in appendix A.

B. Instrumentation and turbine operation

A measurement and control stack was designed to accurately resolve the mechanical loads produced by the model turbine. Shaft torque, τ , angular velocity ω , force components at the tower base (F_x , F_y , and F_z), as well as moments at the tower base (M_x , M_y , and M_z) are measured simultaneously during an experimental campaign. The physical layout of the model and measurement stack starts with the solid rotor model of fixed pitch as described in II A. The model is mounted on the input shaft of the tower. Inside the tower itself is a small right-angle bevel gearbox which re-directs the mechanical power 90 degrees and outside of the tunnel test section for measurement. Correction methodologies which account for gearbox inefficiencies are discussed in section A 1. A six axis force and moment transducer (JR3 Inc. model 75E20A4) is mounted at the base of the tower, for measurement of the aforementioned forces and moments on the tower. The force sensor body is bolted to a rotary table, allowing for adjustment of the turbine yaw. The output shaft for the tower gearbox is located in the center of the measurement stack and passes through the central axis of the force sensor and rotary table. The output shaft is then coupled to a torque transducer (Magtrol model TM-305 with a range of ± 2 Nm). This unit allows for time-resolved measurements (temporal resolution of 5 kHz.) of the torque signal and determination of the rotational speed via an internal optical encoder. Power is dissipated from the system using a magnetic hysteresis brake (Magtrol model AHB-3), which applies precise shaft torque loads; giving full control over ω independently of wind speed and density. The brake serves the same function as the generator of a full-scale turbine, with greatly increased accuracy and flexibility in its operating window. All of these components together make up the measurement stack, shown in figure 3. The uncertainties associated with each measurement device are summarized in table II.

III. EXPERIMENTAL PROCEDURE

The HAWT model used in these experiments is operated in a manner similar to that of full scale modern wind turbines with full variable speed drives [21]. The experiments presented here can easily be operated at many different rotation rates as all the mechanical energy is dissipated as heat by the magnetic hysteresis brake, which is passively cooled

TABLE II. Experimental uncertainty sources listed include linearity, hysteresis, and temperature influences combined in a root-mean-square sense for each sensor.

Measurement Unit	Symbol	Total Uncertainty
Torque Signal	τ	$u_\tau = \pm 0.003$ (Nm)
Angular Velocity	ω	$u_\omega = \pm 0.105$ (rad/s)
Axial Thrust Force	F_t	$u_{F_t} = \pm 2.5$ (N)
Pitot-Static Pressure Transducer	\bar{p}	$u_{\bar{p}} = \pm 34$ (Pa)
Density	ρ	$u_\rho = \pm 0.36\%$
Viscosity	μ	$u_\mu = \pm 0.8\%$

by the high density air. This method is in principle a full variable-speed wind turbine, where any ω may be specified during operation. Field data is often viewed in terms of the inflow velocity U , since ω is fixed. This creates uncertainty when viewing data plotted as a function of λ , as wind and rotor speed correlation only is obtained through the 10 min binning discussed earlier. Another issue with this method of viewing data is that not only is λ changing, but Re_D is additionally being altered along the abscissa, making it inherently difficult to separate these two effects in the field when plotting data as a function of tip speed. For the experiments presented here we have elected to keep U and ρ approximately constant during a run, and vary ω over a pre-determined range. This means that for a given measured C_p or C_t curve, the inflow conditions, and hence Re_D , remain constant while λ is altered. In this way Reynolds number effects and tip-speed-ratio effects can directly and independently be observed and studied. Operating the model turbine with fixed inflow additionally allows for convenient data collection. If the model were to be operated as in the field, an additional controller would be needed to maintain a fixed rotation rate as the tunnel velocity or density is altered. If field-style data is required, it may be interpolated from the finely resolved measurements at the desired inflow conditions. Dynamic similarity implies that for a geometrically similar rotor, when Re_D and λ are matched, all other Reynolds numbers such as Re_c , or however Re is defined, are matched as well.

The following sections explore the power-output and resulting thrust forces on the HAWT model. The experiments presented herein are the first of their kind in which a small-scale model is tested with Reynolds number, tip speed ratio, and Mach numbers that simultane-

ously match those experienced by full-scale wind turbines. The primary goal of this work is to gain quantitative insight into the effects of Reynolds number on the performance of modern day wind turbines. Furthermore, it sets the stage for a long list of questions that can be answered using the same methodology. The set of experiments presented here have been restricted to what can be considered the most canonical case for a wind turbine, where the inflow is steady, uniform and laminar, the rotor plane is aligned perpendicular to the inflow velocity vector, and the free-stream conditions are fixed for each power curve (i.e. Re_D constant during a run). A significant amount of consideration has also been given to account for experimental uncertainties in the drive-train and for blockage effects, as detailed in the appendix A. All of these methods have enabled an unprecedented level of precision in the data acquisition, and allowed for a detailed investigation of Re_D and λ effects.

IV. UNTRIPPED HAWT ROTOR PERFORMANCE WITH REYNOLDS NUMBER

Performance of the wind turbine model is characterized using the non-dimensional power coefficient as given by equation 1 and the thrust coefficient:

$$C_t = \frac{F_t}{\frac{1}{2}\rho U^2 A}, \quad (7)$$

where F_t is the streamwise force exerted on the hub by the rotor (commonly referred to as the thrust force). Together, C_p and C_t indicate the forcing placed onto the flow and therefore drive wake structure and dynamics. Furthermore, they are typically used as the defining performance metrics during the design phase, with C_p in particular being directly tied to the projected revenue of a turbine. In the context of these experiments, careful measurements have been made of both parameters so that conclusions may be drawn as to their dependence on both tip speed ratio and Reynolds number. The following section describes the method of data validation used for these experiments. Then Reynolds number trends are discussed for the untripped rotor. The same rotor is then studied with the transition location fixed near the leading edge along the span via the use of an array of miniature tripping devices.

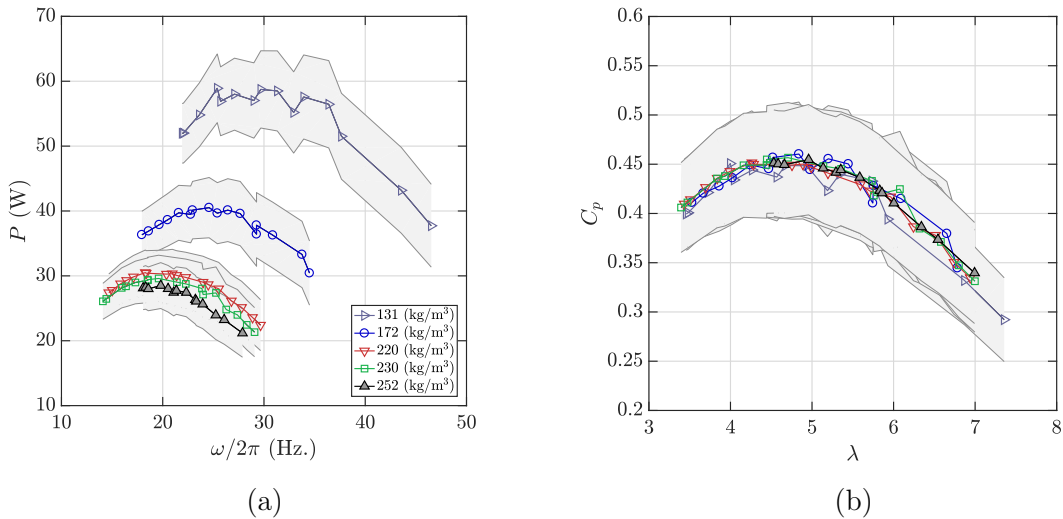


FIG. 4. Dimensional plots in (a) show measured power versus the rotational frequency at a matched Reynolds number of $Re_D = 5.099 \times 10^6 \pm 34,000$. Note that the data set at $\rho = 252 \text{ kg/m}^3$ (with shaded symbols) was taken with a different gearbox. The plot to the right in (b) shows the same data non-dimensionalized by the free-stream conditions. Shaded area represents experimental uncertainty.

A. Experimental Data Validation

The unique nature of the HRTF allows for adjustment of the tunnel density independently of the free-stream velocity to achieve a given value of the Reynolds number. Utilizing this capability, a specific Reynolds number case can be achieved using various combinations of operating conditions. As such, different combinations of velocity, density and rotational speed can result in exactly the same Reynolds number and tip-speed-ratio and thus yield identical values of the power and thrust coefficient. For all possible operating conditions, the free-stream Mach number is always low enough to neglect compressibility effects. This is not only an excellent method to validate the experimental results, it also enables significant reduction of measurement uncertainty since the forces and torques can be tailored to the instrumentation. Figure 4 highlights this unique feature, where different operating conditions together yield a mean Reynolds number of $Re_D = 5.099 \times 10^6 \pm 34,000$. The bounds on Re_D reflect the maximum deviation of any given data set from the mean Reynolds number value due to slight variations in tunnel conditions from run-to-run. Tunnel density is shown

in the legend of figure 4 (a), as well as the gearbox used for the run (with the legend also applying to plot 4 (b)). Note that despite very different densities between the data sets, the power curves collapse well within the experimental uncertainty when non-dimensionalized in 4 (b) with the shaded bars giving the uncertainty calculated at each operating point (details of the uncertainty analysis are given in table II). Collapse is seen across all cases in C_p , with slightly more scatter in the $\rho = 131 \text{ kg/m}^3$ case, which may be due to the increased rotational rate of the lower-density, higher free-stream velocity of this run. A single, high-density case using a different gearbox at $\rho = 252 \text{ kg/m}^3$ is also given and agrees well with the other three data sets, providing validation for the correction methodology used for the gearbox (as discussed in appendix A). The experimental data were validated using the above methodology at several Reynolds numbers ($Re_D = 7 \times 10^6$, 10×10^6 , and 12×10^6). The resulting non-dimensional power and thrust are shown in figure 5. The right-most column of plots of figure 5 show the thrust coefficient, which displays more scatter than the power coefficient, especially at higher Reynolds numbers of 10×10^6 and 12×10^6 . This is primarily due to the larger uncertainty associated with the load cell used for axial force measurement (details in section II B). The power coefficient shows excellent collapse across all tested Reynolds numbers and gearboxes used for these measurements. As the Reynolds number is increased, the ratio of signal to noise ratio also increases due to the larger loads measured. This has the direct effect of reducing the uncertainty as Re_D is increased, which is reflected by the shrinking error-bars shown in gray. As mentioned earlier, each case can be tailored to maximize the measurement range of the sensors, and as such reducing the uncertainty. For example, at low Reynolds number combining lower density with higher velocity yields larger forces and torques. Such optimization of the operating conditions are not possible in an atmospheric-pressure facility, where instead larger uncertainty often must be accepted, or different instrumentation must be used for each test case.

B. Untripped Rotor Performance with Reynolds Number

The power and thrust coefficients are shown in figure 6 for a range of Re_D values from 4 to 14 million. The power coefficient shows a clear dependence on Reynolds number, with the lowest Re_D case tested giving the highest power coefficient and a clear trend where the power coefficient is reduced as Reynolds number is increased. This observation is quite unexpected,

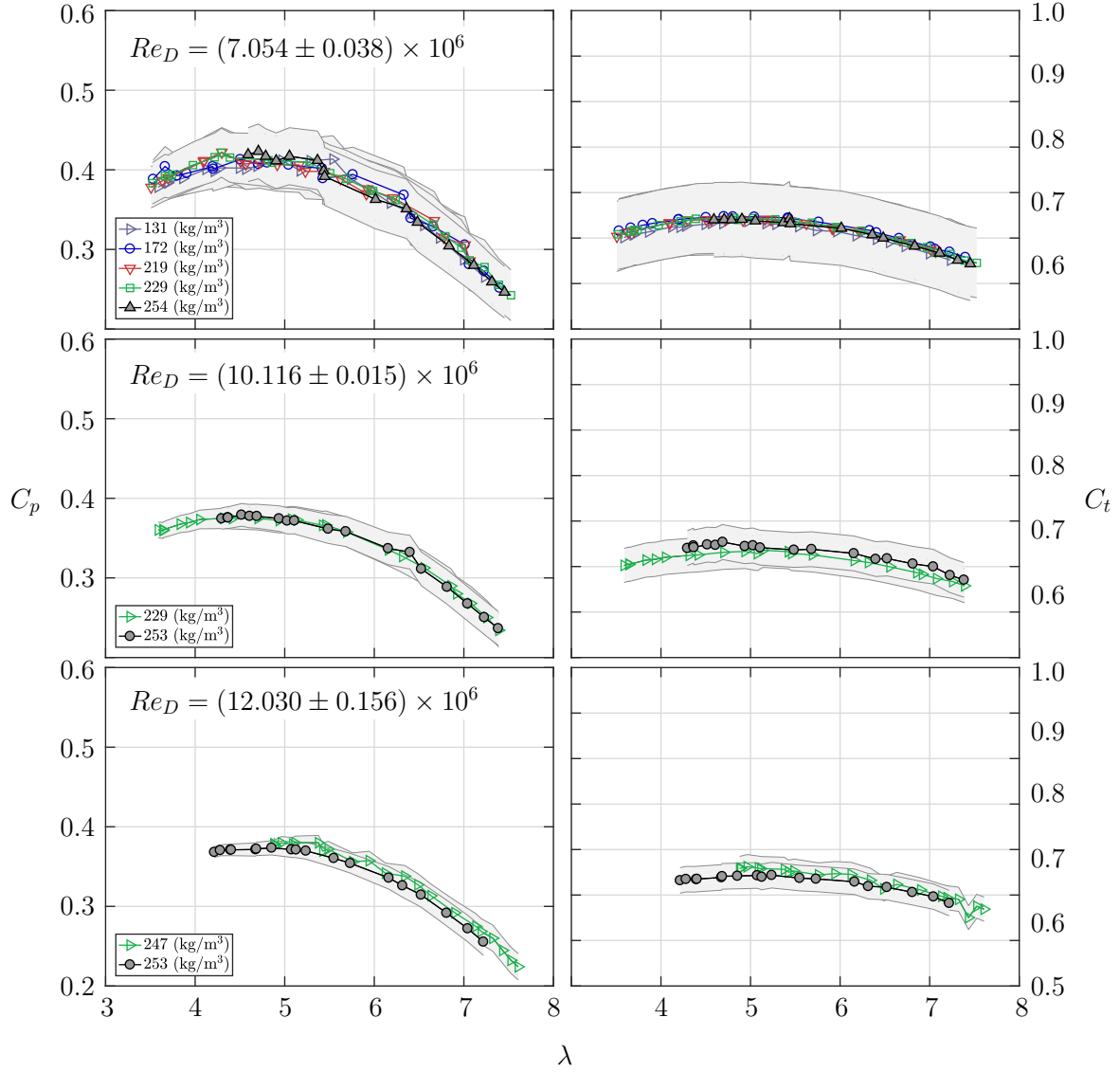


FIG. 5. Power and thrust coefficient data validation for three different Reynolds numbers. Labels for the Reynolds number and the legends apply to each pair of horizontal plots. Data sets with shaded symbols used a different gearbox.

as prior literature near these Re_D values has reported the opposite trend [10], although the specific airfoils used for these two rotors are different. It is further observed that the power coefficient levels off and is starting to exhibit collapse at higher Reynolds numbers. This implies that for the specific rotor geometry and inflow conditions used here, above a critical Re_D value the power coefficient is independent of Reynolds number. The results on the thrust coefficient are less pronounced with no clear trend evident with Reynolds number, although

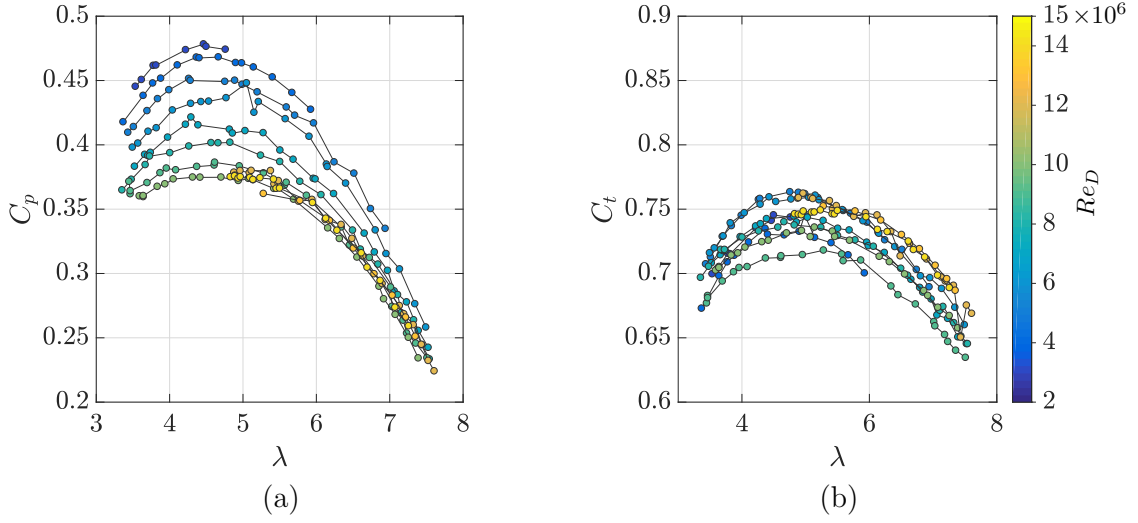


FIG. 6. Reynolds number trends of the untripped rotor for power (a) and thrust (b) coefficients. Colorbar at right represents the Reynolds number based on rotor diameter for both plots, and is held constant for each measured curve.

strong conclusions cannot be made at this point, as the data fall within the experimental uncertainty. However, it is clear that if a trend exists with Reynolds number it is much less pronounced compared to that in the power coefficient.

Results from the power coefficient indicated a relatively large Re_D value was necessary for invariance to the Reynolds number. However, higher values of λ appear to show invariance at lower Re_D . For instance, at $\lambda = 7$, invariance occurs around $Re_D \geq 8 \times 10^6$ whereas at $\lambda = 5$ a $Re_D \geq 10 \times 10^6$ is required. Such a two-parameter dependence indicates that neither parameter independently captures the physical mechanisms at play. Traditionally, aerodynamics is parameterized with the Reynolds number based on the chord length and the relative velocity [8]. Such parameterization is quite inconvenient in this case as the chord Reynolds number varies throughout the rotor. However, the physical effects described by the chord Reynolds number can be captured by a combination of Re_D and λ and, for example, the chord length along the blade. This results in a non-dimensional group from easily measured and reproducible quantities. Here, a Reynolds number based on the tip geometry has been utilized which may be determined if Re_D , λ , and the ratio of tip chord to diameter are known as:

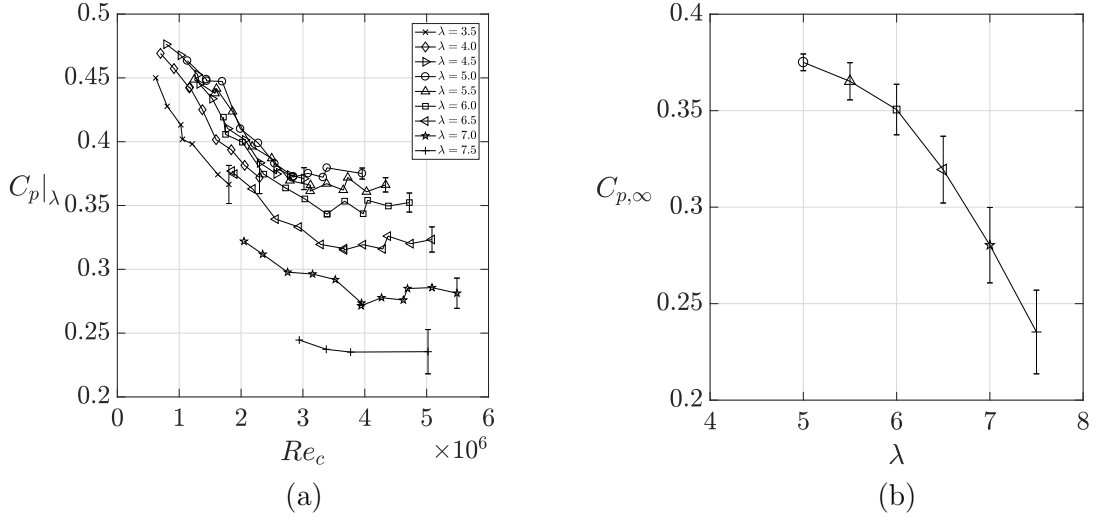


FIG. 7. Power coefficient as a function of the local blade Reynolds number for a variety of fixed tip speed ratios in (a). Figure (b) shows the Reynolds number invariant power curve for the model turbine geometry used under laminar inflow conditions. This plot was created by finding the mean value of C_p at fixed λ when $Re_c \geq 3.5 \times 10^6$.

$$Re_c = \frac{\rho c \sqrt{U^2 + (\omega R)^2}}{\mu} = Re_D \frac{c}{D} \sqrt{1 + \lambda^2} \quad (8)$$

The parameter Re_c represents the maximum possible Reynolds number which could be encountered at the rotor tip, and as such the true chord Reynolds number is slightly lower. Furthermore, experimental data from many sources can be couched in terms of this definition of the Reynolds number if only a few measured quantities are known and no modeling is necessary to determine Re_c . The current data was not acquired at predetermined values of the tip speed ratio, and so the data presented in figure 6, along with data from additional cases, have been interpolated to a fixed λ grid. This makes calculating Re_c straightforward for all data points. The power coefficient as a function of Re_c is shown in figure 7 (a) for various values of the tip speed ratio.

Individual curves in this figure represent the fixed λ grid values to which the measured power coefficient was interpolated. Moving up in Re_c (i.e. across the abscissa of figure 7 (b)) is equivalent to fixing λ and traveling vertically downwards in the power curves of figure 6 (a). Whenever a power curve is crossed, the local value of C_p is interpolated and the resulting value of Re_c is calculated. Since the power curves are relatively dense with

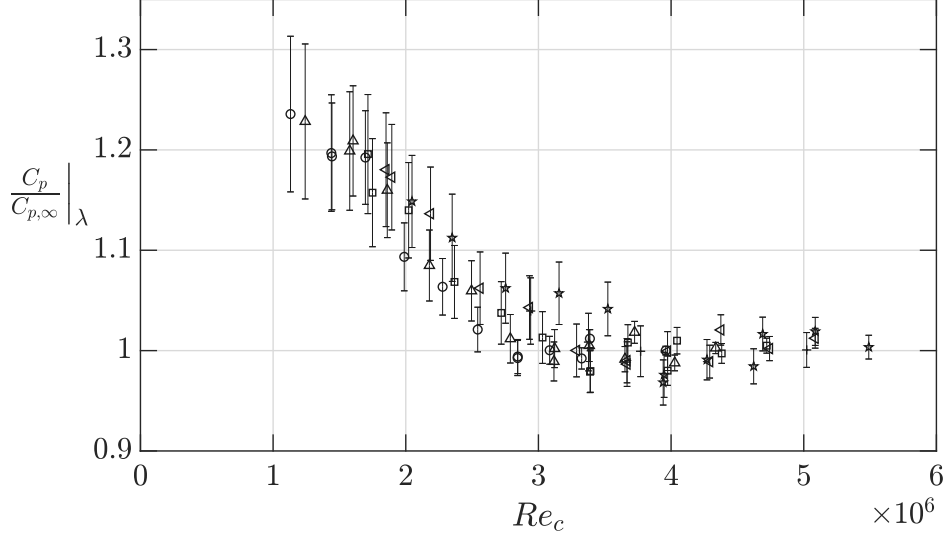


FIG. 8. Power coefficient normalized by the value at Reynolds number invariance for several tip speed ratios. Symbols correspond to λ : 5.0 = \circ , 5.5 = \triangle , 6.0 = \square , 6.5 = \triangleleft , 7.0 = \star , 7.5 = $+$.

data points (typically consisting of more than fifteen individual tests), errors due to this interpolation are expected to have minimal effect on the results. In this way, the rate at which the power curves approach the high Reynolds number limit can be directly observed. The resulting plot gives the power coefficient as a function of the blade Reynolds number and is shown in figure 7 (a).

Neglecting the $\lambda = 3.5, 4.0,$ and 4.5 cases due to the low maximum values of Re_c , the remaining curves show a plateau-like behavior above $Re_c = 3.5 \times 10^6$ whereby any additional increases in Re_c do not appear to affect the power coefficient of the turbine. This suggests that C_p has become invariant to the Reynolds number above this limit. Using the data of figure 7 (a), the invariant power coefficient can then be directly calculated by averaging power coefficient values which fall above the threshold of $Re_c \geq 3.5 \times 10^6$. The resulting parameter is denoted as $C_{p,\infty}$ and is shown in figure 7 (b). This is the power curve which would be returned by a model or field-scale turbine of the same geometry when $Re_c \geq 3.5 \times 10^6$. Such a Reynolds number invariant power curve can be used as a reference point for numerical simulations or model building studies, and to evaluate Re behavior of other experiments using the same geometry.

Further insight can be gained into the behavior of the rotor aerodynamics at lower Reynolds number by combining the results of figures 7 (a) and (b). For each tip speed

ratio, the entire curve of figure 7 (a) is normalized by the relevant $C_{p,\infty}$ value of figure 7 (b). This is shown in figure 8. If the cutoff Reynolds number has been chosen correctly, all curves will trend to unity, with some scatter due to experimental uncertainty as can be seen in the figure. An expected collapse is seen across all tip-speeds for lower Re_c values as well. This further indicates that the parameter Re_c accurately characterizes the physics responsible for the lower Reynolds number augmentation. This implies that the performance of the turbine at reduced Reynolds numbers can be found with a limited number of experiments. For example, if the invariant power curve is known, then experiments at a single λ for a range of Re_c values gives the resulting C_p for any other tip speed. While this specific result is only applicable to the current turbine and test conditions, future work will aim to determine if this is a universal trait of wind turbine operation at high Reynolds numbers.

V. BOUNDARY LAYER TRANSITION EFFECTS

Generally, increasing the Reynolds number of a boundary layer will move the point of transition, from laminar to turbulent, upstream. The exact position where the boundary layer transitions is not fully understood and as such, is challenging to predict. The situation is further complicated on a wind turbine rotor where the boundary layer is experiencing imposed external pressure gradients, streamline curvature, as well as centrifugal forces. Therefore, it is common to pin the transition point using tripping devices near the leading edge with the goal of forcing the boundary layer to be turbulent over nearly all of the airfoil [22, 23]. Fundamentally, this has the benefit of eliminating some of the problems which are commonly associated with an airfoil section experiencing transition, such as extreme sensitivity to boundary and initial conditions and laminar separation. Ideally, a tripped airfoil will better approximate the performance of the untripped model tested at very high Re values, where the boundary layer would naturally transition early on the airfoil surface. Practically, tripping devices are not perfect and typically add some amount of section drag, thus affecting overall performance compared to a naturally transitioning flow.

To determine if transition is contributing to the somewhat unexpected Reynolds number behavior observed with the untripped rotor, the same rotor model was equipped with tripping devices close to its leading edge. The exact same methodology as was used to study the untripped rotor was otherwise used for the tripped rotor. In the field, effects due to

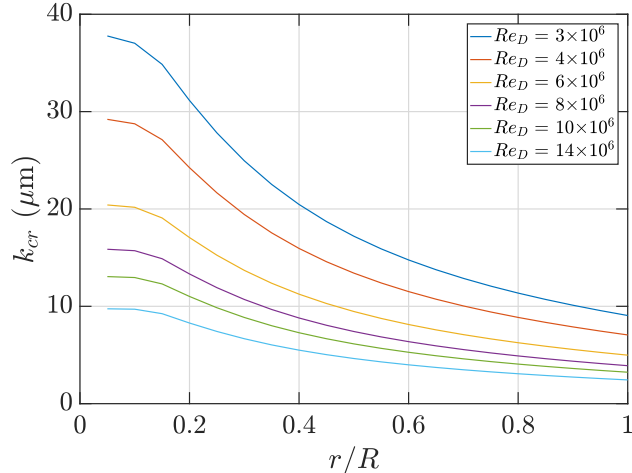


FIG. 9. Critical roughness height for $Re_k = 600$ as a function of radial location for various free-stream Reynolds numbers. Note that the external tip speed was fixed at $\lambda = 5.0$.

transition might be less significant as debris and other imperfections on the rotor contribute to earlier transition. However, since transition is highly sensitive to Reynolds number, and a phenomenon well known to be challenging to capture numerically, it is important to perform any such studies at field-scale relevant Reynolds numbers.

A. Trip Geometry

Tripping devices were added to the suction and pressure side of the model rotor blade with the goal of fixing the transition location. The trip height, k_{cr} , was determined by using a roughness Reynolds number, $Re_k = 600$ as in the work of Braslow and Knox [22]. External velocity was estimated along the rotor span via $U_{ext} = \sqrt{U^2 + \omega r^2}$, where U is the free-stream velocity and r the local radius. Determination of k_{cr} was performed at a fixed external tip speed of $\lambda = 5.0$ for simplicity and due to the fact that this corresponds to the maximum power coefficient of the untripped rotor for most Reynolds numbers (see figure 7 (a)). The value of k_{cr} along the rotor span is given for a variety of representative Re_D values in figure 9.

From this figure, it was determined that a critical roughness height of $k_{cr} \approx 8 \mu\text{m}$ would be sufficient to trip the rotor at all Reynolds numbers and tip speed ratios. Ideally, the roughness height would vary with Re_D , λ , and radial location, but this would have created an impractical number of experimental configurations. The main drawback of using a single

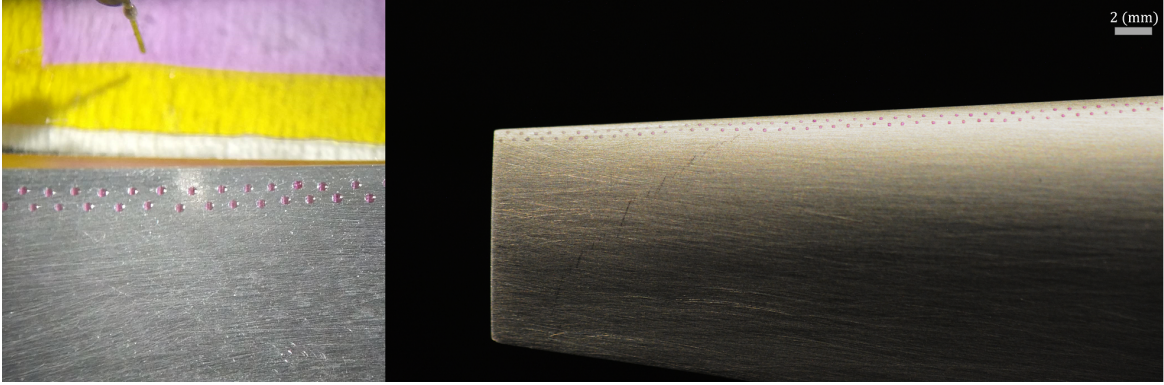


FIG. 10. Dot application process shown at left, performed via microscope and an epoxy-bonding tool. Right image shows the tip of a finished rotor blade with dots applied.

sized tripping device is that it can yield additional drag in some cases.

Various methodologies were attempted to produce a reliable and repeatable tripping geometry at the micron scale. Traditional tripping devices such as sand-grain type grit, zig-zag tape, and trip wires could not be applied at sufficiently small scale to satisfy the requirements on k_{cr} . The final methodology involved using MEMS-based clean-room tools (West-Bond Incorporated epoxy bonder model 7200A) to manually apply ultra-violet cureable epoxy dots (Norland Electronics Adhesive part number 123SBL) to the surface of the rotor. A macro-photograph of the resulting epoxy micro-dots is shown in figure 10.

Following application to both the suction and pressure side of the rotor, a sample of dots were imaged with a confocal microscope (Leica DCM 3D micro-optical system) at various locations on both sides of two blades. The resulting trip height was found to be $k = 8.82 \pm 3.95 \mu\text{m}$ for the front row and $k = 10.86 \pm 4.11 \mu\text{m}$ for the downstream row. Average diameter was measured to be $184 \mu\text{m}$ with a spacing around $700 \mu\text{m}$. Row spacing was found to be $330 \mu\text{m}$, on average. The dimensions of the trip pattern approximately correspond to classical zig-zag tape used in full scale wind turbine testing.

B. Tripped Rotor Performance

Plots of power and thrust coefficients for the tripped rotor are given in the figures of 11. Untripped rotor data from figure 6 (a) and (b) are shown for comparison in the left-most plots. Note that not all Re_D cases tested for the untripped case are currently available for

the tripped rotor. Interestingly, collapse in the power coefficient is seen, within experimental error, over the entire Reynolds number range, with only the lower Reynolds number and tip speed deviating slightly. This result implies that whatever mechanism is causing the performance augmentation at lower Re_D values observed on the untripped rotor is related to, or at least affected by, transition. Interestingly, a more clear Reynolds number trend is observed in the plots of C_t than that for the untripped rotor. Higher Re_D values correspond to a larger thrust coefficient for the tripped case, with $Re_D = 10 \times 10^6$ and 14×10^6 cases collapsing. Data for the tripped rotor was interpolated to a fixed λ grid, as previously done for the untripped rotor, to determine the Reynolds number trends in more detail. Figure 12 (a) shows the tripped data as a function of Re_c . Note that very little change is seen for any tip speed ratio as Re_c is increased. This confirms the trend observed in the prior figure. It appears that prematurely forcing boundary layer transition along the rotor surface causes it to perform in a similar manner as the untripped rotor in the high Reynolds number limit. There are slight differences in the behavior, which are more readily observed when viewing the respective $C_{p,\infty}$ values for the tripped versus untripped rotor in figure 12 (b). It appears that the addition of tripping devices has slightly decreased the high Re performance. This could be due to the additional drag introduced by the trip devices themselves.

Finally, the data of figure 12 (a) are normalized with the invariant power curves as in the untripped case. The result is given in figure 13. As expected, the specific tip speed chosen has little effect on how the power coefficient changes with Re_c . When calculating $C_{p,\infty}$ for the tripped case, the restriction of $Re_c \geq 3.5 \times 10^6$ could be removed. Invariant behavior is achieved almost immediately, although no Re_c values below 1 million are available to check this behavior at what could be considered conventional laboratory Reynolds numbers.

VI. DISCUSSION OF OBSERVED ROTOR BEHAVIOR

Two potential mechanisms for the observed rotor behavior are discussed: changes to the 2-D lift curve due to thick airfoil sections and sectional drag changes due to surface geometry. The first mechanism is related to a decrease in the lift coefficient with Reynolds number. This method of operation is non-standard with regard to classic thin-airfoil behavior [23], however a majority of the rotor utilizes airfoils above 20% thickness ratio, and could be

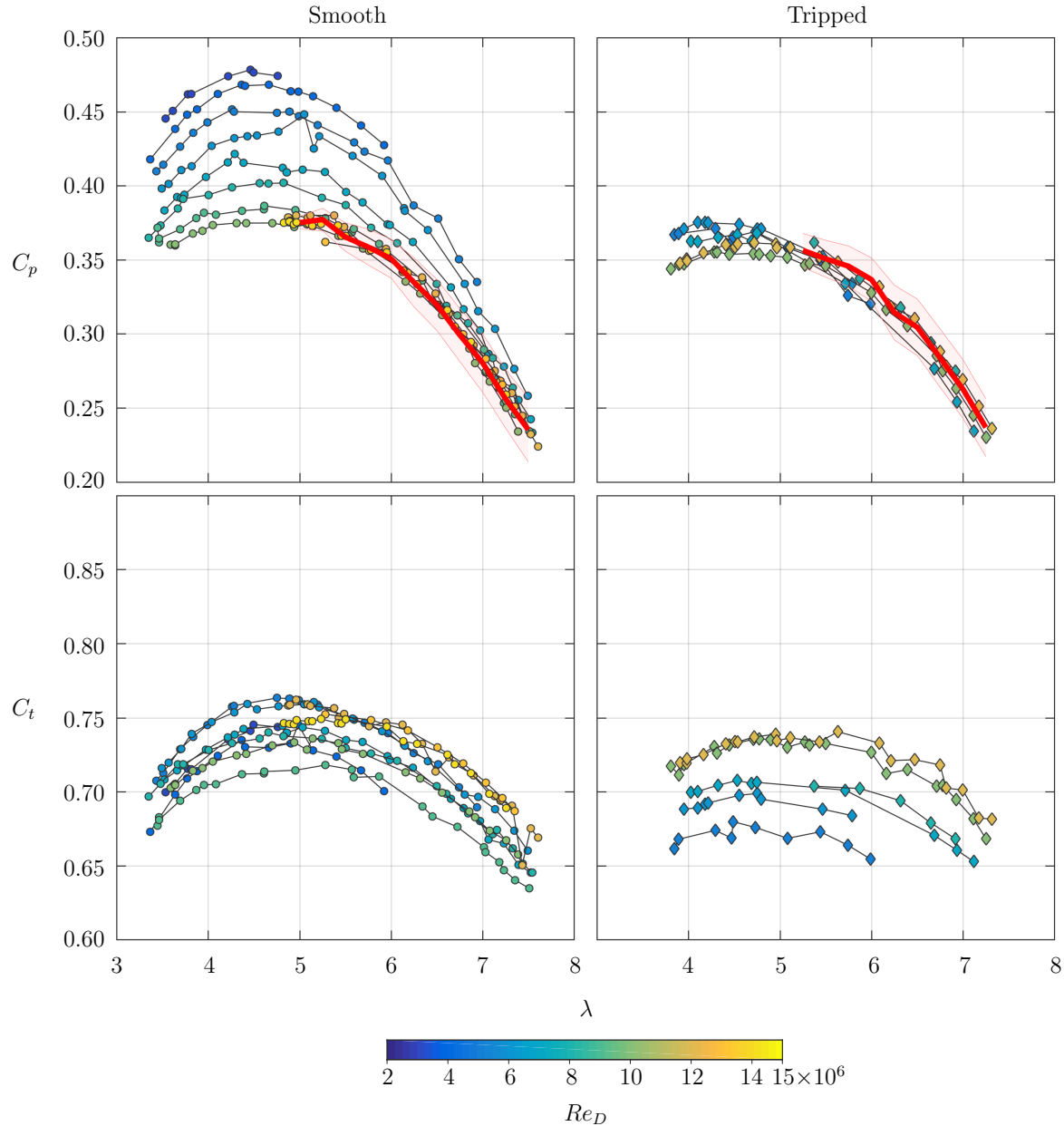


FIG. 11. Power and thrust coefficients for the untripped and tripped rotor geometries. The left-most plots are reproduced from figure 6 for comparison. The red lines represent the respective $C_{p,\infty}$ curve for each rotor case. The value is defined as the mean C_p when $Re_c \geq 3.5 \times 10^6$.

expected to have different behavior from the thin airfoil case. Preliminary measurements have been conducted for two sectional airfoil profiles in order to gain additional insight into their behavior. These are the tip NACA 63-214 (14% thickness) and the root NACA 63-235 (35% thickness) airfoils. Several different Reynolds numbers were investigated (on the same

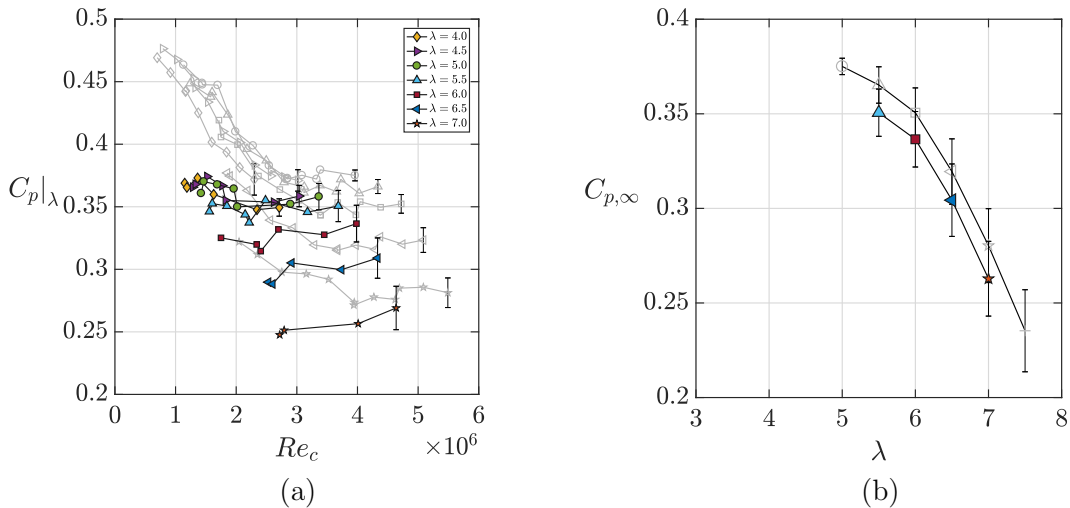


FIG. 12. Power coefficient as a function of the local blade Reynolds number in (a) for a variety of fixed tip speed ratios, similar to figure 7. Figure (b) shows the Reynolds number invariant power curve for the model turbine geometry used under laminar inflow conditions. Untripped data points are shown as gray symbols in both plots for reference.

order as the fully-three dimensional rotor tests) with the 63-214 profile agreeing well with numerical simulations performed using Mark Drela’s XFOIL code [24]. The thicker 63-235 airfoil section diverged from typical Reynolds number behavior, specifically the lift-curve slope with angle of attack, $\frac{\partial C_l}{\partial \alpha}$, was observed to decrease as Reynolds number of the airfoil increased. This would indicate reduced performance of the inner sections with increased Re_c (for a fixed α value) consistent with the observed decrease in rotor performance. These preliminary experiments indicate that the thicker sections of the NACA 6-series may diverge significantly from thin-airfoil theory, with the mechanism causing this divergence still under investigation. It is also not yet clear at what thickness this behavior begins to manifest, experiments by other authors performed at up to 21% thickness ratios using this airfoil family (NACA 63₃-221 section by Abbott and Von Doenhoff [23]) did not display a changing lift curve slope with Reynolds number. Therefore, we expect this transition from classical airfoil behavior to that observed for the thicker 6-series to occur somewhere between these two values. Given that the airfoil section at mid-radius of the rotor is approximately 26%, a majority of the rotor may be susceptible to these effects.

Another plausible mechanism accounting for the decreased rotor performance is related

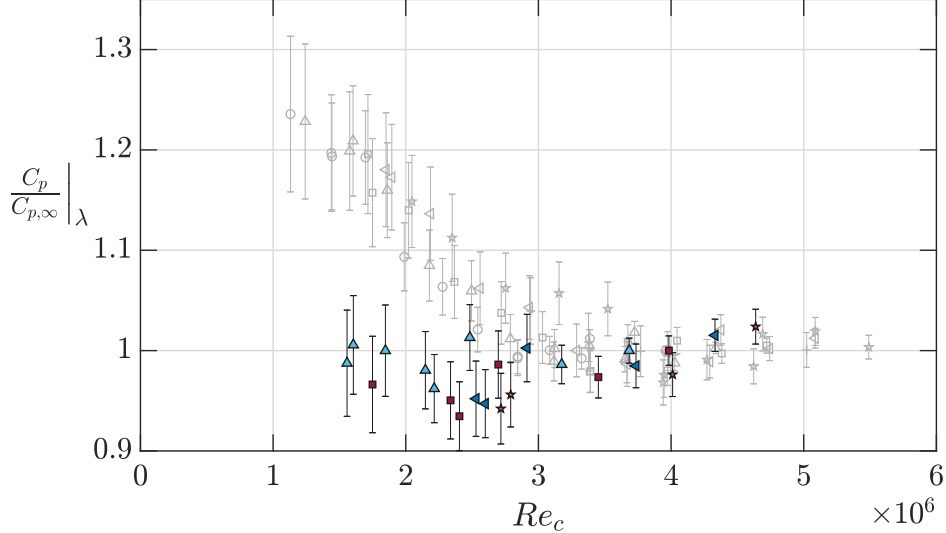


FIG. 13. Power coefficient normalized by $C_{p,\infty}$ for the tripped rotor (color filled symbols) and the untripped rotor data (as gray markers). Symbol shape corresponds to λ : 5.0 = \circ , 5.5 = \triangle , 6.0 = \square , 6.5 = \triangleleft , 7.0 = \star , 7.5 = $+$.

to the surface features on the rotor itself. In section II A the surface roughness was measured to be 800 nm in height, on average, across the rotor blade. Although this value is small, the roughness height may be large enough to have some effect if Re_c is made large enough. The complicated nature of surface roughness interactions with the airfoil boundary layer means that a variety of sectional performance changes are possible. In one case, the airfoil boundary layer may be transitioning from a laminar state to turbulence earlier than would be predicted with a numerical code. This would cause additional drag on the rotor, and hence reduce performance, with this effect becoming more pronounced as Re_c is increased until the boundary layer over the airfoil is completely turbulent. This mechanism is supported by the results of section V where the rotor was artificially forced to transition from laminar to turbulent flow near the leading edge, which resulted in decreased, low Re performance that approximated the un-tripped rotor case operating at high Re .

A second method by which the surface features can affect rotor performance is via aerodynamic roughness. A surface in turbulent flow may become aerodynamically rough if the roughness height becomes larger than the viscous sublayer. In this context, the flow is already turbulent over the airfoil surface and as Re is increased, the height of the viscous sublayer decreases so that the roughness elements begin to reach beyond the sublayer and

affect the buffer region (and potentially beyond) in the boundary layer. This causes an increase in overall section drag as Reynolds number is increased, until a fully-rough regime is achieved where pressure drag on the surface elements dominates viscous drag. In this case, above a particular Reynolds number no additional changes in the drag coefficient of the surface are observed. This type of behavior is evident in a global sense with the power coefficient measurements of the rotor, which are particularly susceptible to changes in drag coefficient.

Both lift reduction (via changes to the lift-curve slope) and drag augmentation (via transition and/or aerodynamic roughness) could be acting on the rotor surface to varying degrees. Additional numerical and experimental work which carefully probes the near-surface flow condition is required to further understand the relevance of each mechanism. The authors do not suspect that rotational (or so-called 3-D effects) are causing the observed behavior due to the de-coupling of λ and Re_c possible in this work. If λ effects were present, we would expect to see no change as Re_D is altered for a fixed λ (see figure 7 (a)). The results do highlight how sensitive a design can be to the effects of Reynolds number, even for commonly utilized airfoil families at very large values of Re_c .

VII. CONCLUSIONS

This study presents the highest Reynolds number data currently available for a horizontal axis wind turbine in a laboratory setting. The unique conditions were achieved using a wind tunnel that uses highly compressed air as the working fluid. For a rotor with free-transition, Reynolds number effects were clearly seen across a large range of Re_D up to 10 million, when considering the peak power coefficient. These observations are surprising given the relatively large values of Re of this rotor, compared to previous work which examined Reynolds number scaling of performance. It is shown that Reynolds number, and hence scale effects, can alter turbine performance significantly even at relatively large values. Although the exact nature of the trends might be a direct function of the specific rotor geometry and airfoils chosen. However, it is likely that a number of designs may show similar performance trends as this rotor uses an airfoil family which is common in the wind industry. Further work is needed to identify the exact mechanism driving the the observed trends and to explore the large parameter space of geometric effects in detail.

The ability to control tip speed ratio independently from the Reynolds number is leveraged to gain additional insight into scaling of the performance with the blade Reynolds number, Re_c . This has allowed for exploration of Re sensitivity beyond the BEM calculations based on data from individual airfoil sections tested in wind tunnels. With the ability to change model rotational speed accurately, similar to a truly variable speed drive on a full-scale turbine, many different λ were tested for fixed Re_D values. The data could then be re-interpreted in terms of the chord-based Reynolds number which more clearly outlined the scale dependency. For the untripped rotor, a value of $Re_c \geq 3.5 \times 10^6$ was required before Reynolds number invariance was observed in the power coefficient. This cutoff value was independent of the specific Re_D and λ operating point, indicating that the performance scaling of this rotor was not driven by rotational effects but by the Reynolds number of the rotor blade itself. This was further tested by re-normalizing the power curves by the Reynolds number invariant C_p values. In this way the rotational dependence is removed and all curves showed a similar shape. This result has direct implications for modeling and simulation efforts of rotor performance.

Finally, the effect of transition on rotor performance was investigated in detail by adding carefully prescribed tripping devices to the rotor surface in the form of microdots. With these elements in place, low- Re performance augmentation was eliminated; suggesting that whatever mechanism is causing the increase in C_p is related to, or affected by, transition. Future work will investigate this mechanism in additional detail. The results indicate that the boundary layer state is of critical importance to the operation of a turbine, even at relatively high Reynolds numbers.

VIII. ACKNOWLEDGEMENTS

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Appendix A: Appendix: Correction Methodologies

In the processing of the experimental data sets, two specific corrections were made to account for the effects of drivetrain losses inside the gearbox and model blockage in the

tunnel. These corrections were standardized and included in the post-processing of all experimental data sets. The results of section IV and V are therefore the true aerodynamic power produced by the rotor.

1. Gearbox Efficiency Correction

To recover the aerodynamic input power, measured mechanical power from the turbine model was corrected in post-processing to account for drive-train losses. These inefficiencies mainly stem from the constant meshing of gear teeth inside the turbine gearbox, but can also be attributed to frictional losses in the bearings and lubricant. To capture these effects, a bulk efficiency of the drive-train is defined as the ratio of output to input power

$$\varepsilon = \frac{\tau\omega|_{output}}{\tau\omega|_{input}} \quad (\text{A1})$$

where ε is the measured efficiency. Prior to beginning an experimental campaign, ε was measured with a custom-designed test rig located outside of the HRTF wind tunnel facility. Using this setup, shaft loads representative of those undergone by a wind turbine model could be directly applied to the drive-train. The rig itself consists of a 2.24 kW variable-frequency (AC) motor connected to a torque transducer via a flexible coupling. Input torque and rotational speed output from the motor are measured by the first transducer. Next, in place of the model rotor, a second coupling is attached to the input shaft of the tower gearbox. At this point, the measurement stack is the same as that used during an experiment (described in II B). This process involves measuring the output power transferred from the tower to the second torque transducer. Power is then removed via the magnetic hysteresis brake. The main benefit of this setup is that the entire measurement stack as used during an experiment (and as shown in figure 3) is used for measuring ε . The test rig with measurement stack mounted in place is shown in figure 14. Measurements of ε are completed at over 175 different operating points (torque and speed settings) representative of those encountered inside the HRTF. The resulting efficiency map is shown in figure 15. The individual test points for ε are shown as black dots and the contour has been generated to aid in visualizing the dependency of the efficiency on ω and τ . A sharp drop is seen in ε when $\tau_{output} \leq 0.1$ (Nm). This indicates that below some loading threshold the uncertainty in measured efficiency is large due to the steep slope in the efficiency curve. In contrast, very little dependency is

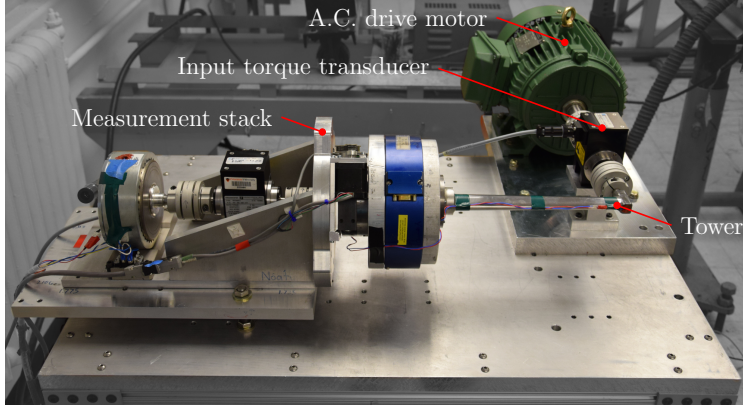


FIG. 14. Test rig shown with measurement stack loaded for efficiency tests.

seen for ω . Only small variations are seen across the range of speeds for a fixed output torque. The exception to this case is when $\omega/2\pi \leq 40$ where less data is available. However, experiments are rarely performed in this regime and so for the bulk of the operating space of the turbine, speed dependence is negligible.

A functional and simple correction methodology was desired so that mapping the measured power to the true aerodynamic power would be a straightforward and repeatable process. Given the results shown in figure 15, a fit of the form $\varepsilon = f(\tau)$ was sought, with errorbars which are proportional to the scatter in ω . A power-law relationship was found to capture the changes in efficiency with torque:

$$\varepsilon = a(\tau_{output})^b + c \quad (\text{A2})$$

where a , b , and c are adjustable constants determined by a best fit of the measured efficiency from the test rig. Since the dependency on ω has been neglected, data was bin-averaged by τ across all speeds in steps of $\Delta\tau = 0.05$ (Nm) over $\tau \in [0.10, 1.2]$. The standard deviation of the resulting bin-averaged value of ε gives an estimate of the error associated with neglecting the speed dependency. The results of this method are shown in figure 16. Above a minimum applied torque (with a small functional dependence on operating speed) the gearbox efficiency exceeded 90%, which compares well to the value of $\varepsilon = 98\%$ found in the literature for right-angle bevel gearboxes [25, 26]. It is interesting to note the sharp drop off in efficiency at low torque values in figure 15, supporting the idea that a gearbox of this type needs some minimum loading in order to operate efficiently.

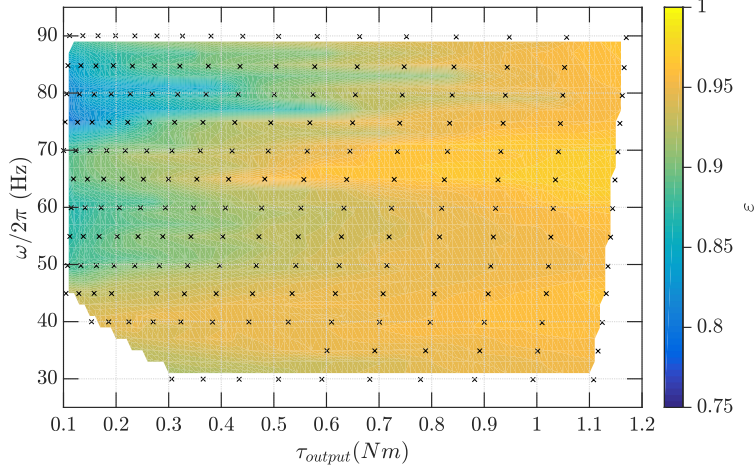


FIG. 15. Efficiency map as measured on the test rig. Black crosses represent individual test points where ε was measured. To aid in visualizing the efficiency and its dependence on both τ and ω , a color contour map was generated from the data at these test points with the magnitude given by the color bar at right.

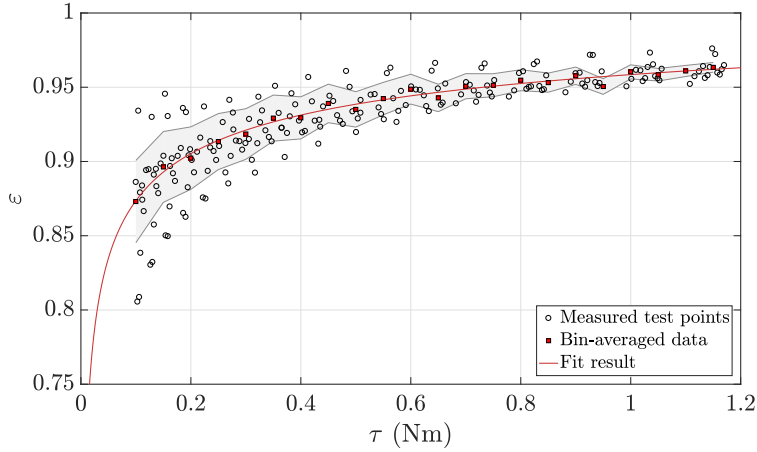


FIG. 16. Measured gearbox efficiency as a function of the input torque only. Also shown are the bin-averaged data and resulting curve fit using equation A2 implemented to correct experimental data.

2. Model Blockage Correction

Flow acceleration due to the presence of a model and constraining walls affects all wind tunnel experiments to a varying degree. For turbine and propeller studies, the method of Glauert [5] is typically used to correct the free-stream velocity (see for example Mikkelsen [27], Bahaj *et al.* [28]). This methodology has been applied to the current experiments by

utilizing the thrust coefficient (as given by the axial force measured at the tower base) and the known geometric blockage of the turbine. An iterative solver is implemented to find the corresponding equivalent free air speed, U . This is the free-stream velocity that gives the same thrust for a corresponding rotor velocity as the model operating in the tunnel and is used in place of the tunnel velocity, U_t for all experimentally determined values.

a. Tower Drag Effects on Blockage

The axial thrust force is recorded by the 6-axis load cell located at the base of the turbine and therefore the reported thrust coefficient values include the axial force generated by the turbine plus drag due to the tower assembly. The magnitude of this effect can be estimated if it is assumed that the rotor thrust and tower drag are linear so that the measured thrust is $F_t = F_{\text{rotor}} + F_{\text{tower}}$, and the thrust coefficient becomes:

$$C_t = \frac{F_{\text{rotor}} + F_{\text{tower}}}{\frac{1}{2}\rho U^2 A_{\text{rotor}}} = C_{t,\text{rotor}} + C_{d,\text{tower}} \frac{A_{\text{tower}}}{A_{\text{rotor}}} \quad (\text{A3})$$

where $C_{d,\text{tower}}$ is the drag coefficient of the tower geometry and A_{tower} is the frontal area of the tower which characterizes this drag. For a cylinder at moderate Reynolds numbers, this drag coefficient could be as large as 0.5 but will decrease as Re of the tower increases. In the case of the HAWT model tower, a more aerodynamic diamond-shaped profile was used. For these experiments, the drag coefficient of the tower was not measured directly as a function of Reynolds numbers, but estimates can be made of their effect using equation A3 and an assumed value for $C_{d,\text{tower}}$. For the total frontal area of the rotor:

$$\frac{A_{\text{tower}}}{A_{\text{rotor}}} = 0.161 \quad (\text{A4})$$

For a worst-case scenario of $C_{d,\text{tower}} = 0.5$, the increase in measured thrust coefficient would be 0.081, or using a more realistic value of $C_{d,\text{tower}} = 0.1$ returns a change in C_t of 0.0161, which is nominally near the sensor resolution. For all of the data reported here, no correction for tower drag was made to any of the reported thrust coefficient values for several reasons. The first is that the specific value of $C_{d,\text{tower}}$ is in reality difficult to separate from the measured $C_{t,\text{rotor}}$ because the two interact in a complicated, and likely non-linear fashion with Reynolds number. The prior discussion also assumed a single velocity scale

determined the tower drag, but a significant portion of the tower is downstream of the rotor, meaning that the resulting drag force could be much less than expected. Therefore any corrections applied to the thrust coefficients for the tower drag would need to make a number of assumptions about the way the drag varies across the tower and with Re . Ideally, an alternative method would be utilized to measure the rotor thrust, but this is not feasible with the current setup.

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