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Influence of interfacial elasticity on liquid entrainment in thin foam films

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Abstract

The influence of interfacial elasticity on the rate of liquid drainage from gas-liquid interfaces is a subject that has encouraged prolific scientific work on coalescence and film stability. Elucidating this relationship is important for the design of surfactant mixtures where the amount of liquid content of the foam is critical for the aesthetics and/or effectiveness of the product. However, contradictory theoretical predictions exist with regard to how surface elasticity may influence thin-film dynamics. In this work, interferometric studies were performed to measure the liquid film entrainment between a bubble and an air-liquid interface in response to systematic variations of the surface elasticity. The surface elasticity was varied by adjusting the age of the interface or by adjusting the bulk concentration of a surface-active molecule known to form highly elastic surface layers. Surprisingly, the results indicate the absence of a strong relationship between the surface shear elasticity and the entrainment of liquid in foam films. In addition, qualitative differences are observed between the shapes of foam films with differences in interfacial shear viscosity, with no net effect on liquid entrainment under the conditions studied.

1. Introduction

Foams are dispersions of gas in liquid and are well-known to the public because of their ubiquity in food beverages, [1, 2, 3] pharmaceuticals, [4, 5, 6, 7] and commercial cleaning products, as well as to industry for their utility in removing organic pollutants from industrial waste streams [8, 9]. Each application requires different foam characteristics that often vary as a function of time [10, 11].

Drainage of liquid from the interstitial spaces of a foam, that is, through thin films, Plateau borders, and nodes, results in the separation of the liquid from the gas phase [12, 13]. Films can thin as the result of gravitationally- and/or capillary-driven flows. The consequent volume and rate of liquid loss from the foam can impact a consumer’s experience with food and beverages, such as the tactile sensation of froth in a freshly poured glass of beer. A foam can also experience a gradual growth of the average bubble size, known as *coarsening*, due to the coalescence of adjacent bubbles or from diffusive mass transfer of gas from small bubbles to large bubbles [14]. Because the present work aims to investigate the *initial* liquid fraction of a newly formed foam, the discussion here will exclude coarsening effects and will primarily focus on drainage processes.

When discussing the rate of drainage of liquid from a foam, one should note that this process is strongly influenced by the presence and composition of surface-active species (surfactants, proteins, polymers, etc.), which facilitate foam formation by lowering the energy required to create excess area. The process of selecting a surfactant for a particular foam should be accompanied by consideration of its physicochemical properties, including its bulk and interfacial diffusivities, adsorption/desorption kinetics at interfaces, pC_{20} value (measure of surfactant efficiency), and micellar structure, as well as its safety, chemical stability, and ecotoxicity profile [15, 16, 17, 18]. The interfacial viscoelasticity conferred by surfactant-adsorbed layers may also affect the stress response to shearing and dilational deformation (expansion/compression) during drainage [19].

The desire to understand how surfactants influence drainage rates and liquid entrainment in foams and emulsions has inspired researchers over many decades. One simple approach used by many groups is to assume that the interface has a range of “mobility” that is restricted by Marangoni stresses that resist surface tension gradients, with the limiting case of “immobile” corresponding to zero tangential velocity [20, 21, 22, 23, 24]. Under this assumption, the dynamics of foam interfaces should be agnostic of surfactant type, provided that enough surfactant is present to immobilize the interface. However, Frostad and coworkers found significant quantitative differences in both foam density and liquid entrainment in individual films for solutions of simple, water-soluble surfactants at concentrations above the critical micelle concentration [18]. Furthermore, data from Bhamla and coworkers show that films bound by viscoelastic interfaces can drain more slowly than what is predicted by the “immobile” limit [25].

46 A more comprehensive approach would therefore include not only consid-
 47 erations of Marangoni stresses but also the effects of structure in the adsorbed
 48 layer. Measurement of the surface rheology is one attempt to account for
 49 these structural effects in terms of liquid-like (viscous) and solid-like (elas-
 50 tic) properties that are believed to arise from intermolecular forces at the
 51 interface. The material properties that describe the viscous and elastic prop-
 52 erties of the surface are defined relative to the deformation applied to the
 53 surface (e.g. dilational and shear) and change dramatically with surfactant
 54 type. For example, under shear deformation, the commonly studied small-
 55 molecule surfactants such as sodium dodecyl sulfate (SDS) exhibit immeasur-
 56 ably small surface shear viscosities (smaller than $0.01 \mu \text{ N s/m}$ (10^{-8} N s/m)
 57 for SDS) [26], while proteins, which are much larger and conformationally
 58 complex, can exhibit significant surface shear viscosities ranging from 10^{-5}
 59 N s/m to 1 N s/m [27, 28, 29], with the values depending on the unfolding
 60 characteristics of the protein and other testing parameters [19].

61 Under dilational deformation, on the other hand, small-molecule surfac-
 62 tants like SDS display a measurable elasticity, though this is merely due to the
 63 the surface-tension gradient effects (also known as the Gibbs-Marangoni ef-
 64 fect) and normally referred to as the Gibb’s elasticity. Alternatively, proteins
 65 such as those studied in this manuscript may have strong intermolecular in-
 66 teractions and exhibit dilational viscosity and elasticity that greatly exceed
 67 the resistance to deformation associated with the Gibb’s-Marangoni effect
 68 [30, 31]. In particular, we aim to study interfaces that are predominantly
 69 elastic as opposed to viscoelastic or purely viscous.

70 Using variations of these two frameworks for modeling interfaces, previous
 71 researchers have attempted to determine the impact that interfacial elasticity
 72 will have on the dynamics in foams and other multiphase systems, sometimes
 73 with contradictory results. Within the construct of the mobility framework,
 74 Zapryanov and coworkers developed a hydrodynamic model for predicting
 75 the time for the thin film between coalescing liquid droplets to drain to a
 76 final thickness. Their model predicts an *increase* in the drainage time with a
 77 decrease in mobility caused by an increase in the Gibbs elasticity, and with
 78 an increase in the sum of dilatational and shear viscosity within a range of
 79 $10^{-6} \text{ Pa}\cdot\text{m}\cdot\text{s}$ to $10^{-3} \text{ Pa}\cdot\text{m}\cdot\text{s}$ [32]. In agreement with this prediction, Tambe
 80 and colleagues numerically calculated the rate of drainage of an axisymmet-
 81 ric, plain-parallel, horizontal film between two droplets that shows decreased
 82 drainage rates with increasing Gibb’s elasticity. They also considered the
 83 effect of increasing the dilatational surface elasticity and total surface vis-

84 cosity using a generalized Maxwell model with a continuous distribution of
85 relaxation times, and predicted that an increase in either the elasticity or
86 viscosity of the surface will increase the thickness of the entrained film at a
87 given reference time [33].

88 In contrast, a recent hydrodynamic model presented by Ramachandran
89 and Leal predicts a *decrease* in the drainage time of a thin film between
90 two vesicles or capsules with an increase in the area expansion modulus of
91 the vesicle membrane [34]. Because the vesicle membrane is modeled as a
92 thin shell, its area expansion modulus can be thought of as analogous to the
93 interfacial elasticity of a two-dimensional fluid interface. This is in contrast
94 again to a previous theoretical study from Biswas and Haydon, which predicts
95 that interfacial elasticity would not have a significant impact on the drainage
96 rate of thin films bounded by viscoelastic interfaces [35].

97 Many experimental studies have also been conducted on viscoelastic inter-
98 faces by examining film stability against coalescence and, to a lesser extent,
99 film drainage and liquid entrainment [36, 37, 38, 39]. Unfortunately, exper-
100 imental work has not yet resolved the contradictory theoretical predictions
101 outlined above. Part of the reason for this is that developing methods to
102 characterize the viscoelasticity of interfaces is still an active area of research
103 [40, 41, 31, 42]. Another reason is that it is difficult to produce interfaces
104 with well-controlled properties.

105 Protein-laden interfaces are often studied because they have been found
106 to produce a wide range of viscoelastic behavior, though it is often time-
107 dependent (usually increasing with time) [43, 44, 19], and may be disrupted
108 by the addition of small-molecule and polymeric surfactants to reduce the
109 viscoelasticity [45, 46]. For example, Van Aken and colleagues found that in-
110 creasing the ratio of low-molecular-weight surfactants to protein β -lactoglobulin
111 increased the rate of emulsion film rupture [37]. Similarly, Blomqvist and col-
112 leagues discovered that adding non-ionic polymeric surfactant F127 signifi-
113 cantly reduced the dilatational and shear elasticity of lactoglobulin solutions
114 and decreased the time for the film to drain to an equilibrium thickness, but
115 did not affect the long-term stability of the residual film due to long-range
116 steric interactions provided by F127 layers [47]. Both studies suggest that
117 increasing viscoelasticity ought to slow film drainage, but were not sufficient
118 to systematically validate prior theoretical predictions.

119 These lingering contradictions in the theoretical models compel our study,
120 which aims to systematically vary the surface elasticity in thin-film drainage
121 experiments. In the present work, the central hypothesis is that the sur-

face elasticity influences the volume of liquid entrained in a thin film and its subsequent drainage. It is important to emphasize that in this study the elasticity arises from intermolecular interactions among surface-active species that either irreversibly adsorb to the interface and impart gel-like characteristics or engage in other strong intermolecular bonding at the surface. Thus, the interfaces will not be directly comparable to small-molecule surfactant solutions where the Gibbs elasticity is the primary source of dilational elasticity. To quantify the entrained volume we utilize an interferometry-based technique that we refer to as a dynamic fluid-film interferometer (DFI). Similar to other instruments of this type, it uses reflectance interferometry to generate 3D representations of foam film profiles [18, 48].

Instruments that use reflectance interferometry to measure the thicknesses of microscopic films are well documented in literature, such as the well-known Scheludko cell (and modernized versions thereof) [49, 50, 51, 52, 53]. The DFI used in this study is an extension of the i-DDrOP apparatus developed previously in our lab [25] and is somewhat similar to the apparatuses used by Sett et al. [54] and Troian et al. [55]. However, it is important to note that the bubble radius in the present work is at least an order of magnitude smaller in size (bubble or solid surface) than in these studies. This point is critical to our analysis since the smaller bubble size favors capillary-pressure-driven drainage over the gravitationally-driven drainage studied previously. Additionally, the DFI used for the present study has the advantage of providing independent control over bubble size, approach velocity, and film size [18].

In this study, we restrict our attention to the drainage of a thin film formed between a bubble and a bulk, air-solution interface. Our work follows recently published work using the same experimental technique, which demonstrated correlations between the volume of liquid entrained in the thin film and the film thinning rates to the densities of freshly formed foams of the same surfactant solutions [18]. This underscores the utility of simple thin-film measurements for studying foam behavior. In this study the elasticity of the interfaces is systematically varied while attempting to hold all other variables constant. We primarily studied bovine serum albumin (BSA) because it is a commonly studied globular protein known to unfold and form interfacial networks with significant elasticity at air-liquid interfaces [56, 44]. To supplement the studies with BSA, we used escin, a monodesmosidic triterpenoid saponin molecule (1 sugar chain with 3 hydrophobic residues) known to form surface layers with significant surface elasticity arising from extensive

hydrogen bonding [57, 58].

2. Methods

2.1. Experimental overview

To modulate the interfacial rheology of the air-liquid interface, we vary the bulk surface-active species concentration or the surface age in separate sets of experiments. The general process is outlined as follows: first, the bulk air-water and bubble interfaces are aged simultaneously under quiescent conditions with the bubble far away from the bulk interface. Then, the distance between the bubble and the bulk interface is decreased until the two surfaces deform and entrain a thin film of liquid. The difference between the aging studies and concentration studies is that the former varies the aging time at constant bulk concentration of the surface-active species, whereas the latter varies the bulk concentration of surface-active species while maintaining a constant aging time.

For this study, the BSA concentration studies were conducted for surfaces aged 40 minutes, and the surface aging studies were conducted at a constant BSA concentration of 0.96 mM. Complementary to the set of BSA experiments, the escin studies utilized only surface aging studies and were completed at a constant escin concentration of 4.4 mM. These concentration and surface aging times were chosen to yield a range of surface elasticity values for comparison in investigating the effect on thin-film properties for the molecules studied.

2.2. Materials

Several batches of lyophilized BSA (MW = 66 kDa) were purchased from Sigma Aldrich (cat. #A7906, CAS: 9048-46-8, $\geq 98\%$ purity). Solutions of 1.5×10^{-3} mM (0.1 mg/mL) to 0.96 mM (64 mg/mL) were made by dissolving measured masses of the lyophilized powder with phosphate-buffered solution (PBS 1x from Corning Cellgro: cat. #21-040-CV) within glass vials before gently stirring the contents with a stir bar for at least an hour. When not in use, the solutions were kept refrigerated at 4°C. All solutions were made with an ionic strength of 0.16 M. The concentration of the solutions was verified using UV-Vis absorption at 280 nm on a NanoDrop instrument and the built-in permittivity constant for BSA.

193 The escin saponin was purchased as a powder from Alfa Aesar (cat.
 194 #J66968, CAS: 6805-41-0, 98% purity, formula weight: 1131.26). The struc-
 195 ture of a saponin is inverted from common surfactants since a saponin molecule
 196 possesses a hydrophobic head called an aglycone linked to one or several
 197 sugar chains by glycoside bonds, which contrasts with the *hydrophilic* head
 198 and *hydrophobic* tail found in a common surfactant. Solutions of escin were
 199 made from powdered escin added to phosphate-buffered solution (PBS 1x
 200 from Corning Cellgro: cat. #21-040-CV) in glass vials. The solutions were
 201 sonicated in a liquid bath for at least half an hour to dissolve the escin.
 202 Afterwards, the solution was filtered through a 0.22 μm and 13 mm diam-
 203 eter Millipore Durapore PVDF membrane filter (cat. # SLGV013SL) to
 204 remove heterogeneous materials, including observed colored insoluble impu-
 205 rities present in the solution, and thus minimize variation in the turbidity of
 206 the solutions. When not in use, the solutions were kept refrigerated at 4°C.
 207 All solutions were made with an ionic strength of 0.16 M .

208 2.3. Pendant drop tensiometry

209 A standard, pendant drop tensiometer method was utilized to measure
 210 the surface tension of the air-liquid interfaces. It is important to note that
 211 while this method is valid for pure liquid-liquid interfaces, previous studies
 212 have found increasing error of the fitted Laplace shape to pendant drops with
 213 increasing surface pressure that is associated with the liquid-solid transition
 214 of the interface [59, 60]. Usually, the solidification is observed by the inter-
 215 facial compression and expansion of the drop. The present measurements
 216 monitor only the *apparent* surface tension changes at a constant volume that
 217 are due to adsorption and conformational changes of surface-active species
 218 at the stationary air-liquid interface. Considering this, we collected the data
 219 with a focus on identifying the relative magnitudes of the apparent surface
 220 tension and trends in the time-evolution at different bulk concentrations.

221 For surface tension measurements, a droplet on the order of 100 μL is
 222 dispensed through a syringe needle of outer diameter 2.413 mm connected
 223 to a 1 mL syringe. In each case, the first two droplets are discarded to purge
 224 the system. A disposable plastic cuvette filled with 1 mL of distilled water
 225 is placed around the pendant drop to maintain a more controlled and hu-
 226 midified environment to mitigate evaporation effects. Back illumination of
 227 the droplet with a source of uniform diffuse lighting produces sharp contrast
 228 at the droplet edges. An Edmund Optics camera with a Nikon F-Bayonet
 229 lens is used to capture images of the droplet which are then analyzed with

an iterative shape-fitting algorithm. For convenience, we report the measurements here as the surface pressure, defined as $\pi = \gamma_0 - \gamma(t)$, in which γ_0 is the surface tension of the pure liquid and $\gamma(t)$ is the dynamic surface tension. In these experiments, the droplet formed from solution already has surface-active species adsorbed at the interface at early times and for this reason the plotted surface pressure appears as finite near $t = 0$. This early time data is not needed for the present experiments in which aging times are on the order of 10's of minutes.

2.4. Bulk viscosity measurements

A standard Cannon-Fenske glass viscometer of size 50 was utilized to measure the kinematic viscosities of the solutions. The viscometer constant for the specific viscometer was verified with the measured efflux time of water and its known viscosity at a specified temperature. Before use, the viscometer is rinsed several times with distilled water and ethanol before it is dried by flowing air through the glassware. Then, prior to filling, the viscometer walls are primed with several milliliters of the sample. A consistent volume of 5 mL of solution was used for each measurement and the fluid was assumed to be Newtonian.

2.5. Interfacial rheology measurements

We characterized the interfacial shear rheology of the interfacial protein layers with an AR-G2 rheometer (TA Instruments, New Castle, DE) and a Du Noüy ring attachment made of platinum/iridium wire (CSC Scientific, Fairfax, VA, catalog #70542000) of an inner diameter of 0.46 inches and an outer diameter of 0.5 inches [61]. Before each experiment, the Du Noüy ring is flame-cleaned to remove any organic residues.

A Teflon trough was constructed to hold the solution, with a 0.5 mm step size at the outer Teflon wall such that the radius of the outer wall with the step is 1.04 inches. The trough is filled with about 4.5 mL of solution such that the liquid level reaches the step and the air-liquid interface is pinned. After each experiment, the Teflon trough is cleaned by rinsing with both water and ethanol, scrubbed with Q-tips, and allowed to air dry before the next use.

For all aging and bulk concentration experiments, the Peltier plate is kept at 25°C. The rheological characterization experiments performed in this study monitored the interfacial rheology over time with oscillatory shear measurements. After an initial equilibration time of 1 minute, the interface

266 was periodically sheared at an angular frequency of 0.5 rad/s and 1% strain.
 267 We found that rheological experiments at other frequencies exhibit similar
 268 qualitative trends. Additionally, strain sweeps performed on BSA-adsorbed
 269 interfaces indicated that the utilized 1% strain was within the linear vis-
 270 coelastic regime. In comparison, the interfacial shear rheology of escin was
 271 conducted at a lower strain of 0.1% for the deformation response to remain
 272 within the linear viscoelastic regime.

273 Interfacial dilational rheology measurements were not performed in this
 274 study due to the inherent difficulty in obtaining systematic measurements
 275 for this system. Nevertheless, we make the assumption that the intermolec-
 276 ular interactions that result in high shear elasticity will also result in a high
 277 dilational elasticity as well. This assumption is based on the theoretical pre-
 278 diction that, for predominantly elastic interfaces, the dilational modulus will
 279 be proportional to the shear modulus, which has in fact observed in experi-
 280 ments for other globular protein solutions [35, 27, 44, 19, 29, 62]. Note that
 281 this is only expected to be the case for our BSA solutions, and will not nec-
 282 essarily hold for the escin solutions or other viscoelastic interfaces in general
 283 (such as phospholipid bilayers). Finally, because we are varying the interfa-
 284 cial rheology without changing the molecular composition, we expect other
 285 factors that may influence interfacial rheology to be constant.

286 2.6. *Dynamic fluid-film interferometer (DFI)*

287 The DFI is an apparatus that can be used to characterize thin-film prop-
 288 erties premised upon the interference of light reflected from boundaries of
 289 a thin liquid film. As shown in Figure 1a, the DFI consists of a syringe
 290 pump (Harvard Apparatus Pump 11 Elite cat. #HA1100W) fitted with a
 291 gas-tight 100 μ L syringe (Hamilton cat. #1710CX) that forms the bubble in
 292 a custom-machined Delrin chamber with a 6 mL capacity that is open to the
 293 atmosphere. Narrow gas-tight plumbing (tubing: IDEX PEEK 1/16" OD x
 294 0.030" ID cat. #1533L) conveys air from the syringe to the 16G blunt-tipped
 295 capillary needle (1.194 mm I.D.; 1.651mm O.D.) that forms the bubble in
 296 the chamber. A motor (Newport cat. #TRA12PPD/cat. #SMC100PP)
 297 attached to the solution chamber moves up or down to change the rela-
 298 tive distance between the bubble and interface, and a pressure transducer
 299 (Omegadyne cat. #PX409-10WGUSBH) provides the option of measuring
 300 the pressure within the bubble. Two orthogonally positioned cameras provide
 301 imaging of the top-view (Imaging Development Systems cat. #UI-3060CPC)
 302 and side-view (ThorLabs cat. #DCU223) of the chamber. Illumination from

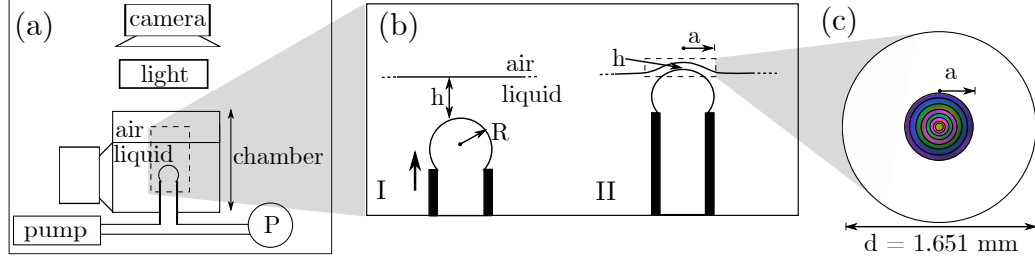


Figure 1: (a) Overview of the DFI used for thin-film measurements: two cameras, a light source, a syringe pump, a pressure transducer (labeled as P), and a chamber capable of vertical translational motion. (b) Diagram of the process for a typical thin-film experiment: (I) Initially, the bubble and bulk air-solution interface are stationary and separated. (II) The interfaces are brought into contact resulting in deformation of the two interfaces that traps a thin film of liquid. The term a denotes film radius, R the bubble radius, and h the film thickness (on the order of $0.1 - 1 \mu\text{m}$). Frame (c) provides a to-scale top view of the interferometry patterns that arise from liquid entrainment in the thin film. The term d denotes the capillary outer diameter.

303 a light source (CCS Inc. cat. #LAV-80SW2) that induces reflection interfer-
 304 ence is conditioned with a dichroic filter (Edmund Optics cat. #87245) with
 305 pass bands at 457 nm, 530 nm, and 628 nm. The equipment is operated via
 306 a custom-written MATLAB script.

307 2.6.1. Protocol for a typical DFI experiment

308 The general operation of the DFI is shown in Figure 1b. The experiments
 309 are performed by adding approximately 5 mL of solution to the Delrin cham-
 310 ber. A bubble of approximately $1.10 \mu\text{L}$ is formed at the tip of the capillary,
 311 which is submerged in the solution. At this point the bubble is positioned a
 312 distance of one bubble radius below the upper air-liquid surface via transla-
 313 tion of the chamber and then aged as needed for the particular experiment.
 314 After aging is complete, the pressure inside the bubble is monitored for 10
 315 seconds to ensure that the bubble volume is stable against environmental
 316 disturbances. The chamber is then moved down at a speed of $150 \mu\text{m s}^{-1}$
 317 for all experiments, causing the bubble and bulk surface to interact. The
 318 chamber is moved instead of the capillary to ensure that the bubble is a
 319 fixed distance away from the camera lens and remains in focus. During the
 320 approach of the bubble and top surface, hydrodynamic and capillary forces
 321 cause the deflection of the upper surface and compression of the bubble that
 322 results in the entrainment of a liquid film between the surfaces. The forma-

tion of the thin liquid film gives rise to the interferometry patterns shown in Figure 1c.

2.6.2. Drainage of thin films

After the initial formation of a liquid film between the surfaces, the radius of the film continues to expand as the bubble compresses into the interface, continuing until the motion of the chamber is stopped. In contrast, the mean and maximum thicknesses of the film are observed to decrease monotonically with time. As a consequence of the simultaneous increase in film radius and decrease in film thickness, the volume of the liquid film increases with time to reach a maximum value after the formation of the initial film. If we assume that the liquid film is cylindrical in shape, the volume can be simply written as $V = \pi a^2 h_m$, where V is the film volume, a is the radial extent of the film, and h_m is the mean film thickness. The rate of change in volume, or the film thinning rate dV/dt , can then be written as:

$$\frac{dV}{dt} = \pi a^2 \frac{dh_m}{dt} + 2\pi a h_m \frac{da}{dt}.$$

The time at which the maximum volume occurs depends on the balance of the two terms on the right-hand side of the equation. The first term describes the drainage of the film, which in these experiments is always negative. In comparison, the second term, which describes fluid capture due to the expansion of the film, is initially positive at early experiment times and then zero after the chamber stops moving. For relatively small elevation velocities, the expansion of the film is small, and the volume maximum occurs while the film is still expanding [18]. In these experiments, the elevation velocity of the chamber is sufficiently high that the maximum in the volume always occurs exactly when the film stops expanding, which is convenient for analysis. Because changes in normal-stress and tangential-stress boundary conditions impact the drainage dynamics, this technique affords a convenient way to quantify the effect of changing the interfacial elasticity on the drainage process.

2.6.3. Analysis of reflectance interferometry data

The interference data recorded as videos during thin-film experiments are converted to film thicknesses with the “Color Analyzer” software (version 2.3.1.1) written with Python and Qt [18]. The software first generates a color map unique to the system’s hardware configuration and film material.

Then, a graphical user interface is used to process individual video frames. To analyze an individual video frame, the user manually selects a color on the colormap and matches it to pixels along each distinct region of color in the interference pattern. Linear interpolation of user-selected points is used to create a 3D projection of the film onto a planar surface. On average, the manual matching process results in an estimated error of about ± 15 nm, though it can be slightly lower or higher depending on the user's ability to discriminate colors [18].

To quantify liquid entrainment, a single video frame from each experiment was analyzed for the period while the thin film is still expanding when it reached a radius of 112 ± 1 μm . Trends in mean film thickness are used for comparing the effects of the different experimental conditions because they change in a similar manner as trends in the film volume, yet are less sensitive to small variations in film radius. Measurements of mean film thickness are calculated as the spatial average of the film thickness over the film region and the reported error bars represent a standard deviation based on at least two replicates at each condition.

3. Results of BSA studies

3.1. Interfacial properties of BSA

Figure 2 shows a time-sweep plot of the surface pressure for several BSA concentrations. It is accompanied by Figure 3, which shows time-sweep plots of the surface shear elastic and viscous moduli for several BSA concentrations. Both figures indicate that the surface properties evolve more rapidly at initial times before approaching approximately constant values at longer times. Both figures also show that increasing concentration results in systematic increases in surface pressure, elastic modulus, and viscous modulus. We assume that the transition from a rapid change in surface pressure to a slower increase over long periods of time indicates that adsorption of BSA is completed and further changes are due to structural changes in the protein and/or protein network. Therefore, we assume that effects due to adsorption kinetics can be avoided by aging the interface for at least 5 minutes.

Examination of Figure 3 reveals a wide spread in the value of the surface shear moduli across concentrations and aging time, with values on the order of 10 mN/m for G'_s and 1 mN/m for G''_s . For the first 50 minutes, the elastic modulus and viscous modulus of interfaces at higher bulk BSA

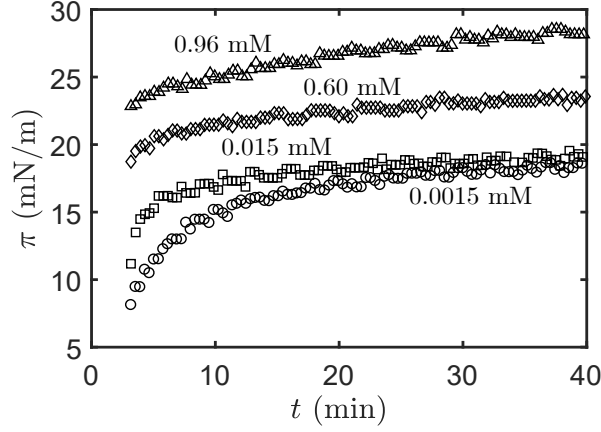


Figure 2: The plot shows representative dynamic air-solution surface pressure behavior for a range of bulk BSA concentrations (1.5×10^{-3} mM [0.1 mg/mL], 1.5×10^{-2} mM [1 mg/mL], 0.60 mM [40 mg/mL], and 0.96 mM [64 mg/mL], respectively).

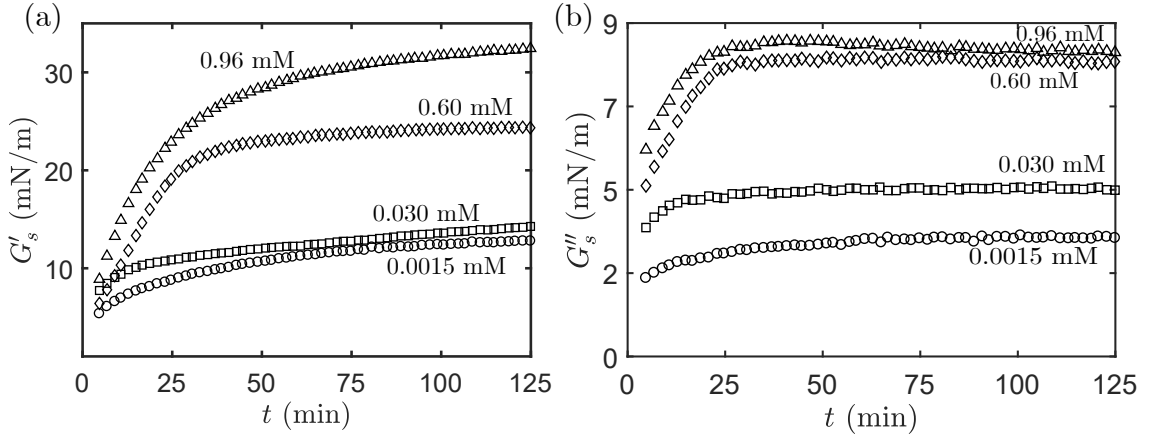


Figure 3: Time (t) sweep of the interfacial shear elastic modulus ((a): elastic modulus G'_s , (b): viscous modulus G''_s) for several bulk concentrations of BSA. Subsequent figures will compare the trends in interfacial shear rheology at either a surface aging time of 40 minutes for concentration-dependent studies, or at a bulk BSA concentration of 0.96 mM for surface aging-dependent studies.

391 concentrations exhibit the greatest increase among the investigated concen-
392 trations. At longer times, the elastic modulus shows more modest growth,
393 and the viscous modulus approaches a constant value. In general, the BSA-
394 adsorbed interfaces are predominantly elastic, and the elastic modulus is 3 -

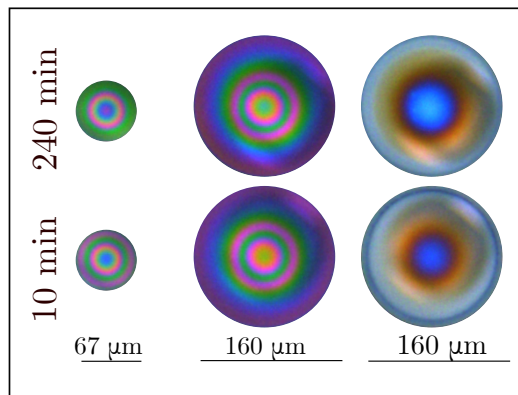


Figure 4: The effect of aging on the film drainage for 0.96 mM BSA films. Left to right, the interferometry patterns are shown at three representative timepoints: 1.46 seconds before the chamber stops moving, the time at which the chamber stops moving (corresponding to maximum film volume), and 59.9 seconds after the chamber stops. The bottom row corresponds to air-solution surfaces aged for 10 minutes, whereas the top row corresponds to surfaces aged for 240 minutes. Note the axisymmetry in film shape.

4 times larger than the viscous modulus in most cases. Because the rheology of the interfaces is sensitive to changes in both bulk concentration and to surface aging time, either parameter can be used to tune the elasticity of the interface.

3.2. BSA film properties

Next, we examine results from the thin-film experiments. Qualitatively, Figure 4 shows that BSA films exhibit axi-symmetric shapes starting from initial film formation and throughout film drainage for all studied surface-aging times. Notably, there is an absence of asymmetric surface flows driven by Marangoni stresses across all investigated concentrations, which is consistent with the relatively high elasticity measured for these BSA-adsorbed surfaces. The absence of surface mobility is also consistent with Koehler and coworkers' observations of approximately zero surface velocities for protein surfactants at aqueous foam surfaces [63].

Figure 5(a) shows that the mean film thickness (taken at the same point in time during the drainage process) exhibits a modest increase with increasing bulk BSA concentration for a fixed surface aging time of 40 minutes. The lowest concentration in the plot is 1.5×10^{-3} mM (rather than zero) and the mean film thickness increases by about 150 nm as the bulk concentration is

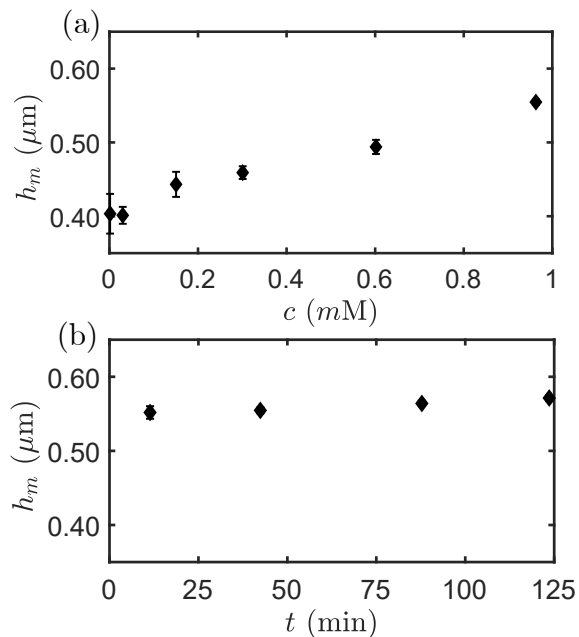


Figure 5: (a) Mean film thickness h_m as a function of bulk BSA concentration c at a surface aging time of $t = 40$ min, with a lower concentration limit of 0.0015 mM; (b) Mean film thickness h_m as a function of surface aging time t at a bulk BSA concentration c of 0.96 mM.

414 increased from the lowest concentration to 0.96 mM. Compared to the effect
 415 of increasing bulk concentration, the effect of increasing surface aging time
 416 results in a smaller increase in mean film thickness, about 20 nm, over the
 417 range of investigated aging times at 0.96 mM BSA, shown in Figure 5(b).

418 The changes in film thickness can now be compared to the interfacial
 419 elasticity. To accomplish this, both sets of data are normalized by their
 420 respective “initial” values at the lowest bulk concentration (Figure 6) and
 421 at the shortest aging time (Figure 7). In Figure 6, we observe that the
 422 surface shear elastic and viscous moduli increase strongly as a function of
 423 concentration, and each increases to about 3 times the initial values over the
 424 concentration range. The trends in the surface pressure, bulk viscosity, and
 425 mean film thickness reveal that each of the three quantities increase to ap-
 426 proximately 1.5 times their initial values over the same concentration range.
 427 Overall these results show a positive correlation between the bulk concen-
 428 tration and the surface characteristics. However, since the film thickness is
 429 expected to be influenced by bulk viscosity and surface pressure as well as

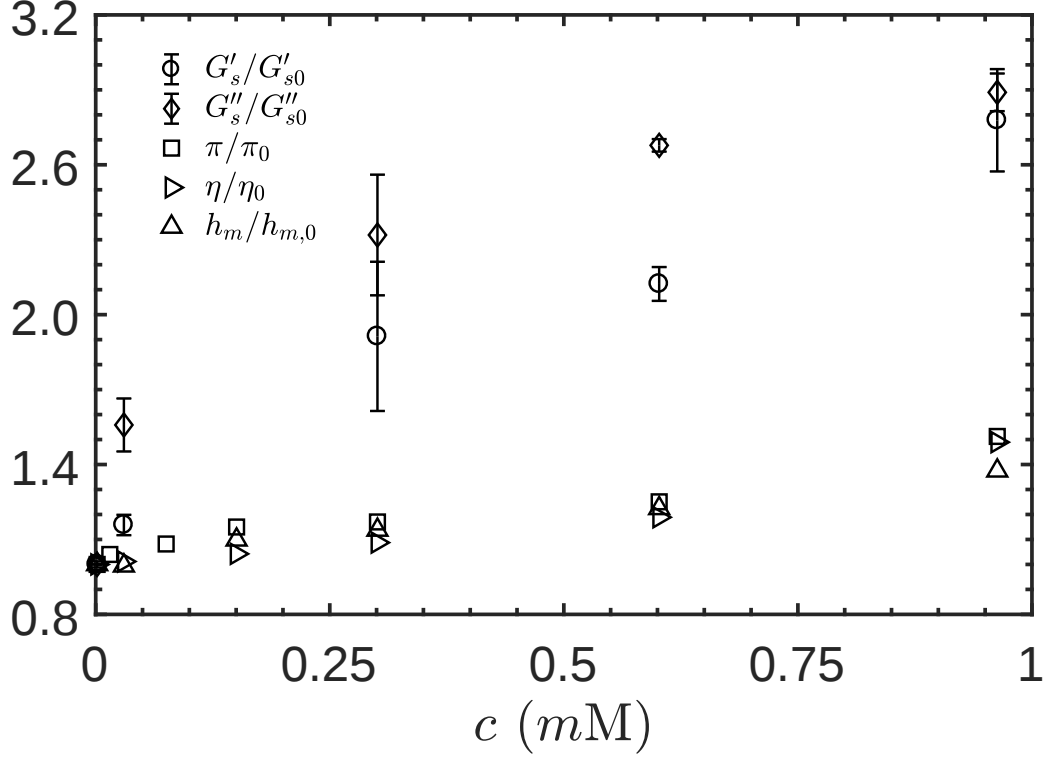


Figure 6: The plot shows the concentration dependence of interfacial and bulk properties in BSA solutions normalized by initial values at 1.5×10^{-3} mM. The circles and diamonds correspond to the normalized surface shear elastic G'_s and shear viscous modulus G''_s , respectively. Squares, right-facing triangles, and upward-facing triangles correspond to normalized surface pressure π , normalized bulk viscosity η , and normalized mean thickness h_m , respectively.

the interfacial rheology, these results alone are insufficient to determine the relationship between film thickness and interfacial elasticity. In contrast, the data from the experiments with surface aging at a fixed concentration have the same bulk viscosity and can be used to help clarify the dependence.

Figure 7 shows the normalized surface elastic and viscous moduli along with the mean film thickness and surface pressure. The bulk viscosity is not shown because its value is independent of time. By comparing this data to Figure 6, we see that the bulk viscosity appears to be primarily responsible for the observed increase in film thickness with increasing concentration. This is not unexpected since we know from lubrication theory that the thinning

440 rate of a film (for rigid surfaces) is inversely proportional to bulk viscosity
 441 [64].

442 We also see that a large increase in surface elasticity with aging time and
 443 with a relatively constant surface viscous modulus and surface pressure is
 444 accompanied by only a tiny increase in mean film thickness. This suggests
 445 that the liquid entrained in foam films is in fact only very weakly correlated
 446 to surface elasticity. This result is not very intuitive for three reasons. First,
 447 according to the prevailing thinking in terms of interfacial mobility, most
 448 theoretical studies cited in the introduction anticipated the increased elas-
 449 ticity to be accompanied by a decreased mobility and hence slower drainage
 450 and a thicker film. Second, one would expect instead that a higher interfacial
 451 shear elasticity for a predominantly elastic interface would result in a higher
 452 dilational elasticity (though there may be exceptions to this), which would
 453 effectively increase the capillary pressure in the film due to the increased
 454 resistance to dilational deformation and speed up the rate of drainage [34].
 455 Third, experimental results have suggested that increasing the value of the
 456 *Gibb's elasticity* results in significant increases in entrained liquid in foam
 457 films under gravitational drainage [54].

458 Although our findings appear to refute the majority of theoretical predic-
 459 tions, one theoretical prediction by Biswas and Haydon [35] does predict a
 460 negligible dependence on elasticity in film drainage, with a stronger depen-
 461 dence on surface viscosity. However, their model is based on thin shell theory
 462 for a viscoelastic sheet as a model for the interface (the interface is referred
 463 to as the “film” in that paper) and does not include the hydrodynamics of
 464 drainage within the thin film. Because of this, it is difficult to use their
 465 analysis to point to a qualitative mechanism that might explain the present
 466 findings, but their analysis may inspire future theoretical developments.

467 3.3. Drainage behavior of aged BSA surfaces

468 While the mean film thickness at the maximum film volume captures the
 469 aggregate influence of the hydrodynamic boundary conditions into a single
 470 measurement and is therefore useful for comparison, it does not tell the whole
 471 story. Another important metric is how the film thins as a function of time.
 472 Figure 8 compares the film volume over time for BSA surfaces with low (at 10
 473 min aging) and high (at 240 min aging) surface shear elasticities. The initial
 474 time $t_d=0$ corresponds to when the film reaches its maximum volume, which
 475 in this case corresponds to when the chamber stops moving. Each pair of the
 476 interferometric patterns (inset in the figure) corresponds to a different time

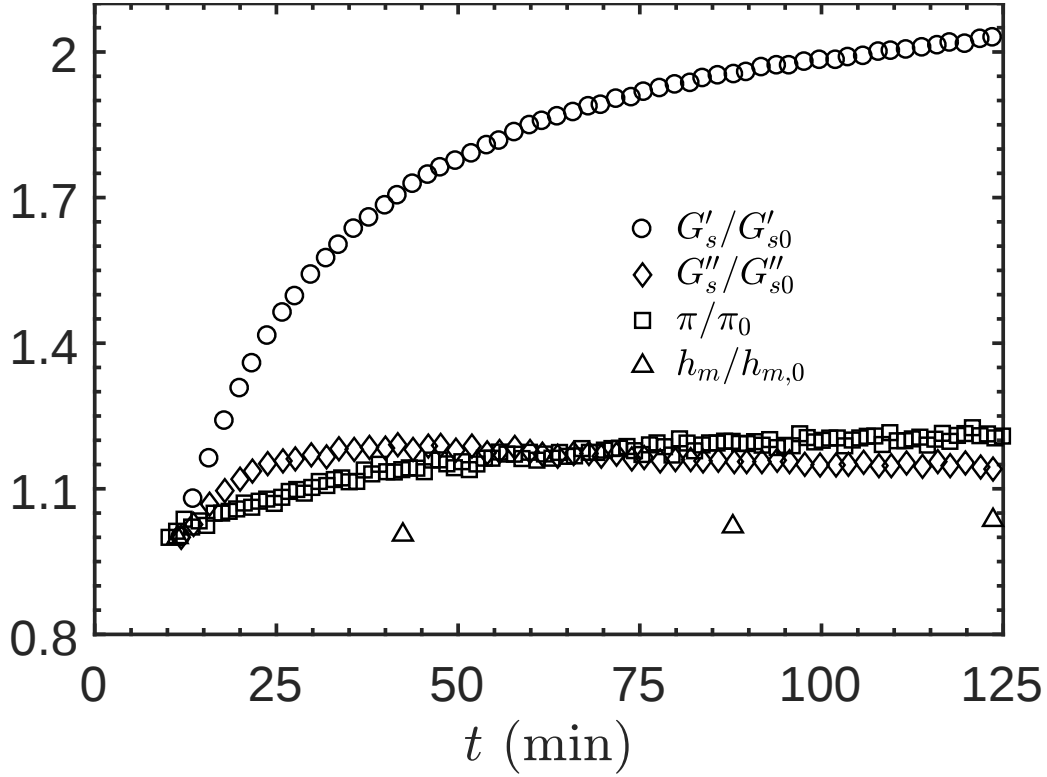


Figure 7: The plot shows the temporal behavior for several interfacial parameters and the mean film thickness in a solution of 0.96 mM [64 mg/mL] BSA, with the data normalized by initial values at 10 minutes aging time. The circles and diamonds denote the normalized surface shear elastic G'_s and shear viscous modulus G''_s , respectively. Squares correspond to the normalized surface pressure π , and the upward-facing triangles correspond to the normalized mean thickness h_m .

point in the film drainage process. Comparison of the volume curves and the interference patterns at initial, intermediate, and long drainage times shows only modest differences in the maximum amount of entrained liquid and in the rate of film drainage. The one notable difference observed is a dip in volume at around 40 seconds for the 10-min-aged surfaces; however, this was found to be the result of a fluctuation in the bubble size due to a pressure fluctuation in the laboratory air-handling system.

Another way of understanding the drainage of the film is to examine the film thickness as a function of time. Many researchers have investigated this relationship, resulting in a variety of differing predictions for the minimum

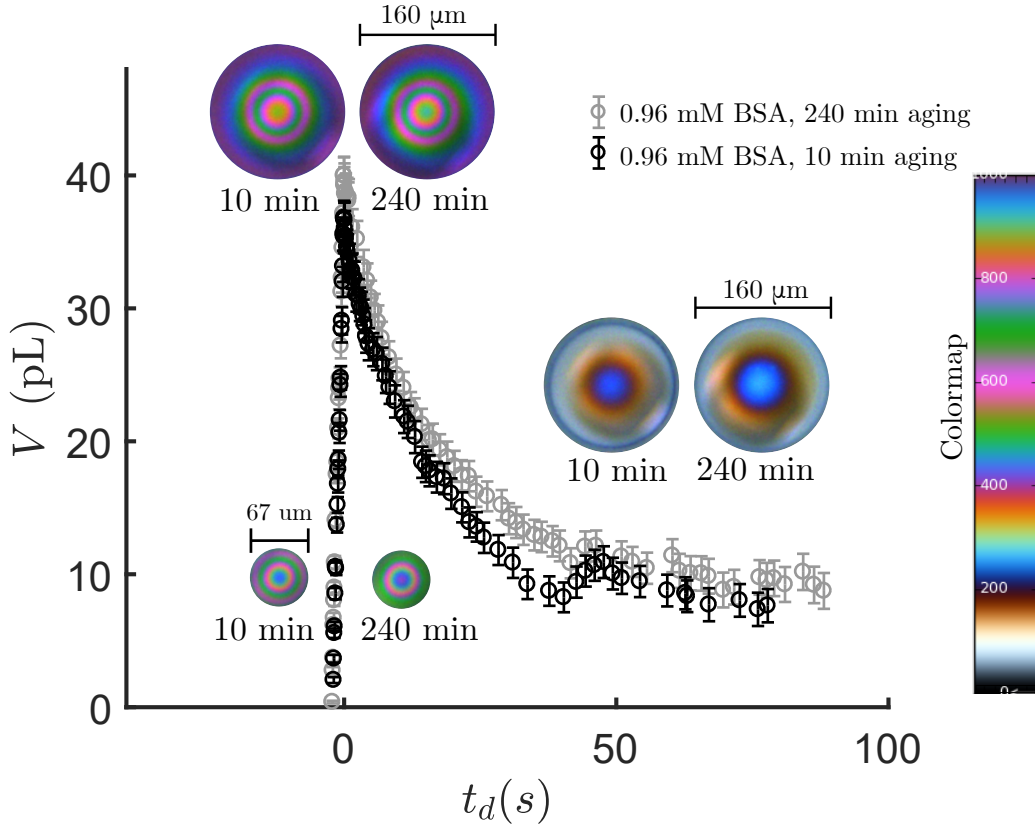


Figure 8: Film volume V as a function of thin-film drainage time t_d for 0.96 mM BSA surfaces aged for 10 min ($G' = 14$ mN/m, black circles) and for in 240 min ($G' = 33$ mN/m, gray circles) prior to film formation. Note that the time-axis is shifted such that $t_d = 0$ corresponds to the occurrence of the maximum film volume, which in this case also corresponds to the time at which the chamber stops moving. Accompanying the volume curves are three pairs of interferometry patterns corresponding to approximately $t_d = -1.46$ s, 0 s, and 59.9 s. Each pair compares the interferometry patterns for a film aged briefly (left) and for a prolonged period (right).

487 film thickness as a function of time [65, 55, 54, 66]. Figure 9 shows the
 488 maximum, mean, and minimum film thickness for the same data as in Fig-
 489 ure 8 along with a few examples of the predicted scaling relations from the
 490 literature (for the assumption of “immobile” interfaces) [67, 68]. Unfortu-
 491 nately, the uncertainty in the data for the minimum film thickness is too
 492 large to make a confident statement about the experimental drainage rate,
 493 but two sample power-law predictions ($h_{min} \sim t^{-1/2}$ and $h_{min} \sim t^{-2/3}$ [67])

are shown for comparison anyway. On the other hand, the maximum and mean film thicknesses appear to approach power-law behavior at long times (with slopes of approximately -0.55 and -0.62, respectively), but when compared to a prediction for maximum thickness ($h_{max} \sim t^{-1/4}$ [68]) the data clearly do not match well. As with the volume entrained, there is very little difference in the maximum, mean, and minimum film thickness for the two different aging times. This further supports the observation that changes in surface elasticity have little impact on the film drainage process under these conditions.

Other researchers have made similar experimental measurements of film thickness versus time [69, 70, 23, 54, 53]. However, the present results are not expected to be directly comparable because of significant differences in the interfacial rheology of the systems studied and/or significant differences in the length scale and driving force for drainage (e.g. gravity vs. capillarity) of the film. Indeed, even if one compares the results of two studies like Bhamla and colleagues (drainage from a film on a solid sphere) and of Sett and colleagues (drainage from a bubble), in which the length scales of the film curvature are the same, one sees different drainage behavior ($t^{-\frac{1}{2}}$ vs. t^{-1}). These differences underscore the need for additional research in this area.

4. Results of escin studies

The preceding section examined the use of BSA to modulate and measure the impact of interfacial elasticity on film drainage. In this section, another surface-active species, escin, will be used to help determine if the findings are unique to BSA. To avoid changing the bulk viscosity, only surface aging will be used to vary the interfacial elasticity of an escin solution with a concentration of 4.4 mM. We selected escin to study alongside BSA because other researchers reported that it can form predominantly elastic layers at air-water interfaces [58]. Unfortunately, our measurements show that the escin used in this study does not form predominantly elastic interfaces (see next section), presumably due to the natural variability of escin and purity differences between suppliers. Nevertheless, the results show interesting trends.

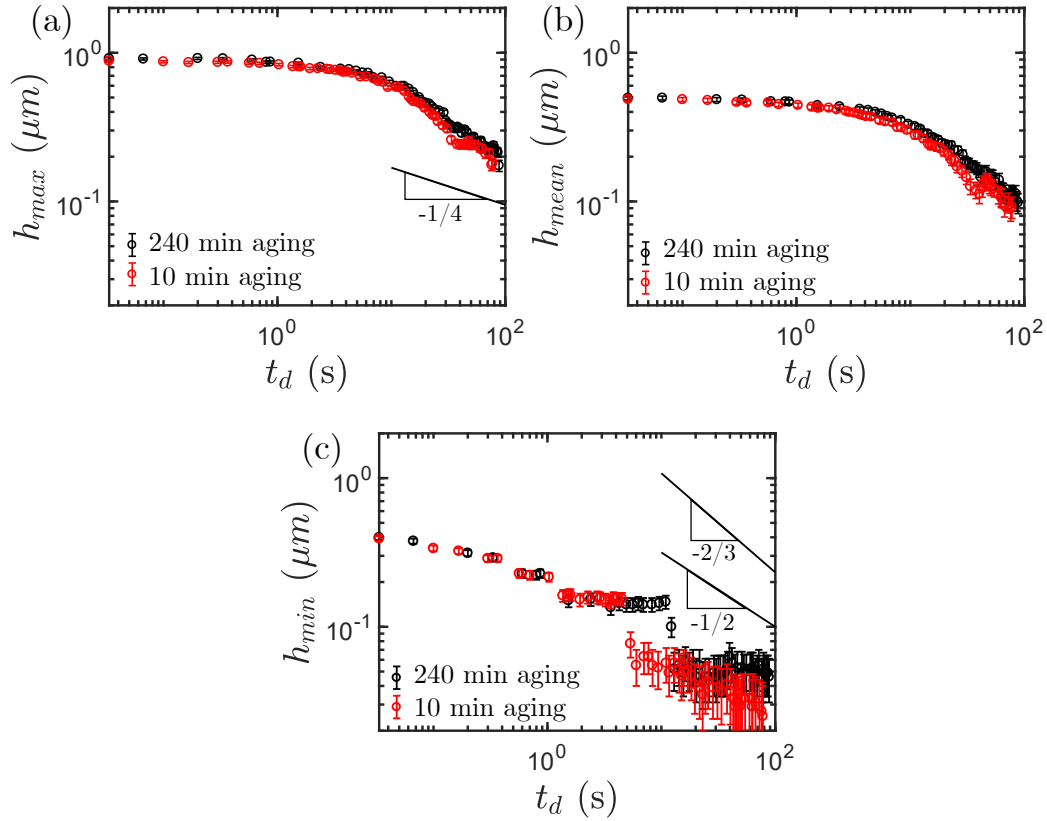


Figure 9: (a) Maximum film thickness h_{max} , (b) mean film thickness h_{mean} , and (c) minimum film thickness h_{min} as a function of thin-film drainage time t_d for BSA surfaces aged for short (10 min, red circles) and long (240 min, black circles) times before film formation. Note that the time-axis is shifted such that $t_d = 0$ corresponds to the occurrence of the maximum film volume.

4.1. Escin film properties

Figure 10 shows that, as with BSA, both the interfacial shear rheology and surface pressure increase with time. The surface pressure, shown in Figure 10(b), exhibits an initial increase with time before saturating at a constant value within about 10 minutes. In contrast to BSA, the escin surface layers exhibit interfacial shear viscous moduli that are on the same order as the interfacial shear elastic moduli over the examined aging times, indicating a viscoelastic, rather than a predominantly elastic film. Nevertheless, the shear elasticity values for escin range from near zero (below the resolution of the instrument) to 50 mN/m, which one might expect to span the range from

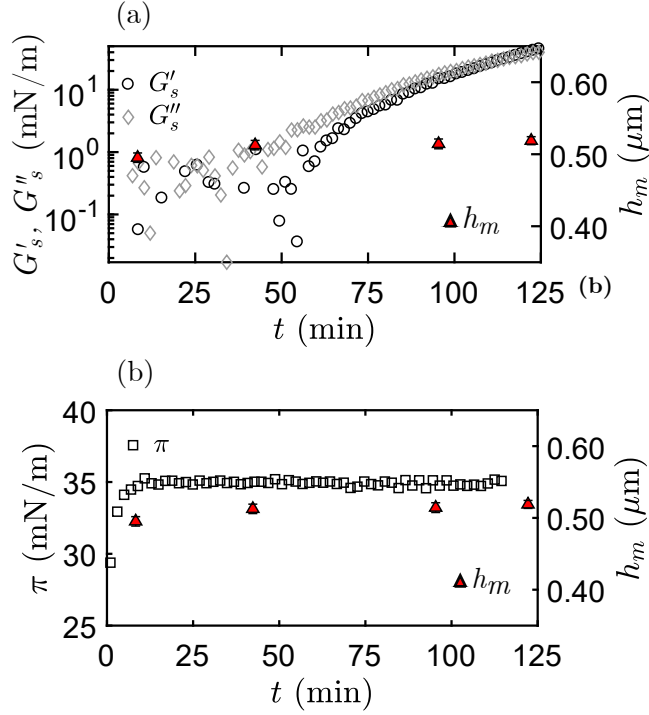


Figure 10: (a) Comparison of the surface shear elastic modulus G'_s and the surface shear viscous modulus G''_s (left y-axis) with the mean film thickness (right y-axis) for 4.4 mM escin. (b) Comparison of dynamic surface pressure π (left y-axis) with mean film thickness h_m (right y-axis) for 4.4 mM escin.

537 “low tangential mobility” to “high tangential mobility”.

538 Interestingly, even over this very large range of interfacial shear moduli,
 539 the mean film thicknesses as shown in Figure 10(a-b) changes negligibly.
 540 This trend is consistent with the changes in mean film thickness observed
 541 with BSA films, but in this case is even more significant because at the
 542 shortest aging time the magnitudes of the elastic and viscous moduli are
 543 below the resolution of the rheometer. At present, we prefer not to attempt
 544 to provide a rationalization for this observation as this would be a worthy
 545 topic for future research; however, we may at least conclude that these data
 546 do not contradict the findings for BSA in which interfacial elasticity shows
 547 an extremely weak influence on entrainment of liquid in foam films of this

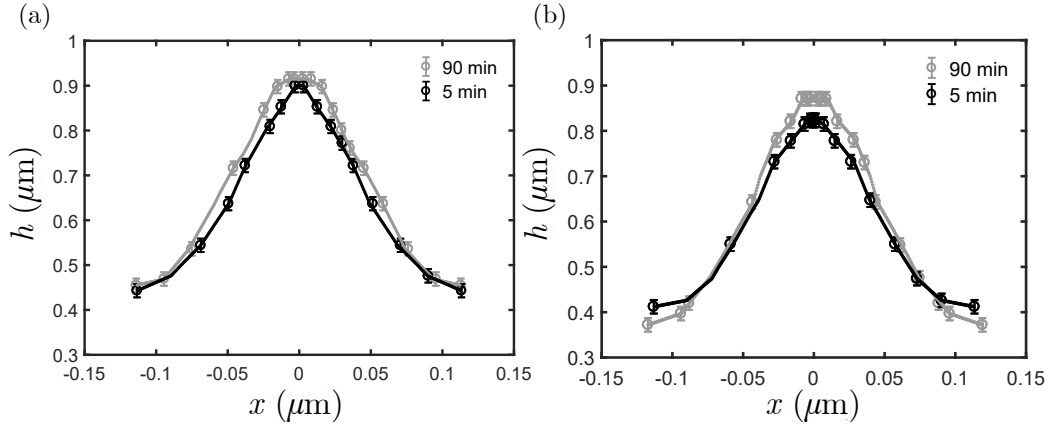


Figure 11: Comparison of film contours arising from 5-min (black) and 90-min (gray) aged surfaces for (a) 0.96 mM BSA and (b) 4.4 mM escin. The outermost points in the figures demarcate the edge of the film as observed in the interference patterns. The circles represent user-selected points, connected by lines of interpolated points.

type.

4.2. BSA and escin film shape

Apart from the mean film thickness and film volume, our experimental apparatus also enables us to examine the film shape. Because of the axisymmetric character of these films we can look at the cross-sectional profile as shown in Figure 11. Note that for these plots, the outermost points shown in each contour demarcate the boundary of the film beyond which the film thickens too rapidly with increasing radial position to be resolved by the camera.

For films of 0.96 mM BSA, we see a marginal thickening throughout the film that is more pronounced within the central region of the film (the dimple) as surface aging is increased. On the other hand, films of 4.4 mM escin show a more noticeable change in shape with increasing surface age, consisting of an increase in thickness in the center along with a thinning at the outer edge of the film. This suggests that even though the films show very little change in mean film thickness, the viscoelastic nature of the escin films produces qualitatively different drainage dynamics than the predominantly elastic BSA films. This observation underscores the importance of accounting separately for viscous and elastic contributions to the mechanical behavior of the interface. This also strengthens the finding that surface elasticity has a

negligible impact on thin film drainage dynamics relative to other properties.

5. Conclusion

The goal of this work is to experimentally quantify how interfacial elasticity influences the rate of liquid drainage from films between gas-liquid interfaces, and consequently, affects the density of freshly formed foams. Elucidating this relationship is important for the design of surfactant mixtures that achieve specific foam properties, especially in applications such as beer foam, medicated foams, and cosmetic foams, where the initial liquid density of the foam is critical for the aesthetics and/or effectiveness of the product.

The thin-film and surface characterization experiments performed in this study show only a very small correlation between surface shear elasticity and liquid entrainment in a freshly-formed thin film of BSA and escin solutions. Not only did we observe minimal change in the mean film thickness with large increases in the interfacial shear elasticity, but also we found minimal differences in time-dependent drainage behavior between fresh BSA surfaces (less elastic) and aged (more elastic) surfaces.

It was not possible to isolate the effect of surface elasticity for both BSA and escin because escin exhibited significant viscoelasticity in contrast to the predominantly elastic BSA surfaces. However, comparing the two systems led us to observe qualitative differences in the shape of the film between BSA and escin at comparable levels of surface elasticity that are masked in integrated metrics such as mean film thickness or film volume.

In conclusion, we find that use of surface-active species which form highly elastic surface layers will not necessarily result in films with greater initial liquid entrainment or slower film drainage as predicted by prior theoretical studies. Questions persist, and these findings motivate the need for further research, both experimentally and theoretically, to parse out the specific role of surface elasticity in dictating interfacial dynamics. It also highlights the usefulness of interferometry in probing thin-film dynamics.

- [1] A.D. Rudin. Measurement of the Foam Stability of Beers. *Journal of the Institute of Brewing*, 63(6):506–509, 1957.
- [2] Juan M. Rodríguez Patino, Cecilio Carrera Sánchez, and Ma Rosario Rodríguez Niño. Implications of interfacial characteristics of food foaming agents in foam formulations. *Advances in Colloid and Interface Science*, 140(2):95–113, 2008.

- 603 [3] G.M. Campbell. *Aerated Foods*. Elsevier Ltd., 1 edition, 2016.
- 604 [4] Dov Tamarkin, Doron Friedman, and Avner Shemer. Emollient foam
605 in topical drug delivery. *Expert opinion on drug delivery*, 3(6):799–807,
606 2006.
- 607 [5] Tim Kealy, Alby Abram, Barry Hunt, and Richard Buchta. The rheo-
608 logical properties of pharmaceutical foam: Implications for use. *Inter-
609 national Journal of Pharmaceutics*, 355(1-2):67–80, 2008.
- 610 [6] A. Arzhavitina and H. Steckel. Foams for pharmaceutical and cos-
611 metic application. *International Journal of Pharmaceutics*, 394(1-2):1–
612 17, 2010.
- 613 [7] Yanjun Zhao, Stuart A Jones, and Marc B Brown. Dynamic foams in
614 topical drug delivery What are topical foams ? *Journal of pharmacy
615 and pharmacology*, 62:678–684, 2010.
- 616 [8] Robert Lemlich. Adsorptive Bubble Separation Methods; Foam Frac-
617 tionation and Allied Techniques. *Ind. Eng. Chem. Res*, 60(10):16–29,
618 1968.
- 619 [9] J. Rubio, M. L. Souza, and R. W. Smith. Overview of flotation as a
620 wastewater treatment technique. *Minerals Engineering*, 15(3):139–155,
621 2002.
- 622 [10] Arnaud Saint-Jalmes and Dominique Langevin. Time evolution of aque-
623 ous foams: drainage and coarsening. *Journal of Physics: Condensed
624 Matter*, 14(40):9397–9412, 2002.
- 625 [11] Arnaud Saint-Jalmes. Physical chemistry in foam drainage and coars-
626 ening. *Soft Matter*, 2(10):836, 2006.
- 627 [12] Stephan A Koehler, Sascha Hilgenfeldt, and Howard A Stone. A Gen-
628 eralized View of Foam Drainage: Experiment and.pdf. *Langmuir*,
629 16(15):6327–6341, 2000.
- 630 [13] S. A. Koehler, S. Hilgenfeldt, and H. A. Stone. Foam drainage on the
631 microscale: I. Modeling flow through single Plateau borders. *Journal of
632 Colloid and Interface Science*, 276(2):420–438, 2004.

- [14] Sascha Hilgenfeldt, Stephan A. Koehler, and Howard A. Stone. Dynamics of coarsening foams: Accelerated and self-limiting drainage. *Physical Review Letters*, 86(20):4704–4707, 2001.
- [15] Raoul Zana. *Dynamics of Surfactant Self-Assemblies Micelles, Microemulsions, Vesicles and Lyotropic Phases*. CRC Press, 2005.
- [16] John C. Berg. Thermodynamics of Interfacial Systems. *An Introduction to Interfaces and Colloids The Bridge to Nanoscience*, pages 107–213, 2010.
- [17] Milton J. Rosen and Joy T. Kunjappu. *Surfactants and Interfacial Phenomena*. John Wiley & Sons, Inc., Hoboken, 4th edition, 2012.
- [18] John M Frostad, Daniele Tammaro, Luciano Santollani, Simone Bochner de Araujo, and Gerald G Fuller. Dynamic fluid-film interferometry as a predictor of bulk foam properties. *Soft Matter*, pages 9266–9279, 2016.
- [19] Erik M. Freer, Kang Sub Yim, Gerald G. Fuller, and Clayton J. Radke. Shear and dilatational relaxation mechanisms of globular and flexible proteins at the hexadecane/water interface. *Langmuir*, 20(23):10159–10167, 2004.
- [20] S. A. K Jeelani and S Hartland. Effect of Interfacial Mobility on Thin-Film Drainage. *J. Colloid. Interf. Sci.*, 164:296–308, 1994.
- [21] Steven L. Carnie, Derek Y C Chan, Craig Lewis, Rogério Manica, and Raymond R. Dagastine. Measurement of dynamical forces between deformable drops using the atomic force microscope. I. Theory. *Langmuir*, 21(7):2912–2922, 2005.
- [22] J M Frostad. *Fundamental Investigations of Phase Separation in Multiphase Fluids*. PhD thesis, University of California, Santa Barbara, 2013.
- [23] M Saad Bhamla, Caroline E Giacomini, Caroline Balemans, and Gerald G Fuller. Influence of interfacial rheology on drainage from curved surfaces. *Soft Matter*, 10(36):6917–6925, 2014.
- [24] Pavel Yazhgur, Emmanuelle Rio, Florence Rouyer, Franck Pigeonneau, and Anniina Salonen. Drainage in a rising foam. *Soft Matter*, 12(12):905–913, 2016.

- 665 [25] M. Saad Bhamla, Chew Chai, Marco A. Alvarez-Valenzuela, Javier
666 Tajuelo, and Gerald G. Fuller. Interfacial mechanisms for stability of
667 surfactant-laden films. *PLoS One*, 12(5), 2017.
- 668 [26] Zachary A Zell, Arash Nowbahar, Vincent Mansard, L Gary Leal,
669 Suraj S Deshmukh, Jodi M Mecca, Christopher J Tucker, and Todd M
670 Squires. Surface shear inviscidity of soluble surfactants. *Proceedings*
671 *of the National Academy of Sciences of the United States of America*,
672 111(10):3677–3682, 2014.
- 673 [27] Brent S Murray and Eric Dickinson. Interfacial Rheology and the Dy-
674 namic Properties of Adsorbed Films of Food Proteins and Surfactants.
675 *Food Sci. Technol., Int.*, 2(3):131–145, 1996.
- 676 [28] Prajnaparamita Dhar, Yanyan Cao, Thomas M Fischer, and J A Za-
677 sadzinski. Active interfacial shear microrheology of aging protein films.
678 *Physical Review Letters*, 104(016001):1–4, 2010.
- 679 [29] Vivek Sharma, Aditya Jaishankar, Ying-chih Wang, and Gareth H
680 McKinley. Rheology of globular proteins : apparent yield stress , high
681 shear rate viscosity and interfacial viscoelasticity of bovine serum albu-
682 min solutions. *Soft Matter*, pages 5150–5160, 2011.
- 683 [30] L.E. Scriven. Dynamics of a fluid interface Equation of motion for New-
684 tonian surface fluids. *Chemical Engineering Science*, 12(2):98–108, 1960.
- 685 [31] Anthony P Kotula and Shelley L Anna. Regular perturbation analysis
686 of small amplitude oscillatory dilatation of an interface in a capillary
687 pressure tensiometer. *Journal of Rheology*, 59(1):85–117, 2015.
- 688 [32] Z. Zapryanov, a. K. Malhotra, N. Aderangi, and D. T. Wasan. Emulsion
689 stability: an analysis of the effects of bulk and interfacial properties on
690 film mobility and drainage rate. *International Journal of Multiphase*
691 *Flow*, 9(2):105–129, 1983.
- 692 [33] D E Tambe and M M Sharma. Hydrodynamics of Thin Liquid-Films
693 Bounded By Viscoelastic Interfaces. *Journal of Colloid and Interface*
694 *Science*, 147(1):137–151, 1991.

- 695 [34] Arun Ramachandran and Gary Leal. A scaling theory for the hydro-
696 dynamic interaction between a pair of vesicles or capsules. *Physics of*
697 *Fluids*, 22(9):091702–1–091702–4, 2010.
- 698 [35] Byomkesh Biswas and D.A. Haydon. The Coalescence of Droplets
699 Stabilised by Viscoelastic Adsorbed Films. *Kolloid-Zeitschrift und*
700 *Zeitschrift fur Polymere*, 185(1):31–38, 1962.
- 701 [36] David E Tambe and Mukul M Shaftma. The effect of colloidal particles
702 on fluid-fluid interfacial properties and emulsion stability. *Advances in*
703 *Colloid and Interface Science*, 52:1–63, 1994.
- 704 [37] George A. Van Aken. Competitive adsorption of protein and surfac-
705 tants in highly concentrated emulsions: effect on coalescence mecha-
706 nisms. *Colloids and Surfaces A: Physicochemical and Engineering As-*
707 *pects*, 213(2-3):209–219, 2003.
- 708 [38] D. Varade, D. Carriere, L.R. Arriaga, A.L. Fameau, E. Rio, D. Langevin,
709 and W. Drenckhan. On the origin of the stability of foams made from
710 catanionic surfactant. *Soft Matter*, 7:6557–6570, 2011.
- 711 [39] David Harbottle, Qian Chen, Krishna Moorthy, Louxiang Wang, Sheng-
712 ming Xu, Qingxia Liu, Johan Sjoblom, and Zhenghe Xu. Problematic
713 Stabilizing Films in Petroleum Emulsions: Shear Rheological Response
714 of Viscoelastic Asphaltene Films and the Effect on Drop Coalescence.
715 *Langmuir*, 30(23):6730–6738, 2014.
- 716 [40] Gerald G. Fuller and Jan Vermant. Complex Fluid-Fluid Interfaces:
717 Rheology and Structure. *Annual Review of Chemical and Biomolecular*
718 *Engineering*, 3(1):519–543, 2012.
- 719 [41] T. Verwijlen, P. Moldenaers, and J. Vermant. A fixture for interfacial
720 dilatational rheometry using a rotational rheometer. *European Physical*
721 *Journal: Special Topics*, 222(1):83–97, 2013.
- 722 [42] Javier Tajuelo, J.M. Pastor, and Miguel Angel Rubio. A magnetic rod
723 interfacial shear rheometer driven by a mobile magnetic trap. *Journal*
724 *of Rheology*, 60:1095–1113, 2016.

- [43] Eric Dickinson. Adsorbed protein layers at fluid interfaces: Interactions, structure and surface rheology. *Colloids and Surfaces B: Biointerfaces*, 15(2):161–176, 1999.
- [44] Luis GP Pereira, Harvey W Blanch, and Clayton J Radke. Dilatational Rheology of BSA Conformers at the Air / Water Interface. *Langmuir*, 19(6):2349–2356, 2003.
- [45] M Coke, P J Wilde, E J Russell, and D C Clark. the Influence of Surface-Composition and Molecular-Diffusion on the Stability of Foams Formed From Protein Surfactant Mixtures. *Journal of Colloid and Interface Science*, 138(2):489–504, 1990.
- [46] Pj Wilde and Dc Clark. The competitive displacement of β -lactoglobulin by Tween 20 from oil-water and air-water interfaces. 155:48–54, 1993.
- [47] B. Rippner Blomqvist, M. J. Ridout, A. R. Mackie, T. Wörnheim, P. M. Claesson, and P. Wilde. Disruption of viscoelastic beta-lactoglobulin surface layers at the air-water interface by nonionic polymeric surfactants. *Langmuir*, 20(23):10150–10158, 2004.
- [48] M. Saad Bhamla, Chew Chai, Noelle I. Rabiah, John M. Frostad, and Gerald G. Fuller. Instability and Breakup of Model Tear Films. *Investigative Ophthalmology & Visual Science*, 57:949–958, 2016.
- [49] A. Scheludko and D. Exerowa. Über den elektrostatischen Druck in Schaumfilmen aus wässrigen Elektrolytlösungen. *D.Kolloid-Z*, 165(148):148–151, 1959.
- [50] LG Pereira, C Johansson, H W Blanch, and C J Radke. A bike-wheel microcell for measurement of thin-film forces. *Colloids and Surfaces A: Physicochemical and Engineering Aspects*, 186:103–111, 2001.
- [51] Peter A. Wierenga, Elka S. Basheva, and Nikolai D. Denkov. Modified capillary cell for foam film studies allowing exchange of the film-forming liquid. *Langmuir*, 25(11):6035–6039, 2009.
- [52] Peter J. Beltramo, Rob Van Van Hooghten, and Jan Vermant. Millimeter-area, free standing, phospholipid bilayers. *Soft Matter*, 12:4324–4331, 2016.

- 756 [53] Y. Zhang, S. Yilixiati, C. Pearsall, and V Sharma. Nanoscopic Ter-
757 races, Mesas, and Ridges in Freely Standing Thin Films Sculpted by
758 Supramolecular Oscillatory Surface Forces. *ACS Nano*, 10:4678–4683,
759 2016.
- 760 [54] S. Sett, S. Sinha-Ray, and A. L. Yarin. Gravitational drainage of foam
761 films. *Langmuir*, 29(16):4934–4947, 2013.
- 762 [55] Steffen Berg, Eric A. Adelizzi, and Sandra M. Troian. Experimental
763 study of entrainment and drainage flows in microscale soap films. *Lang-*
764 *muir*, 21(9):3867–3876, 2005.
- 765 [56] Luis GP Pereira, C Johansson, C J Radke, and H W Blanch. Sur-
766 face Forces and Drainage Kinetics of Protein-Stabilized Aqueous Films.
767 *Langmuir*, 19(18):7503–7513, 2003.
- 768 [57] Paul M Dewick. *Medicinal Natural Produces: A Biosynthetic Approach*.
769 John Wiley & Sons, Ltd, Baffins Lane, Chichester, West Sussex, Eng-
770 land, 2nd edition, 2002.
- 771 [58] Konstantin Golemanov, Slavka Tcholakova, Nikolai Denkov, Edward
772 Pelan, and Simeon D. Stoyanov. Remarkably high surface visco-
773 elasticity of adsorption layers of triterpenoid saponins. *Soft Matter*,
774 9:5738, 2013.
- 775 [59] Sameh M I Saad, Zdenka Policova, Edgar J. Acosta, and A. Wilhelm
776 Neumann. Range of validity of drop shape techniques for surface tension
777 measurement. *Langmuir*, 26(17):14004–14013, 2010.
- 778 [60] Sebastian Knoche, Dominic Vella, Elodie Aumaitre, Patrick Degen,
779 Heinz Rehage, Pietro Cicuta, and Jan Kierfeld. Elastometry of deflated
780 capsules: Elastic moduli from shape and wrinkle analysis. *Langmuir*,
781 29(40):12463–12471, 2013.
- 782 [61] Steven Vandebril, Aly Franck, Gerald G. Fuller, Paula Moldenaers, and
783 Jan Vermant. A double wall-ring geometry for interfacial shear rheom-
784 etry. *Rheologica Acta*, 49(2):131–144, 2010.
- 785 [62] Z. Zhang, S. Barman, and G.F. Christopher. The role of protein content
786 on the steady and oscillatory shear rheology of model synovial fluids.
787 *Soft Matter*, 10(32):5965–5973, 2014.

- 788 [63] Stephan A. Koehler, Sascha Hilgenfeldt, Eric R. Weeks, and Howard A.
789 Stone. Drainage of single Plateau borders: Direct observation of rigid
790 and mobile interfaces. *Physical Review E - Statistical, Nonlinear, and*
791 *Soft Matter Physics*, 66(4):1–4, 2002.
- 792 [64] L. Gary Leal. *Advanced Transport Phenomena*. Cambridge University
793 Press, 2007.
- 794 [65] John M. Frostad, Alexandra Paul, and L. Gary Leal. Coalescence of
795 droplets due to a constant force interaction in a quiescent viscous fluid.
796 *Physical Review Fluids*, 1(3):033904, 2016.
- 797 [66] Joseph D. Berry and Raymond R. Dagastine. Mapping coalescence of
798 micron-sized drops and bubbles. *Journal of Colloid and Interface Sci-*
799 *ence*, 487:513–522, 2017.
- 800 [67] J. M. Frostad, J. Walter, and L. G. Leal. A scaling relation for the
801 capillary-pressure driven drainage of thin films. *Physics of Fluids*,
802 25(5):1–17, 2013.
- 803 [68] Laure Bluteau, Maurice Bourrel, Nicolas Passade-Boupat, Laurence Tal-
804 ini, Emilie Verneuil, and Franois Lequeux. Water film squeezed between
805 oil and solid: drainage towards stabilization by disjoining pressure. *Soft*
806 *Matter*, 13(7):1384–1395, 2017.
- 807 [69] T. T. Traykov, E.D. Manev, and I.B. Ivanov. Hydrodynamics of thin
808 liquid films. Experimental investigation of the effect of surfactants on the
809 drainage of emulsion films. *International Journal of Multiphase Flow*,
810 3(5):485–494, 1977.
- 811 [70] A.A. Sonin, A. Bonfillon, and D. Langevin. Role of Surface Elasticity in
812 the Drainage of Soap Films. *Physical Review Letters*, 71(14):2342–2345,
813 1993.