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Mechanical energy based amplifiers for probing interactions of DNA with metal ions

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We report our development of a simple and cost-effective method to amplify and probe the interactions of DNA with metal ions, which are important for various fundamental processes in live systems. This method is based on perturbing energy landscapes using mechanical energy stored in bent DNA molecules. In this proof-of-principle study, the mechanical energy based amplifiers were applied to examine the interactions between DNA and Mg^{2+} ions, or Ag^+ ions. We demonstrated that interactions between DNA and Mg^{2+} or Ag^+ ions, which are not detectable using gel electrophoresis without amplification, can be easily measured using our molecular amplifiers. In addition, we showed that quantitative details about the DNA-metal interactions can be estimated using our method. Our method is simple, sensitive, and cost-effective. We expect that the developed method will be useful for various applications.

I. INTRODUCTION

A fascinating concept in physics is that many properties of a system (including the equilibrium and dynamics) are governed by the system's Hamiltonian H , or the potential energy V , which has been commonly referred to as the “energy landscape” of the system and been increasingly useful in other fields such as chemistry, biochemistry and biology [1]. An interesting direction rising from this concept is to perturb the energy landscape to possibly modulate and/or bias chemical and biochemical systems and reactions by various means [2]. Among the available means, mechanical methods are particularly appealing because mechanical methods are *universal* in the sense that they do not depend on the exact type and details of the involved chemical and biochemical systems and reactions. Therefore, it is of great interest to make use of mechanical energies and forces for controlling chemical, biochemical and biological reactions, with significant progresses in the past three decades [1]. For example, mechanical forces induced by ultrasound have been applied to polymer solutions to accelerate and alter the course of the related chemical reactions [3]. In addition, mechanical tensions have been introduced to enzymes using DNA molecular springs to control their enzymatic activities [4–6].

In this article, we report our development of a new concept of exploiting mechanical energies/forces to amplify the interactions between DNA and metal ions, which are important for life [7]. On one hand, DNA-metal interactions are essential for various fundamental processes in cells. For example, the formation of secondary and higher-order structures of nucleotides, DNA repair, and genomic stability require the presence, mediation, and/or participation of metal ions such as magnesium ions (Mg^{2+}) [8–10]. On the other hand, many metal ions could be toxic, resulting in DNA damage and cell

death, which can accumulate and possibly lead to diseases such as cancers and other diseases [11]. For example, many studies showed that Ag^+ , Cu^{2+} and Al^{3+} ions induce DNA damage and have genotoxicity [12]. Therefore, it is important to understand the interactions between DNA and metal ions in solutions, which however is not straightforward to measure directly. First, most chemical and biochemical methods are not sensitive enough: the most well studied DNA-metal interactions using biochemical methods are DNA cleavages [7], but most DNA-metal interactions are much milder. In addition to biochemical assays, many spectroscopic methods have been used to study DNA-metal interactions. However, while some of them are not sensitive enough (e.g., X-ray absorption spectroscopy), some require samples in solid phase and thus are not suitable for studies in solutions (e.g., electron paramagnetic resonance) [7]. Furthermore, sensitive techniques such as infrared and Raman spectroscopy and nuclear magnetic resonance spectroscopy typically require expensive equipment [7]. Therefore, there is an urgent need for developing simple, sensitive, and cost-effective methods to study the interactions between DNA and metal ions.

In this work, we took advantage of mechanical energy stored in bent DNA molecules and developed a simple, cost-effective method to amplify and probe the interactions between DNA with metal ions. The strategy of this method is illustrated in Fig. 1a and 1b, where hypothetical energy landscapes along the DNA-metal “reaction” coordinate are shown, assuming one of the local minima in the energy landscape (indicated by the open magenta arrow) gives the detectable signal of the DNA-metal interaction. Without amplification (i.e., the normal linear DNA), the signal from the interaction at equilibrium might be too low to detect; however, by perturbing the energy landscape using the bending energy stored in bent DNA molecules, more molecules might be distributed in the detectable state (open magenta arrow), resulting in an amplification of the detectable signals. It is noted that the mechanical energy stored in the bent DNA does not necessarily introduces additional interac-

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93 tions of DNA with metal ions; instead, the mechanical
 94 energy improves the sensitivity for observing the interac-
 95 tions. A good analog to illustrate this idea is throwing
 96 marble balls onto wooden sticks. If the collisions are
 97 weak enough, the sticks rarely crack, producing “low signals”.
 98 In contrast, after applying stress and pre-bending
 99 the sticks so that they are close to break down, collisions
 100 at the same strength would result in higher number of
 101 cracked sticks, generating “higher signals”. The mechan-
 102 ical energy stored in the pre-bent sticks does not change
 103 their interactions with the balls; instead, it makes the
 104 signals much easier to be observed. In other words, the
 105 mechanical energy “amplifies” the signals.

106 The bent DNA molecules are achieved following the pi-
 107 oneer work by the Zocchi group [13–15]. Briefly, as shown
 108 in Fig. 1c and 1d, two single-stranded DNA sequences are
 109 designed. The left 1/3 of the long sequence (light blue)
 110 hybridizes to the left half of the short sequence (dark
 111 red), while the right 1/3 of the long sequence hybridizes
 112 to the right half of the short sequence, leaving the mid-
 113 dle 1/3 of the long sequence unhybridized. This design
 114 will produce, upon hybridization, a bent double-stranded
 115 DNA (containing a nick), while the single-stranded part
 116 is stretched. In contrast to previous work focusing on un-
 117 derstanding the mechanical properties and bending en-
 118 ergy of the bent DNA molecules (with or without nicks)
 119 [13–16], the goal of the current study is to explore appli-
 120 cations of the bent DNA molecules.

121 As a proof-of-concept, these mechanical energy based
 122 amplifiers were applied to examine the interactions be-
 123 tween DNA and Mg^{2+} ions, or Ag^+ ions. We demon-
 124 strated that interactions between DNA and Mg^{2+} or Ag^+
 125 ions, which are not detectable using gel electrophoresis
 126 without amplification, can be easily measured using our
 127 molecular amplifiers. In addition, we showed that our
 128 method is capable of obtaining quantitative details about
 129 the DNA-metal interactions. Our method is simple, sen-
 130 sitive, and cost-effective, without requiring sophisticated
 131 and/or expensive equipment. We expect that the devel-
 132 oped method will be useful broadly for various applica-
 133 tions involving interactions of DNA with ions, molecules,
 134 reagents and drugs.

135 II. METHODS AND MATERIALS

136 Synthesized single-stranded DNA molecules were pur-
 137 chased from Integrated DNA Technologies (IL, USA),
 138 and resuspended in distilled water to a final concentra-
 139 tion of 100 μM . The sequences of DNA strands for con-
 140 structing bent DNA molecules and the controls (Fig. 1e)
 141 are listed in Table I. The long strand of the bent molecule
 142 (construct B in Fig. 1e) has 45 bases, while the length
 143 of the short strand is 30. Upon hybridization, a circular
 144 construct is formed, with a double-stranded portion of 30
 145 basepairs (with a nick) and a single-stranded portion of
 146 15 bases (Fig. 1c and 1d). Three linear constructs (C1,
 147 C2 and C3 in Fig. 1e) were used as negative controls.

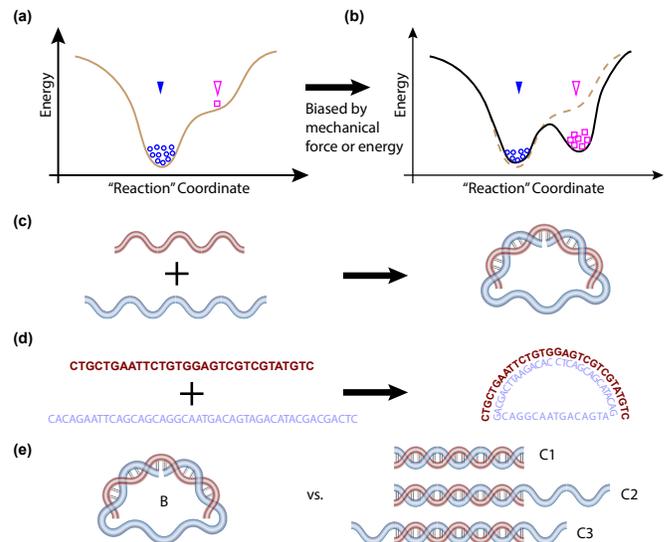


FIG. 1. Overall strategy of the mechanical energy based amplifiers for probing interactions of DNA with metal ions. (a, b) Perturbing a hypothetical energy landscape to redistribute molecules so that higher signals are detected. With the original, unperturbed energy landscape (a), fewer molecules are distributed on the detectable state (open magenta arrow), producing lower signals. In contrast, after biasing the energy landscape by mechanical forces or energies (b), more “molecules” are redistributed on the detectable state (open magenta arrow), “amplifying” the signals for detections. (c) Self-assembly of a bent double-stranded DNA. (d) Self-assembly of a bent double-stranded DNA with sequences shown. (e) Bent DNA molecules (construct B) as amplifiers vs. linear DNA molecules (constructs C1, C2 and C3) as negative controls.

148 Upon hybridization, C1 is double-stranded completely,
 149 while C2 and C3 have overhangs of single strands on one
 150 or two sides, respectively. The long strands for C2 and
 151 C3 are the same as the long one in the bent molecule.

152 Single strands were mixed at equal molar amount in
 153 background buffer (0.4 mM Tris-HCl with pH adjusted
 154 to 7.5 using NaOH, 0.5 mM NaCl; the ionic strength
 155 is ~ 1 mM) to reach a final concentration of 2 μM with
 156 Mg^{2+} or Ag^+ ions at various concentrations ($[Mg^{2+}] = 0,$
 157 1, 2, 3, 4, 5, 6, 7 mM; $[Ag^+] = 0, 10, 20, \dots, 80, 90 \mu M$).
 158 Mg^{2+} and Ag^+ ions were provided from aqueous solu-
 159 tions of $MgCl_2$ and $AgNO_3$, respectively. The mixtures
 160 were heated to 75°C for 2 minutes, and gradually cooled
 161 down to 22°C (room temperature) in 5 hours. The mix-
 162 tures were incubated at 22°C for overnight to allow full
 163 equilibrium, followed by gel electrophoresis on the second
 164 day.

165 Polyacrylamide gels (12%) were prepared in the labora-
 166 tory. Briefly, 3 mL of acrylamide/bis solutions (40%, Bio-
 167 Rad Laboratories, CA, USA), 1 mL of 10X tris-borate-
 168 EDTA (TBE) buffer (Bio-Rad Laboratories), 20 μL of
 169 freshly made ammonium persulfate (APS, 10% in water,
 170 Thermo Fisher Scientific, MA, USA) and 6 mL of dis-

Construct	Sequences (5'-3')
B	CTG CTG AAT TCT GTG GAG TCG TCG TAT GTC CAC AGA ATT CAG CAG CAG GCA ATG ACA GTA GAC ATA CGA CGA CTC
C1	GAG ATG TCA AGA ATT CCG TCA GCA C GTG CTG ACG GAA TTC TTG ACA TCT C
C2	TAC TGT CAT TGC CTG CTG CTG AAT TCT GTG CAC AGA ATT CAG CAG CAG GCA ATG ACA GTA GAC ATA CGA CGA CTC
C3	GTA TGT CTA CTG TCA TTG CCT GCT GCT GAA CAC AGA ATT CAG CAG CAG GCA ATG ACA GTA GAC ATA CGA CGA CTC

TABLE I. DNA sequences used in this study. The labels of the constructs refer to their schematic sketches shown in Fig. 1e.

171 tilled water were mixed thoroughly and degassed for 10
172 minutes in vacuum. The mixture was poured into gel
173 cast cassette immediately after adding 8 μL of tetram-
174 ethylethylenediamine (TEMED) (Thermo Fisher Scien-
175 tific), followed by incubation at room temperature for
176 one to two hours to allow full gelation before use.

177 5 μL of the prepared DNA samples were mixed thor-
178 oughly with 5 μL of water and 2 μL of 6X DNA loading
179 buffer (Bio-Rad Laboratories). The mixtures were loaded
180 into the wells of the prepared gel. The gel electrophore-
181 sis (apparatus purchased from Edvotek Inc., DC, USA)
182 was run at 100V for 45–60 minutes in 1X TBE buffer,
183 followed by staining the gel with 1X SYBR Safe solution
184 (Thermo Fisher Scientific) for 15–30 minutes with gentle
185 shaking. The stained gel was then imaged with a typical
186 exposure time of 2–5 seconds using a gel documentation
187 system (UVP LLC., CA, USA). The acquired gel images
188 were analyzed using ImageJ [17, 18].

189 III. RESULTS AND DISCUSSIONS

190 A. DNA-Mg²⁺ Interactions

191 We first examined the well-known interaction between
192 DNA and Mg²⁺ ions using our method (Fig. 2). As
193 DNA molecules are negatively charged, electrostatic in-
194 teractions are expected between Mg²⁺ ions and DNA.
195 In addition, electrostatic screening effects due to Mg²⁺
196 ions stabilize double-stranded DNA molecules, which has
197 been measured by magnetic tweezers, optical tweezers
198 and atomic force microscopy [19–22]. However, such in-
199 teractions between DNA and Mg²⁺ ions cannot be eas-
200 ily observed with standard chemical/biochemical assays
201 such as gel electrophoresis. For example, short linear
202 double-stranded DNA molecules treated with Mg²⁺ from
203 0 mM (control) to 7 mM did not show any difference in gel

204 electrophoresis (Fig. 2a, indicated by red squares). To
205 quantify this observation, we measured the band intensi-
206 ties using ImageJ [17, 18] and compared them with the
207 control (i.e., [Mg²⁺] = 0 mM), and observed a flat curve
208 (red squares in Fig. 2e). In contrast, when amplifying
209 the signal of DNA-Mg²⁺ interactions using the bent DNA
210 molecules, the effect of Mg²⁺ at the same concentrations
211 (0–7 mM) is quite obvious (Fig. 2d): the intensity of the
212 bent DNA band (indicated by blue circles in Fig. 2d)
213 decreased as the concentration of Mg²⁺ increased. In
214 addition, we found that the dependence on Mg²⁺ concen-
215 tration of the intensity of the bent DNA band is roughly
216 linear (blue circles in Fig. 2e). We note that a change
217 was observed for [Mg²⁺] = 1 mM with the bent DNA
218 amplifiers, while such a change was absent with [Mg²⁺]
219 = 7 mM without amplification, indicating that the “am-
220 plification gain” of our bent DNA amplifiers for prob-
221 ing DNA-Mg²⁺ interactions is at least 7. To exclude
222 the possibility that the observed change in the gel elec-
223 trophoretic pattern is due to the single-stranded portion
224 of the bent molecules, we performed control experiments
225 with linear DNA molecules that contains both double-
226 stranded and single-stranded parts (constructs C2 and
227 C3 in Fig. 1e). We observed little changes for constructs
228 C2 and C3 in the presence of 1–7 mM Mg²⁺ as shown in
229 Fig. 2b, 2c, and 2e (orange triangles and magenta \times).
230 This observation suggests that the bent double-stranded
231 DNA and the stored elastic energy are critical to detect
232 the DNA-Mg²⁺ interactions.

233 In addition, our mechanical energy based amplifiers are
234 capable of reporting quantitatively the interaction be-
235 tween Mg²⁺ and DNA molecules. Figure 2D shows that
236 bands with heavier molecular weights appeared in the
237 presence of Mg²⁺ ions (indicated by the green triangle
238 and the cyan “}” in Fig. 2d). Previous studies by Qu et
239 al. showed that these bands correspond to higher-order
240 multimers [13–15]: for example, two monomers form a
241 dimer; one monomer and one dimer (or three monomers)
242 form a trimer; one monomer and one trimer (or four
243 monomers) form a tetramer. Although the heavier multi-
244 mers (i.e., tetramers and above) were not resolved in our
245 experiments, it is clear that the intensities of the bent
246 monomer bands (blue circle) decreased in the presence of
247 Mg²⁺ ions, while the intensities of the bands with heav-
248 ier molecular weight increased. This observation sug-
249 gests that Mg²⁺ ions lead to a conversion from the bent
250 DNA monomers to the relaxed DNA dimers and multi-
251 mers (Fig. 2f). A complete quantitative understanding of
252 the observation requires taking into account all the possi-
253 ble reactions; however, for simplicity, here we focus only
254 on the conversion (“reaction”) between monomers and
255 dimers (Fig. 2f). The conversion between the monomers
256 and dimers can be understood by starting with the chem-
257 ical potential of solute molecules μ_s in water,

$$258 \mu_s = \epsilon_s + k_B T \ln \left(\frac{N_s}{N_w} \right) = \epsilon_s + k_B T \ln(x_s) \quad (1)$$

259 where ϵ_s is the energy of each solute molecule, k_B the

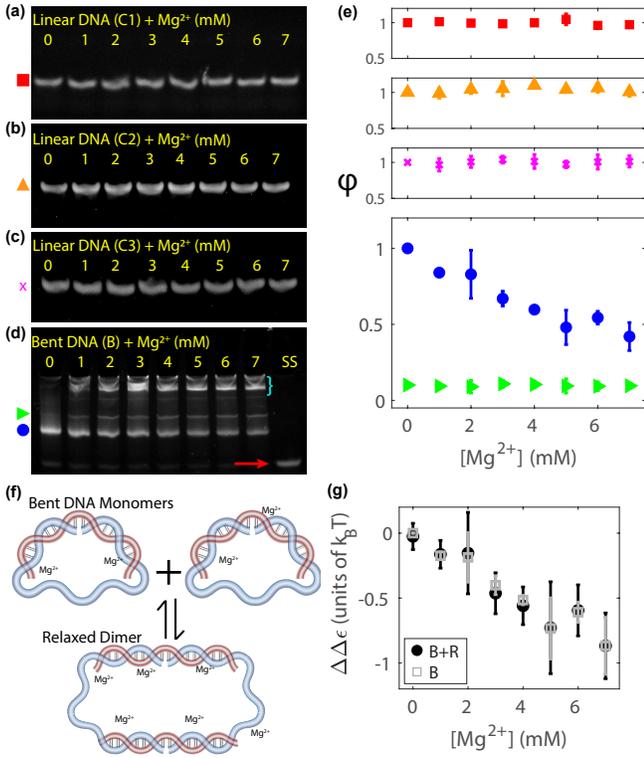


FIG. 2. Probing DNA-Mg²⁺ interactions using bent DNA amplifiers. (a-c) Gel electrophoresis for linear DNA controls in the presence of Mg²⁺ ions of 0–7 mM. a: construct C1, b: construct C2, c: construct C3. (d) Gel electrophoresis for bent DNA in the presence of Mg²⁺ ions of 0–7 mM. Lane SS: the long single-stranded DNA (45 bases) in the absence of Mg²⁺ ions. (e) Dependence on Mg²⁺ concentration of the intensities of the bands indicated by the corresponding markers in panels a–d. Error bars stand for standard deviation of replicates. (f) Conversion (“reaction”) between bent DNA monomers (blue circles in panel d) and relaxed dimers (green triangles in panel d). (g) Estimated change in the difference of free energy between the relax dimers and bent monomers as a function of Mg²⁺ concentration. Estimations were carried out using either the bent monomer band only (B, gray squares) or both the bent monomer and relaxed dimer bands (B+R, black circles).

Boltzmann constant, T the temperature, N_s the number of solute molecules, N_w the number of water molecules, and $x_s = N_s/(N_w + N_s) \approx N_s/N_w$ the molar fraction of the solute molecules [23]. At equilibrium, we have $\mu_r = 2 \cdot \mu_b$, where μ_r is the chemical potential of a relaxed DNA dimer and μ_b the chemical potential of a bent DNA monomer. Therefore, we have [13],

$$\epsilon_r - 2\epsilon_b = k_B T \ln \left(\frac{x_b^2}{x_r} \right) \quad (2)$$

The difference in the free energy between half a dimer and a single bent DNA molecule is then

$$\Delta\epsilon = \frac{\epsilon_r}{2} - \epsilon_b = k_B T \ln(x_b) - \frac{1}{2} k_B T \ln(x_r) \quad (3)$$

As a result, this difference $\Delta\epsilon$ can be estimated from the molar fractions of the bent DNA monomers and the relaxed dimers, which are proportional to the band intensities, $x_b = \beta I_b$ and $x_r = \frac{1}{2} \beta I_r$, where β is a constant. Note that, as the length of the relaxed dimers are twice that of the monomers, each dimer contributes twice the intensity of a monomer. Since the intensity of the dimer bands remains almost constant (green triangles in Fig. 2d and 2E), the observed decrease in the band intensity of the bent DNA monomers (blue circles in Fig. 2e) in the presence of [Mg²⁺] suggests that $\Delta\epsilon$ decreased as [Mg²⁺] increased.

More quantitatively, we estimated the effect of Mg²⁺ ions on DNA (i.e., the change of $\Delta\epsilon$ in the presence (+) and absence (–) of Mg²⁺ ions) by

$$\Delta\Delta\epsilon = \Delta\epsilon^+ - \Delta\epsilon^- = k_B T \left[\ln \left(\frac{x_b^+}{x_b^-} \right) - \frac{1}{2} \ln \left(\frac{x_r^+}{x_r^-} \right) \right] \quad (4)$$

If we normalize the molar fractions to the control (i.e., [Mg²⁺] = 0 mM), $\varphi_b^- = \frac{x_b^-}{x_b^-} = 1$, $\varphi_b^+ = \frac{x_b^+}{x_b^-}$, $\varphi_r^- = \frac{x_r^-}{x_b^-}$, and $\varphi_r^+ = \frac{x_r^+}{x_b^-}$, we have

$$\Delta\Delta\epsilon = k_B T \left[\ln(\varphi_b^+) - \frac{1}{2} \ln \left(\frac{\varphi_r^+}{\varphi_r^-} \right) \right] \quad (5)$$

Using the data in Fig. 2e (both blue circles and green triangles), it was found that $\Delta\Delta\epsilon$ decreases linearly as the concentration of Mg²⁺ increases, as shown in Fig. 2g (black circles). Furthermore, we examined the possibility of using the dependence of $\Delta\Delta\epsilon$ on the molar fraction of the bent DNA monomer φ_b to capture the main feature of $\Delta\Delta\epsilon$ in the presence of Mg²⁺ ions (i.e., $\Delta\Delta\epsilon$ decreases as [Mg²⁺] increases). For this purpose, we estimated $\Delta\Delta\epsilon$ by considering the first term and ignoring the other bands,

$$\Delta\Delta\epsilon \sim k_B T \ln(\varphi_b^+) \quad (6)$$

It turns out that the estimations from the bent monomer only (gray squares in Fig. 2g) are very close to the calculations using both the bent monomer and the relaxed dimer (black circles in Fig. 2g). A caveat to emphasize here is that the heavier multimers have been ignored in the current analysis (Fig. 2g). As a result, we have underestimated φ_r^+/φ_r^- and thus $\Delta\Delta\epsilon$ in Eq. (5).

To better understand the physics of how Mg²⁺ ions promote the conversion from the bent monomers to the relaxed dimers/multimers, we examined qualitatively several possible contributions to $\Delta\Delta\epsilon = \frac{1}{2}(\epsilon_r^+ - \epsilon_r^-) - (\epsilon_b^+ - \epsilon_b^-)$. The purpose of the discussions below is to assess the *order of magnitude* of various potential contributions; further quantitative investigations are needed to determine their exact values. These discussions are based on the well-known electrostatic screening effects of Mg²⁺ ions, including (a) stabilization of base-pairing and base-stacking [24, 25], and (b) contribution to electrostatic interactions.

The stabilization of base-pairing and base-stacking in DNA due to Mg^{2+} ions is expected to affect the behavior of the nick in our bent DNA monomers, the persistence length of double-stranded DNA, and the hybridization between two DNA strands.

(a1) Effects on the nick-behavior. It has been shown that sharply bending a double-stranded DNA with a nick leads to kink-formation (i.e., disruption of base-stacking) and even strand-peeling (disruption of base-pairing) [16]. The disruptions of base-stacking and base-pairing will then reduce the hybridization energy in the bent monomers. As Mg^{2+} ions stabilize the base-pairing and base-stacking [24, 25], we would have less disruption and thus less reduction in the hybridization energy in the presence of Mg^{2+} , i.e., $(\frac{1}{2}\epsilon_{r,nh}^+ - \epsilon_{b,nh}^+) < (\frac{1}{2}\epsilon_{r,nh}^- - \epsilon_{b,nh}^-)$. Therefore, we obtain $\Delta\Delta\epsilon_{nh} < 0$, which has the same sign with the measurement (Fig. 2g). In addition, the stabilization of base-stacking and base-pairing due to Mg^{2+} ions is likely to render a higher bending elastic energy in the bent monomers, $\epsilon_{b,ne}^+ > \epsilon_{b,ne}^-$, which gives $\Delta\Delta\epsilon_{ne} = -(\epsilon_{b,ne}^+ - \epsilon_{b,ne}^-) < 0$. Therefore, we expect that the effect of the nick in the DNA, $\Delta\Delta\epsilon_n = \Delta\Delta\epsilon_{nh} + \Delta\epsilon_{ne}$, is < 0 , showing the same sign as our experimental results ($\Delta\Delta\epsilon < 0$ as shown Fig. 2g). We note that the order of magnitude of $\Delta\Delta\epsilon_n$ can be estimated from the computational work by Cong et al. [16]. If we assume that the Mg^{2+} -stabilized nicked DNA is similar to an nick-free one (an over-estimation), we expect that $\Delta\Delta\epsilon_n$ is between 0 and $-5 k_B T$ if only base-unstacking is present, or between $-5 k_B T$ and $-15 k_B T$ if strand-peeling occurs [16].

(a2) Effects on persistence length (L_p). When *ignoring kink-formation or strand-peeling* due to the nick, Mg^{2+} ions' electrostatic screening effects will shorten the persistence length L_p of double-stranded DNA [19–22]. For example, Baumann et al. measured that the persistence length of DNA reduced to 42%–54% in the presence of 100 μM Mg^{2+} ions [19]. In addition, Brunet et al. proposed an interpolation formula in a recent work [21], which fitted their experimental data very well [21] and predicted that the persistence length of our DNA would be reduced to $\sim 80\%$ when the ionic strength increased from ~ 1 mM ($[\text{Mg}^{2+}] = 0$ mM) to ~ 22 mM ($[\text{Mg}^{2+}] = 7$ mM) in our experiments. These experimental results [19–22] suggested that the decrease in the persistence length of DNA due to Mg^{2+} ions is in the order of ~ 0.5 . The persistence of a polymer is tightly related to the bending elastic energy (ϵ_e , as the bending stiffness B is proportional to L_p), which is expected to contribute to $\Delta\Delta\epsilon$. For relaxed molecules, as they are not bent, the bending energy is negligible; therefore, changes in the persistence length due to Mg^{2+} ions

do not contribute: $\epsilon_{r,e}^+ - \epsilon_{r,e}^- \sim 0$. In contrast, for the bent monomers, a shorter persistence length resulted in a lower bending elastic energy, $\epsilon_{b,e}^+ - \epsilon_{b,e}^- < 0$. Therefore, we have $\Delta\Delta\epsilon_e > 0$, which shows the opposite sign compared to the measurement ($\Delta\Delta\epsilon < 0$ as shown Fig. 2g). Using the elastic bending energy measured by Qu et al. [13], $8.6 - 9.7 k_B T$ (or in the order of $\sim 10 k_B T$) for a bent monomer with 30 bp of the double-stranded segment and 15 bases of the single-stranded segment, we estimate that $\Delta\Delta\epsilon_e$ is in the order of $\sim 5 k_B T$ for 7 mM Mg^{2+} ions in our experiments.

(a3) Effects on hybridization energy (ϵ_h). Even if *ignoring kink-formation or strand-peeling* due to the nick, it has been reported that Mg^{2+} ions stabilize the hydrogen bonds for the base-pairing of double-stranded DNA [24, 25]. Therefore, the hybridization energy (ϵ_h) could be a potential contribution to $\Delta\Delta\epsilon$. However, in the absence of strand-peeling (or unzipping), the hybridization energy is expected to be proportional to the number of base-pairs. As the length of the relax dimers is twice of the length of bent monomers, we have $(\epsilon_{r,h}^+ - \epsilon_{r,h}^-) = 2 \times (\epsilon_{b,h}^+ - \epsilon_{b,h}^-)$. Therefore, the effect of Mg^{2+} on the hybridization energy cancels out, resulting in $\Delta\Delta\epsilon_h \approx 0$.

The presence of Mg^{2+} ions is also likely to affect electrostatic interactions inside DNA molecules and that between DNA and Mg^{2+} ions.

(b1) Effects on electrostatic interactions inside DNA molecules. For double-stranded DNA segments, it is likely that the electrostatic interactions ϵ_{esn} are reduced for both bent monomers and relaxed molecules, $\Delta\Delta\epsilon_{r,esn} < 0$ and $\Delta\Delta\epsilon_{b,esn} < 0$, due to the screening effect of Mg^{2+} ions. For the single-stranded segments, we expect a shorter persistence length ($L_{p,ss}$), which results in higher entropic elastic energy ($\epsilon_{ss} \propto k_B T / N_s L_{p,ss}^2$ where N_s is the length of the single-stranded segment). Therefore, we have $\Delta\Delta\epsilon_{r,ss} > 0$ and $\Delta\Delta\epsilon_{b,ss} > 0$. Qu et al. showed that the combined contribution from the electrostatic interactions inside DNA molecules and entropic elastic energy of the single-stranded segments is $9.7 - 8.6 = 1.1 k_B T$ [13], or in the order of $\sim 1 k_B T$. Therefore, we expect that $|\Delta\Delta\epsilon_{esn} + \Delta\Delta\epsilon_{ss}|$ is also in the order of $\sim 1 - 2 k_B T$.

(b2) Effects on electrostatic interactions between DNA and Mg^{2+} ions (ϵ_{esi}). Because these electrostatic interactions do not depend on the conformation of the DNA, and that the length of the relax dimers is twice of the length of bent monomers, we expect that $(\epsilon_{r,esi}^+ - \epsilon_{r,esi}^-) = 2 \times (\epsilon_{b,esi}^+ - \epsilon_{b,esi}^-)$. Therefore, we have $\Delta\Delta\epsilon_{esi} \sim 0$, which is negligible.

By comparing the signs of the various contributions ($\Delta\Delta\epsilon_e, \Delta\Delta\epsilon_h, \Delta\Delta\epsilon_n, \dots$) with that of the experimental

433 results ($\Delta\Delta\epsilon < 0$ as shown in Fig. 2g), we concluded
 434 that, although Mg^{2+} ions play a role in most of these
 435 terms, the stabilization of Mg^{2+} on base-stacking and
 436 base-pairing in the nicked DNA is likely the main driving
 437 “forces” for the monomer-to-multimer conversion (Fig.
 438 2f). Therefore, both the bending of the DNA molecules
 439 and the nick are important for perturbing the energy
 440 landscape and amplifying the DNA- Mg^{2+} interactions.

441 B. DNA- Ag^+ Interactions

442 With the successful application of our bent DNA ampli-
 443 fiers to study DNA- Mg^{2+} interactions, we exploited
 444 them to investigate the interactions of DNA with Ag^+
 445 ions. The significance of DNA- Ag^+ interactions includes
 446 their genotoxicity and potential uses as antibiotic alter-
 447 natives. For example, it has been reported that Ag^+ ions
 448 at $< 100 \mu\text{M}$ concentrations show significant antibiotic
 449 activities against bacteria [26, 27]. More importantly, it
 450 has been argued that it is more difficult for bacteria to
 451 develop resistance to Ag^+ ions compared to commonly
 452 prescribed antibiotics [28]. Therefore, it is of great inter-
 453 est to understand the antibiotic mechanism of Ag^+ ions,
 454 which includes DNA- Ag^+ interactions. It was measured
 455 that Ag^+ ions caused DNA condensation in bacteria [29];
 456 however, this result could not be verified previously by
 457 *in vitro* experiments such as gel electrophoresis [30].

458 Here, we demonstrate that our method can be used to
 459 sensitively measure the interactions between DNA and
 460 Ag^+ ions. First, we examined the effect of Ag^+ ions (0–
 461 $90 \mu\text{M}$) on linear double-stranded DNA (construct C1),
 462 and observed no changes with gel electrophoresis (Fig.
 463 3a, and red squares in Fig. 3e), consistent with previous
 464 reports [30]. In addition, similar to the experiments with
 465 Mg^{2+} ions, two other controls with both double-stranded
 466 segments and single-stranded overhangs (constructs C2
 467 and C3) were tested (Fig. 3b and 3c). Again, little
 468 changes were observed (orange triangles and magenta \times
 469 in Fig. 3e). In contrast, using the bent DNA amplifiers,
 470 the interactions between DNA and Ag^+ ions were easily
 471 observed at $10 \mu\text{M}$ of Ag^+ ions, as shown in Fig. 3d. We
 472 note that our method can detect changes at $[\text{Ag}^+] = 10$
 473 μM , while, without amplification, no such changes were
 474 observed with even $[\text{Ag}^+] = 90 \mu\text{M}$. The “amplification
 475 gain” of our method for probing DNA- Ag^+ interactions
 476 is at least 9.

477 It was observed that Ag^+ ions caused the intensity of
 478 the bent DNA band to decrease (blue circles in Fig. 3d
 479 and Fig. 3e), similar to the apparent effect of Mg^{2+} ions.
 480 On the other had, different from Mg^{2+} , DNA dimers and
 481 higher-order multimers did not appear significantly in the
 482 presence of Ag^+ ions. Instead, the band of the single-
 483 stranded DNA showed up in the presence of Ag^+ ions
 484 (indicated by the green triangle in Fig. 3d), suggesting
 485 that the DNA- Ag^+ interactions are different from the
 486 DNA- Mg^{2+} interactions. In addition, the emergence of
 487 the single-stranded DNA band indicates that Ag^+ ions

488 likely affect DNA hybridization, which is not surprising
 489 as Ag^+ ions have been found to interact with DNA bases,
 490 especially cytosine [31, 32], and possibly induce chain-
 491 slippage [33].

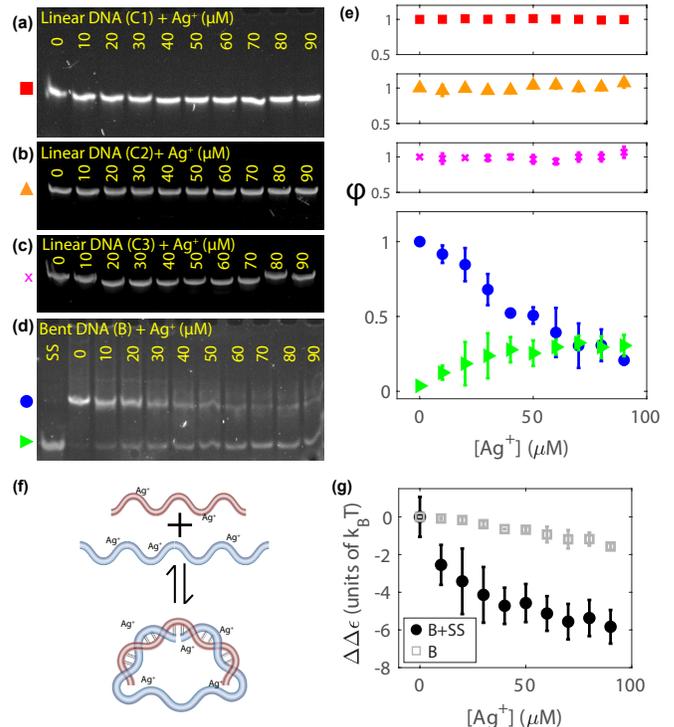


FIG. 3. Probing DNA- Ag^+ interactions using bent DNA ampli-
 fiers. (a-c) Gel electrophoresis for linear DNA controls
 in the presence of Ag^+ ions of 0– $90 \mu\text{M}$. a: construct C1, b:
 construct C2, c: construct C3. (d) Gel electrophoresis for bent
 DNA in the presence of Ag^+ ions of 0– $90 \mu\text{M}$. Lane SS: the
 long single-stranded DNA (45 bases) in the absence of Ag^+
 ions. (e) Dependence on Ag^+ concentration of the intensities
 of the bands indicated by the corresponding markers in panels
 a–d. Error bars stand for standard deviation of replicates. (f)
 Conversion (“reaction”) between bent DNA monomers (blue
 circles in panel d) and unhybridized single strands (green tri-
 angles in panel d). (g) Estimated change in the difference of
 free energy between the unhybridized single-strands and bent
 monomers as a function of Ag^+ concentration. Estimations
 were carried out using either the bent monomer band only (B,
 gray squares) or both the bent monomer and unhybridized
 single-stranded bands (B+SS, black circles).

492 To quantify the DNA- Ag^+ interactions, we focused on
 493 the hybridization “reaction” of DNA as shown in Fig. 3f.
 494 With Eq. (1) and the equilibrium condition $\mu_b = 2\mu_{ss}$,
 495 we have,

$$496 \quad \Delta\epsilon = 2\epsilon_{ss} - \epsilon_b = k_B T \ln \left(\frac{x_b}{x_{ss}^2} \right) \quad (7)$$

497 and

$$498 \quad \Delta\Delta\epsilon = \Delta\epsilon^+ - \Delta\epsilon^- = k_B T \left[\ln \left(\frac{x_b^+}{x_b^-} \right) - 2 \ln \left(\frac{x_{ss}^+}{x_{ss}^-} \right) \right] \quad (8)$$

499 If we normalize the molar fractions to the control (i.e.,
 500 $[\text{Ag}^+] = 0 \mu\text{M}$), $\varphi_b^- = \frac{x_b^-}{x_b^-} = 1$, $\varphi_b^+ = \frac{x_b^+}{x_b^-}$, $\varphi_{ss}^- = \frac{x_{ss}^-}{x_b^-}$, and
 501 $\varphi_{ss}^+ = \frac{x_{ss}^+}{x_b^-}$, we obtain

$$502 \quad \Delta\Delta\epsilon = k_B T \left[\ln \left(\frac{\varphi_b^+}{\varphi_b^-} \right) - 2 \ln \left(\frac{\varphi_{ss}^+}{\varphi_{ss}^-} \right) \right] \quad (9)$$

503 We estimated $\Delta\Delta\epsilon$ from the experimental data (blue cir-
 504 cles and green triangles in Fig. 3e) and found that $\Delta\Delta\epsilon$
 505 decreased with increasing $[\text{Ag}^+]$ as shown in Fig. 3g
 506 (black circles).

507 We note that the dependence of $\Delta\Delta\epsilon \sim k_B T \ln(\varphi_b^+)$
 508 (i.e., using the monomer band only) is also able to cap-
 509 ture the main feature of $\Delta\Delta\epsilon$ in the presence of Ag^+ ions
 510 (i.e., $\Delta\Delta\epsilon$ decreases as $[\text{Ag}^+]$ increases), as shown in Fig.
 511 3g (gray squares). However, unlike the result for Mg^{2+}
 512 ions, the estimations based on the $\Delta\Delta\epsilon \sim \ln(\varphi_b^+)$ depen-
 513 dence are quantitatively off. The reason for this deviation
 514 is that the intensities of the dimer bands stay constant
 515 in the presence of Mg^{2+} ions (green triangles in Fig. 2d)
 516 but the intensities of the single-stranded bands increase
 517 steadily in the presence of Ag^+ ions (green triangles in
 518 Fig. 3d).

519 IV. CONCLUSION

520 To conclude, we developed a simple and cost-effective
 521 method to amplify and probe the interactions between
 522 DNA and metal ions by taking advantage of mechan-
 523 ical energy stored in bent DNA molecules. We demon-
 524 strated these mechanical energy based amplifiers by ap-
 525 plying them to examine the interactions between DNA
 526 and Mg^{2+} ions, or Ag^+ ions. In addition, we showed
 527 that quantitative details about the DNA-metal interac-
 528 tions can be obtained with our method. This method is
 529 simple and convenient as the bent DNA molecules were
 530 self-assembled. Our method is cost-effective because it
 531 uses gel electrophoresis, a standard and commonly used
 532 biochemical technique. By perturbing the energy land-
 533 scape, our method amplifies the DNA-metal interactions,
 534 making it sensitive and capable of detecting the effect of
 535 metal ions on DNA that are not detectable using the
 536 same biochemical assay.

537 As a proof-of-concept, we have focused on our study
 538 on Mg^{2+} and Ag^+ ions. However, we expect that our
 539 method is readily applicable to other metal ions. As the
 540 concentrations of metal ions are important indicators of
 541 water quality, we expect that our method could be used
 542 for monitoring water quality. One advantage of our DNA-
 543 based method is biocompatibility. In addition to metal
 544 ions, it is likely that our bent DNA amplifiers can be
 545 used to investigate the interactions of DNA with other

546 chemicals, including organic molecules and reagents. In
 547 principle, it is even possible to develop our method into a
 548 convenient technique for screening DNA-targeting drugs.
 549 Furthermore, our method can be used for improving ex-
 550 isting assays and techniques in various applications, such
 551 as isolation of aptamers for metal ions [34].

552 The goal of this work is to demonstrate the princi-
 553 ple and feasibility of the developed method. However, it
 554 would be interesting to examine the method in more de-
 555 tails and to push the sensitivity of the method for further
 556 applications. For example, as it has been reported that
 557 nicks promote DNA base-pair disruption in bent double-
 558 stranded DNA molecules [16], an immediate question is
 559 how the metal ions affect the stability of the nicks, which
 560 could possibly be answered using our method with appro-
 561 priate designs (i.e., by varying the length and sequence)
 562 of the bent DNA. In addition, in combination with other
 563 techniques (such as fluorescence resonance energy trans-
 564 fer), the mechanical energy based amplifiers might be
 565 capable of examining the dynamics of the conversion be-
 566 tween smoothly bent DNA and sharply kinked DNA in
 567 the presence of nicks, as well as how the dynamics de-
 568 pends on the metal ions. Furthermore, we point out
 569 that our method is versatile to control the sensitivity,
 570 as the mechanical energy in the bent DNA can be mod-
 571 ulated conveniently by changing the length of the single-
 572 stranded part of the self-assembled DNA [13–15].

573 Finally, we point out that there are several ways to
 574 use our mechanical energy based amplifiers to examine
 575 interactions of DNA with metal ions, and likely other
 576 molecules. For example, DNA-metal interactions can be
 577 qualitatively reported by the visual changes in the gel
 578 electrophoretic patterns (Fig. 2a–e and Fig. 3a–e). In
 579 addition, the quantitative information about the DNA-
 580 metal interactions can be extracted (black circles in Fig.
 581 2g and 3g), especially when the underlying “reactions”
 582 caused by the metal ions are clear (Fig. 2f and 3f). Fur-
 583 thermore, the dependence of $\Delta\Delta\epsilon$ on the molar fractions
 584 of the bent monomers alone can semi-quantitatively re-
 585 port the interactions of DNA and metal ions, which po-
 586 tentially provides a convenient way in practice for look-
 587 ing at the interactions but without knowing the details or
 588 mechanisms. As a result, our method is expected to be
 589 versatile for various applications at different levels and
 590 complexity.

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