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Phys. Rev. E **97**, 062402 — Published 6 June 2018

DOI: [10.1103/PhysRevE.97.062402](https://doi.org/10.1103/PhysRevE.97.062402)

Entropy Analysis of Frequency and Shape Change in Horseshoe Bat

Biosonar

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ABSTRACT

Echolocating bats use ultrasonic pulses to collect information about their environments. Some of this information is encoded at the baffle structures – noseleaves (emission) and pinnae (reception) – that act as interfaces between the bats’ biosonar systems and the external world. The baffle beam patterns encode the direction-dependent sensory information as a function of frequency and hence represent a view of the environment. To generate diverse views of the environment, the bats can vary beam patterns by changes to: 1) the wavelengths of the pulses or 2) the baffle geometries. Here, we compare the variability in sensory information encoded by just the use of frequency or baffle shape dynamics in horseshoe bats. For this, we use digital and physical prototypes of both noseleaf and pinnae. The beam patterns for all prototypes were either measured or numerically predicted. Entropy was used as a measure to compare variability as a measure of sensory information encoding capacity. It was found that new information was acquired as a result of shape dynamics. Furthermore, the overall variability available for information encoding was similar in case of frequency or shape dynamics. Thus, shape dynamics allows the horseshoe bats to generate diverse views of the environment in the absence of broadband biosonar signals.

1 I. INTRODUCTION

2 Bats have mastered life in complex environments by relying primarily on their biosonar systems
3 to collect sensory information about the presence, location, and nature of sound sources in the
4 environment [1–3]. A good example of these capabilities are greater horseshoe bats (*Rhinolophus*
5 *ferrumequinum*), a species that is able to navigate in dense structure-rich vegetation [4, 5] and hunt
6 prey either in flight or by gleaning from surfaces [6, 7]. The sensory information required to
7 accomplish this must be encoded at the interfaces of the bats’ biosonar system and the external
8 world, i.e., as the emitted sounds exit the bat’s nostrils or as the returning echoes impinge on its
9 ears. The space-frequency characteristics of the emission and reception structures can be described
10 by a “beampattern”, a scalar-valued function that specifies the output or input gain of the system
11 as a function of spatial direction and frequency. Each beampattern can hence be seen as a space-
12 frequency filter that provides a certain view of the environment. The ability to generate different
13 beampatterns could help the bats to obtain different views of their environment in order to tailor
14 the received sensory information to their current needs.

15 Beampatterns are the result of a diffraction process in which the outgoing or incoming ultrasonic
16 wave packets interact with the surfaces of baffles shapes such as the noseleaves (emission) and the
17 outer ears (reception). Hence, the beampatterns are determined by the geometry of the diffracting
18 surface in conjunction with the wavelength of the diffracted sound. In principle, bats could utilize
19 two different kinds of mechanisms to change their beampatterns, i.e., by virtue of: (i) changing
20 the wavelength of their pulses or (ii) by changing the geometry of the diffracting surfaces. Bat
21 species with broadband ultrasonic pulses (frequency-modulated or FM-bats for short [7]) should
22 be in a good position to vary their beampattern shapes as a function of frequency. Their broad
23 frequency bands correspond to a likewise broad range of wavelengths that can interact with the

24 baffle shapes in different ways to generate significantly different beampatterns [8, 9]. In general,
25 beamwidth can be expected to decrease with increasing frequency resulting in a broader view of
26 the environment at lower frequencies and a narrower for high frequencies [10–13]. In addition to
27 the overall beamwidth, the shape of the beampatterns can depend strongly on frequency in terms
28 of lobes of the beampattern that can appear, disappear, or change position with frequency [13, 14].
29 Thus, as a result of all these possible variations in the beampatterns with frequency, objects that
30 are located at different angular positions in the environment will get illuminated by different signal
31 spectra that could impact the information that will be encoded in the returning echoes. Echo spectra
32 are known to encode information about the nature and location of targets [7, 12, 14–16]. As of now,
33 there is very limited evidence that FM bats have control over the shapes that diffract their emitted
34 pulses and the received echoes, an exception being the observation that certain FM bats (*Hypsugo*
35 *bodenheimeri*) can change their emission beamwidth by varying their mouth gape [12].

36 Horseshoe bats (family Rhinolophidae) are so-called CF-FM bats (for constant-frequency -
37 frequency-modulated [2]). Their biosonar calls consist of multi-harmonic signals, where each har-
38 monic is dominated by a long narrow-band portion (CF component) that is framed by a frequency
39 modulated (FM) component at the start and at the end [7].

40 However, the pulse energy in these calls tends to be concentrated in the CF component with the
41 FM component containing either comparatively low portions of the pulse energy or even being left
42 out completely on occasion [4, 17, 18]. In addition, all but the second harmonic in these multi-
43 harmonic biosonar calls are also relatively weak. This restricts the ability of such bats to generate
44 differing beampatterns due to variation of beampattern shape with frequency.

45 However, unlike what is currently known about FM-bats, CF-FM bats have a very conspicuous
46 dynamic dimension associated with the baffles that surround the sites of ultrasonic emission (nose-

47 leaves) and reception (pinna, see Fig. 1). These baffles can undergo fast non-rigid deformations
48 on time scales similar to the duration of individual pulse emissions and return echoes [19–21].
49 The deformations are a result of specific muscular action [22, 23] with deformation amplitudes
50 significant in comparison to the wavelength used [19–21].

51 Some of the recent studies have shown that the deformations of the emission and reception
52 baffles can bring about a significant change in the beampatterns (emission & reception) [13, 19,
53 21, 24, 27]. In addition, changes in the emission beampatterns of horseshoe bats during natural
54 biosonar behaviors have been recently reported, though the underlying physical mechanism re-
55 mains unknown [26]. Taken together, these studies suggest that dynamics is an important aspect
56 of bat biosonar. It could be hypothesized that the function of the dynamics in the emission and
57 reception baffle shapes of horseshoe bats is to produce a diversity in the views of the environment
58 that bats with great biosonar bandwidth can achieve by virtue of frequency changes.

59 The goal of the work presented here has hence been to compare the diversity introduced into
60 views of the environment by the use of either frequency or shape dynamics in horseshoe bats (*Rhi-*
61 *nolophous ferrumequinum*) through an information-theoretical (entropy) analysis of the beampat-
62 terns. The analyzed beampatterns were obtained from detailed digital prototypes of the natural
63 geometries of noseleaves [13, 24] & pinnae [21] as well as measurements using the biomimetic
64 physical prototypes [24, 27]. These four different models were considered to ensure that the phe-
65 nomena observed were robust functions of frequency or shape dynamics and not due to specific
66 features in one of the model system that may not apply to bats and may be hard to reproduce in
67 another experiment.

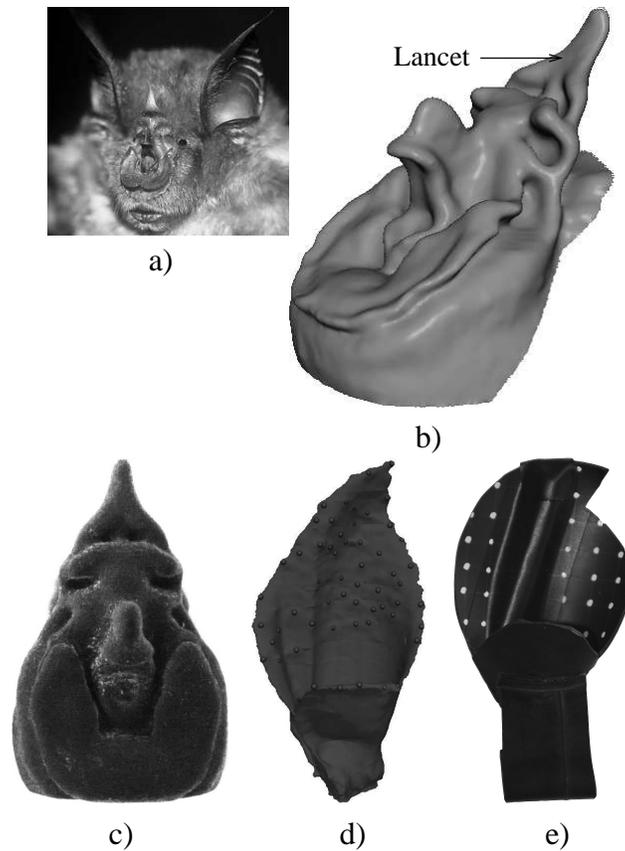


Figure 1. Different shape sample types used to obtain acoustic far-field (beampattern) data on the noseleaf and pinna dynamics of greater horseshoe bat : a) Portrait of a greater horseshoe bat (BP) b) Digital model used for computer animation of *in-vivo* bat noseleaf dynamics (NN), c) Exact deformable physical replica of the bat noseleaf created through 3D printing (PN, scaled $2\times$ BP) d) Digital pinna model used to recreate bat pinna dynamics (NP), e) Simplified deformable physical prototype of bat pinna (PP, scaled $2.5\times$ BP).

68 **II.. MATERIALS AND METHODS**

69 To obtain the shape data used in the present analysis, an adult greater horseshoe (*Rhinolophous*
 70 *ferrumequinum*) bat was taken from the caves in the vicinity of Jinan, Shandong Province, China

71 (latitude - $36^{\circ}40'05''$ N, longitude - $116^{\circ}59'49''$ E, elevation - 32 m) to serve as an experimental
72 subject. The animal was housed in an indoor enclosure during the experiments and noseleaf and
73 pinna motions were recorded using high-speed video cameras. In order to do the acoustic charac-
74 terization of shape deformations in the study subject, four models that included both digital and
75 physical prototypes of noseleaf and pinna were obtained. The models represented either the exact
76 biological or biomimetic motion.

77 The life-like digital models were obtained from μ CT scans of the noseleaf and pinna samples.
78 In order to recreate baffle dynamics observed in high-speed video recordings of the behaving bat,
79 different set of techniques were used for noseleaf and pinna respectively. For the noseleaf, the
80 digital model was computer-animated using skeletal animation techniques. This involved setting
81 up of a skeleton with control points and joints attached to the mesh such that it approximates ob-
82 served noseleaf motion in bats [24] (see Figs. 1(b), 2). For the pinna, a linear elastic finite element
83 model was used to combine the static pinna geometry with the three-dimensional time trajectories
84 of the landmark points (marked on pinna) extracted from video recordings of the behaving bat [21]
85 (see Fig. 1(d)). The acoustic properties (beampatterns) of the baffle shape deformations were then
86 numerically predicted [21, 24] (see Figs. 3, 4).

87 Like the digital noseleaf model, the geometry for the physical noseleaf prototype came from
88 μ CT scan and was reproduced in full biological detail. The geometry was scaled to twice the size
89 of horseshoe bat noseleaf and fabricated from an elastic material by 3D printing (Objet 3D printer).
90 The geometry was scaled to ease handling and permit use of lower frequencies. The prototype was
91 actuated by a simple linear actuator (Firgelli L12-1) that applied a force from behind to bend the
92 lancet of the noseleaf forward mimicking the motion observed in bats [24](see Fig. 1(c)).

93 However, unlike the physical noseleaf prototype, the geometry for the physical pinna prototype

94 was a simplified version (scaled $2\times$ the horseshoe bat pinna) of the biological pinna. It was fabri-
95 cated from an isobutyl rubber sheet and was actuated by a simple linear actuator (Firgelli L12-1)
96 like the noseleaf prototype. A force was applied from the pinna backside to mimic the motion
97 observed in bats [28] (see Fig. 1(e)).

98 The acoustic properties of all four models were characterized by beampatterns that were ob-
99 tained either by measurement [24, 28] or numerical prediction [21, 24]. These beampatterns were
100 acquired over a range of angles that spanned 180° in azimuth and 120° in elevation with a reso-
101 lution 3° . For all models, the beampatterns were obtained for five equidistant frequencies across
102 bats' biosonar frequency broadcast range (60-80 kHz). The frequencies were adjusted inversely to
103 compensate for the scaling of the respective physical models.

104 To compare the variability in the sensory information encoded across changes in frequency and
105 baffle shape (diversity of views), the beampatterns were characterized by kernel density estimates
106 (KDE) [29] of the probability density functions (PDFs) of the beampattern amplitudes. To compute
107 the KDE estimates of the amplitude PDFs, a Gaussian kernel was used. The size (bandwidth) of
108 the kernel was selected automatically using a plug-in type estimator [29–31]. The amplitude PDFs
109 computed by KDE to characterize the beampattern data were as follows:

- 110 1. Two-dimensional joint amplitude PDFs combining beampatterns associated with different
111 frequencies. One dimension of these PDFs was the beampattern amplitude at a reference
112 frequency of 60 kHz and the other the beampattern amplitude at one of the five frequencies
113 at which the bat's main biosonar band (60-80 kHz) was sampled. The values of the PDF
114 were estimated for 2501 points along each dimension. Joint PDF estimates were obtained
115 for each of the shape conformation stages in the studied sample.

- 116 2. Two-dimensional joint amplitude PDFs combining beampatterns associated with different
 117 shape conformation stages (see Fig. 5). One dimension of these PDFs was the beampattern
 118 amplitude associated with the upright shape change stage and the other the beampattern
 119 amplitude associated with one of the five stages in the entire shape change cycle. The values
 120 of the PDF were estimated for 2501 points along each dimension. Joint PDF estimates were
 121 obtained for each of the frequencies analyzed.
- 122 3. Five-dimensional joint amplitude PDFs where each dimension represented the beampattern
 123 amplitude for one of the five shape change stages in shape change cycle. Along each dimen-
 124 sion the PDF values were estimated for 2501 points. A separate five-dimensional joint PDF
 125 was computed for each of the analyzed frequencies.
- 126 4. Five-dimensional joint amplitude PDFs where each dimension represented one of the five
 127 equidistant frequencies in the bat's biosonar range (60-80 kHz). Along each dimension the
 128 PDF values were estimated for 2501 points. A separate five-dimensional joint PDF was
 129 computed for each of the stages in the shape change cycle represented in the sample.

130 For each of the above KDE of the amplitude PDFs, differential entropy [31, 32] (Eq. 1) was com-
 131 puted to quantify the differences in variability in the sensory information encoded by just the use of
 132 frequency and shape change respectively. If X_1, X_2, \dots, X_n are a set of jointly distributed contin-
 133 uous random variables with joint probability density function $f(x_1, x_2, \dots, x_n)$, the nonparametric
 134 estimate of joint differential entropy is given by Eq. 1.

$$\hat{h}(X_1, X_2, \dots, X_n) = -\frac{1}{n} \sum \ln(\hat{f}(x_1, x_2, \dots, x_n)) \quad (1)$$

135 where $\hat{h}(X_1, X_2, \dots, X_n)$ is the nonparametric estimate of joint differential entropy $h(X_1, X_2, \dots, X_n)$,

136 $\hat{f}(x_1, x_2, \dots, x_n)$ is the kernel density estimate (KDE) estimate of joint probability density function

137 $f(x_1, x_2, \dots, x_n)$ and n is the number of samples.

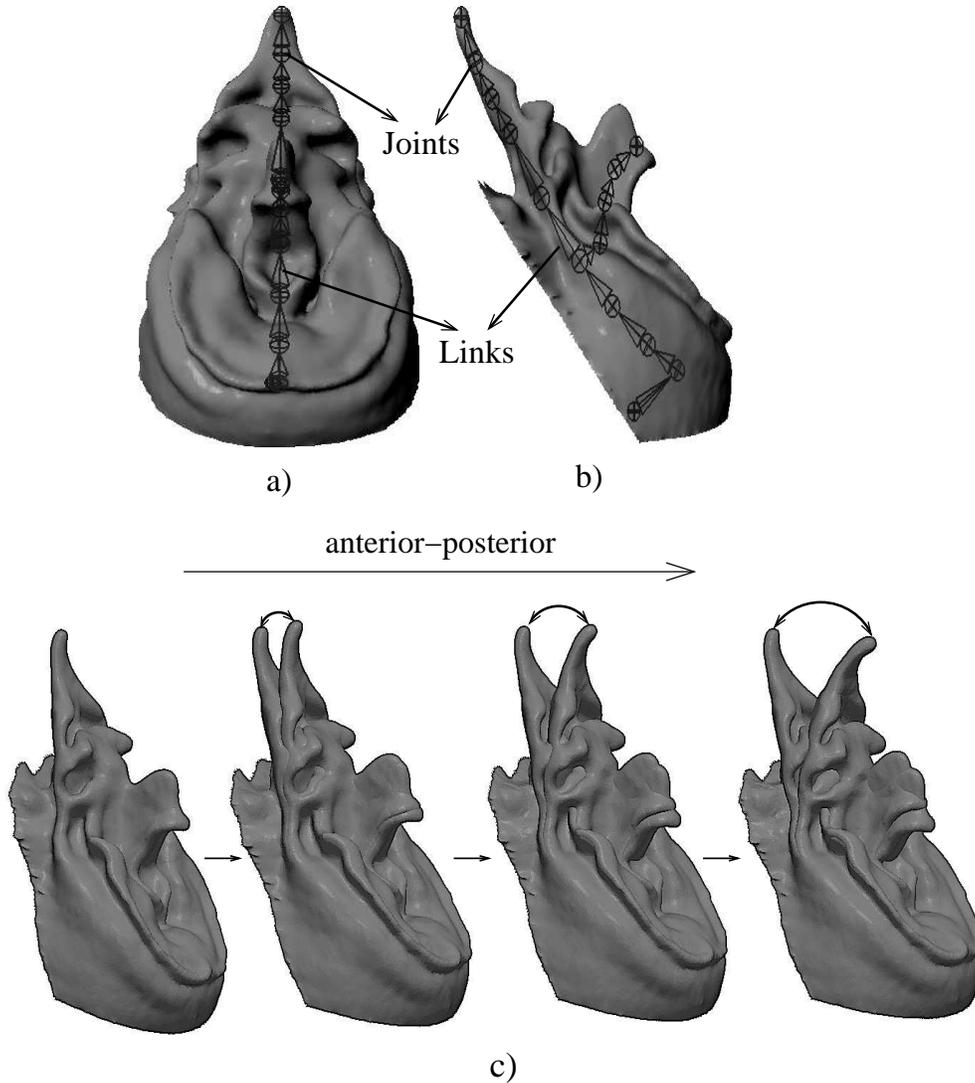


Figure 2. Digital rigged noseleaf model of greater horseshoe bat (*Rhinolophus ferrumequinum*): a) front view, b) side view, c) Lancet anterior-posterior motion recreated in digital bat noseleaf model using skeletal animation techniques (rigging).

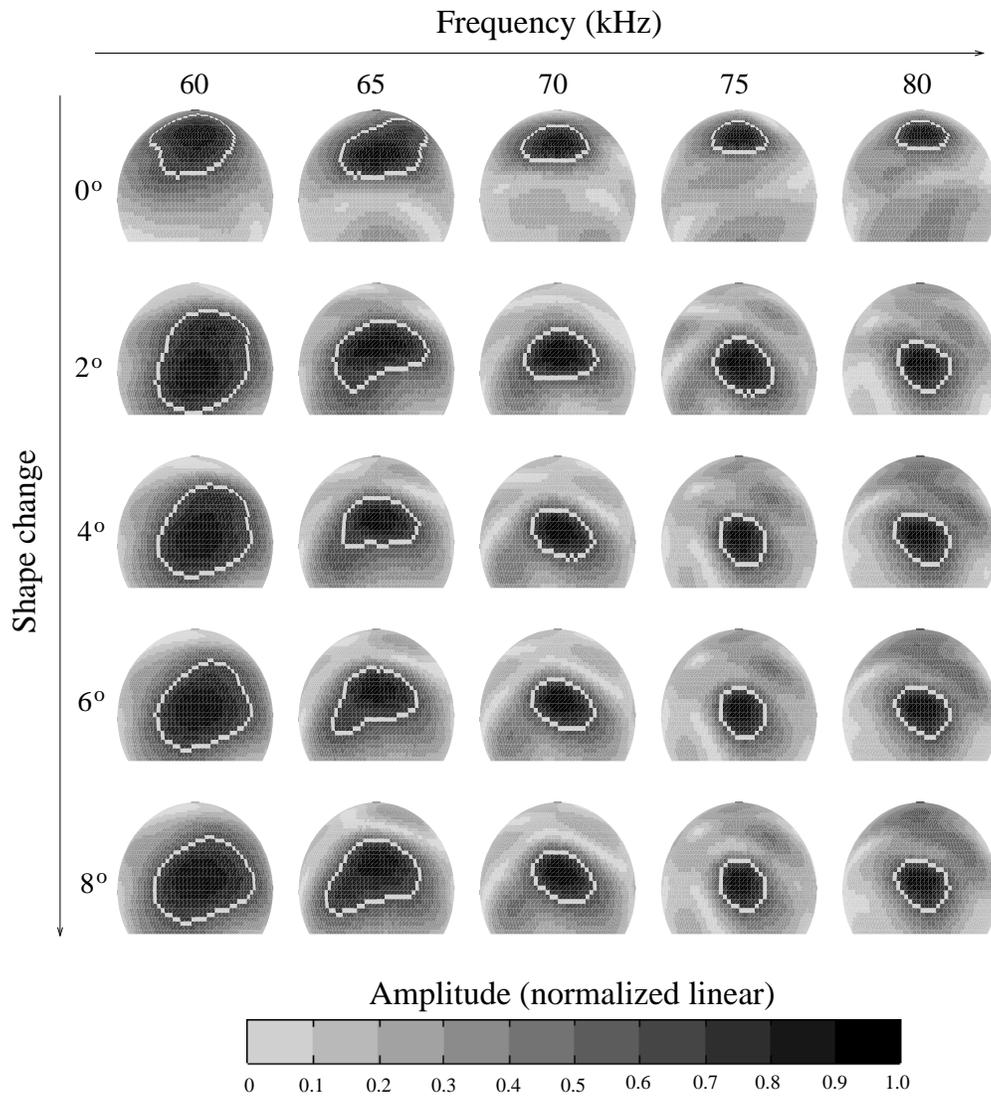


Figure 3. Numerically predicted beampatterns for the bat noseleaf digital model. Each row shows different lancet positions. Each column shows different frequencies. The gray-level coding is linear.

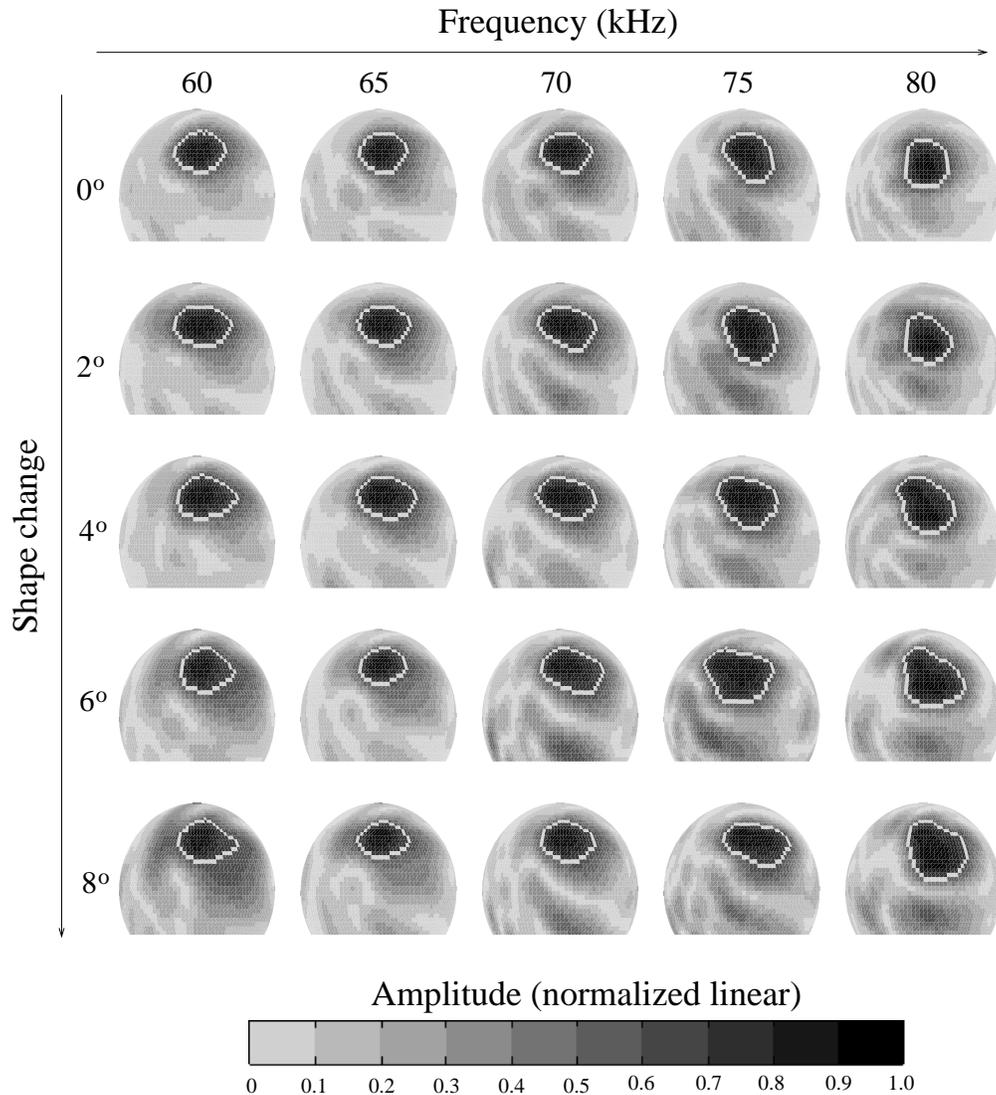


Figure 4. Numerically predicted beampatterns for bat pinna digital model. Each row shows different pinna positions. Each column shows different frequencies. The gray-level coding is linear.

138 III. RESULTS

139 The joint 2D probability density functions of the normalized beampattern amplitudes across
 140 shape change stages (Fig. 5) and across frequency (Fig. 6) were both found to deviate considerably
 141 from a diagonal structure which would indicate that no additional information encoding capacity

142 is created by adding frequencies or shape conformations. They were also far from uniform which
143 would maximize the joint information encoding capacity, but showed intricate patterns, i.e., the
144 beampattern amplitudes across different frequencies or shape conformations were found to have
145 complex statistical dependencies, evident in multiple ridges in the pdfs.

146 The patterns in the joint 2d pdfs differed between the shape conformations and the frequencies
147 indicating that the statistical dependencies are not the same for changes in shape and changes in
148 frequency.

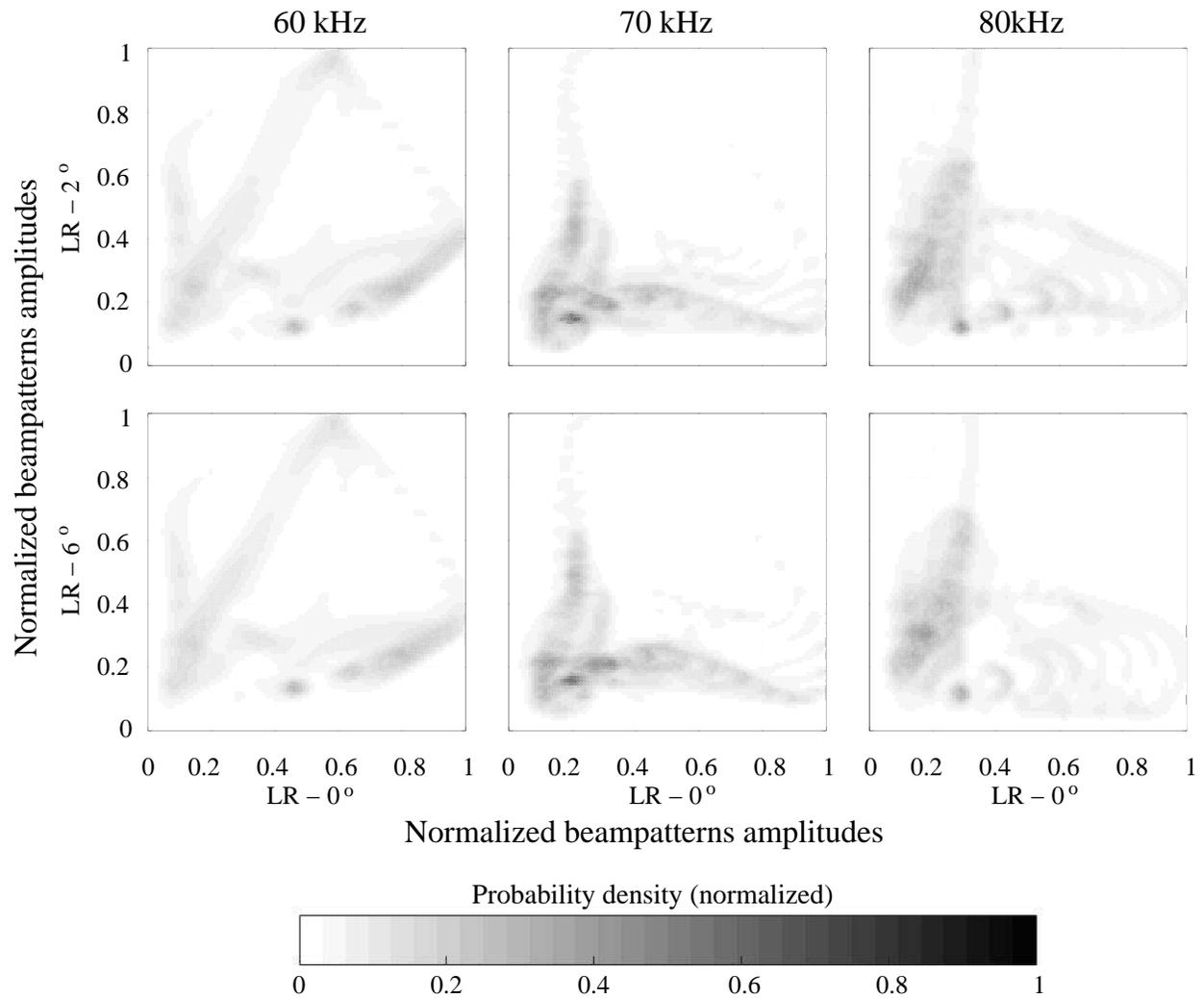


Figure 5. Joint probability density function across lancet shape change. The rows show the 2D joint probability density functions between the lancet upright stage ($LR - 0^\circ$) and subsequent shape change stages i.e. $LR - 2^\circ$ & $LR - 6^\circ$ respectively, in the shape change cycle. The columns show the joint pdfs between lancet shape change stages for multiple frequencies in bats' biosonar frequency broadcast range (60-80 kHz). Datasets used here are numerically predicted acoustic estimates for NN model. NN refers to the sample shown in Fig.1. LR refers to lancet rotation.

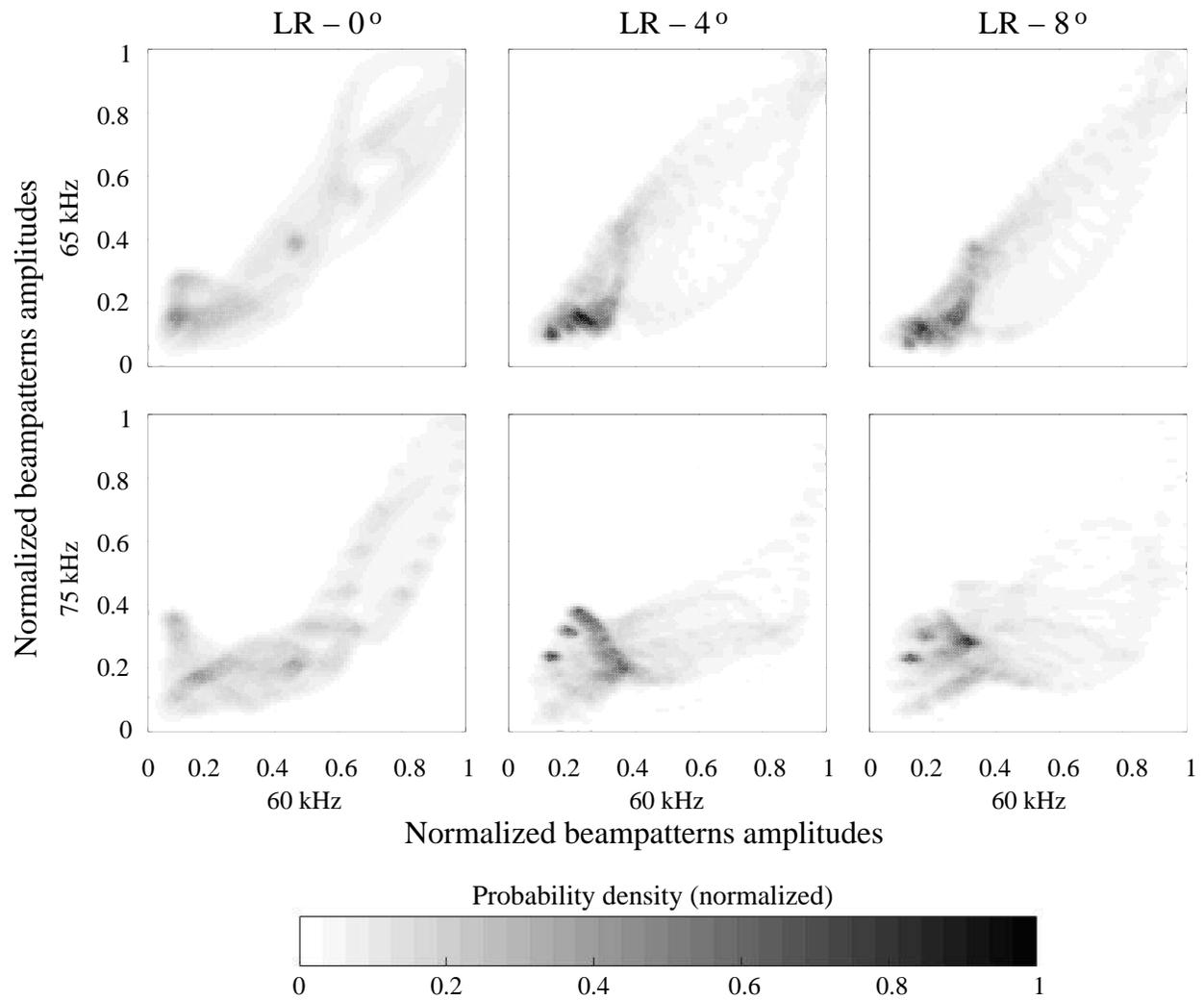


Figure 6. Joint probability density function across frequency. The rows show the 2D joint probability density functions between the lowest frequency (60 kHz) and subsequent frequencies, i.e. 65 kHz & 75 kHz respectively in bats' biosonar frequency broadcast range (60-80 kHz). The columns show the 2D joint pdfs between frequencies for multiple lancet shape change stages in the shape change cycle. Datasets used here are numerically predicted acoustic estimates for NN model. NN refers to the sample shown in Fig.1. LR refers to lancet rotation.

149 For changes in baffle shape, the joint entropy values estimated from the joint pdfs depended
 150 on the distance between the two shape conformations that were used to compute the joint entropy

151 (Fig. 7(a)). The further a tested conformation stage was separated from the upright stage that was
152 used as a reference, the larger the joint entropy between these two stages. With the exception of
153 the numerical noseleaf model (NN), an average increase of one bit (approx. 21%) in joint entropy
154 was observed between the upright stage and the farthest conformation stage across all models
155 (Fig. 7(a)).

156 The joint entropy values computed by combining different frequencies did not show the same
157 systematic dependence on distance between the compared beampatterns that was seen among the
158 changes in shape. For the frequencies, a reference frequency of 60 kHz was compared to five
159 frequencies spaced equally between 60 and 80 kHz. For all models, this comparison led to an
160 average joint entropy change of 0.4 bits (approx. 12%) between the lowest and highest entropy
161 values regardless of the spectral separation between the two frequencies (Fig. 7(b)).

162 To compare the variability in encoded information across all five shape conformation stages and
163 five frequencies, five dimensional joint pdfs were estimated for both cases, i.e., across frequency
164 and shape change. The entropy estimates for the joint pdfs across all five shape change stages and
165 five frequencies were found to be comparable, with an average difference in entropy of 1.2 bits
166 (approx. 8%) observed across all models (Fig. 8).

167 The different frequency and shape change configurations were additionally tested for a broad
168 range of SNR (signal-to-noise-ratio) values (-50 to -15 dB) to test the dependence of observed
169 effects on SNR. It was found that the effects of frequency and shape change were qualitatively
170 similar across all tested SNR values.

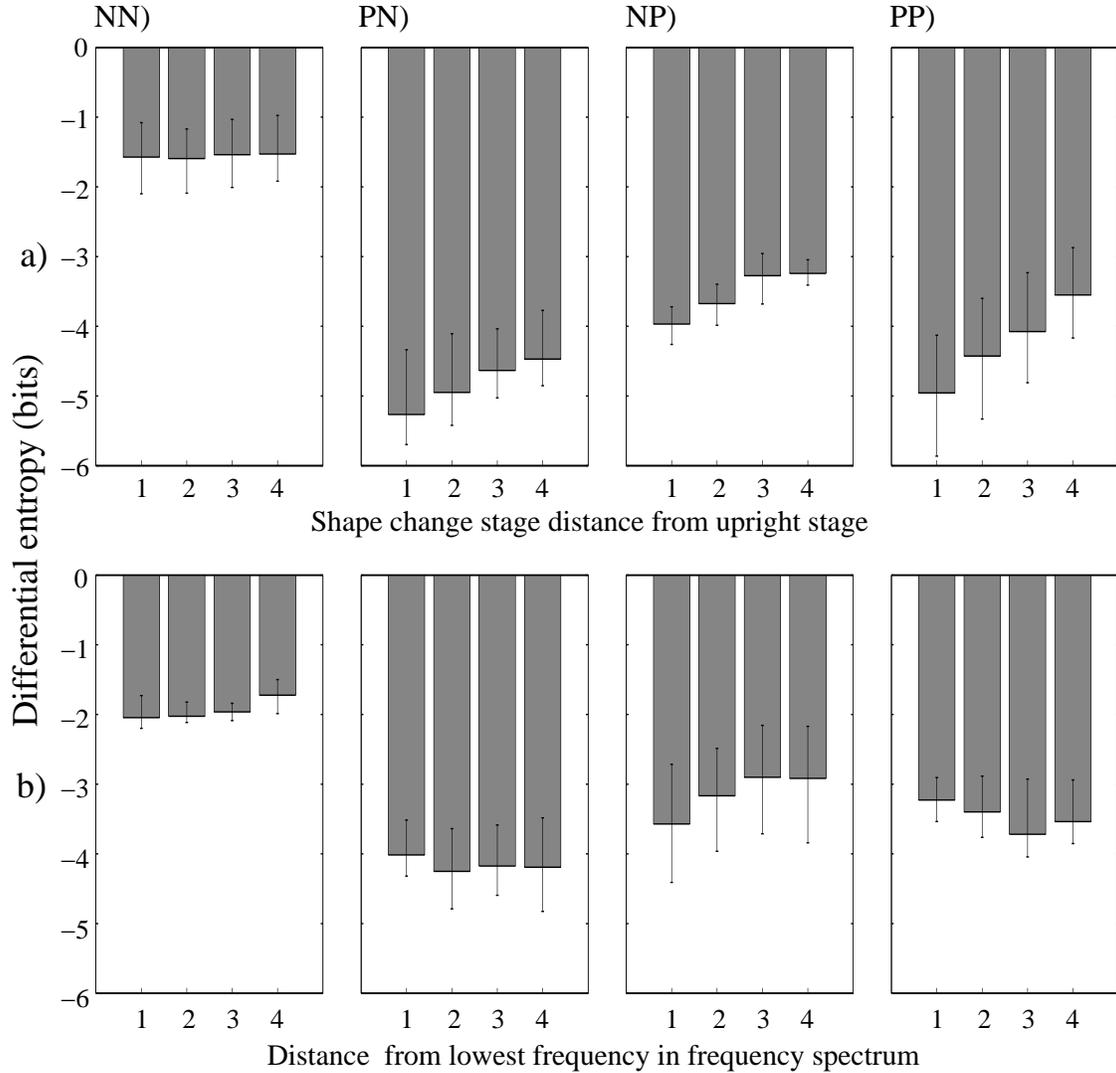


Figure 7. Average joint entropy estimates in bits. (a) From left to right, bar height represents the joint entropy estimate for a shape change stage with upright (reference) stage as a function of distance from the upright (reference) stage in shape change cycle (averaged over five equidistant frequencies between 60-80 kHz). (b) From left to right, bar height represents a joint entropy estimate for a frequency with lowest frequency (60 kHz) as a function of distance from the lowest frequency in bats' biosonar frequency broadcast range (60-80 kHz) divided into five equidistant frequencies (averaged over five stages in shape change cycle). Error bars indicate the minimum and maximum values of entropy. NN, PN, NP, PP refer to the samples shown in Fig.1.

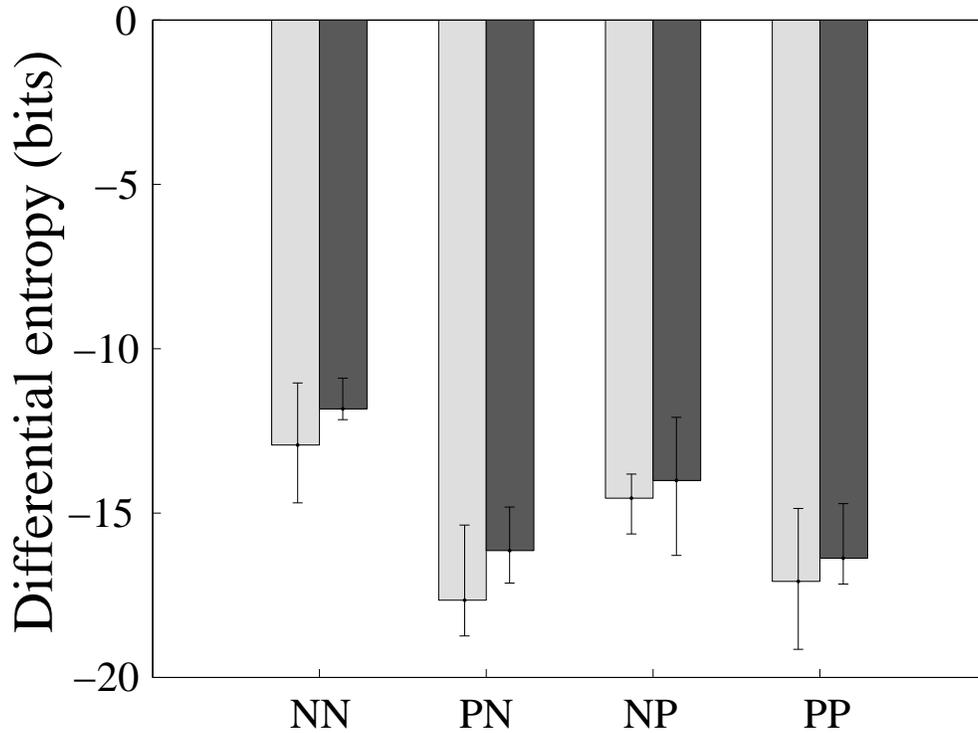


Figure 8. Pooled average entropy estimates in bits. Light gray bar height represents the joint entropy estimate across all the shape change stages (averaged over five equidistant frequencies between 60-80 kHz). Dark gray bar height represents the joint entropy estimate across all five equidistant frequency in bats' biosonar frequency broadcast range (60-80 kHz) (averaged over five stages in shape change cycle). Error bars indicate the minimum and maximum values of entropy. NN, PN, NP, PP refer to the samples shown in Fig.1.

171 **IV.. DISCUSSION**

172 In the results presented here, both shape change and frequency change were found to have an
 173 approximately equal effect on increasing the variability (entropy) of the sensory inputs.

174 Since the analysis presented here has been aimed at investigating the relative merit of frequency

175 and shape changes for sensory information encoding, it did not delve into how this sensory infor-
176 mation capacity could translate into performance into any given sensory task or how far such a
177 performance would be from an optimum solution. Since it is well established that spectral features
178 (i.e., changes over frequency) can support source localization in bats (e.g., [33]) and shape change
179 and frequency were found to have a similar effect on sensory information encoding capacity, it
180 can be hypothesized that the shape changes could also support the animal's need for direction-
181 dependent sensory information.

182 The joint probability density function estimates obtained here indicate that neither additional
183 shape conformations nor additional frequencies enhances information encoding capacity in an op-
184 timum way that would be given by a uniform joint PDF. This could be due to physical constraints
185 on changes that can be made to the shapes of a noseleaf or pinna, how much these changes can
186 influence the beampatterns, and how different beampatterns are possible. A recent study [34] has
187 shown that bat biosonar beampatterns are more variable than a random reference (irregular cones
188 made from crumpled aluminum foil) in terms of beamwidth which could be seen as an indication
189 that factors other than beamwidth have driven the evolution of these characteristics.

190 The only difference found between altering the beampattern based on frequency or shape
191 change was that whereas the differential entropy values increased with the distance between dif-
192 ferent shape conformations, they remained approximately the same between frequencies, i.e.,
193 regardless of the spectral distance between these frequencies. Since the change in wavelengths
194 (about 1.5 millimeter over the analyzed frequency band) were substantially less than the maximum
195 displacements associated with the changes in shape (several millimeters), this cannot be explained
196 by the amplitude of the geometrical changes. Instead, it could be hypothesized that the difference
197 is due to the local nature of the shape changes where only certain parts of the baffle being moved

198 versus the global nature of the frequency changes where the wavelength changes affect the entire
199 diffraction process.

200 The observed effects were found to be qualitatively similar across all four datasets despite the
201 differences in either experimental approach (numerical versus physical) or biological detail repro-
202 duced (life-like versus simplified). This suggests that the results are a robust function of either
203 overall shape dynamics or frequency and not due to methodological peculiarities as the datasets
204 have little in common in terms of experimental protocol.

205 The observed similarity between the variability that has been introduced by changes in baffle
206 shapes or frequency changes indicates that both types of changes could be equally well suited
207 for enhancing the encoding of sensory information through the diverse sets of beampatterns they
208 create. Hence, horseshoe bats could have two alternative mechanisms for increasing the amount of
209 sensory information they receive via their biosonar echoes: relying on the echoes to the FM-tails
210 of their biosonar pulses or changing the shape of their noseleaves and pinnae. The bats could use
211 both mechanisms for pulses that contain strong FM-tails and are accompanied by noseleaf and/or
212 pinna motions. They could rely on frequency diversity only for pulses that have strong FM-tails
213 but are not accompanied by any dynamic shape changes changes. Finally, the bats could rely on
214 shape diversity only in situations where the FM-tails are weak, but the CF-components of their
215 pulses are accompanied by dynamic changes in baffle shape. Only in cases, where the bats emit
216 pulses with a weak FM-tail and no shape changes would they be left with a minimum of monaural
217 information related to target direction.

218 The need to concentrate pulse energy in a narrow frequency band for the detection of Doppler
219 shifts could have been an evolutionary driving force behind the evolution of the noseleaf and pinna
220 dynamics in horseshoe bats. The narrower the frequency band of the pulses, the smaller the amount

221 of monaural, direction-related sensory information that the animals have access to. Noseleaf and
222 pinna deformation could hence be seen as evolutionary innovations to break this linkage between
223 bandwidth and the encoding of monaural direction information. The current findings affirm the
224 importance of biosonar dynamics in the biosonar system of horseshoe bats which is in accordance
225 with a host of recent studies: Dynamic changes in the shape of lancet [19], anterior leaf [20] and
226 pinnae [21] have been previously reported. These motions were found to occur on timescales of
227 individual pulses or echoes and have been hypothesized to have an effect on encoding of sensory
228 information [19–21]. Moreover, horseshoe bats have been shown to actively adjust beam width
229 during terminal stages of prey capture [26]. Furthermore, the shape changes in lancet and pinnae
230 have been previously reported to help encode additional information that significantly improves
231 the number of resolvable directions and accuracy of direction finding in horseshoe bats [35]. The
232 present findings give further credence to the hypothesis that dynamics plays an important role in the
233 encoding of sensory information. The current finding is particularly interesting as it suggests that
234 baffle shape change could be a novel way evolved by CF-FM bats to generate diverse beampatterns
235 to tailor the biosonar view to the task at hand in the absence of broadband biosonar signals.

236 **ACKNOWLEDGMENTS**

237 We thank Li Gao, Mittu Pannala & Yanqing Fu for sharing their numerical pinna, physical
238 pinna & physical noseleaf beampattern datasets. This work was supported through funding from
239 Virginia Tech’s Institute of Critical Technology & Applied Sciences (ICTAS), the National Sci-
240 ence Foundation (NSF grant IDs 1053130 and 1362886), the Army Research Office (grant num-
241 ber 451069), and the National Natural Science Foundation of China (grant numbers 11374192,
242 11574183, 31270414-1), the Chinese Ministry of Education (Tese Grant), and the Fundamental

243 Research Fund of Shandong University (No. 2014QY008).

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