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Phys. Rev. E **95**, 053211 — Published 24 May 2017

DOI: [10.1103/PhysRevE.95.053211](https://doi.org/10.1103/PhysRevE.95.053211)

Optimisation of Plasma Amplifiers

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Plasma amplifiers offer a route to side-step limitations on chirped pulse amplification and generate laser pulses at the power frontier. They compress long pulses by transferring energy to a shorter pulse via the Raman or Brillouin instabilities. We present the first extensive kinetic numerical study of the three-dimensional parameter space for the Raman case. Further particle-in-cell simulations find the optimal seed pulse parameters for experimentally relevant constraints. The high efficiency self-similar behaviour is only observed for seeds shorter than the linear Raman growth time. A test case similar to an upcoming experiment at the Laboratory for Laser Energetics is found to maintain good transverse coherence and high energy efficiency. Effective compression of a 10 kJ, nanosecond long driver pulse is also demonstrated in a 15 cm long amplifier.

Solid state grating pulse compressors are used in many petawatt laser systems to reduce the duration of a long chirped pulse. Due to their damage thresholds and considerations of pulse quality, the incident fluence is limited. The cost and complexity of the metre scale compressors poses a significant challenge for the proliferation and advancement of petawatt sources. The grating technology is mature, with advanced systems at LLNL [1] and OMEGA EP [2] giving high efficiency and phase control.

Optical parametric chirped pulse amplifiers (such as the Vulcan 10PW project [3]) promise power improvements in femtosecond pulses, but will also still be limited by the final compressor.

Continued development towards higher intensity pulses is motivated by applications in ultra-relativistic laser plasma experiments. For example, it was predicted that virtual pairs will produce vacuum birefringence [4], and solid targets will generate macroscopic matter-antimatter plasmas and kilojoules of gamma photons under irradiation approaching 10^{24} W/cm². This will require laser powers up to 100 PW.

High power laser pulses are also used to drive secondary sources such as betatron X-ray emission, GeV electron beams and neutron beams [5], however the repetition rate must be improved in order to compete with conventional technology. This could be better facilitated by plasma optics and compressors as there is no degradation over time. Better laser pulse compression would therefore lead to improvements in technology and advances in basic science concerning quantum-plasma effects and pair production.

Laser pulse compression in a plasma [6] will permit orders of magnitude reduction in size and cost of the compression medium. In addition, the requirements on the stretched pulse are greatly reduced as it is only used as a driver, in contrast to nonlinear optics methods with strict

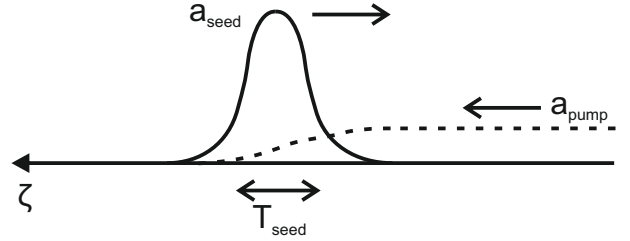


FIG. 1. Schematic of the Raman amplifier scheme in an under-dense plasma, where the long pump pulse (dashed) counter-propagates with a short seed pulse (solid line) downshifted from the pump by the plasma frequency. To achieve high energy transfer and pump depletion, as shown here, equation (4) must be satisfied.

beam requirements. These facts could facilitate scaling to currently infeasible pulse powers. Finally, Raman backward scattering is scale invariant with wavelength and therefore compresses long ultra-violet pulses as effectively as infra-red light, a clear advantage over gratings. High energy ultra-violet short pulses would dramatically lower the requirements for inertial confinement fusion. The fast ignition scheme intends to ignite a compressed fusion fuel pellet within the 30 ps before it disassembles [7, 8]. However, efficient laser to fuel coupling is only realistic using these shorter wavelengths.

The Raman amplifier scheme, illustrated in Fig. 1, transfers energy from the long pump pulse, frequency ω , to the short counter-propagating seed pulse. This is achieved by overlapping the pulses in an underdense plasma to excite beneficial Raman backward scatter-

ing. A counter-propagating geometry maximises the interaction length as well as the instability growth rate. The seed frequency is downshifted from the pump by the plasma frequency $\omega_p = \sqrt{ne^2/(\epsilon_0 m_e)}$, where $n \simeq n_{crit}/100$ is the plasma electron number density, n_{crit} is the critical plasma density and other symbols have their usual meanings. As a result, the beating of the two waves at frequency ω_p will resonantly excite an electron plasma wave through the ponderomotive force. The plasma wave has a slow phase speed of approximately $c\omega_p/(2\omega)$ and a wavelength approximately half that of the pump pulse. The pump pulse will then scatter from the plasma wave and amplify the shorter pulse, reaching powers greatly in excess of its pump pulse.

Previous studies have verified the high energy transfer efficiency with a variety of numerical methods and approximations [9–11], however a full prescription of optimal parameters (including the short seed pulse) is needed. In this paper we present the first extensive numerical study that uses a fully kinetic code to assess the amplifier efficiency across all three main parameters. These are the pump pulse intensity, the plasma electron density and electron temperature. The performance is limited by kinetic effects across a large region of the parameter space. However, even with temperatures typical of experimental pre-formed plasmas, high efficiency is achievable. We then present a further performance improvement based on tailoring the seed pulse.

The self-similar solution of Malkin *et al.* [6, 12] gives the seed pulse envelope and its evolution in the advanced non-linear amplification stage. The seed power greatly exceeds the pump pulse power, the pump is significantly depleted and the energy transfer converges to a constant rate. The condition for this behaviour can be simply derived from the coupled envelope equations for the three wave process [6, 13]:

$$2\frac{\partial a_{pump}}{\partial \zeta} = \omega_p a_L a_{seed} \quad (1a)$$

$$\frac{\partial a_L}{\partial \zeta} = -\omega a_{pump} a_{seed}^*/2 \quad (1b)$$

$$\frac{\partial a_{seed}}{\partial t} = -\omega_p a_L^* a_{pump}, \quad (1c)$$

where (for linear polarisation) $a_{seed} = 8.55 \times 10^{-10} \sqrt{I_{seed} \lambda_{\mu m}^2}$ is the dimensionless seed pulse peak amplitude, with the peak intensity $I_{seed}(t)$ in units W/cm^2 , a_{pump} is the same for the pump pulse, and a_L is the Langmuir plasma wave amplitude normalised to $m_e c \omega_p / e$. The equations are taken in the moving frame such that t is the propagation time and $\zeta = t + x/c$ is the coordinate in the frame moving with the seed pulse. We have neglected the temporal derivatives in the first two equations, i.e.

$$\frac{\partial a_{pump}}{\partial \zeta} \gg \frac{\partial a_{pump}}{\partial t}, \quad (2)$$

thus finding the behaviour in the limit that the seed pulse duration is much shorter than its timescale of evolution. The approximate solution is found by taking a constant real amplitude seed pulse. We may find the time taken for full pump depletion by differentiating (1a) and substituting equation (1b) to give

$$\frac{\partial^2 a_{pump}}{\partial \zeta^2} + \frac{\omega \omega_p}{4} a_{seed}^2 a_{pump} = 0. \quad (3)$$

The solution is

$a_{pump}(\zeta) = a_{pump}(0) \cos(\sqrt{\omega \omega_p} a_{seed} \zeta / 2)$, meaning full pump depletion is achieved at the first zero when $a_{seed} T_{seed} \sqrt{\omega \omega_p} \simeq \pi$, where T_{seed} is the seed pulse duration given by the full width at half maximum of the power envelope. Importantly, it is a condition on the seed pulse only, suggesting that achieving high efficiency from the start of the amplifier requires careful preparation of an intense seed pulse. The more thorough self-similar derivation [6, 13] gives

$$a_{seed} T_{seed} \sqrt{\omega \omega_p} \simeq 5. \quad (4)$$

This condition is an attractor; once it is met, it continues to hold throughout the non-linear regime. The pulse therefore shortens and gains bandwidth as its intensity grows, typically to sub-picosecond duration. Experimental attempts have had some success in reaching this non-linear behaviour, however none have achieved the full potential of the scheme [14–18].

I. OPTIMAL EFFICIENCY

The efficiency theoretically converges to a value of $1 - \omega_p/\omega$ in the non-linear regime, found from the Manley-Rowe relations [19]. In practice, plasma kinetic effects will cause a convergence to a lower value [20, 21]. These effects are heavily dependent on the laser dimensionless amplitude, plasma electron density and temperature.

Fig. 2 indicates the limited efficiency, as found from 1,200 one-dimensional particle-in-cell (PIC) simulations covering the parameter space. These simulations initialise a large number of macro-particles, each representing many electrons. These evolve according to their self consistent electromagnetic fields which are calculated on a Cartesian grid. As such, there are no appreciable approximations to the physics apart from artificial noise levels and the available grid resolution. These simulations accurately model kinetic effects and relativistic corrections, but the following loss mechanisms are not included: collisional damping, competing plasma instabilities of the seed pulse, and spontaneous Raman and Brillouin scattering of the pump pulse before it encounters the seed.

The pump dimensionless amplitude a_{pump} and plasma density were constant in each simulation and the seed pulse initially met the non-linear condition (4) with dimensionless amplitude $a_{seed} = 0.1$ and central frequency

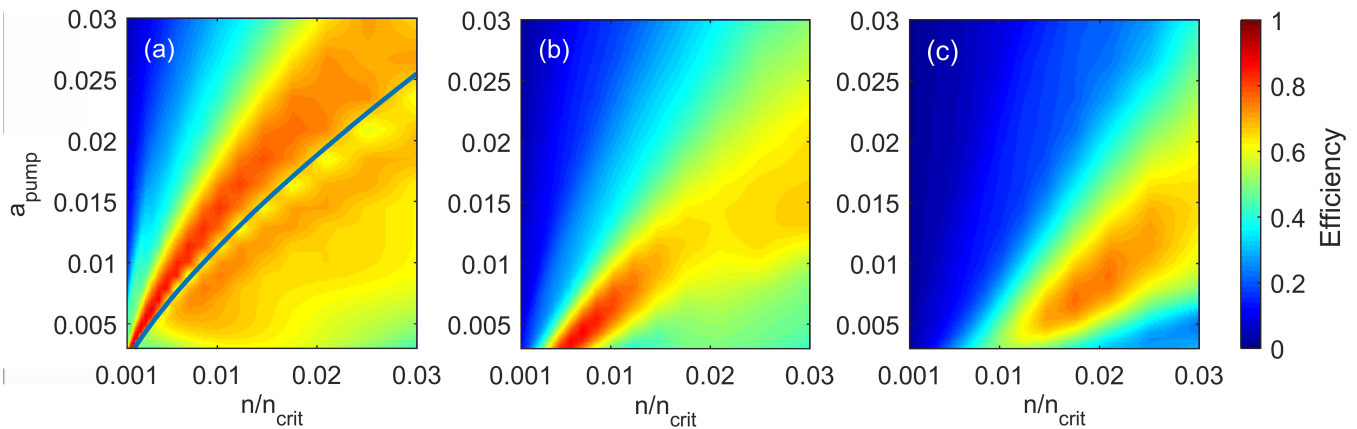


FIG. 2. (Colour) Simulated energy transfer efficiency of Raman compression, including kinetic effects, for the three different electron temperatures of (a) 0 eV, (b) 100 eV, and (c) 400 eV. The plots show the maximal amplifier efficiency in the non-linear regime, as found from 1,200 one-dimensional particle-in-cell simulations covering the parameter space. The pump pulse dimensionless amplitude is a_{pump} and the plasma electron density n is normalised to the pump pulse critical density. Above the theoretical Langmuir wave-breaking threshold for cold plasma (blue solid line), the amplifier efficiency rapidly decreases.

$\omega - \omega_p$. The efficiency is defined as the change in seed energy divided by the total pump energy it has propagated through, taken at a time when this has converged to a constant value. Only the energy of the main amplified spike was considered, neglecting any pre-pulse or trailing secondary spikes. Neutralising ions were kept static and the seed and pump polarisations were linear and aligned. Simulations used the code OSIRIS [22] with 60 cells and 480 particles per wavelength with cubic interpolation.

Some consideration must be given to unphysical numerical effects that could be present in the simulations. Artificial numerical electron heating occurs for Debye lengths shorter than the grid spacing. For the 100 eV and the 400 eV simulation the Debye length was resolved, and for the cold plasma case this effect was negligible due to the continuous initialisation of new plasma at the leading edge of the simulation box, which moved along with the seed pulse. The typical timescale for the numerical heating is $> 1000\omega_p^{-1}$, but the amplified pulse encounters newly initialised plasma after just $20\omega_p^{-1}$. This was confirmed with observation of the macro-particle phase space diagrams.

Particle trapping effects may also be over estimated as a result of the accumulation of interpolation errors. This increases the spread of particle momentum, thus artificially increasing the likelihood of a macro-particle becoming trapped in the plasma wave [23]. As a result, higher order interpolation methods reduce this source of error, so a cubic interpolation technique was employed. To verify convergence, several simulations were repeated with 10 times the particle number, with only minor differences seen in the low power trailing parts of the amplified pulse. Since the high power main peak is of primary interest for an amplifier, the particle number employed for the main parameter scan is sufficient. The final pulse energies agreed to within 5%.

When the plasma wave is over-driven, a large proportion of electrons exceed the wave phase velocity and the wave will become turbulent and break, ending the energy transfer [11]. This will occur [24] for pump dimensionless amplitudes above $a_{pump} = 0.35(n/n_{crit})^{0.75}$, shown by the solid blue line on the cold plasma case in Fig. 2. Beyond this threshold, the amplifier efficiency rapidly decreases [25–27], also consistent with recent Vlasov simulations [28]. For a given density, the peak efficiency is close to $1 - \omega_p/\omega$ and occurs slightly beyond the theoretical wave-breaking threshold.

For increasing electron temperature, the wave-breaking threshold decreases due to the distribution having a larger number of particles exceeding the plasma wave’s phase velocity [29]. This effect was clear when the study was repeated with electron temperatures 100 eV and 400 eV, shown in Fig. 2b,c. The optimal region is localised and is a strong function of temperature, suggesting good characterisation and control of experimental plasma conditions is necessary. Furthermore, temperature increases due to collisional damping of the pump pulse must be considered.

For higher temperatures, thermal motion of the electrons can also cause particle trapping and the plasma wave is Landau damped. This limits the optimal region towards regions of higher plasma density, where the plasma wave phase velocity is greater. The analytical condition that the wave phase velocity greatly exceeds the electron thermal velocity yields $n/n_{crit} \gg 4K_B T/(m_e c^2)$. This is well matched to the regions of highest efficiency at temperatures 100 eV and 400 eV.

Considering Fig. 2, there is a clear advantage to maintaining a low temperature, as a wider range of plasma density is then accessible. Many studies [30–35] have focussed on the scheme where the pump or a pre-pulse ionises and heats the plasma, ruling out the benefits of a

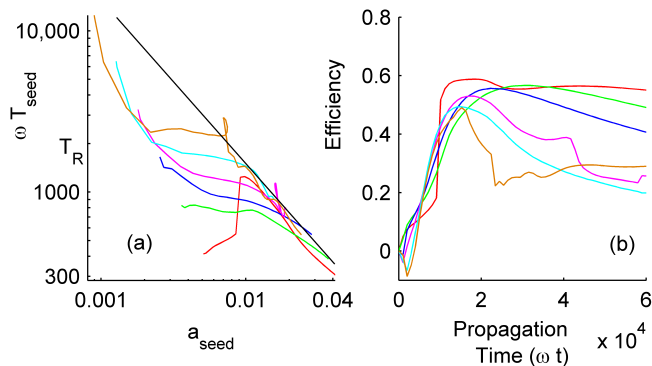


FIG. 3. (Colour) Investigation of the optimal seed pulse with six one-dimensional PIC simulations. The plasma had zero temperature and constant density $n = n_{crit}/100$, with constant pump amplitude $a_{pump} = 0.003$. The development of six seed pulses, varied in initial duration at constant energy, is shown with a separate colour for each seed pulse. (a) The development of the duration versus the dimensionless peak amplitude of each seed on logarithmic scales. Equation (4) is shown by the black line. The total propagation time was $60000\omega^{-1}$ for each seed pulse. (b) The energy transfer efficiency from the pump to the main peak of the seed pulse, as a function of propagation time. Note that the peak efficiency of 0.6 agrees with Fig. 2.

low temperature interaction. A promising alternative is to keep the pump below the ionisation threshold, so the plasma is only ionised once the higher intensity seed arrives [36, 37]. The seed duration is similar to the electron thermalisation time, so the effective longitudinal temperature of the interaction is low compared to the pump ionisation scheme. There is also the added benefit of minimising the ionised volume, which reduces losses and unwanted pre-pulse from premature pump back-scatter [38, 39].

II. OPTIMAL SEED PULSE

Following Trines *et al.* [13] we now present a numerical investigation to optimise the initial seed pulse duration. We assumed the typical experimental constraint of constant seed pulse energy (i.e. constant $a_{seed}^2 T_{seed}$) and constant bandwidth.

Subject to these constraints one can always lengthen the seed until it satisfies equation (4), or choose a shorter, more intense pulse, right down to its bandwidth limited duration. It is shown here that, for experimentally relevant conditions, the optimal performance is obtained for the shortest seed pulses.

In neglecting temporal derivatives (equation 2), the derivation of the nonlinear behaviour assumed a seed pulse shorter than the characteristic growth time for lin-

ear Raman backward scattering [40]

$$T_R = \frac{2}{a_{pump}\sqrt{\omega\omega_p}}. \quad (5)$$

This means the self-similar behaviour could break down for seed pulses longer than T_R , even if they satisfy equation (4).

We investigated the domain of the high efficiency self-similar behaviour with further one-dimensional simulations. The pump amplitude was constant at $a_{pump} = 0.003$ and the plasma assumed pre-ionised, with zero temperature and uniform density $n_{crit}/100$. The simulations used a window moving with the seed pulse, with 120 cells and 960 particles per wavelength. Boundary conditions were free space.

Six simulations, each with a chirped Gaussian seed (frequency 0.9ω) of differing initial duration, were propagated for $\omega t = 60000$. These parameters were chosen to reflect a new Raman amplification experiment [41] at the Laboratory for Laser Energetics (LLE, address on p.1) and reside in the high efficiency region of the parameter space.

The development of the seed pulses in the a_{seed}, T_{seed} plane is shown in Fig. 3a. The solution (4), shown by the straight black line, accurately describes the later evolution of all seed pulses. Furthermore, its attractive nature is verified by seeds that start away from the line.

There is evidence that the analytic solution is only partially true for seeds longer than T_R , as they initially deviate from the line, before rejoining at around $\omega T_{seed} = \omega T_R \simeq 2000$. The pulses longer than T_R exhibited the undesirable characteristic of breaking in to several amplified pulses, whereas the shorter seeds gave a much higher power single spike. The evolution of the longer pulses showed dependence on small changes in the initial conditions, suggesting large shot to shot variation.

The energy transfer efficiency to the most prominent peak is shown versus propagation time in Fig. 3b. For some cases, it drops at later stages due to the energy transfer to other competing amplified spikes. By the end, the shortest seed (red) reaches over three times the power and twice the energy than for the longest seed (orange). This is true despite starting further from the attractive solution (4). The self similar behaviour is not observed unless $T_{seed} < T_R$.

As noted previously [28, 42], more intense seeds also work better beyond the wave-breaking threshold. We conclude that short and intense seed pulses are preferable to a much longer seed that satisfies equation (4). The pulse should certainly be shorter than T_R to avoid breaking in to two amplified pulses. These conclusions are for seeds with a fixed fluence and bandwidth.

If a seed pulse must ionise the plasma, it would likely need to be compressed to a short duration $T < T_R$ for the requisite ionisation intensity, but these results show this is also the condition for best amplifier performance.

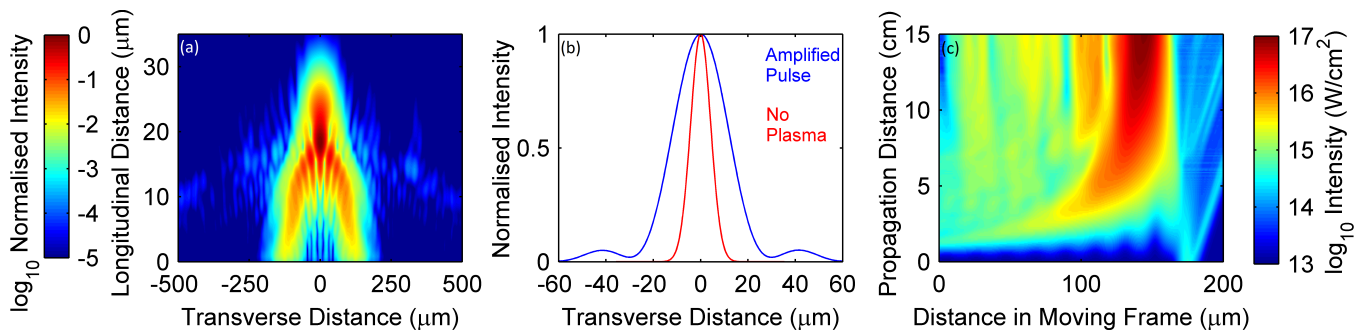


FIG. 4. (Colour) (a,b) A two-dimensional simulation of a primary stage amplifier with finite focal length, demonstrating that the process is possible in a focusing geometry and that transverse coherence is retained. (a) shows the amplified pulse at the time of best focus in vacuum, propagating upwards, whereas (b) compares this transverse profile (at the position of peak intensity) with that of the seed pulse focussed with no plasma interaction. The plasma profile had the form $1.5 \times 10^{19} \exp[-(x/2 \text{ mm})^6] / \text{cm}^3$, meaning $n/n_{crit} = 0.015$, with fixed temperature 400 eV. The seed and pump were Gaussian in space and time, with durations 50 fs and 25 ps, wavelengths 1200 nm and 1054 nm, both with peak intensity $3 \times 10^{14} \text{ W/cm}^2$ in the plasma ($a_{pump} = 0.016$). Both pulses had transverse width $800 \mu\text{m}$ in the plasma and focus 15 mm beyond the plasma. (c) Output similar to the first stage amplifier in (a), albeit at a shorter wavelength, is used to seed a larger secondary stage amplifier using the seed ionisation scheme, simulated in one-dimension. The simulation used a 10 kJ, 1 ns, 1054 nm pump pulse at 10^{13} W/cm^2 and a 15 J, 50 fs, 1081 nm seed pulse at $3 \times 10^{14} \text{ W/cm}^2$. The electron density was $6 \times 10^{17} / \text{cm}^3$ ($n/n_{crit} = 0.0006$) across a $1 \times 1 \times 15 \text{ cm}$ region. The intensity across the space time diagram is shown in a frame moving right, at the group velocity of the amplified pulse.

Further simulations (not shown) found that changing the shape of the temporal envelope for the seed had little effect compared to changing the duration.

III. TRANSVERSE COHERENCE

We now investigate adverse effects of the plasma on the transverse coherence of the amplified pulse. A two-dimensional PIC simulation amplified the pulse in a focusing geometry (as originally illustrated in reference [6]) and then propagated to its focus in vacuum.

Fig. 4a,b shows the intensity profile at the focus of the amplified pulse, together with the equivalent profile in the control simulation with no plasma. The peak intensity has been normalised to compare the two spot sizes. Parameters were chosen to reflect the ongoing experiment at LLE as closely as possible and they are close to the optimal values found in the previous sections. The simulation box moved with the seed pulse. Its width was 1.3 mm and length was $70 \mu\text{m}$, with 30 cells per wavelength, cell width 450 nm and 16 electrons per cell. The seed pulse duration of 50 fs is less than the linear Raman growth time of 200 fs, satisfying the conclusions of Fig. 3.

This PIC result agrees with the numerical results in references [43, 44] in that the amplified pulse largely retains its focusing geometry and coherence. The total energy transfer efficiency from pump to seed was 30%, consistent with Fig. 2. This high value is largely due to the powerful initial seed pulse, with power comparable to the pump.

Since the amplified pulse is far above the threshold power for relativistic self focusing, choice of lower laser intensities reduces the filamentation growth rate and preserves the wavefront fidelity. Analytical esti-

mates confirm this. Energy conservation gives $\eta a_{pump}^2 t = a_{seed}^2 T_{seed}$ for efficiency η . Combining with equation (4) and the filamentation growth rate [45] gives the growth rate $\gamma_{fil} = \eta^2 a_{pump}^4 \omega_p^3 t^2 / 200$. Integrating over propagation time gives an estimate of the maximum length of amplifier before the pulse filamentation becomes unbearable:

$$\frac{L}{\lambda} = \frac{1}{2\pi} \left(\frac{600G}{\eta^2 a_{pump}^4} \right)^{\frac{1}{3}} \left(\frac{n}{n_{crit}} \right)^{-\frac{1}{2}}, \quad (6)$$

where G is the maximum tolerable number of e-foldings. Taking $G = 5$, the maximum length is 1.1 cm for the simulation in Fig. 4a, over double the interaction length. This agrees with the low levels of filamentation seen in the simulation.

Relativistic self-focusing moved the position of best focus from 15 mm to 12 mm after the centre of the plasma, suggesting that even with minimal filamentation there could be large variations in the focal position. This could be alleviated by a seed pulse with a tighter focus than simulated here.

These results are important for using the technique to focus to frontier level intensities. It also means the output is ideal as a seed for a larger main amplifier stage with a nanosecond pump pulse. The wide bandwidth developed will give some freedom to use a lower electron density for the larger amplifier and still maintain resonance.

Fig. 4c simulates a hypothetical secondary amplifier stage using the seed ionisation scheme. For this main amplifier, the simulations included a field ionization model for hydrogen. It calculates the field ionised fraction at each time-step and initialises free electrons accordingly, with a transverse velocity of $0.05c$.

The seed and pump had energy 15 J and 10 kJ respectively. This one-dimensional moving window simulation used 120 cells and 960 electrons per wavelength. At this low density, ionisation causes little energy loss and it quickly enters the high efficiency nonlinear regime after 3 cm, with a total pump to seed energy transfer of 50%. The pulse envelope remains smooth. The pump will not be adversely affected by the neutral hydrogen gas as the full B integral was estimated at 0.02 [46]. Extrapolated transversely, the output contains 5 kJ in 60 fs. Such a pulse would be invaluable for high field experiments.

Transverse ponderomotive filamentation of the amplified pulse is unlikely to be an issue [47]. Equation (6) gives the maximum length before excessive filamentation as 36 cm, more than double the plasma length. Maintaining wavefront fidelity will necessitate a uniform plasma density. However for many applications (fast ignition, X-ray generation), exquisite focusing is less important than maximising the energy of the pulse, as lower intensities are sometimes desirable.

Compression of ultra-violet pulses is also feasible. A seed pulse with wavelength 355 nm could be used with a 351 nm, 10 kJ pump pulse such as those currently available on the National Ignition Facility. Neglecting losses from any collisional damping, the results of Fig. 4c apply equally to amplifiers at shorter wavelengths. This is provided that the intensities and the plasma density are scaled proportional to λ^{-2} . With a critical surface much closer to the dense hydrogen fuel, short ultra-violet pulses will reduce the required energy and open new windows for fast ignition.

In summary, we have performed the first exten-

sive parameter scan for the optimal performance of plasma amplifiers for compression of large amounts of nanosecond duration energy ($> \text{kJ}$) into sub-picosecond pulses. We have conclusively demonstrated that the choice of initial seed greatly influences the ascent into the nonlinear regime, allowing rapid access to high efficiencies. The simulations predict an efficiency for the LLE experiment of 30% with pump ionisation or 50% with the seed ionisation scheme. Good focusing has been explicitly demonstrated for an output pulse. We have discussed how a two stage plasma amplifier could represent a step change for generation of high energy short pulses for high energy density science.

ACKNOWLEDGMENTS

This work has been carried out within the framework of the EUROfusion Consortium and has received funding from the Euratom research and training programme 2014-2018 under grant agreement No 633053. This work has also been funded by EPSRC grant number EP/L000237/1 and by STFC. This work was also supported by the U.S. Department of Energy, Office of Fusion Energy Sciences Award No. DE-SC-0016253. The authors would like to thank the Osiris consortium and the staff of the Central Laser Facility and Scientific Computing Department at STFC Rutherford Appleton Laboratory. This work used the ARCHER UK National Supercomputing Service (<http://www.archer.ac.uk>) and STFC's SCARF cluster, totalling 5000 CPU-days.

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