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FLOW-INDUCED SEPARATION IN WALL TURBULENCE

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One of the defining characteristics of turbulence is its ability to promote mixing. We present here a case where the opposite happens – simulation results indicate that particles can separate near the wall of a turbulent channel flow, when they have sufficiently different Schmidt numbers without use of any other means. The physical mechanism of the separation is understood when the interplay between convection and diffusion, as expressed by their characteristic time scales, is considered, leading to the determination of the necessary conditions for a successful separation between particles. Practical applications of these results can be found when very small particles need to be separated or removed from a fluid.

I. INTRODUCTION

Separation of particles in a flow field is important in many processes, such as biological analysis, environmental assessment and food processing. As the number and applications of microfluidic devices increase, different separation techniques, both passive and active, have been employed not only in the laboratory but also in industry. While passive techniques only rely on the flow field and device geometry, active techniques utilize effects of external fields for better performance [1]. Some popular passive techniques are pinched flow fractionation (PFF) [2-4], inertia and dean flow fractionation [5,6], membrane-based methods [7-11], and hydrodynamic filtration [12,13]. Active techniques could use electric fields [14-17], centrifugal forces [18,19], or different types of external field as in field-flow fractionation [20-23].
In most of these cases, the flows are at rather low Reynolds number. On the other side, separation of particles in turbulence has not been explored. Instead, particle transport related issues have been investigated with a focus on turbulent mixing [24-26] and particle dispersion [27-32]. This is because the fluctuating velocity in turbulence usually leads to rapid mixing, instead of separation. In this work we present the opposite, the case where particles can be separated in turbulence without using any means other than the turbulent flow field.

II. NUMERICAL METHODOLOGY

A numerical method that involves a combined direct numerical simulation (DNS) of the flow field and Lagrangian scalar tracking (LST) of mass markers is used. The pseudo-spectral DNS algorithm documented by Lyons et al. [33], and validated with experiments by Gunther et al. [34] is implemented. All variables are made dimensionless using the friction velocity, $u^*$, and the kinematic viscosity of the fluid, $\nu$, namely, the viscous wall units. The dimensions of the computational box are $4\pi h \times 2h \times 2\pi h$ in the streamwise, $x$, normal, $y$, and spanwise, $z$, directions, respectively, where $h = 300$ is the half channel height. The computational box is meshed with $256 \times 129 \times 256$ grid points in the $x$, $y$ and $z$ directions. The Reynolds number based on the mean centerline velocity and half of the channel height is 5,700. The channel is simulated as infinitely long in $x$ and $z$ and with periodic boundary conditions with periodicity lengths of $4\pi h$ and $2\pi h$, respectively. No-slip and no-penetration boundary conditions are imposed at the rigid channel walls. The fluid flowing in the channel is an incompressible Newtonian fluid with constant density and viscosity.

Scalar markers that represent mass particles are released into the flow field. These markers are passive and do not affect the flow field, which is realistic for dilute solutions. The tracking algorithm of Kontomaris et al. [35] is used to track individual trajectories of these markers in space and time in a Lagrangian framework, in conjunction with the DNS. The combined DNS/LST approach has been previously used to study heat transfer in high Prandtl or Schmidt number fluids [36,37]. Discussion about the accuracy of this method and comparisons of the results with experimental findings can also be found in previous publications [38-41].

Mass markers are released into the flow field after the velocity field reaches steady, fully developed state. If $\vec{V}(\vec{x}_0, t)$ is the Lagrangian velocity of a particle that was at location $\vec{x}_0$ at time $t = t_0 = 0$, then the position $\vec{X}(\vec{x}_0, t)$ of the marker at time $t$ is calculated based on the equation

\[
\vec{X}(\vec{x}_0, t) = \int_0^t \vec{V}(\vec{x}(\vec{x}_0, \tau), \tau) d\tau + \vec{x}_0,
\]
At this point we make a basic assumption that a marker at any time has the velocity of the fluid particle on which it rides, which means that the relation between the Lagrangian velocity and the Eulerian velocity $\mathbf{U}$ is

$$\mathbf{V}(\mathbf{x}_0, t) = \frac{\partial \mathbf{X}(\mathbf{x}_0, t)}{\partial t}$$

(1)

Since the mass markers can move off a fluid particle due to molecular diffusion, the diffusion effect has been represented by adding a random walk on the marker motion after each simulation time step. The value of the diffusion step is estimated by a Gaussian distribution in each space direction with a zero mean and a standard deviation, $\sigma$, depending on the Schmidt number, $Sc$, ($\sigma = \sqrt{2\Delta t^*/Sc}$) where $\Delta t^*$ is the time step of the simulation. Multiple values of $Sc$ are examined ($Sc = 0.1, 0.7, 6, 20, 50, 100, 200, 500, 1000, 2400, 7500, 15000, 30000, 40000, \text{and } 50000$) representing different substances. For each $Sc$, 10000 markers are released instantaneously at the entrance of the computational box ($x = 0$). The markers are distributed with uniform spacing ($2\pi h/10000$) from a line in the spanwise direction. To study the effect of the vertical position of release, markers are also released at different elevated locations, $y_o = 0, 1, 2, 4, 5, 7, 9, 11, 13, 14, \text{and } 15$ wall units away from the bottom wall.

III. RESULTS AND DISCUSSION

a. Flow-induced separation

With the term flow-induced separation we mean that turbulence in a flow field can be used for particle separation when different particles have different diffusivity. Previous results in our laboratory have shown that markers with lower $Sc$, released at the channel wall, would diffuse into the flow field faster than markers with higher $Sc$ [40]. This effect is clearly shown in Figure 1, in which positions of markers with $Sc$ of 0.1 and 500 at different times are displayed. Both types of markers were released into the turbulent flow field from the bottom wall ($y_o = 0$), at the same line ($x = 0$) and at the same time. The markers painted green are the markers with $Sc = 0.1$ and the crimson markers have $Sc = 500$. It is seen that the $Sc = 0.1$ markers form a leading cloud, while a trailing cloud is formed by the $Sc = 500$ markers. This is caused due to the differences in the diffusivity of the two types of particles. Low $Sc$ markers have high molecular diffusivity, so they can diffuse with larger Brownian random motion jumps away from the near-wall region, where they can get convected by the larger turbulent velocity fluctuations in the $y$
direction and by larger mean velocity in the streamwise direction. High $Sc$ markers have low diffusivity and they cannot leave the region next to the channel wall as fast as the lower $Sc$ markers, so they are trapped in a low velocity region for a long time.

At this point, it is convenient and necessary to define an overlap region based on the streamwise location of the clouds of markers with the two different $Sc$. The overlap region is the region between the slowest moving marker of the leading cloud and the fastest moving marker of the trailing cloud. The number of markers from each cloud within the overlap region can be used to quantify the separation of the two clouds. In Figure 1, as time advances, a clear separation can be observed between the leading and the trailing clouds. Eventually, however, the trailing cloud will catch up with the leading cloud forming a short overlap region. This happens because at some point in time several markers from the trailing, high $Sc$ cloud, will leave the viscous sublayer close to the channel wall and will start moving fast due to the turbulent mean flow, while some of the low $Sc$ particles will diffuse back in the viscous wall region and will move slower than the rest of the particles of their type. The number of particles present in the overlap region reduces to zero when separation occurs, and becomes some finite number when the trailing cloud catches up with the leading cloud.

To explore the effects of $Sc$ on particle separation, the number of markers in the overlap region of two clouds is shown in Figure 2 for several cases with different $Sc$. In all these cases, the $Sc = 0.1$ markers always form the leading cloud, while the trailing cloud is formed by markers with $Sc = 0.7, 6, 50, 500$ or $50000$. All markers are released simultaneously from the channel wall, at $y_0 = 0$. It is apparent that the two clouds with the largest $Sc$ difference show the least number of markers in the overlap region for the longest time. As the $Sc$ for the two clouds becomes comparable, there does not exist a time at which the overlap region disappears and separation does not occur. See Supplemental Material at [URL will be inserted by publisher] for full animations of the cloud motion.)
Figure 1: Locations of markers with $Sc = 0.1$ (green) and 500 (crimson) at different times from their simultaneous release: a) $t = 50$; b) $t = 100$; c) $t = 220$. Clear separation between the two clouds is observed in panel (b), while a thin overlap region is observed at $x \approx 1000 - 1200$ in panel (c). Only the bottom half of the channel is shown, from $y = 0$ to 300. See Supplemental Material at [URL will be inserted by publisher] for full animations of the cloud motion.)
Figure 2: Number of markers in the overlap region, $N_{ov}$, when markers with $Sc = 0.1$ are released simultaneously with markers of different $Sc$. a) Number of markers from the leading cloud, $Sc = 0.1$; b) Number of markers from the higher $Sc$ trailing cloud.

Markers are also released from different sources elevated away from the wall at locations mentioned previously. In Figure 3, we show the number of markers from the leading cloud, in (a), and trailing cloud, in (b), that are in the overlap region for markers with $Sc = 0.1$ and $Sc = 2400$ released at $y = 0$, $5$ and $15$. It is obvious that separation occurs most effectively when the markers are released from the wall.
Figure 3: Number of markers in the overlap region when markers with $Sc = 0.1$ and 2400 are simultaneously released at different initial vertical positions; a) markers of the leading cloud; b) markers of the trailing cloud.

**b. Separation Mechanism**

The question that arises now is what the mechanism behind this type of separation is, and whether there is any constraint for a successful separation. Herein, we consider the two clouds to be separated if less than 0.5% of the total number of markers of any cloud (leading or trailing) is present in the overlap region. It has been shown above that if the two $Sc$ are too close to each other, separation would not occur. In Table 1, we present the minimum value of the higher $Sc$ for each of the lower $Sc$ in order for separation to occur. To smooth out fluctuation effects in the instantaneous flow fields, three different simulations with different initial velocity fields were used to calculate the reported results, which were determined as average values from the three runs.

The physics of why the separation occurs can be revealed when one considers the development of an instantaneous cloud of particles released in a turbulent flow field – this cloud
is usually called a puff. Careful experiments have shown that there are different zones of
development of a puff, which are distinct based on the physical mechanism of dispersion that is
dominant in each zone [42,43]. Simulations have also shown that when markers are released into
the flow field, they move through three stages: zone I, in which molecular diffusion dominates
dispersion; zone II, which is a transition zone; and, finally, zone III, in which turbulent
convection dominates dispersion. Within zone I there is a zone in which 95% of particle
displacement happens because of molecular diffusion. The average time spent by markers of
different $Sc$ in this first zone, $\tau_{95}$, and the time at which the particles move into zone III, $\tau_{III}$, are
also included in Table 1, as obtained through the following empirical equations [40]:

$$\tau_{95} = 8.34 \times Sc^{0.38} \quad (2)$$
$$\tau_{III} = 101.2 \times Sc^{0.35} \quad (3)$$

Table 1: Summary of cases of low and high $Sc$, in which separation is observed using the 0.5%
purity criterion. The transition times $\tau_{95}$ and $\tau_{III}$ are also presented.

<table>
<thead>
<tr>
<th>$Sc$ ($\tau_{III}$)</th>
<th>0.1 (46)</th>
<th>0.7 (90)</th>
<th>6 (190)</th>
<th>20 (289)</th>
<th>50 (398)</th>
<th>100 (507)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low $Sc$ ($\tau_{95}$)</td>
<td>100 (48)</td>
<td>500 (89)</td>
<td>7500 (248)</td>
<td>15000 (323)</td>
<td>30000 (420)</td>
<td>40000 (468)</td>
</tr>
</tbody>
</table>

The ratio $R_t$ of the $\tau_{III}$ of the low $Sc$ over the $\tau_{95}$ of the high $Sc$ of all successful
separation cases is related to the separation time (defined as the time at which separation begins,
$\tau_S$). The correlation obtained is shown in the following equation and plotted in Figure 4

$$\tau_S = a \times \exp(b \times R_t^2) \quad (4)$$

with values of the two parameters found to be $a = 11$, $b = 2.5$.

The ratio $R_t$ in Equation (4) gives information about the difference of the relative motion
of markers with these two $Sc$. It is observed that separation will happen faster if this ratio
becomes smaller. If the ratio is smaller than 1 (which happens for successful separation cases), it
is implied that markers with lower $Sc$ enter zone III before the markers with higher $Sc$ leave zone
I. Turbulent convection is the dominant transport mechanism in zone III – this means that the
leading cloud gets accelerated by turbulent convection before the trailing cloud exits the
molecular diffusion regime. This process would cause the two clouds to separate. The two cases
that have this ratio slightly larger than 1 (1.01 and 1.08) are very close to the limit for classifying
a case as successful separation (99.5% of the clouds are separated). For this study, where we defined separation as the point at which 0.5% or less of a cloud can be in the overlap region, the upper limit of $R_t$ is 1.08. If the ratio gets higher, more markers with high $Sc$ would leave zone I before markers with low $Sc$ enter zone III. Because of that, more high $Sc$ markers accelerate and catch up with the low $Sc$ markers and the needed purity constraint will not be satisfied.

![Figure 4: Separation time as a function of the ratio $R_t$ of the $\tau_{III}$ of the low $Sc$ over the $\tau_I$ of the high $Sc$. The solid line is Equation (4).](image)

Since the times for zone transitions occur as a function of $Sc$ in Equations (2) and (3), the limit 1.08 of the time zones ratio can be expressed as a relationship between the $Sc$ of the particle cloud pairs. In order to have separation then, it is required that

$$\frac{Sc_{Low}}{Sc_{High}} \leq 0.001 * Sc_{High}^{0.09}$$

(5)

Given the separation criterion of 0.5% and Equation (5) as a constraint for achieving separation, this method could be employed in practice. For example, consider the separation of colloidal particles (with radii between 1nm and 1µm) in water at room temperature. Using the equations below [44], one can calculate the corresponding $Sc$ of a particle with a given size, as

$$D_{AB} = \frac{\kappa T}{6\pi \mu_B R_A}$$

(6)
where \( D_{AB} \) is the diffusivity of particle A in the continuous phase B, \( T \) is the absolute temperature, \( \kappa \) is the Boltzmann constant, \( R_A \) is the radius of the spherical particle A, \( \mu_B \) is the dynamic viscosity and \( \nu \) is the kinematic viscosity of the continuous phase. Since the \( Sc \) depends linearly on the radius, one can easily calculate the ratio of \( Sc \), and check whether Equation (5) is satisfied.

As an example, this method could be applied to separate viruses from red blood cells in normal saline 0.9% as the continuous phase. This is an example that is offered as a proof of concept calculation. Given that the diffusivity value of red blood cells in water is \( 10^{-13} \) \((\text{m}^2/\text{s})\) [45], and assuming that the viscosity and density of normal saline are equal to those of water due to very low concentration of sodium chloride, the corresponding \( Sc \) of red blood cells in saline is about \( 10^7 \). Different types of viruses, with diameters ranging from 10nm to 100nm [46], would have \( Sc \) from 23,445 to 234,450 (for instance, the diameter of HIV virus is 100nm and the \( Sc \) is 234,450). Therefore, if a mixture of red blood cells and viruses is released in pulses into a flow field, the viruses will leave the cells behind (with the high \( Sc \) equal to \( 10^7 \)). Using Equation (5), it is obvious that some types of viruses will not satisfy the 0.5% criterion for separation. Significant separation will, however, occur in the overlap region, and then one can achieve further separation by repeating the process several times.

c. A model for particle displacement

Einstein [47] developed the following relation for molecular dispersion in a non-turbulent field

\[
\frac{dX^2}{dt} = 2D,
\]

where \( D \) is the molecular diffusivity and \( X \) is the displacement from the source. The most influential contribution to the theory of dispersion in a turbulent field is Taylor’s description of the dispersion of particles from a point source in a homogeneous, isotropic turbulence [48]. With respect to anisotropic turbulent flows, Batchelor [49] modified Taylor’s theory to predict the statistical behavior of a cloud dispersed from a source in a turbulent boundary layer. We examine here whether Taylor dispersion can be used to reproduce the simulation results and whether particle separation can be predicted based on Taylor’s and Batchelor’s models, bypassing the need to conduct DNS and LST.
First, we examine the mean displacement of the particles in the streamwise and vertical directions. Results for selected $Sc$ are presented in Figure 5. It is obvious, however, that differences in the mean values of streamwise displacement should not be used alone in predicting separation with a criterion like the 0.5% criterion used above, since they only represent mean positions of the clouds without any indication of the spread of the clouds in $x$.

![Graph a)

Figure 5: Mean displacement of particles with different $Sc$ in: a) streamwise direction; b) vertical direction. Data obtained from LST simulations.
The displacement of particles in the vertical direction plays a significant role in determining streamwise velocity and position of a cloud. As previously described, particle clouds go through three different zones of development after they are released from a source at the wall. It appears that for every $Sc$ the transition to zone III occurs when $\bar{Y} \approx 30$. At that point, at $t = \tau_{III}$, the cloud enters the zone where turbulent convection dominates the dispersion process. Identifying the proper dispersion mechanism in each zone would help build a model to predict displacement in the channel. In zone I, our earlier study found that dispersion in the direction of the velocity gradient, $y$, agrees well with the theory of Einstein and Taylor [40]. Since molecular diffusion is the dominant mechanism in this zone, we propose the following model for the mean vertical displacement:

$$\bar{Y} = C \times Sc^d t^e \quad \text{for } t < \tau_{05} \quad (8)$$

The model contains the effect of molecular motion only. As previously discussed, the value of the diffusion step is estimated by a Gaussian distribution in each space direction with a zero mean and a standard deviation, $\sigma$, which is proportional to $Sc^{-1/2}$. The exponent $d$ in Equation (8) can therefore be chosen to be $d = -\frac{1}{2}$. The coefficients $C$ and $e$ were then found to be 0.89 and 0.55, respectively, by fitting the equation with our LST data, as seen in Figure 6.

![Figure 6: Prediction of vertical displacement in zone I: comparison between the model of Equation (9) (lines marked with open circles) and LST results (lines without any markings).](image)
In the case of shear flow, as is the case with our channel geometry, Batchelor suggested that the following expression can be used to predict the average motion of particles dispersing in the turbulent constant stress region [49]

\[ \bar{V} = \frac{d\bar{y}}{dt} = bu^* \quad (9) \]

where \( b = 0.2 \) should be a universal constant according to Batchelor. This expression implies that particles with different \( Sc \) will have the same mean vertical velocity. Plotting \( \bar{Y} \) versus time for different \( Sc \) in the log layer region (\( \bar{Y} \geq 30 \) or \( t \geq \tau_{\text{III}} \)) can be used to compare our LST data to Batchelor’s prediction, as seen in Figure 7. It is observed that particles move in the vertical direction with almost constant velocities, though particles with different \( Sc \) have slightly different velocities, and low \( Sc \) particles tend to have higher velocities initially that decreases as time increases. Because of this, we propose that the Batchelor constant \( b \) has values that depend on the \( Sc \), as shown in Table 2. These values agree well with previously published results by different authors [50-52].

![Figure 7: Mean vertical displacement of particles in the log layer. Data obtained from LST simulation.](image-url)
Table 2: Batchelor’s constant $b$ for different $Sc$

<table>
<thead>
<tr>
<th>Sc</th>
<th>$b$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>0.3</td>
</tr>
<tr>
<td>0.7</td>
<td>0.3</td>
</tr>
<tr>
<td>6</td>
<td>0.25</td>
</tr>
<tr>
<td>20</td>
<td>0.2</td>
</tr>
<tr>
<td>50 and above</td>
<td>0.15</td>
</tr>
</tbody>
</table>

Though diffusion mechanisms of particles in the vertical direction within zone I and zone III have been identified with corresponding description [Equations (8) and (9)], diffusion in the transition zone, starting from $\tau_95$ to $\tau_{III}$, remains to be determined. Since the transition zone lies between zones I and III, we suggest the following expression to determine the vertical mean displacement for $\tau_95 < t < \tau_{III}$, based on information from zones I and III:

$$
\tilde{Y}_t = \tilde{Y}_{t-1} + \left[ \frac{dy}{dt_{t=\tau_95}} + \left( \frac{t-\tau_95}{\tau_{III}-\tau_95} \right) \times \left( b - \frac{dy}{dt_{t=\tau_95}} \right) \right] \times \Delta t
$$

(10)
in which $b$ is Batchelor’s constant, and $\Delta t$ is the time step between times $t$ and $(t-1)$. Using Equations (8), (9) and (10) as a model, the mean vertical displacement of each $Sc$ particle is plotted in Figure 8 and compared with LST results. Since separation of particles happens for $t < 200$, only results up to $t = 200$ are plotted in Figure 8. Reasonable agreement between our LST data and results from this model is obtained. It is worth noting that Equations (8), (9) and (10) were developed based on the theories of Einstein, Taylor and Batchelor, and this agreement encourages the use of these theories to predict mean displacement in a direction normal to the mean flow for small times.
Batchelor [49] further assumed that a constant \( c \) exists such that the mean Lagrangian velocity of a particle cloud in the streamwise direction equals the Eulerian velocity located at \( c \mathcal{Y} \), this is due to the decrease of \( \frac{dU}{dy} \) with height in the channel. Based on this assumption, we have the following equation

\[
V_{\mathcal{X}} = \frac{dx}{dt} = [\bar{U}(y)]_{y=c\mathcal{Y}} \tag{11}
\]

It is now necessary to determine the mean velocity in the channel. Based on our DNS study, the mean flow field velocity in the channel could be described as below

\[
y \leq 5: \quad U = y
\]
\[
5 < y \leq 30: \quad U = 4.9*\ln(y) - 3
\]
\[
30 < y: \quad U = 2.6*\ln(y) + 4.5
\]

Having information of velocity in the channel and an appropriate constant \( c \), one can use Equation (11) to calculate \( V_{\mathcal{X}} \), thus obtain \( \bar{X} \) of a particle cloud. Based on our LST data, \( c = 0.6 \) is the best fit, as seen in Figure 9, and could be used in Batchelor’s theory to predict mean streamwise displacement in the channel.
Figure 9: Mean streamwise displacement of different $Sc$: a) $Sc = 0.1$, b) $Sc = 6$, c) $Sc = 100$. Results are obtained from LST data (lined without markers) and Batchelor’s model (lines marked with open circles).

At this point, it is seen that modified Taylor and Batchelor’s theories produce similar results to our DNS-LST method, in terms of mean displacement in $x$ and $y$ directions. A further attempt is made to determine if using mean displacement as a main tool could predict separation
at reasonable accuracy. However, as explained above, the mean displacement should not be used alone in predicting separation with high purity criterion. Because of turbulent velocity fluctuations the particle clouds stretch forward and backward. The stretching of the clouds also depends on molecular diffusion. We hereby define the standard deviation (STD) for the particle position in each $Sc$ by the following expression

$$STD = \sqrt{(x - \bar{X})^2}$$

in which $\bar{X}$ represents mean location of the particle cloud that varies with time, and $x$ indicates the location of each particle. Since no particle distribution function in $x$ is available at this time, we assume that the concentration distribution in a particle cloud follows a normal distribution. Therefore, 99% of the particle population in the streamwise direction would lie within boundaries determined by adding and subtracting 2.5 times the STD to and from the mean streamwise displacement (which is also the cloud mean streamwise position). In Figure 10, we plot calculations for two pairs of $Sc$ that have been found to separate when applying the 0.5% purity criterion. For each $Sc$, the front and back boundaries of 99% of the population in the $x$ direction are plotted as time increases, using $\bar{X}$ and STD from the LST data. The results indicate that clouds with $Sc = 0.7$ and 30000 would not be able to separate from each other at any time earlier than 100, while that number is 512 for $Sc = 6$ and 7500. However, by counting the number of particles left in the overlap region, we found that $Sc = 0.7$ and 30000 would separate from time equal to 14, while $Sc = 6$ and 7500 separate from time equal to 45. The disagreement indicates that the normal distribution is not an accurate approximation for the concentration distribution in $x$, One should rely on previously presented tools, i.e., Equations (2-5), to predict separation. However, the models that we developed to predict $\bar{X}$ and $\bar{Y}$ could still be used for other applications, or to predict separation, if one could obtain a more accurate particle distribution function.
Figure 10: (a) Front and back boundaries of 99% of population of each Sc in the streamwise direction, using mean displacement and normal distribution to predict the concentration distribution.

IV. CONCLUSION

In this work, particles with different diffusivities, represented by passive markers with different Sc, have been found to separate from each other in turbulent flow, under certain conditions. Separation is observed when there are large differences in the particle Sc, and would occur most effectively in cases where the particles are released from sources on the channel wall. An analysis of the stages of development of puff dispersion is the explanation of the mechanism
responsible for the separation. A correlation is derived to relate the time at which separation begins to the ratio of the characteristic times of development of the two clouds. This flow-induced separation can be applied to separate microscopic and nanoscopic particles with different sizes, and could be a good solution in separating very small particles especially in very dilute systems. A model, based on Batchelor’s extension of the Taylor dispersion theory for shear flows, has been developed to predict mean displacement of particles with different $Sc$ in the streamwise and vertical directions with good agreement to our LST data. It was also found that information about the mean location is not enough to predict particle separation using a high purity criterion. Instead, one should rely on the previously presented correlation to predict separation in channel. The effect of the Reynolds number on flow induced separation needs to be examined in future work.

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