# Electric fields enable tunable surfactant transport to microscale fluid interfaces

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# Electric fields enable tunable surfactant transport to microscale fluid interfaces

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The transport dynamics of oil-soluble surfactants to oil-water interfaces are quantified using a custom-built electrified capillary microtensiometer platform. Dynamic interfacial tension measurements reveal that surfactant transport is enhanced under a D.C. electric field, due to electromigration of charge carriers in the oil toward the interface. Notably, this enhancement can be precisely tuned by altering the field strength and temporal scheduling. For the first time, we demonstrate electric fields as a new parameter to manipulate surfactant transport to microscale fluid-fluid interfaces.

## I. INTRODUCTION

Electric fields act across fluid-fluid interfaces in electrocoalescence [1, 2], inkjet printing [3, 4], electroemulsification [5–7], and microfluidic devices [8–11]. These systems typically consist of drops of one fluid dispersed in another, with surfactants adsorbing from the bulk phases to the interface. Electric fields give rise to stresses at the interface. Depending on the strength of the field, the interface may attain a deformed steady shape, or undergo an instability to form smaller drops. Interface deformation, and mechanisms of instability for systems of pure fluids, i.e., without added surfactant, has been well characterized [12–21]. The limited existing work on the deformation of surfactant-laden interfaces under electric fields is restricted to experiments and computations to predict drop deformation and breakup [22–27]. An inherent assumption in the computations is that the surfactant is insoluble; therefore, the effect of electric field on surfactant transport from bulk to the interface is not accounted for.

Surfactant transport from bulk to a fluid-fluid interface in the absence of electric field follows two transport processes [28, 29]. Bulk surfactant diffuses to the interface (diffusion), and surfactant near the interface undergoes ad/desorption to/from from the interface (kinetic). The transport is known to be a function of bulk concentration, isotherm, local convection and interface geometry [30–36]. However, the impact of electric fields has not been determined. For oil-water interfaces, the electric field acts almost solely in the oil phase because the electrical conductivity of deionized water is nearly $\mathcal{O}(10^6)$ larger than most oils. Surfactants are frequently added to oils and non-polar liquids in several applications. For example, OLOA 11000, a poly-isobutylene succinimide surfactant, is added to motor oil to prevent soot formation in internal combustion engines, disperse pigments in oils for use in electrophoretic displays, and even to prevent sparking during pumping of oils [37–39]. The addition of surfactants to oils has been observed to increase the electrical conductivity, both below and above the critical micellar concentration (CMC), even when the surfactant is considered nonionic [39, 40]. It is hypothesized that below the CMC surfactant molecules form complexes with ionic impurities in oil, which acquire charge by disproportionation [40]. An electric field will exert a force on these charged species, and could influence their bulk transport. Thus, the first step to accurately predict the deformation and breakup of surfactant-laden interfaces under electric fields is to determine whether bulk surfactant transport couples with electric fields.

Here, we present novel experiments to quantify the transport of oil-soluble surfactants to oil-water interfaces using a microscale capillary tensiometer platform, under a D.C. electric field. Dynamic interfacial tension was measured under different electric field strengths to determine the rate of surfactant transport to the interface. We show that for a system whose electrical conductivity increases on addition of surfactant, the transport is enhanced under electric fields. The rate of surfactant transport can be manipulated by tuning the strength of the electric field. On the contrary, a system whose electrical conductivity is unaffected by surfactant addition does not show any coupling of surfactant transport with electric field.

## II. MATERIALS AND METHODS

The surfactants chosen were a poly-isobutylene succinimide surfactant, commercially known as OLOA 11000, donated by Chevron Oronite (San Ramon, CA, USA), and a polyethylene-polypropylene block copolymer, Pluronic L64, purchased from BASF. The surfactants were reported to have a molecular weight of 950 and 2900 g/mol, respectively. Stock solutions of 0.62 mM OLOA was prepared in Isopar-M, an alkane mixture purchased from Exxon Mobil, and 3.71 mM Pluronic was prepared in 100 cSt silicone oil, purchased from Gelest, Inc. The stock solutions were diluted to different concentrations for the experiments. Deionized water was taken from a Barnstead UV Ultrapure II purification system (resistivity of 18.2 MΩ cm).

The experimental setup is an electrified version of the microtensiometer platform described in [35]. The schematic is shown in figure 1, with gravity pointing into the plane of the paper. Surfactant solution is filled in a

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cell of rectangular cross-section (35 mm ×25 mm), 3D printed using an acrylic material. Two electrodes are attached to opposite walls of the cell, 25 mm apart. Voltages in the range $0.1 - 2$ kV were applied using a voltage source, setting electric fields $\sim 0.04 - 0.8$ kV/cm across the cell. The electrodes have a hole of diameter 6 mm drilled through them. A glass capillary containing deionized water is inserted through one of the walls of the cell, and one electrode. All capillaries used were pulled using a micropipette puller to diameters $\sim 70 - 80$ $\mu$m. The capillary is connected to a differential pressure transducer, with the other end connected to the opposite wall of the cell. The other two walls have glass windows to enable viewing of the interface, which is imaged using a camera attached to a Nikon microscope objective lens (20 X), and a radius fitted using a Labview routine. The capillary is inserted 6 mm away from the wall near the camera. COMSOL simulations predict the electric field lines to be unaffected by the wall when the gap between the wall and the capillary is more than twenty capillary radii. This chosen distance ensures that the capillary is within the field of view of the microscope objective, and field lines are not affected by the cell wall.

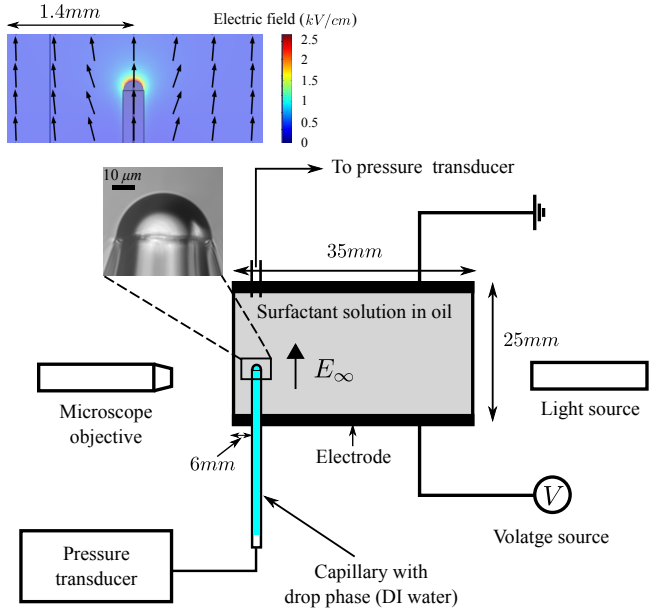


FIG. 1. Schematic of the experimental setup. Top left inset shows COMSOL simulations of electric field lines around a capillary of diameter 70 $\mu$m.

Surfactant transport is quantified by the dynamic interfacial tension, $\gamma$, of the interface. This is obtained from the instantaneous measurement of the radius of curvature of the hemispherical interface, $R$, and the pressure jump across the interface, $\Delta P$, using the Young-Laplace equation, $\gamma = \Delta P \times R/2$. The interface is maintained at a constant pressure head, and the change in interfacial tension is primarily accounted for by the change in radius of curvature of the interface. Under electric fields, the Laplace equation will have an additional contribution from electric (Maxwell) stresses acting at the interface, which scale as $\epsilon_o E_\infty^2$, where $\epsilon_o$ is the permittivity of the oil, and $E_\infty$ is the field strength. The scaled stress balance equation at the interface assumes the form $\Delta P/(\gamma/R) = 2 + Ca_E \Delta T_E$, where $Ca_E = R\epsilon_o E_\infty^2/\gamma$ is the electric capillary number, and $\Delta T_E$ is the dimensionless electric stress jump across the interface. For all field strengths and interface radii, $Ca_E < \mathcal{O}(10^{-4})$. Thus, electric stresses were ignored while calculating the dynamic interfacial tension. The low $Ca_E$ also ensured that the interface remained hemispherical at all field strengths studied.

## III. RESULTS AND DISCUSSION

The principle of the instrument has been previously used to characterize transport of surfactants from water to air-water [35, 36], and oil-water interfaces [43, 44], with the aqueous surfactant solution in the cell. Here, we have the oil-soluble surfactant in the cell, and water in the capillary; and quantify surfactant transport from the oil phase to the oil-water interface. The interfacial tension of pure Isopar-water was measured to be $52.5 \pm 0.3$, which is typical of alkane-water interfaces [43], and that of silicone oil-water was $40.3 \pm 0.4$ mN/m, in agreement with reported values [45]. Under an applied electric field, the interfacial tension was not observed to change beyond the error of the instrument (1 mN/m), for field strengths used in this study.

The transport and adsorption of OLOA in Isopar was measured to the Isopar-water interface at two different surfactant concentrations (4 $\mu$M and 10 $\mu$M), under different electric field strengths. A new interface was formed by subjecting the drop phase in the capillary to a high pressure head, using a solenoid valve. For a newly formed interface, the interfacial tension starts decreasing from the clean interfacial tension value, and relaxes to a steady state of $26.2 \pm 0.3$ mN/m for the 4 $\mu$M system, and $22.9 \pm 0.3$ mN/m for the 10 $\mu$M system. The system is deduced to reach steady state when the interfacial tension does not change by more than 1 mN/m for at least 1000 s. The dynamic interfacial tension of the 4 $\mu$M system is shown in figure 2(a). For the experiments, data was collected at each millisecond; however, for clarity, we show fifty data points spaced equally on a logarithmic scale in the figure. The inset shows the dynamic interfacial tension for the last 1000 s under each electric field, with a shifted time axis, on a linear scale. Surfactant transport is known to depend on the radius of curvature of the interface [35]. In all the experiments, the pressure head was held constant at the same value, ensuring the initial radius of curvature for all the interfaces differed by $< 5$ $\mu$m. It follows that the time to reach steady state decreases with increasing values of the electric field. Under a field of 0.4 kV/cm, the system reaches steady state nearly four times faster than under no applied field. The effect is more prominent at lower values of the electric

field. Dynamic interfacial tension curves for the 0.2 and 0.4 kV/cm nearly overlap with each other, having slightly faster dynamics under 0.4 kV/cm. All the curves reach the same steady state interfacial tension, indicated by the dashed line and depicted in the inset. This suggests that the electric field has negligible effect on the adsorption isotherm. The dynamic interfacial tension for 10 $\mu$M OLOA showed a similar trend. Evidently, the transport of OLOA to the Isopar-water interface is enhanced under electric fields.

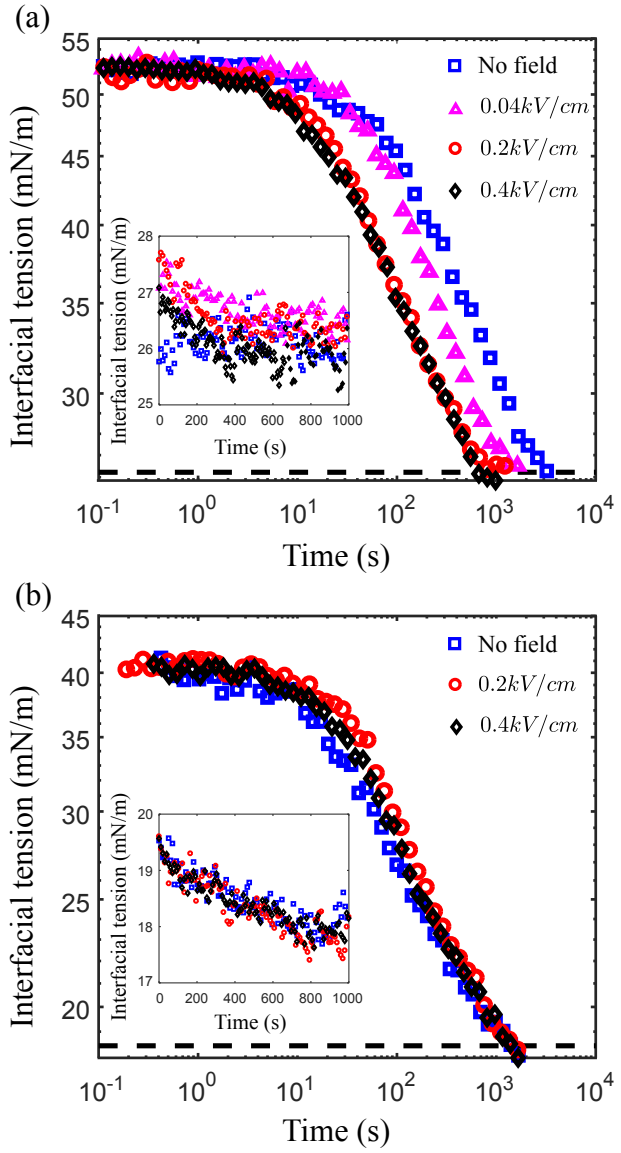


FIG. 2. Dynamic interfacial tension for (a) 4 $\mu$M OLOA 11000 in Isopar-M, and (b) 10 $\mu$M Pluronic L64 in 100 cSt silicone oil. The dashed line represents the steady state interfacial tension. Inset: Dynamic interfacial tension for each system during the last 1000 s under each electric field. The time axis has been shifted so that all the curves fit in the same time range of 0 to 1000 s.

In contrast, the transport of Pluronic to the silicone oil-water interface was not influenced by the electric field (figure 2(b)). For a 10 $\mu$M system, the interfacial tension relaxes from the clean value and approaches steady state. Even at the highest value of the field strength, the dynamic interfacial tension curve overlaps the curve obtained in the absence of a field. As shown in the inset, the interfacial tension did not completely relax to a steady state value, however the slope of the curves flatten out, suggesting that the system approaches steady state. Since the curves overlap each other throughout the experiment, we conclude that similar to the OLOA system, the steady state interfacial tension is unaltered by the electric field.

As a measure of the effect of electric field on surfactant transport, we plot the time required for the interfacial tension to relax from the clean value to a specific value, $\gamma_t$, for each system, as a function of the field strength. For OLOA in Isopar, we choose $\gamma_t = 35$ mN/m, and for Pluronic in silicone oil, $\gamma_t = 30$ mN/m. These values are chosen because they are roughly half the value of the interfacial tension of the pure oil-water interface and the steady state interfacial tension at the given surfactant concentration. For low bulk surfactant concentrations, as has been chosen in this study, a specific value of interfacial tension physically corresponds to the interface reaching a specific surfactant coverage. The result is shown in figure 3. For the OLOA system, this time scale follows a power law scaling, with the exponents 0.41 and 0.52 for the 4 $\mu$M and 10 $\mu$M systems, respectively. The 10 $\mu$M system reaches the same surfactant coverage faster than the 4 $\mu$M system at all field strengths, in agreement with previous observations of faster diffusion from a more concentrated bulk solution to an interface [35]. The power law scaling with electric field is analogous to the effect of bulk phase convection on surfactant transport to fluid-fluid interfaces, rendered rigid due to large gradients in interfacial surfactant concentration [36]. Convection in the continuous phase reduces the effective boundary layer thickness for mass transport of the surfactant, thus, the time scale for the surfactant to diffuse from the bulk to the interface reduces. For Pluronic in silicone oil, the time scale does not change on the application of an electric field, as is shown by the dotted line.

The observed phenomena can be explained from the measurement of the electrical conductivity of surfactant doped oils as a function of surfactant concentration, shown in the inset of figure 3. The conductivity was measured using a nonaqueous conductivity probe, DT 700 (Dispersion Technology). For OLOA, the conductivity increases linearly, while for Pluronic, the conductivity does not change with surfactant concentration. The CMC of OLOA 11000 in Isopar-L is reported to be around 140 $\mu$M [42], and is shown by the arrow in the inset. Assuming a similar CMC in Isopar-M, it follows that the conductivity of the oil increases both above and below the CMC, implying the presence of charged species even at concentrations below the CMC. Analogous to a previous study, we hypothesize that OLOA forms charged

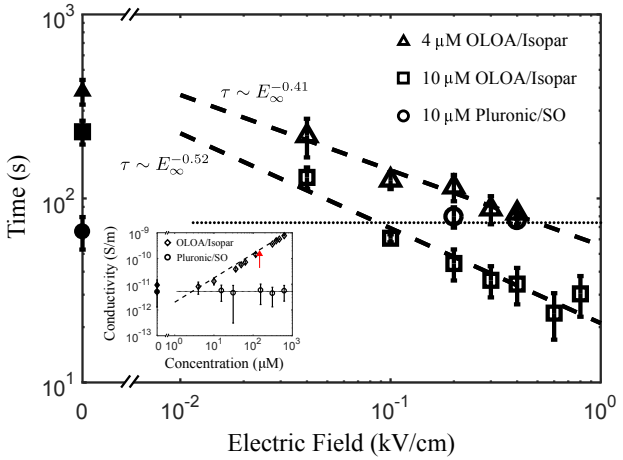


FIG. 3. Time required for the oil-water interface to reach an interfacial tension of 35 mN/m for OLOA 11000 in Isopar-M, and 30 mN/m for Pluronic L64 in silicone oil as a function of electric field. The dashed lines represent power law scalings for OLOA in Isopar-M. The horizontal dotted line establishes that the time scale is independent of field strength for Pluronic in silicone oil. The filled symbols denote the time scale under zero electric field. Inset: Electrical conductivity as a function of surfactant concentration. The arrow shows the CMC of OLOA 11000 in Isopar-L [42]. The dashed line shows the linear dependence of conductivity with concentration for OLOA in Isopar-M. The dotted horizontal line shows the conductivity of Pluronic in silicone oil is independent of surfactant concentration. The filled symbols denote the conductivity of pure oils, without externally added surfactant.

complexes with ionic impurities present in Isopar below the CMC [40].

The surfactant complex experiences an electric force $qE_\infty$, where $q$ is the charge of the complex. It moves with an electrophoretic velocity, $U_E = qE_\infty/6\pi\mu_o l$, where $\mu_o$ is the viscosity of the oil, and $l$ is the characteristic linear dimension of the complex. Assuming, $q$ is equal to the charge of one electron, and typical size of surfactant molecules $l \approx 5$ nm [47], $U_E \approx 5\times10^{-3} - 5\times10^{-2}$ mm/s under the field strengths studied. For diffusion to spherical interfaces, the length scale for diffusion, $h_s$, depends on the radius of curvature of the interface, bulk concentration and isotherm [34]. We do not measure the equilibrium isotherm of OLOA at the Isopar-water interface, however, using typical parameter values of equilibrium surfactant coverage for surfactants at oil-water interfaces [45], and the radii and bulk concentrations used in this study, $h_s \approx 0.35 - 3.5$ mm. The time scale for the surfactant complex to migrate this distance under an electric field is $\tau_E = h_s/U_E \approx 7 - 700$ s. The diffusion time scale is given by $\tau_d = h_s^2/D$, where $D$ is the diffusion coefficient. For the dilute bulk surfactant concentrations chosen in this study ($\leq 5\times10^{-4}$ wt %), we assume that the surfactant complexes do not interact with each other, and estimate $D$ using the Stokes-Einstein equation, $D = k_BT/6\pi\mu_o l$, $k_B$ and $T$ being the Boltzmann constant and temperature, respectively [46]. Using this, we estimate $\tau_d \approx 3.8\times10^3 - 3.8\times10^5$ s. An electric Pectlet number can be calculated as the ratio of the diffusion to electrophoretic time scale, $Pe_E = qE_\infty h_s/k_BT$. For the field strengths used in this study, $Pe_E \sim 55 - 5500$. Even at the smallest field, electrophoretic migration is faster than diffusion. This manifests as an enhanced transport to the interface. Although a more rigorous analysis involving an investigation of the dependence of $h_s$ on $E_\infty$, and measurement of charge on the complex is required to explain the power law coefficient, the migration of charged surfactant complexes under electric fields at time scales faster than the diffusion time qualitatively explains the results.

The Pluronic surfactant does not acquire charge in silicone oil, hence will not experience electrophoretic migration under an electric field. The conductivity difference between the silicone oil and water is huge: $\sim \mathcal{O}(10^6)$. As a consequence, the tangential electric stresses at the interface is negligible, eliminating any electrohydrodynamic flow. Surfactant motion due to dielectrophoresis is nearly $\mathcal{O}(10^{-3})$ slower than diffusion. Hence, the transport of Pluronic to silicone oil-water interface is not influenced by the applied field.

The surfactant transport can be precisely controlled by temporal variation of the field. This is demonstrated in figure 4 for 4 $\mu$M OLOA in Isopar. We performed an experiment which started under no external field. A field of 0.2 kV/cm was applied at 200 s, before steady state was reached. The transport dynamics changes at the instant the field is turned on, and the dynamic interfacial tension curve shifts from the curve obtained under zero field (for all times) to the curve obtained under 0.2 kV/cm (for all times). Another experiment was performed, which started under a field of 0.2 kV/cm, with the field switched off at 100 s. Again, the dynamics changes instantaneously with the field being turned off, and the curve shifts to the one obtained under zero field. Similar control and precision was observed in experiments performed at other field strengths, and for 10 $\mu$M OLOA, confirming that this is a robust phenomena. Note that figure 4 shows data 10 s after a new interface was formed; hence the curves do not start from the same value of interfacial tension.

For all experiments where the field was turned on at some point before steady state, the time to shift from the curve under zero field to the curve under an applied field is around 100 s. This is comparable to the electrophoretic time, $\tau_E$, assuming $h_s \sim 1$ mm, reaffirming that surfactant migration due to electrophoresis is likely responsible for this phenomena. The time scale to move from the curve under an applied field to a curve under zero field is significantly smaller than the diffusion time assuming $h_s \approx 1$ mm.

Experiments performed with the direction of the electric field reversed showed the same effect as shown in figures 2 and 4. This is expected because the interface is radially symmetric. Further, assuming disproportionation to be the charging mechanism, an equal number of

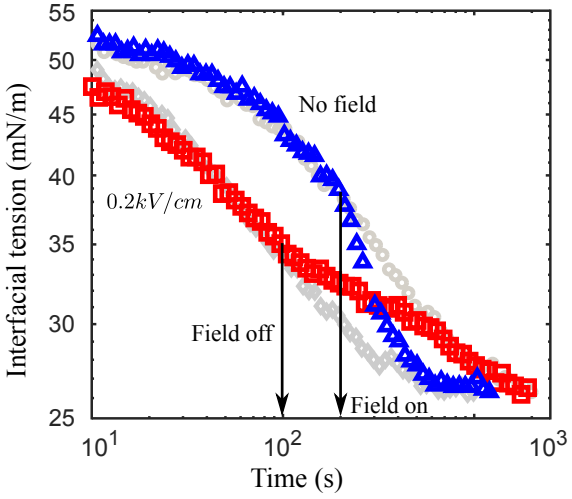


FIG. 4. Dynamic interfacial tension for 4 $\mu$M OLOA 11000 in Isopar-M at zero electric field ($\circ$), 0.2 kV/cm ($\diamond$), from zero field to 0.2 kV/cm at 200 s ($\triangle$), and from 0.2 kV/cm to zero field at 100 s ($\square$). The arrows indicate the time when the field was switched off or on.

positively and negatively charged surfactant complexes will be formed. Hence, the transport will be enhanced, regardless of the direction of the electric field.

The phenomena observed in this work would be difficult to capture in a pendant drop apparatus, which is traditionally used to measure surfactant transport to fluid-fluid interfaces. That technique requires millimeter size interfaces to accurately measure the dynamic interfacial tension. At such length scales $Ca_E \approx 0.1$ resulting in significant deformation, or even electric field induced instability of the interface. This will significantly reduce the range of field strength that can be studied in such devices. Further, the time scale for adsorption to millimeter size interfaces is nearly an order of magnitude slower than to the microscale interfaces used here [35]; hence a significantly longer experiment would be needed to capture any effect. Although bulk phase convection has been observed to enhance surfactant transport [36] akin to electric fields, the "on-off "experiments shown in figure 4 are more precise due to the instantaneous scheduling of the electric fields.

## IV. CONCLUSIONS

We have reported robust and novel experiments to demonstrate electric fields as a new parameter to precisely manipulate the rate of surfactant transport to microscale oil-water interfaces. This phenomena should be generic to oil-soluble surfactants which form charge carriers. The field enhanced transport could enable new tools for controlled electrocoalescence of drops in nonpolar media, or lab-on-chip methods for droplet manipulation in microfluidic devices.

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