



CHORUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

Critical assessment of CMB limits on dark matter-baryon scattering: New treatment of the relative bulk velocity

Kimberly K. Boddy, Vera Gluscevic, Vivian Poulin, Ely D. Kovetz, Marc Kamionkowski, and Rennan Barkana

Phys. Rev. D **98**, 123506 — Published 10 December 2018

DOI: [10.1103/PhysRevD.98.123506](https://doi.org/10.1103/PhysRevD.98.123506)

A Critical Assessment of CMB Limits on Dark Matter–Baryon Scattering: New Treatment of the Relative Bulk Velocity

Kimberly K. Boddy,¹ Vera Gluscevic,^{2,3} Vivian Poulin,¹ Ely D. Kovetz,¹ Marc Kamionkowski,¹ and Rennan Barkana⁴

¹*Department of Physics & Astronomy, Johns Hopkins University, Baltimore, MD 21218, USA*

²*School of Natural Sciences, Institute for Advanced Study, Einstein Drive, Princeton, NJ 08540, USA*

³*Department of Physics, University of Florida, Gainesville, Florida 32611, USA*

⁴*Raymond and Beverly Sackler School of Physics and Astronomy, Tel-Aviv University, Tel-Aviv 69978, Israel*

We perform an improved cosmic microwave background (CMB) analysis to search for dark matter–proton scattering with a momentum-transfer cross section of the form $\sigma_0 v^n$ for $n = -2$ and $n = -4$. In particular, we present a new and robust prescription for incorporating the relative bulk velocity between the dark matter and baryon fluids into the standard linear Boltzmann calculation. Using an iterative procedure, we self-consistently include the effects of the bulk velocities in a cosmology in which dark matter interacts with baryons. With this prescription, we derive CMB bounds on the cross section, excluding $\sigma_0 > 2.3 \times 10^{-33} \text{ cm}^2$ for $n = -2$ and $\sigma_0 > 1.7 \times 10^{-41} \text{ cm}^2$ for $n = -4$ at 95% confidence, for dark matter masses below 10 MeV. Furthermore, we investigate how these constraints change when only a subcomponent of dark matter is interacting. We show that *Planck* limits vanish if $\lesssim 0.4\%$ of dark matter is tightly coupled to baryons. We discuss the implications of our results for present and future cosmological observations.

I. INTRODUCTION

Cosmological observables provide a unique avenue to search for evidence of non-gravitational interactions between dark matter (DM) and the Standard Model particles, and thereby gain insight into the unknown physical nature of DM. In particular, elastic scattering between DM and baryons transfers heat and momentum between the two fluids. The time evolution for the rate of momentum transfer depends on how the interaction cross section scales with the relative particle velocities, and the effects of scattering can be important at different cosmological epochs. If scattering is efficient before recombination, it affects the temperature, polarization, and lensing anisotropies of the cosmic microwave background (CMB), as well as the linear matter power spectrum on small angular scales [1–6]. If scattering is significant in the post-recombination Universe, it can result in anomalous late-time heating or cooling of the baryon gas, altering the 21-cm signal from neutral hydrogen at redshifts prior to the Epoch of Reionization [7–9].

In a Λ CDM Universe, there is a relative bulk velocity between the cold DM and baryon fluids, which results in supersonic coherent flows of the baryons post recombination [10]. If DM and baryons interact, but the rate of momentum transfer is low, the drag force between the two fluids may not efficiently dissipate their relative bulk velocity, allowing it to dominate over the thermal particle motions, once the Universe is sufficiently cooled. Furthermore, if the relative bulk velocity is significant prior to recombination, the computation of the Boltzmann equations for the CMB becomes infeasible using standard methods: the equations describing the velocity fluctuations of the fluids become nonlinear, resulting in the coupling of individual Fourier modes. In an attempt to address this issue when computing CMB limits on DM–baryon interactions, previous studies [3, 6, 11] used the root-mean-square (RMS) of the relative bulk velocity as a correction to the thermal velocity dispersion, suppressing the rate of momentum transfer, and thus obtaining conservative upper limits on DM–baryon interactions. That approach has two important caveats: the RMS velocity was computed in Λ CDM, inconsistent with a cosmology that features DM–baryon interactions; and the same RMS velocity was used in the Boltzmann equations for all Fourier modes, neglecting differences in how modes contribute at a given scale.

In this work, we develop an improved treatment of the relative bulk velocity and reassess CMB limits on DM–proton scattering. Specifically, we supplement the standard Boltzmann linear calculations with an iterative procedure that self-consistently includes the effects of the relative bulk velocity in a cosmology in which dark matter interacts with baryons. We parameterize the momentum-transfer cross section as $\sigma_{\text{MT}} = \sigma_0 v^n$, where v is the relative velocity between the scattering particles, and focus on two interaction models for which the relative bulk velocity is expected to have a substantial impact: $n = -2$ (arising in the case of, *e.g.*, electric or magnetic dipole interactions through light mediators) and $n = -4$ (from, *e.g.*, Coulomb-like interactions or Yukawa interactions through light mediators). We analyze the latest public CMB data from the *Planck* 2015 data release [12, 13] and find $\sigma_0 < 2.3 \times 10^{-33} \text{ cm}^2$ for $n = -2$ and $\sigma_0 < 1.7 \times 10^{-41} \text{ cm}^2$ for $n = -4$ at the 95% confidence level (C.L.) for DM masses below 10 MeV. We forecast the sensitivity of the next-generation ground-based CMB experiment and find that CMB-Stage 4 [14] could deliver roughly a factor of ~ 3 improvement (not including a CMB lensing analysis), for a DM mass of 1 MeV. Additionally, we report limits on σ_0 for scenarios in which only a fraction of DM interacts with protons. For very small fractions, large values of σ_0 are allowed, and there exists a regime in which the DM and baryons are tightly

coupled, such that DM behaves as baryons and experiences acoustic oscillations. We find that the constraining power of *Planck* is drastically diminished when less than 0.4% of DM is interacting.

The Experiment to Detect the Global Epoch of Reionization Signature (EDGES) recently reported an anomalously large sky-averaged absorption signal [15], which was attributed to dark matter interactions with baryons [9]. Our results do not rule out a phenomenological $n = -4$ interaction invoked to explain the EDGES signal [9]; however, we do exclude a percent of DM interacting with ions only, at a level consistent with the EDGES signal [16]. In a separate study, we investigate the regime of subpercent fractions of millicharge-like DM and discuss the implications of our newly-derived CMB limits for the DM interpretation of EDGES [17].

This paper is structured as follows. In Section II, we derive the Boltzmann equations that include DM–baryon scattering and present a new treatment of the relative bulk velocity. In Section III, we describe and quantify the effects of scattering on the CMB power spectra. In Section IV, we describe our analysis of *Planck* 2015 data and present new limits on the interactions with $n = -2$ and $n = -4$. We discuss and conclude in Section V.

II. MODIFIED COSMOLOGY

In this section, we incorporate the DM–baryon collision term into the Boltzmann equations and present an improved treatment to account for a non-negligible relative bulk velocity between baryons and DM. Further details of our calculations are provided in Appendix A. We consider DM interactions with protons and parameterize the momentum-transfer cross section as $\sigma_{\text{MT}} = \sigma_0 v^n$, where v is the relative velocity between the scattering particles. Scattering with helium involves non-trivial form factors that depend on the specific structure of the interaction [5, 18], and it is mainly relevant for DM masses above 1 GeV [4, 5]. We neglect it here for simplicity; incorporating it would improve our constraints presented in Section IV.

A. Evolution of perturbations and temperatures

The scattering between DM and protons introduces a drag force and heat exchange between the DM and baryon fluids. Hence, the Boltzmann equations governing the evolution of their velocity perturbations and of their temperatures must be adjusted accordingly. We assume that the DM and baryon fluids are nonrelativistic, with energy densities ρ_χ and ρ_b , temperatures T_χ and T_b , and sound speeds c_χ and c_b , respectively. The motion of the two fluids is given by their peculiar velocities \vec{V}_χ and \vec{V}_b , with a relative bulk velocity $\vec{V}_{\chi b} \equiv \vec{V}_\chi - \vec{V}_b$.

The linear Boltzmann equations incorporate terms only up to first order in the metric fluctuations and fluid perturbations. However, in the presence of DM–baryon interactions, the equations become nonlinear at times when the relative bulk velocity exceeds the relative thermal velocity dispersion. Therefore, we begin by describing the evolution of the temperatures and peculiar velocities in real space without assuming a small relative bulk velocity. We show the full derivation in Appendix A, where we present generic expressions for $n > -5$ and for scattering with multiple species of baryons. This calculation was previously performed in Ref. [8] for the specific case of $n = -4$, and our results agree.

From Eq. (A13), the peculiar velocities evolve as

$$\frac{\partial \vec{V}_\chi}{\partial \tau} - c_\chi^2 \vec{\nabla} \delta_\chi + \frac{\dot{a}}{a} \vec{V}_\chi = R_\chi (\vec{V}_b - \vec{V}_\chi) {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{V_{\chi b}^2}{2\bar{v}_{\text{th}}^2} \right) \quad (1a)$$

$$\frac{\partial \vec{V}_b}{\partial \tau} - c_b^2 \vec{\nabla} \delta_b + \frac{\dot{a}}{a} \vec{V}_b = R_\gamma (\vec{V}_\gamma - \vec{V}_b) + \frac{\rho_\chi}{\rho_b} R_\chi (\vec{V}_\chi - \vec{V}_b) {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{V_{\chi b}^2}{2\bar{v}_{\text{th}}^2} \right), \quad (1b)$$

and from Eq. (A21), the temperatures evolve as

$$\begin{aligned} \dot{T}_\chi + 2\frac{\dot{a}}{a}T_\chi &= 2R'_\chi \left\{ (T_b - T_\chi) \right. \\ &\times \left[{}_1F_1 \left(-\frac{n+3}{2}, \frac{3}{2}, -\frac{V_{\chi b}^2}{2\bar{v}_{\text{th}}^2} \right) - \frac{V_{\chi b}^2}{3\bar{v}_{\text{th}}^2} {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{V_{\chi b}^2}{2\bar{v}_{\text{th}}^2} \right) \right] + \frac{m_p}{3} V_{\chi b}^2 {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{V_{\chi b}^2}{2\bar{v}_{\text{th}}^2} \right) \left. \right\} \end{aligned} \quad (2a)$$

$$\begin{aligned} \dot{T}_b + 2\frac{\dot{a}}{a}T_b &= 2\frac{\mu_b}{m_e} R_\gamma (T_\gamma - T_b) + 2\frac{\mu_b}{m_\chi} \frac{\rho_\chi}{\rho_b} R'_\chi \left\{ (T_\chi - T_b) \right. \\ &\times \left[{}_1F_1 \left(-\frac{n+3}{2}, \frac{3}{2}, -\frac{V_{\chi b}^2}{2\bar{v}_{\text{th}}^2} \right) - \frac{V_{\chi b}^2}{3\bar{v}_{\text{th}}^2} {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{V_{\chi b}^2}{2\bar{v}_{\text{th}}^2} \right) \right] + \frac{m_\chi}{3} V_{\chi b}^2 {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{V_{\chi b}^2}{2\bar{v}_{\text{th}}^2} \right) \left. \right\}, \end{aligned} \quad (2b)$$

where ${}_1F_1$ is the confluent hypergeometric function of the first kind, $\bar{v}_{\text{th}}^2 = T_\chi/m_\chi + T_b/m_p$ is the relative thermal velocity dispersion squared, m_χ is the DM mass, m_p is the proton mass, m_e is the electron mass, μ_b is the mean molecular weight of the baryons, and δ_χ and δ_b are density perturbations in DM and baryons, respectively. These equations are written in synchronous gauge, where a is the scale factor, and the dot notation indicates a derivative with respect to conformal time τ . The terms proportional to R_γ and R_χ in Eq. (1) represent drag terms, which describe the transfer of momentum between the interacting fluids. The momentum-transfer rate coefficient R_γ arises from photon–baryon interactions through Compton scattering, while R_χ arises from the new DM–proton interactions and is given by

$$R_\chi = a\rho_b \frac{Y_H \sigma_0}{m_\chi + m_p} \mathcal{N}_n \bar{v}_{\text{th}}^{(n+1)}, \quad (3)$$

where $\mathcal{N}_n \equiv 2^{(5+n)/2} \Gamma(3+n/2)/(3\sqrt{\pi})$ and Y_H is the mass fraction of hydrogen. The heat-transfer rate coefficient in Eq. (2) is $R'_\chi = R_\chi m_\chi/(m_\chi + m_p)$.

The competition between R_χ and the expansion rate aH determines the efficiency of momentum transfer at a given redshift: when $R_\chi/aH \gg 1$, the fluids are tightly coupled and move together. Given the current CMB limits for interactions with $n \geq 0$, this regime occurs at very early times ($z \gg 10^4$), and results in dark acoustic oscillations that imprint oscillatory features in the linear matter power spectrum at small scales [4, 5]. In that case, the drag between the DM and baryon fluids couples their motion, resulting in a small relative bulk velocity—compared to the thermal particle velocities at redshifts relevant for CMB measurements—and can thus be ignored. However, for $n \leq -2$, the two fluids have a feeble interaction rate at early times, and the relative bulk velocity is non-negligible. As a result, Eqs. (1) and (2) are nonlinear. In the following, we present a new prescription for capturing the effects of the relative bulk velocity on the momentum-transfer rate between DM and baryons in both regimes.

B. Treatment of relative bulk velocity

Standard CMB computations rely on linearity of the Boltzmann equations, for which it is possible to Fourier transform real-space equations and independently track the evolution of each Fourier mode with wave number k . In the limit $V_{\chi b}^2 \ll \bar{v}_{\text{th}}^2$, the ${}_1F_1$ functions in Eqs. (1) and (2) asymptote to 1, and the evolution of the peculiar velocities is indeed linear (and the temperature evolution equations are independent of the relative bulk velocity). It is then possible to take the divergence and the Fourier transform of Eq. (1) to obtain the evolution equations for the velocity divergences of the DM and baryons, $\theta_\chi(k, z)$ and $\theta_b(k, z)$, respectively. However, when this approximation breaks down, the Boltzmann equations are nonlinear, resulting in coupling of Fourier modes.

In order to bypass this difficulty, we first define

$$V_{\text{flow}}^2(k, z) \equiv \int_0^k \frac{dk'}{k'} \Delta_\zeta^2(k') \left[\frac{\theta_b(k', z) - \theta_\chi(k', z)}{k'} \right]^2 \quad (4)$$

$$V_{\text{RMS}}^2(k, z) \equiv \int_k^\infty \frac{dk'}{k'} \Delta_\zeta^2(k') \left[\frac{\theta_b(k', z) - \theta_\chi(k', z)}{k'} \right]^2, \quad (5)$$

where $\Delta_\zeta^2(k)$ is the initial curvature perturbation variance per $\ln k$. We then propose the following prescription to reduce Eq. (1) to a linear expression, while modifying the momentum-transfer rate coefficient to reincorporate the effects of mode mixing. For a given mode k^* , the density perturbations from larger scales cause a relative bulk

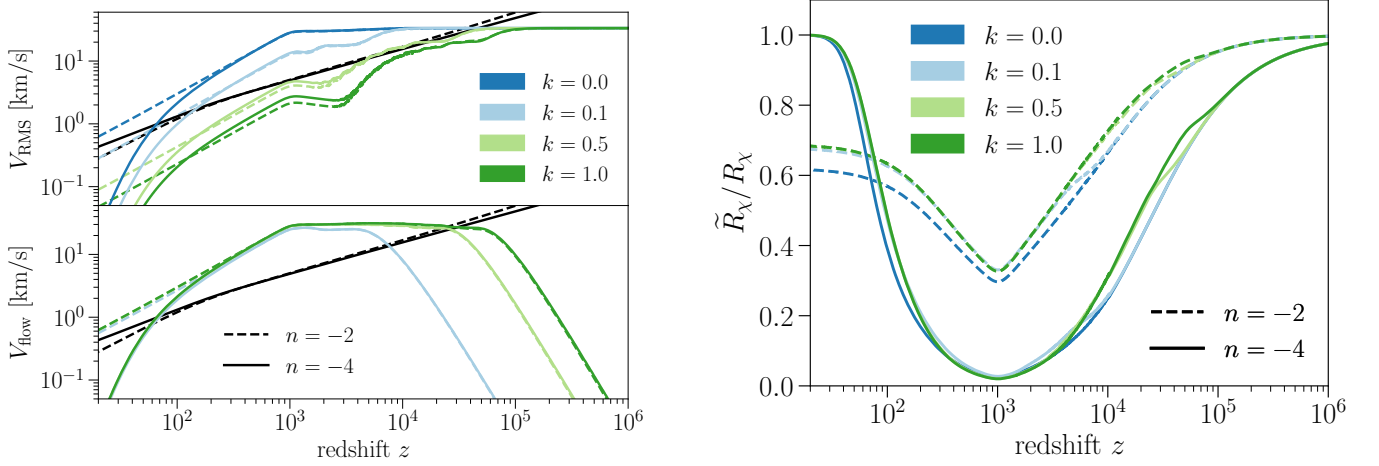


FIG. 1. **[Left]** Evolution of V_{RMS} (top panel) and V_{flow} (bottom panel) as a function of redshift for various wave numbers k , indicated in the legend. The thermal velocity \bar{v}_{th} (black) is shown for reference. **[Right]** Modification to the coefficient of the momentum-transfer rate from Eq. (7) for various k . In both panels, we show the $n = -2$ (dashed) and $n = -4$ (solid) interactions, for a DM mass of 1 MeV. We set the coefficients of the momentum-transfer cross section to their respective 95% C.L. upper limit, derived using our “main” prescription, reported in Section IV.

flow between the DM and baryon fluids that contributes to their existing relative bulk motion.¹ To account for the bulk flow, we absorb the ${}_1F_1$ function into the momentum-transfer rate coefficient, replacing $V_{\chi b}$ with $V_{\text{flow}}(k^*, z)$. Meanwhile, the density perturbations from smaller scales collectively act as a source of velocity dispersion, in addition to the thermal dispersion. We thus augment all instances of \bar{v}_{th}^2 with the square of the one-dimensional RMS velocity $V_{\text{RMS}}^2(k^*, z)/3$. With this prescription, the Boltzmann equations in Fourier space become

$$\dot{\delta}_\chi = -\theta_\chi - \frac{\dot{h}}{2}, \quad \dot{\theta}_\chi = -\frac{\dot{a}}{a}\theta_\chi + c_\chi^2 k^2 \delta_\chi + \tilde{R}_\chi(k)(\theta_b - \theta_\chi), \quad (6a)$$

$$\dot{\delta}_b = -\theta_b - \frac{\dot{h}}{2}, \quad \dot{\theta}_b = -\frac{\dot{a}}{a}\theta_b + c_b^2 k^2 \delta_b + R_\gamma(\theta_\gamma - \theta_b) + \frac{\rho_\chi}{\rho_b} \tilde{R}_\chi(k)(\theta_\chi - \theta_b), \quad (6b)$$

where h is the trace of the scalar metric perturbation, and the modified momentum-transfer rate coefficient is

$$\tilde{R}_\chi = R_\chi \left[1 + \frac{V_{\text{RMS}}^2(k, z)/3}{\bar{v}_{\text{th}}^2} \right]^{(n+1)/2} {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{V_{\text{flow}}^2(k, z)}{2[\bar{v}_{\text{th}}^2 + V_{\text{RMS}}^2(k, z)/3]} \right). \quad (7)$$

In the limit $V_{\text{RMS}}^2, V_{\text{flow}}^2 \ll \bar{v}_{\text{th}}^2$, we recover the results from Refs. [3–6].

In the left panel of Figure 1, we show the evolution of V_{RMS} (top panel) and V_{flow} (bottom panel), with $k=0$ (dark blue), $k=0.1$ (light blue), $k=0.5$ (light green), and $k=1$ (dark green), for $n = -2$ (dashed lines) and $n = -4$ (solid lines). We also show the evolution of \bar{v}_{th} (black). Since $V_{\text{flow}}(k=0)$ vanishes by definition, there is no associated curve plotted in the bottom panel. In the right panel of Figure 1, we show the evolution for the ratio \tilde{R}_χ/R_χ for the same values of k in the left panel. At early times, \tilde{R}_χ approaches R_χ , since \bar{v}_{th} dominates over V_{RMS} and V_{flow} . For redshifts $z \lesssim 10^5$, V_{RMS} and V_{flow} become increasingly important and suppress the rate of momentum transfer. At recombination near $z \sim 10^3$, the baryons decouple from the photons, causing V_{RMS} and V_{flow} to suddenly begin decreasing adiabatically, thereby lessening the suppression of the rate.

We note that the evolution of \tilde{R}_χ is quite similar between various k , indicating that incorporating the k dependence via V_{RMS} and V_{flow} might not play a significant role; indeed, we can understand this observation from the limiting behavior of \tilde{R}_χ . The full variance, integrated over all k , of the relative bulk velocity is given by $\langle V_{\chi b}^2 \rangle \equiv V_{\text{flow}}^2 + V_{\text{RMS}}^2$. For small values of k , $V_{\text{flow}}^2 \rightarrow 0$ while $V_{\text{RMS}}^2 \rightarrow \langle V_{\chi b}^2 \rangle$; thus, the ${}_1F_1$ function in Eq. (7) approaches 1. For large values of

¹ Reference [10] similarly had to account for the bulk flow between the DM and baryon fluids within the context of Λ CDM. In that study, there was a clear separation of scales such that the post-recombination Universe could be represented as individual patches across the sky, each with a particular value of the relative bulk velocity. Averaging over the various patches yielded a local isotropically averaged power spectrum. Since we do not have a similar separation of scales, it is not appropriate to follow the same technique.

k , $V_{\text{RMS}}^2 \rightarrow 0$ while $V_{\text{flow}}^2 \rightarrow \langle V_{\chi b}^2 \rangle$; furthermore, if V_{flow} is much larger than \bar{v}_{th} , the ${}_1F_1$ function in Eq. (7) asymptotes to $\sim \{V_{\text{flow}}^2/[2(\bar{v}_{\text{th}}^2 + V_{\text{RMS}}^2/3)]\}^{(n+1)/2}$. In either case, the modified momentum-transfer rate coefficient has the form

$$\tilde{R}_{\chi}^{Xb} = R_{\chi} \left[1 + \frac{\langle V_{\chi b}^2 \rangle / 3}{\bar{v}_{\text{th}}^2} \right]^{(n+1)/2}, \quad (8)$$

ignoring an n -dependent prefactor in the large- k limit. Thus, this form of the modified rate may sufficiently capture the combined large-scale and small-scale effects of mode mixing. In either case, for the temperature evolution equations in Eq. (2), we substitute $V_{\chi b}^2$ for its average value $\langle V_{\chi b}^2 \rangle$. In the limit $\langle V_{\chi b}^2 \rangle \ll \bar{v}_{\text{th}}^2$, we again recover previous results [3–6].

This work builds upon the mean-field approach introduced in previous studies investigating DM–baryon scattering [3]. In that study, the modified momentum-transfer rate was

$$\tilde{R}_{\chi}^{cb} = R_{\chi} [1 + \langle V_{cb}^2 \rangle / (3\bar{v}_{\text{th}}^2)]^{(n+1)/2}, \quad (9)$$

where²

$$\langle V_{cb}^2 \rangle \equiv \int_0^{\infty} \frac{dk'}{k'} \Delta_{\zeta}^2(k') \left[\frac{\theta_b(k', z) - \theta_c(k', z)}{k'} \right]^2 \quad (10)$$

is the variance of the relative bulk velocity in Λ CDM [which is approximately $\langle V_{cb}^2 \rangle = 10^{-8}$ at $z > 10^3$ and redshifts as $(1+z)^2$ at later times [6, 11]] and θ_c is the velocity divergence for cold collisionless DM [10]. We improve upon the previous work in two important ways. First, we compute the variance $\langle V_{\chi b}^2 \rangle$ in a consistent manner, using the values of θ_{χ} and θ_b obtained in a cosmology that includes DM–baryon scattering; this improvement corresponds to using the modified momentum-transfer rate in Eq. (8). Second, we treat the effects of mode coupling from smaller scales ($k > k^*$) separate from those arising from larger scales ($k < k^*$). These two steps constitute our main prescription captured in Eq. (7). When the rate of momentum exchange is sufficiently small at times relevant for *Planck*, using θ_c within Λ CDM is a decent estimation. This condition is satisfied for the upper limits on σ_0 derived assuming all of DM interacts with baryons, and in that case we find little difference from our improved treatments of the relative bulk velocity. However, if the rate is moderate or large, momentum exchange drives the values of θ_{χ} and θ_b closer together, such that $\langle V_{cb}^2 \rangle$ computed in Λ CDM overestimates the relative bulk velocity and thus overly suppresses the interaction rate. This situation arises if only a subcomponent of DM is allowed to couple to baryons, and it is thus essential to employ the techniques presented in this work in order to derive limits on the DM–baryon interaction for that case.

Throughout the remainder of this work, we refer to various treatments of the relative bulk velocity that enable us to explore how various aspects of our new prescription affect our constraints on the DM–baryon scattering cross section. The “main” prescription is our primary treatment given by Eq. (7), and we consider it to be the most accurate for any regime of DM–baryon coupling. The “ k -independent” prescription is the treatment given by Eq. (8). These two prescriptions both have the feature that the variance of the relative bulk velocity is computed self-consistently within an interacting cosmology, using the iterative procedure described in Appendix B. The “cdm” prescription is that found in previous literature [3, 6, 11] and uses Eq. (9); in this case, we employ the same temperature evolution equations presented in those works and not the full expressions of our Eq. (2). Finally, the “aggressive” prescription uses Eq. (3) and naively ignores the relative bulk velocity entirely in both the temperature and velocity evolution equations. The constraints on σ_0 resulting from this prescription are thus the most aggressive; their comparison with the other constraints reported in this work quantifies the importance of including an accurate treatment of the relative bulk velocity.

III. THE EFFECT ON COSMOLOGICAL OBSERVABLES

In this Section, we discuss the impact of DM–proton scattering on cosmological observables. In Section III A, we show the thermal histories of the DM and baryon fluids, as well as the evolution of the free-electron fraction. In Section III B, we describe the effects on the primary CMB anisotropies, the matter power spectrum, and the CMB lensing power spectrum. In Section III C, we investigate a specific regime in which DM is tightly coupled to, and

² Reference [3] used the quantity $\langle V_{cb}^2 \rangle$, but labeled it as V_{RMS}^2 . We refer to $V_{\text{RMS}}(k, z)$ as a k -dependent quantity, calculated in the interacting theory. The full variances $\langle V_{cb}^2 \rangle$ and $\langle V_{\chi b}^2 \rangle$ are k -independent quantities; the former is calculated in Λ CDM and the latter in the interacting theory.

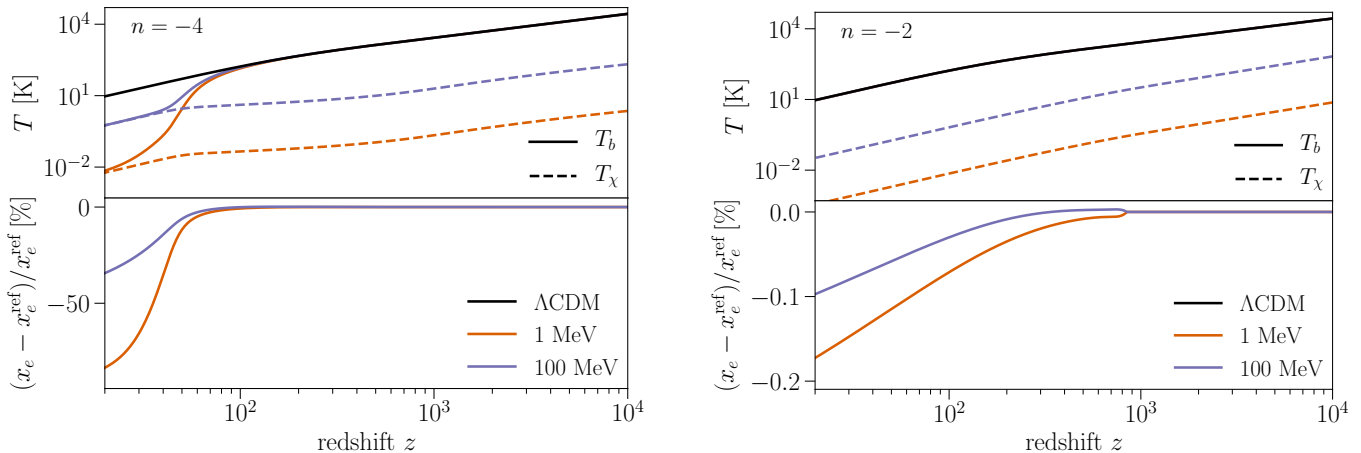


FIG. 2. Temperature evolution (top panels) and residuals of x_e with respect to Λ CDM (bottom panels), for the $n = -4$ (left panels) and $n = -2$ (right panels) interaction, for DM masses of 1 MeV (orange) and 100 MeV (purple). We set the coefficients of the momentum-transfer cross section to their respective 95% C.L. upper limit, derived using our “main” prescription, reported in Section IV. We also show the baryon temperature in Λ CDM (black) for reference.

oscillates together with, the baryons at some point in cosmic history; this regime is allowed by *Planck* data for $n = -4$ if only a small fraction of DM interacts with baryons.

To compute the power spectra, we have incorporated the Boltzmann equations from Section II into the Boltzmann solver CLASS³ [19]. We chose adiabatic initial conditions, and set the DM temperature and velocity divergences to match those of the baryons at the start of the integration ($z = 10^{14}$). For $n = -4$, the rate of heat transfer is too low to maintain thermal equilibrium with the baryons, and the temperature and velocity divergences of the DM rapidly drop from their original values. Thus, our initial conditions are effectively equivalent to starting with vanishing temperature and velocity divergences. In fact, for all interaction strengths relevant in this work, we have verified that the choice of initial conditions is irrelevant, as long as they are set well above $z \sim 10^5$ (roughly the redshift below which modes *Planck* is sensitive to start entering the cosmological horizon). We present further details on our modifications to CLASS in Appendix B.

Throughout this section, we use Λ CDM parameters at their best-fit *Planck* 2015 values [20]. Unless otherwise noted, we fix the coefficient of the momentum-transfer cross section, σ_0 , to its appropriate 95% C.L. upper limit, derived in Section IV using our “main” prescription for the relative bulk velocity. When plotting residuals, we show the relative difference between an observable computed for the cosmology with DM–proton scattering and for the reference Λ CDM cosmology.

A. Thermal history

An accurate determination of the thermal history is essential to the calculation of CMB power spectra. The CMB is very sensitive to the number of free electrons in the plasma through the visibility function and the optical depth in the line-of-sight solution of the Boltzmann equations [21]. Scattering between DM and protons alters the temperature evolution of the baryons, which in turn influences the free-electron fraction, x_e . If interactions with DM cool the baryon gas around recombination, the rate of recombination increases. If cooling occurs at later times, it reduces the number of free electrons in a manner opposite to that of an early reionization from energy injection [22]. In the top panels of Figure 2, we show the evolution of the baryon (solid) and DM (dashed) temperatures as a function of redshift, comparing them to the evolution of the baryon temperature in Λ CDM (black solid), for DM masses of 1 MeV (orange) and 100 MeV (purple), for $n = -4$ (left panel) and $n = -2$ (right panel). In the bottom panels, we show the residuals for the evolution of the free-electron fraction with respect to Λ CDM. We set the values of σ_0 to their respective 95% C.L. upper limits, obtained using our “main” prescription in Section IV. We find that the DM–proton interaction has no strong impact on the recombination era. The impact on the free-electron fraction is substantial

³ <https://github.com/lesgourg/class>

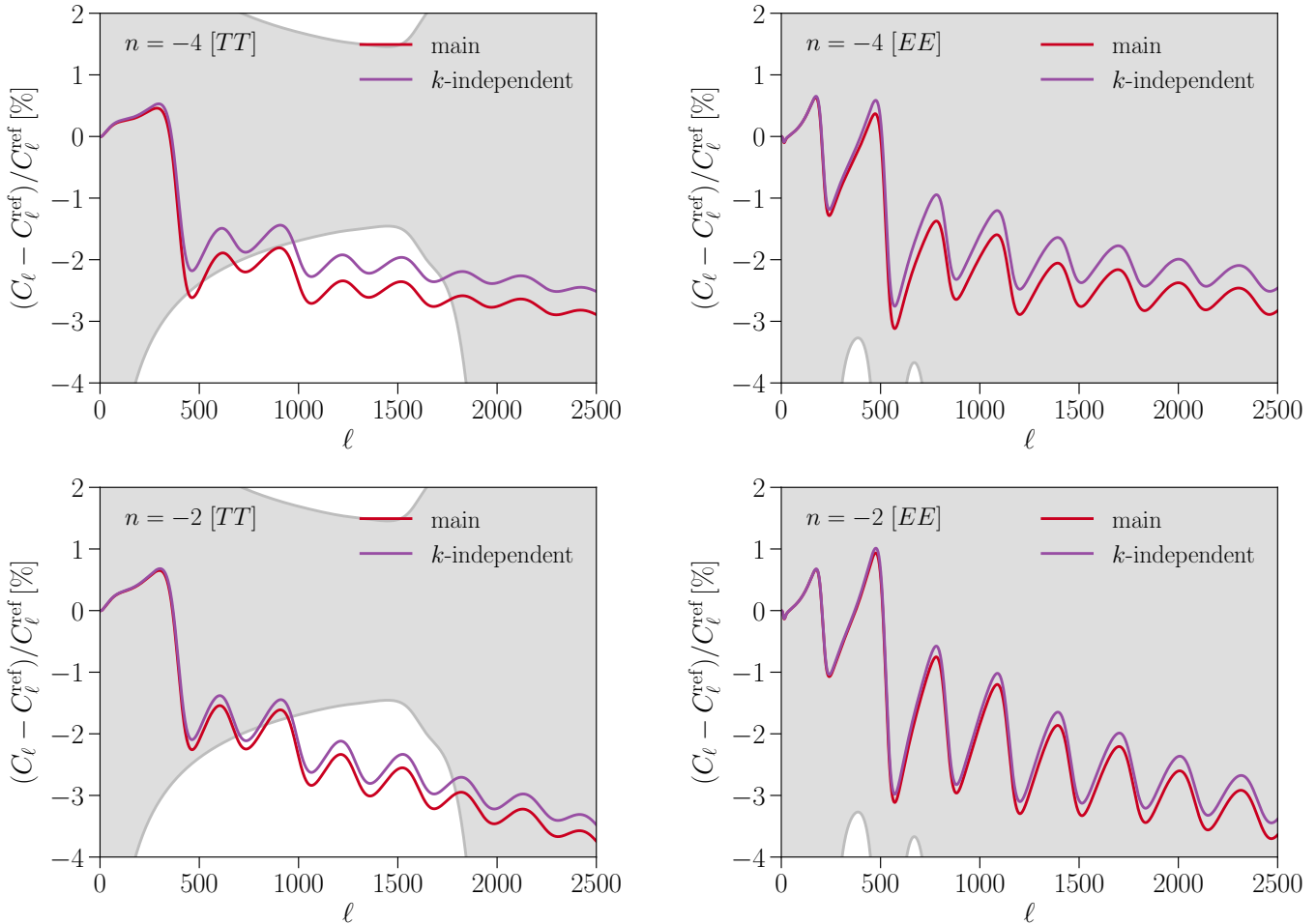


FIG. 3. **[Top]:** Percent residuals (with respect to Λ CDM) of the lensed TT (left panel) and EE (right panel) power spectra for the case of $n = -4$ and a DM mass of 1 MeV. We show residuals for the “main” prescription (red) and the “ k -independent” prescription (purple). In both cases, we set the coefficient of the momentum-transfer cross section to its 95% C.L. upper limit, derived using the “main” prescription. Gray bands roughly represent the 2σ *Planck* error bars, with a bin size of $\Delta\ell = 50$. **[Bottom]:** Same as the top panels, but for the case of $n = -2$. The difference between the two prescriptions is less prominent in this case because of the weaker scaling of the momentum-transfer cross section with relative velocity.

only at late times. Since the CMB is only marginally sensitive to changes in the late-time free-electron fraction (through the low- ℓ EE power spectrum), baryon cooling is a subdominant effect compared to the drag acceleration from scattering, and we have verified that it can be safely ignored for the purposes of this work.

B. Power spectra

In Figure 3, we illustrate the effect of DM–proton interactions on CMB temperature and polarization power spectra by showing their residuals with respect to Λ CDM. We show the power spectra computed using two treatments of the relative bulk velocity, for comparison: the “main” prescription (red) and the “ k -independent” prescription (purple).

In both cases, we fix σ_0 to the 95% C.L. upper limit, derived using the “main” prescription. The effects of DM–proton scattering are as follows:

- The dominant effect on the CMB power spectra is a scale-dependent modulation of the acoustic-oscillation amplitude, which occurs for the following reasons. First, small modes enter the cosmological horizon earlier and are therefore subject to damping due to friction between the two fluids for a longer time than larger modes. Second, the interactions reduce the overall growth of perturbations, as well as the associated metric potentials that directly affect the CMB photons [23]. Prior to recombination, the interactions modify the Sachs-Wolfe (SW)

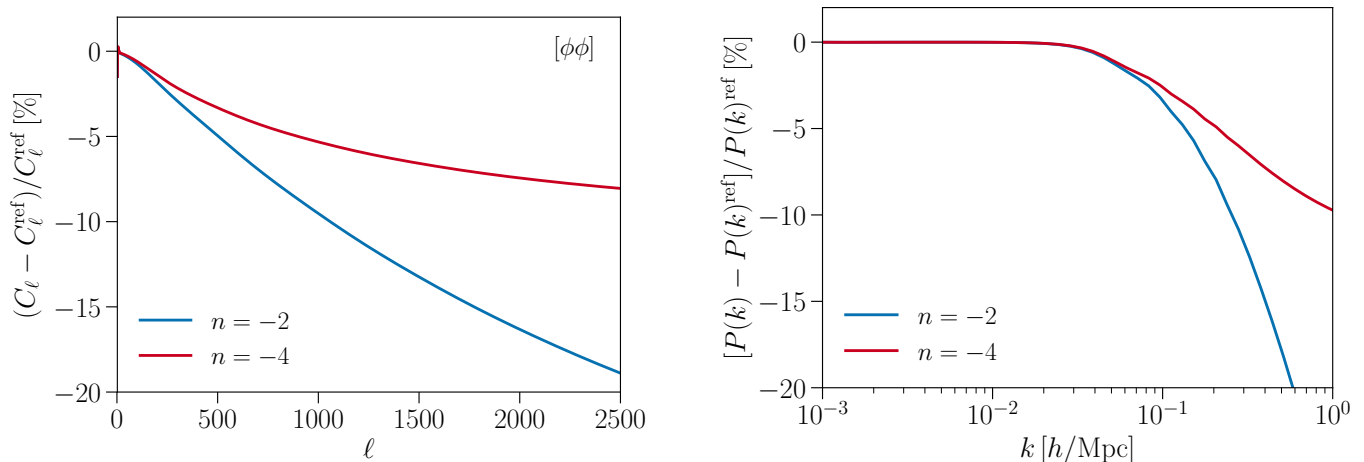


FIG. 4. Percent residuals (with respect to Λ CDM) of the lensing-potential power spectrum $C_\ell^{\phi\phi}$ (left panel) and the linear matter power spectrum $P(k)$ (right panel) for the case of $n = -2$ (blue) and $n = -4$ (red), both for a DM mass of 1 MeV. We use the “main” prescription and set the coefficient of the momentum-transfer cross section to its 95% C.L. upper limit, reported in Section IV.

contribution to the metric perturbations (both in terms of the overall amplitude and zero-point of oscillations in the quantity $\delta_\gamma/4 + \psi$, where ψ is the gravitational potential in the Newtonian gauge). Around recombination, the time evolution of the metric perturbations is affected, in turn contributing to a change in the early integrated Sachs-Wolfe (EISW) effect. In the TT spectrum, modifications of the SW and EISW terms lead to the relative enhancement of the first acoustic peak, while other peaks are suppressed overall.

- At early times, photons are tightly coupled to electrons such that $\theta_b = \theta_\gamma$. The DM–baryon interaction effectively increases the inertia of baryons, suppressing the speed of sound in the plasma and reducing the frequency of the acoustic oscillations; as a consequence, the Doppler peaks shift to smaller physical and angular scales (larger ℓ). We find that this effect is subdominant in the TT spectrum. However, the EE power spectrum is mostly sourced by the quadrupolar temperature patterns close to the last scattering surface [21, 24, 25] and is thus predominantly affected by modifications to the Doppler term.
- The sound speeds of the DM and baryon fluids depend on the fluid temperatures and are therefore affected by the heat transfer. Since the sound-speed terms enter Eq. (6) with a prefactor of k^2 , the dynamics of small angular scales (corresponding roughly to large k) are affected. We find that these terms also have a negligible contribution to the fluid evolution equations.
- Finally, as we detail in Section III A, post-recombination cooling of baryons decreases the number of free electrons, in turn lowering the optical depth to the surface of last scattering, as compared to the Λ CDM case.⁴ This effect is opposite to that of an early reionization and leads to an increase of power in modes that enter the horizon before reionization (*i.e.*, $\ell \gtrsim 20$ for both temperature and polarization) and to lowering of the reionization bump in the EE power spectrum. This effect is also subdominant, as far as the CMB observables are concerned. However, for higher cross sections, it produces a small modulation of power at the lowest values of ℓ in the EE power spectrum.

The primary difference between the power spectra computed using the “main” and the “ k -independent” prescriptions is at high multipoles, where the “main” prescription leads to a more prominent damping tail. For $n = -2$, the scaling of the momentum-transfer cross section with relative velocity is rather weak; the feedback of the interactions on the computation of V_{RMS} and V_{flow} is small, and the power spectra of the two prescriptions look very similar. The power spectra of the prescriptions for $n = -4$ exhibit a more noticeable difference. For the remainder of this paper, we consider only our main “main” prescription.

Finally, in Figure 4, we show the effects of DM–proton scattering on the power spectrum of the CMB lensing potential (left) and the linear matter power spectrum (right); we plot residuals of the power spectra with respect

⁴ As previously mentioned, early-time cooling of baryons accelerates recombination, in turn shifting the peaks toward higher ℓ . However, this effect is not present, in practice, given the strength of the CMB constraints.

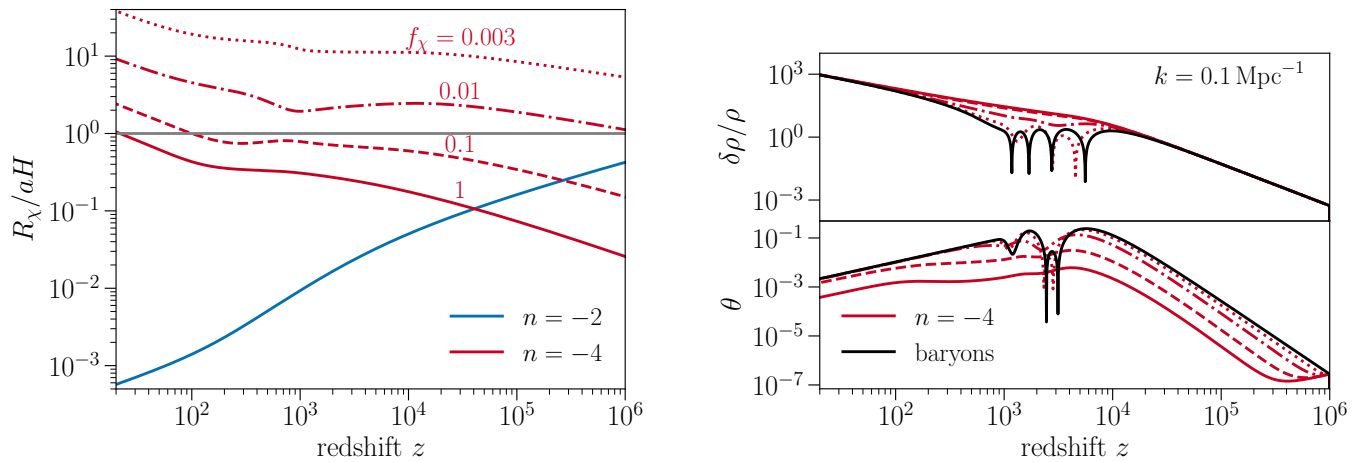


FIG. 5. **[Left]:** The evolution of the ratio of the momentum-transfer rate to the expansion rate of the Universe for $n = -2$ (blue) and $n = -4$ (red), for interacting DM fractions $f_\chi = 1$ (solid), 0.1 (dashed), 0.01 (dot-dashed), and 0.003 (dotted). We show a reference line (solid gray) where the momentum-transfer rate matches the expansion rate. **[Right]:** The density perturbations $\delta\rho/\rho$ (top panel) and velocity divergences (bottom panel) for the mode $k = 0.1 \text{ Mpc}^{-1}$. We show the case of $n = -4$ (red) for the same interacting DM fractions considered in the left panel. For reference, we show the ΛCDM case for baryons (black); note that the line for the density perturbations of cold DM lies underneath those for the $n = -4$ interaction with fractions $f_\chi = 1$ and $f_\chi = 0.1$. In both panels, we set the coefficient of the momentum-transfer cross section to its respective 95% C.L. upper limit, derived using the “main” prescription in Section IV, and set the DM mass to 1 MeV.

to ΛCDM , using the “main” prescription, for $n = -2$ (blue) and $n = -4$ (red). We set σ_0 to its 95% C.L. upper limit, derived using the same prescription in Section IV. The interactions suppress the growth of DM (and baryon) perturbations, resulting in a progressively larger reduction of power at smaller scales. The suppression of lensing power manifests as a reduction of peak smearing in the TT and EE power spectra.

We note that it is possible to use large-scale structure data to constrain DM–baryon interactions with the matter power spectrum. However, for the $n = -2$ and $n = -4$ models, constraints from the Lyman- α flux power spectrum yield a minor improvement upon CMB-only constraints at the $\mathcal{O}(1)$ level [3, 6]; and the Lyman- α data are subject to modeling caveats that the CMB is not.

C. Strongly coupled DM fraction

The discussion thus far has focused on DM comprised entirely of a single species that is only weakly coupled to baryons at all times. It is worth noting that the CMB constraints imply weak coupling at all times only for the specific values of n we are concerned with in this work, while for $n \geq 0$, CMB data constrain the interaction cross section such that the coupling is strong for $z \gtrsim 10^4 - 10^5$ [4, 5]. In the strong-coupling case, DM is tightly coupled to baryons and behaves like an extra baryonic component, with the important caveat that it does not participate in recombination. It does, however, experience dark acoustic oscillations, evident in the behavior of the matter power spectrum at scales $k \gtrsim 1 \text{ Mpc}^{-1}$ [5]. It is also possible to have strong coupling for $n = -2$ and $n = -4$, without violating CMB bounds, if the interacting species represents only a fraction $f_\chi \equiv \rho_\chi / \rho_{\text{DM}}$ of the total DM density, while the remaining fraction is cold collisionless DM. A strongly-coupled subcomponent of DM has been previously studied generically [26] and in the context of millicharged DM [27, 28].⁵

In Figure 5, we demonstrate the behavior of a strongly-coupled DM subcomponent, for $m_\chi = 1 \text{ MeV}$. In the left panel, we compare the evolution of the momentum-transfer rate to the expansion rate of the Universe for $n = -2$ (blue) and $n = -4$ (red), with $f_\chi = 1$ (solid), 0.1 (dashed), 0.01 (dot-dashed), and 0.003 (dotted). In the right panel, we plot the density perturbations and velocity divergences for $n = -4$ (red) and for baryons in ΛCDM . In both panels, we set σ_0 in each case to its appropriate 95% C.L. upper limit, derived using the “main” prescription. For large values of f_χ , *Planck* constrains the momentum-transfer rate to be below the expansion rate, and the density perturbations

⁵ We emphasize that, unlike Refs. [26–28], we do not assume tight coupling between DM and baryons when analyzing data in Section IV; the strong coupling regime occurs as a consequence of the large value of the cross section allowed for small values of f_χ .

of the interacting subcomponent of DM tracks those of cold DM in Λ CDM. As f_χ decreases, the data allow for large momentum-transfer rates, and the interacting DM subcomponent begins to track the motion of the baryons more closely. For $f_\chi = 0.003$, the modes that *Planck* is sensitive to become tightly coupled upon entering the horizon, and the interacting DM subcomponent experiences acoustic oscillations.

IV. PLANCK CONSTRAINTS

In this Section, we constrain DM–proton interactions using *Planck* 2015 data. We describe the data set and analysis method in Section IV A and present numerical results in Section IV B.

A. Data and method

We analyze the *Planck* 2015 temperature, polarization, and lensing power spectra, using the *Planck* Likelihood Code v2.0 (Clik/Plik) [12, 13]; in particular, we use the nuisance-marginalized joint TT , TE , EE likelihood, Clik/Plik lite, and the lensing likelihood with SMICA-map–based lensing reconstruction.⁶ We sample the cosmological parameter space using the MontePython [29] software package with the PyMultinest [30–33] likelihood sampler. We verify that our sampling runs converge by evaluating the variance between several runs and by comparing a subset of results to those we obtain using a Markov chain Monte Carlo (MCMC) sampler. The MCMC sampler implemented in MontePython uses the Metropolis-Hastings algorithm, and chain convergence is evaluated using the Gelman-Rubin convergence criterion $R - 1 < 0.01$ [34].

There are nine free parameters in our interacting cosmology: the DM particle mass m_χ , the fraction f_χ of the interacting subcomponent of DM, the coefficient of the momentum-transfer cross section σ_0 , and the six standard Λ CDM parameters (baryon density $\Omega_b h^2$, total DM density $\Omega_{\text{DM}} h^2$, the Hubble parameter h , the reionization optical depth τ_{reio} , the amplitude of the scalar perturbations A_s , and the scalar spectral index n_s). In most of our analysis runs, we fix the fraction f_χ and the mass m_χ , and sample in the remaining seven free parameters using broad flat priors. We also perform analysis runs in which we allow f_χ (or m_χ) to be a free parameter, in which case we use broad log-flat priors on f_χ (or m_χ) and σ_0 to sample the parameter space effectively. Due to computational difficulties, we do not investigate masses above a GeV. We analyze the data for the $n = -4$ and $n = -2$ interaction models.

B. Numerical results

We first assume that all of the DM matter is interacting ($f_\chi = 1$) and perform the likelihood analysis for $n = -4$ and $n = -2$, sampling the likelihoods in σ_0 and the six Λ CDM parameters, for seven fixed benchmark DM masses between 10 keV and 1 GeV (see Table I). Representative examples of the reconstructed marginalized posterior probability distributions⁷ are shown in Figure 6 for the case of $n = -4$ and $m_\chi = 1$ MeV. The general shape of the posteriors does not significantly vary as a function of DM mass and is qualitatively similar for the $n = -2$ case. There is a prominent (positive) degeneracy between σ_0 and the scalar spectral index n_s : DM interactions suppress power on small scales in the CMB TT power spectrum, and an increase in n_s can counteract this suppression. The mild correlations with A_s and τ_{reio} are also due to the suppression of power at high values of ℓ , but arise from a combination of the TT and lensing likelihood. The value of A_s controls the overall amplitude of all power spectra, but it is modulated by a factor $\exp(-2\tau_{\text{reio}})$ above $\ell \simeq 20$ in the TT power spectrum. Increasing A_s compensates for the power suppression in the lensing power spectrum, but it also requires a larger value of τ_{reio} in order to keep the combination $A_s \exp(-2\tau_{\text{reio}})$ fixed, so as not to affect the high- ℓ normalization of the TT power spectrum. The mild anticorrelation with $\Omega_\chi h^2$ is due to the fact that a smaller value of $\Omega_\chi h^2$ leads to a change in the expansion history that compensates for the shift of the peak positions produced by DM–baryon scattering. However, reducing $\Omega_\chi h^2$ also delays matter–radiation equality, which boosts the amplitude of the EISW; thus, the degeneracy is very weak. Similarly, the shift in the peak positions can be compensated by altering the value of the Hubble rate, resulting in a mild, positive correlation between σ_0 and h .

We find no evidence for DM–proton scattering in the *Planck* 2015 data—all marginalized probabilities for σ_0 are consistent with zero, and we use them to infer an upper limit on σ_0 as a function of m_χ . We present our 95% C.L.

⁶ Potential issues with systematic effects in *Planck* high-multipole polarization could, in principle, affect parameter estimation [12, 13], but Refs. [4, 5] have demonstrated that exclusion of high- ℓ polarization degrades constraints on DM interactions by only a few percent.

⁷ Posterior probability distributions in this study were visualized using `corner.py` [35].

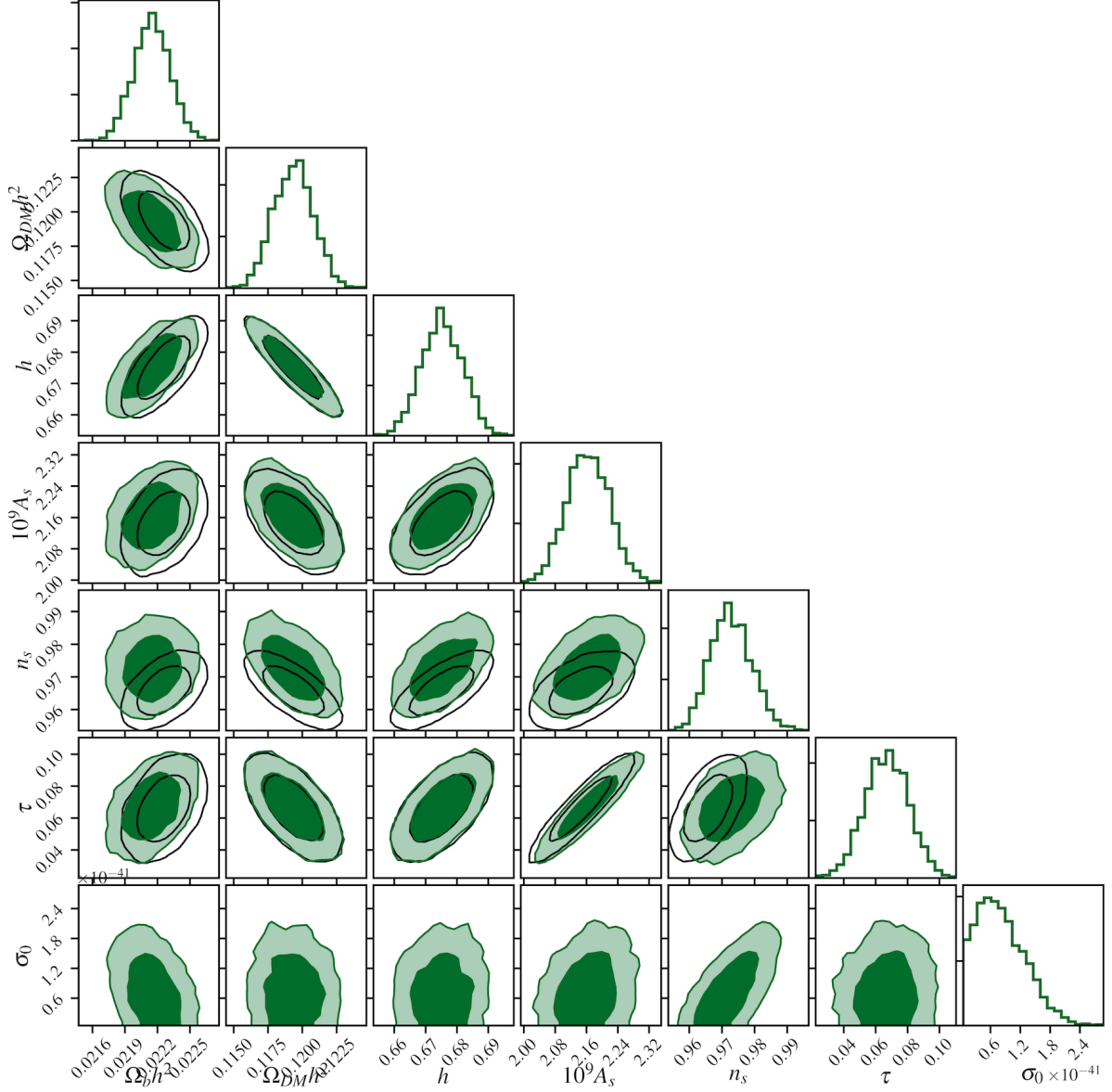


FIG. 6. The posterior probability distribution for the Λ CDM parameters and the coefficient of the DM–proton momentum-transfer cross section for $n = -4$ interaction and a DM mass of 1 MeV. We show the 68% and 95% C.L. contours obtained from a joint analysis of *Planck* 2015 temperature, polarization, and lensing anisotropies for a cosmology with DM–proton interactions (green) and for the standard Λ CDM cosmology (black). The one-dimensional, marginalized posteriors are shown at the top of each column.

exclusion curves in Figure 7 and in the corresponding Table I. In Section III, we have demonstrated the importance of accounting for the relative bulk velocity when computing the effects of scattering on CMB observables. Using the results of our sampling runs, we show the limit (solid red) we obtain with our “main” prescription. Our limits virtually have no mass dependence for $m_\chi \lesssim 10$ MeV (see also Ref. [11]): for $m_\chi \ll m_p$, m_χ appears in the Boltzmann equations via the thermal term \bar{v}_{th} in the momentum-transfer rate. As demonstrated in Figure 2, the DM temperature is negligible for CMB calculations, such that the thermal velocity of the baryons dominates \bar{v}_{th} . Thus, the DM mass dependence drops out of the momentum-transfer rate entirely. On the other hand, increasing the DM mass to become comparable to or exceed the proton mass, the momentum-transfer rate scales as $R_\chi \sim \sigma_0(m_\chi + m_p)^{-1}$, while \bar{v}_{th} continues to be dominated by the thermal velocity of the baryons and thus does not contribute to the mass scaling. Hence, our limits on σ_0 should scale as m_χ for $m_\chi \gg m_p$; a transition towards this behavior is visible at the high-mass end of Figure 7.

	10 keV	1 MeV	10 MeV	100 MeV	200 MeV	500 MeV	1 GeV
$n = -4$	1.7e-41	1.7e-41	1.7e-41	1.9e-41	2.1e-41	2.6e-41	3.5e-41
$n = -2$	2.3e-33	2.3e-33	2.4e-33	2.6e-33	2.8e-33	3.6e-33	4.9e-33

TABLE I. A list of the 95% C.L. exclusion limits on coefficient of the DM–proton momentum-transfer cross section, σ_0 , given in units of cm^2 and obtained from *Planck* 2015 temperature, polarization, and lensing anisotropy measurements, for the $n = -4$ and $n = -2$ interactions. DM masses are listed along the top row. The limits correspond to those in Figure 7 and are computed using our “main” prescription to account for the relative bulk velocity of the DM and baryon fluids.

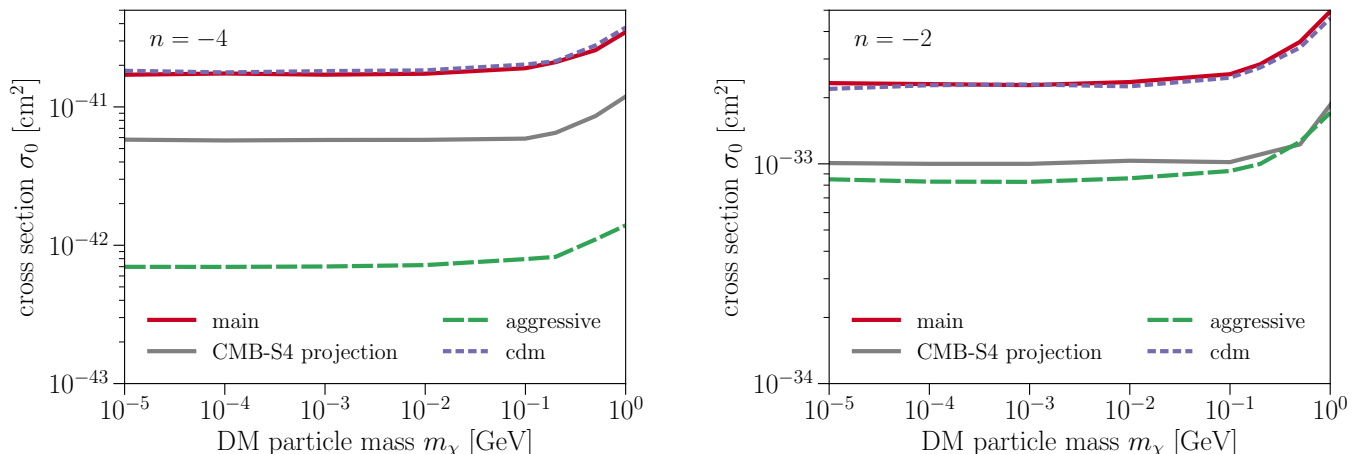


FIG. 7. The 95% C.L. upper limits for the coefficient of the DM–proton momentum-transfer cross section as a function of DM particle mass, obtained from likelihood analysis of *Planck* 2015 temperature, polarization, and lensing anisotropies, for the $n = -4$ (left panel) and $n = -2$ (right panel) interactions. Results are shown for our “main” treatment of the relative bulk velocity between the DM and baryon fluids, described in Section II. Additionally, we show the inferred limit from an “aggressive” assumption, which ignores the impact of the relative bulk velocity. For comparison, we plot the limit we obtain using the prescription proposed in previous literature (denoted as “cdm”) [3]. We also show the projected sensitivity for a future ground-based CMB-Stage 4 experiment (obtained using the “main” prescription).

For comparison, we also reproduce the limit obtained using the prescription from previous literature [3, 6, 11] (dotted line, denoted as “cdm”).⁸ Since the CMB constrains the cross section to be quite small, the amount of interaction does not significantly alter the evolution of $\langle V_{\chi b}^2 \rangle$ from its Λ CDM counterpart $\langle V_{cb}^2 \rangle$. As we discuss at the end of Section II B, this leads to our “main” treatment of the relative bulk velocity to yield similar limits to the “cdm” prescription of previous work. Below, we consider the case of strongly-coupled DM, where the “cdm” prescription of previous work is not valid.

For illustration only, in the same figure, we show “aggressive” constraints that are inferred when a vanishing relative bulk velocity is assumed in Eqs. (1) and (2), and thus the momentum-transfer rate is completely unsuppressed by the bulk motions. This assumption does not hold for the case of $f_\chi = 1$: at the level of the upper limit on σ_0 , there is not enough friction between the DM and baryon fluids to entirely dissipate the relative bulk velocity. The “aggressive” constraint demonstrates the importance of properly incorporating the relative bulk velocity, especially for $n = -4$, where the difference in the limit is more than an order of magnitude. Additionally, while we expect our “main” prescription to well-represent the exact solution, the “aggressive” constraint gives an absolute floor on the possible improvement that an exact treatment of the relative bulk velocity could potentially achieve.

We further perform a forecast of the sensitivity to $n = -4$ and $n = -2$ scattering for a future ground-based CMB-Stage 4 experiment [14]. We consider (in combination with *Planck* data) an experiment with noise levels of $1 \mu\text{K-arcmin}$ and a beam size of 1 arcmin , with a survey covering 40% of the sky, assuming $\ell_{\min} = 30$ and $\ell_{\max} = 3000$. We do not consider CMB lensing in this analysis, which may substantially improve sensitivity [36]; thus, our result is a conservative projection. For $n = -4$, we find an improvement over the current constraints from *Planck* 2015 by a factor of ~ 2.9 for a DM mass of 1 MeV, giving $\sigma_0 < 5.8 \times 10^{-42}$ at 95% C. L. For $n = -2$, we find $\sigma_0 < 1.0 \times 10^{-33}$

⁸ We have verified that the residual spectra (calculated with respect to Λ CDM) we obtain by implementing the methods of Refs. [6, 11] align with those from Ref. [11]. However, we note that we obtain constraints that are a factor of ~ 1.8 weaker for $n = -4$ than those in Refs. [6, 11] (using the same likelihoods and sampling methods as Ref. [11]) and a factor of ~ 1.4 stronger for $n = -2$ than Ref. [6].

for the same mass, which is a factor of ~ 2.3 improvement over *Planck*. In both cases, we use the “main” prescription for the relative bulk velocity. We show the corresponding projected exclusion curves in Figure 7.

To investigate how the limits presented above may change when only a fraction of DM interacts with baryons, we reanalyze *Planck* 2015 data for the case of $n = -4$. In the left panel of Figure 8, we show the upper limits on σ_0 as a function of the DM mass m_χ , fixing the interacting fraction to $f_\chi = 1, 0.1, \text{ and } 0.01$. The mass dependence of the constraint for $f_\chi = 1$ differs from that for 0.1 and 0.01 at high masses. The temperature of the interacting DM subcomponent is negligible compared to the baryon temperature for DM masses $m_\chi \lesssim 10$ MeV; the momentum-transfer rate is essentially independent of the DM mass, and thus so is the limit on σ_0 . At higher DM masses, however, the heat-exchange rate becomes larger for a fixed σ_0 : still neglecting the DM mass dependence of \bar{v}_{th} in the expression for R_χ , the heat-exchange rate coefficient scales as $R'_\chi \sim m_\chi / (m_\chi + m_p)^2$. Hence, at the higher end of the mass region in the right panel of Figure 8, T_χ is no longer negligible compared to T_b , and the momentum-transfer rate scales as $R_\chi \sim \sigma_0 (m_\chi + m_p)^{-1} (T_b/m_p + T_\chi/m_\chi)^{-3/2}$. It is thus reasonable to expect the limit on σ_0 to strengthen over a range of intermediate DM masses (*i.e.*, near the proton mass).

To capture the f_χ dependence of the limits in further detail, we again reanalyze *Planck* 2015 data for the case of $n = -4$, this time fixing the DM mass to $m_\chi = 1$ MeV and sampling the fraction f_χ as a free parameter. In the right panel of Figure 8, we show the resulting marginalized 2d posterior probability distribution for σ_0 versus f_χ ; the shaded region represents the outside of the 95% C.L. contour and is thus excluded. For $f_\chi \gtrsim 2\%$, the limit roughly scales with f_χ , independent of the DM mass. This scaling no longer holds for smaller values of f_χ : as a smaller fraction of DM particles scatters with baryons, CMB bounds permit a larger value of σ_0 . At sufficiently large σ_0 , the small interacting DM subcomponent allowed by data is tightly coupled to the baryons and undergoes (and amplifies) acoustic oscillations, and the effect of DM–baryon scattering on the power spectra saturates. Specifically, when the energy density of the interacting DM subcomponent approaches the uncertainty on the baryon energy density, the interacting DM subcomponent becomes cosmologically indistinguishable from baryons, and the limits on σ_0 entirely relax.⁹ We find that the relaxation occurs for fractions $f_\chi \lesssim 0.4\%$, which is consistent with the value $f_\chi \lesssim 0.6\%$, derived in the tight-coupling approximation [26].

We illustrate this effect in Figure 9, where we show the non-monotonic behavior of the residual in the TT spectra (with respect to ΛCDM) as a function of increasing σ_0 , for $m_\chi = 1$ MeV and $f_\chi = 0.3\%$ in the $n = -4$ case. The residuals are shown at its 95% C.L. upper limit, derived using the “main” prescription (black dotted) and for σ_0 above (purple) and below (green) the upper limit. Decreasing σ_0 well below its upper limit effectively turns off interactions between DM and baryons, and the residuals disappear. On the other hand, a sufficient increase in σ_0 brings the spectrum closer to the reference ΛCDM spectrum, and the residuals saturate as the DM and baryon fluids become as tightly coupled as possible.¹⁰ If the turnover in the residuals is detectable, the inferred posterior is bimodal; we see this behavior for fractions in the range $0.2\% \lesssim f_\chi \lesssim 0.4\%$ in Figure 8.

V. DISCUSSION AND CONCLUSIONS

We have conducted a comprehensive study of the impact of scattering between DM and protons on the CMB power spectra. In particular, we adopted a phenomenological approach of parameterizing the momentum-transfer cross section as $\sigma_{\text{MT}} = \sigma_0 v^n$ (where v is the relative velocity between the scattering particles) and focused on negative powers of velocity dependence that arise in well-motivated simplified models of DM interactions: $n = -2$ and $n = -4$. Such interactions are cosmologically important at times close to recombination, unlike the class of models with $n \geq 0$, for which scattering has the largest impact in the early Universe.

We assessed the impact of the relative bulk velocity between the DM and baryon fluids that may arise in the pre-recombination Universe, when the relative bulk velocity surpasses the relative thermal velocity dispersion. A large relative bulk velocity results in nonlinear Boltzmann equations and the mixing of Fourier modes. We presented a new treatment to sidestep these difficulties, while capturing the physics behind mode coupling: we introduce a mode-dependent RMS velocity dispersion as a proxy for the bulk relative velocity, and we incorporated it into the computation of the linear Boltzmann equations in a self-consistent manner appropriate for a cosmology that includes DM–baryon scattering.

We analyzed *Planck* 2015 temperature, polarization, and lensing data to search for evidence of DM–proton scattering. We found that the data are consistent with no interactions and use our results to produce upper limits on the coefficient of the momentum-transfer cross section as function of DM mass, shown in Figure 7 and provided in

⁹ The caveat is that DM does not participate in recombination and is thus not entirely degenerate with baryons.

¹⁰ Complications occur if the strength of DM interaction with baryons approaches that of the Compton interaction between baryons and photons before CMB decoupling. This regime significantly impacts acoustic oscillations and leads to strong numerical instabilities; thus, we do not consider it further.

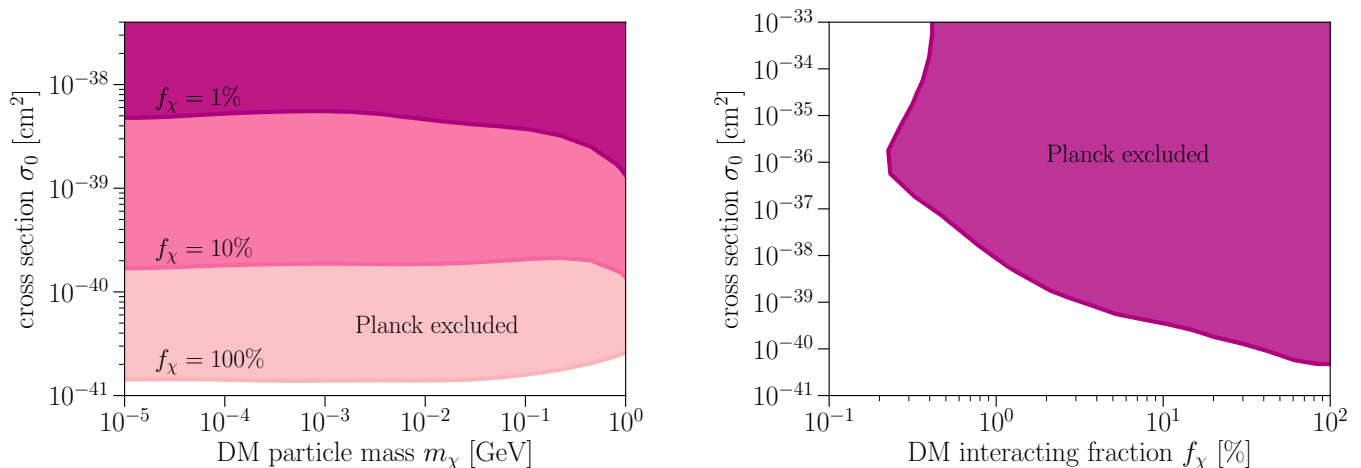


FIG. 8. **[Left]:** The 95% C.L. excluded region for the coefficient of the DM–proton momentum-transfer cross section as a function of DM mass, obtained by analyzing *Planck* 2015 data, when the interacting fraction f_χ of the total DM energy density is fixed to (from the lightest to the darkest pink): 1, 0.1, and 0.01. **[Right]:** The 95% C.L. excluded region for the coefficient of the DM–proton momentum-transfer cross section as a function of the interacting fraction f_χ of the total DM energy density, for a fixed DM mass $m_\chi = 1$ MeV; it is obtained by analyzing *Planck* 2015 temperature, polarization, and lensing anisotropy measurements, for the $n = -4$ interaction, allowing f_χ to vary as a free sampling parameter. The exclusion is bimodal for fractions $0.2\% \lesssim f_\chi \lesssim 0.4\%$ and constraints completely relax for $f_\chi \lesssim 0.2\%$ (where DM becomes cosmologically indistinguishable from a small additional amount of baryons).

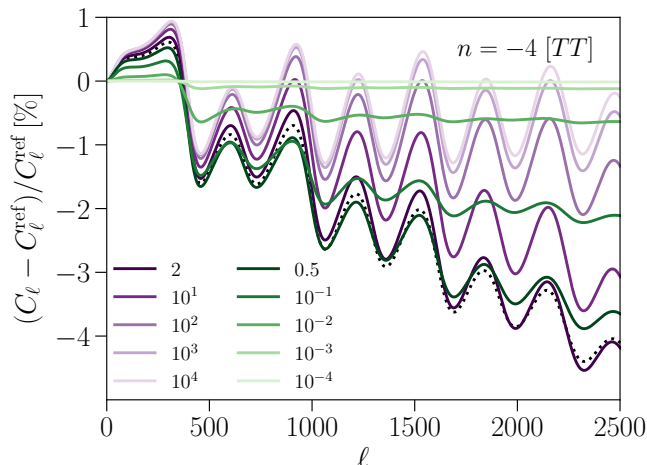


FIG. 9. Percent residuals (with respect to Λ CDM) of the lensed TT power spectra for the case of $n = -4$. The fraction of the total DM energy density in the interacting subcomponent is fixed to 0.3%, for a DM mass of 1 MeV, and we use the “main” prescription. We show the residuals with the coefficient of the momentum-transfer cross section σ_0 set to its 95% C.L. the upper limit (dotted black) and the residuals with σ_0 set to be a numerical factor—given in the legend—above (purple) and below (green) the upper limit. We see the non-monotonic behavior of the residuals as a function of σ_0 , which leads to the bimodality in the inferred posterior of Figure 8 around this value of f_χ , since the regime of the turnover is detectable with *Planck*.

Table I. Additionally, we considered the case in which only a small fraction of DM interacts with protons; for a DM mass of 1 MeV, we constrained the DM–proton interaction as a function of the fraction in Figure 8.

We discussed two regimes of DM–baryon scattering: weak-coupling regime, in which the momentum-transfer rate is inefficient due to Hubble expansion and damps acoustic oscillations on small scales; and a strong-coupling regime, in which DM and baryons are tightly coupled, resulting in DM undergoing acoustic oscillations with the baryons. If all the DM is allowed to interact with baryons, *Planck* data constrain the interaction to be in the weak-coupling regime. However, if only a fraction of DM interacts with baryons, constraints on the cross section progressively weaken as the fraction decreases. For fractions below $\sim 0.4\%$, we find that *Planck* constraints significantly degrade: the DM

and baryons are allowed to be so tightly coupled that DM essentially becomes cosmologically indistinguishable from a small additional amount of baryons.

Interestingly, such strongly-coupled dark matter could alleviate the mild tension between CMB and Big Bang Nucleosynthesis (BBN) measurement of the energy density of baryons. Recent BBN measurements of the deuterium abundance yield the values $\Omega_b h^2 = 0.02166 \pm 0.00015 \pm 0.00011$ [37] and $\Omega_b h^2 = 0.02174 \pm 0.00025$ [38], whereas the latest *Planck* 2018 data yield $\Omega_b h^2 = 0.02237 \pm 0.00015$ [39]. These BBN values for the baryon density are lower than the CMB value by the equivalent of 0.5%–0.6% of the DM energy density, and a strongly-coupled DM subcomponent with $f_\chi \sim 0.4\%$ could largely account for this discrepancy. This feature is not unique to $n = -4$; any interaction that tightly couples this subcomponent of DM to baryons around the time of recombination could be interpreted as an additional contribution to baryons.

The $n = -4$ interaction has received a fair amount of recent attention in light of DM interpretation of the EDGES signal [9]. The initial claim of Ref. [9] was that a phenomenological v^{-4} interaction could explain the EDGES signal—and our CMB analysis does not rule out such a possibility. However, our results do exclude a percent of millicharge-like DM scattering only with ions at the level needed to explain EDGES [16]. Under this millicharge scenario, our constraints are also complementary to bounds from a collider search at SLAC [40], stellar cooling [41], and the cooling of supernova 1987A [42]. These bounds limit the production of millicharged particles and are thus insensitive to the cosmological abundance millicharged DM. We explore the viable parameter space for millicharged DM in the context of EDGES in a separate study [17].

Finally, we presented a conservative forecast for the next-generation ground-based CMB-Stage 4 experiment, and showed a factor of ~ 3 improvement over *Planck* limits on σ_0 for the $n = -4$ interaction. Next-generation ground-based CMB surveys optimized for high-multipole science (where the signals of DM scattering may be particularly prominent) thus have a bright future in terms of DM searches with cosmological data.

ACKNOWLEDGMENTS

K. B. acknowledges the Aspen Center for Physics for their hospitality and support under NSF grant #PHY-1066293, where part of this work was completed. K. B. and V. G. acknowledge KITP and *The Small-Scale Structure of Cold(?) Dark Matter* workshop for their hospitality and support under NSF grant #PHY-1748958, during the completion of this work. V. G. acknowledges the support of the Eric Schmidt fellowship at the Institute for Advanced Study. This work was supported at Johns Hopkins in part by NSF Grant No. 1519353, NASA NNX17AK38G, and the Simons Foundation. For R. B., this publication was made possible through the support of a grant from the John Templeton Foundation; the opinions expressed in this publication are those of the author and do not necessarily reflect the views of the John Templeton Foundation. R. B. is also supported by the ISF-NSFC joint research program (grant No. 2580/17).

The authors thank Yacine Ali-Haïmoud and Julian Muñoz for useful discussions, and particularly Tracy Slatyer and Chih-Liang Wu for their help in cross-comparing residual CMB spectra between this work and Ref. [11].

Appendix A: Derivation of nonlinear terms

In this appendix, we derive the nonlinear terms that appear in the evolution of the DM and baryon peculiar velocities, \vec{v}_χ and \vec{v}_b , in Eq. (1) and in the evolution of their temperatures, T_χ and T_b , in Eq. (2). We drop all terms involving collisions between the baryons and photons for clarity, with the understanding that they must be incorporated to obtain the complete expressions for the baryons. The baryon fluid consists of various species (*i.e.*, electrons, protons, and helium nuclei), which are characterized by the same peculiar velocity and temperature. We denote a particular baryonic species with B and denote properties of baryon fluid as a whole with b . The species B has an energy density $\rho_B = Y_B \rho_b$, where Y_B is its mass fraction and $\sum_B Y_B = 1$. We assume the phase space distribution functions of the DM and baryons are Gaussian, given by

$$f_\chi(\vec{v}_\chi) = \frac{1}{(2\pi)^{3/2} \bar{v}_\chi^3} \exp\left[-\frac{(\vec{v}_\chi - \vec{V}_\chi)^2}{2\bar{v}_\chi^2}\right] \quad \text{and} \quad f_B(\vec{v}_B) = \frac{1}{(2\pi)^{3/2} \bar{v}_B^3} \exp\left[-\frac{(\vec{v}_B - \vec{V}_b)^2}{2\bar{v}_B^2}\right], \quad (\text{A1})$$

where $\bar{v}_\chi^2 = T_\chi/m_\chi$ and $\bar{v}_B^2 = T_b/m_B$ are the thermal velocity dispersions, and m_χ and m_B are the particle masses. Deriving the rates of momentum and heat transfer involves integrating the distribution functions over the velocities of the DM and baryon particles, \vec{v}_χ and \vec{v}_B , in the center-of-mass frame. Anticipating these calculations, it is convenient

to make a change of variables to

$$\vec{v}_m \equiv \frac{\bar{v}_B^2 \vec{v}_\chi + \bar{v}_\chi^2 \vec{v}_B}{\bar{v}_B^2 + \bar{v}_\chi^2} \quad \text{and} \quad \vec{v}_r \equiv \vec{v}_\chi - \vec{v}_b \quad (\text{A2})$$

such that the distribution functions remain factorizable [8]:

$$\int d^3 v_\chi f_\chi(\vec{v}_\chi) \int d^3 v_B f_B(\vec{v}_B) = \int d^3 v_r f_r(\vec{v}_r) \int d^3 v_m f_m(\vec{v}_m). \quad (\text{A3})$$

These new distribution functions have the Gaussian forms

$$f_m(\vec{v}_m) = \frac{1}{(2\pi)^{3/2} \bar{v}_m^3} \exp\left[-\frac{(\vec{v}_m - \vec{V}_m)^2}{2\bar{v}_m^2}\right] \quad \text{and} \quad f_r(\vec{v}_r) = \frac{1}{(2\pi)^{3/2} \bar{v}_r^3} \exp\left[-\frac{(\vec{v}_r - \vec{V}_r)^2}{2\bar{v}_r^2}\right], \quad (\text{A4})$$

where the means and dispersions are

$$\vec{V}_m = \frac{\bar{v}_B^2 \vec{V}_\chi + \bar{v}_\chi^2 \vec{V}_b}{\bar{v}_B^2 + \bar{v}_\chi^2} \quad \text{and} \quad \vec{V}_r = \vec{V}_\chi - \vec{V}_b, \quad \bar{v}_m^2 = \frac{\bar{v}_\chi^2 \bar{v}_B^2}{\bar{v}_\chi^2 + \bar{v}_B^2} \quad \text{and} \quad \bar{v}_r^2 = \bar{v}_\chi^2 + \bar{v}_B^2. \quad (\text{A5})$$

We consider interactions between DM particles and baryons B with momentum-transfer cross sections given by $\sigma_{\text{MT}} = \sigma_0 v_r^n$, and we are particularly interested in $n = -2$ and $n = -4$. As we show below, the rate calculations yield confluent hypergeometric functions of the first kind with the form

$${}_1F_1\left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{r^2}{2}\right) = \begin{cases} \frac{3}{2r^2} \left[\sqrt{\frac{\pi}{2}} \left(r - \frac{1}{r}\right) \text{Erf}\left(\frac{r}{\sqrt{2}}\right) + e^{-r^2/2} \right] & \text{for } n = -2 \\ \frac{3}{r^2} \left[\sqrt{\frac{\pi}{2}} \text{Erf}\left(\frac{r}{\sqrt{2}}\right) - r e^{-r^2/2} \right] & \text{for } n = -4 \end{cases} \quad (\text{A6})$$

$${}_1F_1\left(-\frac{n+3}{2}, \frac{3}{2}, -\frac{r^2}{2}\right) = \begin{cases} \frac{1}{2} \left[\sqrt{\frac{\pi}{2}} \left(r + \frac{1}{r}\right) \text{Erf}\left(\frac{r}{\sqrt{2}}\right) + e^{-r^2/2} \right] & \text{for } n = -2 \\ \frac{1}{r} \left[\sqrt{\frac{\pi}{2}} \text{Erf}\left(\frac{r}{\sqrt{2}}\right) \right] & \text{for } n = -4 \end{cases} \quad (\text{A7})$$

and an overall numerical constant

$$\mathcal{N}_n \equiv \frac{2^{(5+n)/2}}{3\sqrt{\pi}} \Gamma\left(3 + \frac{n}{2}\right) = \begin{cases} \frac{2}{3} \sqrt{\frac{2}{\pi}} & \text{for } n = -2 \\ \frac{1}{3} \sqrt{\frac{2}{\pi}} & \text{for } n = -4, \end{cases} \quad (\text{A8})$$

where we define $r \equiv V_r/\bar{v}_r$.

1. Momentum transfer

In a single collision between a DM particle χ and baryon B , the momentum of the DM particle changes by [3]

$$\Delta \vec{p}_\chi = \frac{m_\chi m_B}{m_\chi + m_B} |\vec{v}_\chi - \vec{v}_B| \left(\hat{n} - \frac{\vec{v}_\chi - \vec{v}_B}{|\vec{v}_\chi - \vec{v}_B|} \right), \quad (\text{A9})$$

where \hat{n} is the direction of the scattered DM particle in the center-of-mass frame. The resulting drag force per unit mass on the DM fluid is

$$\begin{aligned} D_\chi(\vec{V}_r) &= \frac{n_B}{m_\chi} \int d^3 v_\chi f_\chi(\vec{v}_\chi) \int d^3 v_B f_B(\vec{v}_B) \int d\Omega \frac{d\sigma}{d\Omega} v_r \Delta \vec{p}_\chi \\ &= -\frac{Y_B \rho_b \sigma_0}{m_\chi + m_B} \int d^3 v_r f_r(\vec{v}_r) v_r^{n+1} \vec{v}_r \int d^3 v_m f_m(\vec{v}_m), \end{aligned} \quad (\text{A10})$$

where we obtain the second line by completing the integration over angles to obtain the momentum-transfer cross section and by utilizing Eq. (A3). The integral over \vec{v}_m simply evaluates to 1, and the remaining integral over \vec{v}_r yields the result

$$D_\chi(\vec{V}_r) = -\frac{Y_B \rho_b \sigma_0 \mathcal{N}_n}{m_\chi + m_B} \bar{v}_r^{n+1} \vec{V}_r {}_1F_1\left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{r^2}{2}\right). \quad (\text{A11})$$

The evolution of the DM and baryon peculiar velocities obeys

$$\frac{\partial \vec{V}_\chi}{\partial \tau} - c_\chi^2 \vec{\nabla} \delta_\chi + \frac{\dot{a}}{a} \vec{V}_\chi = -a \sum_B \frac{Y_B \rho_b \sigma_0 \mathcal{N}_n}{m_\chi + m_B} \bar{v}_r^{n+1} \vec{V}_r {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{r^2}{2} \right) \quad (\text{A12})$$

$$\frac{\partial \vec{V}_b}{\partial \tau} - c_b^2 \vec{\nabla} \delta_b + \frac{\dot{a}}{a} \vec{V}_b = +a \sum_B \frac{Y_B \rho_\chi \sigma_0 \mathcal{N}_n}{m_\chi + m_B} \bar{v}_r^{n+1} \vec{V}_r {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{r^2}{2} \right). \quad (\text{A13})$$

If we neglect the terms proportional to the speeds of sound, c_χ and c_b , we may combine these equations to obtain the following expression for the evolution of the relative bulk velocity:

$$\frac{\partial \vec{V}_r}{\partial \tau} + \frac{\dot{a}}{a} \vec{V}_r = -a \sum_B \frac{Y_B (\rho_b + \rho_\chi) \sigma_0 \mathcal{N}_n}{m_\chi + m_B} \bar{v}_r^{n+1} \vec{V}_r {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{r^2}{2} \right). \quad (\text{A14})$$

By further assuming the baryon fluid is comprised of a single species with a mass given by the mean molecular weight μ_b and plugging in $n = -4$, we find

$$\frac{\partial \vec{V}_r}{\partial \tau} + \frac{\dot{a}}{a} \vec{V}_r = -a \frac{(\rho_b + \rho_\chi) \sigma_0}{m_\chi + \mu_b} \frac{\hat{V}_r}{V_r^2} \left[\text{Erf} \left(\frac{r}{\sqrt{2}} \right) - \sqrt{\frac{2}{\pi}} r e^{-r^2/2} \right], \quad (\text{A15})$$

which agrees with Ref. [8].

2. Heat transfer

The amount of energy transferred to the DM fluid is

$$\Delta E_\chi = \Delta \vec{p}_\chi \cdot \vec{v}_{\text{cm}}, \quad (\text{A16})$$

where the center-of-mass velocity may be written as

$$\vec{v}_{\text{cm}} = \vec{v}_m + \frac{m_\chi \bar{v}_\chi^2 - m_B \bar{v}_B^2}{(m_\chi + m_B)(\bar{v}_\chi^2 + \bar{v}_B^2)} \vec{v}_r. \quad (\text{A17})$$

In order to find the amount of heat transfer, we work in the instantaneous rest frame of the fluid so as not to incorporate its kinetic energy due to its bulk motion [8]. In Eqs. (A1) and (A5), for the DM fluid, we set $\vec{V}_\chi = 0$ and $\vec{V}_b = -\vec{V}_r$; for the baryon fluid, we set $\vec{V}_b = 0$ and $\vec{V}_\chi = \vec{V}_r$. The rate of heat exchange for the DM fluid is

$$\begin{aligned} \frac{dQ_\chi}{dt} &= \sum_B n_B \int d^3 v_\chi f_\chi(\vec{v}_\chi) \int d^3 v_B f_B(\vec{v}_B) \int d\Omega \frac{d\sigma}{d\Omega} v_r \Delta E_\chi \\ &= - \sum_B \frac{m_\chi Y_B \rho_b \sigma_0}{m_\chi + m_B} \int d^3 v_r f_r(\vec{v}_r) v_r^{n+1} \vec{v}_r \cdot \int d^3 v_m f_m(\vec{v}_m) \vec{v}_{\text{cm}}, \end{aligned} \quad (\text{A18})$$

where we obtain the second line by completing the integration over angles to obtain the momentum-transfer cross section and by utilizing Eq. (A3). For the first term in \vec{v}_{cm} , the integration over \vec{v}_m simply returns the mean \vec{V}_m ; while for the second term, there is no \vec{v}_m dependence and, after factoring out constants, the integration over \vec{v}_m returns 1. The remaining integral over \vec{v}_r yields the result

$$\begin{aligned} \frac{dQ_\chi}{dt} &= 3 \sum_B \frac{m_\chi Y_B \rho_b \sigma_0 \mathcal{N}_n}{(m_\chi + m_B)^2} \bar{v}_r^{n+1} \left\{ (T_b - T_\chi) \left[{}_1F_1 \left(-\frac{n+3}{2}, \frac{3}{2}, -\frac{r^2}{2} \right) - \frac{r^2}{3} {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{r^2}{2} \right) \right] \right. \\ &\quad \left. + \frac{m_B}{3} V_r^2 {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{r^2}{2} \right) \right\}. \end{aligned} \quad (\text{A19})$$

Similarly, the rate of heat exchange for the baryon fluid is

$$\begin{aligned} \frac{dQ_b}{dt} &= 3 \sum_B \frac{\mu_b \rho_\chi \sigma_0 \mathcal{N}_n}{(m_\chi + m_B)^2} \bar{v}_r^{n+1} \left\{ (T_\chi - T_b) \left[{}_1F_1 \left(-\frac{n+3}{2}, \frac{3}{2}, -\frac{r^2}{2} \right) - \frac{r^2}{3} {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{r^2}{2} \right) \right] \right. \\ &\quad \left. + \frac{m_\chi}{3} V_r^2 {}_1F_1 \left(-\frac{n+1}{2}, \frac{5}{2}, -\frac{r^2}{2} \right) \right\}. \end{aligned} \quad (\text{A20})$$

The temperature evolution equations are

$$\dot{T}_\chi + 2\frac{\dot{a}}{a}T_\chi = \frac{2}{3}a\frac{dQ_\chi}{dt} \quad \text{and} \quad \dot{T}_b + 2\frac{\dot{a}}{a}T_b = \frac{2}{3}a\frac{dQ_b}{dt}. \quad (\text{A21})$$

Assuming the baryon fluid is comprised of a single species with a mass given by the mean molecular weight μ_b and plugging in $n = -4$, we find

$$\dot{T}_\chi + 2\frac{\dot{a}}{a}T_\chi = \frac{2}{3}a\frac{m_\chi\rho_b\sigma_0}{(m_\chi + \mu_b)^2}\bar{v}_r^{-3} \left\{ \sqrt{\frac{2}{\pi}}(T_b - T_\chi)e^{-r^2/2} + \mu_b V_r^2 \frac{1}{r^3} \left[\text{Erf}\left(\frac{r}{\sqrt{2}}\right) - \sqrt{\frac{2}{\pi}}re^{-r^2/2} \right] \right\} \quad (\text{A22})$$

$$\dot{T}_b + 2\frac{\dot{a}}{a}T_b = \frac{2}{3}a\frac{\mu_b\rho_\chi\sigma_0}{(m_\chi + \mu_b)^2}\bar{v}_r^{-3} \left\{ \sqrt{\frac{2}{\pi}}(T_\chi - T_b)e^{-r^2/2} + m_\chi V_r^2 \frac{1}{r^3} \left[\text{Erf}\left(\frac{r}{\sqrt{2}}\right) - \sqrt{\frac{2}{\pi}}re^{-r^2/2} \right] \right\}, \quad (\text{A23})$$

which agrees with Ref. [8].

Appendix B: Implementation in CLASS

The implementation of the DM–baryon interaction requires modifying both the `thermodynamics` and the `perturbations` module of `CLASS`. In the `perturbations` module, we have incorporated the full Boltzmann system of equations (6). In principle, `CLASS` is able to solve for each k mode in parallel. However, the “main” prescription described in Section II B introduces mode mixing; thus, we must determine $V_{\text{RMS}}(k^*, z)$ and $V_{\text{flow}}(k^*, z)$ [which requires us to know the values of $\theta_b(k, z)$ and $\theta_\chi(k, z)$ at all k to perform the integration in Eqs. (4) and (5)] while concurrently solving the Boltzmann equations at a given redshift z and Fourier mode k^* [which requires us to know $V_{\text{RMS}}(k^*, z)$ and $V_{\text{flow}}(k^*, z)$ for the rate of momentum transfer in Eq. (7)]. To circumvent this difficulty, we repeat the calculations of the `perturbations` module, iteratively updating the values of $V_{\text{RMS}}(k^*, z)$ and $V_{\text{flow}}(k^*, z)$ until we achieve convergence at the 1% level. In practice, we initialize $V_{\text{RMS}}(k^*, z)$ and $V_{\text{flow}}(k^*, z)$ to the variance of the relative bulk velocity in Λ CDM given by Eq. (10) for all k ; the choice of the initial condition merely affects the number of iterations required to achieve convergence. This full procedure requires starting with sufficiently large k_{max} such that the relative bulk velocities are not coherent [10] for the highest range of redshifts that *Planck* is sensitive to. We find that $k_{\text{max}} = 5$ is sufficient for $V_{\text{RMS}}(k^*, z)$ to reach its plateau at high z , shown in the left panel of Figure 1.

In the `thermodynamics` module, we have included the modified thermal evolution of the baryon and DM fluids, given by Eq. (2). These evolution equations depend on the relative bulk velocity between the DM and baryon fluids, which we take to be the square root of the variance $\langle V_{\chi b}^2 \rangle$ to obtain the average evolution. We thus include the `thermodynamics` module within the iterative procedure, and recalculate the recombination and thermal history for each iteration. To compute the recombination of hydrogen and helium, `CLASS` can call either `Recfast` [43] or `HyRec` [44] code. Although `Recfast` provides a slight improvement in computational speed, it uses various “fudge functions” to achieve sub-percent accuracy [45] (established through validation against more accurate codes such as `HyRec` and `CosmoRec` [46] within Λ CDM), and thus may be unreliable for calculations within a modified cosmology. We have modified both recombination codes to include DM–proton scattering and find that our modified version of `Recfast` performs with very good accuracy. Given that `Recfast` is slightly faster, we use it to produce all numerical results shown in this work.

In `Recfast`, the recombination equation (before the introduction of “fudge functions”) takes the form of an effective three-level atom approximation: the evolution equation of the free-electron fraction x_e , which directly depends on the baryon temperature T_b , takes the form¹¹ [43]

$$\frac{dx_e(z)}{dz} = \frac{C}{(1+z)H(z)} \left[\alpha_H x_e^2 n_H - \beta_H (1 - x_e) e^{-\frac{h\nu_\alpha}{k_b T_\gamma}} \right], \quad (\text{B1})$$

where T_b is governed by Eq. (2). The coefficients $\alpha_H(T_b, T_\gamma)$ and $\beta_H(T_\gamma)$ are the effective recombination and photoionization rates, ν_α is the Lyman- α frequency, and C is the Peebles factor, representing the probability for an electron in the $n=2$ state to relax to the ground state before being ionized. An accurate calculation of the baryon temperature is essential, because it enters in the recombination rate; a smaller T_b can accelerate recombination and decrease the number of free electrons in the remaining plateau. However, both `HyRec` and `Recfast` do not follow the full evolution

¹¹ Following Ref. [47], we explicitly evaluate the photoionization rate as a function of T_γ , instead of T_b as done in the original version of `Recfast`.

of T_b up to the initial redshift of the calculation. Above the redshift $z \sim 850$, the codes assume that $T_b = T_\gamma - \epsilon$, and a linearized system of equation is solved instead [44, 48]. In **Recfast**, the switch to solving the full evolution equation is set by the ratio $r_{\text{CH}} \equiv t_C/t_H \sim 10^{-3}$, where t_C is the Compton interaction time and t_H the Hubble time [48]. We find that an incorrect generalization of the linearized steady-state approximation to include DM–proton interactions can lead to significant numerical glitches in the evolution of T_b , which artificially enhance the impact of DM–proton scattering on the CMB power spectra. We thus adapt the value of the switch such that we compute the full evolution equation up to $z \sim 10000$, before recombination starts. The impact of the DM–proton heat exchange on the baryon temperature is typically negligible before $z \sim 850$, because for any value of the momentum-transfer cross section not already excluded by *Planck* with a negative power-law scaling of the relative velocity, the cooling time t_χ is always negligible before the Compton time t_C until recombination. Hence, we neglect the modification to the baryon temperature at early times, when both codes solve the linearized system of equations. We correctly include DM–proton scattering at and below $z \simeq 850$, when the free-electron fraction and the Compton rate begin to drop. We have verified that both methods are in excellent agreement.

-
- [1] Xue-lei Chen, Steen Hannestad, and Robert J. Scherrer, “Cosmic microwave background and large scale structure limits on the interaction between dark matter and baryons,” *Phys. Rev. D* **65**, 123515 (2002), [astro-ph/0202496](#).
- [2] Kris Sigurdson, Michael Doran, Andriy Kurylov, Robert R. Caldwell, and Marc Kamionkowski, “Dark-matter electric and magnetic dipole moments,” *Phys. Rev. D* **70**, 083501 (2004), [Erratum: *Phys. Rev. D* 73, 089903 (2006)], [arXiv:astro-ph/0406355](#) [[astro-ph](#)].
- [3] Cora Dvorkin, Kfir Blum, and Marc Kamionkowski, “Constraining dark matter-baryon scattering with linear cosmology,” *Phys. Rev. D* **89**, 023519 (2014), [arXiv:1311.2937](#) [[astro-ph.CO](#)].
- [4] Vera Gluscevic and Kimberly K. Boddy, “Constraints on scattering of keV–TeV dark matter with protons in the early Universe,” [arXiv:1712.07133](#) [[astro-ph.CO](#)].
- [5] Kimberly K. Boddy and Vera Gluscevic, “First Cosmological Constraint on the Effective Theory of Dark Matter-Proton Interactions,” [arXiv:1801.08609](#).
- [6] Weishuang Linda Xu, Cora Dvorkin, and Andrew Chael, “Probing sub-GeV Dark Matter-Baryon Scattering with Cosmological Observables,” (2018), [arXiv:1802.06788](#).
- [7] Hiroyuki Tashiro, Kenji Kadota, and Joseph Silk, “Effects of dark matter-baryon scattering on redshifted 21 cm signals,” *Phys. Rev. D* **90**, 083522 (2014), [arXiv:1408.2571](#) [[astro-ph.CO](#)].
- [8] Julian B. Muñoz, Ely D. Kovetz, and Yacine Ali-Haïmoud, “Heating of baryons due to scattering with dark matter during the dark ages,” *Phys. Rev. D* **92**, 083528 (2015), [arXiv:1509.00029](#).
- [9] Rennan Barkana, “Possible interaction between baryons and dark-matter particles revealed by the first stars,” *Nature* **555**, 71–74 (2018), [arXiv:1803.06698](#) [[astro-ph.CO](#)].
- [10] Dmitriy Tsaliakhovich and Christopher Hirata, “Relative velocity of dark matter and baryonic fluids and the formation of the first structures,” *Phys. Rev. D* **82**, 083520 (2010), [arXiv:1005.2416](#).
- [11] Tracy R. Slatyer and Chih-Liang Wu, “Early-Universe Constraints on Dark Matter-Baryon Scattering and their Implications for a Global 21cm Signal,” (2018), [arXiv:1803.09734](#) [[astro-ph.CO](#)].
- [12] R. Adam *et al.* (Planck Collaboration), “Planck 2015 results. I. Overview of products and scientific results,” *Astron. Astrophys.* **594**, A1 (2016), [arXiv:1502.01582](#).
- [13] N. Aghanim *et al.* (Planck Collaboration), “Planck 2015 results. XI. CMB power spectra, likelihoods, and robustness of parameters,” *Astron. Astrophys.* **594**, A11 (2016), [arXiv:1507.02704](#).
- [14] K. N. Abazajian *et al.* (CMB-S4), “CMB-S4 Science Book, First Edition,” [arXiv:1610.02743](#).
- [15] Judd D. Bowman, Alan E. E. Rogers, Raul A. Monsalve, Thomas J. Mozdzen, and Nivedita Mahesh, “An absorption profile centred at 78 megahertz in the sky-averaged spectrum,” *Nature* **555**, 67–70 (2018).
- [16] Rennan Barkana, Nadav Joseph Outmezguine, Diego Redigolo, and Tomer Volansky, “Signs of Dark Matter at 21-cm?” (2018), [arXiv:1803.03091](#) [[hep-ph](#)].
- [17] Ely D. Kovetz, Vivian Poulin, Vera Gluscevic, Kimberly K. Boddy, Rennan Barkana, and Marc Kamionkowski, “Tighter Limits on Dark Matter Explanations of the Anomalous EDGES 21cm Signal,” (2018), [arXiv:1807.11482](#) [[astro-ph.CO](#)].
- [18] Riccardo Catena and Bodo Schwabe, “Form factors for dark matter capture by the Sun in effective theories,” *J. Cosmol. Astropart. Phys.* **4**, 042 (2015), [arXiv:1501.03729](#) [[hep-ph](#)].
- [19] Diego Blas, Julien Lesgourgues, and Thomas Tram, “The Cosmic Linear Anisotropy Solving System (CLASS). Part II: Approximation schemes,” *J. Cosmol. Astropart. Phys.* **7**, 034 (2011), [arXiv:1104.2933](#) [[astro-ph.CO](#)].
- [20] P. A. R. Ade *et al.* (Planck), “Planck 2015 results. XIII. Cosmological parameters,” *Astron. Astrophys.* **594**, A13 (2016), [arXiv:1502.01589](#) [[astro-ph.CO](#)].
- [21] Uros Seljak and Matias Zaldarriaga, “A Line of sight integration approach to cosmic microwave background anisotropies,” *Astrophys. J.* **469**, 437–444 (1996), [arXiv:astro-ph/9603033](#) [[astro-ph](#)].
- [22] Vivian Poulin, Julien Lesgourgues, and Pasquale D. Serpico, “Cosmological constraints on exotic injection of electromagnetic energy,” *J. Cosmol. Astropart. Phys.* **1703**, 043 (2017), [arXiv:1610.10051](#) [[astro-ph.CO](#)].
- [23] Manuel A. Buen-Abad, Martin Schmaltz, Julien Lesgourgues, and Thejs Brinckmann, “Interacting Dark Sector and

- Precision Cosmology,” *J. Cosmol. Astropart. Phys.* **1801**, 008 (2018), [arXiv:1708.09406 \[astro-ph.CO\]](#).
- [24] Marc Kamionkowski, Arthur Kosowsky, and Albert Stebbins, “Statistics of cosmic microwave background polarization,” *Phys. Rev. D* **55**, 7368–7388 (1997), [arXiv:astro-ph/9611125 \[astro-ph\]](#).
- [25] Matias Zaldarriaga and Uros Seljak, “An all sky analysis of polarization in the microwave background,” *Phys. Rev. D* **55**, 1830–1840 (1997), [arXiv:astro-ph/9609170 \[astro-ph\]](#).
- [26] Roland de Putter, Olivier Doré, Jérôme Gleyzes, Daniel Green, and Joel Meyers, “Dark Matter Interactions, Helium, and the CMB,” (2018), [arXiv:1805.11616 \[astro-ph.CO\]](#).
- [27] S. L. Dubovsky, D. S. Gorbunov, and G. I. Rubtsov, “Narrowing the window for millicharged particles by CMB anisotropy,” *JETP Lett.* **79**, 1–5 (2004), [*Pisma Zh. Eksp. Teor. Fiz.* 79,3(2004)], [arXiv:hep-ph/0311189 \[hep-ph\]](#).
- [28] A. D. Dolgov, S. L. Dubovsky, G. I. Rubtsov, and I. I. Tkachev, “Constraints on millicharged particles from Planck data,” *Phys. Rev. D* **88**, 117701 (2013), [arXiv:1310.2376 \[hep-ph\]](#).
- [29] Benjamin Audren, Julien Lesgourgues, Karim Benabed, and Simon Prunet, “Conservative constraints on early cosmology with MONTE PYTHON,” *J. Cosmol. Astropart. Phys.* **2**, 001 (2013), [arXiv:1210.7183 \[astro-ph.CO\]](#).
- [30] J. Buchner, A. Georgakakis, K. Nandra, L. Hsu, C. Rangel, M. Brightman, A. Merloni, M. Salvato, J. Donley, and D. Kocevski, “X-ray spectral modelling of the AGN obscuring region in the CDFS: Bayesian model selection and catalogue,” *Astron. Astrophys.* **564**, A125 (2014), [arXiv:1402.0004 \[astro-ph.HE\]](#).
- [31] F. Feroz and M. P. Hobson, “Multimodal nested sampling: an efficient and robust alternative to Markov Chain Monte Carlo methods for astronomical data analyses,” *Mon. Not. R. Astron. Soc.* **384**, 449–463 (2008), [arXiv:0704.3704](#).
- [32] F. Feroz, M. P. Hobson, and M. Bridges, “MULTINEST: an efficient and robust Bayesian inference tool for cosmology and particle physics,” *Mon. Not. R. Astron. Soc.* **398**, 1601–1614 (2009), [arXiv:0809.3437](#).
- [33] F. Feroz, M. P. Hobson, E. Cameron, and A. N. Pettitt, “Importance Nested Sampling and the MultiNest Algorithm,” [arXiv:1306.2144 \[astro-ph.IM\]](#).
- [34] Andrew Gelman and Donald B. Rubin, “Inference from Iterative Simulation Using Multiple Sequences,” *Statist. Sci.* **7**, 457–472 (1992).
- [35] Daniel Foreman-Mackey, “corner.py: Scatterplot matrices in python,” *The Journal of Open Source Software* **24** (2016), [10.21105/joss.00024](#).
- [36] Zack Li, Vera Gluscevic, Kimberly K. Boddy, and Mathew S. Madhavacheril, “Disentangling Dark Physics with Cosmic Microwave Background Experiments,” (2018), [arXiv:1806.10165 \[astro-ph.CO\]](#).
- [37] Ryan J. Cooke, Max Pettini, and Charles C. Steidel, “One Percent Determination of the Primordial Deuterium Abundance,” *Astrophys. J.* **855**, 102 (2018), [arXiv:1710.11129 \[astro-ph.CO\]](#).
- [38] E. O. Zavarygin, J. K. Webb, S. Riemer-Sørensen, and V. Dumont, “Primordial deuterium abundance at $z_{abs} = 2:504$ towards Q1009+2956,” *Proceedings, International Youth Conference Physica.Spb/2017: Saint-Petersburg, Russia, October 24-26, 2014*, *J. Phys. Conf. Ser.* **1038**, 012012 (2018), [arXiv:1801.04704 \[astro-ph.CO\]](#).
- [39] N. Aghanim *et al.* (Planck), “Planck 2018 results. VI. Cosmological parameters,” (2018), [arXiv:1807.06209 \[astro-ph.CO\]](#).
- [40] A. A. Prinz *et al.*, “Search for Millicharged Particles at SLAC,” *Phys. Rev. Lett.* **81**, 1175–1178 (1998), [arXiv:hep-ex/9804008 \[hep-ex\]](#).
- [41] Hendrik Vogel and Javier Redondo, “Dark radiation constraints on minicharged particles in models with a hidden photon,” *J. Cosmol. Astropart. Phys.* **2**, 029 (2014), [arXiv:1311.2600 \[hep-ph\]](#).
- [42] Jae Hyeok Chang, Rouven Essig, and Samuel D. McDermott, “Supernova 1987A Constraints on Sub-GeV Dark Sectors, Millicharged Particles, the QCD Axion, and an Axion-like Particle,” *JHEP* **09**, 051 (2018), [arXiv:1803.00993 \[hep-ph\]](#).
- [43] Sara Seager, Dimitar D. Sasselov, and Douglas Scott, “A new calculation of the recombination epoch,” *Astrophys. J.* **523**, L1–L5 (1999), [arXiv:astro-ph/9909275 \[astro-ph\]](#).
- [44] Yacine Ali-Haïmoud and Christopher M. Hirata, “HyRec: A fast and highly accurate primordial hydrogen and helium recombination code,” *Phys. Rev. D* **83**, 043513 (2011), [arXiv:1011.3758 \[astro-ph.CO\]](#).
- [45] J. A. Rubino-Martin, J. Chluba, W. A. Fendt, and B. D. Wandelt, “Estimating the impact of recombination uncertainties on the cosmological parameter constraints from cosmic microwave background experiments,” *Mon. Not. R. Astron. Soc.* **403**, 439 (2010), [arXiv:0910.4383 \[astro-ph.CO\]](#).
- [46] J. Chluba and R. M. Thomas, “Towards a complete treatment of the cosmological recombination problem,” *Mon. Not. R. Astron. Soc.* **412**, 748 (2011), [arXiv:1010.3631 \[astro-ph.CO\]](#).
- [47] Jens Chluba, D. Paoletti, F. Finelli, and Jose-Alberto Rubio-Martín, “Effect of primordial magnetic fields on the ionization history,” *Mon. Not. R. Astron. Soc.* **451**, 2244–2250 (2015), [arXiv:1503.04827 \[astro-ph.CO\]](#).
- [48] Douglas Scott and Adam Moss, “Matter temperature after cosmological recombination,” *Mon. Not. R. Astron. Soc.* **397**, 445–446 (2009), [arXiv:0902.3438 \[astro-ph.CO\]](#).