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Particle Swarm Optimization based search for gravitational waves from compact binary coalescences: performance improvements

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While a fully-coherent all-sky search is known to be optimal for detecting signals from compact binary coalescences (CBCs), its high computational cost has limited current searches to less sensitive coincidence-based schemes. For a network of first generation GW detectors, it has been demonstrated that Particle Swarm Optimization (PSO) can reduce the computational cost of this search, in terms of the number of likelihood evaluations, by a factor of $\approx 10$ compared to a grid-based optimizer. Here, we extend the PSO-based search to a network of second generation detectors and present further substantial improvements in its performance by adopting the local-best variant of PSO and an effective strategy for tuning its configuration parameters. It is shown that a PSO-based search is viable over the entire binary mass range relevant to second generation detectors at realistic signal strengths.

I. INTRODUCTION

The advanced Laser Interferometric Gravitational-wave Observatory (LIGO) [1] and the Advanced Virgo [2] detectors have detected gravitational waves (GWs) from several compact binary coalescence (CBC) events over their recently concluded observation runs. Among the detected signals, GW150914 [3], GW151226 [4], and GW170104 [5] are binary black hole (BBH) mergers detected in two-way coincidence between the LIGO detectors, while GW170814 [6] is a BBH merger detected in three-way coincidence after Virgo joined the LIGO observation runs. GW170817 [7], the final event in the last observing run, was a binary neutron star (BNS) inspiral. Its prompt localization on the sky by the LIGO-Virgo network allowed the detection of an electromagnetic (EM) counterpart [8], establishing BNS mergers as the source of some short gamma-ray bursts.

Over the next few years, LIGO and Virgo will be joined by the KAGRA [9] detector in Japan and LIGO-India [10]. Combining the data from this network of geographically distributed second generation detectors will significantly increase both the detection sensitivity and sky localization of CBC sources [11, 12].

It is known that the optimal data analysis methods for the detection and estimation of CBC signals with a network of GW detectors are the Generalized Likelihood Ratio Test (GLRT) and Maximum Likelihood Estimation (MLE) respectively [13]. In the GW literature, the GLRT is called the fully coherent all-sky search. (For a single detector, the GLRT is the matched filter [14].)

In both GLRT and MLE, the joint likelihood function of data from a network of detectors needs to be maximized over the space of CBC signal parameters. However, the computational cost of this task has proven to be a limiting factor in running the GLRT as an always-on search. The difficulty of the optimization stems from a combination of (i) the high dimensionality of the search space, and (ii) the high computational cost of evaluating the likelihood at a given point in the search space. The latter is due to the requirement of correlating pairs of time series that involve $O(10^6)$ samples each (for low binary component masses).

To circumvent the computational bottleneck above, current CBC searches use a coincidence-based semi-coherent approach in which the GLRT is only used when (i) computationally cheaper single-detector matched filter searches result in the crossing of preset detection thresholds in any pair of detectors, and (ii) the corresponding estimated signal parameters are proximal within some preset tolerances. As shown in [15], a semi-coherent search trades-off a significant amount of sensitivity for the reduced computational cost, with the detection volume being $\sim 25\%$ smaller than a fully-coherent search.

It has recently been demonstrated in [16], henceforth referred to as WM, that Particle Swarm Optimization (PSO) [17], a family of stochastic global optimization methods based on the behavior of biological swarms, can potentially solve this challenge. Simulation of a four detector network, coinciding with the location and orientation of the LIGO Hanford (H), LIGO Livingston (L), Virgo (V), and KAGRA (K), showed that the number of likelihood evaluations required by PSO is $\sim 1/10$ that of a grid-based search in which the search space is populated densely with a fixed set of sampling locations.

The results in WM were derived under the following limitations. (i) It was assumed that the noise in each
detector had a Power Spectral Density (PSD) given by the initial LIGO design sensitivity curve [18]. This was primarily done to keep signal lengths short (≤ 30 sec) and the computational run time manageable given the MATLAB [19] based implementation of the search. (ii) As with any stochastic optimization algorithm, PSO is not guaranteed to converge to the global optimum. For the so-called global-best variant of PSO used in WM, this led to a small but non-zero reduction in detection probability of ≤ 2.5%. (iii) A PSO-based search can be parallelized efficiently in a multi-processor environment but the code did not implement all of the possible layers of parallelization.

In this paper, we develop the PSO-based fully-coherent all-sky search further by overcoming the above limitations. (i) We shift to the advanced LIGO design sensitivity and examine the performance of PSO for both short (O(1) min) and long (O(30) min) data lengths. (ii) We use the local-best variant of PSO and find it to be significantly better in terms of convergence, achieving ≤ 0.5% loss in detection probability for ≈ 1 min long data at lower signal strengths than the one used in WM. (iii) Besides translating the code into the C language, a two-layered parallelization scheme is implemented that speeds up execution by a factor of ≈ 7.5.

The rest of the paper is organized as follows. Sec II sets up the data model used in this paper and provides pertinent details of the fully-coherent all-sky search. Sec. III describes the local best PSO algorithm and a general purpose strategy for tuning its performance on parametric GW data analysis problems. The simulation setup and results on detection and estimation performance of the PSO-based search are presented in Sec. IV. The computation time of the current code is discussed in Sec. V along with possible future avenues that could reduce it substantially. The conclusions from our study are presented in Sec VI.

II. FULLY-COHERENT ALL-SKY SEARCH

While the review of the data model and the fully-coherent all-sky search in this section provides a self-contained background for the rest of the paper, we refer the reader to WM and references therein for a comprehensive presentation of mathematical details.

A. Data and Signal Models

Consider the $i^{th}$ detector in a network of $D$ detectors. A segment of the strain time series recorded by the detector is given by

$$x^{i}(t) = \begin{cases} n^{i}(t); & H_{0}, \\ h^{i}(t) + n^{i}(t); & H_{1} \end{cases}$$

where $h^{i}(t)$ is the detector response to the incident GW and $n^{i}(t)$ denotes detector noise. $H_{0}$ and $H_{1}$ correspond to the two hypotheses one can propose about the data where a signal is, respectively, absent or present.

We will assume that $n^{i}(t)$ is a realization of a zero-mean, stationary Gaussian stochastic process,

$$E[n^{i}(t)] = 0; \quad (2)$$

$$E[n^{i}(t)n^{i}(t')] = \frac{1}{2} \int_{-\infty}^{\infty} \delta(t-t') S_{n}(f) , \quad (3)$$

with $S_{n}(f)$ denoting the one-sided noise power spectral density (PSD). It does not carry a detector index in this paper because we assume identical PSD for all the detectors.

For a source located at an azimuthal angle $\alpha$ and polar angle $\delta$ in the Earth Centered Earth Fixed Frame (ECEF) [20], the detector responses are given by

$$\begin{pmatrix} h^{1}(t + \Delta^{1}(\alpha, \delta)) \\ h^{2}(t + \Delta^{2}(\alpha, \delta)) \\ \vdots \\ h^{D}(t + \Delta^{D}(\alpha, \delta)) \end{pmatrix} = \mathbf{F}(\alpha, \delta, \psi) \begin{pmatrix} h_{+}(t) \\ h_{x}(t) \end{pmatrix} , \quad (4)$$

where the $i^{th}$ row of the antenna pattern matrix $\mathbf{F}(\alpha, \delta, \psi)$ contains the antenna pattern functions $(F^{+}_{i}(\alpha, \delta, \psi), F^{x}_{i}(\alpha, \delta, \psi))$ of the $i^{th}$ detector, $h_{+}(t)$ and $h_{x}(t)$ are the TT gauge polarization components of the GW plane wave incident on the origin of the ECEF, and $\Delta^{i}(\alpha, \delta)$ is the time delay between the plane wave hitting the ECEF origin and the $i^{th}$ detector. The polarization angle $\psi$ gives the orientation of the wave frame axes with respect to the fiducial basis formed by $-\hat{\alpha}$ and $\hat{\delta}$ in the plane orthogonal to the wave propagation direction.

The condition number [21] of the antenna pattern matrix as a function of $\alpha$ and $\delta$ plays an important role in determining the errors in the estimation of the source location [22]. In general, the errors worsen as the condition number at the source location increases. However, as will be apparent in Sec. IV C, the influence of the condition number is more subtle than this empirical rule of thumb.

In this paper, we use a four-detector network consisting of the two LIGO detectors at Hanford (H) and Livingston (L), Virgo (V) and KAGRA (K). For simplicity, we assume the advanced LIGO design PSD [23] corresponding to the “ZERO DET high P” configuration for the noise in each detector. The orientations and locations of the detectors, listed in table II of WM, match their real-world values. A sky map of the condition number of the antenna pattern matrix for the above detector network is shown in Figure 4 of WM.

The polarizations $h_{+}(t)$ and $h_{x}(t)$ used in this paper are given by the restricted 2-PN waveform from a circularized binary consisting of non-spinning compact objects [24] that depends on the following parameters. (i) The component masses $m_{1}$ and $m_{2}$ expressed through
the chirp times $\tau_0$ and $\tau_{1.5}$,
\[
\tau_0 = \frac{5}{256\pi} f_s^{-1} \left( \frac{GM}{c^3} \pi f_s \right)^{-5/3} \eta^{-1},
\]
(5)
\[
\tau_{1.5} = \frac{1}{8} f_s^{-1} \left( \frac{GM}{c^3} \pi f_s \right)^{-2/3} \eta^{-1},
\]
(6)
\[
M = m_1 + m_2, \quad \mu = \frac{m_1 m_2}{M}, \quad \eta = \mu M,
\]
(7)
where $f_s$, set to 10 Hz in this paper, is the lower cutoff frequency of the detector arising from the steep rise in seismic noise. (ii) The time $t_c$ at which the end of the inspiral signal arrives at the ECEF origin. (iii) The phase of the signal at $t_c$ given by $\phi_c$. (iv) The overall amplitude of the signal denoted by $A$. The duration of the signal starting from the time at which its instantaneous frequency equals $f_s$ to $t_c$ is given by $\tau_0 + \tau_1 = \tau_{1.5} + \tau_2$ where,
\[
\tau_1 = \frac{5}{192\pi} f_s^{-1} \left( \frac{GM}{c^3} \pi f_s \right)^{-1} \eta^{-1} \left( \frac{743}{336} + \frac{11}{4} \eta \right),
\]
(8)
\[
\tau_2 = \frac{5}{128\pi} f_s^{-1} \left( \frac{GM}{c^3} \pi f_s \right)^{-1/3} \eta^{-1} \left( \frac{3058673}{1016064} + \frac{5429}{108} \eta + \frac{617}{144} \eta^2 \right),
\]
(9)
are additional chirp times for the 2PN waveform.

**B. Likelihood ratio for a detector network**

Under our assumption of Gaussian, stationary noise, the log-likelihood Ratio (LLR) [25] for the $i^{th}$ detector is given by,
\[
\ln \lambda^i = \langle x^i | h^i \rangle - \frac{1}{2} \langle h^i | h^i \rangle,
\]
(10)
where, with $\tilde{a}(f)$ denoting the Fourier transform of any function $a(t)$ of time,
\[
\langle p | q \rangle = 4 \text{ Re } \int_0^\infty df \frac{\tilde{p}(f) \tilde{q}^*(f)}{S_a(f)} .
\]
(11)

If we assume the noise in different detectors to be statistically independent, the log-likelihood for a $D$ detector network is given by,
\[
\ln \lambda = \sum_{i=1}^D \left[ \langle x^i | h^i \rangle - \frac{1}{2} \langle h^i | h^i \rangle \right].
\]
(12)

It follows that, for a given data realization, the log-likelihood is a function of the parameters $\theta = \{\tau_0, \tau_{1.5}, \alpha, \delta, t_c\}, A, \psi, \text{ and } \phi_c$.

The GLRT statistic is the global maximum of the LLR over the parameters mentioned above. Adopting the notation in [26], we use the equivalent of the GLRT statistic defined as
\[
\rho_{\text{coh}}^2 = 2 \max_{A,\psi,\phi_c,\theta} \ln \lambda ,
\]
(13)
and call $\rho_{\text{coh}}$ the *coherent search statistic*. The Maximization can be carried out as,
\[
\rho_{\text{coh}}^2 = \max_{\theta} \gamma^2(\theta),
\]
(14)
\[
\gamma^2(\theta) = 2 \max_{A,\psi,\phi_c} \ln \lambda .
\]
(15)
The inner maximization can be performed analytically, while the outer maximization over $\theta$ must be carried out numerically.

For fixed $\{\tau_0, \tau_{1.5}, \alpha, \delta\}$, the maximization over $t_c$ can be carried out very efficiently using the Fast Fourier Transform (FFT) [26]. The FFT-based approach is made especially convenient by the fact that the polarization waveforms can be generated directly in the Fourier domain using the stationary phase approximation [27]. Thus, the outer maximization can be further split over $\Theta = \{\tau_0, \tau_{1.5}, \alpha, \delta\}$ and $t_c$. We call the *coherent fitness function*. The computational cost of maximizing the coherent fitness over $\Theta$ is the main challenge in the implementation of a fully coherent search.

In any practical implementation of the fully-coherent all-sky search, the data streams from GW detectors must be analyzed in finite length segments. Consequently, for fixed $\Theta$, $\gamma^2(\theta)$ is not valid for $t_c$ greater than the length of the segment being analyzed. However, the FFT-based calculation generates $\gamma^2(\theta)$ for $t_c$ going up to the sum of the segment length and the length of the signal corresponding to $\Theta$. To account for this effect, the spurious values of $\gamma^2(\theta)$ are deleted and consecutive data segments are overlapped by at least the length of the signal. In this paper, we analyze simulated data realizations that are generated independently of each other. Hence, there is no need to overlap them. However, care is taken to ensure that the signal embedded in the data has a $t_c$ that is sufficiently small. As long as the estimated $t_c$ does not stray too far from its true value, which was verified to be the case in our simulations, ignoring deletion and overlapping does not affect our results.

**III. PARTICLE SWARM OPTIMIZATION**

Although PSO started off as a single algorithm, the term now refers to a diverse set of algorithms and it is viewed more properly as a metaheuristic – a general approach to optimization based on a particular type of physical or biological model. In the case of PSO, the model happens to be the flocking or swarming behavior of biological agents (birds, fish etc.). In fact, the PSO metaheuristic is one among many others that are inspired by nature.

PSO uses a fixed number of samples (called *particles*) of the function to be optimized (called the *fitness function*). The particles move in the search space following stochastic iterative rules called the *dynamical equations*. 
In WM, the PSO algorithm used was the global-best (or gbest) variant. In this paper, we use the local-best (or lbest) variant of PSO described below that leads to a significantly improved performance.

A. The lbest PSO algorithm

We adopt the following notation in this section for describing lbest PSO.

- \( f(x) \): the scalar fitness function to be maximized, with \( x = (x^1, x^2, \ldots, x^d) \in \mathbb{R}^d \). In our case, \( x = \Theta, f(x) \) is the coherent fitness function \( \Gamma^2(\Theta) \) (c.f., Eq. 16) and \( d = 4 \).

- \( S \subset \mathbb{R}^d \): the search space defined by the hypercube \( a^i \leq x^i \leq b^i, \ i = 1, 2, \ldots, d \). Among a set of locations in \( S \), the best location is the one with the maximum fitness.

- \( N_p \): the number of particles in the swarm.

- \( x_i[k] \): the position of the \( i^{th} \) particle at the \( k^{th} \) iteration.

- \( p_i[k] \): the best location found by the \( i^{th} \) particle over all iterations up to and including the \( k^{th} \). \( p_i[k] \) is called the personal best position of the \( i^{th} \) particle.

\[
f(p_i[k]) = \max_{j \leq k} f(x_i[j]) . \tag{17}
\]

- \( n_i[k] \): a set of particles, called the nearest neighbors of particle \( i \), \( n_i[k] \subseteq \{1, 2, \ldots, N_p\} \setminus \{i\} \). There are many possibilities, called topologies, for the choice of \( n_i[k] \). In this paper, we use the ring topology with 2 neighbors in which

\[
n_i[k] = \begin{cases} 
\{i - 1, i + 1\} , & i \notin \{1, N_p\} \\
\{N_p, i + 1\} , & i = 1 \\
\{i - 1, 1\} , & i = N_p 
\end{cases} . \tag{18}
\]

- \( l_i[k] \): the best location among the particles in \( n_i[k] \). \( l_i[k] \) is called the local best position of the \( i^{th} \) particle.

\[
f(l_i[k]) = \max_{j \in \{i\} \cup n_i[k]} f(x_j[k]) . \tag{19}
\]

- \( p_g[k] \): The best location among all the particles over all iterations up to and including the \( k^{th} \).

\[
f(p_g[k]) = \max_{1 \leq j \leq N_p} f(x_j) . \tag{20}
\]

The dynamical equations for lbest PSO are as follows.

\[
v_i[k + 1] = w[k]v_i[k] + c_1 r_1(p_i[k] - x_i[k]) + c_2 r_2(l_i[k] - x_i[k]) . \tag{21}
\]

\[
x_i[k + 1] = x_i[k] + z_i[k + 1] , \tag{22}
\]

\[
z_i^j[k] = \begin{cases} 
v_i^j[k] , & -v_{max}^j \leq v_i^j[k] \leq v_{max}^j \\
-v_{max}^j , & v_i^j[k] < -v_{max}^j \\
v_{max}^j , & v_i^j[k] > v_{max}^j 
\end{cases} . \tag{23}
\]

Here, \( v_i[k] \) is called the “velocity” of the \( i^{th} \) particle, \( w[k] \) is a deterministic function known as the inertia weight (see below), \( c_1 \) and \( c_2 \) are constants, and \( r_i \) is a diagonal matrix with independent, identically distributed random variables having a uniform distribution over \([0, 1]\). The second and third terms on the RHS of Eq. 21 are called the cognitive and social terms respectively.

The iterations are initialized at \( k = 1 \) by independently drawing \( (i) x_i^1[1] \) from a uniform distribution over \([a^i, b^i]\), and \( (ii) v_i^j[1] \) from a uniform distribution over \([-v_{max}^j, v_{max}^j]\). The algorithm terminates when the number of iterations reaches a prescribed number \( N_{iter} \). The solutions to the maximizer and maximum value of the fitness found by PSO are \( p_g[N_{iter}] \) and \( f(p_g[N_{iter}]) \) respectively.

To handle particles that exit the search space, we use the “let them fly” boundary condition under which a particle outside the search space is assigned a fitness value of \(-\infty\). Since both \( p_i[k] \) and \( l_i[k] \) are always within the search space, such a particle is eventually dragged back into the search space by the cognitive and social terms.

Every practical stochastic optimization method, including PSO, has two fairly distinct phases, called exploration and exploitation, of behavior. In the case of PSO, the exploratory phase involves a rapid increase in the best fitness value as the particles quickly find better locations compared to their initial ones. At some point the behavior of the particle swarm transitions into the exploitative phase in which the particles converge to a promising region of the search space where the improvement in the best fitness value becomes considerably slower.

The role of the inertia weight, \( w[k] \), is to control the degree of exploration of the search space by allowing a particle to overcome the attractive cognitive and social terms. In the version of PSO used here, the inertia weight \( w[k] \) decreases linearly with \( k \) from an initial value \( w_{max} \) to a final value \( w_{min} \). Decreasing the inertia weight transitions PSO from the initially exploratory to a final exploitative phase, and the longer the interval, namely \( N_{iter} \), over which this happens, the later the onset of the transition.

B. PSO tuning metric

As mentioned earlier, PSO is not guaranteed to converge to the global optimum of a fitness function and, as with any stochastic optimization algorithm, its parameters need to be tuned for it to perform well on
a given fitness function. Fortunately, extensive studies have shown that most of the parameters of PSO can be set at near-fiducial values across a wide range of fitness functions [28]. In WM, the only parameter that was tuned was \( N_{\text{iter}} \), while the rest were fixed as follows: \( N_p = 40, c_1 = c_2 = 2.0, w_{\text{max}} = 0.9, w_{\text{min}} = 0.4, \) and \( v_{\text{max}} = 0.2. \)

For a given \( N_{\text{iter}} \), the probability of convergence can be increased by the simple strategy of running multiple runs of PSO on the same data realization and choosing the best fitness value found across the runs. The probability of missing the global optimum decreases exponentially as \((1 - P_{\text{conv}})^{N_{\text{runs}}}\), where \( P_{\text{conv}} \) is the probability of successful convergence in any one run. This strategy was used in WM with an ad hoc choice for \( N_{\text{runs}} \). In this paper, we propose a metric-based objective process for tuning both \( N_{\text{runs}} \) and \( N_{\text{iter}} \).

The metric we use for tuning PSO follows from [29] and is based on the fact that estimation error is caused by a shift of the global maximum of the coherent fitness function away from the true signal parameters. Therefore, the minimum expectation from any optimization method is that the value found for the coherent fitness be higher than its value at the true signal parameters. A failure of this condition indicates that the global maximum of the coherent fitness function was not found. It is important to emphasize here that a failure in locating the global maximum does not necessarily mean a failure in detecting a signal. This point is discussed further in Sec. IV B.

Stated formally, let \( \rho_{\text{coh}}(N_{\text{runs}}, N_{\text{iter}}) \) be the best coherent fitness value found over \( N_{\text{runs}} \) independent runs of PSO, with \( N_{\text{iter}} \) iterations per PSO run. (We will occasionally drop \( N_{\text{iter}} \) when there is no scope for confusion.) Let \( \rho_{\text{coh}}^{(0)} \) be the coherent fitness value for the true signal parameters. (Note that \( \rho_{\text{coh}}^{(0)} \) is a random variable due to noise in the data.) The metric, denoted by \( \mathcal{M}(N_{\text{runs}}, N_{\text{iter}}) \), is defined as

\[
\mathcal{M}(N_{\text{runs}}, N_{\text{iter}}) = \Pr \left( \rho_{\text{coh}}(N_{\text{runs}}, N_{\text{iter}}) \leq \rho_{\text{coh}}^{(0)} \right)
\]  

where \( \Pr \) represents probability. The goal of tuning PSO should be to reduce \( \mathcal{M}(N_{\text{runs}}, N_{\text{iter}}) \) to an acceptable level, with \( \mathcal{M}(N_{\text{runs}}, N_{\text{iter}}) = 0 \) being the most stringent requirement.

Performing multiple runs of PSO does not add to the execution time of the overall search if the runs can be implemented in parallel. Hence, \( N_{\text{runs}} \) need not be tuned carefully if one has access to a sufficient number of processors. In most situations, however, where the user of a supercomputer is billed by the number of hours and processors consumed, tuning \( N_{\text{runs}} \) can be beneficial. The tuning of \( N_{\text{runs}} \) is, of course, a definite requirement in situations where it affects the execution time of a search.

\[\text{IV. RESULTS}\]

The performance of PSO is analyzed using simulated realizations of data, following the model described in Sec II A, for the H, L, V, and K detector network.

The simulated signals are normalized to have a specified optimal network signal to noise ratio \( (\text{SNR}_{\text{opt}}) \), defined as,

\[
\text{SNR}_{\text{opt}} = \left[ \frac{1}{D} \sum_{i=1}^{D} \left( |h_i^*| h_i \right)^2 \right]^{1/2}.
\]

\( \text{SNR}_{\text{opt}} \) has the straightforward interpretation of being the ratio of the mean of the LLR under \( H_1 \) to its standard deviation under \( H_0 \) in the case of binary hypotheses, where the waveform \( h(t) \) is completely known under \( H_1 \). Although it does not numerically match the corresponding ratio for the GLRT, \( \text{SNR}_{\text{opt}} \) is still a convenient way to normalize signals because the performance of GLRT depends monotonically on it and it admits a closed form expression.

For the data realizations under \( H_1 \), we use the source locations \( L4 (\alpha = 32.09^\circ, \delta = -53.86^\circ) \) and \( L5 (\alpha = 150.11^\circ, \delta = -60.16^\circ) \) from WM that correspond to the worst and best condition numbers of the antenna pattern matrix. The signal waveforms used correspond to binaries with equal mass components, with the component mass labeled by M1 (14.5 \( M_\odot \)) and M2 (1.506 \( M_\odot \)). The signal lengths corresponding to M1 and M2 are 20.8 sec and 23 min respectively.

Data realizations containing the M1L, \( a = 4, 5, \) signal, called M1 data, have a length of 64 sec, while those with the M2L signal, called M2 data, are 30 mins long. The sampling frequency of the data in all cases is 2048 Hz. The signal start times were fixed at 10 secs and 5 mins for M1 and M2 data respectively.

The search space for PSO is fixed as follows. The range for \( \alpha \) and \( \delta \) covers the entire sky. For M1 data realizations, \( \tau_0 \in [0, 50] \) sec and \( \tau_{1.5} \in [0, 5] \) sec. For M2 data realizations, \( \tau_0 \in [500, 1000] \) sec and \( \tau_{1.5} \in [5, 10] \) sec.

The results from the simulations are organized as follows. First, we compute the PSO tuning metric \( \mathcal{M}(N_{\text{runs}}, N_{\text{iter}}) \) defined in Eq. 24 for a discrete set of \( \text{SNR}_{\text{opt}} \) values and obtain the optimum settings for \( N_{\text{runs}} \) and \( N_{\text{iter}} \) for each \( \text{SNR}_{\text{opt}} \). Next, the detection performance is quantified with these settings for each \( \text{SNR}_{\text{opt}} \).

From this, we obtain the minimum \( \text{SNR}_{\text{opt}} \) at which there is almost complete separation of the distributions of \( \rho_{\text{coh}}(N_{\text{runs}}, N_{\text{iter}}) \) under \( H_0 \) and \( H_1 \). The estimation performance of the PSO-based search is then quantified at this value of \( \text{SNR}_{\text{opt}} \) and the associated optimum settings for \( N_{\text{runs}} \) and \( N_{\text{iter}} \).

\[\text{A. PSO tuning}\]

The metric \( \mathcal{M}(N_{\text{runs}}, N_{\text{iter}}) \) is estimated using simulated data realizations. The computational burden of
this estimation can be reduced substantially, following the strategy described below, by taking into account the fact that the information needed for a given $N_{\text{runs}}$ is already nested within that for a larger $N_{\text{runs}}$.

For a given $N_{\text{iter}}$ and SNR$_{\text{opt}}$, simulate $N_{\text{trials}}$ data realizations containing the same signal in each.

- For each data realization, do $N_{\text{runs,max}}$ independent PSO runs and obtain the corresponding values of $\rho_{\text{coh}}^r(N_{\text{runs}}, N_{\text{iter}})$.
- For any $N_{\text{runs}} < N_{\text{runs,max}}$, and for each data realization, draw $N_{\text{bootstrap}}$ bootstrap [30] samples of size $N_{\text{runs}}$ from the set of $N_{\text{runs,max}}$ values.
- For each bootstrap sample, obtain the best fitness value among $N_{\text{runs}}$ runs, yielding $N_{\text{bootstrap}}$ values of $\rho_{\text{coh}}^r(N_{\text{runs}}, N_{\text{iter}})$.
- Estimate $M(N_{\text{runs}}, N_{\text{iter}})$ for each realization as the fraction of bootstrap samples for which $\rho_{\text{coh}}^r(N_{\text{runs}}, N_{\text{iter}}) \leq \rho_{\text{coh}}^0$.

Finally, from the $N_{\text{trials}}$ value of $M(N_{\text{runs}}, N_{\text{iter}})$ thus obtained, estimate suitable statistical summaries. By repeating the above process for different values of $N_{\text{iter}}$ and $N_{\text{runs}} < N_{\text{runs,max}}$, one can pick the best combination based on some preset thresholds on the statistical summaries and available computational resources for carrying out the PSO-based search.

In this paper, we tune the PSO-based search for a given SNR$_{\text{opt}}$ using $N_{\text{trials}} = 120$, $N_{\text{runs,max}} = 12$, and $N_{\text{bootstrap}} = 1000$. Table I shows statistical summaries – the 1st, 50th (median), and 99th percentiles – of the distribution of $M(N_{\text{runs}}, N_{\text{iter}})$ for a discrete set of SNR$_{\text{opt}}$ values.

For each SNR$_{\text{opt}}$, we pick the first pair of $N_{\text{runs}}$ and $N_{\text{iter}}$, at which all the three percentiles become zero, implying that the estimated $M(N_{\text{runs}}, N_{\text{iter}}) = 0$ for all $N_{\text{trials}}$ realizations. Where the choice is between $N_{\text{runs}} = 3$ and $N_{\text{runs}} = 4$, we pick the latter as it is the more conservative option. As noted earlier, picking a slightly larger $N_{\text{runs}}$ does not necessarily increase the execution time of the search since the independent PSO runs can be conducted in parallel (given the resources). Thus, the combinations ($N_{\text{runs}}, N_{\text{iter}}$) used are (4, 1500) and (4, 1000) for SNR$_{\text{opt}} = 9$ and SNR$_{\text{opt}} \in \{10, 11\}$ respectively.

The metric $M(N_{\text{runs}}, N_{\text{iter}})$ used in the tuning is estimated from a finite number of data realizations. As such, there is a non-zero probability of $M \neq 0$ even if it is estimated to be zero in the tuning. To validate the tuning process, therefore, we test the performance of the tuned PSO over a much larger number of data realizations.

Figures 1 to 3 show the validation of tuning for SNR$_{\text{opt}} = 9, 10,$ and 11 respectively. For each SNR$_{\text{opt}}$, there are 1000 realizations of M1 data for each of the two sky locations (L4 and L5). The figures show the scatterplot of the best coherent fitness value, $\rho_{\text{coh}}^r(N_{\text{runs}}, N_{\text{iter}})$, found by PSO and the coherent fitness at the true signal parameters, $\rho_{\text{coh}}^0$, where $N_{\text{runs}}$ and $N_{\text{iter}}$ are set to their tuned values.

As expected, the condition $\rho_{\text{coh}}^r \leq \rho_{\text{coh}}^0$ fails in a non-zero fraction of the data realizations. However, the observed performance is a substantial improvement over gbest PSO in WM, where this condition failed in 6.6% of the realizations at SNR$_{\text{opt}} = 12.7$ and $N_{\text{runs}} = 12$. Here, the same condition fails in 2.2%, 1.4%, and 0.3% of trials for SNR$_{\text{opt}} = 9, 10, \text{and} 11$ respectively. Interestingly, the total number of fitness evaluations ($N_{p} \times N_{\text{iter}} \times N_{\text{runs}}$) per data realization, which was found to be $2.4 \times 10^5$ for gbest PSO in WM, remains the same for best PSO despite the lower SNR$_{\text{opt}}$ of 9. The number of fitness evaluations shrinks, compared to gbest PSO, to $1.6 \times 10^5$ at the higher SNR$_{\text{opt}}$ values.

Interestingly, out of the 44, 28, and 6 points that fall below the diagonal in Fig. 1 to Fig. 3 respectively, 42, 28, and all 6 arise from data realizations associated with the L5 location. We do not understand the origin of this effect at present. The L5 location also seems to be asso-
TABLE I. The PSO tuning metric $\mathcal{M}(N_{\text{runs}}, N_{\text{iter}})$ for a discrete set of SNR$_{\text{opt}}$ values. For each $N_{\text{runs}}$ and $N_{\text{iter}}$ combination, there are three rows corresponding (from top to bottom) to SNR$_{\text{opt}}$ = 9, 10, and 11 respectively. In each row, the numbers from left to right are the 1st percentile, Median, and 99th percentile of the distribution of $\mathcal{M}(N_{\text{runs}}, N_{\text{iter}})$.

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FIG. 3. Scatterplot of the best coherent fitness value, $\rho'_\text{coh}(4,1000)$, found by PSO and the coherent fitness at the true signal parameters, $\rho^{(0)}_\text{coh}$, for SNR$_{\text{opt}}$ = 11 and M1 data. Out of a total of 2000 points, 6 (or 0.3%) fall below the diagonal. The blue lines show the detection threshold of 9.168.

FIG. 4. Scatterplot of the best coherent fitness value, $\rho'_\text{coh}(8,1500)$, found by PSO and the coherent fitness at the true signal parameters, $\rho^{(0)}_\text{coh}$, for SNR$_{\text{opt}}$ = 11 and M2 data. Out of a total of 50 points, 4 (or 8%) fall below the diagonal.

associated with a prominent secondary maximum, discussed in Sec. IV C, of the coherent fitness function. It is likely that these effects are linked.

The tuning process described above pertains to the specific length of M1 data. However, the optimum settings for a given data length can serve as useful starting points for other cases. We illustrate this with the challenging case of M2 where the data length is $\approx$ 30 times longer than that for M1. Since the current computation time for the M2 data is extremely long ($\approx$ 18 hours), carrying out a statistically reliable tuning with a sufficiently large number of data realizations is not feasible. Instead, we simply start with the optimum settings found for a given SNR$_{\text{opt}}$ in Table I and explore variations around those settings. Considering the case of SNR$_{\text{opt}}$ = 11 and starting with the tuned settings ($N_{\text{runs}} = 4$ and $N_{\text{iter}} = 1000$) for M1 data, we found that the performance of PSO was not acceptable. However, by increasing $N_{\text{iter}}$ to 1500 and $N_{\text{runs}}$ to 8 a reasonably effective performance level was achieved.

Fig. 4 shows the scatterplot of $\rho'_\text{coh}$ and $\rho^{(0)}_\text{coh}$ for data realizations containing the M2 signal with SNR$_{\text{opt}}$ = 11. There are 25 realizations of M2 data for each of the two sky locations (L4 and L5). The fraction of trials in which the condition $\rho'_\text{coh} \geq \rho^{(0)}_\text{coh}$ fails is now at 8%. As observed in the case of M1 data, these dropouts again arise from the data realizations associated with the L5 location. The fraction of failures should go down with an increase in SNR$_{\text{opt}}$ and further improvements in performance should be possible with some more exploration of $N_{\text{runs}}$ and $N_{\text{iter}}$.

B. Detection performance

Having obtained the best settings for PSO following the tuning strategy described in Sec. IV A, we can characterize the detection and estimation performance that can be expected from the PSO-based search. This is done almost exclusively for the M1 signal in this paper because our current computing resource limitations do not allow a reasonably large number of data realizations, especially
FIG. 5. Histograms of the coherent search statistic found by PSO, $\rho_{\text{coh}}(4,1500)$, for $H_0$ and $H_1$ data realizations. The latter contain the M1 signal with SNR\textsubscript{opt} = 9 at two different sky locations (L4 and L5). The p-value of a two-sample Kolmogorov-Smirnov test between the samples corresponding to L4 and L5 is 0.75.

FIG. 6. Histograms of the coherent search statistic found by PSO, $\rho_{\text{coh}}(4,1000)$, for $H_0$ and $H_1$ data realizations. The latter contain the M1 signal with SNR\textsubscript{opt} = 10 at two different sky locations (L4 and L5). The p-value of a two-sample Kolmogorov-Smirnov test between the samples corresponding to L4 and L5 is 0.46.

FIG. 7. Histograms of the coherent search statistic found by PSO, $\rho_{\text{coh}}(4,1000)$, for $H_0$ and $H_1$ data realizations. The latter contain the M1 signal with SNR\textsubscript{opt} = 11 at two different sky locations (L4 and L5). The p-value of a two-sample Kolmogorov-Smirnov test between the samples corresponding to L4 and L5 is 0.13.

under $H_0$, to be used for the M2 signal. For M1, we use the same data realizations that were used in the validation (c.f., Fig. 1 to Fig. 3) of tuned settings. The number of noise-only data realizations under $H_0$ is 1000 for each of the two $N_{\text{runs}}$ and $N_{\text{iter}}$ combinations obtained from the tuning process.

Figures 5, 6, and 7 show the distributions of the coherent search statistic found by PSO for the different data sets described above. A two-sample Kolmogorov-Smirnoff (KS) test is performed on the samples associated with the two sky locations. In all cases, the test supports the null hypothesis that the two samples are drawn from the same distribution. This shows that, as happens in the case of a grid-based search, the distribution of the coherent search statistic found by PSO depends only on SNR\textsubscript{opt} and not the details of the individual detector responses that vary with the source location.

We fit a lognormal probability density function (pdf) to the distribution of the coherent search statistic under $H_0$ and obtain the detection threshold from this fit for a given false alarm probability (FAP). For a FAP = $2.03 \times 10^{-6}$, which corresponds to a false alarm rate (FAR) of 1 event/year, the detection thresholds for the two different PSO settings, ($N_{\text{runs}} = 4, N_{\text{iter}} = 1500$) and ($N_{\text{runs}} = 4, N_{\text{iter}} = 1000$), differ only marginally at 9.109 and 9.168 respectively. Table II lists the detection probabilities at these thresholds for different SNR\textsubscript{opt} values. We see that the sensitivity of a PSO-based fully-coherent all-sky search reaches an interesting level at around SNR\textsubscript{opt} ≈ 9.

As discussed in Sec. IV A, PSO has a finite probability of not converging to the global maximum of the coherent fitness function. This is shown by the points that fall below the diagonal in Fig. 1 to Fig. 4. However, failure to converge to the global maximum does not necessarily mean failure to detect a signal since the coherent search statistic, $\rho_{\text{coh}}$, obtained from PSO may still exceed the detection threshold. Detection probability is only reduced when $\rho_{\text{coh}}$ falls both below the diagonal and below the detection threshold.

We define the loss in detection probability as

$$L_{DP} = P(\rho_{\text{coh}} \leq \eta | \rho_{\text{coh}}^{(0)} \geq \eta ) ,$$

where $P(A|B)$ denotes the conditional probability of event $A$ given event $B$, and $\eta$ is the detection threshold. As seen from Table II, the estimated $L_{DP}$ is negligible in all cases for the M1 signal at a FAR of 1 false event per year.

As mentioned earlier, we do not have a sufficiently large number of trials under $H_0$ for M2 data to reliably esti-
mate the detection threshold for a realistically small FAP. Instead, we simply pick an ad hoc range of \(9.0 \leq \eta \leq 11.0\) for the detection threshold in this case and find that \(L_{DP}\) varies between 2% and 6%.

C. Estimation performance

Most analyses [31, 32] of parameter estimation for the fully-coherent all-sky CBC search report Bayesian credible regions. A credible region \(\text{CR}_\alpha\) is the smallest volume in signal parameter space that encloses a fraction \(\alpha\) of the total posterior probability. As such, \(\text{CR}_\alpha\) is derived from a single data realization. It should be emphasized that \(\text{CR}_\alpha\) is in general not equivalent to a Frequentist confidence region in that it is not guaranteed to cover the true parameter values with a probability of \(\alpha\) over multiple data realizations. The reduced computational cost of the PSO-based search makes it feasible to obtain Frequentist errors for point parameter estimates using multiple data realizations.

In this paper, we do a limited examination of parameter estimation errors by focusing on only the M1 signal at \(\text{SNR}_{\text{opt}} = 11\) for which its detection probability is nearly unity. A more thorough examination of this topic will be the subject of future work.

Fig. 8 shows the estimated locations on the sky for both L4 and L5. As was observed in WM for the case of initial LIGO PSD, the error in sky location generally follows its dependence on the condition number of the antenna pattern matrix: the estimated locations are distributed over a much more extended region when the source location has a higher condition number.

A caveat to the empirical rule of thumb above is that the L5 location, while exhibiting a more compact distribution of the estimates, also shows a widely separated secondary maximum. Going by the condition \(\rho'_{\text{coh}} \geq \rho^{(0)}_{\text{coh}}\) as an indicator of convergence to the global maximum, we find that the global maximum shifted to the secondary in 4.3% of the trials where this condition was met. At the same time, all but one of the trials where this condition failed also appear at the secondary maximum. Thus, PSO does not go to an arbitrary location but latches on to the secondary when it fails to locate the global maximum. These observations indicate that the secondary maximum is a genuine feature of the coherent fitness function when a source is located at L5 and not an artifact of using PSO.

Fig. 9 shows the estimation error distribution for chirp times \(\tau_0\) and \(\tau_{1.5}\). The main observation here is that these errors are essentially uncorrelated with the errors in sky localization. This is expected from a Fisher information analysis but, as was pointed out in WM, this need not be true for some sky locations.

V. COMPUTATION TIME ANALYSIS

As demonstrated by the rich science payoffs from the joint GW and EM observations of GW170817, the detection of EM counterparts of CBC events is of critical importance. A key factor here is the time elapsed in the dissemination of a follow up alert to EM astronomers.

While the time needed to generate an alert depends on a number of factors, including manual vetting of detector state and data quality, the execution time of the GW search algorithm is the primary determinant. With this in mind, it is important to analyze the computation time of a PSO-based fully coherent search.

The results in this paper are obtained using a code that is implemented in the C programming language. There are two nested layers of parallelization in the code. In the outer layer, parallelization is performed over the in-
The outer parallelization does not involve any communication between the parallel processes. It is implemented using a framework for high throughput computing called LAUNCHER [33] that allows running large collections of independent applications on batch-scheduled clusters. The inner parallelization is implemented as a multi-threaded application based on OpenMP [34, 35], which assigns the fitness calculation for each particle to a unique thread that acts as an effectively independent processing unit.

On the cluster used for obtaining the results in this paper (TACC Lonestar 5 [36]), each independent PSO run is assigned to a separate node, with each node providing up to 48 independent threads (24 processing cores with 2 hardware threads per core). On a given node we assign one thread to each particle, which allows for a parallel calculation of the $N_p$ particle fitness values computed in each iteration of PSO.

Our current parallelization strategy results in the time taken by the whole code running across all the nodes and threads of the cluster being essentially equivalent to the wall-clock computation time. $T_{\text{comp}}$, for one thread. Fig. 10 shows $T_{\text{comp}}$ as a function of the duration, $T_{\text{data}}$, of the data segment analyzed.

We obtain the $T_{\text{comp}}$ values shown by averaging over 4 PSO runs with $N_{\text{iter}} = 1000$ in each run. A linear fit to the data shows that $T_{\text{comp}}$ increases at the rate of 37.2 min per min of data.

In the current implementation, all operations involved in a single fitness evaluation are serialized. However, the principal steps in a single fitness evaluation are themselves highly parallelizable. Each fitness evaluation involves (i) generating the $h_{+x}$ waveforms, and (ii) computing the inner product in Eq. 11.

Generating the $h_{+x}$ waveforms involves independent calculations of the stationary phase approximant of the 2PN waveform [24] at each of the Fourier frequencies in the data. In addition, the inner product in Eq. 11 involves computing the integrand at each Fourier frequency independently.

Thus, an alternative parallelization scheme in a single PSO run is to invert the current scheme by evaluating the fitness values of the $N_p$ particles serially and parallelizing over the array operations involved in each fitness evaluation. If the computation time for a single fitness evaluation is $T_{\text{fit}}$, the current $T_{\text{comp}}$ is approximately $N_{\text{iter}}T_{\text{fit}}$. With the alternative scheme $T_{\text{comp}} \approx N_pN_{\text{iter}}(T_{\text{fit}}/N_{\text{threads}})$, where $N_{\text{threads}}$ is the number of threads used in parallelizing the fitness function evaluation. Thus, $N_{\text{threads}}$ must be substantially greater than $N_p$ in order to make the switch to the alternative scheme beneficial.

With high performance computing moving increasingly towards massive hardware-level parallelism, such as the INTEL XEON PHI KNIGHTS LANDING (KNL) processor with 272 threads or Graphics Processing Units (GPUs) such as the Nvidia V100 with 5120 threads, we are already in the regime where $N_{\text{threads}} \gg N_p$. Thus, the alternative scheme described above could lead to a substantially faster implementation of the fully-coherent all-sky search.

At present, the only objective metric for comparison of computational costs between the PSO-based search and the fully-coherent all-sky search pipeline, LALINFERENCE [32], used for the analysis of LIGO-Virgo data is the total number of fitness (i.e., likelihood) evaluations. The number of fitness evaluations reported in [32] range between $10^9$ and $10^8$ for the Markov Chain Monte Carlo (MCMC) algorithm using a network of first generation detectors and a data segment length of 32 sec. The PSO-based search for second generation detectors continues to maintain the same number of fitness evaluations as found in WM for a first generation network, ranging from a maximum of $2.4 \times 10^5$ to $4.8 \times 10^5$ for the 64 sec and 30 min long data segments respectively. The number of fitness evaluations per independent run of PSO is a factor of 4 and 8 smaller for the respective data lengths.

While the PSO-based search incurs a drastically smaller number of fitness evaluations to compute the coherent search statistic and point estimate of the signal parameters, it should be emphasized that MCMC also provides information about the shape of the posterior probability density function. It may be possible to use the PSO-based search results as a seed to focus the MCMC sampling to a smaller region of parameter space and reduce the computational cost of the latter.

It is also worth noting here that, compared to an MCMC search, the PSO-based search involves very few tunable parameters, namely, only $N_{\text{runs}}$ and $N_{\text{iter}}$. 

![Figure 10](image-url)
VI. CONCLUSION

A fully-coherent all-sky search for CBC signals is implemented that uses PSO as the global optimizer of the joint likelihood function of data from a network of second generation detectors. The results presented here show that PSO allows a significant reduction in the computational cost of this search with negligible loss in sensitivity.

At a FAR of 1 event/year, the PSO-based search achieves a detection probability of \( \approx 0.7 \) at \( \text{SNR}_{\text{opt}} = 9.0 \) for a 20.8 sec long signal, corresponding to an equal mass binary with 14.5 \( M_\odot \) components. For the same signal, the detection probability is \( \approx 0.99 \) at \( \text{SNR}_{\text{opt}} = 11 \). These results demonstrate that the reduced computational cost is achieved without any significant loss of sensitivity in an astrophysically relevant range of signal strength and binary masses.

Low mass binaries \((O(1.4) \ M_\odot \text{ components})\) pose an extreme challenge to fully-coherent all-sky searches with second generation detectors because the signal length becomes \( O(30) \) min. We tested the PSO-based search on a 23 min signal, corresponding to an equal mass binary with 1.506 \( M_\odot \), embedded in 30 min long data segments. We find that the PSO-based search continues to perform well with \( \leq 6\% \) loss in detection probability at \( \text{SNR}_{\text{opt}} = 11 \) for a realistic detection threshold of \( \approx 10 \) on the coherent search statistic. Going beyond Fisher information analyses and Bayesian credible regions obtained with single data realizations, the reduced computational cost afforded by PSO allows Frequentist parameter estimation errors using multiple data realizations to be obtained. A limited study in this paper shows several interesting issues such as (i) variations in localization errors caused by the condition number of the network antenna pattern matrix, (ii) non-Gaussianity in the sky localization estimation error, and (iii) degenerate locations on the sky. A more extensive and realistic parameter estimation study using the PSO-based search will be carried out in the future.

The prospects for further reductions in the computation time of the PSO-based search are very promising. As discussed in the paper, existing and upcoming hardware-level support for massive parallelism could make an alternative parallelization scheme significantly faster than the current one. Incorporating faster waveform generation schemes, such as the one proposed in [37], could reduce the computation time even further. It may even be possible to squeeze out a factor of few from the current code with more efficient implementations of the mathematical formalism. We are currently exploring these possibilities and hope to further push the fully-coherent all-sky search towards real time processing of data.

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