Imprints of gravitational lensing in the Planck cosmic microwave background data at the location of WISE×SCOS galaxies

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Imprints of gravitational lensing in the Planck CMB data at the location of WISExSCOS galaxies

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We detect weak gravitational lensing of the cosmic microwave background (CMB) at the location of the WISE x SuperCOSMOS (WISE x SCOS) galaxies using the publicly available Planck lensing convergence map. By stacking the lensing convergence map at the position of 12.4 million galaxies in the redshift range \(0.1 \leq z \leq 0.345\), we find the average mass of the galaxies to be \(M_{200\text{crit}} = 6.25 \pm 0.6 \times 10^{12} \, M_\odot\). The null hypothesis of no-lensing is rejected at a significance of 17\(\sigma\). We split the galaxy sample into three redshift slices each containing \(\approx 4.1\) million objects and obtain lensing masses in each slice of \(4.18 \pm 0.8, 6.93 \pm 0.9, \) and \(18.84 \pm 1.2 \times 10^{12} \, M_\odot\). Our results suggest a redshift evolution of the galaxy sample masses but this apparent increase might be due to the preferential selection of intrinsically luminous sources at high redshifts. The recovered mass of the stacked sample is reduced by 28\% when we remove the galaxies in the vicinity of galaxy clusters with mass \(M_{200\text{crit}} = 2 \times 10^{14} \, M_\odot\). We forecast that upcoming CMB surveys can achieve 5\% galaxy mass constraints over sets of 12.4 million galaxies with \(M_{200\text{crit}} = 1 \times 10^{12} \, M_\odot\) at \(z = 1\).

I. INTRODUCTION

The path of cosmic microwave background (CMB) photons is perturbed by intervening dark matter haloes and associated structures between the observer and the last scattering surface. The magnitude of the deflection \(\vec{\alpha}(i)\) is directly proportional to the gradient of the underlying lensing potential \(\phi\) and provides an accurate mapping of the total matter distribution in the Universe. Several previous studies have detected lensing of the CMB due to the large-scale structure (LSS) both in CMB temperature and polarization maps [1][5] and references therein] and by cross-correlating the CMB lensing maps against biased tracers of the matter field such as galaxies [6][11]. The lensing on arcminute scales due to massive dark matter haloes has also been detected by stacking techniques [12][16]. This small-scale CMB-halo lensing is especially interesting as it allows us to accurately measure the masses of the astrophysical objects [17][25]. The method is more powerful than galaxy lensing at high redshifts where the observed source galaxy counts drop significantly, degrading the lensing signal-to-noise (S/N). At low redshifts, it is complementary to galaxy lensing allowing systematic checks. The current mass estimates using CMB-halo lensing are uncertain at \(\geq 20\%\) level [16], with the error budget being dominated by statistical uncertainties. However, the field is rapidly evolving with improved CMB maps expected from the upcoming CMB surveys [26][28]. An accurate mass measurement of the largest dark matter haloes (\(M_{200\text{crit}} \gtrsim 10^{13.5} \, M_\odot\)) is important for cosmology as these haloes are signposts of the highest density peaks in the Universe and their abundance as a function of mass and redshift is a sensitive probe of structure growth in the Universe [30]. Obtaining accurate masses of intermediate and lower mass haloes is also important to understand the effects of baryon physics on the formation and evolution of galaxies [29]. For example, determining the stellar-to-halo (\(M_* - M_h\)) mass relation and its redshift evolution can give detailed insights on the history of star formation [31] and references therein. Although CMB-halo lensing signal is faint for a single object (S/N < 0.1 for \(M_{200\text{crit}} = 1 \times 10^{12} \, M_\odot\) at CMB-S4 noise levels), the method offers excellent prospects in determining \(M_* - M_h\) relation out to very high redshifts for the upcoming LSS surveys expected to detect billions of galaxies.

In this work, we extract the halo lensing signal using the Planck data and the all-sky WISE \(\times\) SuperCOSMOS (WISE \(\times\) SCOS hereafter) galaxy catalogue [33]. Specifically, we stack the Planck convergence \(\kappa\) map at the positions of 12.4 million (M) WISE \(\times\) SCOS galaxies. The convergence map quantifies the amount of magnification/demagnification of the source, CMB anisotropies in this case, at a given location and is related to the underlying lensing potential \(\phi\) as \(\kappa = -\frac{1}{2} \nabla^2 \phi\). We also perform a tomographic stacking analysis by splitting the WISE \(\times\) SCOS sample in three redshift bins. Throughout this work, we use the \(\Lambda\)CDM cosmology obtained from the chain that combines Planck 2015 data with external datasets TT, TE, EE+lowP+lensing+ext [34]. We define all the halo quantities with respect to the radius \(R_{200}\) defined as the region within which the average mass density is 200 times the critical density of the universe at the halo redshift.

II. DATASETS

In this work, we use the the publicly available [4] 2015 Planck lensing convergence map [3] and the WISE \(\times\) SCOS [33] galaxy catalogue. The galaxy catalogue [33] contains 20.5M objects and was constructed by cross-matching two of the largest all-sky galaxy samples, the mid-IR AllWISE [35] and the optical SuperCOSMOS [36]. Both the Planck lensing map and the WISE \(\times\) SCOS catalogue were accompanied by masks intended to remove contaminated regions, like the regions of high-galactic emission. We create a combined mask from Planck and WISE \(\times\) SCOS masks, shown as the light-shaded grey region in Fig. [1]. The galaxy sample after employing this
mask has photometric redshifts (photo-zs) distributed between 0 \lesssim z \lesssim 0.4 (\tilde{z} = 0.2) with a normalized scatter \sigma_z = 0.033. From this sample, we remove objects outside the redshift range 0.1 \leq z \leq 0.345 as the stellar contamination outside this range is greater than 20% in WISE \times SCOS catalogue [33]. Our final sample contains 12.4M objects with \fsky = 0.65.

### III. METHODS

The aim of this work is to measure the average mass of the dark matter haloes that host the WISE \times SCOS galaxies in a tomosgraphic approach by stacking the Planck CMB convergence map. To achieve this, we extract 60′×60′ cutouts from the Planck \kappa map at the location of each WISE \times SCOS galaxy by projecting the full-sky map to a tangential flat-sky projection at 1° resolution using healpy.gnomview command. Note that the estimate of the background CMB gradient with a quadratic estimator is underestimated at the location of a dark matter halo due to the additional lensing caused by the halo. This results in a small bias in the reconstructed lensing signal [22][23] and can be mitigated by estimating the gradient at scales larger than L \lesssim 2000 [23]. Ignoring this low-pass filter, as is the case here when using Planck lensing convergence maps, is not an optimal method of extracting the CMB-halo lensing signal. However, this causes negligible effect to the analysis presented here because of the high noise levels in the Planck maps. For the tomosraphic slicing, we split the sample into three redshift bins

\[ \Delta z \gtrsim 0.04. \]

average the respective number of cutouts in each bin to obtain the final cutout. To validate the analysis we also stack the masked \kappa map at a number of random sky locations equal to that of our galaxy sample. These stacked cutouts are shown in the left panel of Fig. 2.

We model the halo density profiles using Navarro-Frenk-White (NFW) dark matter (DM) profile [33] and obtain \kappa_{\text{NFW}} using Eq. (2.8) of Bartelmann [40]. We also include the lensing due to correlated structures along the line-of-sight (2-halo term) [41][42] using Eq. (13) of Oguri & Takashi [43]. We adopt the Tinker et al. [44] formalism to calculate the bias \bfr(M, z) for a halo with mass \Mhalo. Thus, our model for the total lensing convergence is \kappa_{\text{halo}} = \kappa^1 + \kappa^2. Finally, we filter out modes \L > 2048 in \kappa_{\text{halo}} to match the filtering adopted in the Planck lensing map.

We determine the average best-fit galaxy halo mass \Mhalo of the stacked sample in each redshift bin by maximizing the likelihood

\[ -2 \ln L = \sum_{\theta, \theta'} \left[ \hat{\kappa}(\theta) - \kappa_{\text{fit}}(\theta) \right] C^{-1}_{\theta, \theta'} \left[ \hat{\kappa}(\theta') - \kappa_{\text{fit}}(\theta') \right]. \tag{1} \]

Here \hat{\kappa}(\theta) and \kappa_{\text{fit}}(\theta) are the concatenated radially binned profiles of the data and model in the three redshift bins up to 10′ with \Delta \theta = 2′.5. The results are stable to our choice of fitting radius and change only marginally when we increase the radius to 12.5′. We use the median redshift \zbar of the galaxies in each bin \i when determining \kappa_{\text{fit}} for different halo masses. We use the Duffy et al. [43] mass-concentration relation to calculate the concentration parameter \cbar(M, \zbar) for the NFW haloes. The covariance matrix \hat{C}_{12\times12} is calculated using jackknife resampling by dividing the survey region into \N = 1000 samples using

\[ \hat{C}_{\theta, \theta'} = \frac{N - 1}{\N} \sum_{j=1}^{\N} \left[ \hat{\kappa}_j(\theta) - \langle \hat{\kappa}(\theta) \rangle \right] \left[ \hat{\kappa}_j(\theta') - \langle \hat{\kappa}(\theta') \rangle \right], \tag{2} \]

where \hat{\kappa}_j(\theta) is the concatenated data vector from the three redshift bins for the \jth jackknife sample. We have examined how the eigenmodes of this covariance matrix change when varying the number of jackknife splits, and find the eigenmodes are stable beyond 300 splits. It is important to consider the correlations between redshift bins since a given location on sky can be lensed by galaxies in more than one redshift bin. We also perform the fitting in the three redshift bins without including the correlation between different bins. The covariance matrix \hat{C}_{4\times4} in this case is also obtained using jackknife resampling. The average mass of the full sample was then determined by combining the likelihoods of the individual redshift bins. We calculate the 1σ mass uncertainty \Merr as the point when \Delta \chi^2 = -2 \ln L(M_{\text{fit}}) + 2 \ln L(M_{100\text{err}}) becomes unity. The significance of obtaining the estimated lensing mass \M_{\text{fit}} with respect to no-lensing \M_{\text{fit}} = 0 is defined as

\[ \sqrt{2 \ln L(M_{100\text{err}} = M_{\text{fit}}) - 2 \ln L(M_{100\text{err}} = 0)}. \]
FIG. 2. *Left panels:* Stacked Planck convergence maps at the location of WISE × SCOS galaxies in the three redshift slices and in the full sample (upper four boxes), as well as at a number of random positions equal to that of the full galaxy sample (a null test). The dashed and solid contours correspond to regions above 3 and 5σ respectively. The colour scale has been restricted to the range \([-0.002, 0.0035]\) for all panels. *Right panels:* Panels 1-6 show the lensing masses obtained in the three redshift bins when correlations between different bins are included in the fitting. The contours in the off-diagonal panels show the 1σ, 2σ constraints. The orange-solid and black-dash-dotted curves correspond to constraints obtained with and without the inclusion of the 2-halo term. The orange-dashed curves on the diagonal panels are the lensing mass for the three bins when the bin-bin correlations are ignored during fitting. The lensing mass of the full sample along with the null test (purple-dotted) is shown in panel 7.

**IV. RESULTS**

The reconstructed galaxy lensing masses for the three redshift bins are shown in the right panels of Fig. 2. The diagonal panels show the marginalized likelihoods and the off-diagonal contours represent the 1σ, 2σ mass constraints. The orange-solid and the black dash-dotted curves correspond to the fitting performed with and without the 2-halo term. For reference, the lensing masses obtained without including the correlations between the redshift bins are shown as orange-dashed curves. The lensing masses for the full sample along with the null test (purple-dotted) are shown in the panel 7. The no-lensing hypothesis of \(M_{\text{fit}} = 0\) is rejected at 17σ for the full sample. The best-fit lensing masses are tabulated in Table I. Since structures correlated with the individual haloes add to the lensing signal, the inferred masses decrease slightly as expected when including the 2-halo term. The lensing mass of the full sample is \(6.25 \times 10^{12} \, M_\odot\) with (without) the 2-halo term included. Given that the inclusion of the 2-halo term has a significant effect on the fitting, we estimate the signal-to-noise due to \(\kappa_{1h}\) alone by removing the \(\kappa_{2h}\) corresponding to the best-fit mass of \(6.25 \times 10^{12} \, M_\odot\) at the median redshift \(\bar{z} = 0.21\). The detection significance of the resultant signal due to \(\kappa_{1h}\) alone is 10.7σ. This S/N can be compared with other similar works in the literature namely Madhavacheril et al. [12], Baxter et al. [13], Planck Collaboration XXIV [14], Geach &
We find that the reconstructed halo lensing masses increase with redshift. This increase could be due to an evolution of the galaxy properties in the WISE × SCOS sample. Alternatively, the effect can also be explained due to preferential selection of intrinsically luminous sources at high redshifts given that the WISE × SCOS is a flux-limited catalogue. Note that the luminous galaxies are generally expected to reside in massive DM haloes [42]. A thorough investigation of this mass disagreement is left for the future work.

### A. Validation of results

We test the robustness of our results against three effects that could impact our lensing mass measurement: (a) selecting galaxies in dense environments, (b) uncorrelated higher redshift clusters, and (c) redshift binning and uncertainties.

#### 1. Enhanced lensing signal due to dense environments

Given that some of the galaxies reside in galaxy clusters, which at \( M_{200} \gtrsim 10^{14} M_\odot \) can be two or more orders of magnitude more massive than a galaxy, one might worry about what fraction of the stacked lensing signal is due to the host galaxy clusters instead of the galaxy sample. We quantify the magnitude of this effect by comparing the recovered masses for all galaxies to the masses when galaxies near clusters are excluded. To this end, we use the RM cluster catalog from the SDSS-DR8 (dark-blue region in Fig. [1]) dataset [50]. The SDSS-RM catalogue contains 14,750 clusters in our region and redshift range of interest (Planck lensing and WISE × SCOS masks; \( 0.1 \leq z \leq 0.345 \)). We create RM cluster masks for our three redshift bins. The RM cluster masks remove 1–3% galaxies in each bin that are within 7′ of a RM cluster. We stack the convergence before (after) incorporating the RM cluster mask. We find that masking galaxies near galaxy clusters (\( M_{200} \gtrsim 2 \times 10^{14} M_\odot \)) reduces the estimated lensing mass by 30%, 12%, 33% in the three bins and by \( \sim 28\% \) for the full sample. Since the RM catalog does not contain all the clusters in the Universe, a proper way of estimating the environmental effect is to split the WISE × SCOS catalog into central and satellite galaxies and use a detailed halo occupation distribution (HOD) model to populate the galaxies inside the dark matter haloes [51].

#### 2. Residual foregrounds in Planck SMICA maps

The Planck lensing map was reconstructed using the foreground cleaned SMICA [46] temperature and polarization maps which contain residual Sunyaev-Zel’dovich signals [47] (both thermal tSZ and kinetic kSZ) and contamination from the cosmic infrared background (CIB) arising primarily due to high-redshift (\( z \gtrsim 1 \)) infrared galaxies [48, 49] that can bias the lensing analysis. In this work, however, we work with low-redshift galaxies (\( z \leq 0.345; \bar{z} = 0.2 \)) from WISE × SCOS catalogue which contribute only a small fraction of the CIB emission [52, 53]. Thus we ignore CIB effects in this analysis.

The SZ effect from the WISE × SCOS galaxies is expected to be small. However, given that a small fraction of our galaxy sample is close to SDSS RM clusters, we quantify the bias due of SZ signals from RM clusters using the high-resolutions simulations of Sehgal et al. [54]. We start by simulating LSS lensed CMB of the SDSS footprint using the Planck 2015 power spectra described earlier. The simulation was then performed at the location of 4.5 million WISE × SCOS galaxies in the SDSS footprint using an halo of mass \( M_{200} \gtrsim 8 \times 10^{12} M_\odot \) at redshift \( z = 0.3 \) assuming an NFW profile. We smooth the simulated map using a Gaussian beam of \( \theta_{FWHM} = 5′ \) and then add instrumental white noise \( \Delta T = 45 \mu K \) corresponding to the Planck SMICA map. The simulated map was then passed through a QE pipeline to reconstruct the lensing convergence map and filtered similar to the data by setting the modes \( L < 8 \) and \( L > 2048 \) to zero. We refer the reader to Raghunathan et al. [55] for more details about simulation and the lensing pipeline. We stack the lensing convergence at the location of WISE × SCOS galaxies and model them using NFW profile as described in [51]. For this fiducial case, we find a lensing mass of \( 7.1 \pm 1.9 \times 10^{12} M_\odot \) which is less than 0.5σ away from the true halo mass.

Then, for the same simulated sky above, we add residual SZ emissions from the SDSS RM clusters before performing the halo lensing. To this end, we pick the tSZ and kSZ signals from Sehgal et al. [54] simulations corresponding to RM clusters that survived the masks described in [51]. We conservatively assume 100% residual tSZ signal in the Planck SMICA temperature map. We pass them through the lensing pipeline before and after stack the reconstructed convergence map at the location of 4.5 million WISE × SCOS galaxies. In this case, we recover a lensing mass of \( 6.4 \pm 1.8 \times 10^{12} M_\odot \) which is \( < 0.4 \sigma \) from the fiducial case (\( 7.1 \pm 1.9 \times 10^{12} M_\odot \)) without the SZ emission. Given that the shift due to SZ signals from the massive RM clusters is negligible, we ignore the SZ effect from WISE × SCOS galaxies which are expected to be two orders of magnitude smaller. While the effect due to SZ sig-

### TABLE I. Inferred lensing masses for the WISE × SCOS galaxy sample considering the correlations between different bins.

<table>
<thead>
<tr>
<th>Bin</th>
<th>Lensing mass ( M_{200} ) [10^{12} M_\odot]</th>
</tr>
</thead>
<tbody>
<tr>
<td>No 2-halo term</td>
<td>With 2-halo term</td>
</tr>
<tr>
<td>( 0.100 \leq z &lt; 0.178 )</td>
<td>6.45 ± 0.8</td>
</tr>
<tr>
<td>( 0.178 \leq z &lt; 0.246 )</td>
<td>11.88 ± 0.9</td>
</tr>
<tr>
<td>( 0.246 \leq z &lt; 0.345 )</td>
<td>28.55 ± 1.2</td>
</tr>
<tr>
<td>Full sample</td>
<td>10.80 ± 0.6</td>
</tr>
</tbody>
</table>

Peacock [15], Baxter et al. [16]. Our results agree well with the expectations from simulations. We obtain 14.4σ detection significance and \( \sigma(M_{200}) = 0.9 \times 10^{12} M_\odot \) for a sample containing 12.4M galaxies with \( M_{200} = 8 \times 10^{12} M_\odot \) at \( z = 0.2 \). For the null stack, the lensing mass is consistent with zero - corresponding to a no lensing probability-to-exceed (PTE) value of 0.46.
We also check the increased variance due to presence of higher redshift objects uncorrelated with the galaxy sample. We estimate the change in variance by randomly inserting galaxy clusters in a 25 deg$^2$ box behind a galaxy of mass $M_{200,c} = 8.0 \times 10^{13} M_\odot$. For the Tinker et al. [44] halo mass function (HMF), we find that there should be $\sim$1000 clusters above $z = 0.4$ and $M_{200,c} \gsim 7.5 \times 10^{13} M_\odot$ in 25 deg$^2$. For simplicity, while we draw the cluster masses from the Tinker et al. [44] HMF, we assume a spatial Poissonian distribution and fixed redshift of $z = 0.7$ for these clusters to add their convergence signal to the simulations. The results show a slight increase in $\sigma(M_{200,c})$ from 18% to 25% with only $\leq 3\%$ shift in the inferred mass implying no bias as expected.

4. Imperfect redshifts

We make the simplifying assumption while fitting that all galaxies are at the median redshift of a bin, i.e. $z_{\text{eff}} = \bar{z} = 0.142, 0.212, $ and 0.278. This ignores the finite width of the real galaxy redshift distribution, and any systematic offset in the estimated redshifts. We test the redshift sensitivity of the results by shifting $z_{\text{eff}}$ up and down to either lower or upper edge of each redshift bin. We expect the inferred masses to shift systematically towards higher (lower) masses when the $z_{\text{eff}}$ decreases (increases) as the 2-halo term will correspondingly be under (over) estimated. However, we find the systematic shifts in mass due to redshift are small compared to the mass uncertainties, and not readily apparent in the results. We obtain 4.13 (3.98), 7.13 (6.62), and 18.84 (18.44) for the three redshift bins and 6.1 (5.9) $\times 10^{12} M_\odot$ for the full sample for $z_{\text{low}}$ ($z_{\text{high}}$) case. The differences in the mass estimates for this fairly extreme change in redshift are less than 7%, well within the error bars.

B. Future forecasts

Finally, we forecast the mass constraints that can be achieved with temperature data from future CMB surveys like Simons Observatory (SO) and CMB-S4 [28] that will become operational in the next decade. For this, we simulate CMB-S4 and SO like lensing convergence cutouts assuming an experimental beam of $\theta_{\text{FWHM}} = 2\arcmin$. Then we generate lensing reconstruction noise spectra $N_L^x$ for modes up to $L = 5000$ assuming temperature map noise levels of $\Delta T = 1$ and 2.5 $\mu K'$ respectively. We use $N_L^x$ to add noise to the simulations. Considering that the Large Synoptic Survey Telescope is expected to return a galaxy catalogue containing $O(\geq 10^8)$ sources, enabling a fine splitting based on redshift and galaxy properties, we consider a representative subset at redshift $z = 1.0$ comprising 12.4M galaxies of mass $M_{200,c} = 1 \times 10^{12} M_\odot$. We find that CMB-S4 (SO) can detect the lensing signal at $93\sigma$ ($82\sigma$) with uncertainty 5.2% (6.0%) in the inferred mass.

V. CONCLUSIONS

In this Letter, we stack the Planck CMB lensing convergence map around the 12.4M WISE $\times$ SCOS galaxies in the redshift range between $0.1 \leq z \leq 0.345$ and detect a signal at a significance of $17\sigma$. We find a best-fit mass of $6.25 \pm 0.6 \times 10^{12} M_\odot$ by modelling the lensing signal using NFW profile. We perform a null test by stacking the convergence map at random locations and infer a best-fit lensing mass consistent with zero. Using SDSS-RM clusters, we find that the presence of galaxy clusters in our cutouts can increase the lensing mass by 39%. The uncorrelated higher redshift clusters, as expected, do not bias our results but only increases the mass uncertainty to 25% from 18%. The errors introduced due to the use of median redshifts for the stacked sample and the residual foregrounds in the Planck SMICA maps are less than the statistical uncertainties of the measurements.

Although at an early stage of development, CMB-halo lensing represents a promising tool for measuring the total mass of astrophysical objects. We forecast that the future CMB stage-4 surveys can achieve 5-6% mass constraints for high-$z$ galaxies. By piercing the high redshift Universe over large volumes, CMB lensing enables a thorough investigation of the luminous-DM connection in a way complementary to, for example, galaxy weak lensing. This connection is a crucial element not only for a clear understanding of the physics of galaxy formation and evolution, but also for carrying out robust cosmological analyses.

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