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# IC at IC: IceCube can constrain the intrinsic charm of the proton

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The discovery of extraterrestrial neutrinos in the  $\sim 30$  TeV – PeV energy range by IceCube provides new constraints on high energy astrophysics. An important background to the signal are the prompt neutrinos which originate from the decay of charm hadrons produced by high energy cosmic-ray particles interacting in the Earth’s atmosphere. It is conventional to use the calculations of charm hadroproduction using gluon splitting  $g \rightarrow c\bar{c}$  alone. However, QCD predicts an additional “intrinsic” component of the heavy quark distribution which arises from diagrams where heavy quarks are multiply connected to the proton’s valence quarks. We estimate the prompt neutrino spectrum due to intrinsic charm. We find that the atmospheric prompt neutrino flux from intrinsic charm is comparable to those calculated using QCD computations not including intrinsic charm, once we normalize the intrinsic charm differential cross sections to the ISR and the LEBC-MPS collaboration data. In future, IceCube will constrain the intrinsic charm content of the proton and will contribute to one of the major questions in high energy physics phenomenology.

**I Introduction:** Astrophysical neutrinos ( $\equiv \nu + \bar{\nu}$ ) discovered by IceCube provide new insights on profound astrophysics and particle physics questions [1–7]. Many astrophysical models have been proposed to explain these events [8–33] and to constrain various processes [34–55]. These have spurred development of new signatures such as the through-going tracks caused by  $\tau$  leptons [25] and the echo technique [56].

IceCube has detected an excess of neutrinos over the atmospheric neutrino background; however: how well do we know the background? The contribution of conventional atmospheric neutrinos, produced from the decays of  $\pi$ ’s and  $K$ ’s, is known to  $\sim 20\% - 30\%$  precision depending on the energy [57–59]. The major background uncertainty comes from  $pp \rightarrow cX$ , which results in prompt neutrinos produced from the decay of charm hadrons [60–85]. The flavor ratio of prompt neutrinos is  $\nu_e : \nu_\mu : \nu_\tau \approx 1 : 1 : 0.1$ , and  $\nu : \bar{\nu} = 1 : 1$ .

Most calculations of the prompt neutrino spectrum from charm hadroproduction are based within perturbative QCD (pQCD) gluon splitting  $g \rightarrow c\bar{c}$  alone [62–70, 72–80, 84–86]. Inclusion of nonperturbative effects, for e.g., intrinsic charm [87–90], have received much less consideration [60, 61]. Recently attention has been drawn to forward production of charm hadrons by Refs. [82, 83]. Intrinsic charm is a rigorous prediction of QCD (see Supplementary Materials) and it is important to estimate its effect on atmospheric prompt neutrinos.

The important distinction between intrinsic charm and gluon splitting is that intrinsic charm uses the incoming proton energy much more efficiently due to its harder  $d\sigma/dx_F$  distribution. Inclusion of nonperturbative effects are important since the amount of intrinsic charm is an important uncertainty in QCD simulations. Due to its inherent non-perturbative nature, it has not yet been calculated from first principles, and thus its normalization must be inferred from experiment. Experiments have

not yet decisively measured the normalization of intrinsic charm in the proton, which typically dominates the differential cross section at high  $x_F$ .

Various experimental techniques have been suggested for measuring atmospheric prompt neutrinos [91–94]. These studies illustrate how measurements can constrain the underlying QCD mechanism in regions of the parameter space where it is difficult to obtain constraints from colliders [79].

IceCube compares the prompt neutrino spectrum derived by Enberg, Reno and Sarcevic (with modifications by Gaisser) (ERS w/G) [68, 69, 81] with their data. The present upper limits on the prompt neutrinos are near the nominal predictions [6, 7, 95]. An additional contribution to the prompt neutrino spectrum can change the interpretation of the astrophysical neutrinos.

In this paper, we calculate the prompt neutrino contribution from intrinsic charm after normalizing the differential cross section to the ISR and the LEBC-MPS collaboration data [96, 97]. This contribution must be added to the  $g \rightarrow c\bar{c}$  contribution to obtain the total atmospheric prompt neutrino spectrum. We show that the prompt neutrino flux from intrinsic charm can be comparable to those calculated within QCD computations not including intrinsic charm. The inclusion of this component as a background in the atmospheric neutrino flux can have important implications on the flux and spectral shape of the “IceCube excess neutrinos”.

We emphasize that IceCube can test these differential cross sections which have proven to be difficult to measure in colliders. This synergy between IceCube and the collider searches [98–101] can constrain the normalization of the intrinsic charm contribution and contribute to the investigation of a  $\sim 36$  year old puzzle in QCD.

**II Calculations of neutrino fluxes:** The earliest prompt neutrino calculations employed a proton-only cosmic ray flux known as the “broken power-law” [61, 62, 68, 102, 103]. Recent observations of cosmic ray flux indicate a mixed composition [104–106]: the Gaisser 2012 fit [104] with (i) the third component being proton (H3P), or (ii) mixed (H3A), and the Stanev et al., 2014 fit [106] fit with (iii) three (H14A), or (iv) four cosmic ray populations (H14B). We convert these to an equivalent all-proton flux,  $\phi_p(E, X)$ , where  $E$  and  $X$  denote the proton energy and the atmospheric column depth, respectively [74].

Assuming that the fluxes are separable in energy and column depth, we write the cascade equations as [61, 62, 68, 74, 76, 107, 108]

$$\frac{d\phi_p(E, X)}{dX} = -\frac{\phi_p(E, X)}{\lambda_p(E)} + Z_{pp}(E)\frac{\phi_p(E, X)}{\lambda_p(E)}, \quad (1)$$

$$\begin{aligned} \frac{d\phi_m(E, X)}{dX} = & -\frac{\phi_m(E, X)}{\rho(X)\delta_m(E)} - \frac{\phi_m(E, X)}{\lambda_m(E)} \\ & + Z_{mm}(E)\frac{\phi_m(E, X)}{\lambda_m(E)} + Z_{pm}(E)\frac{\phi_p(E, X)}{\lambda_p(E)}, \quad (2) \end{aligned}$$

$$\frac{d\phi_\ell(E, X)}{dX} = \sum_m Z_{m\ell}(E)\frac{\phi_m(E, X)}{\rho(X)\delta_m(E)}, \quad (3)$$

where  $\lambda_p(E)$  [ $\lambda_m(E)$ ] denotes the nucleon [charm hadron] attenuation length. The charm hadron flux [lepton flux from the decay of charm hadron] are denoted by  $\phi_m(E, X)$  [ $\phi_\ell(E, X)$ ]. The atmospheric density and charm hadron decay length is denoted by  $\rho(X)$  and  $\delta_m(E)$ , respectively. The sum includes the contribution of all the relevant charm hadrons.

The production moments  $Z_{pp}(E)$ ,  $Z_{mm}(E)$ , and  $Z_{pm}(E)$  are defined as [62]

$$Z_{kj}(E) = \int_0^1 \frac{dx_E}{x_E} \frac{\phi_k\left(\frac{E}{x_E}, 0\right)}{\phi_k(E, 0)} \frac{\lambda_k(E)}{\lambda_k\left(\frac{E}{x_E}\right)} \frac{dn_{kj}(E/x_E)}{dx_E}, \quad (4)$$

where  $x_E = E/E_k$ , and  $dn_{kj}(E/x_E)/dx_E$  denote the production spectrum of  $j$  from the interaction of  $k$  with the air nucleon. The decay moments  $Z_{m\ell}(E)$  are calculated following Refs. [62, 68].

For  $\lambda_p(E)$ , we take the mean atomic number of air molecules,  $\langle A \rangle = 14.5$ . For the proton - air cross section, we take the values from QGSJet0.1c [109]. Additional parameters required to calculate  $Z_{pp}(E)$ ,  $Z_{mm}(E)$  and  $\lambda_m(E)$  are taken from Refs. [62, 73].

The calculation of  $Z_{pm}(E)$  involves the differential cross section  $\frac{d\sigma}{dx_F}(pp \rightarrow cX)$ . There are substantial uncertainties in this differential cross section, especially at high  $x_F$ . Modern colliders are not capable of measuring this differential cross section in the forward region

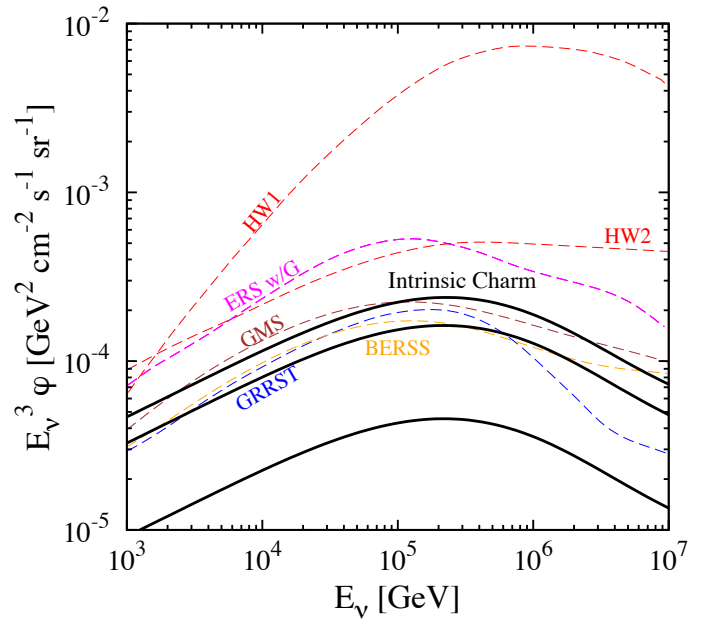


FIG. 1. Predictions for the atmospheric prompt neutrino ( $\nu_e + \bar{\nu}_e$  or  $\nu_\mu + \bar{\nu}_\mu$ ) spectrum,  $\varphi$ , as a function of the neutrino energy  $E_\nu$  using the H3A cosmic ray input flux. We show (i) GRRST [74], (ii) BERSS [73], (iii) GMS [76], (iv) ERS w/G [68, 69], (v) HW1 [82], (vi) HW2 [83], and (vii) our calculation (Intrinsic Charm). The highest, intermediate, and the lowest flux from the intrinsic charm contribution correspond to Case (A), Case (B), and Case (C) respectively. See text for details. The upper limit from the IceCube data on the prompt neutrino flux is 1.06 times the ERS w/G flux [7].

(high  $x_F$ ) [79]. State of the art calculations, which incorporate various different constraints, are also lacking for these differential cross sections at high  $x_F$ . Taking these uncertainties into account, we adopt three test cases using the data presented by the ISR experiments and the LEBC-MPS collaboration.

Case (A): For  $\Lambda_c$  production, we use Ref. [111] which normalizes their differential cross section to the ISR data [96]. For  $D$  mesons, we use the shape of the differential cross sections as calculated in Ref. [112], and normalize them to the data at the highest  $x_F$  ( $d\sigma/dx_F \approx 17_{-9}^{+18} \mu\text{b}$  at  $x_F \approx 0.32$ ) as measured by the LEBC-MPS collaboration [97].

Although the LEBC-MPS measurements extend to the forward region,  $x_F \approx 0.32 \pm 0.08$ , yet due to the uncertainties in the theoretical prediction and experimental measurements, it is difficult to estimate the contribution of intrinsic charm from this. Our strategy is to use the best-fit prediction following Ref. [73] ( $\approx 10 \mu\text{b}$  at  $x_F = 0.32$ ), and use the error bars of the LEBC-MPS measurement to maximize the intrinsic charm contribution. This sets the normalization for the  $D$  mesons.

Case (B): We use the charm hadron differential cross section spectral shapes as derived by Ref. [112]. To normalize these, we assume that the intrinsic charm cross section  $d\sigma/dx_F \approx 25 \mu\text{b}$  at  $x_F \approx 0.32$  for the  $D$  mesons.

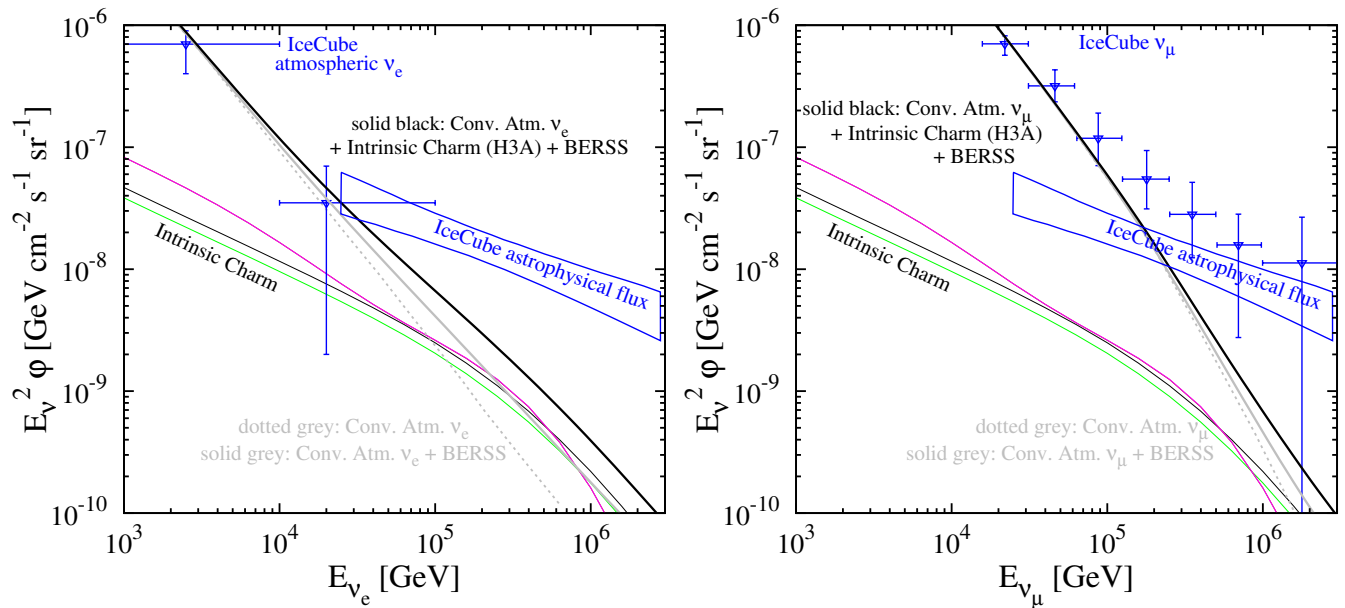


FIG. 2. **Left:** Comparison of the total atmospheric  $\nu_e + \bar{\nu}_e$  data (IceCube-86 for 332 days) with calculations. The contribution to the  $\nu_e + \bar{\nu}_e$  flux from intrinsic charm for Case (A) for various cosmic ray spectra is shown by the dashed lines (H3A = magenta, H3P = green, H14A = brown, and H14B = magenta. H14A and H14B are on top of each other). The conventional  $\nu_e + \bar{\nu}_e$  flux [110], conventional  $\nu_e + \bar{\nu}_e + \text{BERSS}$  (H3A), and conventional  $\nu_e + \bar{\nu}_e + \text{BERSS} + \text{intrinsic charm}$  contribution for H3A are shown. **Right:** Same as the left panel, but for  $\nu_\mu + \bar{\nu}_\mu$  [6] (IceCube-79/ 86 for 2 years). This measurement also includes the astrophysical neutrino flux. The astrophysical flux shown in these panels is from Refs. [4].

Since we are using the same model for the  $D$  mesons and the  $\Lambda_c$  production, this also gives the normalization of the  $\Lambda_c$  cross section.

Case (C): We again use the charm hadron differential cross section spectral shape as derived by Ref. [112]. We normalize the cross section such that the intrinsic charm cross section  $d\sigma/dx_F \approx 7 \mu\text{b}$  at  $x_F \approx 0.32$  for the  $D$  mesons. This corresponds to the best fit point of the LEBC-MPS measurement. Similar to Case (B), we use the same production model for  $D$  mesons and  $\Lambda_c$  production. The above mentioned differential cross section for the  $D$  mesons also set the normalization for the  $\Lambda_c$  production.

The cross sections for various charm mesons and hadrons at  $\sqrt{s} \approx 39 \text{ GeV}$  for the three cases discussed above are given in Table I. The cross section for the production of  $\Lambda_c^+ + \Lambda_c^-$  in Case A is anomalously high as the normalization is fit to the ISR data. The production cross section for these charmed bound states in the other cases are  $\sim \mathcal{O}(\mu\text{b})$  and these are normalized to the LEBC-MPS data.

We illustrate the uncertainty of the intrinsic charm flux by the three cases as mentioned above. The Case (C) does not represent a lower limit to the intrinsic charm contribution to the differential cross section. It is possible that the intrinsic charm contribution is lower, and this will correspond to a lower contribution to the atmospheric prompt neutrino flux compared to what is presented here. As is evident from our discussion, the intrinsic charm cross section is not at all well known. De-

spite decades of effort, colliders have not yet been able to definitively measure its normalization. We examine the role of IceCube in this search.

The intrinsic charm cross section scales with the mass number,  $A$ , approximately as  $A^{0.755 \pm 0.016}$ , according to SELEX [113]. The energy dependence of the intrinsic charm contribution follows the inelastic cross section [114].

We solve Eqs. 1 – 3 separately in the low and high energy regime [61, 62, 68, 74, 76]. The final prompt neutrino flux is a geometric interpolation of the low and high energy solutions and includes the contribution of all the charm hadrons,  $D^0, \bar{D}^0, D^\pm, D_s^\pm, \Lambda_c^\pm$ . The  $\Lambda_c$  shares a  $c$ -quark from the  $|uudc\bar{c}\rangle$  state of the proton, and thus has a harder differential cross section  $d\sigma/dx_F$  when compared to that of the  $D$  mesons.

Our calculation improves over the previous esti-

TABLE I. Production cross sections (in  $\mu\text{b}$ ) at  $\sqrt{s} \approx 39 \text{ GeV}$  for the various charm mesons and baryons via the intrinsic charm models discussed in the text. Here  $\sigma(D_{(s)}^\pm) = \sigma(D_{(s)}^+) + \sigma(D_{(s)}^-)$  and  $\sigma(\Lambda_c^\pm) = \sigma(\Lambda_c^+) + \sigma(\Lambda_c^-)$ .

Case	$\sigma(D^\pm)$	$\sigma(D^0 + \bar{D}^0)$	$\sigma(D_s^\pm)$	$\sigma(\Lambda_c^\pm)$
Case A	3.88	3.88	2.29	183.54
Case B	3.88	3.88	2.29	4.99
Case C	1.09	1.09	0.64	1.47

mates [60, 61, 82, 83, 86] in various important ways. We normalize our calculations to the ISR and the LEBC-MPS collaboration data [96, 97], which were not used in the earliest works. We employ the latest cosmic ray flux measurement, and the experimentally measured nuclear scaling of the cross section, and a theoretically motivated energy dependence of the cross section. We use a more updated calculation of the intrinsic charm cross section which takes into account the inherent non-perturbativeness of the process [111, 112], whereas some of these earlier works [82, 83] used a modified pQCD prescription to account for the high  $x_F$  data.

**III Results:** Our predictions for the flux of neutrinos ( $\nu_\mu + \bar{\nu}_\mu$  or  $\nu_e + \bar{\nu}_e$ ) are shown in Fig. 1. The three flux scenarios are given by Case (A), Case (B), and Case (C). We also show the best-fit flux calculated by BERSS [73], GMS [76], GRRST [74], HW1 [82], HW2 [83], and ERS w/G [6, 95], all of which have large theoretical error bars. Remarkably, we find that the atmospheric prompt neutrino flux due to intrinsic charm can be at the same level as those estimated within QCD calculations not including intrinsic charm.

The neutrino fluxes due to intrinsic charm can be large enough to be detectable by IceCube. The detectability depends on the contribution of the fluxes arising from QCD not including intrinsic charm. For example, if the best fit prediction follows the BERSS flux, and the intrinsic charm contribution is as large as Case (B), then IceCube can get a strong constraint on intrinsic charm provided the uncertainties in BERSS are made smaller. It is important to decrease the uncertainties within the various pQCD predictions in order to obtain a robust constraint on intrinsic charm; global analyses of laboratory data also have this same requirement [115, 116].

For case (A), the dominant contribution to the flux comes from the production of  $\Lambda_c^\pm$ , followed by  $D^\pm$ ,  $D^0 + \bar{D}^0$ , and  $D_s^\pm$ . For cases (B) and (C), the production of  $D^\pm$ ,  $D^0 + \bar{D}^0$ ,  $D_s^\pm$ , and  $\Lambda_c^\pm$  contribute to the atmospheric prompt neutrino flux in decreasing order. These contributions can be simply understood by comparing their respective production cross sections (see Table I) multiplied by the decay branching fractions to neutrinos.

If the intrinsic charm contribution follows Case (C), and the non intrinsic charm contribution follows the BERSS flux, then it will be difficult to measure the intrinsic charm unless very precise measurements of the atmospheric prompt neutrino fluxes are made. Even in this pessimistic case, weak upper limits on intrinsic charm can be obtained from the data. Encouragingly, present IceCube constraints have already started to constrain the forward production within the various QCD computations not including intrinsic charm [80, 84, 85]. It is expected that near future measurements of the prompt atmospheric neutrino flux will further constrain these various contributions in pQCD.

In the intrinsic charm picture, the proton preferentially

forms a charm hadron with a similar energy. In the  $g \rightarrow c\bar{c}$  picture, due to its steeply falling  $d\sigma/dx$  distribution, the charm hadron comes dominantly from a proton at much higher energy. Our results are slightly lower than the calculation presented in Ref. [83] due to the above mentioned refinements.

So far, IceCube has presented upper bounds on prompt neutrinos. IceCube assumes that the prompt neutrino flux is the ERS w/G spectrum and varies the normalization. The present limit on the prompt neutrino spectrum is 1.06 times the ERS w/G flux [7]. These IceCube limits are close to the intrinsic charm prompt neutrino spectrum predictions, implying that IceCube can give information about intrinsic charm content of the proton in the near future.

In Fig. 2 (left), we compare our calculation for Case (A) and the measurement of the atmospheric  $\nu_e$  flux [110]. The conventional atmospheric  $\nu_e + \bar{\nu}_e$  flux (angular averaged) is taken from Refs. [57, 58, 110]. The conventional atmospheric  $\nu_e + \bar{\nu}_e$  flux, the prompt  $\nu_e$  flux due to intrinsic charm in case (A) for various different input cosmic ray model, the total atmospheric  $\nu_e$  flux including the BERSS and due to intrinsic charm in case (A) for the H3A cosmic ray input model are also shown. We also show the astrophysical neutrino spectrum from Ref. [4] in the energy range [25 TeV, 2.8 PeV]. This shows that although the inclusion of the intrinsic charm component can change the background for astrophysical neutrinos, yet atmospheric prompt neutrinos cannot explain the ‘‘IceCube excess neutrinos’’.

Normalizing to the ISR and the LEBC-MPS collaboration data does not contradict the atmospheric  $\nu_e$  measurements. The importance of atmospheric  $\nu_e$  measurement for prompt neutrinos was pointed out in Ref. [92], and we argue that it might be the best channel to search for intrinsic charm as well. We predict that the atmospheric  $\nu_e + \bar{\nu}_e$  flux due to intrinsic charm is larger than  $g \rightarrow c\bar{c}$  contribution at  $\gtrsim 50$  TeV. A more precise measurement of the atmospheric  $\nu_e$  spectrum at slightly higher energies can give strong constraints on the intrinsic charm content of the proton.

Atmospheric prompt neutrinos cannot explain the ‘‘IceCube excess neutrinos’’ since prompt neutrinos have a softer spectral shape and have accompanying muons. The ‘‘IceCube excess neutrinos’’ have an energy spectrum varying within  $\sim E^{-2.1}$  and  $E^{-2.6}$  between  $\sim 30$  TeV and 3 PeV and do not have any accompanying muons. The prompt neutrino flux follows the much softer cosmic ray spectrum.

For downgoing events, the IceCube self veto can discriminate between atmospheric and astrophysical neutrinos [117, 118]. Every atmospheric neutrino is accompanied by a muon or an electromagnetic shower from the same interaction producing the neutrino. The muon or the shower detected in coincidence with the neutrino, reduces the atmospheric neutrino flux by a factor  $\gtrsim 2$  at energies  $\gtrsim 10$  TeV [3]. This also results in a difference in the zenith angle distributions of astrophysical and prompt

neutrinos.

The angular distribution of atmospheric prompt neutrinos is approximately isotropic at  $\lesssim 10^7$  GeV. Conventional atmospheric neutrinos have a smaller vertical flux compared to the horizontal flux. Searching for atmospheric neutrinos in the vertical direction can more easily find the prompt component. More theoretical and experimental work is also required to narrow down the uncertainties of the predictions made within pQCD calculation to extract the contribution of intrinsic charm from the IceCube data.

A comparison of the  $\nu_\mu + \bar{\nu}_\mu$  flux from the Northern Hemisphere with calculations is shown Fig. 2 (right) [6]. The intrinsic charm component is shown for Case (A). The astrophysical neutrino spectrum in the energy range [25 TeV, 2.8 PeV] from Ref. [4] is shown. The neutrino flux due to intrinsic charm cannot increase, since it will be in contradiction with the ISR and the LEBC-MPS collaboration data. The inclusion of this contribution may result in a revision of the astrophysical neutrino spectrum. Since these events are up-going, the atmospheric veto does not play any role, and one needs to model the astrophysical neutrino flux before inferring the prompt neutrino contribution using this detection channel.

In Fig. 2, we only show the intrinsic charm contribution to the prompt atmospheric neutrino flux for Case (A). This has the largest flux among the three cases that we have considered, and hence we are displaying the optimistic case. For this case, the total prompt atmospheric neutrino flux is dominated by the intrinsic charm contribution. The intrinsic charm contribution in Case (B) is comparable to the best fit BERSS flux. If the intrinsic charm contribution follows Case (C), then the total prompt atmospheric neutrino flux will be totally dominated by the BERSS flux. In such case, upper limits on intrinsic charm of the proton can only be obtained if the prompt atmospheric neutrinos are measured quite precisely.

We only plot the best fit BERSS flux in Fig. 2 for clarity. We do not show the uncertainty in this flux which is substantial [73]. It is essential to decrease the uncertainties in this calculation to obtain a more robust constraint on intrinsic charm from astroparticle measurements.

Present upper limits from IceCube have already started to constrain various pQCD computations not including intrinsic charm, and near future data will have stronger constraints [80, 84, 85]. There are spectral differences between astrophysical neutrinos and prompt atmospheric neutrinos. IceCube uses a veto which produces a different angular dependence for the astrophysical neutrinos when compared to the prompt atmospheric neutrinos. These distinct features help in determining the atmospheric prompt neutrino sample in the IceCube data. Various different analyses of IceCube give similar upper limits on prompt atmospheric neutrinos implying that the constraint is robust.

**IV Conclusions:** The landmark discovery of astrophysical neutrinos by IceCube opens up a new era. Due to the atmospheric veto employed by IceCube, any atmospheric neutrino spectrum shows an up v/s down asymmetry. The excess of neutrinos unveiled by IceCube is isotropic implying the astrophysical origin of these events. Careful consideration of the atmospheric neutrino background will impact the astrophysical neutrino flux interpretation.

The neutrino backgrounds considered so far by IceCube are the conventional atmospheric and prompt neutrinos predicted by  $g \rightarrow c\bar{c}$ . Intrinsic charm, rigorously predicted by QCD, has strong theoretical justification and some experimental indications. We find that this often neglected component can be as large as the component estimated within the various pQCD computations not including intrinsic charm, without violating any direct experimental constraints. This has important implications in interpreting the astrophysical neutrino flux, and inferring the atmospheric prompt neutrino component.

We present our calculation of the neutrino flux due to intrinsic charm in Fig. 1 after normalizing to the ISR and the LEBC-MPS collaboration data. We show the atmospheric prompt neutrino flux due to three different scenarios. The atmospheric prompt neutrino flux due to intrinsic charm is comparable to that estimated within various pQCD computations not including intrinsic charm. Our calculation is lower than Refs. [82, 83] as we use improved theoretical and experimental input.

The measurement of atmospheric  $\nu_e + \bar{\nu}_e$  at higher energies is the most promising channel to discover prompt neutrinos and constrain the intrinsic charm of the proton (Fig. 2 left). The comparison of the total atmospheric flux with the  $\nu_\mu + \bar{\nu}_\mu$  data, including the intrinsic charm contribution, is shown in Fig. 2 (right). The total atmospheric neutrino flux including intrinsic charm can dominate the flux contribution within the pQCD framework at energies  $\gtrsim 200$  TeV and  $\gtrsim 2$  PeV for  $\nu_e + \bar{\nu}_e$  and  $\nu_\mu + \bar{\nu}_\mu$  respectively.

The conventional atmospheric  $\nu_e + \bar{\nu}_e$  flux is lower, implying that the prompt component is more visible in this channel. We estimate that a measurement of the atmospheric  $\nu_e + \bar{\nu}_e$  flux at  $\sim 200$  TeV at  $\sim 50\%$  accuracy will cleanly distinguish between the pQCD contribution and intrinsic charm component.

The current upper limit on prompt neutrinos is 1.06 times the ERS w/G flux. The neutrino flux due to intrinsic charm is at the same level as the ERS w/G flux implying that IceCube can constrain intrinsic charm of the proton. This shows that IceCube can constrain QCD predictions in regions of parameter space which have been difficult to constrain in colliders for decades.

The multi-pronged approach consisting of IceCube data, collider physics, and global analysis will help us constrain the intrinsic charm of the proton, a  $\sim 36$  year old problem in QCD. Using the weakly interacting neutrino to constrain the strong interactions also highlights

the importance of cross disciplinary searches in physics.

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- [1] **IceCube** Collaboration, M. G. Aartsen *et al.*, “First observation of PeV-energy neutrinos with IceCube”, *Phys. Rev. Lett.* **111** (2013) 021103, [arXiv:1304.5356](#).
  - [2] **IceCube** Collaboration, M. G. Aartsen *et al.*, “Evidence for High-Energy Extraterrestrial Neutrinos at the IceCube Detector”, *Science* **342** (2013) 1242856, [arXiv:1311.5238](#).
  - [3] **IceCube** Collaboration, M. G. Aartsen *et al.*, “Observation of High-Energy Astrophysical Neutrinos in Three Years of IceCube Data”, *Phys. Rev. Lett.* **113** (2014) 101101, [arXiv:1405.5303](#).
  - [4] **IceCube** Collaboration, M. G. Aartsen *et al.*, “A combined maximum-likelihood analysis of the high-energy astrophysical neutrino flux measured with IceCube”, *Astrophys. J.* **809** (2015), no. 1, 98, [arXiv:1507.03991](#).
  - [5] **IceCube** Collaboration, M. G. Aartsen *et al.*, “Evidence for Astrophysical Muon Neutrinos from the Northern Sky with IceCube”, *Phys. Rev. Lett.* **115** (2015), no. 8, 081102, [arXiv:1507.04005](#).
  - [6] **IceCube** Collaboration, M. G. Aartsen *et al.*, “The IceCube Neutrino Observatory - Contributions to ICRC 2015 Part II: Atmospheric and Astrophysical Diffuse Neutrino Searches of All Flavors”, in “Proceedings, 34th International Cosmic Ray Conference (ICRC 2015)”. 2015. [arXiv:1510.05223](#).
  - [7] **IceCube** Collaboration, M. G. Aartsen *et al.*, “Observation and Characterization of a Cosmic Muon Neutrino Flux from the Northern Hemisphere using six years of IceCube data”, [arXiv:1607.08006](#).
  - [8] R. Laha, J. F. Beacom, B. Dasgupta, S. Horiuchi, and K. Murase, “Demystifying the PeV Cascades in IceCube: Less (Energy) is More (Events)”, *Phys. Rev. D* **88** (2013) 043009, [arXiv:1306.2309](#).
  - [9] K. Murase and K. Ioka, “TeV?PeV Neutrinos from Low-Power Gamma-Ray Burst Jets inside Stars”, *Phys. Rev. Lett.* **111** (2013), no. 12, 121102, [arXiv:1306.2274](#).
  - [10] L. A. Anchordoqui *et al.*, “Cosmic Neutrino Pevatrons: A Brand New Pathway to Astronomy, Astrophysics, and Particle Physics”, *JHEAp* **1-2** (2014) 1–30, [arXiv:1312.6587](#).
  - [11] M. D. Kistler, T. Stanev, and H. Yuksel, “Cosmic PeV Neutrinos and the Sources of Ultrahigh Energy Protons”, *Phys. Rev. D* **90** (2014), no. 12, 123006, [arXiv:1301.1703](#).
  - [12] M. Ahlers and K. Murase, “Probing the Galactic Origin of the IceCube Excess with Gamma-Rays”, *Phys. Rev. D* **90** (2014), no. 2, 023010, [arXiv:1309.4077](#).
  - [13] C.-Y. Chen, P. S. Bhupal Dev, and A. Soni, “Standard model explanation of the ultrahigh energy neutrino events at IceCube”, *Phys. Rev. D* **89** (2014), no. 3, 033012, [arXiv:1309.1764](#).
  - [14] L. A. Anchordoqui, “Neutron beta-decay as the origin of IceCube’s PeV (anti)neutrinos”, *Phys. Rev. D* **91** (2015) 027301, [arXiv:1411.6457](#).
  - [15] K. Fang, “High-Energy Neutrino Signatures of Newborn Pulsars In the Local Universe”, *JCAP* **1506** (2015), no. 06, 004, [arXiv:1411.2174](#).
  - [16] K. Kashiyama and P. Meszaros, “Galaxy Mergers as a Source of Cosmic Rays, Neutrinos, and Gamma Rays”, *Astrophys. J.* **790** (2014) L14, [arXiv:1405.3262](#).
  - [17] P. Baerwald, M. Bustamante, and W. Winter, “Are gamma-ray bursts the sources of ultra-high energy cosmic rays?”, *Astropart. Phys.* **62** (2015) 66–91, [arXiv:1401.1820](#).
  - [18] C.-Y. Chen, P. S. Bhupal Dev, and A. Soni, “Two-component flux explanation for the high energy neutrino events at IceCube”, *Phys. Rev. D* **92** (2015), no. 7, 073001, [arXiv:1411.5658](#).
  - [19] S. Ando, I. Tamborra, and F. Zandanel, “Tomographic Constraints on High-Energy Neutrinos of Hadronuclear Origin”, *Phys. Rev. Lett.* **115** (2015), no. 22, 221101, [arXiv:1509.02444](#).
  - [20] K. Emig, C. Lunardini, and R. Windhorst, “Do high energy astrophysical neutrinos trace star formation?”, *JCAP* **1512** (2015) 029, [arXiv:1507.05711](#).
  - [21] I. Tamborra and S. Ando, “Inspecting the supernova?gamma-ray-burst connection with high-energy neutrinos”, *Phys. Rev. D* **93** (2016), no. 5, 053010, [arXiv:1512.01559](#).
  - [22] K. Murase, D. Guetta, and M. Ahlers, “Hidden Cosmic-Ray Accelerators as an Origin of TeV-PeV Cosmic Neutrinos”, *Phys. Rev. Lett.* **116** (2016), no. 7, 071101, [arXiv:1509.00805](#).
  - [23] M. D. Kistler, “Problems and Prospects from a Flood of Extragalactic TeV Neutrinos in IceCube”, [arXiv:1511.01530](#).
  - [24] M. D. Kistler, “On TeV Gamma Rays and the Search for Galactic Neutrinos”, [arXiv:1511.05199](#).
  - [25] M. D. Kistler and R. Laha, “Multi-PeV Signals from a New Astrophysical Neutrino Flux Beyond the Glashow Resonance”, [arXiv:1605.08781](#).
  - [26] R. Moharana and S. Razzaque, “Angular correlation between IceCube high-energy starting events and starburst sources”, [arXiv:1606.04420](#).
  - [27] F. Halzen and A. Kheirandish, “High Energy Neutrinos from Recent Blazar Flares”, [arXiv:1605.06119](#).
  - [28] G. Pagliaroli, C. Evoli, and F. L. Villante, “Expectations for high energy diffuse galactic neutrinos for different cosmic ray distributions”, [arXiv:1606.04489](#).

- [29] L. A. Anchordoqui, “Neutrino lighthouse powered by Sagittarius A\* disk dynamo”, [arXiv:1606.01816](#).
- [30] R. K. Dey, S. Dam, and S. Ray, “Searching PeV neutrinos from photomeson interactions in magnetars”, [arXiv:1603.07833](#).
- [31] K. Fang and M. C. Miller, “A New Method for Finding Point Sources in High-energy Neutrino Data”, [arXiv:1603.09306](#).
- [32] A. Palladino and F. Vissani, “Extragalactic plus Galactic model for IceCube neutrino events”, [arXiv:1601.06678](#).
- [33] N. Senno, K. Murase, and P. Meszaros, “Choked Jets and Low-Luminosity Gamma-Ray Bursts as Hidden Neutrino Sources”, *Phys. Rev.* **D93** (2016), no. 8, 083003, [arXiv:1512.08513](#).
- [34] M. Bustamante, J. F. Beacom, and W. Winter, “Theoretically palatable flavor combinations of astrophysical neutrinos”, *Phys. Rev. Lett.* **115** (2015), no. 16, 161302, [arXiv:1506.02645](#).
- [35] C. A. Argüelles, T. Katori, and J. Salvado, “New Physics in Astrophysical Neutrino Flavor”, *Phys. Rev. Lett.* **115** (2015) 161303, [arXiv:1506.02043](#).
- [36] A. C. Vincent, S. Palomares-Ruiz, and O. Mena, “Analysis of the 4-year IceCube HESE data”, [arXiv:1605.01556](#).
- [37] J. Kopp, J. Liu, and X.-P. Wang, “Boosted Dark Matter in IceCube and at the Galactic Center”, *JHEP* **04** (2015) 105, [arXiv:1503.02669](#).
- [38] B. Dasgupta and R. Laha, “Neutrinos in IceCube/KM3NeT as probes of Dark Matter Substructures in Galaxy Clusters”, *Phys. Rev.* **D86** (2012) 093001, [arXiv:1206.1322](#).
- [39] K. Murase, R. Laha, S. Ando, and M. Ahlers, “Testing the Dark Matter Scenario for PeV Neutrinos Observed in IceCube”, *Phys. Rev. Lett.* **115** (2015), no. 7, 071301, [arXiv:1503.04663](#).
- [40] C. Rott, K. Kohri, and S. C. Park, “Superheavy dark matter and IceCube neutrino signals: Bounds on decaying dark matter”, *Phys. Rev.* **D92** (2015), no. 2, 023529, [arXiv:1408.4575](#).
- [41] A. Esmaili, S. K. Kang, and P. D. Serpico, “IceCube events and decaying dark matter: hints and constraints”, *JCAP* **1412** (2014), no. 12, 054, [arXiv:1410.5979](#).
- [42] A. Bhattacharya, M. H. Reno, and I. Sarcevic, “Reconciling neutrino flux from heavy dark matter decay and recent events at IceCube”, *JHEP* **06** (2014) 110, [arXiv:1403.1862](#).
- [43] A. Bhattacharya, R. Gandhi, and A. Gupta, “The Direct Detection of Boosted Dark Matter at High Energies and PeV events at IceCube”, *JCAP* **1503** (2015), no. 03, 027, [arXiv:1407.3280](#).
- [44] K. C. Y. Ng and J. F. Beacom, “Cosmic neutrino cascades from secret neutrino interactions”, *Phys. Rev.* **D90** (2014), no. 6, 065035, [arXiv:1404.2288](#), [Erratum: *Phys. Rev.* **D90**, no. 8, 089904 (2014)].
- [45] B. Dutta, Y. Gao, T. Li, C. Rott, and L. E. Strigari, “Leptoquark implication from the CMS and IceCube experiments”, *Phys. Rev.* **D91** (2015) 125015, [arXiv:1505.00028](#).
- [46] P. Ko and Y. Tang, “IceCube Events from Heavy DM decays through the Right-handed Neutrino Portal”, *Phys. Lett.* **B751** (2015) 81–88, [arXiv:1508.02500](#).
- [47] C. El Aisati, M. Gustafsson, T. Hambye, and T. Scarna, “Dark Matter Decay to a Photon and a Neutrino: the Double Monochromatic Smoking Gun Scenario”, *Phys. Rev.* **D93** (2016), no. 4, 043535, [arXiv:1510.05008](#).
- [48] S. M. Boucenna, M. Chianese, G. Mangano, G. Miele, S. Morisi, O. Pisanti, and E. Vitagliano, “Decaying Leptophilic Dark Matter at IceCube”, *JCAP* **1512** (2015), no. 12, 055, [arXiv:1507.01000](#).
- [49] S. B. Roland, B. Shakya, and J. D. Wells, “PeV neutrinos and a 3.5 keV x-ray line from a PeV-scale supersymmetric neutrino sector”, *Phys. Rev.* **D92** (2015), no. 9, 095018, [arXiv:1506.08195](#).
- [50] J. F. Cherry, A. Friedland, and I. M. Shoemaker, “Short-baseline neutrino oscillations, Planck, and IceCube”, [arXiv:1605.06506](#).
- [51] P. S. B. Dev, D. K. Ghosh, and W. Rodejohann, “R-parity Violating Supersymmetry at IceCube”, [arXiv:1605.09743](#).
- [52] P. S. B. Dev, D. Kazanas, R. N. Mohapatra, V. L. Teplitz, and Y. Zhang, “Heavy right-handed neutrino dark matter and PeV neutrinos at IceCube”, [arXiv:1606.04517](#).
- [53] Y. Ema and T. Moroi, “Early Decay of Peccei-Quinn Fermion and the IceCube Neutrino Events”, [arXiv:1606.04186](#).
- [54] P. Di Bari, P. O. Ludl, and S. Palomares-Ruiz, “Unifying leptogenesis, dark matter and high-energy neutrinos with right-handed neutrino mixing via Higgs portal”, [arXiv:1606.06238](#).
- [55] U. K. Dey, S. Mohanty, and G. Tomar, “Leptoquarks: 750 GeV Diphoton Resonance and IceCube Events”, [arXiv:1606.07903](#).
- [56] S. W. Li, M. Bustamante, and J. F. Beacom, “Echo Technique to Distinguish Flavors of Astrophysical Neutrinos”, [arXiv:1606.06290](#).
- [57] M. Honda, T. Kajita, K. Kasahara, S. Midorikawa, and T. Sanuki, “Calculation of atmospheric neutrino flux using the interaction model calibrated with atmospheric muon data”, *Phys. Rev.* **D75** (2007) 043006, [arXiv:astro-ph/0611418](#).
- [58] G. D. Barr, T. K. Gaisser, P. Lipari, S. Robbins, and T. Stanev, “A Three - dimensional calculation of atmospheric neutrinos”, *Phys. Rev.* **D70** (2004) 023006, [arXiv:astro-ph/0403630](#).
- [59] A. Fedynitch, J. Becker Tjus, and P. Desiati, “Influence of hadronic interaction models and the cosmic ray spectrum on the high energy atmospheric muon and neutrino flux”, *Phys. Rev.* **D86** (2012) 114024, [arXiv:1206.6710](#).
- [60] E. V. Bugaev, V. A. Naumov, S. I. Sinigovsky, and E. S. Zaslavskaya, “Prompt Leptons in Cosmic Rays”, *Nuovo Cim.* **C12** (1989) 41–73.
- [61] P. Gondolo, G. Ingelman, and M. Thunman, “Charm production and high-energy atmospheric muon and neutrino fluxes”, *Astropart. Phys.* **5** (1996) 309–332, [arXiv:hep-ph/9505417](#).
- [62] L. Pasquali, M. H. Reno, and I. Sarcevic, “Lepton fluxes from atmospheric charm”, *Phys. Rev.* **D59** (1999) 034020, [arXiv:hep-ph/9806428](#).
- [63] G. Gelmini, P. Gondolo, and G. Varieschi, “Prompt atmospheric neutrinos and muons: NLO versus LO QCD predictions”, *Phys. Rev.* **D61** (2000) 036005, [arXiv:hep-ph/9904457](#).



- [64] G. Gelmini, P. Gondolo, and G. Varieschi, “Prompt atmospheric neutrinos and muons: Dependence on the gluon distribution function”, *Phys. Rev.* **D61** (2000) 056011, [arXiv:hep-ph/9905377](#).
- [65] J. Candia and E. Roulet, “Rigidity dependent knee and cosmic ray induced high energy neutrino fluxes”, *JCAP* **0309** (2003) 005, [arXiv:astro-ph/0306632](#).
- [66] A. D. Martin, M. G. Ryskin, and A. M. Stasto, “Prompt neutrinos from atmospheric  $c\bar{c}$  and  $b\bar{b}$  production and the gluon at very small  $x$ ”, *Acta Phys. Polon.* **B34** (2003) 3273–3304, [arXiv:hep-ph/0302140](#).
- [67] P. Berghaus, T. Montaruli, and J. Ranft, “Charm Production in DPMJET”, *JCAP* **0806** (2008) 003, [arXiv:0712.3089](#).
- [68] R. Enberg, M. H. Reno, and I. Sarcevic, “Prompt neutrino fluxes from atmospheric charm”, *Phys. Rev.* **D78** (2008) 043005, [arXiv:0806.0418](#).
- [69] T. K. Gaisser, “Atmospheric leptons”, *EPJ Web Conf.* **52** (2013) 09004, [arXiv:1303.1431](#).
- [70] E.-J. Ahn, R. Engel, A. Fedynitch, T. K. Gaisser, F. Riehn, and T. Stanev, “Atmospheric neutrinos at high energy”, in “Proceedings, 33rd International Cosmic Ray Conference (ICRC2013): Rio de Janeiro, Brazil, July 2-9, 2013”, p. 1144.
- [71] P. Lipari, “Establishing the astrophysical origin of a signal in a neutrino telescope”, [arXiv:1308.2086](#).
- [72] F. Riehn, R. Engel, A. Fedynitch, T. K. Gaisser, and T. Stanev, “Charm production in SIBYLL”, *EPJ Web Conf.* **99** (2015) 12001, [arXiv:1502.06353](#).
- [73] A. Bhattacharya, R. Enberg, M. H. Reno, I. Sarcevic, and A. Stasto, “Perturbative charm production and the prompt atmospheric neutrino flux in light of RHIC and LHC”, *JHEP* **06** (2015) 110, [arXiv:1502.01076](#).
- [74] R. Gauld, J. Rojo, L. Rottoli, S. Sarkar, and J. Talbert, “The prompt atmospheric neutrino flux in the light of LHCb”, *JHEP* **02** (2016) 130, [arXiv:1511.06346](#).
- [75] R. Gauld, J. Rojo, L. Rottoli, and J. Talbert, “Charm production in the forward region: constraints on the small- $x$  gluon and backgrounds for neutrino astronomy”, *JHEP* **11** (2015) 009, [arXiv:1506.08025](#).
- [76] M. V. Garzelli, S. Moch, and G. Sigl, “Lepton fluxes from atmospheric charm revisited”, *JHEP* **10** (2015) 115, [arXiv:1507.01570](#).
- [77] A. Fedynitch, R. Engel, T. K. Gaisser, F. Riehn, and T. Stanev, “Calculation of conventional and prompt lepton fluxes at very high energy”, *EPJ Web Conf.* **99** (2015) 08001, [arXiv:1503.00544](#).
- [78] A. Fedynitch, R. Engel, T. K. Gaisser, F. Riehn, and S. Todor, “MCEQ - numerical code for inclusive lepton flux calculations”, *PoS ICRC2015* (2015) 1129.
- [79] C. Baus, R. Engel, A. Fedynitch, U. Kramer, T. Pierog, F. Riehn, and R. Ulrich, “The impact of a fixed-target experiment with LHC beam for astroparticle physics”, *PoS ICRC2015* (2015) 407.
- [80] A. Bhattacharya, R. Enberg, Y. S. Jeong, C. S. Kim, M. H. Reno, I. Sarcevic, and A. Stasto, “Prompt atmospheric neutrino fluxes: perturbative QCD models and nuclear effects”, [arXiv:1607.00193](#).
- [81] T. K. Gaisser, “Atmospheric Neutrinos”, *J. Phys. Conf. Ser.* **718** (2016), no. 5, 052014, [arXiv:1605.03073](#).
- [82] F. Halzen and L. Wille, “Upper Limit on Forward Charm Contribution to Atmospheric Neutrino Flux”, [arXiv:1601.03044](#).
- [83] F. Halzen and L. Wille, “On the Charm Contribution to the Atmospheric Neutrino Flux”, [arXiv:1605.01409](#).
- [84] **PROSA** Collaboration, M. V. Garzelli, S. Moch, O. Zenaiev, A. Cooper-Sarkar, A. Geiser, K. Lipka, R. Placakyte, and G. Sigl, “Prompt neutrino fluxes in the atmosphere with PROSA parton distribution functions”, [arXiv:1611.03815](#).
- [85] M. Benzke, M. V. Garzelli, B. Kniehl, G. Kramer, S. Moch, and G. Sigl, “Prompt neutrinos from atmospheric charm in the general-mass variable-flavor-number scheme”, [arXiv:1705.10386](#).
- [86] A. Fedynitch, “Phenomenology of atmospheric neutrinos”, *EPJ Web Conf.* **116** (2016) 11010.
- [87] S. J. Brodsky, P. Hoyer, C. Peterson, and N. Sakai, “The Intrinsic Charm of the Proton”, *Phys. Lett.* **B93** (1980) 451–455.
- [88] S. J. Brodsky, A. Kusina, F. Lyonnet, I. Schienbein, H. Spiesberger, and R. Vogt, “A review of the intrinsic heavy quark content of the nucleon”, *Adv. High Energy Phys.* **2015** (2015) 231547, [arXiv:1504.06287](#).
- [89] S. J. Brodsky, V. A. Bednyakov, G. I. Lykasov, J. Smiesko, and S. Tokar, “The Physics of Heavy Quark Distributions in Hadrons: Collider Tests”, [arXiv:1612.01351](#).
- [90] T. J. Hobbs, “Recent progress on intrinsic charm”, in “12th Conference on Quark Confinement and the Hadron Spectrum (Confinement XII) Thessaloniki, Greece, August 28-September 2, 2016”. 2016. [arXiv:1612.05686](#).
- [91] G. Gelmini, P. Gondolo, and G. Varieschi, “Measuring the prompt atmospheric neutrino flux with down-going muons in neutrino telescopes.”, *Phys. Rev.* **D67** (2003) 017301, [arXiv:hep-ph/0209111](#).
- [92] J. F. Beacom and J. Candia, “Shower power: Isolating the prompt atmospheric neutrino flux using electron neutrinos”, *JCAP* **0411** (2004) 009, [arXiv:hep-ph/0409046](#).
- [93] R. Gandhi and S. Panda, “Probing the cosmic ray ‘Knee’ and very high energy prompt muon and neutrino fluxes via underground muons”, *JCAP* **0607** (2006) 011, [arXiv:hep-ph/0512179](#).
- [94] P. Desiati and T. K. Gaisser, “Seasonal variation of atmospheric leptons as a probe of charm”, *Phys. Rev. Lett.* **105** (2010) 121102, [arXiv:1008.2211](#).
- [95] **IceCube** Collaboration, M. G. Aartsen *et al.*, “Atmospheric and astrophysical neutrinos above 1 TeV interacting in IceCube”, *Phys. Rev.* **D91** (2015), no. 2, 022001, [arXiv:1410.1749](#).
- [96] **R608** Collaboration, P. Chauvat *et al.*, “Production of Lambda(c) With Large X(f) at the ISR”, *Phys. Lett.* **B199** (1987) 304.
- [97] R. Ammar *et al.*, “D-Meson Production in 800-GeV/c p p Interactions”, *Phys. Rev. Lett.* **61** (1988) 2185–2188.
- [98] S. Rostami, A. Khorramian, A. Aleedaneshvar, and M. Goharipour, “The impact of the intrinsic charm quark content of a proton on the differential  $\gamma + c$  cross section”, *J. Phys.* **G43** (2016), no. 5, 055001, [arXiv:1510.08421](#).
- [99] G. Bailas and V. P. Goncalves, “Phenomenological implications of the intrinsic charm in the Z boson production at the LHC”, *Eur. Phys. J.* **C76** (2016), no. 3, 105, [arXiv:1512.06007](#).

- [100] T. Boettcher, P. Ilten, and M. Williams, “Direct probe of the intrinsic charm content of the proton”, *Phys. Rev. D* **93** (2016), no. 7, 074008, [arXiv:1512.06666](#).
- [101] A. V. Lipatov, G. I. Lykasov, Y. Y. Stepanenko, and V. A. Bednyakov, “Probing proton intrinsic charm in photon or Z boson production accompanied by heavy jets at LHC”, [arXiv:1606.04882](#).
- [102] L. Pasquali, M. H. Reno, and I. Sarcevic, “Secondary decays in atmospheric charm contributions to the flux of muons and muon neutrinos”, *Astropart. Phys.* **9** (1998) 193–202, [arXiv:hep-ph/9710363](#).
- [103] L. Pasquali and M. H. Reno, “Tau-neutrino fluxes from atmospheric charm”, *Phys. Rev. D* **59** (1999) 093003, [arXiv:hep-ph/9811268](#).
- [104] T. K. Gaisser, “Spectrum of cosmic-ray nucleons, kaon production, and the atmospheric muon charge ratio”, *Astropart. Phys.* **35** (2012) 801–806, [arXiv:1111.6675](#).
- [105] T. K. Gaisser, T. Stanev, and S. Tilav, “Cosmic Ray Energy Spectrum from Measurements of Air Showers”, *Front. Phys. China* **8** (2013) 748–758, [arXiv:1303.3565](#).
- [106] T. Stanev, T. K. Gaisser, and S. Tilav, “High energy cosmic rays: sources and fluxes”, *Nucl. Instrum. Meth.* **A742** (2014) 42–46.
- [107] T. K. Gaisser, “Cosmic rays and particle physics”, 1990.
- [108] P. Lipari, “Lepton spectra in the earth’s atmosphere”, *Astropart. Phys.* **1** (1993) 195–227.
- [109] N. N. Kalmykov and S. S. Ostapchenko, “The Nucleus-nucleus interaction, nuclear fragmentation, and fluctuations of extensive air showers”, *Phys. Atom. Nucl.* **56** (1993) 346–353, [*Yad. Fiz.*56N3,105(1993)].
- [110] **IceCube** Collaboration, M. G. Aartsen *et al.*, “Measurement of the Atmospheric  $\nu_e$  Spectrum with IceCube”, *Phys. Rev. D* **91** (2015) 122004, [arXiv:1504.03753](#).
- [111] T. J. Hobbs, J. T. Londergan, and W. Melnitchouk, “Phenomenology of nonperturbative charm in the nucleon”, *Phys. Rev. D* **89** (2014), no. 7, 074008, [arXiv:1311.1578](#).
- [112] T. Gutierrez and R. Vogt, “Leading charm in hadron nucleus interactions in the intrinsic charm model”, *Nucl. Phys.* **B539** (1999) 189–214, [arXiv:hep-ph/9808213](#).
- [113] **SELEX** Collaboration, A. Blanco-Covarrubias *et al.*, “Nuclear Dependence of Charm Production”, *Eur. Phys. J.* **C64** (2009) 637–644, [arXiv:0902.0355](#).
- [114] G. Antchev *et al.*, “First measurement of the total proton-proton cross section at the LHC energy of  $\sqrt{s} = 7$  TeV”, *Europhys. Lett.* **96** (2011) 21002, [arXiv:1110.1395](#).
- [115] S. Dulat, T.-J. Hou, J. Gao, J. Huston, J. Pumplin, C. Schmidt, D. Stump, and C. P. Yuan, “Intrinsic Charm Parton Distribution Functions from CTEQ-TEA Global Analysis”, *Phys. Rev. D* **89** (2014), no. 7, 073004, [arXiv:1309.0025](#).
- [116] **NNPDF** Collaboration, R. D. Ball, V. Bertone, M. Bonvini, S. Carrazza, S. Forte, A. Guffanti, N. P. Hartland, J. Rojo, and L. Rottoli, “A Determination of the Charm Content of the Proton”, [arXiv:1605.06515](#).
- [117] S. Schonert, T. K. Gaisser, E. Resconi, and O. Schulz, “Vetoing atmospheric neutrinos in a high energy neutrino telescope”, *Phys. Rev. D* **79** (2009) 043009, [arXiv:0812.4308](#).
- [118] T. K. Gaisser, K. Jero, A. Karle, and J. van Santen, “Generalized self-veto probability for atmospheric neutrinos”, *Phys. Rev. D* **90** (2014), no. 2, 023009, [arXiv:1405.0525](#).