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Probing Squeezed Bino-Slepton Spectra with the Large Hadron Collider

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Abstract

We consider a Minimal Supersymmetric Standard Model scenario in which the only light superparticles are a bino-like dark matter candidate and a nearly-degenerate slepton. It is notoriously difficult to probe this scenario at the Large Hadron Collider, because the slepton pair-production process yields a final state with soft leptons and small missing transverse energy. We study this scenario in the region of parameter space where the mass difference between the lightest neutralino and the lightest slepton (Δm) is ≤ 60 GeV, focusing on the process in which an additional radiated jet provides a transverse boost to the slepton pair. We then utilize the angular separation of the leptons from each other and from the missing transverse energy, as well as the angular separation between the jet and the missing transverse energy, to distinguish signal from background events. We also use the reconstructed ditau mass, the $\cos \theta^*_{\ell_1 \ell_2}$ variable, and for larger Δm , a lower bound on the lepton p_T . These cuts can dramatically improve both signal sensitivity and the signal-to-background ratio, permitting discovery at the Large Hadron Collider with reasonable integrated luminosity over the interesting region of parameter space. Using our search strategy the LHC will be able to exclude $m_{\tilde{\mu}} \approx 200$ GeV for $\Delta m \leq 60$ GeV at $1.5 - 3\sigma$ with 1000 fb⁻¹ of integrated luminosity. Although we focus on a particular model, the results generalize to a variety of scenarios in which the dark matter and a leptonic partner are nearly degenerate in mass, and especially to scenarios featuring a scalar mediator.

1. INTRODUCTION

A well-studied scenario for physics beyond the Standard Model (SM) is one in which there is a new spin-0 particle $(\tilde{\ell})$ with the same Standard Model gauge quantum numbers as a lepton, and a spin-1/2 dark matter particle (χ) which is a Standard Model singlet. This scenario arises in a variety of specific models of new physics, including the MSSM, in the case where the lightest neutralino is bino-like; in this case, $\tilde{\ell}$ is a slepton and χ is the bino. This scenario has thus been the subject of intense study at the Large Hadron Collider (LHC).

The standard LHC strategy for probing this scenario is to search for $\tilde{\ell}^* \tilde{\ell}$ pair-production, with each $\tilde{\ell}$ decaying promptly to χ and a Standard Model lepton (ℓ). This process yields a distinctive signature: two opposite-sign leptons and missing transverse energy. But this strategy tends to fail in the region of parameter space where $\tilde{\ell}$ and χ are nearly mass-degenerate ($\Delta m \equiv m_{\tilde{\ell}} - m_{\chi} \lesssim$ 60 GeV) [1, 2], because (i) the $\tilde{\ell}$ are typically produced with relatively small momenta, implying that the lepton momenta and the missing transverse energy are small in the nearly-degenerate limit, and (ii) processes with equivalent final state topology, i.e. $\bar{t}t$ and V, VV + jets (where V is an electroweak gauge boson), become a major source of background since the leptons arising from W, Z-decays have p_T of around 40 GeV.

The ATLAS collaboration has searched [3] for electroweak production of sleptons with decay to neutralino plus lepton at the LHC13 ($\mathcal{L} = 36.1 \text{ fb}^{-1}$) in the zero-jet dilepton final state. Slepton masses up to 500 GeV are excluded, if one assumes a massless neutralino. However, this search is generally insensitive to the narrow mass splitting $\Delta m \leq 60$ GeV regime. CMS has searched [4] for soft opposite-sign leptons at 13 TeV with $\mathcal{L} = 35.9 \text{ fb}^{-1}$, focusing on the pair-production of charginos and neutralinos χ_1^{\pm}, χ_2^0 with nearly degenerate mass. This study excludes the parameter space up to around 230 GeV, for mass gaps from the lightest neutralino as small as 20 GeV, but no slepton limits are inferred.

Attempts were made to understand this nearly degenerate region for $\Delta m \leq 20$ GeV, utilizing the Vector Boson Fusion topology [5] and monojet plus dileptons [6, 7], and it was found that an upper bound on the lepton transverse momentum ($p_T < 30 \text{ GeV}$) is useful for investigating this region at the LHC. Ref. [6] also made substantial use of the kinematic variable M_{T2} , which sets an upper bound on the mass of pair-produced parent particles that decay into the two visible systems (after making a specific hypothesis for the mass of the associated invisible species). The presence of the jets in both search strategies gives a transverse boost to the $\tilde{\ell}^* \tilde{\ell}$ system, which increases the lepton momenta and the missing transverse energy in order to reduce the SM background. However, none of these search strategies work for $\Delta m \sim 25 - 60 \,\text{GeV}$, due to the aforementioned background W, Z decay processes.

In this work, we consider supplementary strategies for probing this nearly degenerate region of parameter space utilizing searches for a single jet, in addition to the opposite-sign dilepton and missing transverse momentum. We show that the VV background can be reduced significantly, and the signal to background ratio elevated, through additional cuts based on the angular distribution of the leptons and \not{E}_T and the azimuthal angular separation between the jet and the \not{E}_T . These new selection processes allow us to provide an alternative complementary formulation for the investigation of the very low mass splitting regime ($\Delta m \sim 10$ GeV), and also to cope with slightly larger splittings, up to about 60 GeV. We will show that models with $\Delta m \leq 60$ GeV can be probed at $4 - 9\sigma$ confidence with reasonable luminosity (around 300 fb⁻¹) at the LHC for smuon masses around 110 GeV, and will further estimate the efficacy of our analysis for benchmarks with heavier smuons.

The nearly-degenerate region of parameter space has been of great interest due to the novel early Universe cosmology which is possible for such models. For example, if there are non-minimal flavor-violating couplings and if $m_{\chi} \sim m_{\tilde{\ell}} \sim \mathcal{O}(100)$ GeV, then dark matter annihilation $(\chi\chi \to \bar{\ell}\ell)$ through the *t*-channel exchange of $\tilde{\ell}$ can deplete the dark matter relic density enough to achieve consistency with observation [8, 9]. If Δm is sufficiently small (≤ 60 GeV), then both χ and $\tilde{\ell}$ may be abundant at the time of dark matter freeze-out, and co-annihilation may also be important for depleting the dark matter relic density [10, 11]. It is thus quite interesting to develop collider tools for probing this region of parameter space.

The structure of this paper is as follows. In section 2, we describe the underlying strategy for searching for models with a nearly degenerate bino-slepton pair. In section 3, we describe the optimization of selection cuts for different mass-splitting scenarios, and determine the signal significance and signal-to-background ratio the LHC could provide, for a variety of benchmark choices. We conclude in section 4 with a discussion of our results.

2. STRATEGY

We consider a simplified scenario in which the only light sparticles are a single slepton $(\tilde{\ell})$ and a bino (χ) , and the only allowed decay for the slepton is $\tilde{\ell} \to \chi \ell$. Although we have described this scenario in the language of the MSSM, the same scenario arises in a variety of models for new physics (including, for example, WIMPless dark matter [12–15]). The standard strategy for probing this scenario at the LHC is to search for the process $\bar{q}q \rightarrow \gamma^*/Z^* \rightarrow \tilde{\ell}^* \tilde{\ell} \rightarrow \chi \chi \bar{\ell} \ell$. The signature for this process is the production of a same-flavor, oppositesign dilepton pair, accompanied by missing transverse energy $(\not\!\!E_T)$. But for most signal events, the $\tilde{\ell}^* \tilde{\ell}$ pair are produced with negligible transverse boost. If $\Delta m = m_{\tilde{\ell}} - m_{\chi}$ is small, then the χ produced by $\tilde{\ell}/\tilde{\ell}^*$ decay is non-relativistic and the missing transverse energy is small; in this case, the signal is indistinguishable from the large background arising from the Drell-Yan process $\bar{q}q \rightarrow \gamma^*/Z^* \rightarrow \bar{\ell}\ell$. As a result, this LHC search strategy is largely insensitive for $\Delta m \leq 60$ GeV.

To probe this region of parameter space, we will instead focus on the process $gq(\bar{q}q) \rightarrow j\gamma^*/Z^* \rightarrow j\tilde{\ell}^*\tilde{\ell} \rightarrow j\chi\chi\bar{\ell}\ell$, wherein a single additional hard jet is emitted by one of the initial gluon or quarks of the hard process. The emission of a hard jet gives a large transverse boost to the $\tilde{\ell}^*\tilde{\ell}$ system; the decay products of this system are now collimated, and the $\chi\chi$ pair can have a significant transverse momentum which appears as \not{E}_T [4, 16].

2.1. Leading Backgrounds and Primary Event Selections

The dominant SM background processes are:

•
$$pp \to jZ \to j\bar{\tau}\tau \to j\bar{\ell}\ell\bar{\nu}\nu\bar{\nu}_{\tau}\nu_{\tau}$$

•
$$pp \to \bar{t}t(j) \to \bar{b}W^- bW^+(j) \to \bar{b}b\bar{\ell}\ell\bar{\nu}\nu(j)$$

•
$$pp \to jZZ/jW^+W^- \to j\bar{\ell}\ell\bar{\nu}\nu, j\bar{\ell}\ell\bar{\tau}\tau (\to \bar{\ell}\ell\bar{\nu}\nu + \text{jets})$$

where in all cases, the missing transverse energy arises from the neutrinos.

Since the background processes will contribute equally to dimuon and dielectron final states, whereas the signal may be distinguished based upon the identity of the slepton, we opt here to consider $\ell = \mu$ and $\tilde{\ell} = \tilde{\mu}$ (smuon)¹. The electron and selectron scenario will be essentially identical, with some differences emerging at the detector level. The muon has certain advantages in identification, associated with secondary observation in the dedicated exterior detector systems. Since the decay of WWjj to opposite-sign dileptons is expected to produce $(e^+e^- : \mu^+\mu^- : e^{\pm}\mu^{\mp})$ in the ratio (1 : 1 : 2), an interesting parallel strategy involves leveraging the differential measurement of pure and/or mixed flavor dileptons, as well as associated differential kinematic distributions, in order to estimate and control background [17]; however, we will not pursue this possibility further in the current work. The minimal muon transverse momentum is identified in

¹ In particular, we will assume $\tilde{\ell} = \tilde{\mu}_L$, although this choice will have little effect on cut selection.

our default efficiency formula as 10 GeV, although we will subsequently investigate the relaxation of that parameter. For specificity, we consider $m_{\tilde{\mu}} = 110$ GeV for the main analysis, but likewise subsequently investigate the reach of our analysis with heavier smuon masses. Correspondingly, our main analysis will focus on six benchmark scenarios, variously with neutralino masses of $m_{\chi} =$ 50, 60, 70, 80, 90, and 100 GeV.

We will define "primary" cuts as those which are imposed prior to the analysis, for the purpose of fundamentally characterizing the targeted dimuon plus boosted ISR jet event topology. We take a lead at this level from Refs. [6, 7] and [17], which draw in turn from Ref. [18]. In addition to requiring an opposite-sign dimuon pair, we require one and only one jet with $P_T^{j1} > 30$ GeV, and enforce a nominal lower bound on missing transverse energy of $\not E_T > 30$ GeV (hardness of the single jet and the missing momentum will both be substantially escalated at the stage of secondary optimization). We also veto on *b*-tagged jets and tagged hadronically decaying taus, which are reconstructed at detector level. These last cuts significantly reduce the background from $pp \rightarrow \bar{t}t$ and from SM processes in which τ s decay hadronically. These cuts are summarized in Table I, along with the residual effective LHC14 cross sections for the $\bar{t}t$ +Jets, $\tau\tau$ +Jets, Z+Jets, and VV+Jets background components, as well as each of the six signal benchmark models. In what follows, all event shape distributions will be shown after the imposition of these primary cuts.

TABLE I: Jet matched production and residual effective cross sections (fb) at the LHC14 are tabulated for the $\bar{t}t$ +Jets, $\tau\tau$ +Jets, Z+Jets, and VV+Jets backgrounds, as well as the six signal benchmarks S_{Δ}^{110} , with $m_{\tilde{\mu}} = 110$ GeV, and $m_{\chi} = (110 - \Delta)$ GeV. These primary cuts are related to the targeted dilepton plus boosted ISR jet event topology and are applied to all events.

Selection	$tar{t}jj$	au au j j	Z_{jjjj}	ZZjj	WZjj	WWjj	S_{10}^{110}	S_{20}^{110}	S_{30}^{110}	S^{110}_{40}	S_{50}^{110}	S_{60}^{110}
Matched Production	6.1×10^5	5.6×10^4	5.2×10^7	1.3×10^4	4.2×10^4	9.5×10^4	1.9×10^2	1.9×10^2	1.9×10^2	1.9×10^2	1.9×10^2	1.9×10^2
au-veto	5.4×10^5	3.0×10^4	5.1×10^7	1.2×10^4	4.0×10^4	8.9×10^4	1.9×10^2					
OSSF muon	3.5×10^3	4.3×10^2	6.0×10^5	3.2×10^2	5.8×10^2	5.1×10^2	3.9×10^1	6.8×10^1	8.1×10^1	8.8×10^1	8.9×10^1	9.1×10^1
exactly 1 J $P_T > 30$	6.6×10^2	2.6×10^2	7.1×10^4	9.4×10^1	1.5×10^2	1.1×10^2	7.6×10^0	1.3×10^1	1.6×10^1	1.7×10^1	1.7×10^1	1.8×10^1
Jet <i>b</i> -veto	1.9×10^2	2.5×10^2	7.0×10^4	8.0×10^1	1.4×10^2	1.1×10^2	7.5×10^0	1.3×10^1	1.6×10^1	1.7×10^1	1.7×10^1	1.8×10^1
$E_T > 30 \text{ GeV}$	1.6×10^2	1.8×10^2	8.9×10^3	3.3×10^1	6.6×10^1	9.2×10^1	6.3×10^0	1.0×10^1	1.3×10^1	1.4×10^1	1.5×10^1	1.6×10^1

For simulation of the signal and backgrounds events, we use MADGRAPH5 v2.3.3 [19] with the NNPDF23 LO [20] parton distribution function. We pass our simulated events to PYTHIA v6.4 [21] for showering and hadronization, and subsequently to DELPHES v3.3 3 [22] for detector simulation. All the signal samples, plus ditop, ditau, and diboson processes are simulated inclusively with up to two partons, while single vector backgrounds are generated including up to four partons. The MLM scheme [23] for jet-parton matching has been employed to avoid double counting. All computations are performed at tree-level, with no K-factors included. Using PROSPINO 2 [24], we estimate an NLO K-factor of about 1.3 for the 110 GeV signal model, which compares to around 1.3 [25] and 1.7 for the sub-leading and leading (after all cuts) $t\bar{t}$ and W^+W^- backgrounds, respectively. This does not substantially affect projected significances ($\sqrt{1.7} \simeq 1.3$). The DELPHES 3 detector simulation employs a standard LHC-appropriate parameter card, with jet clustering performed using the anti-kt algorithm. The b-tagging efficiency is just above 70% for transverse momenta between about 65 and 200 GeV, with a mistag rate that climbs from about a quarter to a third of a percent over this same energy range. The τ -tagging efficiency is 60%, with a mistag rate of 1%. Selection cuts and computation of collider observables are implemented in the package AEA-CUS 3.24 [26], and all plots are generated in the companion package RHADAMANTHUS 1.6 [26]. While the LHC is currently running at 13 TeV, the larger portion of future integrated statistics are expected to be collected at an energy of 14 TeV. Since the processes being studied are of much lower energy than the beam scale, we do not expect our conclusions to be largely impacted by modifications to the parton distribution and production cross sections between 13 and 14 TeV. For example, event yield for the W^+W^- background changes by about 10%.

Following application of the primary topology cuts (Table I), we choose higher level cuts which are guided by 1) the desire to increase the signal-to-background ratio, in order to ensure that any putative excess is robust against systematic uncertainties, and 2) ensuring that one can obtain good statistical significance with a reasonable integrated luminosity (around 300 fb⁻¹) at the LHC. We have observed that the former metric often provides a much more incisive visual guide to the application of cuts in the current context. Our selections have been guided at each step by iterative analysis of cut thresholds in S/(1+B), $S/\sqrt{1+B}$, and S.

2.2. Kinematic Reconstruction and Secondary Event Selections

We will define "secondary" event selections as those that are globally beneficial to all of the targeted mass splittings $\Delta m = 10 - 60$ GeV, but which go beyond a basic characterization of the topology and are enforced in the course of a detailed analysis. A variety of such cuts can be used to reduce the remaining background, and we will discuss first those involving Z-bosons. At the outset, the process $pp \rightarrow jZZ$, where one Z decays to $\bar{\ell}\ell$ and the other decays to $\bar{\nu}\nu$, can be significantly reduced by rejecting events where the dilepton invariant mass $m_{\ell\ell}$ is close to m_Z , as

illustrated in the left panel of FIG. 1. The process $pp \to jZ$, where the Z decays to $\bar{\tau}\tau$ and the τ s decay leptonically, can be similarly suppressed by a ditau mass cut [6, 17], as illustrated in the right panel of FIG. 1.



FIG. 1: Signal and background event shapes after primary cuts are compared for (left) the visible dilepton mass $m_{\ell\ell}$, and (right) the signed ditau mass $m_{\tau\tau} \equiv \text{sign} [m_{\tau\tau}^2] \times \sqrt{|m_{\tau\tau}^2|}$. The visible dilepton mass reconstruction exhibits a characteristic peak around the Z-boson mass for the vector backgrounds. $m_{\tau\tau}$ is systematically more positive for all signal regions (especially those with narrow mass splitting) than for the diboson and ditop backgrounds. Note the ancillary benefits of a lower-bound cut on $m_{\tau\tau}$ to controlling backgrounds beyond just its namesake target.

To formulate the ditau mass variable, first proposed in Ref. [27], one assumes that the entire missing transverse energy of the process arises from two neutrino pairs, where each pair was emitted collinear with each of the observed leptons and arises (along with the lepton) from the decay of a highly boosted τ . Momentum conservation in the transverse plane is then sufficient to reconstruct the energy of each neutrino pair, which in turn determines the momentum of each putative τ and allows one to reconstruct $m_{\tau\tau}$, the invariant mass of the putative τ pair. In particular, the ditau invariant mass-square may be expressed in closed form as

$$m_{\tau\tau}^2 \equiv -m_{\ell_1\ell_2}^2 \frac{(\overrightarrow{P}_T^{\ell_1} \times \overrightarrow{P}_T^j) \cdot (\overrightarrow{P}_T^{\ell_2} \times \overrightarrow{P}_T^j)}{|\overrightarrow{P}_T^{\ell_1} \times \overrightarrow{P}_T^{\ell_2}|^2},\tag{1}$$

where $m_{\ell_1\ell_2}^2$ is the invariant squared mass of the lepton system, and $\overrightarrow{P}_T^{\ell_1,\ell_2,j}$ are the transverse momenta of the leading lepton, subleading lepton, and jet, respectively. If the leptons and missing momentum arise from the decay of a heavy particle X with mass M_X to $\bar{\tau}\tau$, with each boosted τ decaying leptonically to a collimated system of a lepton and two neutrinos, then one will find that $m_{\tau\tau}^2 = M_X^2$.² The $pp \to jZ \to j\bar{\tau}\tau$ background can thus be removed by a cut on $m_{\tau\tau}$. Note

² This is easy to verify. If $\overrightarrow{P}^{\tau_i} = (1+\zeta_i)\overrightarrow{P}^{\ell_i}$, where ζ_i represent the invisible neutrino momentum fraction, then

that $m_{\tau\tau}^2 > 0$ if either $-\overrightarrow{P}_T^j$ or \overrightarrow{P}_T^j lies between $\overrightarrow{P}_T^{\ell_1}$ and $\overrightarrow{P}_T^{\ell_2}$, and is negative if neither do. This makes it additionally a good kinematic variable for more generally distinguishing event topology, in addition to rejecting events that literally involve the process $Z \to \overline{\tau}\tau \to \overline{\ell}\ell + 4\nu$. We should point out here that to use the additional discriminatory power of the variable mentioned above, we used $m_{\tau\tau} \equiv \text{sign} [m_{\tau\tau}^2] \times \sqrt{|m_{\tau\tau}^2|}$ in our analysis as shown in the right panel of FIG. 1. This gave our variable a real mass dimension. We checked that the discriminatory power of our redefined variable is the same as the original statistic $m_{\tau\tau}^2$, since $m_{\tau\tau}^2$ is monotonic.

$$M_X^2 = (1+\zeta_1)(1+\zeta_2)m_{\ell_1\ell_2}^2. \text{ If } \overrightarrow{P}_X = -\overrightarrow{P}_j = \overrightarrow{P}^{\tau_1} + \overrightarrow{P}^{\tau_2}, \text{ then}$$

$$m_{\tau\tau}^2 \equiv -m_{\ell_1\ell_2}^2(1+\zeta_1)(1+\zeta_2)\frac{(\overrightarrow{P}_T^{\tau_1} \times \overrightarrow{P}_T^j) \cdot (\overrightarrow{P}_T^{\tau_2} \times \overrightarrow{P}_T^j)}{|\overrightarrow{P}_T^{\tau_1} \times \overrightarrow{P}_T^{\tau_2}|^2} = m_{\ell_1\ell_2}^2(1+\zeta_1)(1+\zeta_2), \tag{2}$$

where we have used the fact that, if $\overrightarrow{A} + \overrightarrow{B} = \overrightarrow{C}$, then $\overrightarrow{A} \times \overrightarrow{C} = \overrightarrow{A} \times \overrightarrow{B} = -\overrightarrow{B} \times \overrightarrow{C}$.



FIG. 2: A two-dimensional comparison of the variables $\cos \theta^*_{\ell_1 \ell_2}$ vs. $\Delta \phi(\ell_1, \ell_2)$ for mass gaps $\Delta m = (10 - 60)$ GeV suggests a reasonably consistent region (green) of parameter space in which background is suppressed relative to signal, although the discrimination power is diffused with increasing mass gap. The function $(4/\pi) \times \tan^{-1} \left[\frac{S_i \Sigma B_i}{B_i \Sigma S_i} \right] - 1$ of the fractional (normalized) cell-wise signal-to-background ratio is selected as a mapping of $\{0, \infty\} \to \{-1, +1\}$ that is antisymmetric under the exchange $(S \leftrightarrow B)$.

One of the most difficult backgrounds to control when searching for the targeted range of models is the topologically identical WWj process. Suitable available handles for this discrimination are differences in the spin of the decaying parent, i.e. spin-0 for the smuon vs. spin-1 for the W, and the mass of the invisible daughter, i.e. up to 100 GeV for the neutralino vs. an essentially massless neutrino. One tool that is effective for leveraging the first difference is the $\cos \theta^*_{\ell_1 \ell_2}$ variable, which was introduced in Ref. [28], and applied in Ref. [29] to distinguishing slepton pair-production via Drell-Yan from other processes that could also yield a lepton pair and missing transverse energy. It works on the principles that the angular distribution of intermediary particles with respect to the beam axis in the parton center-of-mass frame is determined by their spin, and that the lepton angular distribution should reflect this heritage. Much of the practical utility of the $\cos \theta_{\ell_1 \ell_2}^*$ variable hinges upon its resiliency against longitudinal boosts of the partonic system. This feature is apparent in the definition $\cos \theta_{\ell_1 \ell_2}^* \equiv \tanh (\Delta \eta_{\ell_1 \ell_2}/2)$, where $\Delta \eta_{\ell_1 \ell_2}$ is the pseudorapidity difference between the two leptons, which is longitudinal boost-invariant. $\cos \theta_{\ell_1 \ell_2}^*$ takes on a rather simpler geometric interpretation in the frame where the pseudorapidities of the leptons are equal and opposite, corresponding there to the cosine of the matched polar angle between each lepton and the beam axis. The W-boson associated backgrounds have a distribution in this variable that is almost flat up to a value around 0.8, whereas distributions for the scalar-mediated signal models more sharply peak at zero, suggesting a clear region of preference, as visible in FIGs. 2. Although transverse boosts resulting from the ISR jet and from increasing Δm will tend to smear out the described distribution, $\cos \theta_{\ell_1 \ell_2}^*$ remains an effective tool for distinguishing signal events involving a spin-0 intermediary from background.

Missing transverse energy and jet momentum provide a way of robustly distinguishing signal events from the $\bar{t}t$ background. $\bar{t}t$ events will only survive the primary cuts if both *b*-jets are misidentified and at least one has small transverse momentum (since the primary cuts reject events with a *b*-jet or with more than one hard jet). But, in this case, the remaining *b*-jet, as well as the leptons and neutrinos, will tend to have $p_T \leq \mathcal{O}(m_t)$; such events can be removed by demanding large $\not{\!\!E}_T$ and P_T^j .

The optimized values of our secondary cuts are summarized in Table II, along with the associated cut flow for signal and background components in terms of the residual cross section. After the primary cuts, the single vector W+Jets background (not tabulated) is fully suppressed. Following the secondary cuts, the Z+Jets background is likewise controlled, and the signal-to-background ratio is roughly (1:3) and (1:2) for the WWjj and $t\bar{t}jj$ components respectively, or roughly (3:1) and (45:1) for the WZjj and ZZjj components respectively. The ditau background component has a signal-to-background ratio of approximately (1:1) at this stage of the event selection; despite the fact that it has not been fully controlled by the $m_{\tau\tau} > 125$ GeV cut, we will show that it does not play a significant role after subsequent the third-level cuts.

TABLE II: Residual effective cross sections (fb) at the LHC14 are tabulated for the $\bar{t}t$ +Jets, $\tau\tau$ +Jets, Z+Jets, and VV+Jets backgrounds, as well as the six signal benchmarks. Secondary cuts at this level are applied to all events.

Selection	$t\bar{t}jj$	$\tau \tau j j$	Z j j j j	ZZjj	WZjj	WWjj	S_{10}^{110}	S_{20}^{110}	S_{30}^{110}	S_{40}^{110}	S_{50}^{110}	S_{60}^{110}
$m_{\ell\ell} \notin M_Z \pm 10 { m ~GeV}$	1.4×10^2	1.8×10^2	6.2×10^2	2.0×10^0	1.0×10^1	7.9×10^1	6.0×10^{0}	9.2×10^0	1.1×10^1	1.2×10^1	1.3×10^1	1.4×10^1
$\cos\theta^*_{\ell_1,\ell_2} < 0.5$	8.1×10^1	1.6×10^2	4.7×10^2	1.4×10^0	6.7×10^0	4.5×10^1	4.8×10^0	6.9×10^0	8.0×10^0	9.0×10^0	9.5×10^0	1.0×10^1
$m_{\tau\tau} > 125 { m ~GeV}$	2.7×10^1	2.3×10^1	8.7×10^1	3.0×10^{-1}	1.4×10^0	1.4×10^1	3.0×10^0	3.4×10^0	3.6×10^0	3.9×10^0	4.1×10^0	4.3×10^0
$\not\!$	2.9×10^0	6.6×10^{-1}	0	1.5×10^{-2}	2.2×10^{-1}	2.3×10^0	5.1×10^{-1}	5.8×10^{-1}	6.6×10^{-1}	7.1×10^{-1}	7.9×10^{-1}	8.9×10^{-1}
Jet $P_T > 125~{\rm GeV}$	1.1×10^0	6.6×10^{-1}	0	1.1×10^{-2}	1.9×10^{-1}	1.7×10^0	4.9×10^{-1}	5.2×10^{-1}	5.2×10^{-1}	4.6×10^{-1}	4.5×10^{-1}	4.5×10^{-1}

2.3. Angular Distributions and Tertiary Event Selections

We will define "tertiary" event selections as those whose impact is differentially correlated with the specific value of the mass splitting Δm . The remaining backgrounds at this stage of the flow are dominated by $t\bar{t}(j)$, $\tau\tau j$, and WWj production. To further distinguish signal events from SM background, one must contrast the energy and angular distribution of the leptons and invisible particles arising from signal events with those arising from background events. Several types of kinematic variables are useful here:

- The relative strengths of the missing transverse energy $\not\!\!\!E_T$ and the jet momentum P_T^j .
- The angle $\Delta \phi(\not\!\!\!E_T, j)$ between the leading jet and the missing transverse energy. This variable and that prior are very useful to identifying the small mass gap scenarios. See FIG. 3.
- The angle $\Delta \phi(\not\!\!\!E_T, \ell_{1,2})$ between either lepton and the missing transverse energy. These variables measure the collimation of the lepton plus invisible system, and demanding smaller values of this angle favors slepton signal events over $\bar{t}t(j)$ background events. See FIG. 3.
- $P_T^{\ell_2}$, the transverse momentum of the sub-leading lepton. This variable measures the hardness of the lepton plus invisible system; demanding a larger value benefits processes with larger mass gaps. Note that a lower bound on this variable implicitly includes a similar bound on the leading lepton. See FIG. 4.

• The angle $\Delta \phi(\ell_1, \ell_2)$ between the leading lepton and the subleading lepton, which is related to the topology and inherited boost of decays into the leptonic system. Demanding larger values of this angle favors processes with heavier parents. See FIGs. 2, 4.



FIG. 3: Signal and background event shapes after primary cuts (discussed in Table I) are compared for the azimuthal angular separation between the missing transverse energy and (left) the leading jet $\Delta \phi(\not\!\!\!E_T, j)$ or (right) the leading lepton $\Delta \phi(\not\!\!\!E_T, \ell_1)$. The leading lepton is systematically more aligned with the $\not\!\!\!E_T$ for signal regions with narrow mass splitting than for background. This statistic can behave favorably as an upper bound for the lighter mass gaps and as a lower bound for the heavier mass gaps. The leading jet is systematically more anti-aligned with the $\not\!\!\!E_T$ for signal regions with narrow mass splitting than for background.



FIG. 4: Signal and background event shapes after primary cuts (discussed in Table I) are compared for (left) the minimal leptonic transverse momentum $P_T^{\ell_2}$ and (right) the azimuthal angular separation between the visible dilepton pair $\Delta \phi(\ell_1, \ell_2)$. The value of $P_T^{\ell_2}$ for models with a mass gap $\Delta m \simeq 30$ GeV closely mimics the background from SM vector decays, whereas smaller mass gaps lead to a softer leptonic system, and vice versa. The dilepton signal pairs are all systematically more widely separated than those arising from SM backgrounds, although the effect becomes more pronounced when the mass splitting is small.

To remove the jWW background, one can utilize the angular distribution of the leptons. For

this purpose, it is convenient to consider the center-of-mass frame for the system consisting of all particles except the hard jet (the unboosted system). For this system, both signal and background processes consist of the production of two intermediary particles ($\tilde{\ell}^* \tilde{\ell}$ and $W^+ W^-$, respectively), followed by the decay of each intermediary to a lepton and an invisible particle (χ and ν , respectively). In both cases, the leptons will tend to be anti-collimated; if the intermediaries are produced at threshold then the lepton distribution will tend to be isotropic, but if the intermediaries are produced with reasonable longitudinal boost (not to be confused with transverse boost coming from hard jets) then their decay products will tend to be collimated with the direction of the parent, yielding leptons which are anti-collimated. The net result will be that the leptons produced from both $\tilde{\ell}^* \tilde{\ell}$ and W^+W^- production processes will be biased towards anti-collimation, in the center-of-mass frame of the unboosted system.

The transverse boost resulting from emission of a jet will tend to smear out these angular distributions. But the heavier the intermediary, the less the distribution will be smeared, since heavier intermediaries acquire a smaller boost from the emission of a jet with fixed momentum. As a result, provided the slepton is heavier than m_W , the leptons arising from $\tilde{\ell}^* \tilde{\ell} j$ production will tend to be more anti-collimated, in the frame of the detector, than the leptons arising from WWjbackgrounds. Moreover, one expects this bias to increase as the sleptons are made heavier.

Conversely, the leading lepton produced from $\tilde{\ell}^* \tilde{\ell} j$ production will tend to be collimated with the missing transverse energy, since both arise from the decay products of a boosted slepton. This correlation can be used to distinguish signal from the $\bar{t}t(j)$ background. The angle between the leading lepton and the missing transverse energy is much more uniform in $\bar{t}t$ background events, since a significant portion of the \not{E}_T in these events arises from mismeasured or missed jets.

Note that one generally expects it to be difficult to trust a determination of missing transverse energy which is either parallel or anti-parallel to a jet, since jet mismeasurement can cause an apparent missing transverse energy along the axis of a jet. But we will always require at least $\not\!\!\!E_T \gtrsim 125 \,\text{GeV}$, and jet mismeasurement is generally a less significant source of uncertainty when the invisible system is harder.

3. FINAL OPTIMIZATION AND RESULTS

In the prior subsection we outlined a set of general considerations governing the selection of tertiary cuts which can distinguish signal from background in the case of a bino-slepton pair with a squeezed spectrum. In this section we provide a detailed application of these cuts differentially to each benchmark mass-splitting ansätz, and subsequently describe our main results.

We remark at this stage that many of the kinematic discriminants considered in the present study exhibit strong correlations, such that multiple semi-equivalent solutions to the optimization puzzle exist in certain cases. Relatedly, the relevant signal vs. background distribution shapes may be altered significantly for the events residual at a certain stage of the flow, as one proceeds successively through the application of cuts. Certain selections which do not visually present a strong discrimination in FIGs. 1–3 at the stage of primary cuts may nevertheless prove to appreciably elevate the signal-to-background ratio, for example, after more cuts have been applied. Finally, given that a certain fraction of the topologically matched WWjj background is (apparently irreducibly) kinematically similar to the signal profile, it becomes beneficial to select relatively soft cuts in certain variables where the signal-to-background resolving power is marginal, in order to emphasize statistical resolution. One might alternatively consider the use of Bayesian optimization techniques, as recently outlined in Ref. [30], for systematic maximization of both the statistical significance and S/B.

The identities and values of these tertiary cuts are detailed in Table III, along with the cross section flow of key event populations, for three scenarios tailored respectively to the narrower, intermediate, and wider mass gap regimes. The intermediate selection scenario provides reasonably balanced performance for all values of Δm , although it is possible to do markedly better for small and large values by a more specialized approach. Also tabulated are the estimated number of signal events (with 300 fb⁻¹ integrated luminosity), signal-to-background ratios, and signal significances after the application of all cuts. We describe each of these three optimizations briefly in the following subsections.

3.1. $\Delta m = 10, 20 \, \text{GeV}$

If Δm is small, ~ 10 GeV, then one finds that the signal lepton plus invisible system tends to be relatively soft, and collimated anti-parallel to the jet momentum, as compared to background events. We emphasize here interesting alternatives to selecting directly for low $p_T^{\ell_{1,2}}$ [6] (although

TABLE III: Residual effective cross sections (fb) after the application of tertiary cuts targeted at smaller, intermediate, and larger mass gaps. Also given are the number of signal events, S/(1+B), and projected significance at 300 fb⁻¹. For each tertiary cut group, the models in the targeted mass gap range are in bold-face.

Selection	$t\bar{t}jj$	au au j j	ZZjj	WZjj	WWjj	S_{10}^{110}	S_{20}^{110}	S_{30}^{110}	S_{40}^{110}	S_{50}^{110}	S_{60}^{110}
Small Mass Gap Optimization											
$1.0 < P_T^j \div \not\!\!\!E_T < 1.3$	4.5×10^{-1}	5.5×10^{-3}	2.7×10^{-3}	6.2×10^{-2}	6.6×10^{-1}	$4.2 imes 10^{-1}$	$3.0 imes10^{-1}$	2.4×10^{-1}	1.8×10^{-1}	1.6×10^{-1}	1.4×10^{-1}
$\Delta \phi(\not\!\!\!E_T,j) \div \pi > 0.95$	1.8×10^{-1}	5.5×10^{-3}	2.2×10^{-3}	2.7×10^{-2}	3.8×10^{-1}	4.0×10^{-1}	$2.3 imes10^{-1}$	1.7×10^{-1}	9.6×10^{-2}	7.7×10^{-2}	6.2×10^{-2}
Events at $\mathcal{L} = 300 \text{ fb}^{-1}$	52.7	1.7	0.7	8.1	113.6	120.0	69.0	51.0	28.8	23.1	18.6
$S \div (1+B)$	-	-	-	-	-	0.68	0.39	0.29	0.16	0.13	0.10
$S \div \sqrt{1+B}$	-	-	-	-	-	9.0	5.2	3.8	2.2	1.7	1.4
Intermediate Mass Gap Optimization											
$\Delta \phi(\ell_1, \ell_2) \div \pi > 0.5$	1.1×10^0	5.5×10^{-3}	7.7×10^{-3}	1.2×10^{-1}	1.3×10^{0}	4.0×10^{-1}	4.0×10^{-1}	4.4×10^{-1}	$4.1 imes 10^{-1}$	3.7×10^{-1}	3.9×10^{-1}
$\Delta \phi(\not\!\!\!E_T,\ell_1) \div \pi < 0.6$	4.8×10^{-1}	5.5×10^{-3}	5.5×10^{-3}	7.9×10^{-2}	9.0×10^{-1}	3.7×10^{-1}	3.3×10^{-1}	$3.3 imes 10^{-1}$	$3.0 imes 10^{-1}$	2.4×10^{-1}	2.1×10^{-1}
$\Delta \phi(\not\!\!\!E_T,\ell_2) \div \pi < 0.6$	1.8×10^{-1}	0.0	4.4×10^{-3}	4.8×10^{-2}	5.1×10^{-1}	2.7×10^{-1}	2.3×10^{-1}	$2.2 imes 10^{-1}$	$2.0 imes10^{-1}$	1.6×10^{-1}	1.4×10^{-1}
Events at $\mathcal{L} = 300 \text{ fb}^{-1}$	52.8	0.0	1.3	14.5	151.7	81.0	69.0	66.0	60.0	48.0	42.0
$S \div (1+B)$	-	-	-	-	-	0.37	0.31	0.30	0.27	0.22	0.19
$S \div \sqrt{1+B}$	-	-	-	-	-	5.4	4.6	4.4	4.0	3.2	2.8
				Larg	e Mass Gap	Optimization					
$\Delta \phi(\not\!\!\!E_T,\ell_1) \div \pi > 0.25$	8.5×10^{-1}	0.0	6.6×10^{-3}	1.0×10^{-1}	9.5×10^{-1}	2.4×10^{-1}	2.7×10^{-1}	3.3×10^{-1}	2.9×10^{-1}	$3.0 imes 10^{-1}$	$3.3 imes10^{-1}$
$P_T^{\ell_2} > 40 \text{ GeV}$	3.4×10^{-1}	0.0	5.6×10^{-4}	3.7×10^{-2}	4.1×10^{-1}	1.1×10^{-2}	7.3×10^{-2}	1.4×10^{-1}	1.5×10^{-1}	$2.1 imes 10^{-1}$	$2.4 imes 10^{-1}$
Events at $\mathcal{L} = 300 \text{ fb}^{-1}$	102.2	0.0	0.2	11.0	124.3	3.3	21.9	42.0	45.0	63.0	72.0
$S \div (1+B)$	-	-	-	-	-	0.01	0.09	0.18	0.19	0.26	0.30
$S \div \sqrt{1+B}$	-	-	-	-	-	0.2	1.4	2.7	2.9	4.1	4.7

3.2. $\Delta m = 30, 40 \, \text{GeV}$

Angular correlation cuts are very useful in this mass gap range to remove the W, Z backgrounds. We turn first to the azimuthal separation $\Delta \phi(\ell_1, \ell_2)$ between the visible leptons. The cut $\Delta \phi(\ell_1, \ell_2)/\pi > 0.5$ is applied first, as motivated in the right panel of FIG. 4, and also FIGs. 2. Next, an upper bound $\Delta \phi(\ell_{1,2}, \not \!\!\!E_T)/\pi < 0.6$ on the angle between the leptons and the missing transverse momentum vector completes the selection, and substantially elevates the signal-to-background ratio, as shown in the left panel of FIG. 5. Overall, the significance after tertiary cuts can be around 4 for luminosity 300 fb⁻¹ and S/B is around 30%.



FIG. 5: Signal-to-background ratios as a function of the final Table III cuts for the intermediate and large mass gap scenarios. The azimuthal angular separation variables, e.g. via an upper bound on $\Delta \phi(\not\!\!\!E_T, \ell_2)$ (left), prove useful for discriminating signal from background in the difficult intermediate mass splitting scenarios, where leptonic transverse momentum magnitude becomes degenerate with that of vector boson decay products. A lower bound on the minimal leptonic $P_T^{\ell_2}$ is useful for discriminating signal from background when the mass gap is larger, and the slepton delivers a correspondingly enhanced boost to its decay products.

3.3. $\Delta m = 50, 60 \,\mathrm{GeV}$

For relatively large Δm , e.g., 50-60 GeV, many of the prior considerations are reversed. As the mass gaps become larger, the lepton plus invisible system becomes harder and less collimated than the background. A better strategy to distinguish these scenarios from the others is to use lower bounds on the angle $\Delta \phi(\ell_1, \not \!\!\!E_T)/\pi > 0.25$ between the leading lepton and the missing transverse momentum vector, and on the leptonic transverse momentum $p_T^{\ell_2} > 40$ GeV (see the right panel of FIG. 5). Note that pushing the $P_T^{\ell_2}$ cut harder, say, to 80 GeV is beneficial for $\Delta m = 60$ GeV, but is costly to the statistical significance for $\Delta m = 50$ GeV. The signal significance after the application of all tertiary cuts can be above 4 for luminosity 300 fb⁻¹ and S/B is above 25%.

3.4. Other Benchmarks

As the smuon mass increases, the smuon production cross section drops. But, this is partially offset by increases in some of the cut efficiencies due to the fact that there is more more $\not E_T$ in the system. In Table IV we show the significance for luminosities of 300, 1000 and 3000 fb⁻¹ for smuon masses up to 300 GeV, and for mass gaps of 10-60 GeV. Most of the benchmarks up to 200 GeV are able to be excluded at or near the 2- σ level, with signal-to-background on the order of 10%. For benchmarks as heavy as 300 GeV, the cross section suppression is too large to overcome. In Table V we examine improvements to the signal yields for small mass splittings when the muon sensitivity is reduced from 10 GeV to 5 GeV. We notice that by reducing the threshold of muon p_T enhances signal yields by 30% for $\Delta m \leq 20$ GeV scenarios.

TABLE IV: Heavier model benchmarks $S_{\Delta m}^{m_{\tilde{\mu}}}$ for the small ($\Delta m = 10, 20 \text{ GeV}$), intermediate ($\Delta m = 30, 40 \text{ GeV}$), and large ($\Delta m = 50, 60 \text{ GeV}$), mass gap tertiary event selection cuts.

Benchmark	S_{10}^{160}	S_{20}^{160}	S_{30}^{160}	S_{40}^{160}	S_{50}^{160}	S_{60}^{160}
Events at $\mathcal{L} = 300 \text{ fb}^{-1}$	42	39	25	28	29	28
$S \div (1+B)$	0.24	0.22	0.11	0.12	0.12	0.12
$S \div \sqrt{1+B}$	3.2	2.9	1.7	1.9	1.9	1.8
Benchmark	S_{10}^{200}	S_{20}^{200}	S_{30}^{200}	S_{40}^{200}	S_{50}^{200}	S_{60}^{200}
Events at $\mathcal{L} = 1000 \text{ fb}^{-1}$	72	67	42	46	53	64
$S \div (1+B)$	0.12	0.11	0.06	0.06	0.07	0.08
$S \div \sqrt{1+B}$	3.0	2.8	1.5	1.7	1.9	2.3
Benchmark	S_{10}^{300}	S_{20}^{300}	S_{30}^{300}	S_{40}^{300}	S_{50}^{300}	S_{60}^{300}
Events at $\mathcal{L} = 3000 \text{ fb}^{-1}$	48	54	33	33	48	60
$S \div (1+B)$	0.03	0.03	0.01	0.01	0.02	0.03
$S \div \sqrt{1+B}$	1.1	1.3	0.7	0.7	1.0	1.2

TABLE V: Scaling of the $m_{\tilde{\mu}} = 110$ GeV benchmark model with reduction of the muon reconstruction p_T
threshold to 5 GeV, assuming small mass gap tertiary event selection cuts.

$5 { m ~GeV}$ muon	S_{10}^{110}	S_{20}^{110}	S_{30}^{110}
Events at $\mathcal{L} = 300 \text{ fb}^{-1}$	153	91	51
Ratio to $P_T^{\mu} > 10 \text{ GeV}$	1.3	1.3	1.0

4. CONCLUSIONS

We have considered strategies for detecting new physics scenarios in which the new light particles are a bino-like LSP and a light slepton with a squeezed spectrum ($\Delta m \leq 60 \,\text{GeV}$). It is well-known that this scenario is difficult to probe, because the squeezed spectrum of new particles implies that both the leptons and missing transverse energy produced through slepton pair production are soft. It is also well-known that one can improve detection prospects for this scenario by requiring the emission of an additional jet, which gives the remaining system a transverse boost; one then searches for a single hard jet, a same-flavor, opposite-sign lepton pair, and missing transverse energy. We study enhancements to this strategy which can improve both signal significance and the signal-to-background ratio, particularly focused on cuts which can distinguish the energy and angular distribution of the signal events from SM background events. One can utilize the angular separation between the jet and the missing transverse energy to distinguish signal from background events.

Focusing on the specific case $m_{\tilde{\mu}} = 110$ GeV, we found that these cuts can be used to achieve a larger signal-to-background ratio in the small mass-splitting regime ($\Delta m = 10, 20$ GeV) than was found in previous analyses using alternative cut strategies, while still maintaining discovery-level signal significance with 300 fb⁻¹ integrated luminosity. We also found selection cuts which allow $4 - 5\sigma$ evidence to be found, with the same luminosity, for Δm as large as 60 GeV. The larger Δm regions can be distinguished by using lower bounds on the p_T of the leptons. These selection cuts remain effective for larger choices of $m_{\tilde{\mu}}$, up to and above $m_{\tilde{\mu}} \simeq 200$ GeV. We found that the LHC can set $\sim 1.5 - 3\sigma$ exclusion limits on $m_{\tilde{\mu}} \approx 200$ GeV, for $\Delta m \lesssim 60$ GeV with 1000 fb⁻¹ of integrated luminosity.

Although we have framed our study in terms of a MSSM scenario with a light bino-slepton

pair, this analysis can be readily adapted to other scenarios in which the LHC can pair-produce a lepton-partner, which then decays to a nearly-degenerate invisible particle and a soft lepton. However, a key feature of our analysis is the use of angular distributions to distinguish slepton production from W^+W^- production, a background which produces distinctive correlations in the outgoing leptons. In a scenario in which the lepton partner were also spin-1 instead of spin-0, one might reevaluate certain aspects of this strategy (in particular, the selection on $\cos \theta^*_{\ell_1 \ell_2}$).

Finally, we note that we have only considered the case in which a bino-like LSP is nearly degenerate with a slepton. There has been great interest in case where the LSP is nearly degenerate with a squark, with much work on LHC strategies for probing this scenario. It would be interesting to determine if any of the strategies we have discussed here could be adapted for that purpose. In a similar vein, it would be interesting to study if ILC searches could provide complimentary probes of scenarios with squeezed bino-slepton spectra.

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