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Resonant Bar Constraints on Macro Dark Matter

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The current standard model of cosmology, Λ CDM, requires dark matter to make up around 25% of the total energy budget of the universe. Yet, quite puzzlingly, there appears to be no candidate particle in the current Standard Model of particle physics. Assuming the validity of the CDM paradigm, dark matter has evaded detection thus far either because it is intrinsically a weakly-interacting substance or because its interactions are suppressed by its high constituent mass and low number density. Most approaches to explain dark matter to date assume the former and therefore require beyond-the-Standard-Model particles that have yet to be observed directly or indirectly. Given the dearth of evidence for this class of candidates it is timely to consider the latter possibility, which allows for candidates that may or may not arise from the Standard Model. In this work we extend a recent study of this general class of so-called *macro dark matter* – candidates with characteristic masses of grams and geometric cross sections of cm^2 . We consider new bounds that can be set using existing data from the resonant bar gravitational wave detectors NAUTILUS and EXPLORER.

I. INTRODUCTION

The last two decades have ushered in a new era of precision cosmology with a plethora of modern experiments and observations all leading to the so called Λ CDM concordance model of the universe. A crucial component of this model is the cold dark matter (CDM) making up around 25% of the total energy density of our universe, as inferred from observations on large scales (see e.g. [1–4]). On intermediate scales its existence is observed indirectly due to the discrepancies between the gravitational and luminous masses of large astrophysical systems. The dark matter cannot be made of ordinary baryonic matter (see e.g. [5, 6], [7], and references therein) nor can it consist of any fundamental particle of the Standard Model of particle physics.

Although a tremendous effort has been devoted to the study of particle candidates that are intrinsically weakly-interacting, such as WIMPs and axions, alternative dark matter candidates deserve increased attention given the lack of direct detection of those canonical possibilities to date (see e.g. [8, 9]). Other candidates can couple to Standard Model particles with high probability but are nevertheless *effectively* weakly-interacting or “dark” because they are very massive, and therefore have a lower number density. Several examples exist in the literature,

most notably nuclear-dense candidates with a Standard Model basis (e.g. [10–12]). Other similarly massive candidates include compact objects with some connection to the Standard Model (e.g. [13–15]), primordial black holes [16], and other candidates that may be found in the literature (e.g. [17–21]).

A wide range of Earth-based constraints on nuclear-dense candidates (nuclearites) were considered in [22] and more recent bounds were presented in [23]. Such constraints are only made for candidates with a fixed internal mass density of roughly $3.5 \times 10^{14} \text{ g/cm}^3$, and therefore they obey the specific cross section-mass relation $\sigma_x \propto M_x^{2/3}$. Recently, however, a model-independent study of the general class of “macroscopic” candidates has been considered in [24]. These macro dark matter candidates, referred to as *Macros*, have characteristic masses and geometric cross sections of grams and cm^2 and *may or may not have a Standard Model origin*. A number of Earth-based, astrophysical, and cosmological observations were used in [24] to place constraints on Macros.

Here we improve upon the constraints found in [24] by extending existing work on nuclearite constraints from resonant bar gravitational wave detectors for application to macro dark matter. The use of large aluminum bars as detectors of gravitational waves has been studied for more than five decades [25], and their sensitivity to cosmic rays has been appreciated for some time [26]. Because of the thermo-acoustic effect and their resonant properties, such aluminum bars are also sensitive (when cryogenically cooled) to other exotic cosmic impactors, such as monopoles [27] and nuclearites [28]. The reso-

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nant bar experiments NAUTILUS [29], which ran from 2003-2012 in Frascati, Italy, and EXPLORER [30], which ran from 2003-2009 at CERN, were recently used to constrain nuclearite dark matter with masses up to $\sim 10^{-4}$ g [31].

Compared to nuclearites, macro dark matter has the added complexity that both the cross section and mass are independent parameters, and both of these determine Macro detectability. Macros of a fixed mass with larger cross sections, for example, will experience more drag and so would arrive at a detector with less energy; they would therefore have a lower probability to reach a detection threshold. Here we expand on the work of [27] and [28], to compute the detectability of macro dark matter as a function of both its cross section and mass. We then use the null results of [31] to constrain a portion of the Macro parameter space and improve on the constraints found in [24] on the elastic scattering cross section of macro dark matter with baryons.

II. MACRO DETECTION VIA RESONANT BAR DETECTORS

A. Macro velocity evolution

Given an incoming Macro galactic velocity, v_0 , its evolution as it impacts the Earth as a function of the reduced cross section, σ_x/M_x , is approximately given by

$$v_x(r) = v_0 e^{-\frac{\sigma_x}{M_x} \langle \rho r \rangle}, \quad (1)$$

where $\langle \rho r \rangle$ is the column density encountered by the Macro. This column density can have three distinct contributions, the first being atmospheric. Simple atmospheric models give an atmospheric density that depends exponentially on altitude:

$$\rho(z) = \rho_0 e^{-z/H}, \quad (2)$$

where z is the altitude above sea level, $\rho_0 \simeq 10^{-3}$ g/cm³, and the scale height, $H \simeq 10$ km. Writing $z = r \cos \theta$, where θ is the impact angle, the column density encountered through the atmosphere is

$$\begin{aligned} \langle \rho r \rangle_{\text{atm}} &= \int_r^\infty dr' \rho \\ &\simeq \frac{\rho_0 H}{\cos \theta} e^{-z/H}. \end{aligned} \quad (3)$$

In addition, we shall conservatively assume that at angles $\theta > \pi/3$ the Macro would encounter an additional column density of 100 meters water equivalent (MWE), or

$$\langle \rho r \rangle_{\text{obst}} = 10^4 \text{ g/cm}^2, \quad (4)$$

due to surrounding structures, mountains, or other obstacles. Lastly, at angles $\theta > \pi/2$ the Macro would pass through the Earth and encounter a column density,

$$\langle \rho r \rangle_{\oplus} = 2R_{\oplus} \rho_{\oplus} |\cos \theta|. \quad (5)$$

B. Thermo-acoustic detection of cosmic particles

Upon its passage through the (identical) NAUTILUS or EXPLORER detectors, a very dense object would deposit energy in a line along its track in the detector. Because the Macro velocity is super-sonic in the aluminum, the energy deposition would be nearly instantaneous. The resulting near-instantaneous thermal expansion would source a pressure wave that would excite the bar's longitudinal vibrational modes. As described in e.g. [27, 28, 31], for a bar of radius R and length L , the energy of the lowest mode is

$$\Delta E = \frac{4}{9\pi} \frac{\gamma^2}{\rho L v_s^2} \left(\frac{dE_x}{dx} \right)^2 G(z_0, l_0, \theta_0), \quad (6)$$

where γ is the Grüneisen parameter, ρ is the bar density, v_s is the longitudinal sound speed, and the energy lost by a nuclearite or, more generally, a Macro is

$$\left| \frac{dE_x}{dx} \right| = \rho \sigma_x v_x^2. \quad (7)$$

The geometric function that depends on the track through the bar is

$$G(z_0, l_0, \theta_0) = \left[\frac{L}{\pi R} \sin\left(\frac{\pi z_0}{L}\right) \frac{\sin\left(\frac{\pi l_0}{2L} \cos \theta_0\right)}{\cos \theta_0} \right]^2, \quad (8)$$

where z_0 is the distance of the track midpoint to one end of the bar, θ_0 is the angle between the track and the bar axis and l_0 is the length of the track. For the bars described in [31], $R = 0.3$ m and $L = 3$ m; the full geometric acceptance is therefore 19.54 m² sr.

C. Application of nuclearite analysis to Macros

In Ref. [31] it is reported that, for the parameters specific to the NAUTILUS and EXPLORER aluminum bars, a vertical impact at the bar center results in an energy deposition (in units of temperature) into the fundamental mode of

$$\Delta E = 10.7 \text{ K} \left(\frac{v_x \xi(M)}{10^{-3} c} \right)^4, \quad (9)$$

where, in our notation, $\xi(M) = (M/1.5 \text{ ng})^{1/3}$ is a function that characterizes the radius of a passing nuclearite as a function of its mass¹.

It is straightforward to apply the analysis in [31] to macro dark matter, considering a nuclearite of mass 1.5 ng would have a cross section, $\sigma_0 \simeq \pi \times 10^{-16}$ cm² at

¹ For an object of constant density $\sigma_x \propto M^{2/3}$, hence from (6) and (7) the $\xi(M)^4$ dependence in (9) can be understood.

the reference density of $3.5 \times 10^{14} \text{ g/cm}^3$. The energy deposition by a Macro can then be readily translated by making the replacement

$$\xi(M)^2 \rightarrow \frac{\sigma_x}{\sigma_0} \quad (10)$$

in (9). We will furthermore use 250 km/s as a reference velocity and reinsert the geometric function, G , writing the excitation energy as

$$\Delta E = 5.2 \text{ K} \left(\frac{v_x}{250 \text{ km/s}} \right)^4 \left(\frac{\sigma_x}{\sigma_0} \right)^2 G(z_0, l_0, \theta_0). \quad (11)$$

Given the detection threshold of 2 K used in [31] and the Macro velocity upon impact given in (1), the fraction of impacts for a given pair of Macro parameters (σ_x, M_x) that exceed this threshold is determined by performing a Monte Carlo simulation over the possible bar impact points and Macro trajectories.

We can, however, give a semi-analytic estimate of the constrained region in the $\sigma_x - M_x$ plane by recognizing that at large σ_x/M_x the only Macros that can make it to the detector with sufficiently high velocity (quantified below) will come from nearly directly overhead. For those impacts $G(z_0, l_0, \theta_0)$ is maximized at unity. The requirement for resonant bar detection is then

$$\left(\frac{v_0}{250 \text{ km/s}} \right)^2 e^{-2 \frac{\sigma_x}{M_x} \langle \rho r \rangle} \left(\frac{\sigma_x}{\sigma_0} \right) \gtrsim 0.62. \quad (12)$$

This inequality is saturated at the critical value $\sigma_{x,c}$, which may be solved implicitly as a function of M_x :

$$\sigma_{x,c} = -\frac{M_x}{2 \langle \rho r \rangle} W(x). \quad (13)$$

Here

$$x \simeq -1.24 \times \langle \rho r \rangle \frac{\sigma_0}{M_x} \left(\frac{v_0}{250 \text{ km/s}} \right)^{-2}, \quad (14)$$

and $W(x)$ is known as the Lambert-W function, defined implicitly by the relation

$$x = W(x) \exp W(x). \quad (15)$$

$W(x)$ has an infinite number of branches, however, the branch $W_{-1}(x)$ delineates the top of the constrained region in the $\sigma_x - M_x$ plane according to (13).

We must also ensure that the Macro velocity exceeds the sound velocity of aluminum, $v_s \simeq 2 \times 10^{-5} c$, otherwise the energy loss rate formula (7) breaks down [31]. From (1) this requires that

$$\begin{aligned} \sigma_x &\lesssim \frac{1}{\langle \rho r \rangle} \log \frac{v_0}{v_s} M_x \\ &\lesssim 3.7 \times 10^{-3} \text{ cm}^2 \left(\frac{M_x}{1 \text{ g}} \right) \end{aligned} \quad (16)$$

where we have used an approximate atmospheric depth² of $\langle \rho r \rangle = 10^3 \text{ g/cm}^2$ and $v_0 = 250 \text{ km/s}$. For masses larger than roughly 10^{-10} g this turns out to be more restrictive than using (13), so it sets the upper edge of the region of constraint in that range.

Lastly, we consider the Macro flux limitation. At large σ_x/M_x , we cannot use the full geometric acceptance of $\simeq 19.54 \text{ m}^2 \text{ sr}$ because of significant additional drag that would be experienced by the Macros during their passage through (i) the environment surrounding the detector (e.g. other buildings, mountains, etc.) and (ii) the integrated depth through the Earth. Likewise, Macros with small σ_x/M_x are more likely to make it to the detector with high enough velocity and energy deposition. Therefore, for the largest σ_x/M_x we use only 1/4 of the geometric acceptance since we can only trust their ability to make it through the atmosphere. For $\sigma_x/M_x \lesssim 10^{-4} \text{ cm}^2/\text{g}$ a Macro could easily pass through surrounding obstacles so that using 1/2 of the full acceptance is justified. Finally, for $\sigma_x/M_x \lesssim (\rho_\oplus R_\oplus)^{-1} \simeq 3 \times 10^{-10} \text{ cm}^2/\text{g}$ the Macro could pass freely through the Earth and in that case we may use the full acceptance. These approximations ignore the detector efficiency as a function of impact trajectory, however this is taken into account in the Monte Carlo simulation.

Given an isotropic dark matter flux of

$$\begin{aligned} \frac{1}{4\pi} n_x v_0 &\simeq 1.2 \times 10^{-9} \text{ m}^{-2} \text{ sr}^{-1} \text{ day}^{-1} \\ &\times \left(\frac{1 \text{ g}}{M_x} \right) \left(\frac{\rho_x}{0.4 \text{ GeV/cm}^3} \right) \left(\frac{v_0}{250 \text{ km/s}} \right) \end{aligned} \quad (17)$$

and the combined 3,921 live-time days of NAUTILUS and EXPLORER, the maximum number of events expected is

$$N \simeq 10^{-4} \left(\frac{1 \text{ g}}{M_x} \right), \quad (18)$$

for a local dark matter density, $\rho_x = 0.4 \text{ GeV/cm}^3$, and $v_0 = 250 \text{ km/s}$. A Macro impact would be a random (Poisson) process, therefore a null detection of Macro passages for which $N > 3$ events are expected will rule them out at greater than 95% confidence. It follows that, accounting for the useable fraction of the geometric acceptance mentioned above, the following macro dark

² We have neglected the additional integrated depth the Macro must pass through due to concrete in the roofing of the building in which EXPLORER was housed, as well as the experimental components mounted to the top of the bars [32]. On the other hand, EXPLORER was itself run at 430 m above sea level at CERN, so we have overestimated the atmospheric depth to it. These two complications (at least) partially offset each other and, in any case, they can be neglected considering the level of accuracy required here.

matter candidates are ruled out by this analysis:

$$M_X < \begin{cases} 3 \times 10^{-5} \text{ g}, & \text{if } \frac{\sigma_X}{M_X} \lesssim 10^{-9} \frac{\text{cm}^2}{\text{g}}; \\ 2 \times 10^{-5} \text{ g}, & \text{if } 10^{-9} \frac{\text{cm}^2}{\text{g}} \lesssim \frac{\sigma_X}{M_X} \lesssim 10^{-4} \frac{\text{cm}^2}{\text{g}}; \\ 10^{-5} \text{ g}, & \text{if } 10^{-4} \frac{\text{cm}^2}{\text{g}} \lesssim \frac{\sigma_X}{M_X} \lesssim 10^{-3} \frac{\text{cm}^2}{\text{g}}. \end{cases} \quad (19)$$

Note that at the smallest σ_X/M_X our bound differs slightly from the one found in [31] because of both our choice of $v_0 = 250$ km/s and 95% confidence requirement. Deviations from these estimates are expected at low enough σ_X because of the decreasing excitation energy as a function of σ_X , as seen in (11). The results of our more accurate Monte Carlo analysis are illustrated in Figure 1, where, however, we have used the fixed value of $v_0 = 250$ km/s.

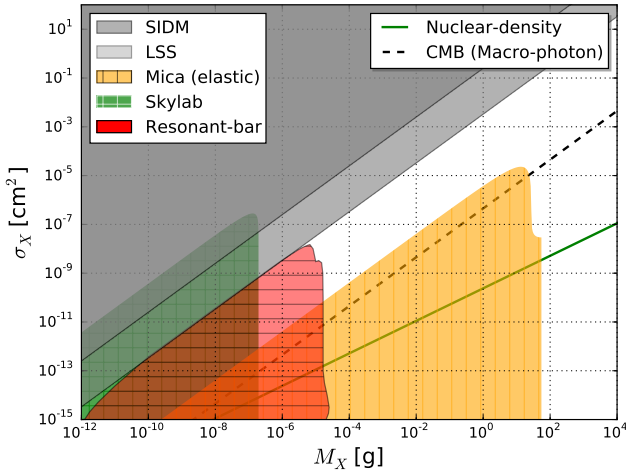


FIG. 1: Existing constraints (described in detail in [24]) on macro dark matter that scatters elastically with baryons and our new constraints from resonant bar displayed in red. Note the marginal overlap between the resonant bar and LSS constraints and that slight improvements to the Skylab and mica constraints have been made as compared to [24]; both of these points are explained in the Discussion. The CMB constraint [24, 33], applicable if Macros couple to photons, rules out Macros above the dashed line.

III. DISCUSSION

Here we have been able to extend existing constraints on nuclearites [31], based on resonant bar gravitational wave detectors, to place new constraints on macro dark matter coupling to baryons. If Macros also couple to photons with their geometric cross section then the CMB constraints indicating $\sigma_X/M_X \lesssim 4.5 \times 10^{-7} \text{ cm}^2/\text{g}$ (dashed line in Figure 1), when taken in combination with the mica constraints, completely overlap with these

constraints. Nevertheless, our results are relevant since they directly constrain Macro-baryon coupling which could, in principle, be different from Macro-photon coupling. Also, the resonant bar detectors have acted as a local probe that directly constrains Macro properties in the solar neighborhood without relying on the (albeit reasonable) assumption that the local dark matter is of similar form and composition to dark matter in different parts and epochs of the universe.

Here the velocity distribution of Macros was taken to be isotropic; in reality the Earth (with the solar system) moves through the galaxy at approximately 200-250 km/s and this should result in an anisotropic distribution observed on the Earth. Also, the Macro velocity distribution presumably has a tail from which it is common to draw an initial Macro velocity, v_0 significantly larger than 250 km/s. This means that the constraints inferred here are conservative and the region of constraint should extend upwards to larger σ_X , i.e. the constraint is stronger than $\sigma_X/M_X \lesssim 3.7 \times 10^{-3} \text{ cm}^2/\text{g}$. Therefore, greater overlap is expected with those determined from large-scale structure, which are $\sigma_X/M_X \lesssim 3.3 \times 10^{-3} \text{ cm}^2/\text{g}$ [34]. On the other hand, the range of σ_X/M_X constrained here is only log-sensitive to v_0 , so we do not expect this to significantly enhance our results.

Here we have also made modest improvements to the constraints inferred from both Skylab [35] and ancient mica [36] compared to those presented in [24]. For both detectors we have more carefully calculated their acceptance, taking into account the column density encountered by a Macro as a function of its impact angle – this resulted in more rounded corners of the constrained regions. For the mica samples studied in [36] the orientation during their ~ 500 Myr exposure time is unknown; we therefore computed the minimum region that is ruled out for a flat mica sample oriented either parallel or perpendicular to the Earth’s surface and have presented those constraints in Figure 1.

The new constraints presented here on macro dark matter from resonant bar detectors provide overlap with both the Skylab and mica constraints, and also fills in part of the gap between the large-scale structure and mica bounds on the coupling of Macros to baryons. In future studies, however, a dedicated experiment of this type is far from ideal due to its relatively limited exposure, which is proportional to the detector surface area and experiment lifetime.

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- [1] Planck, P. Ade *et al.*, *Astron. Astrophys.* **571**, A16 (2014), [1303.5076].
 - [2] BOSS, L. Anderson *et al.*, *Mon.Not.Roy.Astron.Soc.* **441**, 24 (2014), [1312.4877].
 - [3] N. Suzuki *et al.*, *Astrophys.J.* **746**, 85 (2012), [1105.3470].
 - [4] SNLS, A. Conley *et al.*, *Astrophys.J.Suppl.* **192**, 1 (2011), [1104.1443].
 - [5] K. A. Olive, D. N. Schramm, G. Steigman, M. S. Turner and J.-M. Yang, *Astrophys.J.* **246**, 557 (1981).
 - [6] J.-M. Yang, M. S. Turner, G. Steigman, D. Schramm and K. A. Olive, *Astrophys.J.* **281**, 493 (1984).
 - [7] K. Freese, B. Fields and D. Graff, *Nucl.Phys.Proc.Suppl.* **80**, 0305 (2000), [astro-ph/9904401].
 - [8] LUX Collaboration, D. Akerib *et al.*, *Phys.Rev.Lett.* **112**, 091303 (2014), [1310.8214].
 - [9] CAST, M. Arik *et al.*, *Phys.Rev.Lett.* **112**, 091302 (2014), [1307.1985].
 - [10] E. Witten, *Phys.Rev.* **D30**, 272 (1984).
 - [11] K. W. Lynn, A. E. Nelson and N. Tetradis, *Nucl.Phys.* **B345**, 186 (1990).
 - [12] B. W. Lynn, 1005.2124.
 - [13] A. R. Zhitnitsky, *Nucl.Phys.Proc.Suppl.* **124**, 99 (2003), [astro-ph/0204218].
 - [14] A. Zhitnitsky, *Phys.Rev.* **D74**, 043515 (2006), [astro-ph/0603064].
 - [15] J. Rafelski, L. Labun and J. Birrell, *Phys.Rev.Lett.* **110**, 111102 (2013), [1104.4572].
 - [16] B. J. Carr and S. Hawking, *Mon.Not.Roy.Astron.Soc.* **168**, 399 (1974).
 - [17] A. Kusenko and M. E. Shaposhnikov, *Phys.Lett.* **B418**, 46 (1998), [hep-ph/9709492].
 - [18] M. Khlopov, *Int.J.Mod.Phys.* **A28**, 1330042 (2013), [1311.2468].
 - [19] H. Murayama and J. Shu, *Phys.Lett.* **B686**, 162 (2010), [0905.1720].
 - [20] A. Derevianko and M. Pospelov, *Nature Phys.* **10**, 933 (2014), [1311.1244].
 - [21] Y. V. Stadnik and V. V. Flambaum, *Phys.Rev.Lett.* **113**, 151301 (2014), [1405.5337].
 - [22] A. De Rujula and S. Glashow, *Nature* **312**, 734 (1984).
 - [23] S. Burdin *et al.*, 1410.1374.
 - [24] D. M. Jacobs, G. D. Starkman and B. W. Lynn, *Mon.Not.Roy.Astron.Soc.* (2014), [1410.2236].
 - [25] J. Weber, *Phys.Rev.* **117**, 306 (1960).
 - [26] D. Ezrow, N. Wall, J. Weber and G. Yodh, *Phys.Rev.Lett.* **24**, 945 (1970).
 - [27] C. W. Bernard, A. De Rujula and B. Lautrup, *Nucl.Phys.* **B242**, 93 (1984).
 - [28] G. Liu and B. Barish, *Phys.Rev.Lett.* **61**, 271 (1988).
 - [29] P. Astone *et al.*, *Astropart.Phys.* **7**, 231 (1997).
 - [30] P. Astone *et al.*, *Phys.Rev.* **D47**, 4770 (1993).
 - [31] P. Astone *et al.*, 1306.5164.
 - [32] P. Astone *et al.*, *Astropart.Phys.* **30**, 200 (2008), [0806.1335].
 - [33] R. J. Wilkinson, J. Lesgourgues and C. Boehm, *JCAP* **1404**, 026 (2014), [1309.7588].
 - [34] C. Dvorkin, K. Blum and M. Kamionkowski, *Phys.Rev.* **D89**, 023519 (2014), [1311.2937].
 - [35] E. Shirk and P. Price, *The Astrophysical Journal* **220**, 719 (1978).
 - [36] P. B. Price, *Phys.Rev.* **D38**, 3813 (1988).