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J. Wiechczynski et al. (Belle Collaboration)

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Measurement of $B^0 \to D_s^- K_S^0 \pi^+$ and $B^+ \to D_s^- K^+ K^+$ branching fractions

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We report a measurement of the B^0 and B^+ meson decays to the $D_s^- K_S^0 \pi^+$ and $D_s^- K^+ K^+$ final states, respectively, using $657 \times 10^6 B\overline{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric-energy e^+e^- collider. Using the $D_s^- \to \phi \pi^-$, $K^*(892)^0 K^-$ and $K_S^0 K^-$ decay modes for the D_s reconstruction, we measure the following branching fractions: $\mathcal{B}(B^0 \to D_s^- K_S^0 \pi^+) = [0.47 \pm 0.06(\text{stat}) \pm 0.05(\text{syst})] \times 10^{-4}$ and $\mathcal{B}(B^+ \to D_s^- K^+ K^+) = [0.93 \pm 0.22(\text{stat}) \pm 0.10(\text{syst})] \times 10^{-5}$. We find the ratio of the branching fraction of $B^+ \to D_s^- K^+ K^+$ to that of the analogous Cabibbo-favored $B^+ \to D_s^- K^+ \pi^+$ decay to be $\mathcal{R}_{\mathcal{B}} = 0.054 \pm 0.013(\text{stat}) \pm 0.006(\text{syst})$, which is consistent with the naïve factorization model. We also observe a deviation of the $D_s K$ invariant mass distribution from the three-body phase-space model for both studied decays.

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The dominant process for the decays $B^0 \to D_s^- K_S^0 \pi^+$ and $B^+ \to D_s^- K^+ K^+$ [1] is mediated by the $b \to c$ quark transition with subsequent W fragmentation to a charged pion or kaon and includes the production of an additional $s\overline{s}$ pair, as shown in Fig. 1. As the process $B^+ \to D_s^- K^+ K^+$ is Cabibbo-suppressed due to the formation of a $u\overline{s}$ pair from the W vertex (Fig. 1a), its branching fraction can be compared to the measured branching fraction of the Cabibbo-favored $B^+ \to D_s^- K^+ \pi^+$ decay [2, 3].

Within the framework of naïve factorization [4], the ratio of these branching fractions should be proportional to the ratio of the squares of the CKM matrix elements V_{ud} and V_{us} [5, 6]. Such a comparison allows us to check the validity of existing theoretical descriptions of the three-body hadronic decays. In addition, the two-body subsystem of the $D_s^-K_S^0\pi^+$ and $D_s^-K^+K^+$ final states merits study since a significant deviation from the simple phase-space model was observed in the $D_s^-K^+$ invariant mass

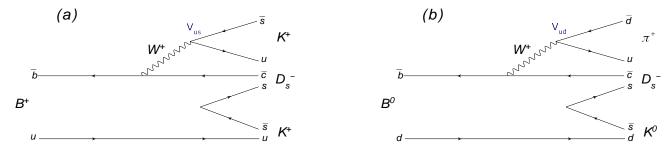


FIG. 1. Dominant Feynman diagram for the (a) $B^+ \to D_s^- K^+ K^+$ and (b) $B^0 \to D_s^- K_S^0 \pi^+$ decay.

for the similar process $B^+ \to D_s^- K^+ \pi^+$ [2, 3] and also in the semileptonic process $B^+ \to D_s^{(*)-} K^+ l^+ \nu_l$ [7]. This constitutes a potential source of new spectroscopy discoveries.

Both $B^0 \to D_s^- K_S^0 \pi^+$ and $B^+ \to D_s^- K^+ K^+$ decay modes have been observed by BaBar [3] and call for confirmation. In this paper, we report measurements of the branching fractions for $B^0 \to D_s^- K_S^0 \pi^+$ and $B^+ \to D_s^- K^+ K^+$ and compare the latter's with the branching fraction for $B^+ \to D_s^- K^+ \pi^+$. The invariant mass distributions for the two-body subsystems are studied to evaluate the discrepancy from the phase-space model. The analysis is performed on a data sample containing $(657 \pm 9) \times 10^6$ $B\overline{B}$ pairs collected with the Belle detector at the KEKB asymmetric-energy e^+e^- collider [8] operating at the $\Upsilon(4S)$ resonance. The production rates of B^+B^- and $B^0\overline{B}^0$ pairs are assumed to be equal.

The Belle detector [9] is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter composed of CsI(Tl) crystals, all located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux return located outside of the coil is instrumented to detect K_L^0 mesons and to identify muons. Two inner detector configurations were used: a 2.0 cm beam pipe with a 3-layer SVD for the first sample of $152 \times 10^6 B\overline{B}$ pairs and a 1.5 cm beam pipe with a 4-layer SVD for the remaining $505 \times 10^6 B\overline{B}$ pairs [10].

Charged tracks are required to have a distance of closest approach to the interaction point of less than 5.0 cm along the positron beam direction (defined to be the z-axis) and less than 0.5 cm in the transverse plane. In addition, charged tracks must have transverse momenta larger than 100 MeV/c. To identify charged hadrons, we combine information from the CDC, ACC and TOF into pion, kaon and proton likelihoods \mathcal{L}_{π} , \mathcal{L}_{K} and \mathcal{L}_{p} , respectively. For a kaon candidate, we require the likelihood ratio $\mathcal{L}_{K/\pi} = \mathcal{L}_{K}/(\mathcal{L}_{K} + \mathcal{L}_{\pi})$ to be greater than 0.6. Pions are selected from all track candidates except for the ones with high kaon probabilities, which are suppressed by requiring $\mathcal{L}_{K/\pi} < 0.95$. For kaons (pions), we

also apply a proton veto criterion: $\mathcal{L}_{p/K}(\mathcal{L}_{p/\pi}) < 0.95$. In addition, we reject all charged tracks consistent with an electron (or muon) hypothesis $\mathcal{L}_{e(\mu)} < 0.95$, where \mathcal{L}_e and \mathcal{L}_{μ} are respective lepton likelihoods. The above requirements result in a typical momentum-dependent kaon (pion) identification efficiency ranging from 92% to 97% (94% to 98%) for various channels, with 2-15% of kaon candidates being misidentified as pions and 4-8% of pion candidates being misidentified as kaons.

The D_s^- candidates are reconstructed in three final states: $\phi(\to K^+K^-)\pi^-$, $K^*(892)^0(\to K^+\pi^-)K^-$ and $K_S^0(\to \pi^+\pi^-)K^-$. We retain K^+K^- ($K^+\pi^-$) pairs as $\phi(K^*(892)^0)$ candidates if their invariant mass lies within 10 (100) MeV/ c^2 of the nominal $\phi(K^*(892)^0)$ mass [11]. This requirement has 91% (95%) efficiency for the respective D_s decay mode. Candidate K_S^0 mesons are selected by combining pairs of oppositely charged tracks (treated as pions) with an invariant mass within 16 MeV/ c^2 (3 σ) of the nominal K_S^0 mass. In addition, the vertices of these track pairs must be displaced from the interaction point by at least 0.5 cm.

A B candidate is reconstructed by combining the D_s candidate with a selected K_S^0 and a charged pion for $B^0 \to D_s^- K_S^0 \pi^+$, and with a pair of kaons of the same charge for $B^+ \to D_s^- K^+ K^+$. A quality requirement on the B vertex-fit statistic ($\chi_B^2/\text{NDF} < 60$) to the $D_s^-K^+K^+$ ($D_s^-K_S^0\pi^+$) trajectories is applied, where the D_s mass is constrained to its world average value [11] and NDF is the number of degrees of freedom. The signal decays are identified by three kinematic variables: the D_s invariant mass, the energy difference $\Delta E = E_B - E_{\rm beam}$, and the beam-energy-constrained mass $M_{\rm bc} = (\sqrt{E_{\rm beam}^2 - |\vec{p}_B|^2 c^2})/c^2$. Here, E_B and \vec{p}_B are the reconstructed energy and momentum of the Bcandidate, respectively, and E_{beam} is the run-dependent beam energy, all calculated in the e^+e^- center-of-mass (CM) frame. We retain candidate events in the threedimensional region defined by 1.91 GeV/ $c^2 < M(D_s) <$ $2.03 \text{ GeV}/c^2$, $5.2 \text{ GeV}/c^2 < M_{\rm bc} < 5.3 \text{ GeV}/c^2$ and $-0.2 \,\mathrm{GeV} < \Delta E < 0.2 \,\mathrm{GeV}$. In the fit described later, we use a narrower range $-0.08 \text{ GeV} < \Delta E < 0.20 \text{ GeV}$ to exclude the possible contamination from $B \to D_s X$ decays having higher multiplicities. From a GEANT3 [12] based Monte Carlo (MC) simulation, we find the signal peaks in a region defined by 1.9532 GeV/ $c^2 < M(D_s) <$

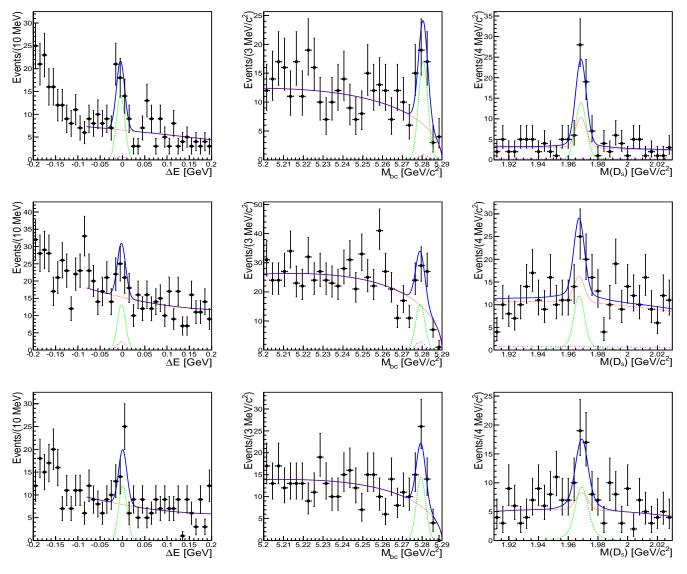


FIG. 2. Distributions of ΔE , $M_{\rm bc}$ and $M(D_s)$ for (top) $B^0 \to D_s^-(\to \phi \pi^-) K_S^0 \pi^+$, (middle) $B^0 \to D_s^-(\to K^{*0}K^-) K_S^0 \pi^+$, and (bottom) $B^0 \to D_s^-(\to K_S^0K^-) K_S^0 \pi^+$ decays. The distribution for each quantity is shown in the signal region of the remaining two. The blue solid curves show the results of the overall fit described in the text, the green dotted curves correspond to the signal component, the red long-dashed curves indicate the combinatorial background (including the peaking D_s component) and the pink dot-dashed curves represent the peaking B^0 background.

1.9832 GeV/ c^2 , 5.27 GeV/ c^2 < $M_{\rm bc}$ < 5.29 GeV/ c^2 and $|\Delta E|$ < 0.03 GeV. Based on MC simulation, the region 2.88 GeV/ c^2 < $M(c\overline{c})$ < 3.18 GeV/ c^2 is excluded to remove background from $B^+ \to (c\overline{c})K^+$ or $B^0 \to (c\overline{c})K^0_S$ decays, where $(c\overline{c})$ denotes a charmonium state such as the J/ψ or η_c and $M(c\overline{c})$ is the invariant mass of its decay products $(K^+K^-\pi^+\pi^-)$ or $K^0_SK^+\pi^-$ for the corresponding D_S mode).

We find that for the $B^0 \to D_s^- K_S^0 \pi^+$ ($B^+ \to D_s^- K^+ K^+$) decay, the average number of B candidates satisfying all selection criteria is 1.14 (1.04) per event. In cases when an event contains more than one B candidate, we select the one with the smallest value of χ_B^2 .

We exploit the event topology to discriminate between spherical $B\overline{B}$ events and the dominant background from jet-like continuum $e^+e^- \to q\overline{q}$ $(q=u,\ d,\ s,\ c)$ events. We require the event shape variable R_2 , defined as the ratio of the second- and zeroth-order Fox-Wolfram moments [13], to be less than 0.4 to suppress the continuum background.

Large MC samples are used to evaluate possible background from $B\bar{B}$ and continuum $q\bar{q}$ events for both studied channels. In the $B^0 \to D_s^- K_S^0 \pi^+$ analysis, a significant contribution from $B^0 \to D_s^- D^+$, $D^+ \to K_S^0 \pi^+$ is identified. We require the quantity $|M(K_S^0 \pi^+) - m_{D^+}|$ to be less (greater) than 30 MeV/ c^2 to select the $B^0 \to$

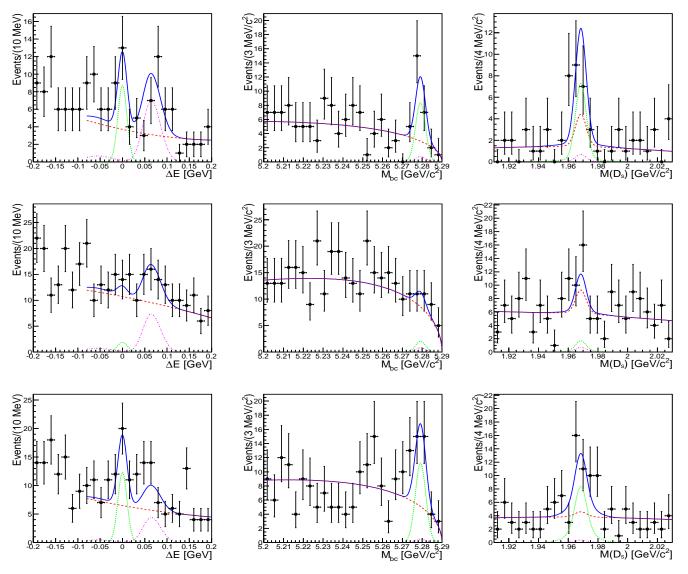


FIG. 3. Distributions of ΔE , $M_{\rm bc}$ and $M(D_s)$ for (top) $B^+ \to D_s^-(\to \phi\pi^-)K^+K^+$, (middle) $B^+ \to D_s^-(\to K^{*0}K^-)K^+K^+$, and (bottom) $B^+ \to D_s^-(\to K_S^0K^-)K^+K^+$ decays. The distribution for each quantity is shown in the signal region of the remaining two. The blue solid curves show the results of the overall fit described in the text, the green dotted curves correspond to the signal component, the red long-dashed curves indicate the combinatorial background (including the peaking D_s component) and the pink dot-dashed curves represent the $B \to D_s^{(*)}K\pi$ contribution.

 $D_s^-D^+$ control sample (to suppress the charm contamination), where m_{D^+} is the world average of the D^+ meson mass. We also find other contributing backgrounds that are taken into account in our fitting procedures (discussed below). The combinatorial background, arising due to a random combination of the tracks, is common for both $D_s^-K_S^0\pi^+$ and $D_s^-K^+K^+$ channels. Its contribution also includes a sub-sample of good D_s candidates randomly combined with K^+K^+ or $K_S^0\pi^+$ (" D_s peaking background"). Two more types of background, specific for each channel, are found. For the $B^0 \to D_s^-K_S^0\pi^+$ decay, we identify a peaking contribution from the B^0 decaying to the same final state of five hadrons (" B^0

peaking background"). Such events do not contain a D_s meson in the decay chain, and mainly include $(c\bar{c})$ states like $\psi(2S),\,\eta_c(2S),\,\chi_{c1}(1P)$ and $\chi_{c0}(1P)$. Finally, we find a significant contribution to $B^+\to D_s^-K^+K^+$ from the $B^+\to D_s^{(*)-}K^+\pi^+$ decays owing to pion-to-kaon misidentification (or a missing photon in the D_s^* reconstruction). We determine the shape of this contribution in $\Delta E,\,M_{\rm bc}$ and $M(D_s)$ using MC samples of $B^+\to D_s^{(*)-}K^+\pi^+$ after subjecting them to the $B^+\to D_s^-K^+K^+$ selection.

The signal yields are obtained from unbinned extended maximum-likelihood fits to the $[\Delta E, M_{\rm bc}, M(D_s)]$ distributions of the selected candidate events. The likelihood

function is given by

$$\mathcal{L} = \frac{1}{N!} \cdot \exp\left(-\sum_{j} N_{j}\right) \cdot \prod_{i=1}^{N} \left(\sum_{j} N_{j} \mathcal{P}_{i}^{j}\right), \quad (1)$$

where j runs over the signal and background components, i is the event index, N_j and \mathcal{P}_i^j denote the yield and probability density functions (PDFs) for each component, respectively, and N is the total number of data events. Neglecting the small correlation between each pair of fit observables, we construct the overall PDF as a product of their individual PDFs. Two components, signal and combinatorial background (j = sig, cmb), are common for $B^0 \to D_s^- K_S^0 \pi^+$ and $B^+ \to D_s^- K^+ K^+$. Their respective PDF parameterizations are constructed as

$$\mathcal{P}_{i}^{\text{sig}} = \mathcal{G}(\Delta E^{i}; \overline{\Delta E}, \sigma_{\Delta E}) \times \mathcal{G}(M_{\text{bc}}^{i}; m_{B}, \sigma_{M_{\text{bc}}}) \times \mathcal{G}_{2}^{\text{sig}}(M^{i}(D_{s}); m_{D_{s}}, \sigma_{D_{s}}^{(1)}, \sigma_{D_{s}}^{(2)}, f_{D_{s}}^{\text{sig}})$$

$$(2)$$

and

$$\mathcal{P}_{i}^{\text{cmb}} = p_{2}(\Delta E^{i}; \ w_{0}, w_{1}, w_{2}) \times A(M_{\text{bc}}^{i}; \ \zeta)
\times \left[f_{D_{s}}^{\text{peak}} \cdot \mathcal{G}_{2}^{\text{bkg}} \left(M^{i}(D_{s}); \ m_{D_{s}}, \sigma_{D_{s}}^{(1)}, \sigma_{D_{s}}^{(2)}, f_{D_{s}}^{\text{bkg}} \right) \right.
+ \left. (1 - f_{D_{s}}^{\text{peak}}) \cdot p_{2}(M^{i}(D_{s}); \ v_{0}, v_{1}, v_{2}) \right].$$
(3)

Here, we use a Gaussian function (\mathcal{G}) to parameterize the signal PDF in ΔE and $M_{\rm bc}$ and a double-Gaussian function (\mathcal{G}_2) with a common mean for the $M(D_s)$ distribution. The combinatorial background component utilizes a second-order Chebyshev polynomial (p_2) in the ΔE distribution and an ARGUS function [14], $A(M_{\rm bc},\zeta) \propto M_{\rm bc} \sqrt{1-(M_{\rm bc}/E_{\rm beam})^2}e^{-\zeta(1-(M_{\rm bc}/E_{\rm beam})^2)}$ for the $M_{\rm bc}$ distribution, where ζ is a fit parameter. The combinatorial background's $M(D_s)$ distribution is described by the sum of a double-Gaussian function for the " D_s peaking background" and a second-order Chebyshev polynomial with a relative fraction $f_{D_s}^{\rm peak}$ of these two components. The double-Gaussian function for component j is defined as

$$\mathcal{G}_{2}^{j}(M^{i}(D_{s}); \ m_{D_{s}}, \sigma_{D_{s}}^{(1)}, \sigma_{D_{s}}^{(2)}, f_{D_{s}}^{j}) =
f_{D_{s}}^{j} \cdot \mathcal{G}(M^{i}(D_{s}); \ m_{D_{s}}, \sigma_{D_{s}}^{(1)})
+ (1 - f_{D_{s}}^{j}) \cdot \mathcal{G}(M^{i}(D_{s}); \ m_{D_{s}}, \sigma_{D_{s}}^{(2)}),$$
(4)

where $f_{D_s}^j$ denotes the relative contribution of the core over the tail Gaussian in the $M(D_s)$ distribution.

In Eqs. (2-4), $\overline{\Delta E}$, m_B , m_{D_s} , $\sigma_{\Delta E}$, $\sigma_{M_{\rm bc}}$, $\sigma_{D_s}^{(1)}$, $\sigma_{D_s}^{(2)}$ (the respective mean values and widths of the Gaussians), $f_{D_s}^{\rm peak}$ and $f_{D_s}^{\rm sig(bkg)}$ are fit parameters. For both channels studied, the parameters $\sigma_{D_s}^{(1)}$, $\sigma_{D_s}^{(2)}$ and $f_{D_s}^{\rm sig(bkg)}$ are fixed to the values obtained from the $B^+ \to D_s^+ \overline{D}{}^0$ control channel. In addition, we use the $B^0 \to D_s^- D^+$ ($B^+ \to D_s^- D^+$)

 $D_s^+ \overline{D}{}^0$) control sample to determine the signal width values for the ΔE and $M_{\rm bc}$ distributions that are later fixed in the fit to the $B^0 \to D_s^- K_S^0 \pi^+ (B^+ \to D_s^- K^+ K^+)$ data sample.

An additional background component $j=B^{0\text{bkg}}$ $(j=D_s^{(*)}K\pi)$ is introduced for $D_s^-K_S^0\pi^+$ $(D_s^-K^+K^+)$, according to the results of dedicated MC studies. For the $B^0\to D_s^-K_S^0\pi^+$ decay, we define

$$\mathcal{P}_{i}^{B^{0}^{\text{bkg}}} = \mathcal{G}(\Delta E^{i}; \ \overline{\Delta E}, \sigma_{\Delta E}) \times \mathcal{G}(M_{\text{bc}}^{i}; \ m_{B}, \sigma_{M_{\text{bc}}}) \times p_{2}(M^{i}(D_{s}); \ v_{0}, v_{1}, v_{2}),$$

$$(5)$$

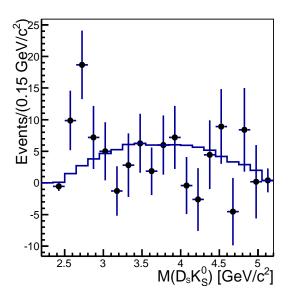
to model the B^0 peaking background. For the $B^+\to D_s^-K^+K^+$ channel, the respective background PDF contribution is defined by

$$\mathcal{P}_{i}^{D_{s}^{(*)}K\pi} = \left[f^{D_{s}K\pi} \cdot \mathcal{G}_{b}(\Delta E^{i}; \overline{\Delta E}^{b}, \sigma_{\Delta E}^{b1}, \sigma_{\Delta E}^{b2}) + (1 - f^{D_{s}K\pi}) \cdot \mathcal{C}(\Delta E^{i}; \overline{\Delta E}^{\mathcal{C}}, \sigma^{\mathcal{C}}, \alpha^{\mathcal{C}}, n^{\mathcal{C}}) \right] \times \left[f^{D_{s}K\pi} \cdot \mathcal{G}(M_{\text{bc}}^{i}; m_{B}, \sigma_{M_{\text{bc}}}) + (1 - f^{D_{s}K\pi}) \cdot \mathcal{G}_{b}(M_{\text{bc}}^{i}; m_{B}^{b}, \sigma_{M_{\text{bc}}}^{b1}, \sigma_{M_{\text{bc}}}^{b2}) \right] \times \mathcal{G}_{2}(M^{i}(D_{s}); m_{D_{s}}, \sigma_{D_{s}}^{(1)}, \sigma_{D_{s}}^{(2)}, f_{D_{s}}^{\text{sig}}),$$

$$(6)$$

where a bifurcated Gaussian (\mathcal{G}_b) and a Crystal Ball function $(\mathcal{C})[15]$ are used to parameterize the $B^+ \to D_s^{(*)-}K^+\pi^+$ component. The relevant parameters $(\overline{\Delta E}^b, \sigma_{\Delta E}^{b1}, \sigma_{\Delta E}^{b2}, m_B^b, \sigma_{M_{bc}}^{b1}, \sigma_{M_{bc}}^{b2}$ for \mathcal{G}_b and $\overline{\Delta E}^{\mathcal{C}}, \sigma^{\mathcal{C}}, \alpha^{\mathcal{C}}, n^{\mathcal{C}}$ for \mathcal{C}) are fixed from a fit to the $B^+ \to D_s^{(*)-}K^+\pi^+$ MC samples; $f^{D_sK\pi}$, the relative contribution of $D_sK\pi$ and $D_s^*K\pi$ we events, is evaluated from the $D_sK\pi$ and $D_s^*K\pi$ MC samples for each D_s mode. The values of the remaining quantities are treated in a fashion similar to that of the $B^0 \to D_s^-K_S^0\pi^+$ channel. The obtained signal yields $(N_{\rm sig})$ are listed in Table I. Figures 2 and 3 show the distributions of ΔE , M_{bc} and $M(D_s)$ for $B^0 \to D_s^-K_S^0\pi^+$ and $B^+ \to D_s^-K^+K^+$, respectively, together with the fits described above.

We study the invariant mass distribution of the $D_s^- K_S^0$ $(D_s^- K_{\rm low}^+)$ subsystem in the $D_s^- K_S^0 \pi^+$ $(D_s^- K^+ K^+)$ final state, where K_{low}^+ is the kaon with the lower momentum. These distributions exhibit a surplus in the low $D_s K$ mass region with enhancements around $2.7\,\mathrm{GeV}/c^2$ (Fig. 4). A similar significant effect has already been observed in other hadronic [2, 3] and semileptonic [7] decays. This phenomenon may be related to strong interaction effects in the $\bar{c}s\bar{s}q$ (q=d,u) system and, in particular, could be explained by the production of charm resonances with masses below the $D_s^{(*)}K$ threshold [16]. Therefore, for the determination of the branching fractions, we use an efficiency $\epsilon[M(D_sK)]$ that is measured in bins of $M(D_sK)$ to account for efficiency variations in the observed data. For each D_s decay mode in both the channels, we obtain the respective branching



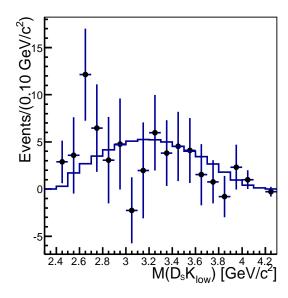


FIG. 4. Invariant mass distributions of (left) $D_s^- K_S^0$ for the $B^0 \to D_s^- K_S^0 \pi^+$ and (right) $D_s^- K_{\rm low}^+$ for $B^+ \to D_s^- K^+ K^+$ decay events in the signal region of ΔE , $M_{\rm bc}$ and M_{D_s} after applying all selection criteria. Points with error bars represent the data after subtraction of the background contribution, estimated from the $M_{\rm bc}$ sideband (5.22 GeV/ c^2 < $M_{\rm bc}$ < 5.26 GeV/ c^2). The histograms show the phase-space distribution of the signal MC sample normalized to the data luminosity.

TABLE I. Signal yields, average reconstruction efficiencies, statistical significances and branching fractions for $B^0 \to D_s^- K_S^0 \pi^+$ and $B^+ \to D_s^- K^+ K^+$ decays.

Decay	$N_{ m sig}$	$\epsilon_{\rm av}[\%]$	$S[\sigma]$	\mathcal{B}	
$B^0 \to D_s^-(\to \phi\pi^-)K_S^0\pi^+$	$34.6^{+7.1}_{-6.3}$	9.09 ± 0.19	7.4	0.37 ± 0.08	
$B^0 \to D_s^- (\to K^{*0}K^-)K_S^0\pi^+$	$32.9^{+8.9}_{-8.2}$	5.99 ± 0.16	4.5	0.46 ± 0.13	$\times 10^{-4}$
$B^0 \to D_s^- (\to K_S^0 K^-) K_S^0 \pi^+$	$29.2^{+7.4}_{-6.7}$	8.68 ± 0.29	5.7	0.72 ± 0.18	
			simultaneous:		
			10.1	$0.47 \pm 0.06 \pm$	± 0.05
$B^+ \to D_s^- (\to \phi \pi^-) K^+ K^+$	$15.2^{+5.0}_{-4.3}$	11.62 ± 0.14	5.1	0.87 ± 0.29	
$B^+ \to D_s^- (\to K^{*0}K^-)K^+K^+$	$3.8^{+4.7}_{-3.8}$	10.22 ± 0.13	1.0	0.22 ± 0.31	$\times 10^{-5}$
$B^+ \to D_s^- (\to K_S^0 K^-) K^+ K^+$	$21.5^{+6.5}_{-5.7}$	12.11 ± 0.29	5.2	2.64 ± 0.78	
		simultaneous:			
			$6.6 \qquad 0.93 \pm 0.22 \pm 0.10$		

fraction (\mathcal{B}) by performing another fit while substituting N_{sig} in Eq.(1) with

$$N_{\text{sig}} = \mathcal{B} \cdot \epsilon[M(D_s K)] \cdot N_{B\bar{B}} \cdot \mathcal{B}_{\text{int}}, \tag{7}$$

where $N_{B\bar{B}}$ is the total number of $B\bar{B}$ pairs in the data sample and $\mathcal{B}_{\rm int}$ is the product of decay branching fractions for the intermediate resonances in the respective decay chain. The combined branching fraction is calculated by performing a simultaneous fit to the three D_s^- decay modes with a common \mathcal{B} value.

The average reconstruction efficiencies ($\epsilon_{\rm av}$), branching fractions and the signal yields, together with their statistical significances (S), are listed in Table I. The significance is defined as $\sqrt{-2\ln(\mathcal{L}_0/\mathcal{L}_{\rm max})}$, where $\mathcal{L}_{\rm max}$ (\mathcal{L}_0) denotes the maximum likelihood with the signal

yield at its nominal value (fixed to zero). The $\epsilon_{\rm av}$ values are calculated from Eq.(7) using the obtained $N_{\rm sig}$ and \mathcal{B} values for each channel, where $\epsilon(M(D_sK))$ is replaced by $\epsilon_{\rm av}$. The systematic uncertainties, described below, are evaluated for the full data sample for all three D_s decay modes

Systematic uncertainties are listed in Table II. The contribution due to the selection procedure, item (a), is dominated by the R_2 requirement. It is estimated in the control channel by comparing the signal ratios for the data and dedicated MC sample. Each ratio is constructed by dividing the nominal signal yield by that without the R_2 requirement. The uncertainty due to the background components (b) for $B^0 \to D_s^- K_S^0 \pi^+$ decay is determined by studying the possible influence of the low- ΔE region on the signal yield by adding the respective component

Source	$B^0 \to D_s^- K_S^0 \pi^+$	$B^+ \to D_s^- K^+ K^+$
(a) Selection procedure	± 3.6	± 3.6
(b) Background components	-3.4	+1.7
(c) Signal shape	± 3.4	± 4.6
(d) MC statistics and fit bias	± 2.8	± 2.9
(e) \mathcal{B}_{int}	± 5.2	± 5.2
(f) Tracking	± 3.6	± 4.6
(g) Hadron identification	± 3.1	± 4.9
(h) K_S^0 reconstruction	± 5.9	± 1.0
(i) Uncertainty in $N(B\overline{B})$	± 1.4	± 1.4
Total	±11.3	±11.0

TABLE II. Systematic uncertainties (in %) on the branching fractions for $B^0 \to D_s^- K_S^0 \pi^+$ and $B^+ \to D_s^- K^+ K^+$ decay modes.

to the PDF, which includes a peaking background in the $M_{\rm bc}$ and M_{D_s} variables. For $B^+ \to D_s^- K^+ K^+$, we compare the nominal branching fraction with the one obtained from the fit with the $B^+ \to D_s^{*-}K^+\pi^+$ component ignored in the PDF. To evaluate the contribution related to the signal shape (c), we repeat the fits while varying the fixed shape parameters by $\pm 1\sigma$. The uncertainty due to limited MC statistics (d) is dominated by the statistical error on the selection efficiency. It is evaluated by varying the $\epsilon(M(D_sK))$ values within their statistical errors in the efficiency distributions over $M(D_sK_s^0)$ and $M(D_sK)$ and comparing the modified branching fractions with the nominal values. This uncertainty also includes a small contribution from the possible fit bias, which is evaluated by comparing the number of MC signal events with the corresponding value obtained from the fit. Contribution (e) is due to uncertainties in the branching fractions for the decays of intermediate particles, predominantly those of the D_s [11]. Items (f),(g),(h) refer to the track reconstruction and particle identification uncertainties, which are related to the detector performance and include potential discrepancies between data and simulations. Finally, the contribution (i) reflects the limited precision on determination of the number of $B\bar{B}$ pairs in the data sample. The overall systematic error is obtained by summing all contributions in quadrature.

Using the branching fraction for the $B^+ \to D_s^- K^+ \pi^+$ decay [2] obtained with a method similar to that of the $B^+ \to D_s^- K^+ K^+$ studies, we calculate the ratio

$$\mathcal{R}_{\mathcal{B}} \equiv \frac{\mathcal{B}(B^{+} \to D_{s}^{-} K^{+} K^{+})}{\mathcal{B}(B^{+} \to D_{s}^{-} K^{+} \pi^{+})}$$

$$= 0.054 \pm 0.013(\text{stat}) \pm 0.006(\text{syst}),$$
(8)

where the common systematic uncertainties cancel. The value of the ratio is consistent with the theoretical expectation from the naïve factorization model,

$$\mathcal{R}_{\mathcal{B}}^{th} = \left(\frac{|V_{us}|}{|V_{ud}|}\right)^2 \cdot \left(\frac{f_K}{f_{\pi}}\right)^2 \cdot \frac{\mathcal{V}(D_s K K)}{\mathcal{V}(D_s K \pi)}$$

$$= 0.066 \pm 0.001,$$
(9)

where f_h is the decay constant for a given hadron h [11]

and $\mathcal{V}(D_sKh)$ is the phase-space volume for the respective final state.

In summary, we have determined the following branching fractions:

$$\mathcal{B}(B^0 \to D_s^- K_S^0 \pi^+) = [0.47 \pm 0.06(\text{stat}) \pm 0.05(\text{syst})] \times 10^{-4}$$
(10)

and

$$\mathcal{B}(B^+ \to D_s^- K^+ K^+)$$

= $[0.93 \pm 0.22(\text{stat}) \pm 0.10(\text{syst})] \times 10^{-5}$. (11)

They are consistent with, and more precise than, the values reported by the BaBar Collaboration [3]. The comparison of the branching fractions for the Cabibbo-suppressed decay $B^+ \to D_s^- K^+ K^+$ to the Cabibbo-favored $B^+ \to D_s^- K^+ \pi^+$ process yields a result compatible with the naïve factorization hypothesis. We also find a deviation from the simple phase-space model in the $D_s K$ invariant-mass distributions for both decays. A more detailed analysis of the enhancement (e.g., a study of the angular distribution) requires larger data samples that will be accessible to the LHCb [17] and Belle II [18] experiments.

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