

This is the accepted manuscript made available via CHORUS. The article has been published as:

B decays into radially excited charmed mesons

J. Segovia, E. Hernández, F. Fernández, and D. R. Entem

Phys. Rev. D **87**, 114009 — Published 10 June 2013

DOI: [10.1103/PhysRevD.87.114009](https://doi.org/10.1103/PhysRevD.87.114009)

B decays into radially excited charmed mesons

J. Segovia,¹ E. Hernández,² F. Fernández,² and D.R. Entem²

¹*Physics Division, Argonne National Laboratory,
Argonne, Illinois 60439-4832, USA*

²*Departamento de Física Fundamental e IUFFyM,
Universidad de Salamanca, E-37008 Salamanca, Spain*
(Dated: May 21, 2013)

It has been recently argued that some longstanding problems in semileptonic B decays can be solved provided the branching ratio for the $B \rightarrow D'^{(*)}$ semileptonic decays are large enough. We have studied these decays in a constituent quark model which has been successful in describing semileptonic and non-leptonic B decays into orbitally excited charmed mesons. Our results do not confirm the hypothesis of large branching ratios for the $B \rightarrow D'^{(*)}$ semileptonic decays. In addition, we calculate the non-leptonic $B \rightarrow D'\pi$ decays which can provide an independent test of the form factors involved in the $B \rightarrow D'^{(*)}$ reactions.

PACS numbers: 12.39.Jh, 12.39.Pn, 13.20.He, 14.40.Lb

I. INTRODUCTION

The determination of exclusive branching fractions of $B \rightarrow X_c l^+ \nu_l$ decays is an essential part of the B -factory program to understand the dynamics of b -quark semileptonic decays and therefore to determine the relevant Cabibbo-Kobayashi-Maskawa matrix elements, $|V_{cb}|$ and $|V_{ub}|$, which are essential parameters of the Standard Model. The methods used to determine the decay rates as a function of $|V_{qb}|$ are very different for inclusive and exclusive decays, and the comparison of these complementary determinations provides an important check on the results.

Current measurements show a discrepancy between the inclusive rate $\mathcal{B}(B^+ \rightarrow X_c l^+ \nu_l)$ and the sum of the measured exclusive channels. At present, the disagreement between the inclusive rate $\mathcal{B}(B^+ \rightarrow X_c l^+ \nu) = (10.92 \pm 0.16)\%$ and the sum of the measured exclusive rates is

$$\begin{aligned} &\mathcal{B}(B^+ \rightarrow X_c l^+ \nu_l) - \mathcal{B}(B^+ \rightarrow D^{(*)} l^+ \nu_l) \\ &- \mathcal{B}(B^+ \rightarrow D^{(*)} \pi l^+ \nu_l) = (1.45 \pm 0.13)\%. \end{aligned} \quad (1)$$

The authors of Ref. [1] argue that this 1.45% discrepancy could be solved, or at least eased, by an unexpectedly large B decay rate to the first radially excited D' and D'^* states ($\mathcal{B}(B \rightarrow D'^{(*)} l^+ \nu_l) \sim \mathcal{O}(1\%)$). It is also stated in Ref. [1] that a potentially large $\mathcal{B}(B^+ \rightarrow D'^{(*)} l^+ \nu_l)$ could help to solve the so called 1/2 vs 3/2 puzzle. This puzzle refers to the discrepancy between heavy quark symmetry based model predictions for B decays into $1P$ D^{**} states and observations. Those calculations predict that these decays should have a substantially smaller rate to the $j_q^P = \frac{1}{2}^+$ doublet than to the $j_q^P = \frac{3}{2}^+$ doublet (see for instance Refs. [2, 3]) whereas roughly equal branching ratios are found experimentally. A large $\mathcal{B}(B^+ \rightarrow D'^{(*)} l^+ \nu_l)$ would result in an excess of the detected $B \rightarrow D_{1/2} \pi l \nu_l$ with respect to $B \rightarrow D_{3/2} \pi l \nu$ due to the fact that the $\Gamma(D' \rightarrow D_{1/2} \pi)$ is much larger than the $\Gamma(D' \rightarrow D_{3/2} \pi)$ because in the first case the pion is

Resonance	Mass (MeV)	Width (MeV)
$D(2550)^0$	$2539.4 \pm 4.5 \pm 6.8$	$130 \pm 12 \pm 13$
$D^*(2600)^0$	$2608.7 \pm 2.4 \pm 2.5$	$93 \pm 6 \pm 13$

TABLE I. Mass and total decay width of the $D'^{(*)}$ resonances as measured by the BaBar Collaboration [4].

emitted in S -wave while in the $D_{3/2}$ one is emitted in P -wave.

Evidence for the $D'^{(*)}$ radial excitations, that would correspond to $2S$ quark model states, have recently been found by the BaBar Collaboration [4]. Their results are summarized in Table I. The $D(2550)$ meson has only been seen in the decay mode $D^* \pi$ and its helicity-angle distribution turns out to be consistent with the prediction of a 2^1S_0 state. The $D^*(2600)$ meson decays into $D\pi$ and $D^* \pi$ final states, and its helicity-angle distribution is consistent with the meson being a $J^P = 1^-$ state. Moreover, its mass makes it the perfect candidate to be the spin partner of the $D(2550)$ meson.

Previous theoretical determinations of $\mathcal{B}(B^+ \rightarrow D'^{(*)} l^+ \nu)$ include an earlier calculation within the ISGW2 model, which incorporates constraints imposed by heavy quark symmetry, where a value of 0.06% was obtained [5]. This is in agreement with the heavy quark effective theory calculation of Suzuki *et al.* [6] which obtained $\mathcal{B}(B^+ \rightarrow D'^{(*)} l^+ \nu) = 0.05\%$. A much larger value is obtained in Ref. [7]. There the authors use a relativistic quark model finding that the calculated branching ratio increases from 0.29%, for infinite heavy quark mass, to 0.40% when $1/m_q$ corrections are taken into account. Although the value is still far from the $\sim 1\%$ needed to explain the experimental discrepancy, the size of the corrections suggests that a complete calculation may further approach the 1% result.

In this work we shall perform a full determination of $\mathcal{B}(B^+ \rightarrow D'^{(*)} l^+ \nu)$ within the framework of the constituent quark model described in Ref. [8]. The model

has recently been applied to mesons containing heavy quarks obtaining a satisfactory description of many physical observables: spectra [9, 10], strong decays and reactions [11, 12], and semileptonic and nonleptonic B and B_s decays into orbitally excited charmed and charmed-strange mesons [13, 14]. We will use the factorization approximation which gave a satisfactory explanation of the decays analyzed in Refs. [13, 14]. The form factors that parametrize the $\Gamma(B \rightarrow D'l\nu)$ decay also appear, evaluated at $q^2 = m_\pi^2$, in the non-leptonic decay $B \rightarrow D'\pi$ evaluated in factorization approximation. The latter decay, if experimentally accessible, could be used to extract information on the form factors near $q^2 = 0$. In this work we also evaluate the $\bar{B}^0 \rightarrow D'^+\pi^-$ branching ratio and its branching fraction relative to the $\bar{B}^0 \rightarrow D^+\pi^-$ decay.

The paper is organized as follows: In Sec. II, we describe the constituent quark model predictions for the first radially excited S -wave states paying special attention to their strong decays. Sec. III is dedicated to explain the theoretical framework through which we calculate the $\mathcal{B}(B^+ \rightarrow D'^*l^+\nu)$ and $\mathcal{B}(\bar{B}^0 \rightarrow D'^+\pi^-)$. Our results are shown in Sec. IV. We summarize our conclusions in Sec. V.

II. CONSTITUENT QUARK MODEL PREDICTIONS FOR $2S$ STATES

All the details on the constituent quark model we use have been described in Ref. [8] and we will only sketch here its main features. The model is based on the assumption that the constituent quark mass of the light quarks is due to the spontaneous chiral symmetry breaking of the QCD Lagrangian. To restore the original symmetry an interaction term, due to Goldstone-Boson exchanges, appears between light quarks. This interaction is added to the perturbative One-Gluon Exchange (OGE) and the non-perturbative confining interactions. In the heavy quark sector, chiral symmetry is explicitly broken and Goldstone-boson exchanges do not appear. Therefore, the corresponding potential for the system stems from the nonrelativistic reduction of the OGE interaction and the confinement component. Explicit formulae and model parameters used herein can be found in Refs. [9, 13].

Concerning the new discovered mesons, $D(2550)$ and $D^*(2600)$, we predict masses of 2.70 GeV and 2.75 GeV which are larger than the experimental ones, 2.54 GeV and 2.61 GeV. While masses are large, the goodness of the meson wave functions has been tested through their strong decays. Those were evaluated in Ref. [11] in which a modification of the phenomenological 3P_0 decay model was proposed. The strength γ of the decay interaction is scale-dependent being a function of the reduced mass of the quark-antiquark pair of the decaying meson. In this way a satisfactory global description of strong decays of mesons which belong to charmed, charmed-strange, hidden charm and hidden bottom sectors was achieved [11]. Using physical masses for the $2S$ states, we obtained the

$D(2550)$ as $nJ^P = 20^-$		
Channel	$\Gamma_{^3P_0}$	$\mathcal{B}_{^3P_0}$
$D^*\pi$	131.90	99.87
$D_0^0\pi$	0.18	0.13
total	132.07	100

TABLE II. Open-flavor strong decay widths, in MeV, and branchings, in %, of the $D(2550)$ meson with quantum numbers $nJ^P = 20^-$.

$D^*(2600)$ as $nJ^P = 21^-$		
Channel	$\Gamma_{^3P_0}$	$\mathcal{B}_{^3P_0}$
$D\pi$	10.84	11.19
$D^*\pi$	54.10	55.83
$D\eta$	11.86	12.24
$D_s K$	8.73	9.01
$D^*\eta$	9.65	9.95
$D_1\pi$	0.28	0.29
$D_1'\pi$	1.44	1.49
$D_2^*\pi$	0.01	0.00
total	96.91	100

TABLE III. Open-flavor strong decay widths, in MeV, and branchings, in %, of the $D^*(2600)$ meson with quantum numbers $nJ^P = 21^-$.

results shown in Tables II and III.

The $D(2550)$ meson has been only seen in the decay mode $D^*\pi$, thus its possible spin-parity quantum numbers up to $J = 3$ are $J^P = 0^-, 1^+, 2^-$ and 3^+ . It is the lower in mass of the newly discovered mesons and within the possible assignments, the 0^- is the most plausible. Assuming it is a $2S, J^P = 0^-$ state, its total width, shown in Table II, predicted by the 3P_0 model is in very good agreement with the experimental value given by the BaBar Collaboration.

The $D^*(2600)$ meson decays into $D\pi$ and $D^*\pi$ final states. Thus, its possible quantum numbers are $J^P = 1^-, 2^+$ and 3^- . The helicity-angle distribution of $D^*(2600)$ is found to be consistent with $J^P = 1^-$. Moreover, its mass makes it the perfect candidate to be the spin partner of the $D(2550)$ meson. Again, the total decay width predicted by the 3P_0 model, assuming it is a $2S, J^P = 1^-$ state, is in good agreement with the experimental data. Besides, we predict the ratio of branching fractions

$$\frac{\mathcal{B}(D^*(2600)^0 \rightarrow D^+\pi^-)}{\mathcal{B}(D^*(2600)^0 \rightarrow D^{*+}\pi^-)} = 0.20 \quad (2)$$

in reasonable agreement with experiment, $0.32 \pm 0.02 \pm 0.09$ [4].

In Tables II and III we also show the contribution of each channel to the total decay width of the $D'^{(*)}$ states. In both cases we obtain that the decay widths of these mesons into $1P$ states are much smaller than the ones into $1S$ states. This is in contrast to Ref. [1] where the authors find plausible that the $D'^{(*)}$ decay rates to $1S$

and $1P$ charmed states may be comparable. That was used in Ref. [1] as a possible explanation of the so called $1/2$ versus $3/2$ puzzle. However, we studied this issue within our model in Ref. [13] where we observed similar B semileptonic decay rates into the two $j_q^P = 1/2^+$ and $j_q^P = 3/2^+$ doublets, being our results for the different channels in agreement with experiment.

III. THE $B^+ \rightarrow D'^{(*)}l^+\nu_l$ AND $B^0 \rightarrow D'^{(*)}\pi$ DECAY WIDTH

The presence of the heavy quark in the initial and final meson states in these decays considerably simplifies

$$\begin{aligned} \frac{\langle D'(p') | \bar{\Psi}_c(0) \gamma^\mu (1 - \gamma_5) \Psi_b(0) | B(p) \rangle}{\sqrt{m_B m_{D'}}} &= h_+(w)(v + v')^\mu + h_-(w)(v - v')^\mu, \\ \frac{\langle D'^*(p') | \bar{\Psi}_c(0) \gamma^\mu (1 - \gamma_5) \Psi_b(0) | B(p) \rangle}{\sqrt{m_B m_{D'^*}}} &= h_v(w) \epsilon^{\mu\nu\alpha\beta} \epsilon_\nu^* v'_\alpha v_\beta \\ &\quad - i[-h_{A_1}(w)(w + 1)\epsilon^{*\mu} + h_{A_2}(w)(\epsilon^* \cdot v)v^\mu + h_{A_3}(w)(\epsilon^* \cdot v)v'^\mu], \end{aligned} \quad (3)$$

where $v(v')$ is the four velocity of the $B(D'^{(*)})$ meson, $\epsilon^{0123} = -1$, ϵ^μ is a polarization vector of the final vector

their theoretical description. Let us start our analysis in the infinitely heavy quark limit, $m_Q \rightarrow \infty$. In this limit the heavy quark symmetry arises. This leads to a considerable reduction of the number of independent form factors which are necessary for the description of heavy-to-heavy semileptonic decays. For example, in this limit only one form factor is necessary for the semileptonic B decay to S -wave D mesons. It is important to note that the heavy quark symmetry requires that matrix elements between a B meson and an excited D meson should vanish at zero recoil as a result of the orthogonality of the wave functions.

As the D' and D'^* states have 0^- and 1^- quantum numbers, the hadronic matrix elements for the semileptonic transition can be parameterized in terms of form factors as [15]

charmed meson and the form factors h_i are dimensionless functions of the product of four-velocities $w = v \cdot v'$. The differential $d\Gamma/dw$ decay widths are given by [15]

$$\begin{aligned} \frac{d\Gamma}{dw}(B^+ \rightarrow D'l^+\nu_l) &= \frac{G_F^2 |V_{cb}|^2 m_B^5}{48\pi^3} (w^2 - 1)^{3/2} r^3 (1 + r)^2 G^2(w), \\ \frac{d\Gamma}{dw}(B^+ \rightarrow D'^*l^+\nu_l) &= \frac{G_F^2 |V_{cb}|^2 m_B^5}{48\pi^3} (w^2 - 1)^{3/2} (w + 1)^2 r^{*3} (1 - r^*)^2 \left[1 + \frac{4w}{w + 1} \frac{1 - 2wr^* + r^{*2}}{(1 - r^*)^2} \right] F^2(w), \end{aligned} \quad (4)$$

where G_F is the Fermi decay constant, $|V_{cb}|$ the modulus of the Cabibbo-Kobayashi-Maskawa matrix element for

a $b \rightarrow c$ transition and $r^{(*)} = m_{D'^{(*)}}/m_B$. As for $G(w)$ and $F(w)$, they are given in term of the form factors as

$$\begin{aligned} G(w) &= h_+(w) - \frac{1 - r}{1 + r} h_-(w), \\ F^2(w) &= \left\{ 2(1 - 2wr^* + r^{*2}) \left[h_{A_1}^2(w) + \frac{w - 1}{w + 1} h_V^2(w) \right] \right. \\ &\quad \left. + \left[(1 - r^*)h_{A_1}(w) + (w - 1)(h_{A_1}(w) - h_{A_3}(w) - r^*h_{A_2}(w)) \right]^2 \right\} \times \left\{ (1 - r^*)^2 + \frac{4w}{w + 1} (1 - 2wr^* + r^{*2}) \right\}^{-1}. \end{aligned} \quad (5)$$

Similarly to the semileptonic $B^+ \rightarrow D^{(*)}l^+\nu_l$ case we have that, in the limit of very large heavy quark masses,

heavy quark symmetry predicts that all form factors are given in terms of just one Isgur-Wise function $\xi(w)$. One

has in that limit

$$h_+(w) = h_V(w) = h_{A_1}(w) = h_{A_3}(w) = \xi(w), \quad (6)$$

while

$$h_-(w) = h_{A_2}(w) = 0. \quad (7)$$

From these results one obtains in that limit

$$G(w) = F(w) = \xi(w). \quad (8)$$

Heavy quark symmetry at the point of zero recoil ($w = 1$) implies $\xi(1) = 0$ in the $B \rightarrow D'^{(*)}$ case since the radial parts of the wave functions for the $D'^{(*)}$ and B mesons are orthogonal in the infinitely heavy quark mass limit. Thus, the value of $\xi(w)$ near zero recoil comes entirely from corrections beyond that limit. This is different from the $B \rightarrow D^{(*)}$ case where $\xi(1) = 1$ in that limit.

As mentioned in Ref. [1], the nonleptonic $\bar{B}^0 \rightarrow D'^+\pi^-$ decay could also give valuable information on $F(w)$ and $G(w)$, as in factorization approximation the width of this process is related to the form factors involved in the semileptonic decay. Factorization approximation has been proven to be correct for $B \rightarrow D\pi$ in the infinite heavy quark mass limit [16], and we expect it should also work for decays B into $D'\pi$.

Following Ref. [17], we calculate the ratio $\mathcal{B}(\bar{B}^0 \rightarrow D'^+\pi^-)/\mathcal{B}(\bar{B}^0 \rightarrow D^+\pi^-)$ which in factorization approximation is given by

$$\begin{aligned} \frac{\mathcal{B}(\bar{B}^0 \rightarrow D'^+\pi^-)}{\mathcal{B}(\bar{B}^0 \rightarrow D^+\pi^-)} &= \left(\frac{m_B^2 - m_{D'}^2}{m_B^2 - m_D^2} \right)^2 \times \\ &\times \left(\frac{\lambda(m_B^2, m_{D'}^2, m_\pi^2)}{\lambda(m_B^2, m_D^2, m_\pi^2)} \right)^{1/2} \left| \frac{f_+^{B \rightarrow D'}(0)}{f_+^{B \rightarrow D}(0)} \right|^2, \end{aligned} \quad (9)$$

where $\lambda(a, b, c) = (a + b - c)^2 - 4ab$, and the $f_+(q^2)$ form factor is related with h_\pm via

$$\begin{aligned} f_+(q^2) &= \frac{1}{2} \left(\sqrt{\frac{m_{D'}}{m_B}} + \sqrt{\frac{m_B}{m_{D'}}} \right) h_+(w) \\ &+ \frac{1}{2} \left(\sqrt{\frac{m_{D'}}{m_B}} - \sqrt{\frac{m_B}{m_{D'}}} \right) h_-(w). \end{aligned} \quad (10)$$

Note q^2 and w are related through $q^2 = m_B^2 + m_{D'}^2 - 2m_B m_{D'} w$. If the $\mathcal{B}(\bar{B}^0 \rightarrow D'^+\pi^-)$ branching ratio is measured experimentally, it could be used to extract information on $f_+^{B \rightarrow D'}(0)$.

IV. RESULTS

In the calculation we use physical masses for the $D'^{(*)}$ mesons. In Fig. 1 we show the different form factors evaluated in our model for the $B \rightarrow D'^{(*)}$ transitions. For the sake of comparison we also show in a different panel the corresponding ones for the $B \rightarrow D^{(*)}$ transitions.

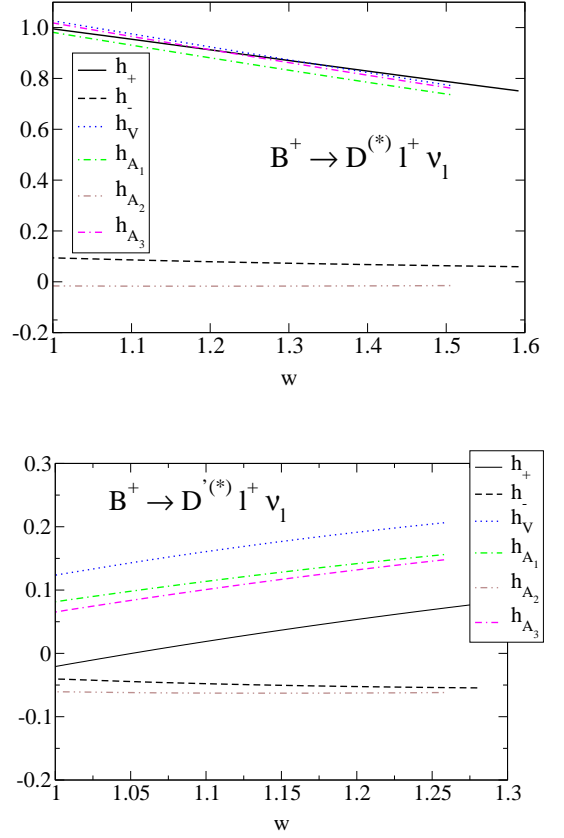


FIG. 1. Upper panel: Form factors for the $B^+ \rightarrow D'^{(*)} l^+ \nu_l$ transition evaluated in our model. Lower panel: The same for the $B^+ \rightarrow D'^{(*)} l^+ \nu_l$ transition.

We see that, even for the actual heavy quark masses the relations, in Eqs. (6) and (7) are approximately satisfied for the $B \rightarrow D^{(*)}$ case over the whole w range. Deviations are expected due to the finite heavy quark masses and the difference between m_b and m_c . For the $B \rightarrow D'^{(*)}$ decays those differences are magnified by the fact that in the infinite heavy quark mass limit we have $\xi(1) = 0$ in this case.

The $F(w)$ and $G(w)$ factors are depicted in Fig. 2. Our results at maximum recoil, $F(w_{\max}) = 0.2$ and $G(w_{\max}) = 0.1$, are compatible with the estimates in Ref. [1]

$$F(w_{\max}) = 0.25 \pm 0.15, \quad G(w_{\max}) = 0.15 \pm 0.1 \quad (11)$$

obtained adapting the light cone sum rule (LCSR) calculation of Ref. [18].

Integrating the differential decay width we obtain $\mathcal{B}(B^+ \rightarrow D' l^+ \nu_l) = (0.012 \pm 0.006)\%$ and $\mathcal{B}(B^+ \rightarrow D'^* l^+ \nu_l) = (0.097 \pm 0.015)\%$, where theoretical uncertainties have been estimated varying the different model parameters within 10% of their central values. For the case of total strong decay widths calculated in Tables II and III, we have seen that this 10% variation in the parameters induces changes which are smaller than the experimental error bars. For the sum of the two

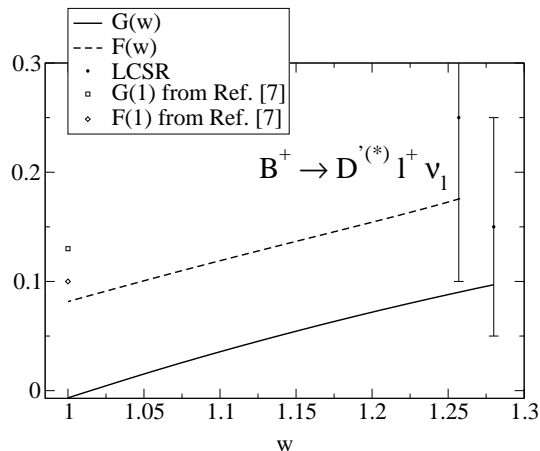


FIG. 2. $G(w)$ and $F(w)$ factors for the $B^+ \rightarrow D'^{(*)} l^+ \nu_l$ and $B^+ \rightarrow D'^{*} l^+ \nu_l$ transitions. We show with error bars the estimates for maximum recoil obtained in Ref. [1] adapting the light cone sum rule calculation of Ref. [18]. We also show the $1/m_Q$ corrected $G(1)$ and $F(1)$ values obtained in Ref. [7] using the relativistic quark model.

semileptonic branching ratios, we thus obtain $\mathcal{B}(B^+ \rightarrow D'^{(*)} l^+ \nu_l) = (0.109 \pm 0.016)\%$. Although this branching ratio is larger than those found by Refs. [5, 6] it is still a factor of ten smaller than the expectation in Ref. [1]. By looking at the individual ratios we also find that $\mathcal{B}(B^+ \rightarrow D' l^+ \nu_l)$ is smaller than $\mathcal{B}(B^+ \rightarrow D'^{*} l^+ \nu_l)$, in agreement with Refs. [5, 6].

Our results for $G(w)$ and $F(w)$ at zero recoil differ from the values obtained in Ref. [7] using the relativistic quark model. The discrepancy, clearly visible in Fig. 2, explains why our branching ratios are much smaller than the ones in Ref. [7]. The change is larger for $F(1)$ which also explains why $\mathcal{B}(B^+ \rightarrow D' l^+ \nu_l) > \mathcal{B}(B^+ \rightarrow D'^{*} l^+ \nu_l)$ in Ref. [7].

Concerning the non-leptonic decay our theoretical result, obtained within the factorization approximation, is

$$\frac{\mathcal{B}(\bar{B}^0 \rightarrow D'^+ \pi^-)}{\mathcal{B}(\bar{B}^0 \rightarrow D^+ \pi^-)} = 0.011 \pm 0.004, \quad (12)$$

which combined with the experimental value for $\mathcal{B}(\bar{B}^0 \rightarrow D^+ \pi^-) = (2.68 \pm 0.13) \times 10^{-3}$ gives for $\mathcal{B}(\bar{B}^0 \rightarrow D'^+ \pi^-) \sim 3 \times 10^{-5}$, sufficiently large to be measured experimentally.

V. CONCLUSIONS

We have performed a theoretical calculation of the branching ratio for the $B^+ \rightarrow D'^{(*)} l^+ \nu_l$ decays within the framework of the constituent quark model described in Ref. [8].

We find branching ratios much smaller than expectations in Ref. [1]. However, the results are sensitive to the amount of orthogonality between the B and $D'^{(*)}$ wave

functions and the latter depend on the quark model used. In order to check that sensitivity, we have performed an estimation of the theoretical uncertainties in our calculation, finding individual branching ratios can change at most by 50%. Our results would not then confirm that these contributions can explain the difference between the inclusive $\mathcal{B}(B^+ \rightarrow X_c l^+ \nu)$ rate and the various exclusive channels.

Concerning the $1/2$ versus $3/2$ puzzle there is no need for a large branching ratio into the $D'^{(*)}$ states to solve it. In fact, it was already shown in Ref. [13] that our model predicts similar B semileptonic decay rates into the two $j_q^P = 1/2^+$ and $j_q^P = 3/2^+$ doublets, being our results for the different channels in agreement with experiment. To us, this apparent puzzle appears only when one works in the infinite heavy quark mass limit and neglects corrections on the inverse of the heavy quark masses.

We have also evaluated, in factorization approximation, the non-leptonic $\mathcal{B}(\bar{B}^0 \rightarrow D'^+ \pi^-)$ branching fraction. The latter reaction may give additional information on the size of the form factors involved in the semileptonic decay [1, 17] provided it can be measured in B -factories or at LHCb in the near future.

ACKNOWLEDGMENTS

This work has been partially funded by Ministerio de Ciencia y Tecnología under Contract Nos. FPA2010-21750-C02-02 and FIS2011-28853-C02-02, by the European Community-Research Infrastructure Integrating Activity 'Study of Strongly Interacting Matter' (Hadron-Physics3 Grant No. 283286) by the Spanish Ingenio-Consolider 2010 Program CPAN (CSD2007-00042) and by U. S. Department of Energy, Office of Nuclear Physics, contract No. DE-AC02-06CH11357.

- [1] F. U. Bernlochner, Z. Ligeti, and S. Turczyk, Phys. Rev. D **85**, 094033 (2012).
- [2] V. Morénas, A. Le Yaouanc, L. Oliver, O. Pène, and J.-C. Raynal, Phys. Rev. D **56**, 5668 (1997).
- [3] I. Bigi, B. Blossier, A. Le Yaouanc, L. Oliver, O. Pène, J.-C. Raynal, A. Oyanguren, and P. Roudeau, The European Physical Journal C **52**, 975 (2007).
- [4] P. del Amo Sanchez et al. (BaBar Collaboration), Phys.Rev. **D82**, 111101 (2010).
- [5] D. Scora and N. Isgur, Phys.Rev. **D52**, 2783 (1995).
- [6] T. B. Suzuki, T. Ito, S. Sawada, and M. Matsuda, Progress of Theoretical Physics **91**, 757 (1994).
- [7] D. Ebert, R. Faustov, and V. Galkin, Phys.Rev. **D62**, 014032 (2000).
- [8] J. Vijande, F. Fernández, and A. Valcarce, Journal of Physics G: Nuclear and Particle Physics **31**, 481 (2005).
- [9] J. Segovia, A. M. Yasser, D. R. Entem, and F. Fernández, Phys. Rev. D **78**, 114033 (2008).
- [10] J. Segovia, A. M. Yasser, D. R. Entem, and F. Fernández, Phys. Rev. D **80**, 054017 (2009).
- [11] J. Segovia, D. Entem, and F. Fernandez, Phys. Lett. **B715**, 322 (2012).
- [12] J. Segovia, D. Entem, and F. Fernandez, Phys. Rev. D **83**, 114018 (2011).
- [13] J. Segovia, C. Albertus, D. R. Entem, F. Fernández, E. Hernández, and M. A. Pérez-García, Phys. Rev. D **84**, 094029 (2011).
- [14] J. Segovia, C. Albertus, E. Hernández, F. Fernández, and D. R. Entem, Phys. Rev. D **86**, 014010 (2012).
- [15] A. V. Manohar and M. B. Wise, Camb. Monogr. Part. Phys. Nucl. Phys. Cosmol. **10**, 1 (2000).
- [16] C. W. Bauer, D. Pirjol, and I. W. Stewart, Phys. Rev. Lett. **87**, 201806 (2001).
- [17] D. Becirevic, B. Blossier, A. Gerardin, A. L. Yaouanc, and F. Sanfilippo, Nucl. Phys. **B872**, 313 (2013), 1301.7336.
- [18] S. Faller, A. Khodjamirian, C. Klein, and T. Mannel, Eur.Phys.J. **C60**, 603 (2009).