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SHIFT IN WEAK PHASE γ DUE TO CP ASYMMETRIES IN D DECAYS TO TWO PSEUDOSCALAR MESONS

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A difference of several tenths of a percent has been observed between the direct CP asymmetries of $D^0 \to K^+K^-$ and $D^0 \to \pi^+\pi^-$. It has been noted recently that CP asymmetries in such singly-Cabibbo-suppressed (SCS) decays can affect the determination of the weak phase γ using the Gronau-London-Wyler method of comparing rates for $B^+ \to DK^+$ and $B^- \to DK^-$, where D is a superposition of D^0 and \overline{D}^0 decaying to a CP eigenstate. Using an analysis of the CP asymmetries in SCS decays based on a $c \to u$ penguin amplitude with standard model weak phase but enhanced by CP-conserving strong interactions, we estimate typical shifts in γ of several degrees and pinpoint measurements which would reduce uncertainties to an acceptable level.

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I Introduction

The precise determination of phases of the Cabibbo-Kobayashi-Maskawa (CKM) matrix is crucial to the understanding of CP violation. At present there appears to be reasonable agreement on magnitudes and phases of CKM matrix elements [1, 2]. However, discrepancies among different determinations of these quantities can signal new physics, for example due to new heavy particles entering into loop diagrams. Consequently, it is essential to pursue the widest variety of measurements of CKM elements.

One quantity which is determined indirectly with reasonable accuracy but whose direct measurement has lagged with respect to many others is the weak phase γ , related to CKM elements V_{ij} by $\gamma = \text{Arg}(-V_{ub}^*V_{ud}/V_{cb}^*V_{cd})$. A promising method for measuring γ directly, proposed by Gronau, London, and Wyler (GLW) [3], compared rates for $B^+ \to DK^+$ and $B^- \to DK^-$, where D is a superposition of D^0 and \overline{D}^0 decaying to a CP eigenstate. In the

initial formulation of this method, CP violation in charm decays was assumed negligible, as suggested by standard model (SM) estimates [4].

Variants of the GLW method include $B^{\pm} \to DK^{*\pm}$, $D^*(\to D\pi^0, D\gamma)K^{\pm}$ and $B^0 \to DK^{*0}$ where D decays to CP eigenstates, and processes of this kind in which D^0 and \bar{D}^0 decay to a common flavor state such as $K^-\pi^+$ [5] or to a three-body self-conjugate final state such as $K_S\pi^+\pi^-$ [6]. Results obtained in these processes have been reported by the BABAR [7, 8], Belle [9, 10], CDF [11], and LHCb [12, 13, 14, 15] collaborations.

A value of several tenths of a percent has now been seen for ΔA_{CP} , the difference between the CP asymmetries of $D^0 \to K^+K^-$ and $D^0 \to \pi^+\pi^-$ [16, 17]. These two asymmetries have been included in a recent experimental study by LHCb of $B^\pm \to DK^\pm$ [13], concluding that their effect on determining γ is marginal at the current level of experimental precision. Refs. [18, 19] have shown that unless CP violation in D decays is taken into account, the determination of γ via the GLW method can be shifted from its true value by up to several degrees.

Three of us have previously assumed that CP violation in charm decays is due to a penguin amplitude with the SM phase but enhanced by CP-conserving strong-interaction effects [20, 21, 22]. The possibility of such an enhancement was pointed out some time ago, in analogy to the likely enhancement of penguin amplitudes in $K \to 2\pi$ decays [23, 24]. A large number of authors have suggested that asymmetries at the level observed in ΔA_{CP} cannot be excluded within the CKM framework [25]. A consistent description of SCS CP-violating charm decays was found in Refs. [20, 21, 22], and predictions were made for correlations between CP asymmetries in several decays of charmed mesons to pairs of light pseudoscalar mesons P.

In the present paper we apply this description to $B^{\pm} \to DK^{\pm}, D \to \pi^+\pi^-, K^+K^-$, studying within the CKM framework shifts in γ due to CP violation in $D \to PP$ decays. We find shifts of up to a few degrees as noted in Refs. [18, 19], where no specific scheme has been used for CP violation and no correlations existed between CP asymmetries in D decays. We identify the most crucial measurements for reducing the uncertainty in effects of these shifts to acceptable levels, i.e., below effects of other uncertainties.

We review the GLW method in Sec. II allowing for CP violation in charm decays, using observables involving minimal systematic uncertainties. Present information on direct CP asymmetries in SCS D decays to two pseudoscalars is summarized in Sec. III. The approach of Ref. [20] is then outlined in Sec. IV, and applied to obtain predictions for shifts in γ in Sec. V. We summarize in Sec. VI.

II GLW method in presence of charm CP violation

We shall be concerned with a single source of information on γ : the decays $B^{\pm} \to DK^{\pm}$, with D decaying to a CP-even eigenstate such as $f_D = \pi^+\pi^-$ or K^+K^- . Our notation will follow that of Ref. [19]. We define

$$A(B^{-} \to D^{0}K^{-}) \equiv A_{B}$$

$$A(B^{-} \to \overline{D}^{0}K^{-}) \equiv A_{B}r_{B}e^{i(\delta_{B}-\gamma)}$$

$$A(D^{0} \to f_{D}) \equiv A_{f},$$

$$(1)$$

where we have taken a strong phase to be zero in $B^- \to D^0 K^-$ with no loss of generality. By CP conjugation we then have

$$A(B^{+} \to \overline{D}^{0}K^{+}) \equiv A_{B}$$

$$A(B^{+} \to D^{0}K^{+}) \equiv A_{B}r_{B}e^{i(\delta_{B}+\gamma)}$$

$$A(\overline{D}^{0} \to f_{D}) \equiv \overline{A}_{f}.$$
(2)

The parameters r_B and δ_B are measurable by combining information from $B^{\pm} \to DK^{\pm}$, where neutral D mesons decay to CP-eigenstates, flavor-specific states or $K_S\pi^+\pi^-$. Current values taken from Ref. [1] are:

$$r_B = 0.099 \pm 0.008 \;, \; \delta_B = (110 \pm 15)^{\circ} \;.$$
 (3)

The magnitudes of the amplitudes $|A_f|$ and $|\overline{A}_f|$ are measurable through the CP-averaged branching ratio for $D^0 \to f$ and $\overline{D}^0 \to f$ (giving $|A_f|^2 + |\overline{A}_f|^2$) and the direct CP asymmetry

$$A_{CP}^{\text{dir}}(f) = \frac{|A_f|^2 - |\overline{A}_f|^2}{|A_f|^2 + |\overline{A}_f|^2} \,. \tag{4}$$

We define the weak (CP-violating) phase $\alpha_f \equiv \text{Arg}(A_f/\overline{A}_f)$. Its value is, as yet, unspecified. If ϕ is taken as the phase of A_f we have

$$A_f = |A_f|e^{i\phi} \; ; \quad \overline{A}_f = |\overline{A}_f|e^{i(\phi - \alpha_f)} \; .$$
 (5)

Using the above definitions we may now construct the following amplitudes:

$$A(B^{-} \to f_{D}K^{-}) = A_{B} A_{f} + \overline{A}_{f} A_{B} r_{B} e^{i(\delta_{B} - \gamma)}$$

$$= A_{B} \left(|A_{f}| + |\overline{A}_{f}| r_{B} e^{i(\delta_{B} - \gamma - \alpha_{f})} \right) e^{i\phi} , \qquad (6)$$

$$A(B^{+} \to f_{D}K^{+}) = A_{B} \overline{A}_{f} + A_{f} A_{B} r_{B} e^{i(\delta_{B} + \gamma)}$$

$$= A_{B} \left(|\overline{A}_{f}| + |A_{f}| r_{B} e^{i(\delta_{B} + \gamma + \alpha_{f})} \right) e^{i(\phi - \alpha_{f})} . \qquad (7)$$

The squared magnitudes of Eqs. (6) and (7) give [19]

$$|A(B^{-} \to f_{D}K^{-})|^{2} = |A_{B}|^{2} \left(|A_{f}|^{2} + r_{B}^{2} |\overline{A}_{f}|^{2} + 2 r_{B} |A_{f}| |\overline{A}_{f}| \cos(\delta_{B} - \gamma - \alpha_{f}) \right),$$
 (8)

$$|A(B^+ \to f_D K^+)|^2 = |A_B|^2 \left(|\overline{A}_f|^2 + r_B^2 |A_f|^2 + 2 r_B |A_f| |\overline{A}_f| \cos(\delta_B + \gamma + \alpha_f) \right).$$
 (9)

Adding and subtracting the above equations we may form quantities that are relevant in constructing the GLW observables:

$$|A(B^{-} \to f_{D}K^{-})|^{2} + |A(B^{+} \to f_{D}K^{+})|^{2} = |A_{B}|^{2}(|A_{f}|^{2} + |\overline{A}_{f}|^{2})$$

$$\left(1 + r_{B}^{2} + 2 \, r_{B}\cos\delta_{B}\cos(\gamma + \alpha_{f})\sqrt{1 - (A_{CP}^{\text{dir}}(f))^{2}}\right) , \tag{10}$$

$$|A(B^{-} \to f_{D}K^{-})|^{2} - |A(B^{+} \to f_{D}K^{+})|^{2} = |A_{B}|^{2}(|A_{f}|^{2} + |\overline{A}_{f}|^{2})$$

$$\left(A_{CP}^{\text{dir}}(1 - r_{B}^{2}) + 2 r_{B} \sin \delta_{B} \sin(\gamma + \alpha_{f}) \sqrt{1 - (A_{CP}^{\text{dir}}(f))^{2}}\right). \tag{11}$$

The last expression differs from a similar one in Ref. [19] by a term $(1-r_B^2)$ $(|A_f|^2-|\overline{A}_f|^2)$, which vanishes only in the absence of direct CP violation in charm and hence cannot be neglected.

We now take the expressions for A_f and \overline{A}_f to be [19]

$$A_f = |A_f^0|(1 + r_f e^{i(\delta_f - \gamma)}), \quad \overline{A}_f = |A_f^0|(1 + r_f e^{i(\delta_f + \gamma)}),$$
 (12)

where A_f^0 is the amplitude in the absence of a CP-violating term, and we have assumed that the source of CP violation has the SM phase $-\gamma$ as in Ref. [20]. The direct CP asymmetry [Eq. (4)] is then given by

$$A_{CP}^{\text{dir}}(f) = \frac{2r_f \sin \delta_f \sin \gamma}{1 + r_f^2 + 2r_f \cos \delta_f \cos \gamma} . \tag{13}$$

The fact that $A_{CP}^{\text{dir}}(f)$ is of order a few times 10^{-3} in $D^0 \to \pi^+\pi^-$ and $D^0 \to K^+K^-$ (see Tables I and II in Section III) suggests that r_f in these processes is also of this order as argued in Refs. [20, 25]. Our subsequent analysis (in particular the discussion in Secs. IV and V) applies also to larger value of r_f , for instance of order 10^{-2} , with an order of magnitude further suppression provided by $\sin \delta_f$. We ignore the fine-tuned solution where r_f is large, but the strong phases in these decays are of order 10^{-3} . One can show that

$$\alpha_f = -\tan^{-1} \left(\frac{2r_f \cos \delta_f \sin \gamma + r_f^2 \sin 2\gamma}{1 + 2r_f \cos \delta_f \cos \gamma + r_f^2 \cos 2\gamma} \right)$$

$$\approx -A_{CP}^{\text{dir}}(f) \cot \delta_f , \qquad (14)$$

where the last approximation holds to leading order in r_f .

It has been suggested in Ref. [26] that when applying the GLW method one normalizes the CP-averaged rate for $B^{\pm} \to f_D K^{\pm}$ by that for $B^{\pm} \to f_D \pi^{\pm}$,

$$R_{K/\pi}^{f} \equiv \frac{\Gamma(B^{-} \to f_{D}K^{-}) + \Gamma(B^{+} \to f_{D}K^{+})}{\Gamma(B^{-} \to f_{D}\pi^{-}) + \Gamma(B^{+} \to f_{D}\pi^{+})} , \qquad (15)$$

and one takes the ratio of this fraction and a corresponding fraction for D^0 flavor state,

$$R(K/\pi) \equiv \frac{\Gamma(B^- \to D^0 K^-)}{\Gamma(B^- \to D^0 \pi^-)} \ . \tag{16}$$

Significant experimental systematic uncertainties cancel in these fractions [7, 9, 11, 13]. Defining ratios of amplitudes and strong phases in $B^- \to D\pi^-$ in analogy with $B^- \to DK^-$,

$$\frac{A(B^- \to \bar{D}^0 \pi^-)}{A(B^- \to D^0 \pi^-)} \equiv r_{B(\pi)} e^{i(\delta_{B(\pi)} - \gamma)} , \qquad (17)$$

one may express the double fraction

$$R_{CP+}^{f} \equiv \frac{R_{K/\pi}^{f}}{R(K/\pi)} \tag{18}$$

in terms of γ and these parameters.

In the absence of CP violation in $D^0 \to f_D$, one has [26]

$$R_{CP+}^{f} = \frac{1 + r_B^2 + 2 \, r_B \cos \delta_B \cos \gamma}{1 + r_{B(\pi)}^2 + 2 \, r_{B(\pi)} \cos \delta_{B(\pi)} \cos \gamma} \,, \tag{19}$$

where the parameter $r_{B(\pi)}$ is expected to be very small, $r_{B(\pi)} \sim r_B \tan^2 \theta_C \sim 0.005$. [See Eq. (3).] We note that in the approximation of neglecting CP violation in $D^0 \to f_D$ the ratio $R_{K/\pi}^f$ may be defined as $R_{K/\pi}^f \equiv [\Gamma(B^- \to D_{CP+}K^-) + \Gamma(B^+ \to D_{CP+}K^+)]/[\Gamma(B^- \to D_{CP+}\pi^-) + \Gamma(B^+ \to D_{CP+}\pi^+)]$. Consequently this ratio and the double ratio R_{CP+}^f do not depend on f_D .

Including CP violation in $D^0 \to f_D$ one finds an expression for R_{CP+}^f which depends on f_D through the CP asymmetry $A_{CP}^{\text{dir}}(f)$,

$$R_{CP+}^{f} = \frac{1 + r_B^2 + 2 \, r_B \cos \delta_B \cos(\gamma + \alpha_f) \sqrt{1 - (A_{CP}^{\text{dir}}(f))^2}}{1 + r_{B(\pi)}^2 + 2 \, r_{B(\pi)} \cos \delta_{B(\pi)} \cos(\gamma + \alpha_f) \sqrt{1 - (A_{CP}^{\text{dir}}(f))^2}} \,. \tag{20}$$

Neglecting corrections in R_{CP+}^f which are quadratic in $A_{CP}^{\text{dir}}(f)$ [$\mathcal{O}(10^{-5})$] and using Eq. (14), we note that corrections linear in $A_{CP}^{\text{dir}}(f) \sim \text{few} \times 10^{-3}$ are multiplied by r_B and are therefore negligible relative to $R_{CP+}^f = 1 + \mathcal{O}(r_B)$. Thus, a comparison of Eqs. (19) and (20) shows that the determination of γ is not affected in a significant way by including $A_{CP}^{\text{dir}}(f)$ in R_{CP+}^f .

The other measurable quantity used in the GLW method is the CP asymmetry A_{CP+}^f ,

$$A_{CP+}^{f} \equiv \frac{\Gamma(B^{-} \to f_{D}K^{-}) - \Gamma(B^{+} \to f_{D}K^{+})}{\Gamma(B^{-} \to f_{D}K^{-}) + \Gamma(B^{+} \to f_{D}K^{+})} . \tag{21}$$

In the absence of CP violation in $D^0 \to f_D$, this asymmetry may be defined as $[\Gamma(B^- \to D_{CP+}K^-) - \Gamma(B^+ \to D_{CP+}K^+)]/[\Gamma(B^- \to D_{CP+}K^-) + \Gamma(B^+ \to D_{CP+}K^+)]$ which is independent of f_D and is given by [26]

$$A_{CP+}^f = \frac{2 r_B \sin \delta_B \sin \gamma}{1 + r_B^2 + 2 r_B \cos \delta_B \cos \gamma} . \tag{22}$$

When including CP nonconservation in $D^0 \to f_D$ the asymmetry A_{CP+}^f becomes dependent on $A_{CP}^{\text{dir}}(f)$. Neglecting terms quadratic in $A_{CP}^{\text{dir}}(f)$, one finds

$$A_{CP+}^{f} = \frac{A_{CP}^{\text{dir}}(f)(1 - r_B^2) + 2 \, r_B \sin \delta_B \sin(\gamma + \alpha_f)}{1 + r_B^2 + 2 \, r_B \cos \delta_B \cos(\gamma + \alpha_f)} \,. \tag{23}$$

The two terms in the numerator and the last term in the denominator involve corrections linear in $A_{CP}^{\text{dir}}(f)$ modifying the expression (22) for the case of no direct asymmetry.

We note that an expression independent of $A_{CP}^{\text{dir}}(f)$ similar to (22), but with an opposite overall sign and an $\mathcal{O}(r_B^2)$ correction with opposite sign, describes the asymmetry for Cabibbo-favored D^0 decays to CP-odd eigenstates (such as $K_S\phi$ and $K_S\pi^0$) where CP violation is negligible in the CKM framework,

$$A_{CP-}^f = -\frac{2 r_B \sin \delta_B \sin \gamma}{1 + r_B^2 - 2 r_B \cos \delta_B \cos \gamma} . \tag{24}$$

A precise measurement of this asymmetry could avoid uncertainties from $A_{CP}^{\mathrm{dir}}(f)$. Writing

$$A_{CP+}^{f} = \frac{2 r_B \sin \delta_B \sin \gamma_{\text{eff}}}{1 + r_B^2 + 2 r_B \cos \delta_B \cos \gamma_{\text{eff}}}, \qquad (25)$$

we assume a measurement of A_{CP+}^f from which γ_{eff} is determined. Our purpose is then to study the shift $\delta\gamma \equiv \gamma - \gamma_{\text{eff}}$ as a function of $A_{CP}^{\text{dir}}(f)$. Defining $\gamma + \alpha_f = \gamma_{\text{eff}} + \delta\gamma + \alpha_f \equiv \gamma_{\text{eff}} + x$, we expand the numerator and denominator in (23) to first order in x. Comparing this expression with (25), cross-multiplying the two ratios, cancelling the leading terms and keeping terms linear in x and $A_{CP}^{\text{dir}}(f)$, one finds

$$\delta\gamma = -\alpha_f - A_{CP}^{\text{dir}}(f) \left[\frac{1 - r_B^2}{2r_B \sin \delta_B} \frac{1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma_{\text{eff}}}{(1 + r_B^2) \cos \gamma_{\text{eff}} + 2r_B \cos \delta_B} \right]$$

$$\approx A_{CP}^{\text{dir}}(f) \left[\cot \delta_f - \frac{1 - r_B^2}{2r_B \sin \delta_B} \frac{1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma_{\text{eff}}}{(1 + r_B^2) \cos \gamma_{\text{eff}} + 2r_B \cos \delta_B} \right]$$

$$\approx 2r_f \cos \delta_f \sin \gamma_{\text{eff}} - A_{CP}^{\text{dir}}(f) \left[\frac{1 - r_B^2}{2r_B \sin \delta_B} \frac{1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma_{\text{eff}}}{(1 + r_B^2) \cos \gamma_{\text{eff}} + 2r_B \cos \delta_B} \right] . \quad (26)$$

While both corrections are exhibited as proportional to $A_{CP}^{\text{dir}}(f)$, the first term appears to diverge as $\delta_f \to 0$. Recalling that this correction is actually $\approx 2r_f \cos \delta_f \sin \gamma_{\text{eff}}$ [Eq. (13)], which is finite at $\delta_f = 0$, we will use the last expression in Sec. V. The second term in (26) illustrates an enhancement by $1/2r_B$ of the shift in γ due to $A_{CP}^{\text{dir}}(f)$ [18, 19].

We mention in passing two approximations which have been applied to the CP asymmetry in (23). Neglecting α_f [which is of the same order in r_f as $A_{CP}^{\text{dir}}(f)$, but leads to a correction linear in r_B] and approximating the overall coefficient of $A_{CP}^{\text{dir}}(f)$ by one, Eq. (23) reduces to an expression employed in Ref. [13],

$$A_{CP+}^{f} \approx \frac{2r_B \sin \delta_B \sin \gamma}{1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma} + A_{CP}^{\text{dir}}(f) . \tag{27}$$

A further approximation, keeping only $\mathcal{O}(r_B)$ in the first term, leads to [19]

$$A_{CP+}^f \simeq 2r_B \sin \delta_B \sin \gamma + A_{CP}^{\text{dir}}(f) \ . \tag{28}$$

A CP asymmetry in $B^{\pm} \to f_D K^{\pm}$ has been measured in Refs. [7, 11, 12] consistent with an estimate $A_{CP+}^f(B^{\pm} \to f_D K^{\pm}) \simeq 2r_B \sin \delta_B \sin \gamma \sim 0.15-0.20$. The current error in the world-averaged value [28], $A_{CP+} = 0.19 \pm 0.03$, is still too large for sensitivity to $A_{CP}^{\rm dir}(f)$. The corresponding error in the world-averaged measurement, $A_{CP-} = -0.11 \pm 0.05$ favoring an opposite sign as anticipated, is somewhat larger.

A much smaller asymmetry is expected in $B^{\pm} \to D\pi^{\pm}$ where we estimated $r_{B(\pi)} \sim 0.005$. This asymmetry is given by an expression similar to (23),

$$A_{CP+}^{f}(B \to f_{D}\pi) = \frac{A_{CP}^{\text{dir}}(f)(1 - r_{B(\pi)}^{2}) + 2 \, r_{B(\pi)} \sin \delta_{B(\pi)} \sin(\gamma + \alpha_{f})}{1 + r_{B(\pi)}^{2} + 2 \, r_{B(\pi)} \cos \delta_{B(\pi)} \cos(\gamma + \alpha_{f})}$$

$$\approx 2 \, r_{B(\pi)} \sin \delta_{B(\pi)} \sin \gamma + A_{CP}^{\text{dir}}(f) \, . \tag{29}$$

The two contributions, which in principle may be disentangled by measuring also $A_{CP-}(B \to f_D \pi) \approx -2 \ r_{B(\pi)} \sin \delta_{B(\pi)} \sin \gamma$, are of comparable magnitudes, each less than a percent. Thus, while the CP-averaged rate for $B^{\pm} \to f_D \pi^{\pm}$ is suitable for normalization [see Eq. (15)], a useful measurement of the corresponding asymmetry does not seem feasible in the foreseeable future.

III Present information on A_{CP}^{dir}

Dedicated measurements of the difference $\Delta A_{CP} \equiv A_{CP}^{\text{dir}}(D^0 \to K^+K^-) - A_{CP}^{\text{dir}}(D^0 \to \pi^+\pi^-)$ (in which many systematic errors cancel) have been performed by the LHCb [16] and CDF [17] Collaborations, while Belle has combined independent measurements of the two asymmetries [27] to obtain a value of ΔA_{CP} . The results are shown in Table I. We shall assume that measured asymmetries are equal to direct ones, neglecting possible contributions from indirect (mixing-induced) asymmetries which would lead to slightly different averages [1, 28].

Table I: Experimental results on $\Delta A_{CP} \equiv A_{CP}^{\rm dir}(D^0 \to K^+K^-) - A_{CP}^{\rm dir}(D^0 \to \pi^+\pi^-)$.

Reference	Value (%)
LHCb [16]	$-0.82 \pm 0.21 \pm 0.11$
CDF[17]	$-0.62 \pm 0.21 \pm 0.10$
Belle [27]	$-0.87 \pm 0.41 \pm 0.06$
Average	-0.74 ± 0.15

Table II: Experimental results on some direct CP asymmetries in D decays.

Decay	Reference	Value (%)
$D^0 \to \pi^+\pi^-$	CDF [29]	$0.22 \pm 0.24 \pm 0.11$
	Belle [27]	$0.55 \pm 0.36 \pm 0.09$
	Average	0.33 ± 0.22
$D^0 o K^+ K^-$	CDF [29]	$-0.24 \pm 0.22 \pm 0.09$
	Belle [27]	$-0.32 \pm 0.21 \pm 0.09$
	Average	-0.28 ± 0.16
$D^+ \to K^+ \overline{K}^0$ (a)	BaBar [30]	$0.46 \pm 0.36 \pm 0.25$
	Belle [27, 31]	$0.08 \pm 0.28 \pm 0.14$
	Average	0.21 ± 0.25

(a) After subtraction of CP asymmetry due to $K^0 - \overline{K}^0$ mixing.

The average in Table I will be used in the next Section to constrain the magnitude of a SM penguin amplitude as a function of its strong phase. (Slightly different averages were used in Refs. [?] and [19].) In addition weak constraints on this strong phase will be seen to result from measured CP asymmetries in individual final states, quoted in Table II.

IV Charm CP violation with enhanced SM penguin

In Ref. [20] three of us have calculated CP asymmetries for several $D \to PP$ decays, where $P = \pi, K$, assuming that the nonzero value of A_{CP}^{dir} is due to a SM penguin amplitude with

Table III: Magnitudes T_f and phases ϕ_T^f for some $D \to PP$ processes.

Decay	$ T_f $	$\phi_T^f = \operatorname{Arg}(T_f)$
mode	$(10^{-7} {\rm GeV})$	(degrees)
$D^0 o \pi^+\pi^-$	4.70	-158.5
$D^0 o K^+K^-$	8.48	32.5
$D^0\to\pi^0\pi^0$	3.51	60.0
$D^+ o K^+ \overline{K}^0$	6.87	-4.2

the weak phase of the standard model $c \to b \to u$ loop diagram, but with a CP-conserving enhancement as if due to the strong interactions. In this case the magnitude and strong phase of this amplitude P_b are correlated in order to fit the observed CP asymmetry, allowing the prediction of CP asymmetries for other singly-Cabibbo-suppressed modes. We refer the reader to that work for details, but outline the method briefly here.

For the decay of a charmed meson D to any final state f we are defining a direct CP asymmetry using the same convention as in (4)

$$A_{CP}^{\text{dir}}(f) \equiv \frac{\Gamma(D \to f) - \Gamma(\bar{D} \to \bar{f})}{\Gamma(D \to f) + \Gamma(\bar{D} \to \bar{f})} \ . \tag{30}$$

We take the CP-conserving amplitudes from a flavor-SU(3) description of charm decays presented previously [32, 33]. A new ingredient [20] with respect to that work is a U-spin breaking $c \to u$ penguin amplitude whose $V_{cd(s)}^*V_{ud(s)}$ term reproduces satisfactorily decay rates for singly-Cabibbo-suppressed (SCS) processes, while its $V_{cb}^*V_{ub}$ term accounts for ΔA_{CP} . This scheme allows the prediction of other CP asymmetries in SCS charmed meson decays.

Denoting by δ_f a phase defined in Ref. [20] as ϕ^f , we write the amplitude for a decay $D \to f$ in a manner similar to (12)

$$\mathcal{A}(D \to f) \equiv A_f = |T_f| e^{i\phi_T^f} (1 + r_f e^{i(\delta_f - \gamma)}) . \tag{31}$$

Here T_f represents terms with the weak phase of the tree-level terms contributing to that amplitude, ϕ_T^f is its strong phase, r_f is the ratio of the magnitude of the CP-violating penguin contribution to that of T_f , $-\gamma$ is the weak phase of the CP-violating penguin, and δ_f is the strong phase of the CP-violating penguin relative to T_f . Here one has

$$\delta_f = \operatorname{Arg}(P_b) - \phi_T^f + \gamma , \quad P_b = pe^{i(\delta - \gamma)} ,$$
 (32)

leading to the relation $\delta_f = \delta - \phi_T^f$. The magnitudes T_f and phases ϕ_T^f for some $D \to PP$ processes [20] are summarized in Table III. For $D^0 \to \pi^0 \pi^0$, the amplitude must be multiplied by an additional factor of $-1/\sqrt{2}$ [20].

The CP asymmetries are then

$$A_{CP}^{\text{dir}}(f) = \frac{2 r_f \sin \gamma \sin \delta_f}{1 + r_f^2 + 2 r_f \cos \gamma \cos \delta_f}$$

$$= \frac{2 p |T_f| \sin \gamma \sin(\delta - \phi_T^f)}{|T_f|^2 + p^2 + 2 p |T_f| \cos \gamma \cos(\delta - \phi_T^f)},$$
(33)

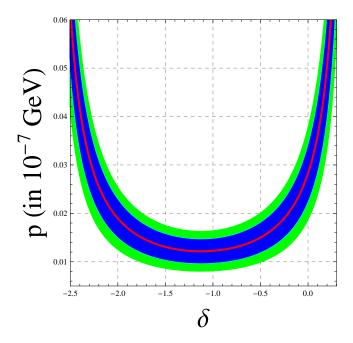


Figure 1: Magnitude p of the CP-violating penguin amplitude as a function of its strong phase δ . The red curve was obtained using the value $\Delta A_{CP} = -0.74\%$, while the inner (blue) and outer (green) bands respectively correspond to $\pm 1\sigma$ and $\pm 1.64\sigma$ shifts from this value, where $\sigma(\Delta A_{CP}) = 0.15\%$. The plot is shown only for $\gamma = 67.2^{\circ}$, as p is not very sensitive to the exact value of γ .

Taking $\gamma = (67.2^{+4.4}_{-4.6})^{\circ}$ from Ref. [1], the world-averaged asymmetry $\Delta A_{CP} = (-0.74 \pm 0.15)\%$ from Table I is used to constrain the magnitude p of the penguin amplitude as a function of its strong phase δ . The value of p, plotted in Fig. 1, is nearly constant at several tenths of a percent of the amplitudes in Table III for a wide range of δ . This corresponds to values of r_f of this order. The value of p and corresponding values of r_f are about an order of magnitude larger for extreme values of δ in Fig. 1. The constraint on p as a function of δ allows one to predict asymmetries for (e.g.) $D^0 \to \pi^+\pi^-, K^+K^-, \pi^0\pi^0$ and $D^+ \to K^+\bar{K}^0$, as plotted in Fig. 2 for $\gamma = 67.2^{\circ}$. Very similar results (not shown) are found for $\gamma = 71.6^{\circ}$ and 62.6° .

For much of the range of δ , $A_{CP}^{\rm dir}(\pi^+\pi^-)$ is predicted to be positive while $A_{CP}^{\rm dir}(K^+K^-)$ is predicted to be negative. (In the U-spin limit they would be equal and opposite.) This is consistent with the central values in Table II. However, the predicted central values for $A_{CP}^{\rm dir}(K^+\overline{K}^0)$ are negative for much of the range of δ , whereas the 2σ lower limit $A_{CP}^{\rm dir}(K^+\overline{K}^0) > -0.3$ would tend to favor values of $\delta > -\pi/2$. Improved measurements of all these individual CP asymmetries would of course be highly desirable.

V Predictions for shifts in weak phase γ

Taking the predicted values of A_{CP}^{dir} , Eq. (26) implies a shift in the weak phase γ associated with the use of each D-decay process with a CP-even final state. In Fig. 3 we present these shifts for the final states $\pi^+\pi^-$ and K^+K^- . In addition to the central value of shifts $\delta\gamma$ we also present errors in $\delta\gamma$ due to the variation of the various measurable parameters. In our

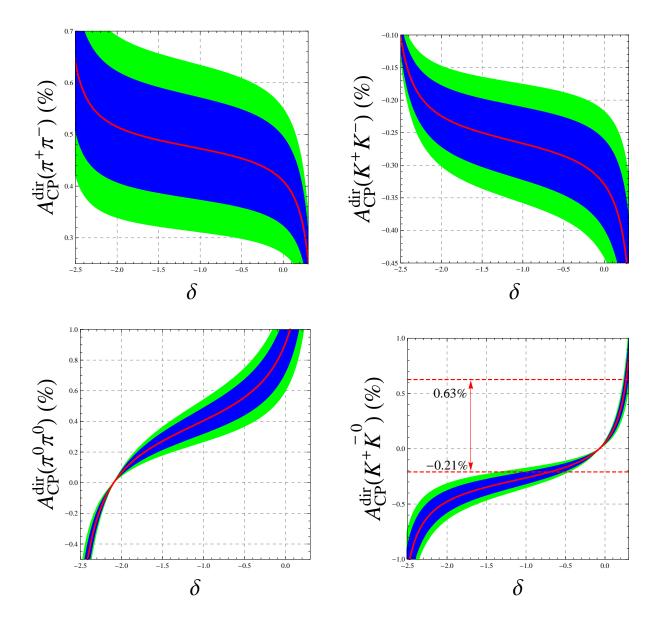


Figure 2: Direct CP asymmetries for some SCS $D \to PP'$ decays. Curves and bands as in Fig. 1. $\gamma = 67.2^{\circ}$ is assumed. Very similar plots (not shown) are obtained for $\gamma = 71.6^{\circ}$ and 62.6°. The dashed horizontal (red) lines in the lower right panel denote 90% C. L. limits based on the average of Belle [27, 31] and BaBar [30] results.

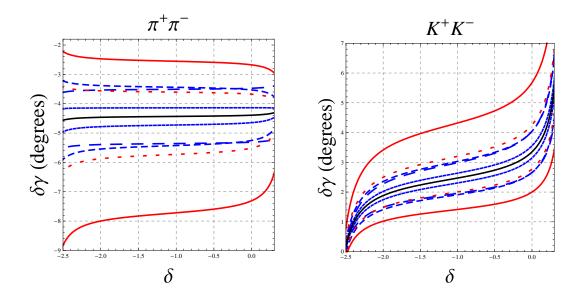


Figure 3: Shifts $\delta \gamma$ as calculated from Eq. (26) for $D^0 \to \pi^+\pi^-$ (left panel) and $D^0 \to K^+K^-$ (right panel). The solid central (black) curves denote the central value for $\delta \gamma$. Also shown are $\pm 1\sigma$ errors in r_B (short dashes [blue]), δ_B (medium dashes [blue]), and ΔA_{CP} (long dashes [blue]). The (red) dots represent the effect of $\pm 1\sigma$ shift in the measured value of γ on the central (black) curve. The solid outer (red) curves denote the effect of a $\pm 1\sigma$ shift in the measured value of γ on the curve that is obtained by adding in quadrature the errors in r_B , δ_B , and ΔA_{CP} . Here $\gamma = (67.2^{+4.4}_{-4.6})^{\circ}$.

calculations of the shifts $\delta \gamma$ we have used the following values of r_B , δ_B , and γ taken from Ref. [1]:

$$r_B = 0.099 \pm 0.008 \; , \; \delta_B = (110 \pm 15)^{\circ} \; , \; \gamma = (67.2^{+4.4}_{-4.6})^{\circ} \; .$$
 (34)

In Fig. 3 the central black curves represent $\delta\gamma$ as obtained from Eq. (26) using central values of the measurable parameters r_B , δ_B , ΔA_{CP} and γ . The errors in $\delta\gamma$ from the 1σ error in the measurement of the first three parameters are shown in blue using short, medium, and long dashes respectively. In order to obtain the effect of varying γ on the shifts $\delta\gamma$ we use Eq. (26) with the value of γ set to its $\pm 1\sigma$ limits given in Eq. (34), while the other parameters are held fixed at their respective central values. This effect is represented by the red dots in Fig. 3. In order obtain the overall error in $\delta\gamma$ we first add in quadrature the errors due to r_B , δ_B , and γ . We then estimate the effect of varying γ between its $\pm 1\sigma$ limits on the quadrature sum. This effect is represented by the solid red curves in Fig. 3.

We see in Fig. 3 that the central value of the shift in γ for the $\pi^+\pi^-$ state is nearly constant over the entire range of allowed values of the strong phase δ . This appears to be the effect of an accidental cancellation between a variation of A_{CP}^{dir} which is modest to begin with and a compensating factor due to the variation in δ_f for $\gamma = 67.2^{\circ}$. When the various sources of errors on $\delta\gamma$ are included, this no longer holds, as depicted by the 1σ boundary red curves in Fig. 3. On the other hand, $\delta\gamma$ obtained using the K^+K^- state shows appreciable variation ($\sim 7^{\circ}$) over the allowed range of δ . A similar exercise when performed using the $\pi^0\pi^0$ state yields an even larger variation in $\delta\gamma$. However, rate asymmetries involving multiple neutral pions in the final state are not expected to be measured with adequate precision in the foreseeable future. We have therefore chosen to omit the $\pi^0\pi^0$ decay mode

from the present discussion.

In view of the variety of dependences of direct CP asymmetries on δ , and different behavior of shifts in γ for $\pi^+\pi^-$ and K^+K^- final states, it would be beneficial to further pin down δ [e.g., with a better measurement of $A_{CP}^{\text{dir}}(K^+\overline{K}^0)$], and to apply the GLW determination of γ to the widest assortment of CP eigenstates in neutral D meson decays. After the appropriate shifts $\delta\gamma$ have been taken into account, inconsistencies in final values of γ obtained for different charm final states could point the way to effects of new physics.

VI Discussion and summary

The determination of the weak phase γ by means of the CP asymmetry in $B^{\pm} \to DK^{\pm}$, followed by the decay of the neutral D meson to a CP eigenstate [3], must take account of asymmetries in the decays of the neutral D mesons [13, 18, 19]. We have calculated the corresponding shifts $\delta\gamma$ in an approach which imagines these CP asymmetries as due to a $c \to u$ penguin amplitude with weak phase of the standard model but enhanced by (presumably nonperturbative) strong interaction effects beyond those anticipated by the majority of authors. The observed value $\Delta A_{CP} \equiv A_{CP}^{\text{dir}}(D^0 \to K^+K^-) - A_{CP}^{\text{dir}}(D^0 \to \pi^+\pi^-) = (-0.74 \pm 0.15)\%$ has been taken as a constraint, leading to a correlation between the magnitude p of the CP-violating penguin and its strong phase δ .

For $\gamma=67.2^{\circ}$ the central value of the shift associated with the decay $D^{0} \to \pi^{+}\pi^{-}$ is approximately $\delta\gamma(\pi^{+}\pi^{-}) \simeq -4.4^{\circ}$, with little dependence on the allowed range of the strong phase δ . However, the factor multiplying $A_{CP}^{\rm dir}(f)/2r_{B}$ in the last expression for $\delta\gamma$ in Eq. (26) is roughly inversely proprtional to $\cos\gamma$, which is fairly small and fairly sensitive to γ . Thus, when γ is varied within its currently allowed range of about $\pm 4.5^{\circ}$, the value of $\delta\gamma$ varies considerably. It is further affected by uncertainties in ΔA_{CP} , r_{B} , and δ_{B} , and acquires some dependence on δ .

The shift associated with $D^0 \to K^+K^-$ is of the other sign (as is A_{CP}^{dir}) and depends on both ΔA_{CP} and δ as well as the uncertainties in r_B and δ_B . Using measurements of A_{CP}^{dir} for both these two decays, with the help of improved knowledge of $A_{CP}^{\text{dir}}(D^+ \to K^+\overline{K}^0)$ to pin down δ , the uncertainty in γ due to CP violation in charm decay can be reduced to a level where it is no longer the dominant uncertainty when applying the GLW method to the decays $B^{\pm} \to DK^{\pm}$.

Let us be clear about the limitation of our study. The shift in γ we calculate using our $c \to u$ penguin amplitude model is based on measuring R_{CP+} and A_{CP+} in $B^- \to (\pi^+\pi^-)_D K^-$, $B^- \to (K^+K^-)_D K^-$ and their CP conjugates, taking r_B and δ_B as given. This assumes that one has measured r_B and δ_B first and then uses only these GLW processes to determine γ .

An actual analysis for determining r_B , δ_B , and γ in $B^{\mp} \to DK^{\mp}$ [8, 10, 11, 12, 13] combines information from D decays to CP eigenstates [3], flavor states [5] and three-body self-conjugate final states [6]. In this global analysis γ is also constrained by rates and asymmetries in $B \to DK$ where there is no direct CP violation in D decay, for instance in decays to flavor states and CP-odd eigenstates. [See Eq. (24)]. Thus any actual determination of γ from $B \to DK$ will involve a considerably smaller shift than we calculate.

Furthermore, it has been noted [26, 34, 35] that in the self-tagged decays $B^0 \to DK^{*0}$ the ratio r_B^* of $B^0 \to D^0K^{*0}$ and $B^0 \to \bar{D}^0K^{*0}$ amplitudes, both of which are color-

suppressed, is expected to be about three times larger than r_B defined in $B^+ \to DK^+$. We have seen an enhancement by $1/2r_B$ of the shift in γ due to $A_{CP}^{\text{dir}}(\pi^+\pi^-, K^+K^-)$ in $B^+ \to DK^+$. This implies that when applying the GLW method to $B^0 \to DK^{*0}$ the shift in γ due to these direct CP asymmetries in D^0 decays is expected to be about three times smaller than calculated above. First measurements of relevant observables in $B^0 \to DK^{*0}$ and its CP-conjugate have been reported very recently by the LHCb collaboration [15]. Early measurements of these processes have been performed by BABAR [36].

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