

CHCRUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

Constraining the unHiggs model with LHC data

Christoph Englert, Dorival Gonçalves Netto, Michael Spannowsky, and John Terning Phys. Rev. D **86**, 035010 — Published 9 August 2012 DOI: 10.1103/PhysRevD.86.035010

Constraining the Unhiggs with LHC data

Christoph Englert,^{1,*} Dorival Gonçalves Netto,^{2,†} Michael Spannowsky,^{1,‡} and John Terning^{3,§}

¹Institute for Particle Physics Phenomenology, Department of Physics,

²Institut für Theoretische Physik, Universität Heidelberg, 69120 Heidelberg, Germany

³Department of Physics, University of California, Davis, CA 95616, USA

Recent measurements by the ATLAS and CMS experiments have excluded the Standard Model Higgs boson in the high mass region, even if it is produced with a significantly smaller cross section than expected. The bounds are dominated by the non-observation of a signal in the clean gold-plated mode $h \rightarrow ZZ \rightarrow 4\ell$ and, hence, are directly related to the special role of the Higgs in electroweak symmetry breaking. A smaller cross section in comparison to the Standard Model is expected if the Higgs is realized as an unparticle in the Unhiggs scenario. With the LHC probing $\sigma/\sigma^{SM} < 1$, we can therefore reinterpret the $h \rightarrow ZZ \rightarrow 4\ell$ exclusion limits as bounds on the Unhiggs' scaling dimension. Throughout the high Higgs mass range, where we expect a large signal in the presence of the Standard Model Higgs for the 2011 ATLAS and CMS data sets, the observed limits translate into mild bounds on the Unhiggs scaling dimension in the high mass region.

I. INTRODUCTION

Recent results on Standard Model Higgs production at the LHC [1–5] have gained lots of attention throughout the high energy physics community. On the one hand, this is due to the tantalizing hints for a light Higgs boson around $m_h \simeq 125$ GeV. The implications of the observed excess have already been discussed in the literature [6], yet, it is too early to claim that the Higgs has been found and we might well observe a statistical fluctuation [7].

On the other hand, the 95% confidence level bounds published by ATLAS and CMS state that if a Higgs-like resonance is to be realized at higher masses, the Higgs boson is significantly underproduced or has suppressed branching fractions to the (partially) visible decay channels. This has triggered some effort in how to reconcile one or more heavy Higgs bosons in the light of this heavily constraining data through modified production cross sections [8], decays [9], or combinations of both [10].

The dominant channel which drives the exclusion bounds in the high Higgs mass regime is the clean Higgs decay channel to four leptons via two Z bosons [3, 5, 11]. This so-called "gold-plated" mode allows a great deal of Higgs "spectroscopy" as soon as the decay channel $h \rightarrow ZZ$ opens up. Statics in this channel is limited due to the branching ratios of the Z bosons to the light and clean leptons e^{\pm}, μ^{\pm} , but it benefits from a large branching ratio $h \rightarrow ZZ$ for heavy Higgs masses $\Gamma(h \rightarrow ZZ) \sim m_h^3/m_Z^2$. The dominant partial decay width to longitudinal W, Z is a direct consequence of electroweak symmetry breaking. The purely leptonic final state of $h \rightarrow 4\ell$ can be fully reconstructed and, hence, its merits range from line-shape measurements [12] to obtaining spin and CP of the reconstructed excess [13]. Of similar importance in the high Higgs mass region at the 14 TeV LHC are the semi-hadronic ZZ decay modes for boosted kinematics [14].

Avoiding a large branching ratio $h \to ZZ$, or in general $h \to VV, V = W^{\pm}, Z$, for heavy Higgs particles is theoretically challenging unless we allow for non-perturbative strong couplings [15]. The reason is that ordinary perturbative $\mathcal{O}(1)$ interactions of a minimally extended Higgs sector, *i.e.* the ones which do not arise from spontaneous symmetry breaking, cannot compete against the fast-growing partial decay width of the Higgs $\sim m_h^3$. Higgs-portal type interactions are pushed into a non-perturbative regime by requiring a vanishing $h \to ZZ$ phenomenology [9].

One way to reconcile a vanishing Higgs phenomenology in $h \to ZZ \to 4\ell$ in a controlled way is by turning to strongly coupled theories in the 't Hooft limit [16]. A playground, which serves as a model-building dictionary, is the AdS/CFT correspondence [17, 18] of Randall-Sundrum models [19]. While RS I type models predict a tower of scalar and/or vectorial resonances which can be tackled with standard search strategies in the VV final states [20, 21], the phenomenology of RS II models can be fundamentally different. Once put into a realistic form by introducing a weak breaking of conformal invariance via a modulation of the AdS metric towards the infrared [22], such models can be interpreted as "Unparticles" in Georgi's language [23]. It has been shown that such a non-local object can, in fact, be responsible for electroweak symmetry breaking, restoring the good high energy behavior of longitudinal gauge boson scattering [24], while it behaves very much like an ordinary Higgs in electroweak precision tests [25]. In essence, the model's gauge sector at low energies is similar to the SM. while this is not necessarily true for the Unhiggs-fermion sector [15]. Therefore every channel which allows crosstalk between the fermion and the gauge boson sector is a strong probe of such a mechanism of electroweak symmetry breaking.

Durham University, DH1 3LE, United Kingdom

^{*}Electronic address: christoph.englert@durham.ac.uk

[†]Electronic address: d.goncalves@thphys.uni-heidelberg.de

[‡]Electronic address: michael.spannowsky@durham.ac.uk

[§]Electronic address: terning@physics.ucdavis.edu

We organize this work as follows: Sec. II provides a recap of the model's properties to make this work selfcontained. In Sec. III we first validate our analysis strategy against the results of Refs. [3, 5]. In particular we show that we can reproduce the experiments' exclusion bounds in the Higgs mass region we are interested in. We subsequently compute the exclusion bounds on the Unhiggs model's parameters that are implied by the data of Refs. [3, 5] in Sec. IV. We give our conclusions in Sec. V.

II. THE MODEL

The gauge interactions of the Unhiggs field H follow from the effective lagrangian [24]

$$\mathcal{L} \supset H^{\dagger} \left(D^{\mu} D_{\mu} + \mu^2 \right)^{2-d} H \,, \tag{1}$$

where D_{μ} denotes the familiar $SU(2)_L \times U(1)_Y$ gauge covariant derivative, d < 2 is the Unhiggs field's scaling dimension and μ is the infrared cut-off of the conformal sector. Consequently, the gauge interactions of the Unhiggs can be dialed away by increasing d > 1. The naive growth with the center of mass energy of the longitudinal gauge boson scattering amplitude, which would eventually lead to unitarity violation if left un-tamed, is cured by non-local interactions [24]. Similar gauge cancellations in massive quark annihilation to longitudinal gauge bosons constrain the Unhiggs scaling dimension $d \lesssim 1.5$ [15]. $d \gtrsim 1.5$ implies modifications of the massive fermion sector by inducing non-local contributions. These can eventually alter also the Higgs phenomenology for low masses in *e.g.* loop-induced $h \to \gamma \gamma$, where the 125 GeV excess is observed. For small $d \simeq 1$ the effective theory that follows from Eq. (1) and the SM Yukawa sector is unitarity-conserving, and results in a similar Higgs phenomenology for Higgs masses below the Z and W^{\pm} thresholds.

Since the resulting Higgs field is manifestly non-local as a consequence of Eq. (1), so are the longitudinal gauge bosons, *i.e.* the would-be Nambu Goldstone bosons in unitary gauge. The Higgs two-point function is given by a pole at what would be interpreted as the physical Higgs particle (dubbed "Unhiggs" in the following) and a branch cut above the conformal symmetry breaking scale μ . The impact of this continuum is, however, phenomenologically irrelevant at the LHC for small d > 1since it is difficult to access the gauge boson's polarizations in a clean way in the context of Higgs production [15, 26]. The resulting contribution to the cross section of the order of a few percent in $pp \to h \to ZZ + X$, is difficult to isolate from background uncertainties, especially at the given luminosity $\mathcal{L} \simeq 5 \text{ fb}^{-1}$, which predicts only a couple of events in the decay leptons invariant mass tails. Hence search strategies will be sensitive to the modifications of the Unhiggs with respect to the SM Higgs.

Due to the modifications of the Higgs sector that arise from Eq. (1) after electroweak symmetry breaking, both the partial decay width (*i.e.* the line shape) and the production cross section are modified. More precisely, the Unhiggs propagator reads [24]

$$\Delta_H = -\frac{i}{(\mu^2 - q^2)^{2-d} - (\mu^2 - m_h^2)^{2-d}}.$$
 (2)

where m_h is the pole mass. The top-Yukawa coupling for $d \leq 1.5$ follows from $\mathcal{L} \supset (\lambda_t/\sqrt{2}) (v^d/\Lambda^{d-1}) \bar{t}_R t_L + \text{h.c.}$, where Λ is the model's cut-off scale (see Refs. [15, 24] for further details).

$$\frac{\Gamma^{\text{Unh}}}{\Gamma^{\text{SM}}} \simeq \frac{(\mu^2)^{d-1}}{2-d} \left(\frac{(\mu^2)^{2-d} - (\mu^2 - m_h^2)^{2-d}}{m_h^2}\right)^2 \frac{-\pi \mathcal{A}_d}{2\pi \sin(\pi d)} \frac{(\mu^2 - m_h^2)^{d-1}}{2-d},\tag{3a}$$

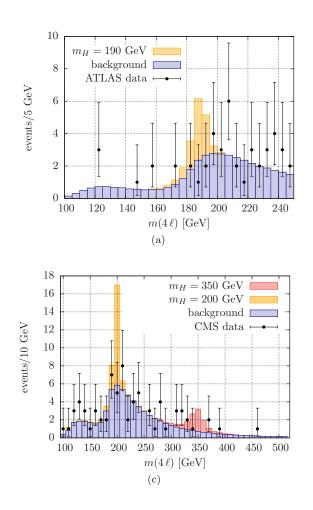
$$\frac{\sigma^{\text{Unh}}(gg \to H \to VV)}{\sigma^{\text{SM}}(gg \to H \to VV)} \simeq \left| \left(1 - \frac{m_h^2}{q^2} \right) \frac{\left[(\mu^2 - q^2)^{2-d} - \mu^{4-2d} \right]}{(\mu^2 - q^2)^{2-d} - (\mu^2 - m_h^2)^{2-d}} \right|_{q=0}^2, \tag{3b}$$

$${}^{\mathrm{M}}(gg \to H \to VV) \cong \left| \left({}^{1} - \frac{1}{q^{2}} \right) \frac{1}{(\mu^{2} - q^{2})^{2-d} - (\mu^{2} - m_{h}^{2})^{2-d}} \right|_{q^{2} = \sqrt{s}}, \tag{3b}$$

where

$$\mathcal{A}_{d} = \frac{16\pi^{5/2}}{(2\pi)^{2d}} \frac{\Gamma(d+1/2)}{\Gamma(d-1)\Gamma(2d)} \,. \tag{3d}$$

The above modification of width stems from the pole contribution and its decay to SM particles. This should be contrasted to an additional imaginary part that the



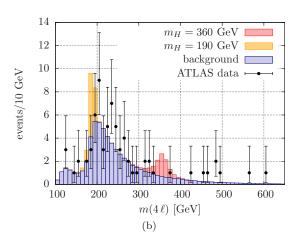


FIG. 1: ATLAS distributions and data (a), (b) (taken from Ref. [3]) and CMS distributions and data (c) (taken from Ref. [5]), which enter the hypothesis tests of Tab. I.

propagator Eq. (2) can pick up. Eq. (3b) gives an approximation for the pole contribution in terms of cross section times branching ratio. In the final analysis we use the full off-shell propagator including imaginary parts in Sec. IV, *i.e.* the one that arises from the conformal structure of the propagator and the one that arises from the decay of the m_h state. Doing so, we recover the SM propagators, widths and cross sections upon taking the limit $d \to 1$. This is also clear from Eq. (3a)-(3d), for $d \to 1$ we have $\sigma^{\text{Unh}}/\sigma^{\text{SM}}, \Gamma^{\text{Unh}}/\Gamma^{\text{SM}} \to 1$.

The $pp \rightarrow ZZ + X \rightarrow 4\ell + X$ channel is potentially sensitive to both of these modifications in the heavy mass region $m_h \gtrsim 200$ GeV, especially because the observed Higgs width is dominated by the physical one [3, 5]. For light Higgs particles the width is dominated by the detector resolution, also in the gold-plated $h \rightarrow ZZ$ decay mode (see *e.g.* [27]).

III. ELEMENTS OF THE ANALYSIS

Statistics

To formulate exclusion bounds on the Unhiggs model, we apply a binned log-likelihood ratio hypothesis test as formulated during the LEP2 era in the context of Higgs searches [28]. The test statistic is given by

$$Q = -2\log\frac{L(\text{data} | \text{Unhiggs} + \text{background})}{L(\text{data} | \text{background})}, \quad (4)$$

where L denotes the Poissonian likelihood, e.g.

$$L(\text{data} | \text{Unhiggs} + \text{background}) = \frac{N^n e^{-N}}{n!}, \quad (5)$$

where $N = (\sigma^{\text{Unh}} + \sigma^{\text{bkg}})\mathcal{L}$ is the number of expected events at a given luminosity and n is the number of actually observed events in the Unhiggs model. The generalization to binned histograms is straightforward.

The test statistic Eq. (4) is different from the profile likelihood which is employed by ATLAS and CMS [29] in its asymptotic behavior and in the treatment of uncertainties. Since the shape and systematic uncertainties are not publicly available, we neglect them throughout and take the distributions by ATLAS and CMS at face value.

It can be expected that the influence of marginalization over nuisance parameters [30] on the computed confidence level is not too important for this clean and well-reconstructible final state. Indeed, we compute 95%

Signal hypothesis	95%	CL exp	pected	95% CL observed			
Signal hypothesis	ATLAS CL_S		$MC+CL_S$	ATLAS	CL_S	$MC+CL_S$	
$m_h = 190 \text{GeV}$	0.81	0.76	0.74	0.52	0.58	0.58	
$m_h = 360 \text{GeV}$	0.79	0.76	0.76	0.57	0.56	0.57	
Signal hypothesis	95%	CL exp	pected	95% CL observed			
	CMS	CL_S	$MC+CL_S$	CMS	CL_S	$MC+CL_S$	
$m_h = 200 \text{GeV}$	0.50	0.49	0.50	0.62	0.52	0.60	
$m_h = 350 \text{GeV}$	0.73	0.67	0.67	0.76	0.78	0.73	

TABLE I: Comparison of expected and observed 95% confidence level bounds for the various Higgs mass hypotheses of Fig. 1. We quote the numbers extracted from the ATLAS and CMS publications [3, 5]. " CL_S " gives the result of the hypothesis test with the histograms and the data of Fig. (1) as input. "MC+ CL_S " refers to the signal histograms generated with our Monte Carlo tool chain.

upper confidence levels using the CLs method [31] in Tab. I, which are in good agreement with the results from ATLAS and CMS. This holds especially for large Higgs masses which we want to study in detail for the purpose of this work. Given this agreement with ATLAS and CMS, our implementation potentially reproduces the findings by ATLAS and CMS at the percent level, well inside the 1σ uncertainty bands for heavy Higgs bosons $m_h \gtrsim 225$ GeV. For $m_h \lesssim 225$ GeV our CL_S implementation shows deviations of $\mathcal{O}(15\%)$ for the experiments' histograms as input. We interpret this deviation as the influence of systematics which plays an important role when the Z bosons are soft and off-shell. Since the resulting distributions' shape uncertainties are not publicly known we cannot reproduce a quantitatively reliable agreement for $m_h \lesssim 200 \text{ GeV}$ within the limitations of our naive detector simulation (for details see below). This region requires the full experimental analysis flow, which is not available to us. Hence, we focus in the following on the heavy Higgses $m_h \gtrsim 200$ GeV.

Event generation and MC Analysis

For the event generation we use a modified version of MadGraph v4 [32], which implements the Unhiggs model as described in Ref. [15]. The parton level events are subsequently showered with Pythia v6 [33]. To account for detector resolution effects we process the showered events with PGS [34]. In order to reliably reproduce the SM Higgs signal distributions that enter the hypothesis tests of ATLAS and CMS, we have performed a dedicated tune of PGS, leading to good agreement of the $m(4\ell)$ distribution at the percent level for heavy Higgs masses $m_h \gtrsim 225$ GeV.

We adopt the cuts from the respective experimental analysis [3, 5]. Concretely this means selecting events with two same-flavor and opposite-sign lepton pairs $\ell^+\ell^-$ with the following features required by each experiment:

ATLAS — The leptons are required to have transverse momenta of at least $p_T^{\ell} > 7$ GeV, where two of them need to pass from a further constraint of $p_T^{\ell} > 20$ GeV.

$m_{4\ell}$ [GeV	/] ≤120	130	140	150	160	165	180	190	≥ 200
$m_{Z_2}^{\min}$ [Ge	V] 15	20	25	30	30	35	40	50	60

TABLE II: Threshold masses for m_{Z_2} with $m_{4\ell}$ used in the ATLAS analysis.

They are reconstructed within the geometrical coverage of $|\eta_e| < 2.47$ and $|\eta_{\mu}| < 2.7$ with a separation $\Delta R > 0.1$. The first reconstructed Z boson, m_{Z_1} , is required to be on-shell by taking its invariant mass closest to the Z boson mass within the range $|m_Z - m_{Z_1}| < 15$ GeV. The invariant mass of the remaining lepton pair, denoted by m_{Z_2} , is required to be $m_{Z_2}^{\min} < m_{Z_2} < 115$ GeV. Where the threshold mass, $m_{Z_2}^{\min}$, depends on the reconstructed four-lepton mass as denoted by the Tab. II.

CMS — The leptons are required to have transverse momenta of $p_T^e > 7$ GeV and $p_T^{\mu} > 5$ GeV being in the pseudorapidity range of $|\eta_e| < 2.5$ and $|\eta_{\mu}| < 2.4$, respectively. One of Z bosons is reconstructed by the pair e^+e^- or $\mu^+\mu^-$ within the mass range 50 GeV $< m_{Z_1} < 120$ GeV and with the transverse momenta for the lepton pair $p_{T,2e} > 20$ GeV or $p_{T,2\mu} > 10$ GeV. The other Z boson is selected by the remaining same flavor combination $\ell^+\ell^-$ and is denoted by Z_2 . It is required that 12 GeV $< m_{Z_2} < 120$ GeV with the additional constrain $m_{4\ell} > 100$ GeV. If more than one combination satisfies these criteria for Z_2 the one with the highest p_T leptons is chosen.

We compare the resulting confidence levels in Tab. 1, where "MC+CL_S" denotes the hypothesis test with the background hypothesis extracted from the experiments and with the signal distributions generated by the described tool chain. In total we find very good agreement for high masses, so that our analysis set-up is sufficiently validated to confront the Unhiggs hypothesis with data

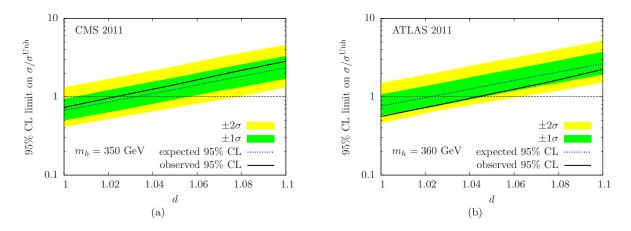


FIG. 2: Observed (solid) and expected (dashed) 95% confidence level exclusion for $\sigma/\sigma^{\text{Unh}}$ for (a) CMS and (b) ATLAS. Note that for d = 1 we recover the "MC+CL_S" values of Tab. I, *i.e.* the SM exclusion.

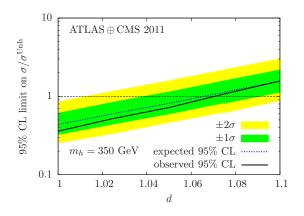


FIG. 3: Combined observed (solid) and expected (dashed) exclusion by ATLAS and CMS for $\sigma/\sigma^{\text{Unh}}$.

IV. BOUNDS ON UNHIGGS PRODUCTION FROM $ZZ \rightarrow 4\ell$

We show the expected and observed 95% confidence level curves for the high mass values quoted in Tab. I in Fig. 2. Throughout, we plot exclusion limits in terms of $\sigma/\sigma^{\text{Unh}}$ as function of the Unhiggs scaling dimension d, keeping $\mu = 600 \text{ GeV}$ fixed. $\sigma/\sigma^{\text{Unh}}$ dominantly depends on d for this choice, and we discuss the influence of μ on the exclusion limits in detail later on. We also show the ATLAS \oplus CMS combination for $m_h = 350 \text{ GeV}$ in Fig. 3.

In Fig. 5 we show the dependence of $\sigma^{\text{Unh}}/\sigma^{\text{SM}}$ on μ for a representative value of the Higgs mass. From this figure we see that a variation of μ in the signal hypothesis leaves our findings for d largely unmodified unless we face a situation where the conformal symmetry breaking scale μ is close to the Unhiggs pole mass. If we consider the situation $\mu < m_h$ there is an additional contribution to the width [24], which eventually can yield $\sigma^{\text{Unh}}/\sigma^{\text{SM}} > 1$. Consequently this region is already now excluded at

the 95% confidence level by the combination, and the observed limits on d are slightly larger than for $\mu > m_h$, with a stronger dependence on μ .

The shape of the exclusion contours of Figs. 2 and 3 is representative for the entire considered mass range 200 GeV $\leq m_h \leq 400$ GeV, while the quantitative details of the observed exclusion on d is mostly driven by actually observed data around the m_h signal hypothesis. Local deficits and excesses in the data do typically not change this situation, *i.e.* when we see a deficit in data this typically carries over to a larger-than-expected d for fixed m_h, μ . The combination of both searches in regions where the data is consistent with the background allows to impose even stronger bounds on Unhiggs production, as can be seen from the comparison of Figs. 2 with 3.

From Fig. 1 (and Refs. [3, 5]), it is clear that for some Higgs masses we observe excesses $\sigma/\sigma^{\rm SM} > 1$ by the in-

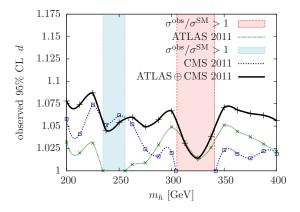


FIG. 4: Observed exclusion of the Unhiggs model ($\mu = 600 \text{ GeV}$) for ATLAS (green, dashed), CMS (blue, dotted) and the mark data excesses $\sigma/\sigma^{\text{SM}} > 1$, so that bounds on Unhiggs production cannot be imposed by ATLAS (blue) and CMS (red) individually.

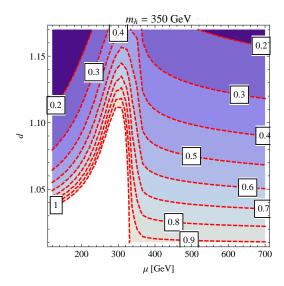


FIG. 5: Representative $\sigma^{\text{Unh}}/\sigma^{\text{SM}}$ as a function of $d \geq 1.01$ and μ for $m_h = 350$ GeV. The blank area correponds to $\sigma^{\text{Unh}}/\sigma^{\text{SM}} > 1$ and is already excluded. For $d \leq 1.01$, $\sigma^{\text{Unh}}/\sigma^{\text{SM}}$ quickly approaches 1 from above. The observed exclusion by the combination coincides with $\sigma^{\text{Unh}}/\sigma^{\text{SM}} = 0.5$.

dividual experiments. Since the Unhiggs model generically predicts smaller cross sections in $pp \rightarrow ZZ + X$ for $\mu > m_h$ than encountered in the SM, we are therefore not able to put bounds on the Unhiggs model in these particular regions for the individual analyses. CMS and ATLAS, however, observe these excesses in different Higgs mass regions. This allows us to constrain the full considered Higgs mass range in the Unhiggs model from the combination of the ATLAS and CMS searches, yielding $\sigma/\sigma^{\rm SM} < 1$ over the entire mass range 200 GeV \leq $m_h \leq 400$ GeV. This is shown in Fig. 4, where we scan the observed 95% CL on d over the mass range $200 \text{ GeV} \le m_h \le 400 \text{ GeV}$ (again for $\mu = 600 \text{ GeV}$). The shaded areas represent Higgs mass regions where ATLAS and CMS cannot constrain the Unhiggs model individually. The combination of the two experiments amounts to a combined bound of $d \sim 1.06$. In the region where no bound can be imposed by the ATLAS experiment, the observed exclusion is $\sigma/\sigma^{\rm SM} \simeq 1.5$, which results from a rather large $\simeq 1.8\sigma$ upward fluctuation. This excess

- ATLAS collaboration, ATLAS-CONF-2012-019. CMS collaboration, CMS-PAS-HIG-12-008.
- [2] ATLAS Collaboration, arXiv:1112.2577 [hep-ex], ATLAS-CONF-2011-162, ATLAS-CONF-2011-163.
- [3] ATLAS collaboration, ATLAS-CONF-2011-161.
- [4] CMS Collaboration, CMS-PAS-HIG-11-029, CMS-PAS-HIG-11-030, CMS-PAS-HIG-11-031, CMS-PAS-HIG-11-032.
- [5] CMS collaboration, CMS-PAS-HIG-11-025.
- [6] D. Carmi, A. Falkowski, E. Kuflik and T. Volan-

weakens the observed CMS exclusion in the combination, which holds also vice-versa for $m_h \simeq 325$ GeV in a more pronounced way.

In total, the resulting SM bounds translate into only mild bounds on Unhiggs production, *i.e.* $d \gtrsim 1.1$. Expecting $d = \mathcal{O}(1)$ in the Unhiggs scenario, these constraints are not strong enough to rule out the existence of the Unhiggs scenario. This, however, should be possible with the future increase of luminosity and center of mass energy.

V. SUMMARY AND CONCLUSIONS

The LHC has tested Standard Model Higgs production at 7 TeV center of mass energy with a luminosity of about 5 fb⁻¹. Significant bounds on the SM Higgs could be established in 2011 by both ATLAS and CMS. The combination of both data sets allows to impose constraints $\sigma/\sigma^{\text{SM}} < 1$ over the range 200 GeV $\leq m_h \leq 400$ GeV in the $pp \rightarrow ZZ + X \rightarrow 4\ell + X$ channel. We show that we can reproduce the experiments sensitivity to very good approximation, thus allowing us to understand the observed underproduction if a Higgs is realized in this particular mass range in terms of Unhiggs symmetry breaking. We find that the data only mildly constrains the Unhiggs scenario $d \gtrsim 1.1$, with a very flat dependence of these results on the high scale conformal symmetry breaking scale as long as $\mu > m_h$.

Acknowledgments

We cordially thank the organizers of the Heidelberg New Physics Forum for a stimulating environment. C.E. and M.S. thank the University of California Davis for the kind hospitality during the time when parts of this work was done. C.E. also would like to thank Markus Schumacher for helpful discussions. C.E. acknowledges funding by the Durham Junior Research Fellowship scheme. D.G. acknowledges support by the International Max Planck Research School for Precision Tests. J.T. was supported by the Department of Energy under grant DE-FG02-91ER406746.

sky, arXiv:1202.3144 [hep-ph]. A. Azatov, R. Contino and J. Galloway, arXiv:1202.3415 [hep-ph]. J. R. Espinosa, C. Grojean, M. Muhlleitner and M. Trott, arXiv:1202.3697 [hep-ph].

- [7] P. P. Giardino, K. Kannike, M. Raidal and A. Strumia, arXiv:1203.4254 [hep-ph]. J. Ellis and T. You, arXiv:1204.0464 [hep-ph].
- [8] B. A. Dobrescu, G. D. Kribs and A. Martin, arXiv:1112.2208 [hep-ph]. V. Ilisie and A. Pich, arXiv:1202.3420 [hep-ph].

- [9] C. Englert, J. Jaeckel, E. Re and M. Spannowsky, Phys. Rev. D 85 (2012) 035008. C. Cheung and Y. Nomura, arXiv:1112.3043 [hep-ph].
- [10] H. de Sandes and R. Rosenfeld, Phys. Rev. D 85, 053003 (2012).
 C. Englert, T. Plehn, M. Rauch, D. Zerwas and P. M. Zerwas, Phys. Lett. B 707 (2012) 512.
- [11] J. M. Campbell, W. T. Giele and C. Williams, arXiv:1204.4424 [hep-ph].
- [12] I. Low, P. Schwaller, G. Shaughnessy and C. E. M. Wagner, Phys. Rev. D 85 (2012) 015009. S. Goria, G. Passarino and D. Rosco, arXiv:1112.5517 [hep-ph].
- [13] S. Y. Choi, D. J. Miller, M. M. Muhlleitner and P. M. Zerwas, Phys. Lett. B **553**, 61 (2003). C. P. Buszello, I. Fleck, P. Marquard and J. J. van der Bij, Eur. Phys. J. C **32** (2004) 209.
- [14] C. Hackstein and M. Spannowsky, Phys. Rev. D 82, 113012 (2010). C. Englert, C. Hackstein and M. Spannowsky, Phys. Rev. D 82 (2010) 114024.
- [15] C. Englert, M. Spannowsky, D. Stancato and J. Terning, arXiv:1203.0312 [hep-ph].
- [16] G. 't Hooft, Nucl. Phys. B 72 (1974) 461.
- [17] J. M. Maldacena, Adv. Theor. Math. Phys. 2, 231 (1998)
 [Int. J. Theor. Phys. 38, 1113 (1999)] [hep-th/9711200].
 S. S. Gubser, I. R. Klebanov and A. M. Polyakov, Phys. Lett. B 428, 105 (1998) [hep-th/9802109]. E. Witten, Adv. Theor. Math. Phys. 2, 253 (1998) [hep-th/9802150].
- [18] N. Arkani-Hamed, M. Porrati and L. Randall, JHEP
 0108 (2001) 017. R. Rattazzi and A. Zaffaroni, JHEP
 0104, 021 (2001). M. Perez-Victoria, JHEP 0105, 064
 (2001). C. Csaki, M. Reece and J. Terning, JHEP 0905
 (2009) 067.
- [19] L. Randall and R. Sundrum, Phys. Rev. Lett. 83 (1999)
 3370. L. Randall and R. Sundrum, Phys. Rev. Lett. 83 (1999) 4690.
- [20] K. Agashe, A. Belyaev, T. Krupovnickas, G. Perez and J. Virzi, Phys. Rev. D 77 (2008) 015003. A. L. Fitzpatrick, J. Kaplan, L. Randall and L. -T. Wang, JHEP 0709 (2007) 013. B. Lillie, J. Shu and T. M. P. Tait, Phys. Rev. D 76 (2007) 115016. K. Agashe, H. Davoudiasl, S. Gopalakrishna, T. Han, G. -Y. Huang, G. Perez, Z. -G. Si and A. Soni, Phys. Rev. D 76 (2007) 115015. B. Lillie, L. Randall and L. -T. Wang, JHEP 0709 (2007) 074. C. Englert, B. Jager, M. Worek and D. Zeppenfeld,

Phys. Rev. D 80 (2009) 035027.

- [21] R. Contino, Y. Nomura and A. Pomarol, Nucl. Phys. B 671 (2003) 148.
 R. Contino, T. Kramer, M. Son and R. Sundrum, JHEP 0705, 074 (2007).
 R. Contino, D. Marzocca, D. Pappadopulo and R. Rattazzi, JHEP 1110 (2011) 081.
- [22] G. Cacciapaglia, G. Marandella and J. Terning, JHEP 0801 (2008) 070. A. Falkowski and M. Perez-Victoria, JHEP 0812, 107 (2008). G. Cacciapaglia, G. Marandella and J. Terning, JHEP 0902, 049 (2009). A. Falkowski, M. Perez-Victoria, Phys. Rev. D79, 035005 (2009).
- [23] H. Georgi, Phys. Rev. Lett. 98 (2007) 221601. H. Georgi, Phys. Lett. B 650, 275 (2007).
- [24] D. Stancato and J. Terning, JHEP 0911, 101 (2009).
- [25] A. Falkowski, M. Perez-Victoria, JHEP 0912, 061 (2009).
- [26] T. Han, D. Krohn, L. T. Wang and W. Zhu, JHEP 1003 (2010) 082.
- [27] G. Aad *et al.* [ATLAS Collaboration], JINST **3** (2008) S08003, G. L. Bayatian *et al.* [CMS Collaboration], J. Phys. G **34** (2007) 995.
- [28] R. Barate *et al.* [LEP Working Group for Higgs boson searches], Phys. Lett. B 565 (2003) 61. P. Bock *et al.* [ALEPH and DELPHI and L3 and OPAL Collaborations], CERN-EP/98-046.
- [29] G. Cowan, K. Cranmer, E. Gross and O. Vitells, Eur. Phys. J. C 71, 1554 (2011).
- [30] T. Junk, Nucl. Meth. А 434 Instrum. (1999)CDF Note 8128 435.Т. Junk, [cdf/doc/statistics/public/8128]. T. Junk, CDF Note 7904 [cdf/doc/statistics/public/7904]. H. Hu and J. Nielsen, in 1st Workshop on Confidence Limits, CERN 2000-005 (2000).
- [31] A. L. Read, CERN-OPEN-2000-205. A. L. Read, J. Phys. G G28 (2002) 2693-2704.
- [32] J. Alwall, P. Demin, S. de Visscher, R. Frederix, M. Herquet, F. Maltoni, T. Plehn and D. L. Rainwater *et al.*, JHEP **0709** (2007) 028.
- [33] T. Sjostrand, S. Mrenna and P. Z. Skands, JHEP 0605, 026 (2006).
- [34] J. Conway et al., http://physics.ucdavis.edu/ ~conway/research/software/pgs/pgs4-general.htm.