Diffractive dijet production in p[over ¯]\textit{p} collisions at 
\sqrt{s}=1.96 \text{ TeV}

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Diffractive dijet production in $p\bar{p}$ collisions at $\sqrt{s}=1.96$ TeV

We report on measurements performed on diffractive dijet production in $\bar{p}p$ collisions at $\sqrt{s} = 1.96$ TeV at the Fermilab Tevatron in Run II using the CDF II detector. The CDF collaboration has previously reported several results on low-transverse-momentum (soft) and high-transverse-momentum (hard) diffractive processes, obtained at the Fermilab Tevatron $\bar{p}p$ collider in Run I (1992–96) [1]-[16] and in Run II (2001–06) [17]-[20]. Three of the Run I results [6, 10, 14] are based on dijet events, $J J$, produced in single dissociation (or single dissociation, SD). These events are characterized by the presence of two jets in the final state and a leading $\bar{p}$ that escapes the collision intact. A large rapidity gap, $G_\rho$, defined as a region of pseudorapidity [21] devoid of particles, is present between the surviving $\bar{p}$

I. INTRODUCTION

We report on a study of diffractive dijet production in $\bar{p}p$ collisions at $\sqrt{s} = 1.96$ TeV using the CDF II detector at the Fermilab Tevatron $\bar{p}p$ collider. A data sample from 310 pb$^{-1}$ of integrated luminosity collected by triggering on a high transverse energy jet, $E_T^{jet}$, in coincidence with a recoil antiproton detected in a Roman pot spectrometer is used to measure the ratio of single-diffractive to inclusive-dijet event rates as a function of $x^p$ of the interacting parton in the antiproton, the Bjorken-$x$, $x_{Bj}^p$, and a $Q^2\approx(E_T^{jet})^2$ in the ranges $10^{-3} < x_{Bj}^p < 10^{-1}$ and $10^2 < Q^2 < 10^4$ GeV$^2$, respectively. Results are presented for the region of $\bar{p}$-momentum-loss fraction $0.03 < \xi_{\bar{p}} < 0.09$ and a four-momentum transfer squared $t_{\bar{p}} > -4$ GeV$^2$. The $t_{\bar{p}}$ dependence is measured as a function of $Q^2$ and $x_{Bj}^p$ and compared with that of inclusive single diﬀraction dissociation. We ﬁnd weak $x_{Bj}^{p\perp}$ and $Q^2$ dependencies in the ratio of single diﬀractive to inclusive event rates, and no signiﬁcant $Q^2$ dependence in the diﬀractive $t_{\bar{p}}$ distributions.

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and the diffractive cluster, $X_p$, composed of the particles from the dissociation of the proton, including $JJ$:

$$\bar{p} + p \rightarrow \bar{p} + G\bar{p} + X_p, \quad X_p \rightarrow X + JJ, \quad (1)$$

where $X$ represents all other particles in the diffractive cluster and will be referred below as the underlying event (UE).

Among the results of the Run I diffractive measurements, the most striking one is the observation of a breakdown of QCD factorization, expressed as a suppression by a factor of $O(10)$ of the diffractive structure function (DSF) measured in dijet production relative to that derived from fits to parton densities measured in diffractive deep inelastic scattering (DDIS) at the DESY $e-p$ collider HERA (see [10]). This result was further explored by CDF in Run I in studies of other diffractive processes, as briefly discussed below.

In this paper, we study diffractive dijet production in Run II with an upgraded CDF detector, incorporating special forward detector-components that expand the kinematic reach of the variables that define the process. Our goal is to further characterize the properties of diffractive dijet production in an effort to decipher the QCD nature of the diffractive exchange, traditionally referred to as Pomeron ($P$) exchange [22]-[24]. Below, we first present a brief physics-oriented summary of the diffractive processes studied and the results obtained in Run I, which is intended to define the terms and concepts used in the present study. Then, we restate the aim of this study in light of the Run I results, and conclude with an outline of the organization of the paper.

In Run I, several soft and hard diffraction processes were studied at $\sqrt{s} = 1800$ GeV, and in some cases at $\sqrt{s} = 630$ GeV. Two types of hard diffraction results were obtained:

(a) gap results: diffractive to non-diffractive (ND) cross section ratios using the (large) rapidity gap signature to select diffractive events;

(b) RPS results: diffractive to ND structure function ratios using a Roman Pot Spectrometer (RPS) to trigger on and measure a leading antiproton.

The diffractive dijet production processes studied are shown schematically in Fig. 1. They include (a) single diffraction (or single dissociation, SD), (b) double diffraction (or double dissociation, DD), and (c) double Pomeron exchange (DPE) or central dissociation (CD). For SD, results have also been obtained for $W$ [5], $b$-quark [9], and $J/\psi$ [13] production.

Soft diffraction processes studied include SD [3], DD [12], DPE (or CD) [16], and single plus double diffraction (SDD) [15]. These processes are defined as follows:

- **SD**: $\bar{p}p \rightarrow \bar{p} + G\bar{p} + X_p$,
- **DD**: $\bar{p}p \rightarrow X_p + G_c + X_p$,
- **DPE or CD**: $\bar{p}p \rightarrow \bar{p} + G\bar{p} + X_c + G_p + p$,
- **SDD**: $\bar{p}p \rightarrow \bar{p} + G\bar{p} + X_c + G_{X_p} + X_p$,

where $X_p$, $X_c$ and $G_c$ are antiproton-, proton- and central-dissociation particle clusters, $G_p$ is a central gap, and $G_{X_p}$ is a gap adjacent to a proton-dissociation cluster.

The results obtained exhibit regularities in normalization and factorization properties that point to the QCD character of diffraction [25]. For example, at $\sqrt{s} = 1800$ GeV the SD/ND ratios, also referred to as diffractive- or gap-fractions, for dijet, $W$, $b$-quark, and $J/\psi$ production, as well as the ratio of DD/ND dijet production, are all $\approx 1\%$. This value is suppressed relative to standard QCD-inspired theoretical expectations (e.g., two-gluon exchange) by a factor of $O(10)$, which is comparable to the suppression factor observed in soft diffraction relative to Regge-theory-based predictions. However, except for an overall suppression in normalization, factorization approximately holds among various processes at fixed $\sqrt{s}$ [25].

In this paper, we report on the dependence on Bjorken-$x$, $Q^2$ and $t$, the square of the four-momentum transfer between the incoming and outgoing antiproton, of the diffractive structure function measured from dijet production in association with a leading antiproton in $\bar{p}p$ collisions at $\sqrt{s}=1.96$ TeV and compare our results with those from HERA and with theoretical expectations.

The paper is organized as follows: in Sec. II we discuss the method we use to extract the diffractive structure function; in Sec. III we describe the experimental apparatus; in Secs. IV and V we discuss the data sets and data analysis; in Sec. VI we present the results; and in Sec. VII we summarize the results and draw conclusions.

II. METHOD

The cross section for inclusive dijet production in $\bar{p}p$ collisions can be written as

\[ \sigma_{\bar{p}p}^{\text{di}}(\bar{p} + p \rightarrow X + JJ) \]
\[
\frac{d^3\sigma^\text{incl}_{jj}}{dx_pdx_{\bar{p}}dt} = \frac{F^\text{incl}_{jj}(x_{\bar{p}}, Q^2)}{x_{\bar{p}}} \cdot \frac{F^\text{incl}_{jj}(x_p, Q^2)}{x_p} \cdot \frac{d\hat{\sigma}_{jj}}{dt},
\]

where \(x_{\bar{p}} (x_p)\) is the Bjorken-\(x\), defined as the forward-momentum fraction of the interacting parton of the antiproton (proton), \(Q^2\) is the factorization hard scale, \(F^\text{incl}_{jj}(x_p, Q^2)\) and \(F^\text{incl}_{jj}(x_{\bar{p}}, Q^2)\) are structure functions, and \(\hat{\sigma}_{jj}\) is the scattering cross section of the two partons producing the final-state jets. The \(\hat{\sigma}_{jj}\) depends on \(x_{\bar{p}}\) and \(x_p\), and also on \(t\), the square of the four-momentum transfer between the interacting partons, on \(Q^2\), and on \(\alpha_s(Q^2)\), the strong-interaction running coupling constant.

The structure function relevant for dijet production is a color-weighted combination of gluon (\(g\)) and quark (\(q\)) terms given by:

\[
F^\text{incl}_{jj}(x, Q^2) = x \left[ g(x, Q^2) + \frac{4}{9} \sum q_i(x, Q^2) \right],
\]

where \(x\) refers to \(x_p\) or \(x_{\bar{p}}\). In analogy with Eq. (2), the differential cross section for diffractive dijet production can be written as [25]

\[
\frac{d^5\sigma^\text{SD}_{jj}}{dx_pdx_{\bar{p}}d\xi dt} = \frac{F^\text{SD}_{jj}(x_{\bar{p}}, Q^2, \xi, t)}{x_{\bar{p}}} \cdot \frac{F^\text{incl}_{jj}(x_p, Q^2)}{x_p} \cdot \frac{d\hat{\sigma}_{jj}}{dt},
\]

where \(F^\text{SD}_{jj}\) is the diffractive structure function, which in addition to the usual dependence on \(x_{\bar{p}}\) and \(Q^2\) also depends on \(\xi\), the fractional forward momentum loss of the antiproton, and on \(t\).

The jet energies measured in the CDF detector must be corrected for various detector effects, which depend on the jet energy and \(\eta-\phi\) coordinates due to differences in calorimeter sub-system designs and calorimeter interfaces [27]. The correction factor generally increases as the jet energy decreases. To avoid systematic uncertainties associated with estimating corrections using Monte Carlo simulations, particularly for diffractively produced jets of relatively low \(E_T\), we measure ratios of SD to inclusive production as a function of Bjorken-\(x\) and \(Q^2\), for which jet-energy corrections due to detector effects nearly cancel out.

Since the single-diffractive cross section is a small fraction of the inclusive one, \(\lesssim 1\% \) of \(\sigma^\text{incl}\), we refer below to “inclusive” and “non-diffractive” (ND) dijet-production interchangeably. Furthermore, we also use this approximation in classifying event samples and associated parameters, as for example between \(F^\text{incl}_{jj}\) and \(F^\text{ND}_{jj}\).

The diffractive structure function is obtained by multiplying the ratio \(R_{SD/ND}(x, \xi, t)\) of the SD to ND event densities, \(n^\text{SD}_{jj}(x, Q^2, \xi, t)\) and \(n^\text{ND}_{jj}(x, Q^2)\), by the ND structure function, \(F^\text{ND}_{jj}(x, Q^2)\):

\[
F^\text{SD}_{jj}(x, Q^2, \xi, t) = R_{SD/ND}(x, \xi, t) \times F^\text{ND}_{jj}(x, Q^2).
\]

This method of measuring diffractive structure functions relies on the LO QCD expectation that cross sections are proportional to structure functions:

\[
R_{SD/ND}(x, Q^2, \xi, t) = \frac{n^\text{SD}_{jj}(x, Q^2, \xi, t)}{n^\text{ND}_{jj}(x, Q^2)} \approx \frac{F^\text{SD}_{jj}(x, Q^2, \xi, t)}{F^\text{ND}_{jj}(x, Q^2)}.
\]

Next-to-leading-order corrections to \(F^\text{SD}_{jj}(x, Q^2, \xi, t)\) obtained by this method are expected to be of \(\mathcal{O}(10\%)\) [28].

### III. EXPERIMENTAL APPARATUS

The CDF II detector is equipped with special forward detectors [18, 29–32] designed to enhance the capabilities for studies of diffractive physics. These detectors include the RPS, the Beam Shower Counters (BSC), and the MiniPlug (MP) calorimeters. The RPS is a scintillator fiber tracker used to detect leading antiprotons; the BSC are scintillator counters installed around the beam-pipe at three (four) locations along the \(p(\bar{p})\) direction and are used to identify rapidity gaps in the region \(5.5 < |\eta| < 7.5\); and the MP calorimeters [31] are two lead-scintillator based forward calorimeters covering the pseudorapidity region \(3.6 < |\eta| < 5.1\). The forward detectors include a system of Cherenkov Luminosity Counters (CLC) [33], whose primary function is to measure the number of inelastic \(\bar{p}p\) collisions per beam-bunch crossing and thereby the luminosity. The CLC covers the range \(3.7 < |\eta| < 4.7\), which substantially overlaps the MP coverage. In this analysis, the CLC is used for diagnostic purposes, and also to refine the rapidity-gap definition by detecting charged particles that might penetrate a MP without interacting, yielding a pulse-height smaller than the MP tower thresholds.

Figure 2 shows a schematic plan view of the beam-line elements and forward detectors along the outgoing antiproton beam direction. The RPS comprises three Roman pot stations located at a distance of \(\sim 57\) m from the nominal interaction point (IP) along the outgoing \(\bar{p}\) direction. Each station is equipped with one Roman Pot Trigger (RPT) counter and an 64-channel scintillator-fiber tracker, which can be used to reconstruct tracks both in the \(X\) (horizontal) and \(Y\) (vertical) coordinates. The tracking information, in conjunction with the interaction point coordinates, provided by the central detector, can be used to calculate the variables \(\xi\) and \(t\) of the recoil antiproton. During running, the RPS detectors were brought up to a distance of \(X \approx 1\) cm from the outgoing antiproton beam, with the (more intense) incoming proton beam positioned \(\sim 2\) mm farther away.

In Run I, in which data were collected at lower luminosities, the RPS detectors were positioned at approx-
IV. DATA SAMPLES AND EVENT SELECTION

The Run I diffractive dijet results were obtained from data samples collected at low instantaneous luminosities to minimize background from pileup events. Constrained by statistics, the $Q^2$ dependence of the DSF was measured over a limited range. Moreover, due to uncertainties in the beam position at the RPS location, it was difficult to reliably extract normalized $t$-distributions. In Run II, our goal was to obtain high statistics diffractive data samples with low pileup backgrounds from which to extract the $Q^2$ and $t$ dependence over a wide range. To achieve this goal, we built special forward detectors, described above in Sec. III, implemented dedicated triggers, and developed analysis techniques for background subtraction and RPS alignment. In this Section, we present the data samples and event selection requirements applied to produce the data sets from which the results were extracted.

This analysis is based on data from an integrated luminosity $L \approx 310$ pb$^{-1}$ collected in 2002–2003. Only “good runs” with a minimum $L \approx 10$ nb$^{-1}$ are used, selected based on beam conditions, detector performance criteria, and the requirement that the following detector components be functional: CCAL, PCAL, MP, CLC, and BSC. On-line event selection is accomplished with a three-level trigger system (L1, L2, L3) which accepts soft-interaction events as well as hard interaction events containing high $E_T$ jets. The latter are selected at the trigger level by requiring at least one calorimeter tower with $E_T > 5$, 20, or 50 GeV within $|\eta| < 3.5$. Leading antiprotons with fractional momentum loss in the range $0.03 < \xi < 0.09$ were triggered on using a three-fold coincidence of the RPT counters.

Jets were reconstructed using a cone algorithm, in which the transverse energy of a jet is defined as $E_T^{\text{jet}} = \Sigma_i E_i \sin(\theta_i)$ with the sum carried over all calorimeter towers at polar angles $\theta_i$ within the jet cone. The midpoint algorithm [41] was used, which is an improved iterative cone clustering algorithm based on calorimeter towers with $E_T > 100$ MeV. The jets were corrected for detector effects and for contributions from the underlying event (UE) [27]. Dijet candidate events were required to have at least two jets with $E_T > 5$, 20, or 50 GeV depending on the event sample, and $|\eta| < 2.5$.

In order to explore the region of large-transverse-energy jets of relatively low cross sections, data samples of RPS-triggered events in conjunction with the presence of a jet with $E_T^{\text{jet}} \geq 5, 20, \text{or } 50$ GeV in CCAL or
PCAL were also studied. These samples are referred to as RPS-Jet5, RPS-Jet20, and RPS-Jet50. Corresponding ND samples (Jet5, Jet20, and Jet50) were used for comparison.

The majority of the data used in this analysis were recorded without RPS tracking information. For these data, the value of $\xi$ was evaluated from calorimeter information and will be referred to as $\xi^{\text{CAL}}$ (see Sec. V C). The $\xi_p^{\text{CAL}}$ was then calibrated against $\xi$ obtained from the RPS, $\xi_p^{\text{RPS}}$, using data from runs in which RPS tracking was available (see Sec. V E). Below, we list the definitions of the triggers used in data acquisition and the data selection requirements applied in obtaining the data samples for this analysis.

The following trigger definitions are used:

- RPS: triple coincidence among the three RPS trigger counters in time with a $\bar{p}$ gate;
- RPS$_{\text{track}}$: RPS with RPS tracking available (included in the RPS trigger);
- J5 (J20, J50): jet with $E_T^{\text{jet}} \geq 5$ (20, 50) GeV in CCAL or PCAL;

The data selection requirements are listed below:

(i) good-run events: accepts events from runs with no problems caused by hardware or software failures during data acquisition;
(ii) $E_T$ significance [42]: selects events with missing transverse energy significance $S_{E_T} < 2$ to reject jet events in which there is $E_T$ due to energy loss in calorimeter cracks and/or events with jets and (undetected) neutrinos, such as from $W \rightarrow l\nu + jets$;
(iii) $N(\text{jet}) \geq 2$: accepts events with two jets of $E_T^{\text{jet}} > 5$ GeV within $|y^{\text{jet}}| < 2.5$;
(iv) splash veto: rejects events that cause splashes (large number of hits) in the RPT counters;
(v) RPT: rejects events that are triggered by accidental (not due to the traversal of a single particle) RPS counter coincidences (less than 0.1%);
(vi) SD (0.03 < $\xi_p^{\text{CAL}}$ < 0.09): accepts SD events with good efficiency, while rejecting backgrounds from pileup events consisting of a soft SD event that triggers the RPS and a ND dijet event.

Table I lists the number of events surviving these requirements when applied successively to the data.

The splash events were studied using the RPS$_{\text{track}}$ data sample before applying the splash veto requirement. The sum of the ADC counts of the three RPT counters, $\text{SumRPT} \equiv \sum_{i=1}^{3} \text{RPT}_i^{\text{ADC}}$, is used to reject splash events. Figure 3(a) shows SumRPT for events with/without a reconstructed RPS track. In the “RPS track” histogram the peak at $\sim 3000$ ADC counts is attributed to a single minimum-ionizing particle (MIP) traversing all three RPT counters. 2-MIP and 3-MIP shoulders are also discernible at $\sim 6000$ and $\sim 9000$ ADC counts, respectively. Events labeled as “No RPS track” are the splash events. These events dominate the region of SumRPT $> 5000$. Detailed studies using various event samples indicate that splash events are likely to be due to high-$\xi_p$ diffractive events for which the $\bar{p}$ does not reach the RPS, but rather interacts with the material of the beam pipe in the vicinity of the RPS producing a spray of particles causing the splash. In the region of SumRPT $< 5000$, the “No RPS track” distribution has a peak similar to that seen in the events with a reconstructed RPS track. These events are interpreted as good events for which the track was not reconstructed due to either malfunction or inefficiency of the fiber tracker.

Events with SumRPT $> 5000$ are rejected. The retained events contain approximately 77% of the RPT sample, as can be qualitatively seen in Fig. 3(b). These events, after applying the RPT selection requirement, constitute the SD event samples listed in Table I. Any possible inefficiency caused by the SumRPT cut is taken into account by folding a 6% uncertainty into that of the extracted cross section (see Sec. VIB 1, Table III).

V. DATA ANALYSIS

Analysis details are discussed here in the following seven sub-sections:

A – Dynamic alignment of Roman pos spectrometer
B – Trigger efficiency of Roman pot spectrometer
C – Antiproton momentum-loss measurement
D – Multiple interactions
E – Calibration of $\xi_p^{\text{CAL}}$
F – MiniPlug contribution to $\xi_p^{\text{CAL}}$
G – Beam-halo background

A. Dynamic alignment of Roman pot spectrometer

The values of both $\xi$ and $t$ can be accurately determined from RPS reconstructed track coordinates and the position of the event vertex at the Interaction Point using the beam-transport matrix between the interaction point and RPS. Crucial for this determination is the detector X-Y alignment with respect to the beam. Below, we describe a method developed to dynamically determine the alignment of the RPS detectors during the RPS$_{\text{track}}$ data collection period. As described in Sec. V E, the resulting $\xi_p^{\text{RPS}}$ distribution is used to calibrate $\xi_p^{\text{CAL}}$.

The dynamic alignment method is illustrated in Fig. 4, where the curve represents a fit to the data (after alignment) with a form composed of two exponential terms,
\[
\frac{d\sigma}{dt} = N_{\text{norm}} \left( A_1 e^{b_1 t} + A_2 e^{b_2 t} \right),
\]
where \( N_{\text{norm}} \) is an overall normalization factor.

Alignment is achieved by seeking a maximum of the \( \frac{d\sigma}{dt} \) distribution at \( t = 0 \). The implementation of the alignment method consists of introducing software offsets \( X_{\text{offset}} \) and \( Y_{\text{offset}} \) in the \( X \) and \( Y \) coordinates of the RPS detectors with respect to the physical beamline, and iteratively adjusting them until a maximum for \( \frac{d\sigma}{dt} \) at \( t = 0 \) (or of the dominant slope \( b_1 \)) is found at the \( (X,Y) \) position where the RPS fiber tracker is correctly aligned. Results for such a fit are shown in Fig. 5. The accuracy in \( \Delta X \) and \( \Delta Y \) of the RPS alignment calibration obtained using the inclusive data sample, estimated from Gaussian fits to the distributions in Fig. 5 around their respective minimum values, is \( \pm 60 \mu \text{m} \). This is limited only by the size of the data sample and the variations of the beam position during data taking. The contribution of the latter is automatically folded within the overall uncertainty as determined by this method.

**B. Trigger efficiency of Roman pot spectrometer**

Due to radiation damage, the position of the minimum ionizing particle (MIP) peak of the three RPT counters shifts toward smaller ADC values as the integrated luminosity, \( L \), of the data sample increases. The same behavior is observed in all three trigger counters. As a direct consequence, the efficiency of the RPT triple coincidence decreases as a function of \( L \). The RPT efficiency, \( \epsilon_{\text{RPT}} \), is measured using a sample of minimum-bias (MB) data from 175.6 pb\(^{-1}\) of integrated luminosity collected with a CLC\(_p\)-CLC\(_p\) coincidence trigger. The ADC distribution of each RPT counter was determined for various periods of data-taking by triggering with the other two RPT counters. Results are shown in Table II for nine data sets of approximately equal integrated luminosity obtained by subdividing the MB data sample. We evaluate \( \epsilon_{\text{RPT}} \) from the number of events with at least 1000 ADC counts in each of the three RPT counters (the trigger requirement) divided by the number of events with at least 500 ADC counts in each counter, the lowest ADC value found among MIP peaks in all three counters and in all data sets:

\[
\epsilon_{\text{RPT}} = \frac{N_{1.2.3}(\text{ADC} > 1000)}{N_{1.2.3}(\text{ADC} > 500)}. \tag{8}
\]

An uncertainty of 10% is assigned to \( \epsilon_{\text{RPT}} \) to account for variations due to the choice of the lowest ADC value of the MIP peak as determined from an analysis of all ADC distributions. The degradation of the RPT counters is taken into account by dividing the number of observed SD events by the RPT efficiency corresponding to the data-taking period to correct for RPT inefficiencies.

**C. Antiproton momentum loss measurement**

The momentum loss of the \( \bar{p} \), \( \xi_{\bar{p}}^{\text{CAL}} \), is calculated using the pseudorapidity \( \eta \) and transverse energy \( E_T \) of all the towers of the CCAL, PCAL, and MP calorimeters,

\[
\xi_{\bar{p}}^{\text{CAL}} = \frac{1}{\sqrt{s}} \sum_{i=1}^{N_{\text{tower}}} E_T e^{-\eta}, \tag{9}
\]

where the sum is carried out over towers with \( E_T > 100 \text{ MeV for CCAL and PCAL and } E_T > 20 \text{ MeV for MP} \). Calibration issues of \( \xi_{\bar{p}}^{\text{CAL}} \) are addressed in Sec. V E.
FIG. 3: SumRPT distributions for events of the SD RPS\textsubscript{track} data sample. (a) Number of events and (b) fraction of events as a function of the sum of ADC counts of the three Roman Pot Trigger (RPT) counters, SumRPT. In (a), the peak at SumRPT $\sim 3000$, attributed to a minimum ionizing particle (MIP) signal, is prominent in the “RPS track” entries, where two-MIP (three-MIP) shoulders at $\sim 6000$ (9000) ADC counts are also discernible. The “No RPS track” entries show a smaller MIP peak and a broad plateau, which is attributed to “splash events” (see text).

The resulting $\xi_{s_p}^{\text{CAL}}$ distributions are shown in Fig. 6. The filled circles in this figure represent the $\xi_{s_p}^{\text{CAL}}$ distribution of the entire RPS-Jet5 data sample after applying all the selection requirements listed in Table I. This distribution shows two peaks: one in the region of $\xi_{s_p}^{\text{CAL}} \lesssim 10^{-1}$ labeled SD, and a broader one at $\xi_{s_p}^{\text{CAL}} \gtrsim 10^{-1}$ labeled BG (background). The data points represented by filled squares are from the inclusive Jet5 data sample normalized (rescaled) to the number of the RPS-Jet5 BG events in the region $3 \times 10^{-1} < \xi_{s_p}^{\text{CAL}} < 2$, and those represented by filled stars are from RPS\textsubscript{track}-Jet5 data sample events with a reconstructed RPS track normalized (rescaled) to the number of RPS-Jet5 events in the SD region of $3 \times 10^{-2} < \xi_{s_p}^{\text{CAL}} < 9 \times 10^{-2}$.

The RPS-Jet5 data distribution is interpreted as follows:

FIG. 4: $t$ distributions for SD RPS\textsubscript{track} events of reconstructed RPS tracks in the range $0 \leq t \leq 1$ GeV$^2$ for the nominal X position and for positive X\textsubscript{offset} shifts relative to the beam line.

FIG. 5: The value of $-b_1$ of the $t$-distribution parametrization of Eq. (7) normalized to its minimum value vs. (a) Y\textsubscript{offset} and (b) X\textsubscript{offset}. 
FIG. 6: The calorimeter-measured antiproton-momentum-loss fraction, \( \xi_{\cal p}^{\text{CAL}} \), for three data samples: (a) RPS-Jet5 (filled circles), (b) RPS\text{\tiny\textsc{track}}-Jet5-rescaled (filled stars), and (c) Jet5-rescaled (filled squares). The regions labeled SD and BG are respectively dominated by SD dijet production. The decline trend of the distribution below \( \xi_{\cal p}^{\text{CAL}} \sim 5 \times 10^{-2} \) occurs in the region where the RPS acceptance is decreasing.

a. Single diffractive region. The events in the SD region are mainly due to SD dijet production. The declining trend of the distribution below \( \xi_{\cal p}^{\text{CAL}} \sim 5 \times 10^{-2} \) occurs in the region where the RPS acceptance is decreasing.

b. Background region. The events in the BG region, which form the broad peak centered at \( \xi_{\cal p}^{\text{CAL}} \sim 0.5 \), are mainly due to overlaps of a ND dijet event and a soft diffractive interaction that triggered the RPS but yielded no reconstructed vertex. A negligibly small fraction of the events in this region are due to SD dijet events superimposed with at least one MB event. Both types of overlap events should yield a value of \( \xi_{\cal p}^{\text{CAL}} \approx 1 \), but the expected nearly \( \delta \)-function distribution is smeared by the resolution of the energy measurement in the calorimeters and shifted toward lower \( \xi_{\cal p}^{\text{CAL}} \) values by particles escaping detection either in the areas of the calorimeter interfaces or due to the imposed energy thresholds.

As the rate of overlap events increases with instantaneous luminosity \( \mathcal{L} \), the ratio of BG/SD events in the \( \xi_{\cal p}^{\text{CAL}} \) distribution of the RPS-Jet5 event sample is expected to decrease with decreasing \( \mathcal{L} \). We verified this effect in the RPS-Jet5 data when binned in intervals of different \( \mathcal{L} \).

c. Diffractive events. The excess of the RPS-Jet5 events over the Jet5 distribution in the SD region is mainly due to diffractive production with no pileup. The fraction of ND events in the region of \( 0.03 < \xi_{\cal p}^{\text{CAL}} < 0.09 \) is \( \approx 12\% \). As the RPS acceptance depends on both \( \xi_{\cal p} \) and \( t \), and \( t \) is not measured for each event, the back-

ground from ND events in the SD region is accounted for in a simple MC simulation designed to calculate the acceptance on an event-by-event basis. Inputs to this simulation are the \( \xi \) and \( t \) distributions measured from data in which RPS tracking is available. Each event generated within a given bin of \( \xi_{\text{RPS}} \) is weighted by a factor equal to the ratio of the total number of events over the number of SD signal events in the corresponding \( \xi_{\cal p}^{\text{CAL}} \) bin of the RPS-Jet5 data plotted in Fig. 6.

D. Multiple interactions

Effects of multiple interactions in the same bunch crossing are handled by using the fraction of one-interaction events in the data sample, namely the fraction of events originating from bunch crossings that have just one \( pp \) interaction, to normalize the SD/ND event ratio in a multiple interaction environment. This fraction is estimated from a \textsc{pythia}-Monte-Carlo-generated sample of events containing the appropriate run-dependent fraction of multiple interactions for each run. The instantaneous luminosities of the various subsamples comprising this dataset vary within the range \( 2 \lesssim \mathcal{L} \lesssim 4 \times 10^{31} \text{cm}^{-2}\text{s}^{-1} \). The ratio of the number of one-interaction events, \( N_{\text{1int}} \), to all events, \( N_{\text{all}} \), decreases with increasing \( \mathcal{L} \) following a distribution well described by an exponential expression

\[
 f_{\text{1int}} \equiv \frac{N_{\text{1int}}}{N_{\text{all}}} \propto \exp(-c \cdot \mathcal{L}). \tag{10}
\]

where \( c = (0.34 \pm 0.06) \times 10^{-31} \text{cm}^2\text{s} \).

An offline analysis vertex requirement (cut) accepting events with only one reconstructed vertex would eliminate a large fraction of ND overlap events, but might also reject diffractive events due to vertex reconstruction inefficiencies, which depend on the event activity and therefore on both \( \xi \) and the number of overlapping events. To avoid biasing the \( \xi_{\cal p}^{\text{CAL}} \) distribution, we apply no vertex cut and correct for the ND overlap event contamination when we evaluate cross sections.

E. Calibration of \( \xi_{\cal p}^{\text{CAL}} \)

The measurement of \( \xi_{\cal p}^{\text{CAL}} \) using Eq. (9) is calibrated by comparing with the RPS measurement of \( \xi_{\text{RPS}} \). The comparison is made using the RPS\text{\tiny\textsc{track}} subsample of events for which tracking information is available. The \( \xi_{\text{RPS}} \) distribution for these events is shown in Fig. 7.

Figure 8 shows a two-dimensional scatter plot of \( \xi_{\cal p}^{\text{CAL}} \) vs \( \xi_{\text{RPS}} \) for the events with a reconstructed RPS track. An approximately linear relationship between \( \xi_{\cal p}^{\text{CAL}} \) and \( \xi_{\text{RPS}} \) is observed along the peak of the distribution of entries in the region of \( \xi_{\cal p}^{\text{CAL}} \lesssim 0.1 \) and \( 0.03 \lesssim \xi_{\text{RPS}} \lesssim 0.09 \).
where the diffractive events are expected. As already discussed, the entries with $\xi _p^{\text{CAL}} > 0.1$ are mainly due to ND dijet event with a superimposed soft SD overlap event. Without the measurement of $\xi _p^{\text{CAL}}$ the overlap events would contribute a large and irreducible background to the SD events.

For a quantitative calibration of $\xi _p^{\text{CAL}}$ the data are divided into bins of width $\Delta \xi _p^{\text{RPS}} = 0.005$ and the $\xi _p^{\text{CAL}}$ values in each bin are fit with a Gaussian distribution. Figure 9 shows such a fit for the bin of $0.055 < \xi _p^{\text{RPS}} < 0.060$. The ratio of the half-width to the average value of the fit curve is found to have the constant value of $0.3$ over the entire $\xi _p^{\text{CAL}}$ range of this data sample.

The results of $\xi _p^{\text{CAL}}$ vs $\xi _p^{\text{RPS}}$ for all the $\Delta \xi _p^{\text{CAL}}$ bins within the plateau region of $0.045 < \xi _p^{\text{RPS}} < 0.09$ of the $\xi _p^{\text{CAL}}$ distribution of Fig. 7 are plotted in Fig. 10. A linear relationship is observed of the form $\xi _p^{\text{CAL}} = p^0 + p^1 \cdot \xi _p^{\text{RPS}}$ with $p^0 = 0.007 \pm 0.002$ and $p^1 = 0.97 \pm 0.04$. The small size of the deviations of $p^0$ and $p^1$ from the ideal values of $p^0 = 0$ and $p^1 = 1$ is testimony to the success of the dynamic alignment of the RPS, which affects $\xi _p^{\text{RPS}}$, and the calorimeter energy calibrations and threshold settings, which influence $\xi _p^{\text{CAL}}$. These deviations do not affect the referral of the measurement of $\xi _p^{\text{CAL}}$ to that of $\xi _p^{\text{RPS}}$ to obtain an RPS-based value of $\xi _p^{\text{CAL}}$ in the data for which no RPS tracking is available.

FIG. 7: The $\xi _p^{\text{RPS}}$ distribution of the RPS$_{\text{track}}$ events.

FIG. 8: Scatter plot of $\xi _p^{\text{CAL}}$ vs $\xi _p^{\text{RPS}}$ for all RPS$_{\text{track}}$ data.

FIG. 9: The $\xi _p^{\text{CAL}}$ distribution of RPS$_{\text{track}}$ events in the range $0.055 < \xi _p^{\text{RPS}} < 0.060$. The curve is a Gaussian fit in the region of $\xi _p^{\text{CAL}} < 0.1$.

FIG. 10: Median values of $\xi _p^{\text{CAL}}$ obtained from fits to RPS$_{\text{track}}$ data in different $\xi _p^{\text{CAL}}$ bins of width $\Delta \xi _p^{\text{CAL}} = 0.05$ (horizontal bars) fitted linearly in the region $0.045 < \xi _p^{\text{CAL}} < 0.09$. 
producing the background due to ND dijet events overlapped the \( \xi \) background to the SD events. In comparison with Fig. 6, the BG peak is shifted towards without the contribution from the MP calorimeters. In Fig. 11 shows the \( \xi_{p}^{\text{CAL}} \) distribution for these samples. Three regions of \( \xi_{p}^{\text{CAL}} \) are of interest:

(i) \( \xi_{p}^{\text{CAL}} > 0.1 \), where ND events dominate;
(ii) \( 10^{-3} < \xi_{p}^{\text{CAL}} < 0.1 \), where SD events are expected;
(iii) \( \xi_{p}^{\text{CAL}} < 10^{-3} \), where “empty” events with one to a few CCAL or PCAL towers above threshold due to beam-halo particles and/or due to calorimeter noise may contribute to \( \xi_{p}^{\text{CAL}} \).

The contribution of a single CCAL or PCAL tower at \( \eta = 0 \) with \( E_{T} = 0.2 \text{ GeV} \) (the threshold used) is estimated from Eq. 9 to be \( \xi_{p}^{\text{CAL}} = 1 \times 10^{-4} \), which is well below the \( \xi \)-range of the RPS acceptance. At \( \xi_{p}^{\text{CAL}} \sim 3 \times 10^{-4} \), we observe a background peak corresponding to an average of \( \sim 3 \) CCAL towers at an event rate of \( \sim 5\% \) of the diffractive signal concentrated at \( \xi_{p}^{\text{CAL}} \sim 5 \times 10^{-2} \). We estimate that an upward fluctuation by a factor of 100 would be required for this background to compete with the overlap background already present within the diffractive region of \( 3 \times 10^{-2} < \xi_{p}^{\text{CAL}} < 9 \times 10^{-2} \). Because of the negligible probability of such a fluctuation, no correction is applied to the data for beam-halo background.

VI. RESULTS

Our results are presented in three subsections VI A–VIC. In VI A, we discuss certain kinematic distributions that establish the diffractive nature of the events in our data samples; in VI B, we present ratios of SD to ND production rates and extract the diffractive structure function; and in VIC, we report results on \( t \) distributions.

A. Kinematic distributions

The presence of a rapidity gap in diffractive events leads to characteristic kinematic distributions. Here, we compare the SD and ND distributions of mean transverse jet energy, mean jet pseudorapidity, jet azimuthal angle difference, and MiniPlug multiplicity.
a. Transverse jet energy. The mean dijet transverse energy, $E_T^* = \frac{E_{T1} + E_{T2}}{2}$, is presented in Fig. 13 for SD and ND events. The total number of ND events is normalized to that of the SD events and the associated statistical uncertainties are rescaled. The SD and ND distributions are very similar. The slightly narrower width of the SD distribution is attributed to the lower effective collision energy in SD ($\sqrt{s_{NN}}$) collision, and the larger fraction of jets at $\eta > 0$ in SD compared to ND events, which tend to have a lower average $E_T$.

b. Jet pseudorapidity. The mean dijet pseudorapidity distribution of the two leading jets, $\eta^* = \frac{\eta_{T1} + \eta_{T2}}{2}$, is shown for SD and ND events in Fig. 14. The ND events are centered around $\eta^* = 0$, while the SD distribution is shifted towards positive values (proton-beam direction) due to the boost of the center of mass system of the $P$-p collision.

c. Azimuthal angle correlations. The distributions of the azimuthal angle difference between the two leading jets, $\Delta \phi = |\phi_{T1} - \phi_{T2}|$, are shown in Fig. 15 for SD and ND events. The SD dijets are more back-to-back than the ND ones, as would be expected from the reduced available sub-energy of the diffractive system.

d. MiniPlug multiplicity. The MP multiplicity distribution for SD and ND events is shown in Fig. 16. Multiplicities are evaluated by counting the number of peaks above calorimeter tower noise levels using “seed” towers with a minimum transverse energy of 20 MeV [32]. Such peaks originate from three sources: (a) charged hadrons traversing the MP without interacting, (b) charged and
neutral hadrons interacting in the material of the MP plates, and (c) electromagnetic energy deposited by e±/γ particles. The SD events have smaller multiplicities in comparison with the ND events, as expected from the reduced center of mass energy in p+p relative to p-p collisions.

B. Ratio of single diffractive to non-diffractive production rates and the diffractive structure function

The ratio $\mathcal{R} \equiv R_{\text{SD/ND}}(x, Q^2, \xi, t)$ of the SD to ND dijet production rates, which in leading order QCD is proportional to the ratio of the corresponding structure functions (see Sec. II), is measured as a function of $x_{Bj}$, the Bjorken-x of the struck parton of the antiproton, and $Q^2 \approx (E_T^\ast)^2$. For each event, $x_{Bj}^\ast$ is evaluated from the $E_T$ and $\eta$ values of the jets using the formula

$$x_{Bj}^\ast = \frac{1}{\sqrt{s}} \sum_{i=1}^{3\text{ jets}} E_T^i e^{-\eta^i}, \quad (11)$$

where the sum is carried out over the two leading jets plus a third jet of $E_T > 5$ GeV, if present. Theoretically, the sum should be over all jets in the final state, but the fraction of events with more than three jets of $E_T > 5$ GeV is relatively small and including them in the evaluation of $x_{Bj}^\ast$ does not significantly affect the obtained results [28].

Jet energies are measured using an algorithm based on measuring the “visible” energy deposited in the detector within a cone of radius $R_{\text{cone}} = \sqrt{\delta \eta^2 + \delta \phi^2} = 0.7$ and applying appropriate corrections [27]. Both the SD and ND jets contain within the jet cone an amount of underlying event (UE) energy from soft spectator partonic interactions, which we subtract from the measured jet energy. For diffractive events, where a large fraction of the event energy is carried away by the recoil antiproton, the amount of UE energy is expected to be smaller than in ND events.

The UE energy in SD events was measured using the sample of RPS inclusive triggered data. To suppress overlap backgrounds, we required the events to be in the region of $0.01 < \xi_p^{\text{CAL}} < 0.14$, which is dominated by SD events from a single $p\bar{p}$ interaction. We then selected events with only one reconstructed vertex with $|z_{\text{vertex}}| < 60$ cm ($\sim 1 \sigma$) and measured the $\Sigma E_T$ of all central calorimeter towers within a randomly chosen cone of radius $R_{\text{cone}} = 0.7$ in the region $0.1 < |\eta| < 0.7$. The UE energy in MB (ND dominated) events was also measured using the random cone technique. From these two measurements we obtained an average UE $E_T$ of 0.90 GeV (1.56 GeV) for SD (ND) events.

1. $x_{Bj}$ dependence

The ratio $\mathcal{R}$ of the number of SD dijet events per unit $\xi$ over the number of ND events of the Jet5 sample is corrected for the effect of multiple interactions and for the RPS detector acceptance.

To account for multiple interactions contributing to the ND sample, the ND $x_{Bj}$ distribution is weighted by the factor

$$f^{\text{int}} = \exp[-c \cdot L],$$

where $L$ is the instantaneous luminosity and $c = (0.34 \pm 0.06) \times 10^{-31}$ cm$^2$/s (see Sec. V D). This correction is not applied to the SD events, since contributions from additional interactions shift $E_T^{\ast\text{CAL}}$ into the BG region. The effect of overlaps of a SD and a ND event with jets in both events, which would tend to shift the $x_{Bj}$ distribution towards higher values, is estimated to be on the 0.1% level and is neglected.

The number of SD events is corrected for the RPS acceptance, which is estimated from a beam optics simulation to be $\epsilon = 0.80 \pm 0.04$ (syst) for $0.03 < \xi < 0.09$ and $t > 1$ GeV$^2$ [18], and the obtained SD and ND data samples are normalized to their respective integrated luminosities.

The results for the ratio $\mathcal{R}$ for events within $0.03 < \xi < 0.09$ are presented in Fig. 17 as a function of $\log_{10} x_{Bj}$, along with the results obtained in Run I for $0.035 < \xi < 0.095$ and $|t| < 1$ GeV$^2$ [10]. The Run I results have an estimated ±25% systematic uncertainty in the overall normalization [10]. The shapes of the two distributions are in good agreement, except in the high $x_{Bj}$ region where the Run I distribution is seen to extend to higher $x_{Bj}$ values. This behavior is expected from the difference in $(E_T^\ast)$ and $\eta$ acceptance for jets in Run I (Run II), which is $(E_T^\ast) \approx 7$ GeV (12 GeV) and $|\eta| < 3.7 (|\eta| < 2.7)$. This difference results in a larger $x_{Bj}$ reach in Run I by a factor of $(12/7) \times e^{3.7-2.7} \approx 2$, as estimated using Eq. 11.

A fit to all Run II data in the range $0.03 < \xi < 0.09$ using the form $\mathcal{R} = R_0 \cdot x_{Bj}^\beta$ subject to the constraint $\beta = (x/\xi) < 0.5$ [10] yields $r = -0.44 \pm 0.04$ and $R_0 = (8.6 \pm 0.8) \times 10^{-3}$. This result is compatible with the
Run I result of \( r = -0.45 \pm 0.02 \) and \( R_0 = (6.1 \pm 0.1) \times 10^{-3} \) obtained by a constrained fit of the form \( R = R_0 \cdot (x_{Bj}/0.0065)^\gamma \) designed to match the data at the average value of \( x_{Bj}/0.0065 \). This constraint accounts for the lower \( R_0 \) value of Run I.

The systematic uncertainties in \( R_0 \) and \( r \) are listed in Table III. The causes of uncertainty investigated include the underlying event, the energy scale, the calorimeter tower \( E_T \) thresholds, overlaps in ND events, instantaneous luminosity \( \mathcal{L} \), bunch-by-bunch variations in \( \mathcal{L} \), RPS acceptance, and “splash” events.

a. **Underlying event.** The underlying event energy is subtracted from the jet energy when the jet energy corrections are applied. The results presented are for a ±30% variation of the UE energy correction, which is sufficient to cover the uncertainty for jets depositing energy near the interfaces or the outer edges of a calorimeter.

b. **Energy scale.** The effect of the energy scale of the CCAL, PCAL and MP calorimeters on \( \xi_{p}^{\text{CAL}} \) and thereby on \( R_0 \) and \( r \) was estimated by changing the CCAL and PCAL jet energies by ±5% and the MP tower energies by ±30%, based on studies of inclusive jets and comparisons of MP \( E_T \) distributions with expectations based on simulations.

c. **Tower \( E_T \) threshold.** Tower energy threshold effects would generally be expected to cancel out in measuring the ratio of rates. However, due to the different UE event contributions in SD and ND events, the tower thresholds applied could affect the result. The uncertainty in \( R \) for jets with mean transverse energy of \( E_T > 10 \text{ GeV} \) (\( E_T^p > 12 \text{ GeV} \)) due to tower threshold effects is estimated to be ±1% (±2%). The effect on both \( R \) and on \( r \) for our total SD event sample is ±1%.

d. **Overlaps in ND events.** To account for event overlaps in ND events occurring at high instantaneous luminosities, each event is weighted by a factor of \( w = \exp[-c \cdot \mathcal{L}] \), where \( c = (0.34 \pm 0.06) \times 10^{-31} \text{ cm}^2/\text{s} \) (see Sec. V D). The uncertainty in \( c \) has a ±8% effect on the determination of \( R_0 \).

e. **Instantaneous luminosity, \( \mathcal{L} \).** We estimate an uncertainty of ±3% in the determination of \( R_0 \) due to an uncertainty of ±6% in the determination of \( \mathcal{L} \) during the data collection period.

f. **Bunch-by-bunch variation in \( \mathcal{L} \).** A bunch-by-bunch variation of ±50% in \( \mathcal{L} \) over the collection period of our data sample contributes a ±4% systematic uncertainty in \( R_0 \).

g. **RPS acceptance.** Using a MC simulation, the uncertainty in \( R_0 \) as estimated to be ±10%.

h. **Splash events.** By evaluating the differences among data subsamples, a systematic uncertainty of ±6% is estimated due to the cut applied to remove the splash events (see Table IV).

Added in quadrature, the above uncertainties yield \( \Delta R \) (syst) = ±18% and \( \Delta r \) (syst) = ±6%.

<table>
<thead>
<tr>
<th>Source of uncertainty</th>
<th>Variation ( \Delta R_0 )</th>
<th>( \Delta r )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Underlying event</td>
<td>±30%</td>
<td>±5%</td>
</tr>
<tr>
<td>Central/plug cal. energy scale</td>
<td>±5%</td>
<td>±8%</td>
</tr>
<tr>
<td>MiniPlug energy scale</td>
<td>±30%</td>
<td>±6%</td>
</tr>
<tr>
<td>Tower ( E_T ) threshold</td>
<td>±10%</td>
<td>±1%</td>
</tr>
<tr>
<td>Overlaps in ND events</td>
<td>±20%</td>
<td>±8%</td>
</tr>
<tr>
<td>Instantaneous luminosity</td>
<td>±6%</td>
<td>±3%</td>
</tr>
<tr>
<td>Bunch-by-bunch luminosity</td>
<td>±50%</td>
<td>±4%</td>
</tr>
<tr>
<td>RPS acceptance</td>
<td>N/A</td>
<td>±10%</td>
</tr>
<tr>
<td>Splash events</td>
<td>N/A</td>
<td>±6%</td>
</tr>
<tr>
<td>Total uncertainty</td>
<td>±18%</td>
<td>±6%</td>
</tr>
</tbody>
</table>

2. **\( Q^2 \) dependence**

As discussed in Sec. IV, special data samples collected with dedicated triggers are used to extend the measurement of the jet energy spectrum to \( E_T^\text{jet} \sim 100 \text{ GeV} \). Results for the ratio \( R \) obtained from an analysis of these samples similar to that described above are presented in Fig. 18 for \( Q^2 \equiv \langle E_T^p \rangle^2 \) in the range of \( \sim 100 < Q^2 < 10^4 \text{ GeV}^2 \). These distributions are mainly affected by the overall uncertainty in normalization, as the relative uncertainties among different \( Q^2 \) bins cancel out in measuring the ratio. A factor of ≤ 2 variation among all distributions is observed over the entire \( Q^2 \) range, as compared to a factor of \( \sim 10^4 \) over the same range between the individual SD and ND distributions shown in Fig. 13.
are constant within the uncertainties over the range of constraints $\Delta R \pm 10\% \cdot R_{PS}$. Crucial for the measurement at $|t| \approx 1$ GeV, and given that $t \propto -q_{\bar{p}}$, where $q_{\bar{p}} \approx Y_{\text{offset}}$, the $|t|$-range of the RPS acceptance is expected to be a factor of $(1 + 0.25)/(1 - 0.25)^2 = 2.8$ larger in the $Y_{\text{track}} > Y_0$ than in the $Y_{\text{track}} < Y_0$ region, where $Y_0$ is the $Y = 0$ horizontal centerline of the detector.

The results of fits performed using the form $R = R_0 \cdot x_{BJ}^\beta$ in the region $1 \times 10^{-3} < x_{BJ} < 2.5 \times 10^{-2}$, where the constraint $\beta = (x/\xi) < 0.5$ is satisfied, are presented for various jet $E_T$ intervals in Table IV. Both $R_0$ and $r$ are constant within the uncertainties over the range of $10^2 < Q^2 < 10^3$ GeV$^2$. This result indicates that the $Q^2$ evolution in diffractive interactions is similar to that in ND interactions [43].

### TABLE IV: Fit parameters of the ratio of SD to ND production rates for events in different $E_T$ bins. The ratios are fitted to the form $R = R_0 \cdot x_{BJ}^\beta$ for $1 \times 10^{-3} < x_{BJ} < 2.5 \times 10^{-2}$.

<table>
<thead>
<tr>
<th>Jet $E_T$ [GeV]</th>
<th>$Q^2$ GeV$^2$</th>
<th>$R_0$</th>
<th>$r$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$8 &lt; E_T &lt; 12$</td>
<td>$Q^2$ GeV$^2$</td>
<td>$8.6 \pm 0.8 \times 10^{-3}$</td>
<td>$-0.44 \pm 0.04$</td>
</tr>
<tr>
<td>$18 &lt; E_T &lt; 25$</td>
<td>$Q^2$ GeV$^2$</td>
<td>$8.0 \pm 1.6 \times 10^{-3}$</td>
<td>$-0.48 \pm 0.05$</td>
</tr>
<tr>
<td>$35 &lt; E_T &lt; 50$</td>
<td>$Q^2$ GeV$^2$</td>
<td>$6.3 \pm 1.8 \times 10^{-3}$</td>
<td>$-0.60 \pm 0.07$</td>
</tr>
<tr>
<td>$50 &lt; E_T &lt; 70$</td>
<td>$Q^2$ GeV$^2$</td>
<td>$5.5 \pm 5.0 \times 10^{-3}$</td>
<td>$-0.64 \pm 0.22$</td>
</tr>
<tr>
<td>$70 &lt; E_T &lt; 90$</td>
<td>$Q^2$ GeV$^2$</td>
<td>$7.0 \pm 7.0 \times 10^{-3}$</td>
<td>$-0.58 \pm 0.26$</td>
</tr>
</tbody>
</table>

#### C. $t$ distribution

The $t$ distribution is measured for both soft and hard SD data samples using the inclusive $R_{PS\text{track}}$ and the $R_{PS\text{track}}$-Jet5 (Jet20, Jet50) data. In Sec. VI C 1, we discuss the $t$ distribution in the region of $0 < |t| < 1$ GeV$^2$ as a function of jet $\langle E_T^\gamma \rangle^2 \approx Q^2$ and characterize the slope parameter at $|t| \approx 0$ as a function of $Q^2$. Then, in Sec. VI C 2, we examine the shape of the $t$ distribution in the region up to $|t| = 4$ GeV$^2$ and search for a diffraction minimum. Crucial for the measurement at $|t| > 4$ GeV$^2$ is the background subtraction.

**a. Background evaluation.** The background is evaluated from the data by taking advantage of the asymmetric vertical position of the RPS detectors during data taking. As shown in Fig. 5, the dynamic alignment method yields $Y_{\text{offset}} \approx 0.25$ cm and $X_{\text{offset}} \approx 0$. The nonzero value of $Y_{\text{offset}}$ results in an asymmetric $t$ range in the acceptance. Since the RPS detectors are 2 cm wide, and given that $t \propto -q_{\bar{p}}$, where $q_{\bar{p}} \approx Y_{\text{offset}}$, the $|t|$-range of the RPS acceptance is expected to be a factor of $(1 + 0.25)/(1 - 0.25)^2 = 2.8$ larger in the $Y_{\text{track}} > Y_0$ than in the $Y_{\text{track}} < Y_0$ region, where $Y_0$ is the $Y = 0$ horizontal centerline of the detector.

Figure 19 shows $t$ distributions of SD $R_{PS\text{track}}$ data events within $0.05 < \xi_{pRPS} < 0.08$ for $Y_{\text{track}} > Y_0$ (up-pointing-triangles) and $Y_{\text{track}} < Y_0$ (down-pointing-triangles), where $Y_0$ is the centerline of the RPS fiber tracker.
where $|t_2| = 2.3 \times 2.8 = 6.5 \text{ GeV}^2$. However, in order to reduce systematic uncertainties on acceptance corrections arising from $(t, \xi)$-resolution and detector edge effects we present in Sec. VI C 2 $|t|$ distributions only up to $|t| = 4 \text{ GeV}^2$.

b. Corrections. The data are corrected by subtracting the background and dividing by the RPS acceptance. In principle, the background subtraction should be performed on an event-by-event basis, since both background and acceptance depend on both $\xi$ and $t$. The acceptance, $A(\xi, t)$, is obtained from a beam-optics simulation. For the data in the plateau region of the $\xi^\text{RPS}$ distribution of Fig. 7 within $0.05 < \xi < 0.08$, which are used for evaluating $t$ distributions, the acceptance $A_{0.05<\xi<0.08}(t)$ is shown in Fig. 20. For each event, the raw values of $\xi$ and $t$ are obtained from the RPS tracker and used to fill the bins of a histogram. Since the acceptance is fairly flat versus $\xi$ within the $t$ region of interest, the incremental value entered into a $t$-bin is reduced by the average background of $N_{\text{bg}} \times \Delta t$ events, where $\Delta t$ is the bin width, and is increased by a factor of $A^{-1}_{0.05<\xi<0.08}(t)$ (a zero value is entered if the number of events in a bin after subtracting the background is found to be $\leq 0$).

1. $t$ distribution for $|t| \leq 1 \text{ GeV}^2$

In this section, we discuss the event selection requirements used for the measurement of the $t$ distribution in the region of $|t| \leq 1 \text{ GeV}^2$, extract the slope parameter(s) from fits to the data, and comment on systematic uncertainties.

Event selection. To minimize the effect of migration of events to and from adjacent $\xi$ bins caused by resolution effects, events are selected in the region of $|t| \leq 1 \text{ GeV}^2$ and $0.05 < \xi^\text{RPS} < 0.08$, where the RPS acceptance is approximately flat (see Fig. 7). To reject overlapping backgrounds, these events are further required to be within $\xi^\text{CAL} < 0.1$, where the SD events dominate (see Fig. 6). The same expression that was used in the RPS dynamic alignment in Sec. V A, composed of two exponential terms with slopes $b_1$ and $b_2$ (Eq. 7), is used to fit the data and obtain the values of the slopes. Fits to data with only statistical uncertainties are shown in Fig. 21 for various $Q^2$ ranges. Systematic uncertainties are discussed below.

b-slope parameters. Results for the slope parameters $b_1$ and $b_2$ and for the ratios $b_1/b_1^{\text{incl}}$ and $b_2/b_2^{\text{incl}}$ are presented in Table V. The slopes $b_1$ and $b_2$ for all samples are plotted in Fig. 22. No significant $Q^2$ dependence is observed from soft diffraction of $< Q^2 > \sim 1 \text{ GeV}^2$ to $Q^2 \sim 10^4 \text{ GeV}^2$. The mean values of $b_1$ and $b_2$ over all data samples are $5.27 \pm 0.33 \text{ (GeV/c)}^{-2}$ and $1.17 \pm 0.17 \text{ (GeV/c)}^{-2}$, respectively. The measured slopes of the inclusive sample are in agreement with theoretical expectations [44].

Systematic uncertainties. We considered the dependence of the results on the RPS fiber-tracker thresholds, the instantaneous luminosity, and the beam-store and run number.

a. RPS fiber-tracker thresholds. Tracks in the RPS are reconstructed from hits above fiber threshold. A threshold value of 30 ADC counts is used for all three RPS stations. The slope values change by $+1\%$ ($-1\%$) when the threshold is lowered down to 20 (raised up to 35) ADC counts, representing a decrease (increase) that doubles (reduces by 50\%) the number of noise hits in the fiber tracker. A systematic uncertainty of $\pm 1\%$ was assigned for this effect.

b. Instantaneous luminosity. The RPS inclusive sample is divided into two luminosity-level subsamples: one consisting of events collected at low instantaneous luminosities, $\mathcal{L} < 1.5 \cdot 10^{31}\text{cm}^{-2}\text{s}^{-1}$, and the other of events collected at $\mathcal{L} > 3.5 \cdot 10^{31}\text{cm}^{-2}\text{s}^{-1}$. A less than $2\%$ difference between the slopes extracted from the two samples is observed, which is well within the statistical uncertainty.

c. Beam conditions. Variations in beam conditions among various beam stores and/or during various time intervals of a given store may affect the slope measurement. To estimate the uncertainty associated with varying beam conditions, we measure the $b$-slopes of data subsamples from several beam stores and from different periods (run number) within a store. The values for $b_1$ and $b_2$ obtained were within the corresponding statistical uncertainties. A systematic uncertainty equal to the statistical uncertainty was estimated.

d. Dynamic alignment. A systematic uncertainty of $5\%$ is estimated from the fits shown in Fig. 5 for the slope $b_1$ arising from the uncertainties of $\pm 60\mu\text{m}$ in the (X,Y) position of the RPS detectors relative to the $\vec{p}$ beam.

The systematic uncertainties are listed in Table VI.

2. $t$ distributions for $|t| \leq 4 \text{ GeV}^2$ and search for a diffraction minimum

We extend the analysis to measure $t$ distributions up to $|t| = 4 \text{ GeV}^2$ and search for a diffraction minimum using inclusive SD RPS$_{\text{track}}$ and RPS$_{\text{track}}$-Jet5 (Jet20) events within $0.05 < \xi^\text{RPS} < 0.08$. This $\xi$-range corresponds to a mean mass for the diffractively dissociated proton $\langle M_X \rangle \approx \xi^\text{RPS} \sqrt{s} \approx 500 \text{ GeV}$. The dijets in the Jet5 (Jet20) data sample have $\langle Q^2 \rangle \approx 225 \text{ (900)} \text{ GeV}^2$. As already discussed in Sec. VI C, the background in these data samples is $N_{\text{bg}} = 20/\text{GeV}^2$, as estimated from the unphysical region of $|t| > |t_1| = 2.5 \text{ GeV}^2$ for $Y_{\text{track}} > Y_0$ in Fig. 19.

Figure 23 shows the sum of the $Y_{\text{track}} > Y_0$ and $Y_{\text{track}} < Y_0$ distributions for the RPS inclusive and RPS-Jet20 data samples after background subtraction and acceptance corrections. The distributions are presented in a variable-bin-width-histogram format. In incrementing the histograms, a fraction is subtracted from
FIG. 20: RPS acceptance: (left) vs $-t$ and $\xi$, and (right) vs $-t$ integrated over $0.05 < \xi < 0.08$.

TABLE V: Slopes of $t$ distributions for soft and hard diffractive events of the SD RPS track data in the range $0.05 < \xi^{RPS} < 0.08$ for different $\langle E_T^2 \rangle$ or $Q^2 \equiv \langle E_T^2 \rangle$ bins obtained from fits to the form of Eq. (7), $d\sigma/dt = N \cdot (A_1 \cdot e^{b_1 t} + A_2 \cdot e^{b_2 t})$, with $A_2/A_1 = 0.11$, fixed at the average value obtained in the dynamic alignment of all different event subsamples. The uncertainties listed are statistical.

<table>
<thead>
<tr>
<th>Event sample</th>
<th>$\langle E_T^2 \rangle$</th>
<th>$Q^2$</th>
<th>$b_1$</th>
<th>$b_2$</th>
<th>$b_1/b_1^{\text{ext}}$</th>
<th>$b_2/b_2^{\text{ext}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>RPS incl.</td>
<td>$\approx 1$</td>
<td>5.4 ± 0.1</td>
<td>1.2 ± 0.1</td>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>RPS-Jet5</td>
<td>15</td>
<td>225</td>
<td>5.0 ± 0.3</td>
<td>1.4 ± 0.2</td>
<td>0.93 ± 0.08</td>
<td>1.12 ± 0.23</td>
</tr>
<tr>
<td>RPS-Jet20</td>
<td>30</td>
<td>900</td>
<td>5.2 ± 0.3</td>
<td>1.1 ± 0.1</td>
<td>0.96 ± 0.07</td>
<td>0.93 ± 0.16</td>
</tr>
<tr>
<td>RPS-Jet50</td>
<td>67</td>
<td>4500</td>
<td>5.5 ± 0.5</td>
<td>0.9 ± 0.2</td>
<td>1.00 ± 0.10</td>
<td>0.72 ± 0.18</td>
</tr>
</tbody>
</table>

FIG. 21: $|t|_p$ distribution shapes for SD RPS track data of different average $Q^2$ values within $0.05 < \xi^{RPS} < 0.08$ (note the different $\xi^{RPS}$ range from that in Table I).

TABLE VI: Systematic uncertainties in the slope parameters $b_1$ and $b_2$ of the diffractive $t$-distributions (from Table V).

<table>
<thead>
<tr>
<th>Source of uncertainty</th>
<th>$\delta b_1$</th>
<th>$\delta b_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>RPS tracker threshold</td>
<td>1%</td>
<td>1%</td>
</tr>
<tr>
<td>Instantaneous luminosity</td>
<td>2%</td>
<td>2%</td>
</tr>
<tr>
<td>Beam conditions</td>
<td>4%</td>
<td>8%</td>
</tr>
<tr>
<td>RPS alignment</td>
<td>5%</td>
<td>5%</td>
</tr>
<tr>
<td>Total (quadrature - sum)</td>
<td>6.8%</td>
<td>9.7%</td>
</tr>
</tbody>
</table>

each entry equal to the average background fraction in that bin, and the acceptance correction is then applied based on the RPS-measured values of $\xi$ and $t$. The dashed curve shown in the figure represents the electromagnetic form factor squared of the Donnachie-Landshoff (DL) model [44], $F_1(t)^2$, normalized to the RPS inclusive data within $-t \lesssim 0.5$ GeV$^2$. The $F_1(t)$ form factor used is given by [44]:
cussed below.\[d\sigma/dt = N \cdot (A_1 \cdot e^{b_1 \cdot t} + A_2 \cdot e^{b_2 \cdot t})\], with $A_2/A_1 = 0.11$ for SD events of different $Q^2$ values (see Table V); the soft diffraction (RPS inclusive) points have been placed arbitrarily at $< Q^2 > 1$ GeV$^2$.

\begin{equation}
F_1(t) = \frac{4m_p^2 - 2.8t}{4m_p^2 - t} \left[ \frac{1}{(1 - t/0.71)} \right]^2,
\end{equation}

In SD, $F_1(t)$ enters in the form [44]:

\begin{equation}
\frac{d\sigma^{SD}}{dt} = N_{\text{norm}} F_1(t)^2 \exp \left[ 2\alpha' \cdot \ln \frac{1}{\xi} \cdot t \right],
\end{equation}

where $\alpha' \approx 0.25$ GeV$^{-2}$ is the slope of the $p$-trajectory [24]. For $|t| \leq 1$ (GeV/c)$^2$ and $0.05 < \xi < 0.08$, the two-component exponential form of Eq. (7) with $A_2/A_1 = 0.11$, the average value obtained in the dynamic alignment method, is a good approximation to that of Eq. (13) with $\langle \xi \rangle = 0.065$ substituted for $\xi$.

The following features of the $t$ distributions are notable:

- **Low-$t$ region** ($-t \lesssim 0.5$ GeV$^2$): the RPS data are in good agreement with the DL curve;
- **Scale independence:** the distributions of the RPS and RPS-Jet5 data are similar in shape;
- **High-$t$ region** ($-t \gtrsim 0.5$ GeV$^2$): the RPS data lie increasingly higher than the DL curve as $-t$ increases, becoming approximately flat for $-t \gtrsim 2$ GeV$^2$. The compatibility of this observation with an underlying diffractive minimum at $-t \sim 2.5$ GeV$^2$ broadened by resolution effects is discussed below.

The physics significance of these results is briefly discussed below.

**FIG. 22**: The slope parameters $b_1$ and $b_2$ of a fit to the form $d\sigma/dt = N \cdot (A_1 \cdot e^{b_1 \cdot t} + A_2 \cdot e^{b_2 \cdot t})$, with $A_2/A_1 = 0.11$ for SD events of different $Q^2$ values (see Table V); the soft diffraction (RPS inclusive) points have been placed arbitrarily at $< Q^2 > 1$ GeV$^2$.

**FIG. 23**: $t$-distributions for two samples of SD RPS\_track events within the region $0.05 < \xi_{pp} < 0.08$ corrected for RPS acceptance after background subtraction: (circles) RPS inclusive and (triangles) RPS-Jet20 ($\langle Q^2 \rangle \approx 900$ GeV$^2$). The curve represents the distribution expected for soft SD in the DL (Donnachie-Landshoff) model [44] (Eq. 13) normalized to the RPS data within $-t \lesssim 0.5$ GeV$^2$.

\begin{itemize}
  \item **Low-$t$ region.** The good agreement between the inclusive $t$ distribution and the DL prediction in this region serves as a basis for a search for deviations in the region of $|t| \gtrsim 0.5$ GeV$^2$ that could arise from a diffraction minimum.
  \item **Scale independence.** The scale independence of the distributions supports a factorization property between the exchange that produces the leading $\bar{p}$ and associated rapidity gap on the one hand, and the final state into which the proton dissociates on the other. Such behavior favors models in which the hard scattering is controlled by the low-$x$ parton distribution function of the recoiling antiproton, just as in ND interactions, while a color-neutral soft exchange allows the antiproton to escape intact forming the rapidity gap (see, for example, Refs. [45]-[48]).
  \item **High-$t$ region.** In $\bar{p}p$ and $pp$ elastic scattering at collider energies, a diffraction minimum (dip) in the $t$ distribution is observed, with its value decreasing as $\sqrt{s}$ increases (see, e.g., Ref. [49]). Recently, the D0 collaboration reported a preliminary Tevatron Run II result on elastic $\bar{p}p$ scattering at $\sqrt{s} = 1960$ GeV, in which a dip (broadened by resolution effects) is observed at $-t \sim 0.7$ GeV$^2$ followed by a maximum (“bump”) at $-t \sim 1$ GeV$^2$ [50]. A dip in the $t$ distribution of $pp$ or $\bar{p}p$ diffraction dissociation has never been reported. In this analysis, since the quasi-elastic diffractive scattering occurs at $s' = \xi \cdot s < s$, the dip, if it exists, would be expected to lie at a higher $|t|$ than in elastic scattering and have a Gaussian-like width due to $\Delta \xi$-bin-size and
t-resolution effects.

The expected contributions to the width of a diffusive dip are summarized below:

(a) $\xi$-bin width: from Eq. (13), $\Delta t|_{\xi}$-bin = $\Delta \ln(1/\xi) = \ln(1/0.05) - \ln(1/0.08) = 0.47$;

(b) $\delta t$ and $\delta t$ resolutions: from Refs. [10, 14], $\delta t = 0.001$ and $\delta t = \pm 0.07$ GeV$^2$ for $|t| \approx 0.05$ GeV$^2$ with a dependence $\propto \sqrt{|t|}$, resulting for $|t| \approx 2.5$ GeV$^2$ in a value larger by a factor $\sqrt{2.5}/\sqrt{0.05} \approx 7$ that yields $\delta t_{\text{res}} \approx 0.5$ GeV$^2$;

(c) total width expected : $\Delta t|_{t=2.5} = \Delta t|_{\xi}$-bin + $\delta t_{\text{res}} \approx 1$ GeV$^2$, where the contributions have been added linearly, since the $\xi$-bin width is not a random variable.

These estimates show that the rather flat $-t$ distributions at large $-t$ shown in Fig. 23 are compatible with a possible existence of an underlying diffraction minimum around $-t \sim 2.5$ GeV$^2$.

VII. CONCLUSION

We present results from a measurement of diffractive dijet production in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV, $p + \bar{p} \rightarrow \{|\text{jet}1 + \text{jet}2 + X\}|_{p} + \bar{p}$, extracted from data collected in Run II of the Fermilab Tevatron $p\bar{p}$ Collider using the CDF II detector. We also present a measurement of the $t$ distribution for single-diffractive events from an inclusive single-diffractive data-sample up to $-t=4$ GeV$^2$, compare it to that of single diffractive dijet production, and search for a diffractive dip.

A system of special forward detectors including a Roman Pot Spectrometer (RPS) for measuring the momentum of the outgoing $\bar{p}$ were used. The measured diffractive dijet production rates as a function of $x_{Bj}$ (x$Bj$-Bjorken), $Q^2 \approx \langle E_T^\gamma \rangle^2$, $x_{\bar{p}}$, and $t_{\bar{p}}$ are compared with the corresponding non-diffractive rates at the same $x_{Bj}$ and $Q^2$. The physics interest in these measurements is to elucidate the QCD nature of the diffractive exchange, traditionally referred to as Pomeron exchange.

Our dijet results are extracted from data samples of diffractive and non-diffractive events corresponding to 310 pb$^{-1}$ of integrated luminosity. To reduce systematic uncertainties, the diffractive and non-diffractive data were collected simultaneously using the same calorimeter trigger to accept high-$E_T$ jets, and were similarly analyzed. The measurements cover the region of $0.03 < x_{\bar{p}} < 0.09$, $|t_{\bar{p}}| \leq 4$ GeV$^2$, $0.001 < x_{Bj} < 0.09$ and $10^2$ GeV$^2 < Q^2 < 10^4$ GeV$^2$.

The $E_T^\gamma$ distribution shapes are similar for single diffractive and non-diffractive events, and the $x_{Bj}$ distribution of the ratio of single diffractive to non-diffractive production rates is relatively flat in the region of $\beta \equiv x_{Bj}/x \leq 0.5$, where $\beta$ is the fraction of the momentum loss carried by the parton in the Pomeron that participates in the interaction. A fit of the form $R = R_{\Sigma \cdot x_{Bj}^\gamma}$ in the region of $0.001 < x_{Bj} < 0.025$, where $\beta < 0.5$, yields $r = -0.44 \pm 0.04$ and $R_{\Sigma} = (8.6 \pm 0.8) \times 10^{-3}$, consistent with the Run I CDF result of $r = -0.45 \pm 0.02$ and $R_{\Sigma} = (6.1 \pm 0.1) \times 10^{-3}$ within the normalization systematic uncertainty of $\pm 30\%$ common to the Run I and Run II data samples.

The $Q^2$ dependence of the ratio of single diffractive to non-diffractive rates is relatively weak, varying by less than a factor of $\sim 2$ over the measured $Q^2$ range within which the individual single diffractive and non-diffractive distributions vary by a factor of $\sim 10^4$.

The $t$ distributions for $-t < 1$ GeV$^2$, for the inclusive and all dijet event samples, can be fit with a sum of two exponential terms of the form $d\sigma/dt = N \cdot (A_1 \cdot e^{b_{1} \cdot t} + A_2 \cdot e^{b_{2} \cdot t})$. The slope parameters $b_1$ and $b_2$ are found to be independent of $Q^2$ over the range of $\sim 1$ GeV$^2$ (inclusive)$<Q^2<10^4$ GeV$^2$. The mean values of $b_1$ and $b_2$ are $5.27 \pm 0.33$ GeV$^{-2}$ and $1.17 \pm 0.17$ GeV$^{-2}$, respectively. Using these slopes, the above double-exponential fit is in good agreement with the prediction from the Donnachie-Landshoff (DL) model [44] for $-t \leq 0.5$ GeV$^2$.

The search for a diffraction minimum in the $t$ distribution is conducted using data with $0.05 < x_{\bar{p}}^{RPS} < 0.08$ and $-t$ up to 4 GeV$^2$. Three event-samples are studied, the inclusive sample and two dijet samples of $Q^2 \approx 225$ and $\approx 900$ GeV$^2$, respectively. The distributions for all three samples at $-t \geq 1.5$ GeV$^2$ display a flattening-out relative to the electromagnetic form factor used in the DL model, possibly due to a diffraction minimum at $-t \sim 2.5$ GeV$^2$ filled by $t$-resolution and $\xi$-dispersion effects.

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[21] Rapidity, \( y = \frac{1}{\ln \frac{1 + p_T}{1 - p_T}} \), and pseudorapidity, \( \eta = -\ln \tan \frac{\theta}{2} \), where \( \theta \) is the polar angle of a particle with respect to the proton beam (+z direction), are used interchangeably for particles detected in the calorimeters, since in the kinematic range of interest in this analysis they are approximately equal.
[26] The scattered (leading) nucleon is assumed to be the antiproton, which at CDF can be detected in a Roman Pot Spectrometer (RPS) installed along the outgoing \( p \) direction (there is no RPS on the \( p \) side).
[41] Transverse energy is defined as \( E_T = E \sin \theta \), and missing \( E_T \) as \( E_T' = |E_T - \sum_i E_{T_i} n_i| \), where \( n_i \) is a
unit vector perpendicular to the beam axis and pointing at the $i^{th}$ calorimeter tower. The sum $E_T$ is defined by $\sum E_T = \sum_i E_{iT}$. Both sums are over all calorimeter towers above the set thresholds. The missing $E_T$ significance is defined as $S_E \equiv E_T / \sqrt{\sum E_{iT}^2}$.


[50] Andrew Brandt (for the D0 Collaboration), “D0 Measurement of the elastic $p\bar{p}$ differential cross section for $0.25 < |t| < 1.2$ GeV$^2$ at $\sqrt{s} = 1.96$ TeV,” presented at XVIII International Workshop on Deep-Inelastic Scattering and Related Subjects, April 19 -23, 2010 Convitto della Calza, Firenze, Italy; Published in PoS DIS2010:059, 2010; Fermilab-conf-10-547.pdf