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## Measurement of the differential cross section $\mathrm{d} \boldsymbol{\sigma} / \mathrm{dt}$ in elastic $\mathrm{p} \overline{\mathrm{p}}$ scattering at $\sqrt{\mathrm{s}}=1.96 \mathrm{TeV}$

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We present a measurement of the elastic differential cross section $d \sigma(p \bar{p} \rightarrow p \bar{p}) / d t$ as a function of the four-momentum-transfer squared $t$. The data sample corresponds to an integrated luminosity of $\approx 31 \mathrm{nb}^{-1}$ collected with the D0 detector using dedicated Tevatron $p \bar{p}$ Collider operating conditions at $\sqrt{s}=1.96 \mathrm{TeV}$ and covers the range $0.26<|t|<1.2 \mathrm{GeV}^{2}$. For $|t|<0.6 \mathrm{GeV}^{2}$, $d \sigma / d t$ is described by an exponential function of the form $A e^{-b|t|}$ with a slope parameter $b=16.86 \pm 0.10$ (stat) $\pm 0.20$ (syst) $\mathrm{GeV}^{-2}$. A change in slope is observed at $|t| \approx 0.6 \mathrm{GeV}^{2}$, followed by a more gradual $|t|$ dependence with increasing values of $|t|$.

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## I. INTRODUCTION

The differential cross section, $d \sigma / d t$, for $p \bar{p} \rightarrow p \bar{p}$, where $t$ is the four-momentum-transfer squared [1], contains information about proton structure and nonperturbative aspects of $p \bar{p}$ interactions. In the $|t|$ range studied here, the nuclear scattering amplitude is expected to dominate [2], and with increasing $|t|, d \sigma / d t$ is expected to fall exponentially, followed by a local diffractive minimum, after which $d \sigma / d t$ continues to decrease [3].

Studies of $d \sigma / d t$ at different center-of-mass energies, $\sqrt{s}$, have demonstrated an effect known as shrinkage,

[^0]namely that the slope of the exponential fall-off of the differential cross section as a function of $|t|$ becomes larger with increasing $\sqrt{s}$, and the $|t|$ value at which the local diffraction minimum occurs is reduced [4]. It has also been observed that the shape of the local diffractive minimum is different between $p p$ and $p \bar{p}$ elastic scattering [5]. The elastic differential cross section plays an important role in constraining soft diffractive models [6-8] which cannot be directly calculated by perturbative QCD [9].

In this Article, we present a measurement of the $p \bar{p}$ elastic differential cross section at $\sqrt{s}=1.96 \mathrm{TeV}$ in the range $0.26<|t|<1.2 \mathrm{GeV}^{2}$, measured using the forward proton detector (FPD) spectrometer system of the D0 experiment [10]. Since $p$ and $\bar{p}$ elastic scattering angles are typically very small (on the order of milliradians), they are not covered by the main D0 detector. The elastically scattered protons and antiprotons are tagged with detectors inserted in the beam pipe on either side of the interaction point (IP). Our measurement extends the $|t|$ range previously studied by the CDF $\left(0.025<|t|<0.29 \mathrm{GeV}^{2}\right)$ [11] and by the E710 ( $0.034<|t|<0.65 \mathrm{GeV}^{2}$ ) [12] Collaborations at the Tevatron and constitutes the first confirmation of
a change in the $|t|$ dependence of $d \sigma(p \bar{p} \rightarrow p \bar{p}) / d t$ at center-of-mass energy $\sqrt{s}=1.96 \mathrm{TeV}$. A similar measurement in $p p$ collisions at $\sqrt{s}=7.0 \mathrm{TeV}$ has recently been reported by the TOTEM Collaboration [13] showing similar trends for the slope of the differential cross section and for the position of the local diffraction minimum, although the local minimum found in $p p$ elastic scattering is much more pronounced than the kink we observe.

This article is organized as follows. First we describe, in Sec. II, the D0 detector, with particular emphasis on the FPD. Next, in Sec. III, we discuss various aspects of the selection of the sample of candidate elastic scattering events, including the details on the position measurements in the FPD, their alignment, the reconstruction of $p$ and $\bar{p}$ scattering angles, the background subtraction, the measurements of acceptance and efficiencies. Systematic uncertainties are discussed in Sec. IV and the results of this measurement are described in Sec. V.

## II. D0 DETECTOR

We briefly describe the elements of the detector that are relevant for the measurement reported here. A detailed description of the D0 detector can be found in reference [10]. The central tracking system of the D0 detector comprises a silicon microstrip tracker (SMT) and a central fiber tracker (CFT), surrounded by a 2 T superconducting solenoidal magnet. The pseudorapidity [14] coverage for the tracking detectors is $|\eta|<3$ for the SMT and $|\eta|<2.5$ for the CFT. Outside of the superconducting magnet, the liquid-argon and uranium calorimeter is composed of three sections housed in separate cryostats: a central calorimeter section covering the pseudorapidity range $|\eta|<1.1$ and two end calorimeter sections that extend coverage to $|\eta| \approx 4.2$ [15]. A muon system [16], outside of the calorimetry, consists of three layers of tracking detectors and scintillation trigger counters, and large toroidal magnets for muon momentum measurement. The luminosity monitor (LM) consists of plastic scintillator arrays located at $z= \pm 140 \mathrm{~cm}$ (where $z$ is measured from the IP along the nominal direction of the proton beam), and covers the pseudorapidity range $2.7<|\eta|<4.4$. The LM is used to detect non-diffractive inelastic collisions and to make an accurate determination of the luminosity.

## A. Forward Proton Detectors

Figure 1 shows the layout of the main components of the FPD system relevant to this measurement [10]. In the center of the diagram is the interaction point, IP, at the center of the main D0 detector. A scattered proton/antiproton goes through 3 Tevatron quadrupole magnets (with a field gradient of about $20 \mathrm{~T} / \mathrm{m}$ ) which alternate defocusing in the horizontal and vertical planes,
passes through the first station of detectors, goes through a region free from magnetic field where electrostatic separators are located, and arrives at a second station of detectors.

The FPD consists of four quadrupole spectrometers on both the scattered proton (P) and scattered antiproton (A) sides plus a dipole spectrometer (not shown). Each quadrupole spectrometer is composed of two scintillating fiber detectors, one located at about $23 \mathrm{~m}\left(\mathrm{~A}_{1}\right.$ or $\left.\mathrm{P}_{1}\right)$ and the second at about $31 \mathrm{~m}\left(\mathrm{~A}_{2}\right.$ or $\left.\mathrm{P}_{2}\right)$ from the IP along the Tevatron beam line. Both detectors are either
 outer side (O) of the beam line. Given the location of the two detectors, the spectrometers on the A side are named $A_{U}, A_{D}, A_{I}$, and $A_{O}$ (a similar definition is made for the P side). The pseudorapidity range covered by the detectors is about $7.3<|\eta|<8.6$. Only the quadrupole spectrometers are used in this analysis, since the dipole spectrometer does not have any significant acceptance for elastically scattered antiprotons.

Scattered protons and antiprotons cross thin stainless steel windows at the entrance and exit of a vessel (Roman pot) containing the detectors [17]. The pots are remotely controlled and moved to within a few millimeters of the beam during stable beam conditions. The Roman pots house position detectors using $0.8 \mathrm{~mm} \times 0.8 \mathrm{~mm}$ square double-clad polystyrene scintillating fibers to detect the passage of charged particles. Each position detector consists of six layers of scintillating fibers $\left(\mathrm{U}, \mathrm{U}^{\prime}, \mathrm{V}, \mathrm{V}^{\prime}, \mathrm{X}\right.$, $\left.\mathrm{X}^{\prime}\right)$, where the scintillating fibers of the $\mathrm{U}, \mathrm{U}^{\prime}\left(\mathrm{V}, \mathrm{V}^{\prime}\right)$ layers are rotated by plus (minus) 45 degrees with respect to the vertical $\mathrm{X}, \mathrm{X}^{\prime}$ fibers (see Fig. 2).

The fibers of the "primed" planes are offset by 0.53 mm (two-thirds of a fiber width) with respect to the fibers of the "unprimed" layers. By combining the fiber information from "primed" and "unprimed" layers, we obtain "wide" fiber segments (about 1.07 mm wide) that are used for triggering and "fine" fiber segments (about 0.27 mm wide) used for offline hit reconstruction (see Fig. 3). Each detector also contains a scintillator (read out by a time-to-digital converter system [10]) which provides a time measurement for particles passing through the detector with a resolution of about 1 ns . The time measurement is used to distinguish particles coming from the center of the D0 detector from background beam halo particles (particles traveling far enough outside of the main beam core that they pass through the FPD detector).

Beyond the active areas of the detectors, matching square clear fibers transport signals from the scintillators to 16 -channel multi-anode photomultiplier tubes. The electronic signals are subsequently amplified, shaped, and sent to the D0 triggering and data acquisition system [10].

The elastic triggers are defined by the logical OR of coincident hits in all four detectors, in either of the four possible configurations of a $\bar{p}$ spectrometer and a diagonally opposite (collinear) $p$ spectrometer: $\mathrm{A}_{\mathrm{U}} \mathrm{P}_{\mathrm{D}}, \mathrm{A}_{\mathrm{D}} \mathrm{P}_{\mathrm{U}}$, $\mathrm{A}_{\mathrm{I}} \mathrm{P}_{\mathrm{O}}$, and $\mathrm{A}_{\mathrm{O}} \mathrm{P}_{\mathrm{I}}$. Several different conditions on the hits in the scintillating fiber detectors were used in the


FIG. 1: Schematic view of the Roman pot stations $\left(\mathrm{A}_{1}, \mathrm{~A}_{2}, \mathrm{P}_{1}, \mathrm{P}_{2}\right)$ comprising the forward proton detector as described in the text (not drawn to scale). The dipole spectrometer is not shown. The letters $\mathrm{U}, \mathrm{D}, \mathrm{I}$, O make reference to the up, down, inner and outer detectors, respectively.


FIG. 2: Schematic view of the design of one FPD scintillating fiber detector. $\mathrm{U}, \mathrm{U}^{\prime}, \mathrm{V}, \mathrm{V}^{\prime}, \mathrm{X}$, and $\mathrm{X}^{\prime}$ are the scintillating fiber layers. The local detector $x, y$ coordinates are indicated by the arrows. The scintillating fibers are indicated by the green stripes.
triggers: a tight ( T ) trigger that registered a single hit formed by the coincidence of $\mathrm{UU}^{\prime}, \mathrm{VV}^{\prime}, \mathrm{XX}^{\prime}$ wide segments; a medium (M) trigger that allowed up to three wide segments; and a loose (L) trigger that allowed hits formed from coincidences of two out of the three $\mathrm{UU}^{\prime}$, $\mathrm{VV}^{\prime}, \mathrm{XX}^{\prime}$ wide segments with no requirements on number of hits. To reduce backgrounds from inelastic collisions, LM vetoes (no hits in either the LM counters on the proton and antiproton sides) were included as part of the elastic triggers. The timing scintillator in each detector is only used for providing time information for off-line analysis and is not part of the triggers.

## III. ELASTIC EVENT SELECTION

An initial data sample is obtained by requiring events to satisfy one of the elastic triggers. The $p$ and $\bar{p}$ hit coordinates are measured in the FPD system using the fibers information and then used to select the sample of


FIG. 3: Schematic view of part of the $U$ and $U^{\prime}$ fiber layers with the definitions of wide and fine fiber segments. Similar definitions are used for the $\mathrm{X}, \mathrm{X}^{\prime}$ and $\mathrm{V}, \mathrm{V}^{\prime}$ fiber layers.
elastic scattering events. We align the detectors with respect to the beam and then use the beam transport matrices [18] (which are functions of the currents of the magnets located between the IP and the FPD detectors and correlate the $x, y$ coordinates and scattering angle of a particle at two specific $z$ locations) to reconstruct the paths of protons and antiprotons through this region of the Tevatron. Next, background subtraction and efficiency corrections are performed. We use a Monte Carlo (MC) event generator to apply corrections for acceptance, detector resolution, beam divergence and IP size effects.

## A. Data Sample

The data for this analysis were collected with dedicated beam conditions designed to facilitate the positioning of the FPD Roman pots as close to the beam axis as possible. The Tevatron injection tune with the betatron function of $\beta^{*}=1.6 \mathrm{~m}$ at the D0 IP was used instead of the standard $\beta^{*}=0.35 \mathrm{~m}$ lattice [19]. Additionally, only one proton bunch and one antiproton bunch were present
in the Tevatron. Scraping in the vertical and horizontal planes to remove the halo tails of the bunches was performed and the electrostatic separators were turned off before initiating collisions. The initial instantaneous luminosity was about $0.5 \times 10^{30} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$ with a lifetime of about 30 hours, corresponding to a mean number of $\approx 0.8$ interactions per bunch crossing. The recorded luminosity is about $\mathcal{L}=31 \mathrm{nb}^{-1}$, which corresponds to the sum of two data sets used in this analysis, each with different detector positions with respect to the beams. One set of data was taken with the closest detector position reaching about 4 mm with respect to the beam (data set 1 ), and the other data set was taken with detectors about 1 mm closer to the beam (data set 2). For the given instantaneous luminosity and the conditions of this store, about $33 \%$ of the elastic events are expected to be produced together with an inelastic collision in the same bunch crossing.

Approximately 20 million events were recorded using a special trigger list optimized for diffractive physics, including triggers for elastic, single diffractive, and double pomeron [20] exchange. This analysis uses elastic triggers, which make up about $10 \%$ of the total data collected. Independent triggers were used to determine efficiencies.

## B. Hit Reconstruction

We reconstruct the proton and antiproton hits using fibers with an associated signal above the same threshold as used in the FPD trigger system, that is tuned to accept hits from a minimum ionizing particle. For each fiber in an un-primed layer above threshold, we verify if there is an adjacent fiber in the primed layer in order to define a "fine" fiber segment through which the particle traversed the plane. Events with more than four fibers firing in a plane are typically not due to single particles and are rejected (more than $99 \%$ of the elastic triggered events survive this condition). We require at least two out of the three $\mathrm{UU}^{\prime}, \mathrm{VV}^{\prime}$, and $\mathrm{XX}^{\prime}$ fine segments to be reconstructed in each detector, with their intersection yielding the transverse coordinates of the hit. Since noise in some of the fibers could produce fake hits, in the case of more than one reconstructed hit in a detector (which happens in about $10 \%$ of the events), we weight the hits by the sum of the analog-to-digital converter (ADC) pulse height of all the fibers that contributed to each hit and retain only the hit with the highest weight. The correction for the selection efficiency, discussed in Sec. IIII, accounts for elastic events discarded by this requirement.

Utilizing events with fine segments in $\mathrm{U}, \mathrm{V}$, and X , we are able to estimate the offset in position and resolution within each detector by taking the difference between the $x$ coordinate obtained from UV fiber intersection and a similar measurement using the X fiber plane. Most of the detectors used in this analysis have a resolution of about $150 \mu \mathrm{~m}$ with the exception of some of the A 2 detectors


FIG. 4: Comparison of detector $y$ coordinates in the spectrometers a) $P_{U}$ and b) $P_{D}$.
that had several inactive scintillating fibers, degrading their resolution to about $250 \mu \mathrm{~m}$.

## C. Selection of Candidate Elastic Events

Elastic collisions produce one of the four possible hit configurations in the FPD: $A_{U} \mathrm{P}_{\mathrm{D}}, \mathrm{A}_{\mathrm{D}} \mathrm{P}_{\mathrm{U}}, \mathrm{A}_{\mathrm{I}} \mathrm{P}_{\mathrm{O}}, \mathrm{A}_{\mathrm{O}} \mathrm{P}_{\mathrm{I}}$. Since the inner and outer detectors are farther from the beam than the U and D detectors, they have poorer acceptance for elastic events and are only used for alignment purposes (see Sec. IIID). If we compare the hit coordinates reconstructed by each of the two detectors of one spectrometer, we observe a correlation band from particles going through the spectrometer, but also observe some uncorrelated background hits (see Fig. 4). We require hits to lie within $\pm 3 \sigma(\sigma \approx 220 \mu \mathrm{~m})$ from the center of the band. We determine the quantity $\sigma$ by fitting a Gaussian distribution obtained by projecting the hits onto an axis perpendicular to the correlation band.

We then investigate the correlation between the co-
ordinates of the protons and antiprotons in diagonally opposite spectrometers. In addition to the expected correlation due to the collinearity of elastic events, some background contamination due to halo particles remains. This contribution is reduced through the use of the FPD timing system, but there is still some residual background, partially due to inefficiency of the trigger scintillators and to different acceptances of the spectrometers. A correction for the contribution from halo within the correlation band is discussed in Sec. III F.

For a specific set of $p$ and $\bar{p}$ spectrometers in an elastic combination, we observe that elastic events with a proton passing through a small region of the detectors in one spectrometer will have $\bar{p}$ positions distributed over a similar but somewhat larger region of the diagonally opposite spectrometer. Depending on the location of the proton, the Gaussian distribution of the $\bar{p}$ position may be truncated due to the finite detector size. After calculating the $\bar{p}$ acceptance correction as a function of the coordinates of the proton spectrometer, a fiducial cut is applied in the $\mathrm{P}_{1}$ detectors such that only regions in these detectors which require a correction of $2 \%$ or less are used. The region we select in the $\mathrm{P}_{1}$ detectors is thus guaranteed to correspond to an acceptance greater than $98 \%$ in the other three detectors. Figure 5 shows the $y_{p}$ vs $y_{\bar{p}}$ coordinate correlation plots ( $y$ coordinate measured in the local coordinate system shown in Fig. 6), the tagging of the hits according to time-of-flight information, and the fiducial cuts applied (indicated by the dashed lines). We also check that there is no activity in the calorimeter for events in the elastic data sample. The contribution to the elastic sample from events that have a non-zero energy in the calorimeter is less than $0.1 \%$ of the total number of selected events. Most of the elastic events produced in beam crossings with multiple $p \bar{p}$ interactions are suppressed by the vetoes on the LM detectors.

## D. Forward Proton Detector Alignment

In order to reconstruct the tracks from the protons and antiprotons, we first align the detectors with respect to the beam and then determine the position and angle of a particle at the IP from the measured hit positions in the FPD detectors after application of the Tevatron transport matrices.

The location of the detectors with respect to the beam is determined using a sample of tracks that pass through one vertical and one horizontal detector at the same Roman pot station, allowing determination of the relative alignment of the detectors. We use elastic events to align one horizontal detector that did not have any overlap with the other detectors at the same $z$ location. We define the center of a vertical and a horizontal pot at each Roman pot station and then measure the positions of all four detectors with respect to this reference system. Due to the beam optics the $x(y)$ hit coordinate distributions in the vertical proton (horizontal antiproton) detectors
are narrower than in the vertical antiproton (horizontal proton) detectors. Because of this effect, the offset of the beam in $x$ for the vertical proton detectors (and the offset of the beam in $y$ for the horizontal antiproton detectors) is determined by fitting a Gaussian distribution to the $x$ and $y$ distributions in these detectors. All other beam offsets are obtained given the fact that the reconstructed IP offset and scattering angle is the same for both the proton and antiproton in an elastic event. We take the average over all four elastic combinations to determine the offset of the beam at each Roman pot station. Figure 6 shows the position of each detector obtained with the alignment procedure described above for the data set corresponding to the detector configuration with Roman pots located closest to the beam. The coordinates are plotted with respect to the beam coordinate system (dashed lines shown in the figure). For the data collected with the Roman pots retracted further away from the beam line, we use positional difference information obtained from the pot motion system added to the previously determined aligned positions. The uncertainty of the location of the detectors after the alignment procedure is estimated to be about $200 \mu \mathrm{~m}$.

## E. Reconstruction of $p / \bar{p}$ tracks and $|t|$ measurement

The Tevatron transport matrices are unique for these data due to the use of the injection lattice. The beam radius (at $1 \sigma$ level) ranges from 0.4 mm to 0.8 mm at the different FPD detector locations while the beam divergence is about $44 \mu \mathrm{rad}$. The change in the proton or antiproton divergence caused by the quadrupoles system is typically of the order of 1 mrad for the smallest $|t|$ values considered in this measurement.

The size of the IP in $x, y$ and $z$ is typically determined by reconstructing the primary vertex using the tracking detectors [10]. Given the absence of central tracks in elastic events, data from non-elastic triggers, simultaneously collected with the elastic scattering events used in this analysis, are used to obtain the $x, y$ and $z$ distributions of the IP. The size of the IP in each direction is obtained by fitting a Gaussian function to each distribution. The measured Gaussian width of the IP distribution is about $100 \mu \mathrm{~m}$ in the transverse plane and about 45 cm along the $z$ axis (see Fig. 7). The offsets observed in $x$ and $y$ from the primary vertex reconstruction are due to the fact that the center of the tracker is shifted with respect to the beam line. We use the reconstructed elastic events to determine these offsets, as described below.

To tag an elastic event, we reconstruct the coordinates of the hits in the two proton and two antiproton detectors. The difference of coordinates between a proton and antiproton detector yields a Gaussian distribution with a width related to the fiber offset and resolution of the two detectors, the IP size, and the beam divergence. Given the previously estimated detector resolutions and IP size,


FIG. 5: The correlation plots $y_{p}$ vs $y_{\bar{p}}$ for the first detectors in the spectrometers ( $y$ coordinates measured in the local coordinate system shown in Fig. 6) for $A_{U} P_{D}$ and $A_{D} P_{U}$. Plots a) and d) show the correlations without any timing requirement; b) and e) correspond to hits with a coincident tag in the corresponding scintillator early time windows; c) and f) show events with no hits within the early time window (most of the hits in this case are in the in-time window). The dashed lines correspond to the fiducial requirements applied.


FIG. 6: Detector positions with respect to beam center (dashed lines) for the data set corresponding to the closest pot insertion to the beam. The arrows indicate the local coordinate system in each detector.
these distributions can be used to estimate the beam divergence. The values obtained are similar ( $40 \pm 5 \mu \mathrm{rad}$ ) to those estimated using the injection tune lattice parameters. With the coordinates of the two detectors in each


FIG. 7: Size of the IP determined by the reconstruction of the primary vertex from non-elastic triggers (black points) fitted with a Gaussian function (solid line). a) $x$ distribution of the IP. b) $y$ distribution of the IP. c) $z$ distribution of the IP.
spectrometer we determine the offsets of the IP $\left(x_{0}, y_{0}\right)$ and the horizontal and vertical scattering angles $\left(\theta_{x}, \theta_{y}\right.$ respectively) by using the following equations:

$$
\begin{align*}
x_{i} & =M_{x, i} x_{0}+L_{x, i} \theta_{x}  \tag{1}\\
y_{i} & =M_{y, i} y_{0}+L_{y, i} \theta_{y}
\end{align*}
$$

where $x_{i}, y_{i}$ are the hit coordinates in a detector $i$ and $M_{x, i}, L_{x, i}\left(M_{y, i}, L_{y, i}\right)$ are the transport matrix elements


FIG. 8: Difference in the reconstructed $|t|$ between $p$ and $\bar{p}$ vertical spectrometers. The MC (solid line) expected distribution is compared to data (solid points). a) $\mathrm{A}_{\mathrm{U}} \mathrm{P}_{\mathrm{D}}$ combination. b) $A_{D} P_{U}$ combination. The number of entries in each distribution is normalized to unity.
in the horizontal (vertical) axis for that detector location. We verify that the distributions of the difference of the IP offsets and scattering angles obtained from the proton spectrometer and the antiproton spectrometer for every event are centered around zero. Since the values of $\theta$ obtained are of the order of milliradians, the four-momentum-transfer squared, $t$, can be approximated as

$$
\begin{equation*}
t=-p^{2}\left(\theta_{x}^{2}+\theta_{y}^{2}\right) \tag{2}
\end{equation*}
$$

where $p$ is the momentum of the scattered particle. Given that the momenta of the elastically scattered proton and antiproton are the same as that of the incoming particles $(980 \mathrm{GeV})$ and that the beam momentum spread is negligibly small ( $0.014 \%$ ) [21], the uncertainty in $|t|$ is dominated by the measurement uncertainty of the scattering angle. Figure 8 shows the difference in the reconstructed $|t|$ from the $\bar{p}$ and $p$ vertical spectrometers, $\Delta|t|=|t|_{\bar{p}}-|t|_{p}$. The non-zero standard deviation of $\Delta|t|, \sigma_{\Delta t}$, is due to the resolution on $|t|_{p}$ and $|t|_{\bar{p}}$. The average of $|t|_{p}$ and $|t|_{\bar{p}}\left(|t|_{\text {ave }}=\left(|t|_{p}+|t|_{\bar{p}}\right) / 2\right)$ has a resolution of approximately $\sigma_{\Delta|t|} / 2$. The $|t|$ bin size is chosen as the largest of the observed $\sigma_{\Delta|t|}$ for the two detector combinations $A_{U} P_{D}$ and $A_{D} P_{U}$, where the difference in $\sigma_{\Delta|t|}$ results from different detector resolutions. We also study the $|t|$ resolution as a function of $|t|$ and observe a gradual increase with $|t|$, from $0.02 \mathrm{GeV}^{2}$ to $0.04 \mathrm{GeV}^{2}$, which is reflected in the bin widths.

## F. Background Subtraction

The primary source of background in the selected sample is due to beam halo, consisting of either a halo proton and a halo antiproton in the same bunch crossing or a halo particle combined with a single diffractive event.

A halo particle passing through the proton detectors in the time window for the protons which have undergone elastic scattering usually passes through the diagonally opposite antiproton detector at an earlier time (and vice versa). Therefore, the time information can be used to veto events with early time hits, consistent with halo protons and antiprotons in the elastic sample. The veto is not $100 \%$ efficient due to a combination of scintillator efficiency and positioning of the detectors with respect to the beam (a closer detector position both increases a detector's signal acceptance and its ability to reject halo). Consequently, it is necessary to subtract the remaining background. We consider an event to be caused by $\bar{p}(p)$ halo if one or both of the two $p(\bar{p})$ detectors of an elastic combination have hits in their early time interval. We require events to have no activity in either the $\bar{p}_{\text {halo }}$ or the $p_{\text {halo }}$ timing window. We select background samples by requiring hits consistent with $p$ halo and $\bar{p}$ halo simultaneously. First, we verify that outside the elastic correlation band between the coordinates of a proton and antiproton detector the signal tagged events have the same $|t|$ dependence as the background tagged ones (see Fig. 5). Next, assuming that signal and background tagged events also have the same $|t|$ dependence inside the correlation band, we use the ratio of these two distributions and use it to estimate the percentage of background events inside the signal tagged correlation band. This background is subtracted from all events inside the correlation band to obtain $d N / d t$ as a function of $|t|$. The amount of background subtracted inside the elastic correlation band varies from $1 \%$ at low $|t|$ to $5 \%$ at high $|t|$. The absolute uncertainty of the background, which is propagated as a statistical uncertainty to $d \sigma / d t$, varies from $0.3 \%$ at low $|t|$ to $5.0 \%$ at high $|t|$. As a cross check, we vary the detector band cuts from $3.0 \sigma$ to $3.5 \sigma$ and to $6.0 \sigma$, to allow more background, and obtain similar $d N / d t$ results after applying the same background subtraction procedure (within $1 \%$ ).

## G. Monte Carlo Simulation of Elastic Events

We have developed a MC generator interfaced with the Tevatron transport matrices to generate elastic events. The MC allows us to study the geometrical acceptance of the detectors, resolution of the position measurement, alignment, and effects of the beam size and beam divergence at the IP. The generation of events is based on an Ansatz function that we obtain by fitting the $d N / d t$ distribution of the data. We study the acceptance and bin migration effects using samples generated with a wide range of different $d N / d t$ Ansatz distributions. The variations in the corrections are included as systematic uncertainties.

The positions of hits in each detector are transformed into fiber hit information, and the reconstruction then proceeds using these hits, following the same procedure as with the data. The reconstructed correlation patterns


FIG. 9: Comparison of MC (solid line) and data (black points) for the coordinate difference $y_{p}-y_{\bar{p}}$ for the elastic configuration $\mathrm{A}_{1, \mathrm{U}} \mathrm{P}_{1, \mathrm{D}}$ for the data set with detectors closer to the beam.
in MC are in good agreement with those observed in data. In addition, the MC also predicts the widths of the different correlations as shown in Fig. 8 and Fig. 9 .

## H. Acceptance and Bin Migration Correction

Due to accelerator optics, protons and antiprotons of a particular $|t|$ are transported to an elliptical region in the $x-y$ plane at each detector location. Each detector has a different coverage in the azimuthal angle $\phi$ and therefore a different coverage of the ellipses of constant $|t|$. The $\phi$ acceptance correction accounts for the fraction of the $|t|$ ellipse for each $|t|$ bin that is not covered by the fiducial area used in each detector. This correction depends only on the detector location with respect to the particle beam and on the geometry of the fiducial area used in the detector for selecting the events. Figure 10 shows the $\phi$ acceptance calculated as a function of $|t|$ for data at the closest detector position with respect to the beam and after the fiducial cuts. We obtain similar results for the $\phi$ acceptance using the MC described in the previous section before adding the effects of beam divergence, IP size and detector resolution. The uncertainty in the $\phi$ acceptance correction, which comes from the size of the MC sample used, is less than $0.1 \%$ at low $|t|$ values and less than $1.0 \%$ at high $|t|$ values. To estimate the correction for bin migration effects that is applied in data to obtain the $d \sigma / d t$ distribution, we include the measured values of beam divergence, IP size, detector resolution and pot position uncertainties in the MC generator and compare to a same size MC sample with no smearing effects.


FIG. 10: Azimuthal acceptance of the FPD in data, after fiducial cuts, for the closest detector position of the $\mathrm{A}_{\mathrm{U}} \mathrm{P}_{\mathrm{D}}$ elastic combination. The points correspond to MC, the solid line corresponds to the calculation of the $\phi$ acceptance from the detector positions and the fiducial area.

## I. Selection and Trigger Efficiencies

We simultaneously determine the effects of selection and trigger efficiencies for each of the four detectors corresponding to an elastic configuration. To determine the efficiency of a particular detector, we use an independent trigger which does not include that detector. We obtain the $d N / d t$ distributions with an elastic track reconstructed in the other three detectors and for all four detectors, with the trigger conditions satisfied. The ratio of the two distributions is used to extract the efficiency of the detector as a function of $|t|$ (where $|t|$ is reconstructed from the coordinates of the opposite side spectrometer). To avoid any additional effect from detector acceptance, we use only hits in the other three detectors in a region determined to have full geometrical acceptance in the detector of interest. We repeat a similar procedure for each of the four detectors in every elastic combination and multiply the efficiencies of the four detectors to determine the final efficiency correction. Typical selection and trigger efficiencies are in the range of $50 \%$ to $70 \%$ depending on the detector and trigger requirements. Additionally, we make a correction for the veto in the LM which was part of the elastic trigger. This veto filters out elastic events that are produced in coincidence with an inelastic collision in the same bunch crossing (pileup). To make this correction, we use a trigger based on hits in the proton spectrometers with no LM requirement and determine the fraction of candidate elastic events reconstructed in coincidence with the LM. We find that about $27 \%(20 \%)$ of elastic events for data set 1 (2) as defined in Sec. III A were removed by the LM veto.

## J. Luminosity

Since elastic data were collected with Tevatron conditions modified with respect to standard operations of the D0 experiment, we compare the number of inclusive jet events obtained from our data to the number of jet events used for the inclusive cross section measurement discussed in [22] to determine the integrated luminosity. The corresponding integrated luminosity for data set 1 (2) is $18.3 \mathrm{nb}^{-1}\left(12.6 \mathrm{nb}^{-1}\right)$, with an uncertainty of $13 \%$. We add in quadrature the uncertainty in the standard luminosity determination ( $6.1 \%$ [23]) and obtain an overall normalization uncertainty of $14.4 \%$.

## IV. SYSTEMATIC UNCERTAINTIES

The major $|t|$-dependent contributions to the systematic uncertainties in the measurement of $d \sigma / d t$ are due to detector efficiencies, beam divergence, detector positions, and the choice of the Ansatz function. The luminosity measurement contributes to the overall normalization uncertainty. The Tevatron beam transport matrices are known with high precision (within $0.1 \%$ ) and therefore produce a small uncertainty in our results compared to the other sources. We take the uncertainty in the position of the pot from the beam center as an extra "smearing" factor for the hit coordinates in the MC. Since the efficiencies vary with $|t|$, we fit either a polynomial or an exponential function to each trigger efficiency and propagate the uncertainties in the fit parameters to $d \sigma / d t$, using the covariance matrix of the fit. For the beam divergence term, we vary the beam divergence by $\pm 5 \mu \mathrm{rad}$ in the MC, and we propagate the change in the acceptance correction bin-by-bin to $d \sigma / d t$. We also consider 26 possible variations of the Ansatz function used in the MC to account for the uncertainties in the logarithmic slopes before and after the kink and also for the $|t|$ value where the kink is observed.

## V. RESULTS

In total, we have four independent measurements of $d \sigma / d t$ that come from the two elastic combinations $\left(\mathrm{A}_{\mathrm{U}} \mathrm{P}_{\mathrm{D}}\right.$ and $\left.\mathrm{A}_{\mathrm{D}} \mathrm{P}_{\mathrm{U}}\right)$ and two data sets, which agree with each other within the uncertainties. We combine the four measurements using a bin-by-bin weighted average. The resulting values for the $d \sigma / d t$ distribution, together with their total uncertainties, are listed in Table I and shown in Fig. 11. The uncertainties are the total experimental uncertainties excluding the $14.4 \%$ normalization uncertainty. The $|t|$ bin centers are determined using the prescription described in [24], however, the values found are very close to the middle of the bin. Two phenomenological model predictions for $\sqrt{s}=1.96 \mathrm{TeV}$ (BSW [25], Islam et al. [26]) are also shown. The BSW model shows a good description of the data in shape and normalization

TABLE I: The $d \sigma / d t$ differential cross section. The statistical and systematic uncertainties are added in quadrature. The luminosity uncertainty of $14.4 \%$ is not included.

| $\|t\|\left(\mathrm{GeV}^{2}\right)$ | $d \sigma / d\|t\|\left(\mathrm{mb} / \mathrm{GeV}^{2}\right)$ |
| :---: | :---: |
| 0.26 | $(47.3 \pm 2.6) \times 10^{-1}$ |
| 0.30 | $(21.4 \pm 0.72) \times 10^{-1}$ |
| 0.34 | $(10.6 \pm 0.37) \times 10^{-1}$ |
| 0.38 | $(5.64 \pm 0.22) \times 10^{-1}$ |
| 0.42 | $(2.98 \pm 0.14) \times 10^{-1}$ |
| 0.46 | $(14.2 \pm 0.83) \times 10^{-2}$ |
| 0.50 | $(7.46 \pm 0.51) \times 10^{-2}$ |
| 0.54 | $(3.81 \pm 0.36) \times 10^{-2}$ |
| 0.58 | $(2.20 \pm 0.30) \times 10^{-2}$ |
| 0.64 | $(1.04 \pm 0.13) \times 10^{-2}$ |
| 0.72 | $(1.19 \pm 0.17) \times 10^{-2}$ |
| 0.80 | $(9.28 \pm 1.5) \times 10^{-3}$ |
| 0.88 | $(11.2 \pm 1.7) \times 10^{-3}$ |
| 0.96 | $(8.1 \pm 1.5) \times 10^{-3}$ |
| 1.04 | $(5.77 \pm 1.3) \times 10^{-3}$ |
| 1.12 | $(5.73 \pm 1.3) \times 10^{-3}$ |
| 1.20 | $(2.84 \pm 1.7) \times 10^{-3}$ |



FIG. 11: The measured $d \sigma / d t$ differential cross section. The normalization uncertainty of $14.4 \%$ is not shown. The uncertainties are obtained by adding in quadrature statistical and systematic uncertainties. The predictions of BSW ([25]) and Islam et al. ([26]) are compared to the data.
and is able to reproduce the kink within experimental uncertainties.

The $|t|$ range covered by our measurement is $0.26<|t|<1.2 \mathrm{GeV}^{2}$. We observe a change in the logarithmic slope of the $d \sigma / d t$ distribution at $|t| \approx 0.6 \mathrm{GeV}^{2}$. A fit to the $d \sigma / d t$ distribution in the range $0.26<|t|<0.6$ with an exponential function of the form $A e^{-b|t|}$ yields a logarithmic slope parameter of $b=16.86 \pm 0.10$ (stat) $\pm 0.20$ (syst) $\mathrm{GeV}^{-2}$


FIG. 12: The $d \sigma / d t$ differential cross section measured by the D0 Collaboration and compared to the CDF and E710 measurements at $\sqrt{s}=1.8 \mathrm{TeV}$, and to the UA4 measurement at $\sqrt{s}=0.546 \mathrm{TeV}$ (scaled by a factor of 100). A normalization uncertainty of $14.4 \%$ on the D0 measurement is not shown.
( $\chi^{2}=6.63$ for 7 degrees of freedom).
Figure 12 shows a comparison of our results to those obtained at $\sqrt{s}=1.8 \mathrm{TeV}$ by the CDF and E710 Tevatron Collaborations [11, 12], and also to that of the UA4 Collaboration at $\sqrt{s}=0.546 \mathrm{TeV}$ [27]. Our measurement of the slope parameter agrees within uncertainties with previous measurements by the CDF ( $b=16.98 \pm 0.25$ $\left.\mathrm{GeV}^{-2}\right)$ and E710 ( $b=16.30 \pm 0.30 \mathrm{GeV}^{-2}$ ) Collabora-
tions. A comparison of the shape of our measured $d \sigma / d t$ to UA4 measurement shows that the kink in $d \sigma / d t$ moves towards lower $|t|$ values as the energy is increased, but, as in the UA4 data, we do not see a distinct minimum as observed in $p p$ elastic interactions ([13]).

In summary, we have presented the first measurement of $d \sigma(p \bar{p} \rightarrow p \bar{p}) / d t$ as a function of $|t|$ at $\sqrt{s}=1.96 \mathrm{TeV}$. Our measurement extends the $|t|$ and $\sqrt{s}$ range previously studied and shows a change in the $|t|$ dependence, consistent with the features expected for the transition between two diffractive regimes.

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