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We report the first observation of the radiative decay $B^0 \rightarrow \phi K^0 \gamma$ using a data sample of $772 \times 10^6 B\bar{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric-energy $e^+e^-$ collider. We observe a signal of $37 \pm 8$ events with a significance of 5.4 standard deviations including systematic uncertainties. The measured branching fraction is $B(B^0 \rightarrow \phi K^0 \gamma) = (2.74 \pm 0.60 \pm 0.32) \times 10^{-6}$, where the uncertainties are statistical and systematic, respectively. We also report the first measurements of time-dependent CP violation parameters: $S_{\phi K^0 \gamma} = +0.74^{+0.72}_{-1.07}$ (stat) $^{+0.22}_{-0.25}$ (syst) and $A_{\phi K^0 \gamma} = +0.35 \pm 0.58$ (stat) $^{+0.23}_{-0.30}$ (syst). Furthermore, we measure $B(B^+ \rightarrow \phi K^+ \gamma) = (2.48 \pm 0.30 \pm 0.24) \times 10^{-6}$, $A_{\phi} = -0.03 \pm 0.11 \pm 0.08$ and find that the signal is concentrated in the $M_{\phi K}$ mass region near threshold.


Rare radiative $B$ meson decays play an important role in the search for physics beyond the standard model (SM). These are flavor changing neutral current decays, forbidden at tree level in the SM but allowed through electroweak loop processes. The loop can be mediated by non-SM particles (for example, charged Higgs or SUSY particles) and therefore is sensitive to new physics (NP). Here we report the first observation of a new $b \rightarrow s$ radiative penguin decay mode, $B^0 \rightarrow \phi K^0 \gamma$, as well as measurements of its time-dependent CP asymmetry. This type of decay is sensitive to NP from right-handed currents [1] and will be useful for precise time-dependent measurements at future high-luminosity flavor facilities [2–4].

The emitted photons in $b \rightarrow s \gamma \bar{b} \rightarrow \pi \gamma$ decays are predominantly left-handed (right-handed) in the SM, and hence the time-dependent CP asymmetry is suppressed by the quark mass ratio $(2m_s/m_b)$. The expected mixing-induced CP asymmetry parameter ($S$) is $O(3\%)$ and the direct CP asymmetry parameter ($A$) is $\sim 0.6\%$ [1]. In several extensions of the SM, both photon helicities can contribute to the decay. Therefore, any significantly larger CP asymmetry would be clear evidence for NP. In contrast to $B^0 \rightarrow K^{0*}(\rightarrow K_S^0 \pi^0) \gamma$ [5, 6], another related mode that is sensitive to NP, the time dependence of $B^0 \rightarrow \phi K_0^0 \gamma$ can be measured from the $\phi \rightarrow K^+ K^-$ decay and does not require a difficult measurement of the long lived $K_0^0$ decay inside the inner tracking volume or reconstruction of a low energy $\pi^0$. The $B \rightarrow \phi K \gamma$ mode can be used to search for a possible contribution from kaonic resonances decaying to $\phi K$. Furthermore, we can also probe the photon polarization using the angular distributions of the final state hadrons [7].

Results on $B \rightarrow \phi K \gamma$ decays have been reported by both Belle and BaBar collaborations based on $96 \times 10^6 B\bar{B}$ [8] and $228 \times 10^6 B\bar{B}$ [9] pairs, respectively. Only upper limits on $B(B^0 \rightarrow \phi K^0 \gamma)$ were given. Here we report the first observation of $B^0 \rightarrow \phi K^0 \gamma$, the first measurements of time-dependent CP violation in this mode, as well as more precise measurements of $B^+ \rightarrow \phi K^+ \gamma$ [10]. The data set used consists of $772 \times 10^6 B\bar{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the Belle detector [11] at the KEKB asymmetric-energy $e^+e^-$ (3.5 on 8.0 GeV) collider [12].

At KEKB, the $\Upsilon(4S)$ is produced with a Lorentz boost of $\beta\gamma = 0.425$ along the $z$ axis, which is defined as opposite to the $e^+$ beam direction. In the decay chain $\Upsilon(4S) \rightarrow B^0 \bar{B}^0 \rightarrow f_{\text{rec}} f_{\text{tag}}$, where one of the $B$ mesons decays at time $t_{\text{rec}}$ to the signal mode $f_{\text{rec}}$ and the other decays at time $t_{\text{tag}}$ to a final state $f_{\text{tag}}$ that distinguishes between $B^0$ and $\bar{B}^0$, the decay rate has a time depen-
dence given by
\[
\mathcal{P}(\Delta t) = \frac{e^{-|\Delta t|/\tau_B}}{4\tau_B} \left\{ 1 + q \left[ S \sin(\Delta m_d \Delta t) + A \cos(\Delta m_d \Delta t) \right] \right\}.
\]

Here $\tau_B$ is the neutral lifetime, $\Delta m_d$ is the mass difference between the two neutral B mass eigenstates, $\Delta t = t_{\text{rec}} - t_{\text{tag}}$, and the b-flavor charge $q$ equals $+1 \,-(1)$ when the tagging B meson is a $B^+$ ($\bar{B}^0$). Since the $B^0$ and $\bar{B}^0$ are approximately at rest in the $\Upsilon(4S)$ center-of-mass system (cms), $\Delta t$ can be determined from $\Delta z$, the displacement in $z$ between the two decay vertices: $\Delta t \simeq \Delta z/(\beta \gamma) c$.

Signal candidates are reconstructed in the $B^+ \rightarrow \phi K^+\gamma$ and $B^0 \rightarrow \phi K^0_S\gamma$ modes, with $\phi \rightarrow K^+K^-$ and $K^0_S \rightarrow \pi^+\pi^-$. Charged kaons are identified by requiring a likelihood ratio $L_{K/\pi} = [L_K/(L_K + L_\pi)] > 0.6$, which is calculated using information from the aerogel Cherenkov, time-of-flight, and drift chamber detectors. This requirement has an efficiency of 90% for kaons and an 8% pion fake rate. A less restrictive selection $L_{K/\pi} > 0.4$ is applied to the kaon candidates that are used to reconstruct the $\phi$ meson. The invariant mass of the $\phi$ candidates is required to satisfy $|M_{K^+K^-} - m_\phi| < 10 \text{ MeV}/c^2$, where $m_\phi$ denotes the $\phi$ meson world-average mass [13]. The $K^0_S$ selection criteria are the same as those described in Ref. [14]; the invariant mass of the pion pairs should be in the range $M_{\pi^+\pi^-} \in [482, 514] \text{ MeV}/c^2$. The high energy prompt photons must lie in the barrel region of the calorimeter (ECL), have a cms energy $E_{\gamma}^\text{cms} \in [1.4, 3.4]$ GeV and a shower shape consistent with that of a photon. We also suppress the background photons from $\pi^0(\eta) \rightarrow \gamma \gamma$ using a likelihood $L_{\pi^0(\eta)} < 0.25$, as described in Ref. [15].

We combine a $\phi$ meson candidate, a charged or neutral kaon candidate, and a radiative photon to form a $B$ meson. $B$ candidates are identified using two kinematic variables: the energy difference $\Delta E \equiv E_B - E_{E_{\gamma}^\text{cms}} - E_{\text{beam}}$ and the beam-energy-constrained mass $M_{bc} \equiv \sqrt{(E_{E_{\gamma}^\text{cms}}/c^2)^2 - (p_B^\text{cms}/c)^2}$, where $E_{\text{beam}}$ is the beam energy in the cms, and $E_{E_{\gamma}^\text{cms}}$ and $p_B^\text{cms}$ are the cms energy and momentum, respectively, of the reconstructed $B$ candidate. In the $M_{bc}$ calculation, the photon momentum is replaced by $(E_{E_{\gamma}^\text{cms}} - E_{\gamma^*})$ to improve its resolution. The candidates that satisfy the requirements $M_{bc} > 5.2 \text{ GeV}/c^2$ and $|\Delta E| < 0.3$ GeV are retained for further analysis. Using Monte Carlo (MC) simulations, we find nearly 12% (3%) of signal events in the charged (neutral) mode have more than one $B$ candidate. In case of multiple candidates, we choose the best candidate based on a series of selection criteria, which depend on a $\chi^2$ variable formed using the candidate's $\phi$ mass (and the $K^0_S$ mass in the neutral mode) as well as the highest $E_{E_{\gamma}^\text{cms}}$ and the highest $L_{K/\pi}$ in the charged mode. For events with multiple candidates, this selection method chooses the correct $B$ candidate for the charged (neutral) mode 57% (69%) of the time.

The dominant background comes from $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) continuum events. We use two event-shape variables [a Fisher discriminant formed from modified Fox-Wolfram moments [16] and the cosine of the angle between the $B$ flight direction and the beam axis, $\cos\theta_B$ (in the cms frame)] to distinguish spherically symmetric $B\bar{B}$ events from the jet-like continuum background. From these variables we form a likelihood ratio, denoted by $R_{q/b}$. We require $R_{q/b} > 0.65$, which removes 91% of the continuum while retaining 76% of the signal. In addition to the continuum, various $B\bar{B}$ background sources are also studied. In the $B^0 \rightarrow \phi K^0_S \gamma$ mode, backgrounds from some $b \rightarrow c$ decays such as $D^0\pi^0$, $B^0\eta$, and $D^-\rho^+$, peak in the $M_{bc}$ distribution. We remove the dominant peaking backgrounds by applying a veto to $\phi K^0_S$ combinations consistent within detector resolution ($\pm 4\sigma$) with the nominal $D$ mass [13]. Some of the charmless backgrounds, where the $B$ meson decays to $\phi K^*(892), \phi K^0\pi^0$ and $\phi K\eta$ also peak in $M_{bc}$ but shift towards lower $\Delta E$. Another significant background is non-resonant (NR) $B \rightarrow K^+K^-K_\gamma$, which peaks in the $\Delta E$-$M_{bc}$ signal region; it is estimated using the $\phi$ mass sideband, $M_{K^+K^-} \in [1.05, 1.30] \text{ GeV}/c^2$, in data.

![Image](image_url)

**FIG. 1:** $\Delta E$ and $M_{bc}$ projections for $B^+ \rightarrow \phi K^+\gamma$ (upper) and $B^0 \rightarrow \phi K^0_S\gamma$ (lower). The $\Delta E$ projections include the requirement $M_{bc} \in [5.27, 5.29] \text{ GeV}/c^2$ while the $M_{bc}$ projections require $\Delta E \in [-0.08, 0.05] \text{ GeV}$. The points with error bars are the data. The curves show the total fit function (solid red), total background function (long-dashed black), continuum component (dotted blue), the $b \rightarrow c$ component (dashed-dotted green) and the non-resonant component as well as other charmless backgrounds (filled magenta histogram).

The signal yield is obtained from an extended unbinned maximum-likelihood (UML) fit to the two-dimensional $\Delta E$-$M_{bc}$ distribution. We model the shape for the signal component using the product of a Crystal Ball line
shape [17] for $\Delta E$ and a Gaussian for $M_{bc}$. The continuum background is represented by the product of a first-order polynomial for $\Delta E$ and an ARGUS [18] function for $M_{bc}$. The $b \to c$ background is described by the product of a second-order polynomial for $\Delta E$ and the sum of an ARGUS and a Gaussian function for $M_{bc}$. For the small charmless backgrounds (except for the NR component), we use the sum of two Gaussians for $\Delta E$ and a Gaussian for $M_{bc}$. The probability density function (PDF) is the product of these two functional forms [19].

In the final fit the continuum parameters are allowed to vary while all other background parameters are fixed to the values from MC simulations. The shapes of the $b \to c$ and NR peaking background components are fixed to that of the signal. In the charged mode, the NR background yield, $(12.5 \pm 6.7)\%$ of the signal, is fixed from the $\phi$ mass sideband. Since the neutral mode is limited by statistics, we assume isospin symmetry and use the same NR fraction. The signal shapes are adjusted for small differences between MC simulations and data using a $B^0 \to K^+(892)^0(\to K^+\pi^-\gamma)$ control sample, with $M_{K^+\pi^-} \in [820,970] \text{ MeV}/c^2$. The fit yields a signal of 144 $\pm 17$ $B^+ \to \phi K^+\gamma$ and 37 $\pm 8$ $B^0 \to \phi K^0_s\gamma$ events. The projections of the fit results onto $\Delta E$ and $M_{bc}$ are shown in Fig. 1. The signal significance is defined as $140 \pm 6 \sqrt{\ln(L_0/L_{\text{max}})}$, where $L_{\text{max}}$ is the maximum likelihood for the nominal fit and $L_0$ is the corresponding value with the signal yield fixed to zero. The additive sources of systematic uncertainty (described below) are included in the significance by varying each by its error and taking the lowest significance. The signal in the charged mode has a significance of 9.6 $\sigma$, whereas that for the neutral mode is 5.4 $\sigma$.

![FIG. 2: Background-subtracted and efficiency-corrected $\phi K$ mass distributions for the charged (left) and neutral (right) modes. The points with error bars represent the data. The yield in each bin is obtained by the fitting procedure described in the text. A three-body phase-space model from MC simulation is shown by the filled circles (blue points) and normalized to the total data signal yield.](image)

To measure the $M_{\phi K}$ distribution, we repeat the fit in bins of $\phi K$ mass and the resulting signal yields are corrected for the detection efficiency. Nearly 72% of the signal events are concentrated in the low-mass region, $M_{\phi K} \in [1.5,2.0] \text{ GeV}/c^2$, as shown in Fig. 2. The MC efficiencies are reweighted according to this $M_{\phi K}$ dependence. These spectra are consistent with the expectations from the pQCD model for non-resonant $B \to \phi K\gamma$ decays [20]. With the present statistics no clear evidence is found for the existence of a kaonic resonance decaying to $\phi K$.

From the signal yield ($N_{\text{sig}}$), we calculate the branching fraction $[B]$ as $N_{\text{sig}}/(\epsilon \times N_{B\overline{B}} \times B_{\text{sec}})$, where $\epsilon$ is the weighted efficiency $(15.3 \pm 0.1(\text{stat}))\%$ for the charged mode and $(10.0 \pm 0.1(\text{stat}))\%$ for the neutral mode, $N_{B\overline{B}}$ is the number of $B\overline{B}$ pairs in the data sample, and $B_{\text{sec}}$ is the product of daughter branching fractions [18]. We obtain $B(B^+ \to \phi K^+\gamma) = (2.48 \pm 0.30 \pm 0.24) \times 10^{-6}$ and $B(B^0 \to \phi K^0\gamma) = (2.74 \pm 0.60 \pm 0.32) \times 10^{-6}$, where the uncertainties are statistical and systematic, respectively.

We evaluate the systematic uncertainties on the signal yield by fitting the data with each fixed parameter varied by its $\pm 1\sigma$ error, and then taking the quadratic sum of all differences from the nominal value. The largest contribution of 8.0% arises from the NR yield. Other sources of systematic error are from charged track efficiency ($\sim 1.1\%$ per track), photon detection efficiency (2.4%), particle identification (1.4%), number of produced $B\overline{B}$ pairs (1.4%), $\phi$ and $K^0_S$ branching fractions (1.2%), $K^0_S$ reconstruction (4.6%), and the requirement on $R_{s/b}$ (0.3%). The statistical uncertainty on the MC efficiency after reweighting is 1.0% (1.2%) in the charged (neutral) mode. Furthermore, we assign a systematic error of 0.2% (2.7%) for possible fit bias, which is obtained from ensemble tests with MC pseudo-experiments. The total systematic uncertainty on the branching fraction is 9.5% (11.7%).

For the $CP$ asymmetry fit, we select events in the signal region defined as $M_{bc} \in [5.27,5.29] \text{ GeV}/c^2$ and $\Delta E \in [-0.2,0.1] \text{ GeV}$. Different selection criteria on $R_{s/b}$ are used depending upon the flavor-tagging information. In addition, ECL endcap region photons are included in the analysis. We use a flavor tagging algorithm [21] to obtain the $b$-flavor charge $q$ and a tagging quality factor $r \in [0,1]$. The value $r = 0$ signifies no flavor discrimination while $r = 1$ implies unambiguous flavor assignment. The data are divided into seven $r$ intervals. The vertex position for the $f_{\text{rec}}$ decay is reconstructed using the two kaon tracks from the $\phi$ meson and that of the $f_{\text{tag}}$ decay is from well-reconstructed tracks that are not assigned to $f_{\text{rec}}$ [22]. The typical vertex reconstruction efficiency ($z$ resolution) is 96% (115 $\mu$m) for $f_{\text{rec}}$ and 94% (104 $\mu$m) for $f_{\text{tag}}$. After all selection criteria are applied, we obtain 75 (436) events in the signal region for the $CP$ fit with a purity of 45% (37%) in the neutral (charged) mode.

We determine $S$ and $A$ by performing an UML fit to the observed $\Delta t$ distribution by maximizing the likelihood function $L(S,A) = \prod_i P_i(S,A;\Delta t_i)$, where the product is over all events in the signal region. The like-
The likelihood $P_t$ for each event is given by
\[
P_t = (1 - f_{\od}) \int \left[ \sum_j f_j P_j(\Delta t') R_j(\Delta t - \Delta t') \right] d(\Delta t')
\]
where $j$ runs over signal and all background components. $P_j(\Delta t)$ is the corresponding PDF and $R_j(\Delta t)$ is the $\Delta t$ resolution function. The fraction of each component ($f_j$) depends on the $r$ region and is calculated for each event as a function of $\Delta E$ and $M_{bc}$. The signal PDF is given by a modified form of Eq. (1) by fixing $\tau_{B^0}$ and $M_{d4}$ to their world-average values [13] and incorporating the effect of incorrect flavor assignment. The distribution is then convolved with a resolution function to take into account the finite vertex resolution. Since the NR component is expected to have the same NP as the signal
\[
\text{fraction of each component } (f_{\od}) \text{ depends on the } r \text{ region and is calculated for each event as a function of } \Delta E \text{ and } M_{bc}. \text{ The signal PDF is given by a modified form of Eq. (1) by fixing } \tau_{B^0} \text{ and } M_{d4} \text{ to their world-average values [13] and incorporating the effect of incorrect flavor assignment. The distribution is then convolved with a resolution function to take into account the finite vertex resolution. Since the NR component is expected to have the same NP as the signal, we treat this as signal for the time-dependent fit [23]. For the other $B\bar{B}$ components, we use the same functional forms as signal with an effective lifetime taken from MC and $CP$ parameters fixed to zero. For the continuum background, we use the form described in Ref. [22]; the parameters are determined from a fit to the $\Delta t$ distribution of events in the data sample $M_{bc} < 5.26 \text{ GeV}/c^2$ and $\Delta E \in [0.1, 0.3] \text{ GeV}$. The term $P_{\od}(\Delta t)$ is a broad Gaussian function that represents an outlier component with a small fraction $f_{\od}$. The PDFs and resolution functions are described in detail elsewhere [22].

We perform various consistency checks of the $CP$ fitting technique. A lifetime fit to the $B^0 \to K^{*0}(\to K^+\pi^-)\gamma$, $B^+ \to \phi K^+\gamma$ and $B^0 \to \phi K_S^0\gamma$ data sample yields $1.56 \pm 0.03 \text{ ps}$, $1.70 \pm 0.20 \text{ ps}$ and $2.09 \pm 0.45 \text{ ps}$, respectively. These are all consistent with the world-average values of the $B$ lifetimes. The results of the $CP$ asymmetry fit to the $B^0 \to K^{*0}(\to K^+\pi^-)\gamma$ ($S = +0.02 \pm 0.06$, $A = -0.06 \pm 0.04$) and $B^+ \to \phi K^+\gamma$ ($S = +0.25 \pm 0.33$, $A = +0.18 \pm 0.26$) are consistent with zero. A fit to the sideband events in the $B^0 \to \phi K_S^0\gamma$ data sample gives an asymmetry consistent with zero ($S = -1.77 \pm 1.30$, $A = -0.04 \pm 0.14$).

The results of the fit are $S = +0.74^{+0.72}_{-1.05}(\text{stat})^{+0.10}_{-0.24}(\text{syst})$ and $A = +0.35 \pm 0.58(\text{stat})^{+0.24}_{-0.10}(\text{syst})$, where the uncertainties are obtained as described below. We define the raw asymmetry in each $\Delta t$ bin by $(N_+ - N_-)/(N_+ + N_-)$, where $N_+$ ($N_-$) is the number of events with $q = +1$ ($-1$). Figure 3 shows the $\Delta t$ distributions and raw asymmetry for events with good tagging quality ($r > 0.5, 48\% \text{ of the total}$).

We find that the error on $S$ in the MINUIT minimization [24] is much smaller than the expectation from MC simulations and has a probability of only $0.6\%$ [25]. This is due to low statistics and the presence of a single special event (with $\Delta t = -3.64 \text{ ps}$ and $r = 0.96$). A similar effect was found in our early time-dependent analyses of $B^0 \to \pi^+\pi^-$ [26]. Instead of the errors from MINUIT, we use the $\pm 68\%$ confidence intervals in the residual distributions of $S$ and $A$, determined from toy MC simulations as the statistical uncertainties on the result.

We evaluate the systematic uncertainties from the following sources. A significant contribution is from the vertex reconstruction $(0.08 \text{ on } S, 0.04 \text{ on } A)$. We refit the data with each fixed parameter varied by its error to evaluate the uncertainties due to signal and background fractions $(0.03, 0.07)$, resolution function $(0.02, 0.03)$, $\Delta E$-$M_{bc}$ shapes $(0.01, 0.01)$, continuum $\Delta t$ PDF $(0.01, 0.02)$, flavor tagging $(0.01, 0.01)$ and effects of tagside interference [27] $(0.004, 0.030)$. The uncertainty from physics parameters $(\tau_{B^0}, M_{d4})$, effective lifetime and $CP$ asymmetry of the $B\bar{B}$ background, is $(0.05, 0.03)$. We also include a possible fit bias due to low statistics and the proximity of the central value to the physical boundary $(+0.09, -0.21)$. MC simulations show that this bias decreases to $0.04$ with twice the signal yield. Adding all these contributions in quadrature, we obtain a systematic error of $+0.10$ on $S$ and $-0.16$ on $A$.

In summary, we report the first observation of a new radiative decay mode, $B^0 \to \phi K^-\gamma$ using a data sample of $772 \times 10^6 B\bar{B}$ pairs. The observed signal yield is $37 \pm 8$ with a significance of $5.4\sigma$ including systematic uncertainties, and the measured branching fraction is $B(B^0 \to \phi K^0\gamma) = (2.74 \pm 0.60 \pm 0.32) \times 10^{-6}$. We also measure $B(B^+ \to \phi K^+\gamma) = (2.48 \pm 0.30 \pm 0.24) \times 10^{-6}$ with a significance of $9.6\sigma$. Furthermore, we measure the charge asymmetry $A_{CP} = [N(B^-) - N(B^+)]/[N(B^-) + N(B^+)] = -0.03 \pm 0.11 \pm 0.08$, where $N(B^-)$ and $N(B^+)$ are the signal yields for $B^-$ and $B^+$ decays, respectively. The signal events are mostly concentrated at low $\phi K$ mass near threshold. The branching fractions and $\phi K$ mass spectra are in agreement with the theoretical prediction of Ref. [20]. We also report the first measurements of time-dependent $CP$ violation parameters in the neutral mode: $S = +0.74^{+0.72}_{-1.05}(\text{stat})^{+0.10}_{-0.24}(\text{syst})$ and $A = +0.35 \pm 0.58^{+0.23}_{-0.10}$. We have established that the mode $B^0 \to \phi K_S^0\gamma$ can be used at future high luminosity $e^+e^-$ [2, 3] and hadronic facilities [4] to perform time-
dependent CP violation measurements and to carry out sensitive tests for NP.

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[10] Throughout this Letter, the inclusion of the charge-conjugate decay mode is implied unless otherwise stated.


[19] \( f(\Delta E, M_{bc}) = [G_1(\Delta E - E_1) + G_2(\Delta E - E_2)] G(M_{bc} - M_0) \), where \( G_1, G_2 \) and \( G \) are Gaussian functions and \( E_1, E_2 \) and \( M_0 \) are constants.

[20] C. H. Chen et al. (BaBar Collaboration), Phys. Rev. D 70, 054006 (2004) and private communication with H.-n. Li. The pQCD model is in qualitative agreement with our data after including the kinematic effect of the kaon mass.


[23] Private communication with A. Soni.


[25] The MINOS errors are \( +0.32_{-0.45} \) on \( S \) and \( \pm0.45 \) on \( A \) for data, while the toy MC distributions with input values equal to those measured in data have a width of \( +0.72 \) for \( S \) and \( \pm0.58 \) for \( A \). The correlation between \( S \) and \( A \) is found to be 0.009 in data.
