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The Fate of R -Parity

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The possible origin of the R -parity violating interactions in the minimal supersymmetric standard model and its connection to the radiative symmetry breaking mechanism (RSBM) is investigated in the context of the simplest model where RSBM can be implemented. We find that in the majority of the parameter space R -parity is spontaneously broken at the low-scale. These results hint that R -parity violating processes could be observed at the Large Hadron Collider, if Supersymmetry is realized in nature.

I. INTRODUCTION

The minimal supersymmetric standard model (MSSM) is considered as one of the most appealing extensions of the standard model of strong and electroweak interactions. This theory has a variety of appealing characteristics including solutions to the hierarchy problem and a dark matter candidate. However, at the renormalizable level, the MSSM Lagrangian contains flagrant baryon and lepton number violating operators, the most infamous of which lead to rapid proton decay (See Ref. [1] for a review on supersymmetry (SUSY) and Ref. [2] for the study of the proton decay issue in SUSY.).

The most common approach to this problem is the introduction of a discrete symmetry, R -parity, defined as $R = (-1)^{3(B-L)+2S}$, where B , L and S are baryon and lepton number, and spin, respectively (See Ref. [3] for a review on R -parity violation.). The conservation of R -parity also ensures that the lightest SUSY particle (LSP) is stable and therefore a cold dark matter candidate. While R -parity is closely linked to $B - L$, they are not synonymous. Specifically, R -parity allows for terms that break $B - L$ by an even amount. For general arguments on R -parity conservation see Refs. [4] and [5].

Theories with local $B - L$ symmetries help shed light on R -Parity. R -parity is an exact symmetry as long as the same is true for $B - L$. Breaking $B - L$ by a field with even charge (the canonical $B - L$ model) guarantees automatic R -parity conservation even below the symmetry scale, since only $B - L$ violation by an even amount is allowed. An alternative is $B - L$ breaking through the right-handed sneutrino, a field which must always be included due to anomaly cancellation. Since the right-handed sneutrino has a charge of one, its VEV results in spontaneous R -parity violation.

Phenomenologically, this is a viable scenario that does not induce tree-level rapid proton decay and dark matter is still possible if the gravitino is the LSP.

Recently, spontaneous R -parity violation has been studied in the case of minimal $B - L$ models [6–10]. However, the following question is still relevant: *Does the canonical $B - L$ model favor R -parity conservation or violation?* In this letter we study this question in the simplest local $U(1)_{B-L}$ extension of the MSSM assuming, for simplicity, MSUGRA boundary conditions for the soft terms. We investigate the fate of R -parity using the radiative symmetry breaking mechanism and show that for the majority of the parameter space, R -parity is broken, namely it is the right-handed sneutrino that acquires a negative mass squared and therefore a vacuum expectation value (VEV). This is a surprising result that at the very least questions the feasibility of conserving R -parity in such a framework. These results are quite general and apply to any SUSY theory where $B - L$ is part of the gauge symmetry.

II. THEORETICAL FRAMEWORK

We investigate the possible connection between RSBM and the fate of R -parity in the simplest $B - L$ model, based on the gauge group:

$$SU(3) \otimes SU(2)_L \otimes U(1)_Y \otimes U(1)_{B-L}$$

with particle content listed in Table I.

Field	$SU(2)_L$	$U(1)_Y$	$U(1)_{B-L}$
$\hat{Q} = (\hat{u}, \hat{d})$	2	1/6	1/3
\hat{u}^c	1	-2/3	-1/3
\hat{d}^c	1	1/3	-1/3
$\hat{L} = (\hat{\nu}, \hat{e})$	2	-1/2	-1
\hat{e}^c	1	1	1
$\hat{\nu}^c$	1	0	1
$\hat{H}_u = (\hat{H}_u^+, \hat{H}_u^0)$	2	1/2	0
$\hat{H}_d = (\hat{H}_d^0, \hat{H}_d^-)$	2	-1/2	0
\hat{X}	1	0	-2
$\hat{\bar{X}}$	1	0	2

TABLE I: $SU(2)_L \otimes U(1)_Y \otimes U(1)_{B-L}$ charges for the particle content.

The most general superpotential is given by

$$\mathcal{W} = \mathcal{W}_{MSSM} + \mathcal{W}_{B-L}, \quad (1)$$

$$\mathcal{W}_{MSSM} = Y_u \hat{Q} \hat{H}_u \hat{u}^c + Y_d \hat{Q} \hat{H}_d \hat{d}^c + Y_e \hat{L} \hat{H}_d \hat{e}^c + \mu \hat{H}_u \hat{H}_d, \quad (2)$$

$$\mathcal{W}_{B-L} = Y_\nu \hat{L} \hat{H}_u \hat{\nu}^c + f \hat{\nu}^c \hat{\nu}^c \hat{X} - \mu_X \hat{X} \hat{\bar{X}}, \quad (3)$$

and the corresponding soft SUSY breaking Lagrangian is

$$\begin{aligned} -\mathcal{L}_{\text{Soft}} \supset & \left(a_\nu \tilde{L} H_u \tilde{\nu}^c - a_X \tilde{\nu}^c \tilde{\nu}^c X - b_X X \bar{X} + \frac{1}{2} M_{BL} \tilde{B}' \tilde{B}' + h.c. \right) \\ & + m_X^2 |X|^2 + m_{\bar{X}}^2 |\bar{X}|^2 + m_{\tilde{\nu}^c}^2 |\tilde{\nu}^c|^2, \end{aligned} \quad (4)$$

where we have suppressed flavor and group indices and \tilde{B}' is the $B - L$ gaugino.

Spontaneous $B - L$ violation requires either the VEV of X , \bar{X} or $\tilde{\nu}^c$ to be nonzero, however the fate of R -parity lies solely in the VEV of $\tilde{\nu}^c$: $\langle \tilde{\nu}^c \rangle = 0$ corresponds to R -parity conservation while $\langle \tilde{\nu}^c \rangle \neq 0$ indicates spontaneous R -parity violation. Addressing the values of these VEVs requires the minimization conditions which can be derived from the full potential where $(\langle X \rangle, \langle \bar{X} \rangle, \langle \tilde{\nu}^c \rangle) = 1/\sqrt{2}(x, \bar{x}, n)$ ¹:

$$\langle V \rangle = \langle V_F \rangle + \langle V_D \rangle + \langle V_{\text{Soft}} \rangle, \quad (5)$$

$$\langle V_F \rangle = \frac{1}{4} f^2 n^4 + f^2 n^2 x^2 + \frac{1}{2} \mu_X^2 (x^2 + \bar{x}^2) - \frac{1}{\sqrt{2}} f \mu_X n^2 \bar{x}, \quad (6)$$

$$\langle V_D \rangle = \frac{1}{32} g_{BL}^2 (2 \bar{x}^2 - 2 x^2 + n^2)^2, \quad (7)$$

$$\langle V_{\text{Soft}} \rangle = -\frac{1}{\sqrt{2}} a_X n^2 x - b_X x \bar{x} + \frac{1}{2} m_X^2 x^2 + \frac{1}{2} m_{\bar{X}}^2 \bar{x}^2 + \frac{1}{2} m_{\tilde{\nu}^c}^2 n^2. \quad (8)$$

Only two cases exist for spontaneous $B - L$ symmetry breaking: Case *i*) $n = 0$; $x, \bar{x} \neq 0$ implying R -parity conservation or Case *ii*) $x, \bar{x}, n \neq 0$ implying spontaneous R -parity violation. Note that a third case, $n \neq 0$; $x, \bar{x} = 0$ cannot exist due to the linear term for x in Eq. (8) and for \bar{x} in Eq. (6), which always induce a VEV for these fields.

- Case *i*): **R -Parity Conservation**

This is the traditional case studied in the literature. The minimization conditions for x and \bar{x} are very similar in form to those of v_u and v_d in the MSSM:

$$\frac{1}{2} M_{Z'}^2 = -|\mu_X|^2 + \frac{m_X^2 \tan^2 z - m_{\bar{X}}^2}{1 - \tan^2 z}, \quad (9)$$

¹ Technically, the left-handed sneutrino has a VEV as well, but in order to generate the correct neutrino masses, this VEV must be quite small compared to the others and so can safely be ignored here [7].

where $\tan z \equiv x/\bar{x}$ and $M_{Z'}^2 \equiv g_{BL}^2 (x^2 + \bar{x}^2)$, which is the mass for the Z' boson associated with broken $B - L$.

To attain a better understanding of the situation, let us examine Eq. (9) in the limit $x \gg \bar{x}$, with $m_X^2 < 0$ and $m_{\bar{X}}^2 > 0$, so that it reduces to

$$\frac{1}{2}M_{Z'}^2 = -|\mu_X|^2 - m_X^2. \quad (10)$$

Since the left-hand side is positive definite, *the relationship $-m_X^2 > |\mu_X|^2$ must be obeyed for spontaneous $B - L$ violation*: a tachyonic m_X^2 is not enough. This relationship between μ_X and m_X is similar to the relationship in the MSSM between μ and m_{H_u} a relationship typically referred to as the μ problem, *i.e.* why is μ of the order of the SUSY mass scale. Then in case *i*, in addition to the MSSM μ problem, we have introduced a new μ problem for μ_X .

As can be seen from Eq. (10), x is of order the SUSY mass scale or about a TeV. Replacing X by its VEV in the term $f\nu^c\nu^c X$ in the superpotential leads to the heavy Majorana mass term for the right-handed neutrinos and ultimately to the Type I seesaw mechanism [11] for neutrino masses:

$$m_\nu = v_u^2 Y_\nu^T (fx)^{-1} Y_\nu. \quad (11)$$

Since the mass of the right-handed neutrinos are of order TeV, realistic neutrino masses require, $Y_\nu \sim 10^{-6-7}$. The rest of the spectrum is given in Appendix B.

• Case ii): R -Parity Violation

Evaluation of the minimization conditions in this case is illuminating in the limit $n \gg x, \bar{x}, a_X$ and $g_{BL}^2 \ll 1$, which will prove to be the case of interest in the numerical section:

$$n^2 = \frac{(-m_{\bar{\nu}^c}^2) \Lambda_{\bar{X}}^2}{f^2 m_{\bar{X}}^2 + \frac{1}{8} g_{BL}^2 \Lambda_{\bar{X}}^2}, \quad (12)$$

$$\bar{x} = \frac{(-m_{\bar{\nu}^c}^2) f \mu_X}{\sqrt{2} \left(f^2 m_{\bar{X}}^2 + \frac{1}{8} g_{BL}^2 \Lambda_{\bar{X}}^2 \right)}, \quad (13)$$

$$x = \frac{(-m_{\bar{\nu}^c}^2) [a_X \Lambda_{\bar{X}}^2 + f b_X \mu_X]}{\left(2 f^2 - \frac{1}{4} g_{BL}^2 \right) (-m_{\bar{\nu}^c}^2) \Lambda_{\bar{X}}^2 + f^2 m_{\bar{X}}^2 \Lambda_X^2 + \frac{1}{8} g_{BL}^2 \Lambda_{\bar{X}}^2 \Lambda_X^2}, \quad (14)$$

where $\Lambda_X^2 \equiv \mu_X^2 + m_X^2$ and $\Lambda_{\bar{X}}^2 \equiv \mu_{\bar{X}}^2 + m_{\bar{X}}^2$.

These equations indicate several things: *spontaneous $B - L$ symmetry breaking in the R -parity violating case only requires $m_{\bar{\nu}^c}^2 < 0$ and does not introduce a new μ problem so that*

μ_X can be larger than the TeV scale; that x and \bar{x} are triggered by linear terms since they go as these linear terms suppressed by the effective mass squared; and all VEVs increase with μ_X up to a point after which n asymptotes while x and \bar{x} decrease as $1/\mu_x$. The $\mu_X \rightarrow \infty$ serves as a decoupling limit since $x, \bar{x} \rightarrow 0$ and $n^2 \rightarrow -8m_{\tilde{\nu}^c}/g_{BL}^2$ as in the minimal model [7]. Neutrino masses in this case will have a more complicated form that will depend both on the type I seesaw contribution and an R -parity contribution although the bounds on Y_ν are similar to Case *i*). The Z' mass in this case is

$$M_{Z'}^2 = \frac{1}{4}g_{BL}^2 (n^2 + 4x^2 + 4\bar{x}^2). \quad (15)$$

and the rest of the spectrum is given in Appendix B.

The important question now becomes: are either of these cases possible from the perspective of RSBM? Specifically, will running from some SUSY breaking boundary conditions drive either X or $\tilde{\nu}^c$ tachyonic, or neither? To answer this, we adopt the MSUGRA Ansatz motivated by the fact that gravity is one of the simplest ways to transmit SUSY breaking [12]. The following boundary conditions are valid at the GUT scale:

$$m_X^2 = m_{\bar{X}}^2 = m_{\tilde{\nu}_i^c}^2 = \dots = m_0^2 \quad (16)$$

$$A_X = f A_0; A_\nu = Y_\nu A_0; \dots \quad (17)$$

$$M_{BL} = \dots = M_{1/2}, \quad (18)$$

where \dots indicates MSSM parameters.

The necessary renormalization group equations (RGEs), derived using [13], will only be functions of the beyond the MSSM couplings since Y_ν is small enough to be neglected. We assume that g_{BL} unifies with the other gauge couplings at the GUT scale and use the SO(10) GUT renormalization factor, $\sqrt{3/8}$. In the approximation $f_3 = f \gg f_1, f_2$, the RGEs are given by²

$$16\pi^2 \frac{dm_{\tilde{\nu}^c}^2}{dt} = [8f^2 X_X - 3g_{BL}^2 M_{BL}^2], \quad (19)$$

$$16\pi^2 \frac{dm_X^2}{dt} = [4f^2 X_X - 12g_{BL}^2 M_{BL}^2], \quad (20)$$

$$16\pi^2 \frac{dm_{\bar{X}}^2}{dt} = -12g_{BL}^2 M_{BL}^2, \quad (21)$$

where $t = \ln \mu$, and $X_X \equiv m_X^2 + 2m_{\tilde{\nu}^c}^2 + 4a_X^2$. See Appendix A for the full set of RGEs including the contributions from three families of right-handed neutrinos.

² We would like to note that our results are in disagreement with the results in Ref. [14].

Experience from radiative electroweak symmetry breaking in the MSSM [15], indicates that Yukawa terms in the beta functions tend to drive the masses squared negative while gaugino terms do the opposite. Due to its smaller $B-L$ charge, $\tilde{\nu}^c$ has the smallest gaugino factor while also having the largest Yukawa factor. Since in MSUGRA, all of these fields have the same mass at the GUT scale, it is clear that $m_{\tilde{\nu}^c}^2$ will evolve to the smallest value in the simple one family approximation. When including all three families, m_X^2 gets an enhancement from trace of f , Eq. (A10), which could lead to it being tachyonic and therefore to R -parity conservation. The question of whether RSBM is possible as well as the fate of R -parity throughout the parameter space will be addressed numerically in the next section. It is important to mention that one gets only bilinear interactions which violate R -parity after symmetry breaking. For details see Ref. [6–10].

III. R-PARITY: CONSERVATION OR VIOLATION ?

In addition to addressing the feasibility of RSBM in general and the fate of R -parity specifically, it would also be prudent to identify the part of parameter space that leads to a realistic spectrum. One strong experimental constrain is the bound on the Z' mass: $M_{Z'}/g_{BL} > 5$ TeV [16], indicating the need for a large mass scale, independent of the fate of R -parity, and translates into a large value for m_0 at the GUT scale.

The hyperbolic branch/focus point region of MSUGRA [17] allows for such large m_0 without too much fine-tuning in the MSSM Higgs sector and naturally leads to a slight hierarchy between the electroweak scale and the $B-L$ scale. Also, the approximations made in the previous section for case *ii* are valid. Values for $\tan\beta$ and f are inputted at the SUSY scale and we assume g_{BL} unifies with the other gauge couplings at the GUT scale. We find that A_0 has very little effect and therefore set it to zero. The EWSB minimization conditions are solved for μ and B and we assumed that $B_X = B$ at the GUT scale, where $b_X = B_X\mu_X$. Specifying μ_X then determines the spectrum.

Calculating the soft masses of X and $\tilde{\nu}^c$ with increasing f_3 yields Fig. 1, for $m_0 = 2000$ GeV, $M_{1/2} = 200$ GeV, $A_0 = 0$ and negligible f_1 and f_2 . As expected, in the $f_1, f_2 \ll f_3$ limit, only the $\tilde{\nu}^c$ mass becomes tachyonic, so while RSBM can be successful, it leads to spontaneous R -parity breaking. Note that f_3 exhibits fixed-point like behavior (as discussed in a similar scenario in [18]). This means that its range allowing for RSBM, corresponds to a larger range of values at the GUT scale. In Fig. 2, are the X and $\tilde{\nu}^c$ soft masses for different values f_3 versus m_0 with all other parameters the same as in Fig. 1. It indicates that the m_0 parameter also plays an important role

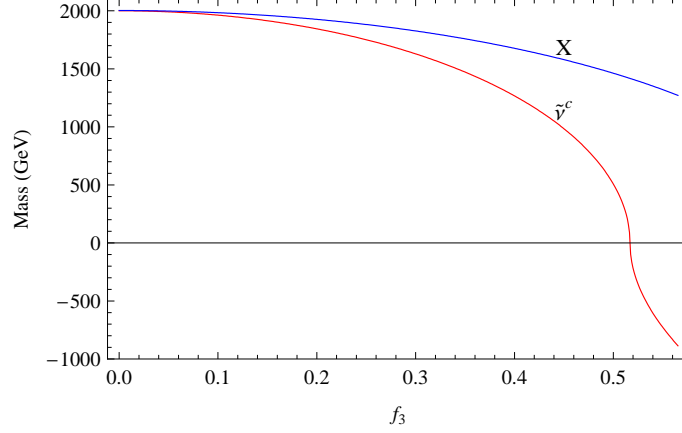


FIG. 1: Soft masses in the form $\text{sign}(m_\phi^2)|m_\phi|$ for X (blue) and $\tilde{\nu}^c$ (red) versus f_3 , for $m_0 = 2000$ GeV, $M_{1/2} = 200$ GeV, $A_0 = 0$ and negligible f_1 and f_2 . RSBM is possible for $f_3 \gtrsim 0.51$ and spontaneous R -parity violation.

in determining the overall size of the tachyonic mass, and therefore the Z' mass, and can even derail RSBM for lower values of f_3 .

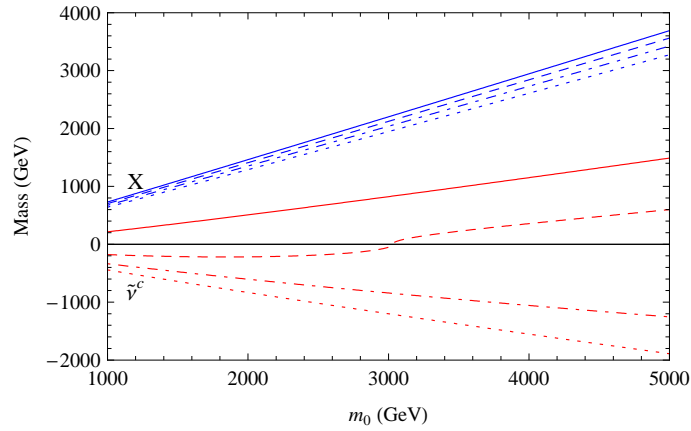


FIG. 2: Soft masses in the form $\text{sign}(m_\phi^2)|m_\phi|$ for X (blue) and $\tilde{\nu}^c$ (red) versus m_0 for $f_3 = 0.5$ (solid), 0.52 (dashed), 0.54 (dot-dashed), 0.56 (dotted) and all other parameters the same as in Fig. 1.

For $f_1 \sim f_2 \sim f_3$, the Yukawa term in the RGE for m_X^2 is effectively enhanced by a factor of three, see Eq. (A10) as compared to Eq. (20), which can lead to an R -parity conserving minima since no such factor appears for $m_{\tilde{\nu}^c}^2$. We show these effects in Fig. 3, where red dots indicate spontaneous R -parity violation and blue dots show the region of R -parity conservation in the f_2 - f_1 plane for $f_3 = 0.4$ (a) and $f_3 = 0.55$ (b) and $m_0 = 2000$ GeV, $M_{1/2} = 200$ GeV and $A_0 = 0$. In Fig. 3(a) f_1 or $f_2 \sim 0.52$ is needed for RSBM while only $f_1 \sim f_2 \gtrsim 0.4$ allows for

R -parity conservation (there is about a 50-50 split between R -parity conservation and violation). If f_1 or $f_2 > 0.52$, these couplings are no longer perturbative at the GUT scale. As one increases the value of f_3 , the R -parity conserving points disappear as reflected in Fig. 3(b). In this case, f_1 or $f_2 \gtrsim 0.4$ leads to non-perturbative values at the GUT scale due to the larger value of f_3 .

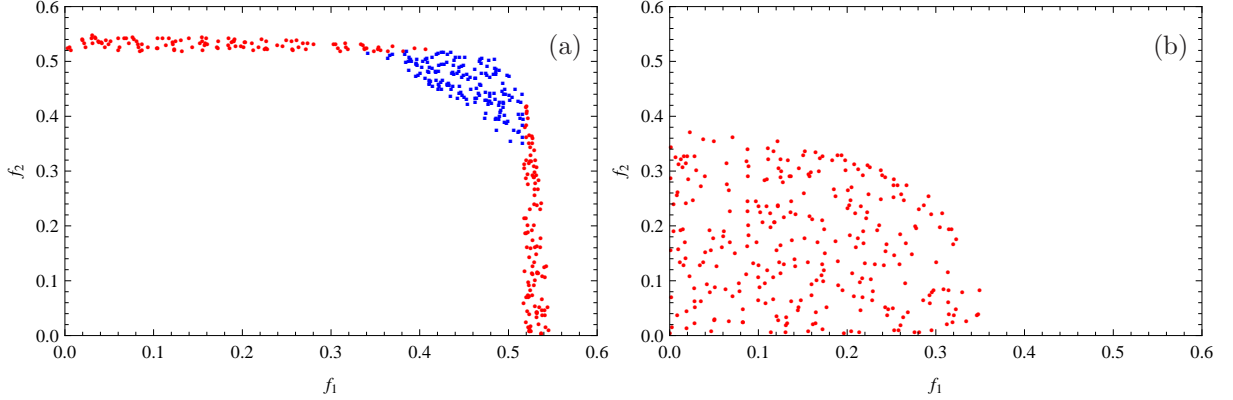


FIG. 3: The state of the $B - L$ breaking vacuum in the f_2 - f_1 plane with $m_0 = 2000$ GeV, $M_{1/2} = 200$ GeV and $A_0 = 0$ for $f_3 = 0.4$ (a) and $f_3 = 0.55$ (b). Blue dots indicate R -parity conservation while red dots R -parity violation. In (a), the empty space below the curve indicates no RSBM, while in both graphs, in the space above the curves, the f 's are no longer perturbative at the GUT scale. In (a), there is about an even number of R -parity conserving and violating vacua but increasing f_3 tips the favor towards R -parity violation and eventually only allows for R -parity violation as in (b).

The graphs in Fig. 3 are a bit misleading since they are just slices of the three dimensional space $f_1 - f_2 - f_3$, which is displayed in Figs. 4 and 5, with the same legend as the former figure. The points sit on a shell that roughly composes one eighth of a cube with sides of about length one. Below the shell, RSBM is not possible due to the small values of f , while those outside are not perturbative up to the GUT scale. The majority of the parameter space which allows for RSBM is dominated by R -parity violation (five times more prevalent) while only $f_1 \sim f_2 \sim f_3$ allows for R -parity conservation. This last figures summarize the findings of this letter: when RSBM is realized the R -parity breaking vacuum is more probable than the R -parity conserving one, especially when a hierarchy exists within the f matrix. Only when this matrix is fairly degenerate (degenerate right-handed neutrinos) does the running allow for R -parity conservation.

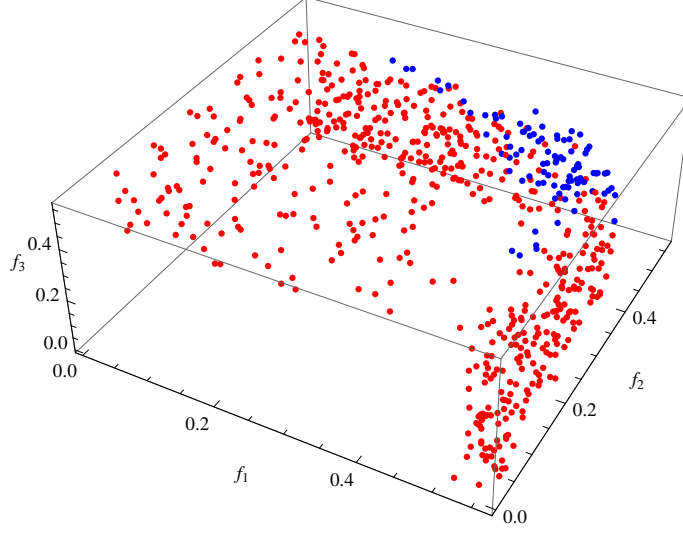


FIG. 4: The state of the $B-L$ breaking vacuum in the $f_1 - f_2 - f_3$ space with $m_0 = 2000$ GeV, $M_{1/2} = 200$ GeV and $A_0 = 0$. Blue dots indicate R -parity conservation while red dots R -parity violation, the latter appears five times more often. The key point is that only fairly degenerate values of f (and therefore the right-handed neutrinos) allow for R -parity conservation. We have checked that all physical masses are positive in these cases.

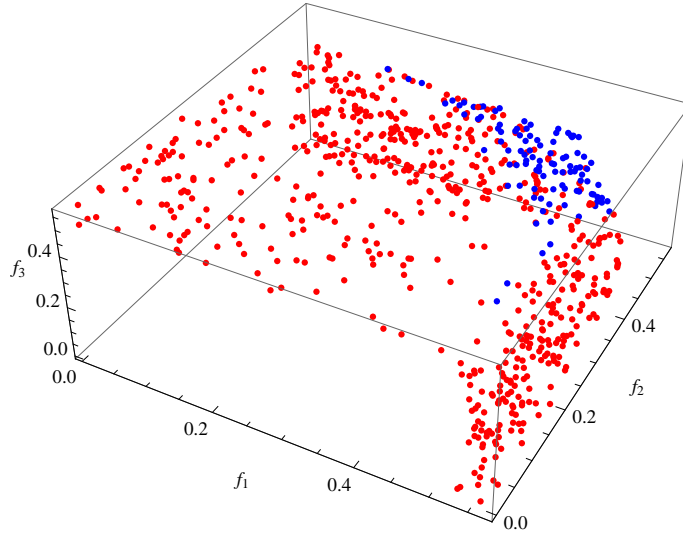


FIG. 5: The state of the $B-L$ breaking vacuum in the $f_1 - f_2 - f_3$ space with $m_0 = 5000$ GeV, $M_{1/2} = 500$ GeV and $A_0 = 0$. The legend and results are is in Fig 4.

IV. SUMMARY

The possible origin of the R -parity violating interactions in the MSSM and its connection to the radiative symmetry breaking mechanism has been investigated in the simplest possible model. We have found that in the majority of the parameter space R -parity is spontaneously broken at the low-scale and the soft SUSY mass scale defines the $B - L$ and R -parity breaking scales. These results can be achieved in any extension of the MSSM where $B - L$ is part of the gauge symmetry, and only bilinear R -parity violating interactions are generated. The main result of this letter hints at the possibility that R -parity violating processes will be observed at the Large Hadron Collider, if Supersymmetry is discovered.

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Appendix A: Renormalization Group Equations

We present first the gamma functions, which are useful for deriving the RGEs. Here $i = 1, 2, 3$.

$$\gamma_X = \frac{1}{16\pi^2} (2 \text{Tr } f^2 - 3 g_{BL}^2), \quad (\text{A1})$$

$$\gamma_{\bar{X}} = \frac{1}{16\pi^2} (-3 g_{BL}^2), \quad (\text{A2})$$

$$\gamma_{\nu_i^c} = \frac{1}{16\pi^2} \left(4 f_i^2 - \frac{3}{4} g_{BL}^2 \right), \quad (\text{A3})$$

where repeated indices are not summed and $f = \text{diag}(f_1, f_2, f_3)$, since f can always be diagonalized by rotating the right-handed neutrino fields. The same holds true here for a_X due to the MSUGRA Ansatz.

The RGEs are given by

$$16\pi^2 \frac{dg_{BL}}{dt} = 9 g_{BL}^3, \quad (\text{A4})$$

$$16\pi^2 \frac{df_i}{dt} = f_3 \left(8 f_i^2 + 2 \text{Tr } f^2 - \frac{9}{2} g_{BL}^2 \right), \quad (\text{A5})$$

$$16\pi^2 \frac{dM_{BL}}{dt} = 18 g_{BL}^2 M_{BL}, \quad (\text{A6})$$

$$16\pi^2 \frac{da_{X_i}}{dt} = f_X (16 f_i a_{X_i} + 4 \text{Tr}(f a_X) - 9 g_{BL}^2 M_{BL}) \quad (\text{A7})$$

$$+ a_{X_i} \left(8 f_i^2 + 2 \text{Tr } f^2 - \frac{9}{2} g_{BL}^2 \right), \quad (\text{A8})$$

$$16\pi^2 \frac{dm_{\bar{X}}^2}{dt} = -12 g_{BL}^2 M_{BL}^2, \quad (\text{A9})$$

$$16\pi^2 \frac{dm_X^2}{dt} = [4 \text{Tr } f^2 m_X^2 + 8 \text{Tr}(f^2 m_{\nu^c}^2) + 4 \text{Tr } a_X^2 - 12 g_{BL}^2 M_{BL}^2], \quad (\text{A10})$$

$$16\pi^2 \frac{dm_{\nu_i^c}^2}{dt} = [8 f_i^2 (m_X^2 + 2 m_{\nu_i^c}^2) + 8 a_{X_i}^2 - 3 g_{BL}^2 M_{BL}^2]. \quad (\text{A11})$$

Appendix B: Spectrum

In calculating the following spectrum we assume $\langle \tilde{\nu}_3^c, X, \bar{X} \rangle = \frac{1}{\sqrt{2}}(n, x, \bar{x})$ and all others zero. Pseudoscalar mass matrix in the basis $\text{Im}(\tilde{\nu}_3^c, X, \bar{X})$:

$$\mathcal{M}_P = \begin{pmatrix} 2\sqrt{2}(a_X x + f_3 \mu_X \bar{x}) & \sqrt{2} a_X n & -\sqrt{2} f_3 \mu_X n \\ \sqrt{2} a_X n & \frac{a_X n^2 + \sqrt{2} b_X \bar{x}}{\sqrt{2} x} & b_X \\ -\sqrt{2} f_3 n \mu_X & b_X & \frac{f_3 \mu_X n^2 + \sqrt{2} b_X x}{\sqrt{2} \bar{x}} \end{pmatrix}. \quad (\text{B1})$$

Scalar mass matrix in the basis $\text{Re}(\tilde{\nu}_3^c, X, \bar{X})$:

$$\mathcal{M}_S = \begin{pmatrix} (2f_3^2 + \frac{1}{4}g_{BL}^2)n^2 & (4f_3^2 - \frac{1}{2}g_{BL}^2)n x - \sqrt{2}a_X n & -\sqrt{2}f_3\mu_x n + \frac{1}{2}g_{BL}^2 n \bar{x} \\ (4f_3^2 - \frac{1}{2}g_{BL}^2)n x - \sqrt{2}a_X n & \frac{a_3 n^2 + \sqrt{2}b_X \bar{x}}{\sqrt{2}x} + g_{BL}^2 x^2 & -b_X - g_{BL}^2 x \bar{x} \\ -\sqrt{2}f_3\mu_x n + \frac{1}{2}g_{BL}^2 n \bar{x} & -b_X - g_{BL}^2 x \bar{x} & \frac{f_3\mu_X n^2 + \sqrt{2}b_X x}{\sqrt{2}\bar{x}} + g_{BL}^2 \bar{x}^2 \end{pmatrix}. \quad (\text{B2})$$

Neutralino mass matrix in the basis $(B', \nu^c, \tilde{X}, \tilde{\bar{X}})$:

$$\mathcal{M}_{\chi^0} = \begin{pmatrix} M_{BL} & \frac{1}{2}g_{BL}n & -g_{BL}x & g_{BL}\bar{x} \\ \frac{1}{2}g_{BL}n & \sqrt{2}f_3x & \sqrt{2}f_3n & 0 \\ -g_{BL}x & \sqrt{2}f_3n & 0 & -\mu_X \\ g_{BL}\bar{x} & 0 & -\mu_X & 0 \end{pmatrix} \quad (\text{B3})$$

The sfermion mass, with matrices in the basis $(\tilde{f}_L, \tilde{f}_R)$

$$\mathcal{M}_u^2 = \begin{pmatrix} m_{\tilde{Q}}^2 + m_u^2 - \frac{1}{8}(g_2^2 - \frac{1}{3}g_1^2)(v_u^2 - v_d^2) + \frac{1}{3}D_{BL} & \frac{1}{\sqrt{2}}(a_u v_u - Y_u \mu v_d) \\ \frac{1}{\sqrt{2}}(a_u v_u - Y_u \mu v_d) & m_{\tilde{u}^c}^2 + m_u^2 - \frac{1}{6}g_1^2(v_u^2 - v_d^2) - \frac{1}{3}D_{BL} \end{pmatrix}, \quad (\text{B4})$$

$$\mathcal{M}_d^2 = \begin{pmatrix} m_{\tilde{Q}}^2 + m_d^2 + \frac{1}{8}(g_2^2 + \frac{1}{3}g_1^2)(v_u^2 - v_d^2) + \frac{1}{3}D_{BL} & \frac{1}{\sqrt{2}}(Y_d \mu v_u - a_d v_d) \\ \frac{1}{\sqrt{2}}(Y_d \mu v_u - a_d v_d) & m_{\tilde{d}^c}^2 + m_d^2 + \frac{1}{12}g_1^2(v_u^2 - v_d^2) - \frac{1}{3}D_{BL} \end{pmatrix}, \quad (\text{B5})$$

$$\mathcal{M}_e^2 = \begin{pmatrix} m_{\tilde{L}}^2 + m_e^2 + \frac{1}{8}(g_2^2 - g_1^2)(v_u^2 - v_d^2) - D_{BL} & \frac{1}{\sqrt{2}}(Y_e \mu v_u - a_e v_d) \\ \frac{1}{\sqrt{2}}(Y_e \mu v_u - a_e v_d) & m_{\tilde{e}^c}^2 + m_e^2 + \frac{1}{4}g_1^2(v_u^2 - v_d^2) + D_{BL} \end{pmatrix}, \quad (\text{B6})$$

$$m_{\tilde{\nu}_L}^2 = m_{\tilde{L}}^2 - \frac{1}{8}(g_2^2 + g_1^2)(v_u^2 - v_d^2) - D_{BL}, \quad (\text{B7})$$

$$m_{\tilde{N}_{I_i}}^2 = m_{\tilde{\nu}_i^c}^2 + 2f_i^2 x^2 - f_i f_3 n^2 + \sqrt{2}a_{X_i}x + \sqrt{2}f_i \mu_X \bar{x} + D_{BL}, \quad (\text{B8})$$

$$m_{\tilde{N}_{R_i}}^2 = m_{\tilde{\nu}_i^c}^2 + 2f_i^2 x^2 + f_i f_3 n^2 - \sqrt{2}a_{X_i}x - \sqrt{2}f_i \mu_X \bar{x} + D_{BL}. \quad (\text{B9})$$

where $D_{BL} \equiv \frac{1}{8}g_{BL}^2(2\bar{x}^2 - 2x^2 + n^2)$, and m_u , m_d and m_e are the respective fermion masses and a_u , a_d and a_e are the trilinear a -terms corresponding to the Yukawa couplings Y_u , Y_d and Y_e . The right-handed sneutrino eigenstates are the scalars \tilde{N}_{R_i} and pseudoscalars \tilde{N}_{I_i} where i runs only over the first two generations and repeated indices are not summed. The third generation mixes with the Higgses, Eqs. (B1, B2). The above masses are for R -parity violation, case ii from

the text. For the R -parity conserving case, case i , take the limit $n \rightarrow 0$ and the $B - L$ Higgs masses are given by the lower two-by-two block matrices of Eqs. (B1, B2) and i in Eqs. (B8, B9) runs over all three generations.

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