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# Neutron capture-induced nuclear recoils as background for CEvNS measurements at reactors

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Nuclear reactors represent a promising neutrino source for CEvNS (coherent-elastic neutrinonucleus scattering) searches. However, reactor sites also come with high ambient neutron flux. Neutron capture-induced nuclear recoils can create a spectrum that strongly overlaps the CEvNS signal for recoils  $\leq 100 \text{ eV}$  for nuclear reactor measurements in silicon or germanium detectors. This background can be particularly critical for low-power research reactors providing a moderate neutrino flux. In this work we quantify the impact of this background and show that, for a measurement 10 m from a 1 MW reactor, the effective thermal neutron flux should be kept below  $\sim 7 \times 10^{-4} \text{ n/cm}^2 \text{s}$  so that the CEvNS events can be measured at least at a  $5\sigma$  level with germanium detectors in 100 kg yr exposure time. This flux corresponds to 60% of the sea-level flux but needs to be achieved in a nominally high-flux (reactor) environment. Improved detector resolution can help the measurements, but the thermal flux is the key parameter for the sensitivity of the experiment. For silicon detectors, the constraint is even stronger and thermal neutron fluxes must be near an order of magnitude lower. This constraint highlights the need of an effective thermal neutron mitigation strategy for future low threshold CEvNS searches. In particular, the neutron capture-induced background can be efficiently reduced by active veto systems tagging the deexcitation gamma following the capture.

# I. INTRODUCTION

Coherent Elastic Neutrino Nucleus Scattering (CE $\nu$ NS) is the transfer of momentum between a neutrino and a nucleus as a whole via neutral current exchange. This process is experimentally significant for detecting low energy ( $\lesssim$  MeV) neutrinos due to its large cross-section, two to four orders of magnitude larger than the commonly used inverse beta decay (IBD) [1, 2]. This allows CE $\nu$ NS detectors to be much smaller than their IBD counterparts.

The CEvNS process has already been measured at an accelerator site by the COHERENT collaboration using the Spallation Neutron Source at Oak Ridge National Laboratory as a neutrino source [3]. The accelerator provides neutrinos of a few tens of MeV, and other measurements using this type of source are planned, for example the upcoming European Spallation Source [2]. Likewise, recent studies show potential for measurements at reactor sites, where the sources of MeV antineutrinos are commercial or research fission reactors [4–11].

The trade-off for CEvNS' relatively high interaction rate is that it is exceptionally difficult to detect because of the tiny (sub-keV) recoil of the target nuclei, even despite recent advances in detector resolution near threshold, for example in silicon [12, 13]. One major hurdle is that distinguishing a nuclear recoil event caused by CEvNS from one caused by other sources is difficult. In the vicinity of nuclear reactors, a large reactogenic thermal neutron flux could cause enough neutron-capture-induced recoil events to hide the CEvNS signal. A capture of a neutron via the  $(n,\gamma)$  process produces one or more ~MeV scale prompt gamma rays and a prompt nuclear recoil at the sub-keV scale–coinciding with the energy scale of events from reactor neutrinos.

The recoil spectrum from neutron capture on silicon has been recently measured [14] and creates nuclear recoil events down to  $\sim 100 \text{ eV}$ . This paper investigates the thermal neutron background mitigations needed to measure a CEvNS signal in the vicinity of a nuclear reactor.

### II. CEvNS AND CAPTURE SPECTRA

We used the model given by Mueller [15] for the four principle fissionable isotopes as the model for reactor antineutrino emissions. We attempted to emulate the expected emissions of a low-enriched (~ 20% <sup>235</sup>U) reactor fuel composition, i.e. that employed by the MINER Collaboration at the Nuclear Science Center at Texas A&M University [16]. We assume neutrino emissions consistent with the MINER study [11], i.e., dominated by <sup>235</sup>U (96.7%) with smaller fractions of <sup>238</sup>U and <sup>239</sup>Pu (1.3 and 2.0% respectively), and negligible ( $\leq 0.1\%$ ) <sup>241</sup>Pu.

We tested the target materials silicon and germanium with natural isotope distributions. The reactor spectrum was convoluted with the known CEvNS cross section [2] using the form factor model given by [17] to yield a recoil energy spectrum for CEvNS events. The form factor was quite close to 1, with a largest deviation from Ge at a recoil energy of around 1 keV, where it had a value of 0.9895.

To calculate the expected recoil energy spectrum from neutron captures, we use nrCascadeSim, a publiclyavailable dedicated simulation tool developed by two of the authors here for nuclear recoils resulting from neutron captures [18]. This software was used to generate

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a large sample of capture-induced recoil energies from which we construct a probability density function (PDF) to sample. The code takes into account the most probable multistep cascades in the deexcitation process following capture and the possibility of decay-in-flight for the intermediate atoms/ions within the cascade.

#### ASSUMED DETECTOR CONFIGURATION III.

Recoil datasets were simulated with a total of 3,000 (10,000) CEvNS events, corresponding to approximately a 100 kg yr exposure time of natural silicon (germanium) detectors, at the CEvNS event rate calculated by [11] for detector deployment 10 m from the reactor core. Events that produce energies below the detection threshold are removed when applying the resolution model. Detectors were modeled with a range of different effective resolutions (defined here as resolution  $\sigma$  at a recoil energy of 50 eV). All detector resolutions obeyed a resolution function of the form:

$$\sigma(E) = \sqrt{\sigma_0^2 + AE} \tag{1}$$

where E is the recoil energy,  $\sigma_0$  is the baseline resolution, and A is a detector-specific factor which is varied to achieve a given effective resolution. We also consider several values of  $\sigma_0$ : 1 eV, 5 eV, 10 eV, and 25 eV. Table I shows resolution criteria that are either future targets or have already been achieved for several experimental efforts. We can see that the current best demonstrated solid-target baseline resolution comes from the  $\nu$ -cleus collaboration at 3.7 eV [19]-between our two lowest baseline resolution points and probably achievable in the near future for Si and Ge. Going by the table it is seen that a 25 eV baseline resolution is probably on the horizon for many detectors. For the solid detectors in the table we also see that the typical threshold is a factor of 3-9 larger than the baseline resolution-roughly in line with our requirement that events have energies  $\geq 5\sigma_0$  (see below).

Different levels of ambient thermal neutron flux were surveyed between about  $\sim 10^{-7}$  and  $\sim 10^{-3}$  n/cm<sup>2</sup>s. The flux range is motivated by where this analysis produces high-significance  $(5\sigma)$  in the presence of modest "other" background (see below). The flux range includes the approximate behavior of the Dresden-II [4] published thermal neutron flux–0.25 n/cm<sup>2</sup>s–if we account for an approximately 3000 times higher reactor output power of that commercial reactor. The fluxes were translated to a total capture event count via the neutron capture cross section with natural silicon and germanium and assuming an exposure of 100 kg yr. The capture events were then sampled from the output PDF of nrCascadeSim v1.4.2. All sampled recoils with energy  $\leq 5\sigma_0$  were eliminated to emulate data collection with a finite energy threshold event trigger.

Thermal neutrons are not the only nuclear recoil backgrounds possible in  $CE\nu NS$  experiments, so we in-

CONUS[22]	Ge PPC	200 eVee <sup>b</sup>	$25 \text{ eVee}^{\mathbf{b}}$	
Dresden-II[4]	Ge PPC	$200 \text{ eVee}^{\mathbf{b}}$	$33 \text{ eVee}^{\mathbf{b}}$	
MINER[11]	Si/Ge cal	$\sim 20 \text{ eV}^{a}$	$5 \text{ eV}^{\mathbf{a}}$	
RED-100[23, 24]	$\dot{X}e 2PS$	$300 \text{ eV}^{\mathbf{a}}$	-	
RICOCHET[25, 26]	Si/Ge bol	$\sim 50 \text{ eV}^{a}$	$17 \text{ eV}^{\mathbf{b}}$	
TEXONO[27, 28]	Ge PPC	$300-400 \text{ eVee}^{\mathbf{a}}$	$45 \text{ eVee}^{\mathbf{b}}$	
$\nu$ -cleus[19]	$CaWO_4$ / $Al_2O_3$ cal	$19.7~{\rm eV}^{\rm b}$	$3.7 \text{ eV}^{\mathbf{b}}$	
$\nu \text{GeN}[29]$	Ge PPC	$350 \text{ eV}^{\mathbf{b}}$	$93 \text{ eV}^{\mathbf{b}}$	
TABLE I. Summary of $CE\nu NS$ searches at reactors. Non- standard abbreviations used are as follows. <b>cal</b> : Calorimeter.				

**2PS**: Two-phase scintillator. **bol**: Bolometer. Note also eVee refers to electron-equivalent (ionization) energy; other energies are heat.

<sup>a</sup> target

<sup>b</sup> achieved

Experiment

CONNIE<sup>[20]</sup>

clude an "other" nuclear recoil background with shape  $\propto E^{-0.9}$ , consistent with neutron-scatter background data given by [16], and very similar to the  $E^{-1.2}$  form mentioned in [5]. From MINER's 2017 background measurement they expect a combined 100 events/kg/day in nuclear recoil and electron recoil backgrounds but only 5-20 events/kg/day in CEvNS events [16]. The MINER authors acknowledge the need to control background and other experiments have demonstrated backgrounds with between 40–60% of what is expected from the  $CE\nu NS$ process [10, 30]. Given this information we normalize our nuclear recoil background to 60% of the CEvNS rate below about 1 keV. We do not add any further electron recoil background because it is often diluted to higher electron equivalent energies in ionization-sensitive detectors. Furthermore, the electron recoils in some cases can be discriminated [31–33]. This background model is expected to represent approximately the maximum acceptable background to a typical  $CE\nu NS$  search. Other variations of our fits have been completed in the release of our code for this analysis [34].

#### IV. STATISTICAL COMPARISON

The combined sample of recoil energies from the three sources (CE $\nu$ NS, neutron capture, and other backgrounds), were separated back into  $CE\nu NS$  and neutroncapture components by binned maximum likelihood fits with the likelihood function:

$$\mathcal{L} = e^{-n_{\text{total}}} \prod_{j=1}^{N_{\text{bins}}} \frac{1}{C_j!} \left[ n_{\nu} P_{\nu,j} + n_c P_{c,j} + n_b P_{b,j} \right]^{C_j}, \quad (2)$$

where  $C_j$  is the observed number of events in bin j,  $n_{\nu}$ ,  $n_c$ , and  $n_b$  are the fitted number of CEvNS, capture, and background events, respectively,  $n_{\text{total}}$  is the sum of these, and  $P_{\nu,j}$ ,  $P_{c,j}$ , and  $P_{b,j}$  are the probability of an

event of each type lying in bin j (all normalized such that they sum to unity over all bins).

We employ a likelihood ratio test on  $\mathcal{L}/\mathcal{L}'$ , where  $\mathcal{L}'$ is a similar likelihood function but without the CEvNS contribution-with the parameter  $n_{\nu}$  in Eq. 2 set to zero.

The two likelihoods are compared using Wilks' theorem, which states that  $2\ln(\mathcal{L}/\mathcal{L}')$  is distributed as a chisquared random variable with, in this case, one degree of freedom [35]. This leads immediately to a probability for comparing the nested models, i.e., the probability that the combined model of Eq. 2 is a better model than the simple model with  $n_{\nu}\equiv 0$ . We quantify the confidence level as the Z-value ( $\sigma$  value) corresponding to the symmetric (two-sided) normal error integral with the same probability, i.e.,  $\sqrt{2\ln(\mathcal{L}/\mathcal{L}')}$ .

Figure 1 shows example fits for different combinations of effective resolutions and neutron fluxes in silicon. Resolutions of 10 and 35 eV are used in conjunction with neutron fluxes of  $4.36 \times 10^{-5}$  and  $9.77 \times 10^{-5}$  n/cm<sup>2</sup>s with  $\sigma_0 = 1$  eV. The black points show the histogram of our toy model data for given CEvNS, thermal flux, and background contributions. The toy model data is smeared using our hypothetical resolution functions and plotted for recoil energies between 0 and 1800 eV. Solid blue and orange curves show the fitted PDFs for withand without-CEvNS fits. The dashed blue curve shows the CEvNS contribution to the with-CEvNS fit. The confidence level of each fit is given in the upper left corner of each plot, red if less than  $5\sigma$  and blue if greater.

In Fig. 1 the leftmost and rightmost plots show the two methods by which the  $CE\nu NS$  signal can be detected, either by improving resolution so the  $CE\nu NS$  signal can be discerned on the low-energy downslope (leftmost plot), or by reducing the neutron flux so that the peak caused by  $CE\nu NS$  events is clearly visible over the signal from capture events (rightmost plot). The center plot shows a scenario where the thermal neutron flux is too high to produce a  $5\sigma$  CEvNS detection with the assumed livetime. Fig. 2 shows the analogous fit plots for germanium. In the germanium case we use resolutions of  $20 \,\mathrm{eV}$  and  $45 \,\mathrm{eV}$ with thermal neutron fluxes of  $5.52 \times 10^{-4}$  n/cm<sup>2</sup>s and  $1.75 \times 10^{-4}$  n/cm<sup>2</sup>s. The thermal neutron fluxes used for germanium are generally higher than for silicon because germanium is more resilient to the flux-although there are more capture events the capture spectrum overlaps less strongly than in silicon.

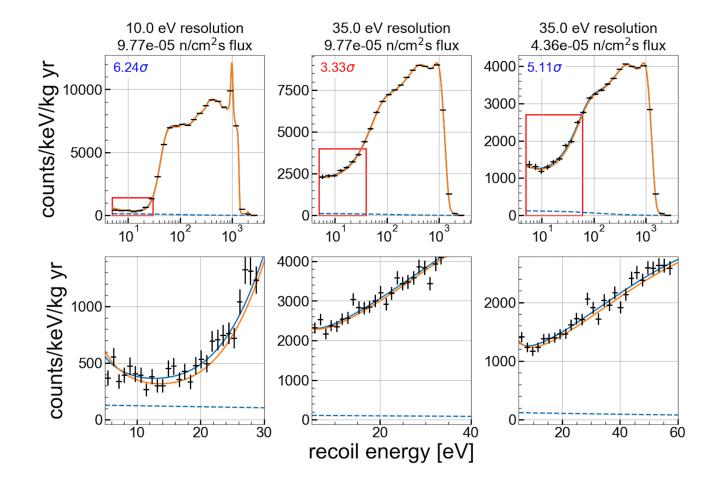


FIG. 1. (Color online) Likelihood fitting examples for three different combinations of resolution and neutron flux for  $\sigma_0 = 1 \text{ eV}$  in silicon. The left two plots show a flux of  $9.77 \times 10^{-5} \text{ n/cm}^2\text{s}$ , corresponding to  $\sim 1.1 \text{ M}$  capture events, and the right is lower flux,  $4.36 \times 10^{-5} \text{ n/cm}^2\text{s}$ , corresponding to  $\sim 500,000$  capture events. The right two plots show data with an effective resolution of 35 eV, and the left plot shows an effective resolution of 10 eV. The black points show the histogram of our toy model data for given CEvNS, thermal flux, and background contributions. Solid blue and orange curves show the fitted PDFs for with- and without-CEvNS fits. The dashed blue curve shows the CEvNS contribution to the with-CEvNS fit.

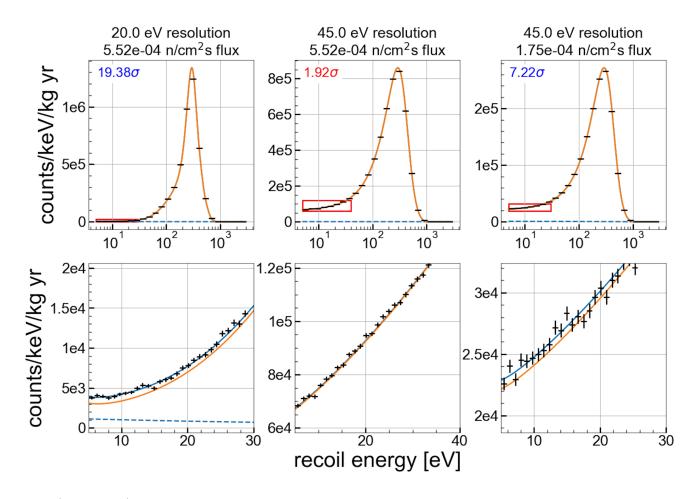


FIG. 2. (Color online) Likelihood fitting examples for three different combinations of resolution and neutron flux for  $\sigma_0 = 1 \text{ eV}$  in germanium. The left two plots show a flux of  $5.52 \times 10^{-4} \text{ n/cm}^2\text{s}$ , corresponding to  $\sim 31.6 \text{ M}$  capture events, and the right is lower flux,  $1.75 \times 10^{-4} \text{ n/cm}^2\text{s}$ , corresponding to  $\sim 10 \text{ M}$  capture events. The right two plots show data with an effective resolution of 45 eV, and the left plot shows an effective resolution of 20 eV. The black points show the histogram of our toy model data for given CEvNS, thermal flux, and background contributions. Solid blue and orange curves show the fitted PDFs for with- and without-CEvNS fits. The dashed blue curve shows the CEvNS contribution to the with-CEvNS fit.

# V. RESULTS AND DISCUSSION

Figure 3 shows the results for 100 kg yr exposure in Si (left) and Ge (right) for  $\sigma_0 = 1$  eV. To produce this plot, we generated a grid of 25 resolution values and 25 flux values and completed fits on that grid for each material. The contour plot is a smoothing of those fit results. The vertical axis shows ambient thermal neutron flux and the horizontal axis shows the effective resolution. Colors correspond to confidence levels. The two horizontal broken lines delineate a few reference flux levels - the gray dashed shows the generally accepted ambient neutron flux at sea level,  $4 \text{ cm}^{-2} \text{ hr}^{-1}$  [36]. The gray dotted shows 1 part in  $10^9$  of the neutron flux measured at the MINER facility.  $5.8 \times 10^7$  cm<sup>-2</sup> s<sup>-1</sup> [16], extrapolated to ten meters from the reactor core. As reference, the two lines correspond to approximately 13,000,000 (63,000,000) and 7,500,000 (37,000,000) neutron capture events in Si (Ge), respectively.

The black lines represent  $5\sigma$  contours, approximately 99.99994% confidence in the presence of the CEvNS signal, for three different values of  $\sigma_0$  (the 1 eV contour is the contour for the pictured colormap data). Each contour was yielded after smoothing the data by six iterations through a Jacobi relaxation scheme. Above each line, it is unlikely that the CEvNS signal can be extracted from the data given that baseline resolution.

Up to statistical fluctuations, the confidence increases monotonically moving toward lower fluxes and better resolutions, as would be expected. This is the case for all baseline resolutions probed.

Many interesting features can be seen in this data. For  $\sigma_0 = 1$  eV, below an effective resolution of ~ 20 eV, improving resolution has a dramatic effect on tolerance to ambient neutrons. An improvement in effective resolution from 10 to 20 eV is enough to allow measurement of CEvNS in an ambient flux three times larger. However, at larger baseline resolutions, the improvement with effective resolution is much smaller, and at  $\sigma_0 = 10$  eV, changing the effective resolution does almost nothing. This is an instructive, and promising, result, emphasizing that the feasibility of CEvNS measurements gets ever greater as detector technologies improve, but that decreasing the thermal neutron flux of current experiments may be a vital step in achieving these measurements.

Further, even with drastic detector improvements, thermal neutrons could still represent a substantial background in the vicinity of nuclear reactors. It can be seen in figure 3 that the measured MINER reactor-adjacent flux needs to be brought down to one part in a billion to begin seeing a CEvNS signal at a baseline resolution of only 1 eV, and must be brought down even further at  $\sigma_0 = 10$  eV. Note that the flux measurement by MINER [16] was early in the campaign. Many materials like boron, cadmium, gadolinium, polyethylene, and more can be used to bring down thermal fluxes by large factors. The thermal neutron background situation is somewhat better in germanium detectors owing to the larger CE $\nu$ NS cross section and lower capture rates at low energy.

We have done our analysis in terms of nuclear recoil energies but many detectors will measure the ionization caused by nuclear recoils instead. This will tend to shift all the nuclear recoil events toward lower energies, as the ionization yield is below unity and typically lower at lower energies [37]. However, we expect our results to be unaffected as the shift is largely the same for both capture and neutrino induced recoils. The resolution and detector threshold would also have to be adapted to the specific case.

In germanium detectors the thermal neutron flux can be measured *in situ* and compared with our results. The flux measurement is based on the rates of one of the Xray emissions from electron capture of <sup>71</sup>Ge. After several half-lives ( $T_{1/2}=11.4$  days) the ambient neutron flux will be equal to the rate of the K-shell electron capture (EC) line divided by a quantity which is the product of the branching of that line, the macroscopic cross section of <sup>70</sup>Ge capture, and the volume of the detector.

Thus far, this study has not discussed the possibility of vetoing events based on outgoing capture gamma rays. In general, capture events are highly vetoable by looking for signs of the gammas emitted during each capture. As a simple estimate of plausible effective flux reduction, Table II lists the expected effective flux  $f_{\text{effective}}$  over the actual flux  $f_{\text{actual}}$  as a function of  $\overline{d}$ , the angle-weighted average distance an emitted gamma would travel before leaving a detector made of either silicon or germanium. Values are based on the probability of gammas from capture event leaving the detector without interacting, based on the same cascades (potentially involving multiple exiting gamma rays) and cascade rates used to generate the capture event spectra, and using gamma/nucleus cross sections yielded via linearly interpolating data from NIST's XCOM database [38]. These estimates show that physically larger detectors can make great gains in reducing the importance of ambient thermal neutrons, particularly in the case of germanium.

	$f_{ m effective}/f_{ m actual}$	
$\bar{d} \; (\mathrm{cm})$	Si	${\rm Ge}$
1	0.8382	0.442
5	0.4267	0.07027
10	0.1937	0.01251
20	0.04538	0.001166
50	0.001747	7.313e-06
100	7.119e-05	1.917 e-09

TABLE II. Expected effective thermal neutron flux  $f_{\text{effective}}$  over actual flux  $f_{\text{actual}}$  in silicon and germanium detectors as a function of  $\bar{d}$ , the average distance a gamma must travel before leaving the detector. Reduction is based on the probability of gammas leaving the detector without interacting.

Some assumptions about the "other" backgrounds should be noted. The low-energy-skewed spectrum  $(\propto E^{-0.9})$  can be viewed as an instantiation of the anomalous excess of events in low-threshold cryogenic de-

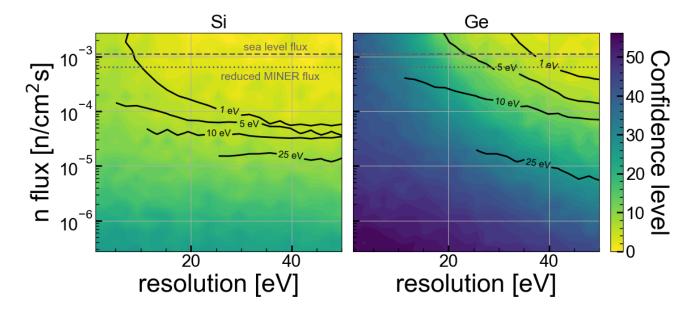


FIG. 3. (Color online) Confidence level for varying ambient thermal neutron flux (vertical axis) and effective resolution (horizontal axis) for a baseline resolution of 1 eV in Si (left) and Ge (right). Horizontal lines mark fluxes corresponding the accepted ambient sea level flux (dashed) and one part in 10<sup>9</sup> of the measured flux at the MINER facility [16] (dotted). Black contour lines representing  $5\sigma$  confidence levels for different values of the baseline resolution  $\sigma_0$  are also shown. The value of  $\sigma_0$  corresponding to each contour is given by the label on each contour.

tectors at low energy recently measured by several collaborations [16, 30, 39–50]. The origin of these events are unclear, and a single common explanation for the excesses is unlikely, making it difficult to assess the likely form for such an excess in our simulated experiment. However, since we consider the nuclear recoil energy scale these excess events are either similarly peaked to our assumed additional background model, or they are more spread out due to the less-than-unity quenching factor of nuclear recoils.

The last point that bears discussion is that the reactor model used here may be a best-case scenario. A parallel track of calculations in silicon using antineutrino spectrum data from the Daya Bay nuclear reactor complex in Southern China [51] yielded consistently lower confidence values. This fact highlights possible systematic uncertainties in our analysis due to uncertainties in the reactor anti-neutrino spectrum. The precise shape and overall normalization of this spectrum is actively being improved [52, 53], but the current status does not preclude changes to our results based on the form of the spectrum. This is expected to be a more significant effect than changes based on uranium enrichment and relative fission contributions from <sup>235</sup>U, <sup>238</sup>U, <sup>239</sup>Pu, and <sup>241</sup>Pu. This is certainly a less significant effect than the ability to veto capture events, but still should be noted.

Overall, our analysis shows that keeping the effective thermal neutron flux (flux after veto) below  $\sim 10^{-4} \,\mathrm{n/cm^2s}$  for a 1 MW reactor at 10 meters is necessary for silicon detectors—even ones with exceptional resolutions. Germanium is somewhat more robust for detectors

tors with exceptional resolution, requiring the flux to be below ~  $7 \times 10^{-4}$  n/cm<sup>2</sup>s under the same conditions. For germanium detectors with 25 eV baseline resolution (still excellent by today's standards) the thermal neutron flux needs to fall below ~  $10^{-5}$  n/cm<sup>2</sup>s. These rules of thumb can be roughly adapted to other reactors by multiplying this flux by the reactor power in MW (uranium enrichment level probably makes a sub-dominant difference) and accounting for the distance by an inverse-square law for the neutrinos.

All of the Python code used for this analysis can be obtained via the Open Storage Framework (OSF) data entry [34]. The PDFs for the thermal neutron-induced nuclear recoils were obtained from our public code [18].

# ACKNOWLEDGMENTS

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