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Utilizing cosmic-ray positron and electron observations to probe the averaged properties of Milky Way pulsars

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Pulsars have long been studied in the electromagnetic spectrum. Their environments are rich in high-energy cosmic-ray electrons and positrons likely enriching the interstellar medium with such particles. In this work we use recent cosmic-ray observations from the AMS-02, CALET and DAMPE collaborations to study the averaged properties of the local Milky Way pulsar population.

We perform simulations of the local Milky Way pulsar population, for interstellar medium assumptions in agreement with a range of cosmic-ray nuclei measurements. Each such simulation contains $\sim 10^4$ pulsars of unique age, location, initial spin-down power and cosmic-ray electron/positron spectra. We produce more than 7×10^3 such Milky Way pulsar simulations. We account for and study i) the pulsars' birth rates and the stochastic nature of their birth, ii) their initial spin-down power distribution, iii) their time evolution in terms of their braking index and characteristic spindown timescale, iv) the fraction of spin-down power going to cosmic-ray electrons and positrons and v) their propagation through the interstellar medium and the Heliosphere. We find that pulsars of ages $\sim 10^5 - 10^7$ yr, have a braking index that on average has to be 3 or larger. Given that electromagnetic spectrum observations of young pulsars find braking indices lower than 3, our work provides strong hints that pulsars' braking index increases on average as they age, allowing them to retain some of their rotational energy. Moreover, we find that pulsars have relatively uniform properties as sources of cosmic-ray electrons and positrons in terms of the spectra they produce and likely release O(10%) of their rotational energy to cosmic rays in the ISM. Finally, we find at $\simeq 12$ GeV positrons a spectral feature that suggests a new subpopulation of positron sources contributing at these energies.

I. INTRODUCTION

Pulsars represent a class of energetic sources whose properties have been probed over more than 50 years via observations in the electromagnetic spectrum. Emission from pulsars and their environments has been detected in the radio, [1–8], infrared and visible [9–13], ultraviolet [14, 15], X-rays, [12, 16–20], gamma-rays [21–26] and most recently, a clear detection of powerful Milky Way pulsars at O(10) TeV gamma-rays has been established [27–31]. Most of the observed photons from pulsars and their surrounding pulsar wind nebulae (PWNe) -where those are present- originate from cosmic-ray electrons and positrons and are emitted via curvature radiation [32, 33], synchrotron radiation [24, 34, 35] and at the highest energies inverse Compton emission [24, 36–38]. The fact that we have observed O(10) TeV gamma-rays from certain pulsars that are still surrounded by their respective PWN clearly sets a lower limit on the electron and positron cosmic-ray energies in these environments. We expect that such pulsars will act as sources of cosmicray electrons and positrons that are released into the interstellar medium (ISM). In fact, we expect for electrons and positrons to be further accelerated as they propagate through the termination shock of the respective PWNe before entering the ISM [39, 40]. If Milky Way pulsars are

prominent sources of high-energy cosmic-ray electrons and positrons then we could expect to see their contribution to the relevant cosmic-ray measurements and most notably in the cosmic-ray positron flux spectrum.

Cosmic-ray positrons are produced in inelastic collisions of high-energy cosmic-ray nuclei with the ISM gas and are typically referred to as secondary positrons. In the same type of interactions matter cosmic-ray secondary electrons and secondary nuclei as Boron are produced. Those have been modeled in [41–49] and are in agreement with the current observations [50-52]. A prominent exception is the spectrum of the positron fraction $e^+/(e^+ + e^-)$, measured by [53–56] to rise above 5 GeV, in disagreement with the expectation from same type of models. This suggests an additional source of high-energy cosmic-ray positrons. Such positrons can come from near-by Milky Way pulsars [40, 57–73]. One alternative to pulsars includes local and recent supernova remnants (SNRs) [74–84]. However, given that SNRs are the major source of all cosmic rays, in order to explain the rising positron fraction, the metallicities of environments of recent and close-by SNRs have to be different from those of the Milky Way on average [80, 81, 85, 86]. Another possibility is that of particle dark matter [67, 87–106]. While such particle dark matter models have been constrained by cosmic microwave background (CMB) data [107–112] and γ -rays [113–115], the full parameter space has not been entirely excluded.

In this paper we are going to use the cosmic-ray observations from the Alpha Magnetic Spectrometer (AMS-

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 $\theta 2$), the Calorimetric Electron Telescope (*CALET*) onboard the International Space Station and the DArk Matter Particle Explorer (*DAMPE*) satellite. We are going to set constraints on the contribution of local Milky Way pulsars to the electron and positron (e^{\pm}) fluxes and in turn probe their averaged properties. For cosmic-ray energies *E* above 10 GeV the propagation of electrons and positrons is mostly affected by their energy losses due to synchrotron radiation and inverse Compton scattering [116]. The relevant energy loss timescale for electrons and positrons of initial energy E_{init} to lose half its energy is,

$$\tau_{\rm loss}(E_{\rm init}) \simeq 20 \times \left(\frac{E_{\rm init}}{10 {\rm GeV}}\right)^{-1} {\rm Myr.}$$
 (1)

Pulsars lose their rotational kinetic energy within O(10) kyr. Roughly that is also equal to the time that magnetic fields in the surrounding PWNe and the further out SNR become weak enough to allow the relevant cosmic-ray e^{\pm} to effectively escape. The O(10) kyr timescale is typically one to four orders of magnitude smaller by comparison to the timescale cosmic rays need to reach us via diffusion from O(100) pc - O(1) kpc distances where most pulsars are at. Thus, pulsars can be treated as approximately injecting an appreciable fraction of their rotational energy to cosmic-ray electrons and positrons at the beginning of their existence [40, 62]¹.

A result of Eq. 1, is that as the observed energy of cosmic rays increases, the number of potential sources drops given that only the most recent pulsars have an age that is similar to $\tau_{\rm loss}$. As pulsars are born in the Milky Way with a rate of $\simeq 1$ per century [118–122], only a small number of them can contribute, and only from an increasingly smaller distance. The relation connecting the maximum energy that electrons and positrons can have originating from a distance R was approximated in [123] to be $E_{\rm max} \sim 100 \,{\rm GeV}(R/2\,{\rm kpc})^{-2}$. For instance at 500 GeV we are probing only pulsars from within ~ 400 pc. As there is only a small number of such pulsars, the discreteness of those sources will result in subsequent features [40, 62, 123, 124] (see also [84] for a similar study on the impact of recent SNRs). With the recent refined observations by AMS-02 and the observations by CALETand DAMPE that extend up to 5 TeV we will probe the properties of these pulsars. The lower energies of 5-500 GeV, are also used and provide us with valuable information on the averaged properties of pulsars that are now "middle aged" and of up to O(10) Myr and are located within 4 kpc. Finally, we will show that we can also

asses information on the properties of the ISM within that same volume.

In section II, we discuss the simulations that we perform to account for astrophysical uncertainties on a) the stochastic birth distribution in space and time of the pulsar source-population, b) the initial properties of the total energy output of these sources, c) their timeevolution, d) their injection spectral properties of cosmicray e^{\pm} and e) the propagation of cosmic rays through the ISM and the Heliosphere. Then in section III, we will discuss the data that we use and our fitting procedure. In section IV, we present our results. We show first our results from comparing to the observations above 15 GeV and then further discuss the lower energy analysis of measurements down to 5 GeV in the positron fraction and flux, where we notice a somewhat significant feature at $\simeq 12$ GeV. Finally, we give our conclusions and summary in section V.

II. MILKY WAY PULSAR SIMULATIONS

Our pulsar simulations account for,

- the stochastic nature of the neutron stars' birth distribution in space and in time. We run simulations for different birth rates of neutron stars,
- the initial conditions of the neutron stars in terms of their initial spin-down power distribution,
- the uncertainties on their time evolution, in terms of the braking index κ and characteristic spin-down timescale τ_0 ,
- the fraction of spin-down power that goes to cosmic-ray electrons and positrons released into the interstellar medium, and the injection spectrum these particles have,
- how the electrons/positrons propagate from the pulsars to us i.e. their propagation through the ISM and the Heliosphere.

In this work we produce 7272 Milky Way pulsar simulations to account for the various combinations of parameters that we vary. Each of our simulations extends out to 4 kpc from the Sun and contains between 5×10^3 to 19×10^3 unique pulsars, depending on the exact assumption of the Milky Way pulsar birth rate. In the following we describe the specific assumptions that we test in our simulations.

A. The birth distribution of pulsars in space and time

From observations along the galactic plane we expect a pulsar birth rate of 1.4 ± 0.2 per century [121]. However, this rate is probably more uncertain as wider estimates have been made in [118–120, 122]. We take three basic choices for the pulsar birth rate of 0.6, 1 and 2 per century

¹ A recent work on pulsars surrounded by TeV halos, has suggested that some pulsars may be able to contain their cosmic rays well after their birth [117]. As long as the injection phase of GeV-TeV cosmic rays from these environments into the ISM occurs on a timescale significantly smaller than their propagation time, our basic analysis is not changed as this would be on average an overall time-shift for the pulsar population.

for the entire Milky Way. We note that more choices for the birth rate between the values of 0.6 and 2 pulsars per century would not change our basic results 2 .

In our simulations pulsars are stochastically generated based on a profile probability density function. We follow the same spatial distribution as in earlier work of [123]. Our spatial distribution relies on observations of Parkes multi-beam pulsar survey at 1.4 GHz [125] and subsequent models in [120, 121, 126]. We assume azimuthal symmetry with respect to the galactic center and an exponentially decreasing pulsar density as we move away from the galactic disk, with a typical scale height of 50 pc. As most of the rotational energy of pulsars is emitted in their first O(10) kyr, the associated natal kicks that are typically $O(10^2)$ km/s, can only result in a displacement of O(1) pc. Such displacements represent a minor correction to the original birth spacial distribution which we ignore.

B. The Pulsars' Initial Spin-Down Distribution Properties

Each pulsar due to asymmetries in the core-collapse of their progenitor star acquires an initial rotational energy. At the same time these are highly magnetized objects with initial B-field strengths at their poles of order 10^{12} G and up to 10^{15} G for magnetars. Typically the axis of rotation is not aligned to the axis of the magnetic field leading to energy losses, known as spin-down. A pulsar's spin-down power \dot{E} evolves with time and is modeled here as [127],

$$\dot{E}(t) = \dot{E}_0 \left(1 + \frac{t}{\tau_0} \right)^{-\frac{\kappa+1}{\kappa-1}}.$$
(2)

 E_0 is the original spin-down power of a given pulsar, τ_0 is its characteristic spin-down timescale and κ its braking index. For a given Milky Way pulsars simulation we assume that the pulsars' initial spin-down power is equal to $\dot{E}_0 = 10^x$ ergs/s with $x = x_{\rm cutoff} - y$. In each of our Milky Way simulations each pulsar has its unique *y*-value, i.e unique initial spin-down power. Using the same parametrization of [123], the *y*-parameter follows a log-normal distribution,

$$f(y) = \frac{\operatorname{Exp}\left\{-\frac{\left[-\mu_y + \ln(y)\right]^2}{2\sigma_y^2}\right\}}{\sqrt{2\pi}y\sigma_y}.$$
(3)

The values for x_{cutoff} and μ_y are constrained by radio observations and subsequent modeling of Myr old pulsars' periods [120]; and by comparing to the ATNF pulsar catalog [128, 129]. We set an upper cutoff $x < x_{\text{max}} = 38.7$



FIG. 1. The cosmic-ray positron flux from a Milky Way pulsars simulation. The solid black line includes the contribution of the cosmic-ray secondaries (from inelastic p-p, p-N and N-N collisions in the ISM). We highlight the contribution to the positron flux from individual pulsars that have ages from O(10) kyr to 5 Myr and that are relatively close-by. The contribution from individual pulsars is enhanced from the original simulation to show their fluxes within the figure. The AMS-02 observation is shown in the data points.

indicative of the Crab pulsar's observed spin-down . We take $\sigma_y = [0.25, 0.36, 0.5, 0.75]$ which allow varying degree of widths in those distributions. A $\sigma_y = 0$ would assume that all pulsars have an identical initial spin-down power. A distribution on the y-parameter should be expected both from the fact that there is a distribution on the magnitude of the initial B-fields at the poles and a distribution in the angle between the magnetic field axis and the axis of rotation.

C. The Pulsars' Spin-Down Evolution

As we said in the introduction we want to test the spin-down properties of pulsars relying on cosmic-ray observations. Detected cosmic rays at the 5 GeV-5 TeV energy range can be used to probe the contribution of pulsars with ages between $O(10^2)$ kyr and $O(10^2)$ Myr as we show in Figure 1, where we have highlighted the contribution of a few specific pulsars of given distance and age ranges. Younger pulsars contribute at TeV energies. Middle-aged pulsars of age $10^2 - 10^3$ kyr contribute dominantly at O(100) GeV and can give spectral features at these energies. Older pulsars have suppressed overall fluxes, but also more prominent peaks and subsequent cut-offs, due to cosmic-ray cooling, and might still be able to give minor spectral features at energies lower than 100 GeV.

As we want to test if the braking index κ is different for $O(10^2)$ - $O(10^5)$ kyr pulsars compared to the much younger objects, we create Milky Way pulsars simulations where all pulsar members have the same value of κ and τ_0 . By creating such simulations we can test if pulsars of older ages statistically prefer certain values of κ .

 $^{^2}$ Our simulations show a preference for a birth rate of 2 pulsars per century, but not in a manner that changes our conclusions.

If a pulsar's angle between its axis of rotation and magnetic field axis evolves with time, that can be interpreted as an evolution of κ [130, 131]. A relatively fast decay of the magnetic field's amplitude at the poles can also lead to a changing braking index [132–137]. In addition, different equations of state can give for the same total mass different values of κ [138, 139]. All these effects can result in the braking index evolving with time. Only a small number of pulsars exist with a reliably measured braking index, and all of them are very young [140, 141] (see however [142]). Such young pulsars have negligible contribution to the observed cosmic-ray spectra and are not the focus of this study.

In Table I, we give all the spin-down power distribution properties for our Milky Way pulsars simulations. We test discrete values of $\kappa = [2.5, 2.75, 3.0, 3.25, 3.5]$, where τ_0 varies from 0.6 kyr for $\kappa = 2.5$ to 30 kyr for $\kappa = 3.5$. These combination of values of τ_0 and κ are picked to be in agreement with surface magnetic fields as well as periods from [120]. We also include different assumptions on the pulsars' distribution of the initial spin-down power. Table I, is an expansion of earlier work in [123]. We typically run 72 simulations per combination of τ_0 , κ , x_{cutoff} , μ_y and σ_y , but in some cases we run up to 108 (as in the 100-1H7) case.

D. Pulsars as Sources of Cosmic-Ray Electrons and Positrons

From microwave, X-ray and gamma-ray observations, we know that high-energy cosmic-ray electrons and positrons exist within a pulsar's magnetosphere. Moreover, electrons and positrons can be further accelerated in the termination shock of the pulsar wind nebula (PWN) and if there still is a supernova remnant shock (SNR), its termination shock just before entering the ISM. In addition observations from HAWC and Milagro show evidence for O(10) TeV γ -rays towards Geminga and Monogem [30, 143, 144]. These observations show that 10-100 TeV cosmic-ray electrons and positrons exist at distances up to $\simeq 10$ pc from these middle aged pulsars.

In Ref. [40], it was shown that as a pulsar's characteristic spin-down timescale τ_0 is ~ 10⁴ yrs, an appreciable fraction (~ 1/2) of the pulsar's initial rotational energy will be lost before the SNR shock front surrounding it stops being an efficient cosmic-ray accelerator. τ_0 is also much smaller than the timescale the surrounding PWN stops accelerating cosmic rays. As cosmic rays typically require $O(10^2)$ kyr to Myr to reach us from individual pulsars through diffusion, we can reliably approximate pulsars to instantaneously inject cosmic-ray electrons and positrons at the time of their birth (see Ref. [40] for further details) ³. The aim of this work is to constrain the averaged cosmic-ray injection spectral index n from pulsars. For the injection spectra we assume,

$$\frac{dN}{dE} \propto E^{-n} \operatorname{Exp}\left\{-\frac{E}{E_{\rm cut}}\right\}.$$
(4)

We take n to follow a uniform distribution within the range of $n \in [1.4, 1.9]$ which we refer to as option "A" or two narrower ranges of $n \in [1.6, 1.7]$, our option "B", or $n \in [1.3, 1.5]$ our option "C". The upper cutoff E_{cut} is taken to be 10 TeV. We find that its exact value does not affect our fitting results. This should be expected as the highest energy cosmic rays lose their energy faster.

Furthermore, we model the fraction η of rotational energy that ends in cosmic rays released into the ISM and the relative variations of that fraction between pulsars. Following [70, 123], we take a log-normal distribution for the η parameter,

$$g(\eta) = \frac{\exp\left\{-\frac{[-\mu + ln(-1+\eta)]^2}{2\sigma^2}\right\}}{\sqrt{2\pi}(\eta - 1)\sigma},$$
 (5)

and take three different choices for (μ, σ) to be (0.32, 0.12) (option "A"), (0.64,0.23) (option "B") and (-0.38, 0.16) (option "C"). These give square root variances of 0.169, 0.454 and 0.112 respectively. In our Milky Way pulsars simulations, before fitting to the data ,we also pick specific values for μ that affect the mean efficiency of these pulsars, $\bar{\eta} = 1 + \exp\left\{\mu + \frac{\sigma^2}{2}\right\}$. These are $\bar{\eta} = 4 \times 10^{-3}$ (for option "A"), 1×10^{-3} (for option "B") and 2×10^{-2} (for option "C"). However, we fit each Milky Way pulsars simulation to the data and thus the $\bar{\eta}$ is reset by the data.

In Figure 2, we show five simulations of Milky Way pulsars to highlight the impact of our assumptions on the braking index κ , the spin-down timescale τ_0 and the variance of the fraction of energy going to cosmic-ray electrons and positrons, where $10^{\sqrt{\text{variance}}} = \zeta$. We simulate 8.6×10^3 individual pulsars, whose locations and ages are fixed. The youngest of these pulsars is 175 yr and the oldest 10 Myr, and all are with 4 kpc from us. We change the spin-down evolution of those pulsars by assuming different values of κ and τ_0 relevant in Eq. 2. taking a fixed value of ζ (red vs black vs blue solid lines). We normalize all simulations in Figure 2 to get the same positron flux at 100 GeV. This is done to showcase the impact of these assumptions in our analysis. As we will describe in section III, we fit the simulated fluxes to the AMS-02 observed flux. Once fitting to the positron flux,

³ An exception to that approximation would be the injection of

cosmic rays from a very young pulsar within < 100 pc. Such pulsars are very rare however, appearing in very few of our simulations. Moreover, as we show in Figure 1, their contribution would appear at very high energies, not observable by the satellite experiments we rely on.

Sim no.	τ_0 (kyr)	κ	$x_{\rm cutoff}$	$\mu_y \sigma_y$
100-1H7	6	3	38.8	$0.25 \ 0.5$
200-2H7	3.3	3	38.8	$0.25 \ \ 0.5$
300-3H7	10	3	38.8	$0.25 \ 0.5$
400-471	3.3	3	39	$0.1 \ 0.5$
500-571	1	2.5	38.8	$0.25 \ 0.5$
600-671	20	3.5	39	0.1 0.5
700-771	0.7	2.5	38.8	$0.25 \ 0.5$
800-871	20	3.5	39.1	$0.0 \ \ 0.25$
900-971	0.6	2.5	39.0	$0.1 \ \ 0.25$
1000-1071	6	3	39.0	$0.1 \ \ 0.25$
1100 - 1071	6	3	38.7	$0.5 \ 0.75$
1200 - 1271	30	3.5	38.8	$0.25 \ 0.5$
1300 - 1371	0.85	2.5	38.5	$0.6 \ 0.75$
1400 - 1471	18	3.5	39.0	$0.0 \ 0.75$
1500 - 1571	10	3	38.7	$0.5 \ 0.75$
1600 - 1671	4	3	39.0	$0.0 \ \ 0.36$
1700 - 1771	1	2.5	38.7	$0.5 \ 0.75$
1800-1871	9	3	38.2	$0.4 \ \ 0.36$
1900 - 1971	0.8	2.5	38.2	$0.4 \ \ 0.36$
2000-2071	0.6	2.5	38.2	$0.4 \ \ 0.36$
2100-2171	30	3.5	38.2	$0.4 \ \ 0.36$
2200-2271	7	3	39.0	$0.1 \ 0.75$
2300-23H7	30	3.5	38.0	$0.5 \ \ 0.36$
2400-24H7	30	3.5	38.7	$0.5 \ 0.75$
2500-25H7	6	3	38.9	$0.18 \ 0.36$
2600-26H7	4.5	3	39.3	$0.0 \ 0.25$
2700-27H7	9	3	38.5	$0.5 \ 0.25$
2800-28H7	27	3.5	38.5	$0.3 \ 0.25$
2900-29H7	33	3.5	38.0	$0.5 \ 0.25$
3000-3071	0.85	2.5	38.3	$0.5 \ 0.25$
3100-3171	18	3.25	38.8	0.25 0.5
3200-3271	15	3.25	38.8	0.25 0.5
3300-3371	18	3.25	38.5	0.4 0.25
3400-3471	20	3.25	38.0	0.4 0.25
3500-3571	15	3.25	38.5	0.4 0.36
3600-3671	20	3.25	38.8	0.5 0.75
3700-3771	2	2.75	38.8	0.25 0.5
3800-3871	1.5	2.75	38.8	0.25 0.5
3900-3871	1.6	2.75	38.5	$0.5 \ 0.25$
4000-4071	1.3	2.75	38.0	0.4 0.25
4100-4171	1.2	2.75	38.3	0.4 0.36
4200-4271	2.4	2.75	38.5	$0.5 \ 0.75$

TABLE I. The Milky Way pulsars'-simulation spin-down power distribution and time evolution assumptions. We provide the names here as a reference to our publicly available list of simulations^a.

^a We have made publicly available our Milky Way pulsars simulations through,

https://zenodo.org/record/5659004#.YYqnbi-ZNOs.

a higher value of κ , would suggest that most flux from pulsars and the associated features are at higher energies. When pulsars have a larger κ they release more slowly their energy. As a result they can remain strong sources of high-energy cosmic rays for a longer amount of time. In turn their combination gives enhanced fluxes at the highest energies.

In Figure 2, we also show the impact of varying the assumptions on the variance, by fixing the spin-down evolution to $\kappa = 3.0$ and $\tau_0 = 3.3$ kyr. Larger values of ζ ,



FIG. 2. The positron flux for different choices of spin-down evolution (red vs black vs blue) for a fixed assumption on $\zeta = 10^{\sqrt{\text{variance}}}$. We also compare different choices for ζ by keeping the spin-down assumptions fixed (black solid vs green dashed vs orange dot-dashed). See text for details.

result in some pulsars depositing a great fraction of their energy in electrons and positrons. Such pulsars are responsible for prominent features in the positron flux (and the positron fraction). A similar effect exists if instead pulsars have a large variance in their initial spin-down power, i.e. the value of σ_y of Eq. 3 is chosen to be high.

E. Cosmic-Ray Propagation through the ISM and heliosphere

Cosmic-ray electrons and positrons propagate in the interstellar medium via diffusion. How fast cosmic rays diffuse depends on the galactic magnetic field's amplitude and structure, and their energy. We assume isotropic and homogeneous diffusion that can be described by a rigidity (R)-dependent diffusion coefficient,

$$D(R) = D_0 \left(\frac{R}{1\,GV}\right)^{\delta}.$$
(6)

 D_0 is the relevant normalization set at 1 GV, regulated by the overall strength of magnetic fields in the Milky Way, while the diffusion index δ is defined by the spectrum of interstellar turbulence. $\delta = 0.33$, is for the case of Kolmogorov turbulence [145], while $\delta = 0.5$ is for Kraichnan two-dimensional turbulence [146]. Systematic study of cosmic-ray observations suggest that the diffusion index δ is within that range of values (see e.g. [48, 147]); which we use in our simulations. We model the diffusion taking place within a cylinder centered at the galactic center, of radius 20 kpc and extending to a height of $\pm z_L$ away from the galactic disk (the disk is at z = 0). Beyond those limits cosmic rays will escape the galaxy.

Furthermore, cosmic-ray electrons and positrons at the 10 GeV to 10 TeV range lose rapidly energy through inverse Compton scattering and synchrotron radiation with

Model	$z_L \ (\mathrm{kpc})$	$b \; (\times 10^{-6} \text{GeV}^{-1} \text{kyrs}^{-1})$	$D_0~({ m pc}^2/{ m kyr})$	δ
A1	5.7	5.05	140.2	0.33
A2	5.7	8.02	140.2	0.33
A3	5.7	2.97	140.2	0.33
C1	5.5	5.05	92.1	0.40
C2	5.5	8.02	92.1	0.40
C3	5.5	2.97	92.1	0.40
E1	6.0	5.05	51.3	0.50
E2	6.0	8.02	51.3	0.50
E3	6.0	2.97	51.3	0.50
F1	3.0	5.05	33.7	0.43
F2	3.0	8.02	33.7	0.43
F3	3.0	2.97	33.7	0.43

TABLE II. The ISM parameters that describe the propagations assumptions of cosmic rays in the Milky Way.

a rate that scales as,

$$\frac{dE}{dt} = -b\left(\frac{E}{1\,GeV}\right)^2.\tag{7}$$

This makes the highest energy cosmic-ray electrons and positrons lose more rapidly their energy and causes a "pile-up" before the cut-off, in the electron/positron fluxes from individual pulsars that is seen in Figure 1. The value of b, set at 1 GeV, is directly proportional to the energy density in the galactic magnetic field and the energy density in the CMB and interstellar radiation field photons. We note that at the highest energies the inverse Compton cross-section is not the Thomson crosssection assumed in Eq. 7, but instead the Klein-Nishina one [148, 149]. In our pulsars simulations we ignore the Klein-Nishina corrections, as we use a wide range of uncertainty on the b parameter, set to be within 3×10^{-6} and $8 \times 10^{-6} \text{ GeV}^{-1} \text{ kyrs}^{-1}$. We also ignore Bremsstrahlung emission losses that cause an energy-loss rate $\propto E$, that become important only at GeV energies.

Cosmic rays also experience diffusive reacceleration [150] and are affected by local convective winds. To account for ISM diffusion uncertainties we use four distinctive models, defined by the letters A, C, E, F. These models are in agreement with AMS-02 observations of the cosmic-ray proton, helium, carbon, oxygen fluxes and the beryllium-to-carbon, boron-to-carbon and oxygen-tocarbon ratios [49]. Each one of these models has three variants to account for uncertainties in the energy losses, i.e the b-parameter, denoted by a second character (1-3). A value of $b = 5.05 \times 10^{-6} \text{GeV}^{-1} \text{kyrs}^{-1}$ (for models A1, C1, E1, and F1), is in agreement with evaluations of the local magnetic and interstellar radiation field [43, 151, 152], while the choices of 2.97×10^{-6} and $8.02 \times 10^{-6} \text{ GeV}^{-1} \text{ kyrs}^{-1}$ represent the relevant uncertainties. All these parameters are described in Table II.

In comparing the ISM model predictions to the AMS-02 cosmic-ray nuclei measurements we used GALPROP v54 [43, 151], where we have included convection, reacceleration and Bremsstrahlung energy-losses. GALPROP gives us a prediction for the primary cosmic-ray electrons (from



FIG. 3. The impact of different ISM assumptions on the positron flux from two individual pulsars. Solid lines (blue, black, green and red) show the impact of different diffusion assumptions. The magenta dashed and orange dot-dashed are to be compared to the black solid line that is made under the same diffusion assumptions.

SNRs) and the secondary electrons and positrons from p - p, p - N and N - N inelastic collisions taking place at the ISM gas. However, for the cosmic-ray electrons and positrons from the individual pulsars the code that we use ignores ISM convection, diffusive reacceleration and Bremsstrahlung energy losses [40, 70, 123]. At the energies of interest the timescale for these effects are significantly larger than the diffusion and energy losses of Eq. 7 timescales. This allows us to place within 4 kpc from the location of the Sun up to 1.9×10^4 pulsars in unique positions and of unique age created in the last 10 Myr. We take the primary electron fluxes and secondary electron and positron fluxes from GALPROP and combine them with the pulsars' electron and positron fluxes from our Milky Way pulsars simulations.

In Figure 3, we show how the positron flux from individual pulsars is affected by different ISM propagation conditions. We model two individual pulsars, Geminga that is taken to be 0.25 kpc away and 3.42×10^5 yr in agreement with observations [129], and a second pulsar 1.0 kpc away and 2.0×10^6 yr old. Both pulsars are taken to have an initial spin-down power of $\dot{E}_0 = 1.1 \times 10^{38}$ erg/s, braking index $\kappa = 3.0$ and $\tau_0 = 6.0$ kyr, that for Geminga would give the currently observed spin-down power of 3.2×10^{34} erg/s. The cosmic-ray injection index of Eq. 4 is taken to be n = 1.65 for both.

Keeping energy losses fixed and changing between A2, C2 and E2 we note the difference in the positron flux's power-law spectrum for energies lower than the sharp cooling cut-off. That is simply affected by the diffusion index δ . For model F2, the flux is significantly larger as the diffusion normalization D_0 is the smallest to account for its small scale height of $z_L = 3$ kpc. Cosmic-ray electrons/positrons from close-by pulsars stay longer close of their source for smaller values of D_0 . That is most evident in Figure 3 with Geminga. The energy losses set the value of the cooling cut-off.

The observed cosmic-ray spectra by AMS-02 are affected by solar modulation. Cosmic rays have to travel through the Heliosphere before being recorded. During their propagation through the Heliosphere, cosmic rays diffuse through a fast evolving anisotropic magnetic field, experience drift effects and adiabatic losses. As a result their energy gets statistically shifted to lower values, described by the solar modulation potential Φ [153]. We use here the time-, charge- and rigidity-dependent formula for the solar modulation potential from [154], that has recently been further constrained in [155]. Our model for solar modulation requires as inputs the value of the total B-field of the Solar Wind at 1 AU, which we take from ACE [156], the tilt angle of the heliospheric current sheet that is modeled in Wilcox Solar Observatory [157] and the polarity of the Heliospheric magnetic field. In turn it gives us a value for the solar modulation potential that the kinetic energy of a particle of mass m, rigidity R and charge q was shifted by at a given Bartels' Rotation number. Our solar modulation model has two freeparameters ϕ_0 and ϕ_1 that we marginalize over within a range of values most recently constrained in [155]. For further details see [154, 155].

III. COSMIC-RAY DATA AND FITTING PROCEDURE

In this section we describe the observational data that we use to test our pulsars population models and the specifics of the fitting procedure that we follow. We account for uncertainties in the overall normalization of the pulsars' contribution, and for spectral and normalization uncertainties of other components in the electron and positron cosmic-ray spectra.

A. Observations of cosmic-ray electrons and positrons

We use the publicly available AMS-02 positron flux, the positron fraction and the $e^+ + e^-$ flux from [55, 56, 158]. Specifically for the $e^+ + e^-$ flux we rely on [56] instead of [55]. The analysis of [56] avoids charge sign identification and therefore results in a higher efficiency. For the $e^+ + e^-$ flux measurements we start at 10 GeV to avoid possible low energy systematics that may exist in comparing the AMS-02 measurement to that of DAMPE [159] or *CALET* [160]. For the positron flux and the positron fraction, we used the measurements at energies of 5 GeV or higher. At lower energies the pulsars' contribution is expected to be subdominant and mostly affected by pulsars several kpc away that we do not model. Moreover, the lower-energy e^{\pm} spectra are strongly affected by solar modulation that we account for, but also other propagation uncertainties as those of diffusive reacceleration and cosmic-ray convection in the ISM that we set to be present but do not further marginalize over.

Dataset	Acquisition Era	$\rm BR \ \#$	Ref.
$AMS-02 e^+$	5/2011 - 11/2017	2426 - 2514	[158]
AMS-02 $e^+/(e^- + e^+)$	5/2011 - 11/2017	2426 - 2514	[55]
$AMS-02 \ e^- + e^+$	5/2011 - 11/2017	2426 - 2514	[56]
$DAMPE \ e^- + e^+$	12/2015 - 6/2017	2488 - 2508	[159]
$CALET \ e^- + e^+$	10/2015 - 11/2017	2486 - 2515	[160]

TABLE III. The cosmic-ray measurements from AMS-02, DAMPE and CALET used in this analysis.

In addition, we perform fits ignoring the measurements below 15 GeV. At ~ 12 GeV there is a bump at the positron fraction that our simulations find it difficult to fit. We will come back to the matter of possible interpretations of this bump in section V. Finally, we use the $e^+ + e^-$ flux measurements from *DAMPE* [159] and *CALET* [160]. The used datasets with their respective data acquisition era and the corresponding Bartels' Rotation (BR) Numbers are presented in Table III.

B. Fitting

We allow for up to seven free parameters to be optimized in our simulations. Two solar modulation parameters ϕ_0 and ϕ_1 , three normalization factors a, b and cfor the primary cosmic-ray e^- flux, secondary cosmic-ray e^{\pm} fluxes and total pulsar e^{\pm} fluxes, and two spectral indices d_1 and d_2 responsible for hardening or softening the primary e^- and secondary e^{\pm} spectra by multiplying them with $(E/1 \text{ GeV})^{d_1}$ and $(E/100 \text{ GeV})^{d_2}$ respectively. We remind to the reader that the primary and secondary fluxes are already modeled to include specific energy losses, diffusion, diffusive re-acceleration, convection and ISM gas distribution assumptions. They also originate from a distribution model for all primary cosmic-ray sources. The additional normalizations (a, b) and spectral freedoms (d_1, d_2) are to account for uncertainties in the overall efficiency and number of the primary cosmicray sources, the total ISM gas density, the exact injection spectra of primary e^- spectra and cosmic-ray nuclei spectra that through their collisions give the secondary e^{\pm} . Neither of these freedoms breaks the consistency in the Milky Way propagation that we model. All cosmic-ray species for a given galactic ISM model of Table II experience the same propagation conditions. These four parameters merely account for the fact that we can not be certain of the original injected primary cosmic-ray electrons and cosmic-ray nuclei flux and spectra.

We fit each produced simulation to each dataset via a χ^2 minimization. While the AMS-02 measurements were acquired during the same era, we do not fit all the AMS-02 datasets simultaneously as they originate using different type of analysis cuts. Similarly, we do not try to fit simultaneously all $e^- + e^+$ measurements from the three different experiments, as some are in statistical tension with each other.

We first fit each simulation to the AMS-02 positron flux. Then, we focus on the realizations that can fit to the positron flux data within 2σ , 3σ or 5σ from an expectation of χ^2 of 1 for each degree of freedom (d.o.f.). For our fits of the the positron spectrum above 5 GeV there are 59 data points being fitted with five parameters. Thus, the 3σ and 5σ limits that we use translate to a χ^2 /d.o.f. of 1.337 and 1.683 respectively. Instead, for the positron spectrum in energies E > 15 GeV there are 44 data points. The relevant 2σ and 3σ limits we present translate to $\chi^2/d.o.f.$ of 1.290 and 1.467. In those fits we take ϕ_0 and ϕ_1 to be within [0.1, 0.6] GV and [0,2] GV respectively. Our range for the normalization b is [0.8, 2] and accounts for uncertainties in the normalizations of both the primary cosmic-ray nuclei fluxes and the ISM gas density. The parameter c is only given an upper bound such that $\bar{\eta} \ c \leq 0.5$ for each realization, while the parameter d_2 is within [-0.1, 0.1], where $d_2 = 0$ represents the original choice that comes from fitting the cosmic-ray primary nuclei [49]. The parameter d_2 is taken to have that narrow range as the dominant cosmic-ray primary hydrogen and helium are well measured [161–163].

We repeat the same fitting procedure with the AMS-02 positron fraction and $e^- + e^+$ flux; where for those we make use of all seven free parameters. We focus only on the simulations that are within the 2σ , 3σ or 5σ positron flux limits. For each of those simulations we take the best fit values of b, c that we got from the relevant positron flux fit and allow for up to a 50% additional variation ⁴. Parameters ϕ_0 , ϕ_1 are taken within the same ranges reported above as we consider these to be quite wide, while d_2 is fixed at its best fit value from the positron flux. Finally, the two newly introduced parameters aand d_1 relating to the primary e^- component take values within the range of [0.6, 1.2] and [-0.2, 0.5] respectively. The wider range of d_1 compared to d_2 , accounts for the fact that the electrons' injection sources properties that include pulsars which we study here, are less well understood compared to the primary cosmic-ray nuclei ones.

We report the simulations that can fit each of the AMS-02 data, i) within 2σ and 3σ for energies of E > 15 and ii) within 3σ and 5σ for $E \ge 5$ GeV for the positron flux and fraction and E > 10 for the total $e^- + e^+$ flux. We then compare the retained simulations from our E > 15fits to the DAMPE and CALET data. The DAMPE and CALET fits are performed in the same manner as the AMS-02 $e^+ + e^-$ flux.

When we fit the positron fraction in each energy bin we use counts instead of fluxes as AMS-02 uses binned data. At the highest energies some of our simulations may suggest the presence of multiple features within the same energy bin. Thus, we integrate the differential flux $d\Phi^{e^{\pm}}/dE$ over the energy range of each bin, and set a number of positron and electron events $N^{e^{\pm}}$ as,

$$N^{e^{\pm}} = \int_{E_{\min}}^{E_{\max}} \frac{d\Phi^{e^{\pm}}}{dE} dE, \qquad (8)$$

where E_{\min} , E_{\max} are the bounds of the bin. We note that $N^{e^{\pm}}$ is not the real event count in each bin as we don't know the exact exposure of the *AMS-02* detector. For any given energy bin assuming the exposure is roughly constant, ignoring it, is not an issue as the exposure cancels in taking the positron fraction ratio.

The positron fraction becomes,

$$\frac{bN_{e^+}^{sec} + cN_{e^+}^{pul}}{aN_{e^-}^{pri} + bN_{e^-}^{sec} + cN_{e^-}^{pul} + bN_{e^+}^{sec} + cN_{e^+}^{pul}}.$$
 (9)

The indices "pri", "sec", "pul" refer to the primary, secondary and pulsar fluxes respectively. We note that the factors $(E/1 \text{ GeV})^{d_1}$ and $(E/100 \text{ GeV})^{d_2}$ have been absorbed into their respective counts. For the positron flux or the $e^+ + e^-$ flux fits using "counts" is not possible as we do not know the exact exposures. Therefore we remain on working with fluxes.

Our minimization procedure uses SciPy's [164] least_ squares routine from the optimize module to solve our non-linear least squares problem. We also tried iMinuit [165] but found out that the least_squares achieves a good minimization much faster 5 .

IV. RESULTS

The first step in testing every Milky Way pulsars simulation is to fit its predicted positron flux in combination with a secondary positron flux component to the AMS-02 positron flux measurement, as shown for one model in Figure 1. The second step is to test that simulation against the positron fraction measurement and the $e^+ + e^-$ measurement (see Section III B for details). Our secondary and primary flux components are evaluated for the same diffusion and energy losses assumptions as the electrons and positrons fluxes originating from pulsars.

In Figure 4, we show the positron fraction spectra from different pulsars simulation assumptions. There is a clear feature that peaks around 12 GeV. A similar feature exists also in the positron flux. In presenting our results we break our discussion into two subsections. The first one (IVA) is focused on fitting only energies above 15

⁴ We always retain the hard limit of $\bar{\eta} c \leq 0.5$ that originates from equipartition of spin-down power to cosmic rays and B-field.

⁵ We noticed that the starting value for the parameter d_1 can cause the minimization in the positron fraction to fall into local minima. Therefore, we minimize each simulation several times, starting from different values for d_1 in its allowed range. In each minimization all the other parameters' starting values are chosen randomly within their allowed ranges as we found that their exact starting value doesn't cause any issues.



FIG. 4. The predicted positron fraction spectra for five different pulsar realizations along with the AMS-02 data. The χ^2 /d.o.f. of these pulsar models are also shown, evaluated at energies greater than 5 GeV. The zoomed part shows the spectrum around the bump that is centered at $\simeq 12$ GeV.

GeV avoiding the impact of a such a feature. Instead in Section IVB, we include the energies of 5 to 15 GeV in our fits.

Pulsar model I of Figure 4, represents the best fit in the positron fraction from energies 5 GeV and above. This same model gives a good fit at E > 15 GeV as well. Our simulations include enough physical variations that the predicted positron fraction spectrum, which increases from 7 to ~ 300 GeV can either keep rising at higher energies (model I), drop (model II,III,V) or flatten out (model IV). We also note that our allowed pulsars simulations can have a noticeable amount of features in them, something that can be searched for independently (see [123] for a detailed discussion).

In Figure 5, we depict the five $e^+ + e^-$ spectra for the same pulsar models (I through V). For model I, we plot the e^- and e^+ fluxes separately and the fluxes from some individual pulsars. These simulations can fit the AMS-02 positron and the $e^+ + e^-$ fluxes well and have $\chi^2/\text{d.o.f.} < 1$, with the exception of model V that has $\chi^2/\text{d.o.f.} = 1.51$ in its $e^+ + e^-$ fit. Similarly to what was shown in Figure 1 for the positrons, individual pulsars can give features in the higher energies of the electron spectrum and possibly explain features in the combined $e^+ + e^-$ spectrum.

A. Results for E > 15 GeV fits

1. Using only AMS-02 data

Of the 7272 astrophysical realizations, 2105 can fit the AMS-02 positron spectrum within 3σ from an expectation of χ^2 of 1 for each degree of freedom. Of these 2105 realizations, 567 (1095) can also fit within 2σ (3σ) the AMS-02 positron fraction spectrum and $e^+ + e^-$ spectrum.

For every Milky Way pulsars simulation we perform a



FIG. 5. The predicted $e^+ + e^-$ spectrum for the same five pulsar simulations of Figure 4, along with the *AMS-02* observation. For model I, we also show the individual electron and positron spectra and fluxes from individual pulsars.



FIG. 6. Examples of low-energy extrapolations on the e^{\pm} flux from a sample of Milky Way pulsars simulations. Normalizations are arbitrary and fluxes do not include the impact of solar modulation. For each original simulation (solid lines) we evaluate the power law before the break and then extrapolate to lower energies (dotted lines).

low-energy extrapolation. We show in Figure 6, examples of that. This extrapolation accounts for the fact that our simulations end at 4 kpc in distance from the Sun and at 10 Myr in age of pulsars. Through this extrapolation, more distant and older pulsars that would contribute at lower energies are included. The total number of Milky Way pulsars simulations that we fit and compare to the observations is thus 14544 (instead of just 7272 simulations). However, we note that simulations that can provide a good fit to the data both with and without their low-energy extrapolation, count only once in the list of simulations that are in agreement with the data.

The exact ISM conditions beyond 4 kpc are not simulated for the pulsars' electron/positron flux components. As the ISM properties gradually change we expect that there is increased modeling uncertainly at the lower energies and both options should be considered viable. Moreover, at low energies we include in our fits the impact of



FIG. 7. In each cell we show the fraction of pulsar population simulations that are consistent within 2σ to the AMS-02 positron fraction spectrum, the positron flux and the electron plus positron flux (see text for details) for the five choices of braking index $\kappa = 2.5, 2.75, 3.0, 3.25, 3.5$ and the twelve choices of ISM propagation conditions modeled by "A1" to "F3" (see Table II).



FIG. 8. Same as Figure 7, for the combination of the six choices ("BC", "AC", "BA", "AA", "BB" and "AB") of n and $g(\eta)$ and the twelve ISM models.

solar modulation with its uncertainties. This can further modify the fluxes' spectral properties at these low energies. We note that while lower birth rates result in small features at the lower energies, this does not affect our ability to perform that extrapolation. That can be seen in Figure 6, by comparing the blue vs black vs magenta lines that are for similar simulation assumptions, but with 2 vs 1 vs 0.6 pulsars/century birth rates respectively. The exact point where the low-energy extrapolation starts depends on the energy losses assumption. Lower energy losses (as the red line in Figure 6) result in a higher energy from which the extrapolation starts.

Our findings on the pulsar properties and the ISM conditions can be summarized in Figures 7, 8 and 9. We show in each cell the percentage of the pulsar population simulations that are consistent within 2σ to the AMS-02 positron fraction spectrum, the positron flux and electron plus positron flux. For instance, at the top left cell of Figure 7, the value of 2.1 refers to the percentage among the simulations with $\kappa = 2.5$, ISM model A1 assumptions, that are consistent with the AMS-02 data within 2σ .



FIG. 9. Similar to Figures 7 and 8, for the combination of the six choices of n and $g(\eta)$ and the five choices for braking index $\kappa = 2.5, 2.75, 3.0, 3.25, 3.5$.

In Figure 7, we show our results for the combination of the five choices of the braking index and the twelve choices of ISM propagation conditions. The choices of braking index $\kappa = 2.5$ and $\kappa = 2.75$ are clearly disfavored. Only a few realizations with these choices survive within 2σ . For $\kappa = 3.0$ and even more so for $\kappa = 3.25$ there is a significant increase on the fraction of simulations consistent to the data. Simulations with $\kappa = 3.5$ are favored as much as simulations with $\kappa = 3.0$. The preference for $\kappa \geq 3.0$ can also be seen in Figure 9. In Ref. [70], a first indication for a $\kappa > 3.0$ tendency was found. We now confirm this tendency with a much larger set of simulations, that account for even greater range of the relevant parameter space being modeled. For the ~ 10 young pulsars that we have reliable measurements of their braking index, typical values are $\kappa < 3$ [140, 141]. A higher value than 3.0 for the braking index, represents a slower spin-down (see Eq. 2) for middle aged and multi-Myr old pulsars. While the sample of young pulsars is still small, one solution between the results from electromagnetic observations and the results of this analysis is that pulsars may increase their braking as they age. As we rely on observations from radio waves and evolve the pulsars back in time to calculate their total power, a constant braking index of $\kappa < 3$, produces pulsars that initially were very powerful sources emitting very large amounts of cosmic-ray electrons and positrons. This increases the emission from the older pulsars compared to the younger ones.

As can be seen from both Figures 7 and 8 there is a small preference for the propagation models "A1, "C1", "E1" and "F1" which are for the more commonly used assumptions on the local cosmic-ray electrons and positron losses . Interestingly, practically 0% of our astrophysical realizations that have propagation model "E3" are consistent to the data. The "E3" simulations model low-energy losses and fast diffusion of high-energy cosmic rays. Also, models for a thin diffusion disk ("F1", "F2" and "F3") are disfavored. Thin disk ISM models make the cosmicray positrons even at low energies quite local and suppress the overall pulsars' contribution, making the combined spectrum from pulsars harder, something that is in tension to the observations.

In Figure 8, we present the results for the combination of the six choices for the injection index n and the energy conversion to cosmic rays $g(\eta)$ ("BC", "AC", "BA", "AA", "BB" and "AB") and the twelve ISM models. We clarify that there are three more choices ("CA", "CB" and "CC") for $n \in [1.3, 1.5]$ that are not shown here. These would be redundant rows in the table as none of the realizations with these choices are within our 2σ limit. The preferences on the ISM properties are there as we noted before. Regarding the index n described by the first letter ("A" or "B") along the rows, there a slight preference for the choice "B" which is for a narrow range of values for $n \in [1.6, 1.7]$ over the choice "A", which is for a wider range of $n \in [1.4, 1.9]$ (see Section IID for further details). The broader range for n (under choice "A") results in a more diverse pulsar population with respect to their injected cosmic-ray electrons and positrons. Therefore pulsars under assumption "A" have quite diverse spectra. The resulting combined pulsars' spectrum in turn has some very pronounced features associated with pulsars that have n closer to 1.4. Such a choice while not fully excluded is less preferable. Choice "C" which is fully excluded, assumed that all pulsars have values of $n \in [1.3, 1.5]$. This resulted in spectra with too many strong spectral features compared to what is observed in the AMS-02 data. Our results suggest that pulsars in the Milky Way most likely have a small range of values for their spectral index n with values of $n \simeq 1.6$.

In Figure 8, when comparing our results with respect to the choices of $g(\eta)$ (depicted by the second letter along the rows), we see a gradient going from our choice "C", to choice "A" and then to "B". Those are ranked from smaller to larger variance on the fraction of power η that goes to cosmic rays (see Section II D). Our results suggest that pulsars simulations with a greater homogeneity in the total spin-down power converted to cosmic rays are preferred. If pulsars had a very large range of η , then even among the older pulsars contributing at the lower energies, we would have a few of them standing out in their produced fluxes. Those pulsars would again give more spectral features than what is observed.

In Figure 9, we present our results for the combination of the six choices for n and $g(\eta)$, and the five choices for braking index. This figure, is given as a projection along that part of the simulations parameter space and very clearly shows the preferences for both $\kappa \geq 3.0$ and the choice "B", to the "A" for n.



FIG. 10. The predicted $e^+ + e^-$ spectra for seven different pulsar models along with their $\chi^2/d.o.f.$ One of the models (model IX in beige color) is excluded by the *DAMPE* data. This model greatly overshoots the data points above 1 TeV. Some fluxes (such as model VI and VIII) contain notable features at TeV energies from individual powerful pulsars.

2. Observations at TeV energies from DAMPE and CALET

The positron flux is measured by AMS-02 up to energies of 1 TeV. Two more experiments, DAMPE [166] and CALET [167] have published their measurements of the total $e^+ + e^-$ CR flux up to 5 TeV [159, 160]. At these energies the pulsars' contribution to the total measured fluxes can be very significant. The combination of volume and age necessary for pulsars to be able to contribute, is reduced at these higher energies. We can only probe the properties of the youngest and most energetic pulsars that are also close-by members of the population. Those are small in number. The result is an $e^+ + e^-$ flux rich in spectral features. Such spectra can be seen in Figures 10 and 11, where we show the predicted $e^+ + e^$ fluxes for some of our pulsars models. Above 1 TeV, the spectra can either have a cut-off, a change in their slope, or in some cases one or more prominent bumps from individual pulsars.

Fitting our simulations to the DAMPE $e^+ + e^-$ spectrum, we can further constrain the local Milky Way pulsars properties. Of the 567 (1095) realizations that were within $2\sigma(3\sigma)$ to all three AMS-02 datasets, 268 (771) are also consistent within $2\sigma(3\sigma)$ to the DAMPE $e^+ + e^$ data. DAMPE allows roughly three quarters of our models at the 3σ level and roughly half of our models at the 2σ level. We note that *DAMPE* excludes models in a uniform manner from the heat maps of Figures 7, 8 and 9. Thus, our conclusions on the averaged properties of pulsars and the local ISM do not change. One difference is that with DAMPE we find a small preference in retaining simulations with lower birth rates suggestive of the fact that smaller rates more easily produce spectral features as the ones seen in the DAMPE data. However, realizations that contain extremely powerful young and near-by pulsars can cause the $e^+ + e^-$ flux to over-



FIG. 11. Seven different predicted $e^+ + e^-$ fluxes from realizations that can fit the *CALET* data and their χ^2 /d.o.f.. Pulsar Model IX, which was excluded by *DAMPE* in Figure 10 can fit the *CALET* data very well. Prominent features are also visible at the highest energies from powerful pulsars (models VI, IX, XI and XII).

shoot the *DAMPE* data at the highest energies and are excluded. In Figure 10, we show the predicted $e^+ + e^-$ flux from six pulsar models that are consistent with the *DAMPE* measurement. We also show, the flux from one model (Pulsar Model IX) that is not consistent with the *DAMPE* data exactly due to the presence of very powerful pulsars at energies that *AMS-02* can not measure.

CALET's observations can not further constrain our astrophysical realizations. Of the 567 (1095) realizations that were consistent with all AMS-02 data at 2σ (3σ), only one is excluded by the CALET $e^+ + e^-$ flux. CALET has larger error bars compared to DAMPE. Almost all of our 1095 realizations that are within 3σ to the AMS-02 measurements, end up with $\chi^2/d.o.f. < 1$ fit to the CALET data. In Figure 11, we show seven different $e^+ + e^-$ fluxes from realizations that fit the CALET observation. Even our model IX, that was excluded by DAMPE with $\chi^2/d.o.f. = 4.96$, can fit the CALET data with $\chi^2/d.o.f. = 0.53$.

Finally, we use the fits to the DAMPE and CALET spectra in combination with the AMS-02 fits, to test the overall conversion efficiency η of pulsars' spin-down power to power in cosmic-ray electrons and positrons. In Figure 12, we show for the allowed pulsars simulations their fitted mean efficiency $\bar{\eta}$. We find that $\bar{\eta}$ is typically between 0.05 and 0.2. Due to equipartition of energy in the pulsar's environments, we do not allow for $\bar{\eta} > 0.5$ in our fits. This is also shown in Figure 12. There is only a small number of pulsar simulations with $\bar{\eta} < 0.01$. Recently, an independent analysis of [73] suggested a similar fraction of spin-down power to cosmic-ray electrons and positrons. We present the simulations that are within the 2σ criterion, but note that even if we used the larger number of simulations that are within 3σ , the results would not differ.



FIG. 12. The distribution of the fitted values for the averaged conversion efficiency $\bar{\eta}$ of pulsars' spin down power to cosmic rays. The y-axis shows the number of allowed Milky Way pulsars simulations within 2σ . Typical values for $\bar{\eta}$ are $\simeq 0.1$.

B. Results for $E \ge 5$ GeV fits

In this section we include the AMS-02 positron fraction and positron flux measurements down to energies of 5 GeV and discuss the relevant implications of the increased energy range. For the total $e^+ + e^-$ flux we still fit the data above 15 GeV. The presence of the feature at $\simeq 12$ GeV has an effect in the results of this section. Instead, in the discussion of Section IV A, we fitted energies E > 15 GeV, avoiding its impact on the Milky Way pulsar properties.

As we have discussed also in Section IVA, for each pulsars simulation, we consider a low energy extrapolation as well. We find that this low-energy extrapolation being included is more important than in Section IVA, where in fact for some ISM energy-loss assumptions the extrapolation starts at energies lower than 15 GeV. Even with the increased level of allowed low-energy flux uncertainty, many more simulations can be excluded by the data than in Section IVA. That is to be expected as the AMS-02 positron and electron fluxes at these energies have significantly smaller statistical errors. However, as we will show the presence of the feature around 12 GeV also has an impact. Including the positron fraction and positron flux measurements from 5 to 15 GeV, only a handful of Milky Way pulsars simulations are within 2σ agreement to the AMS-02 observations. For the remainder we focus on simulations that are within 3σ and 5σ from an expectation of χ^2 of 1 per degree of freedom, i.e. simulations that are not excluded within 3σ and 5σ . To demonstrate how more challenging it is to fit the AMS-02 data at E > 5 GeV compared to E > 15 GeV we include Figure 13. On the left part of that figure, we show the fraction of allowed simulations within 3σ from the fits to E > 15 GeV and on the right the equivalent fraction of allowed simulations within 3σ from the fits to $E \geq 5$ GeV. There is a dramatic decrease in the number of allowed simulations.

We test separately our simulations to each of the three



FIG. 13. Similarly to Figure 9, for given combination of pulsars' properties (each cell), we show the fraction of pulsar population simulations that are consistent within 3σ . On the left we have fitted the simulations to the AMS-02 observations from E > 15 GeV, and on the right to the AMS-02 observations from $E \ge 5$ GeV (see text for further details).

AMS-02 measurements and present results that are consistent with all three (for more details see Section III B). We find that of the 7272 astrophysical realizations, 2831 can fit the AMS-02 positron-flux spectrum within 5σ . Of these 2831 realizations, only 37 (261) can also fit within 3σ (5σ) the AMS-02 positron fraction spectrum and the $e^+ + e^-$ spectrum. The positron fraction has by far the greatest impact in excluding simulations ⁶.

We summarize in tables IV, V and VI the properties of the pulsars and the ISM needed to explain the AMS-02observations. For every cell, we show the percentage of the pulsars simulations that are consistent within 3σ and 5σ (in parentheses) to the AMS-02 data. For instance, in Table IV of the simulations with the combination of $\kappa = 3.0$ and ISM assumptions "A2", only 2% (15%) are consistent within 3σ (5σ) to the AMS-02 data.

In Table IV, we show our results for the combination of the five choices of the braking index and the twelve choices of ISM propagation conditions. There is a clear preference for the ISM models "A2", "C2", "E2" and "F2" that predict the highest energy losses $(b = 8.02 \times 10^{-6} \text{GeV}^{-1} \text{kyrs}^{-1}$ in Table II). That strong preference is mostly the result of a spectral feature at \simeq 12 GeV. The "A2", "C2", "E2" and "F2" without their low-energy extrapolation have a break close to that energy. We believe this feature likely suggests an additional source of positrons around 10-15 GeV, which may be a population of more distant pulsars closer to the inner spiral arm, around 5 kpc away from us. A second reason why low ISM energy losses models perform worse once including the 5-15 GeV data to our fits, is that these simulations predict fluxes that overshoot the observed

spectra at high energies.

Our finding from Section IVA for a preference of a braking index $\kappa \geq 3.0$ remains to be the case even with the lower energy observations. In Table IV, the choices $\kappa = 2.5$ and $\kappa = 2.75$ are almost entirely excluded (see also Table VI). Instead, for $\kappa = 3.0$ there is a significant increase in the percentage of simulations in agreement to the data, followed by an even higher percentage for $\kappa = 3.25$. For $\kappa = 3.5$ we find similar results as for $\kappa = 3.0$.

In Table V, we present as in Figure 8, our results for the combination of injection index n and $q(\eta)$ and the twelve ISM models. Our findings are similar to those presented in Section IVA, with the difference that now there are practically no simulations allowed with $n \in [1.4, 1.9]$ at 3σ (first letter "A" along the raws). Again the choices of "CA", "CB" and "CC" are not presented as only one simulation was found to be within 5σ to the data. Thus in our analysis, we can probe effectively the distribution properties of the injection index n. Yet, the stronger degeneracies on $q(\eta)$ are more difficult to further reduce with the lower energy data. At these low energies we observe the combined fluxes from thousands of pulsars and also the uncertainties associated with the cosmic-ray secondaries become prominent. We note that the similarity on the derived properties of n and $q(\eta)$ in the results of this section and Section IVA are to be expected. Varying the assumptions on n and $q(\eta)$ affects the shape and magnitude of spectral features appearing at high energies and not between 5 and 15 GeV.

In Table VI, we present for completeness our results for the combination of the six choices for n and $g(\eta)$, and the five choices for braking index. The preference for choice "B", followed by choice "A", for n that was described in the previous paragraphs is shown. Also the preference for braking index values $\kappa \geq 3$ is clear.

⁶ Just fitting the the positron fraction, we find only 50 (325) pulsars simulations to it within 3σ (5σ)

	A1	A2	A3	C1	C2	C3	E1	E2	E3	F1	F2	F3
	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)
$\kappa = 2.5$	0 (0)	0.8(4)	0(0)	0 (0)	0(0.8)	0(0)	0(0)	0.8(2)	0(0)	0(0)	0(2)	0 (0)
$\kappa = 2.75$	0 (0)	0(7)	0(0)	0(0)	1(3)	0(0)	0(1)	0(2)	0(0)	0(0)	1(6)	0(0)
$\kappa = 3.0$	0(1)	2(15)	0(0)	0(0)	2(11)	0(0)	0(0)	3(11)	0(0)	0(0)	0.4(4)	0(0)
$\kappa = 3.25$	0(1)	1(16)	0(0)	0(3)	6(18)	0(0)	0(1)	1(20)	0(0)	0(0)	2(10)	0(0)
$\kappa=3.5$	0 (0)	1(11)	0(0)	0(0)	3(15)	0(0)	0(0)	0.6(11)	0(0)	0(0)	0(8)	0(0)

TABLE IV. We show our results for the combination of the five choices of braking index $\kappa = 2.5, 2.75, 3.0, 3.25, 3.5$ and the twelve choices of ISM propagation conditions modeled by "A1" to "F3" (see Table II). We give the fraction of pulsar population simulations that are consistent within 3σ and 5σ limits (in parentheses) to the AMS-02 positron fraction spectrum, the positron flux and the electron+positron flux (see text for details). For the combination of $\kappa = 3$ and "C2" we produced 288 simulations to probe the remaining astrophysical parameters, of which 5 (31) i.e. $\simeq 2\%$ (11%) are allowed within 3σ (5σ).

		A1 (%)	A2 (%)	A3 (%)	C1 (%)	C2 (%)	C3 (%)	E1 (%)	E2 (%)	E3 (%)	F1 (%)	F2 (%)	F3 (%)
BC	$1.6 \le n \le 1.7, \zeta = 1.29$	0 (0)	3 (18)	0 (0)	0 (0)	3 (19)	0 (0)	0 (0)	0.8 (9)	0 (0)	0 (0)	2 (14)	0 (0)
AC	$1.4 \le n \le 1.9, \zeta = 1.29$	0(2)	0(13)	0(0)	0(0)	1(8)	0(0)	0(0)	1(4)	0(0)	0(0)	0(4)	0(0)
BA	$1.6 \le n \le 1.7, \zeta = 1.47$	0(0)	2(19)	0(0)	0(0)	5(15)	0(0)	0(0)	2(20)	0(0)	0(0)	2(6)	0(0)
AA	$1.4 \le n \le 1.9, \zeta = 1.47$	0(1)	0(10)	0(0)	0(0)	0(8)	0(0)	0(0)	0(10)	0(0)	0(0)	0(2)	0(0)
BB	$1.6 \le n \le 1.7, \zeta = 2.85$	0(0)	2(7)	0(0)	0(0)	3(13)	0(0)	0(2)	2(10)	0(0)	0(0)	0(4)	0(0)
AB	$ 1.4 \le n \le 1.9, \zeta = 2.85 $	0(0)	0(2)	0(0)	0(2)	0(2)	0(0)	0(0)	1(7)	0(0)	0(0)	0(1)	0(0)

TABLE V. As in Table IV, we present, for the combination of the six choices ("BC", "AC", "BA", "AA", "BB" and "AB") of n and $g(\eta)$ and the twelve ISM models, the % fraction of pulsar simulations that are consistent within the 3σ and 5σ limits (in parentheses) to the AMS-02 cosmic-ray data.

V. DISCUSSION AND CONCLUSIONS

In this paper we use recent cosmic-ray electron and positron observations from the AMS-02, DAMPE and CALET collaborations as a new handle to constrain the properties of Milky Way pulsars. Unlike electromagnetic spectrum observations that study individual objects, in our work we do not constrain the properties of any single pulsar. Instead, we constrain the properties of the general population of pulsars that can contribute to the observed cosmic-ray fluxes from 5 GeV up to 5 TeV. As the observed electron/positron cosmic-ray energy increases the volume of possible sources decreases. This makes our analysis restricted to a smaller fraction of the local ISM volume at the highest energies.

We created simulations of the Milky Way pulsars that lie within 4 kpc from the location of the Sun. We have performed over 72×10^2 Milky Way pulsars simulations to account for i) the stochastic nature of the neutron stars? birth distribution in space and time, and uncertainties on the pulsars' birth rate, ii) uncertainties on the initial spin-down power distribution that Milky Way pulsars follow, iii) different assumptions on the evolution with time of the pulsars' spin-down power, iv) different assumptions on the cosmic-ray electron and positron fluxes that pulsars inject into the ISM and v) uncertainties on the propagation of these cosmic rays through the ISM and the Heliosphere before they get detected. The range of model parameter values that we explore is wide and varying among different assumptions can significantly affect the observed electron and positron fluxes as shown in Figures 2 and 3. Each of our Milky Way pulsars simulations contains from 5×10^3 to 19×10^3 unique pulsars with ages up to 10 Myr, depending on the exact birth rate assumption. Within a given simulation, each pulsar has a unique location, age, initial spin-down power and spectral index of injected cosmic rays.

In performing our fits to the AMS-02, DAMPE and CALET flux observations, we account also for the existence of cosmic-ray primary electrons from SNRs and secondary electrons and positrons produced in inelastic collisions taking place in the ISM. We also account for those fluxes' respective uncertainties. Examples of our fits are given in Figures 1, 4, 5, 10 and 11.

We find a strong preference for pulsars models with a spin-down braking index of $\kappa \geq 3.0$ (see Eq. 2 and Figures 7, 9 and 13). Such a result is in contrast to observations of the about ten young pulsars, for which a reliable measurement of $\kappa < 3.0$ has been made (with the exception of one [141]). As our analysis tests the averaged properties of much older pulsars than the electromagnetic measurements do, our results show that pulsars' braking index evolves with time to larger values. This results in older pulsars losing their rotational energy at a slower manner than that predicted from the regular magnetic dipole radiation. Our results show a new way of studying the evolution of pulsars. With higher statistics in the future we expect that specific models on the pulsars' braking index evolution with time can be tested.

Furthermore, we find that pulsars inject into the ISM electrons and positrons with relatively similar cosmic-ray spectra that scale roughly as $dN/dE \propto E^{-1.6}$ up to O(10) TeV. Also, pulsars convert O(10%) of their rotational energy into such cosmic rays (see Figure 12). Our conclu-

		$\kappa = 2.5$	$\kappa = 2.75$	$\kappa = 3.0$	$\kappa = 3.25$	$\kappa = 3.5$
		(%)	(%)	(%)	(%)	(%)
BC	$1.6 \le n \le 1.7, \zeta = 1.29$	0(1)	0.6(3)	1(8)	2(10)	1(8)
AC	$1.4 \le n \le 1.9, \zeta = 1.29$	0.5(1)	0(1)	0(4)	0(2)	0.5(3)
BA	$1.6 \le n \le 1.7, \zeta = 1.47$	0.4(3)	0.6(4)	2(7)	2(12)	0.4(7)
$\mathbf{A}\mathbf{A}$	$1.4 \le n \le 1.9, \zeta = 1.47$	0 (0)	0(0.7)	0(4)	0(8)	0(0.9)
BB	$1.6 \le n \le 1.7, \zeta = 2.85$	0 (0)	0(2)	1(4)	1(4)	1(8)
AB	$1.4 \le n \le 1.9, \zeta = 2.85$	0 (0)	0(0)	0.3(2)	0(2)	0(2)

TABLE VI. Similar to the slices in parameter space given in Tables IV and V, we show for the combination of the six choices of n and $g(\eta)$ and the five choices for braking index $\kappa = 2.5, 2.75, 3.0, 3.25, 3.5$, the % fraction of pulsar population simulations that are consistent within 3σ and 5σ to the AMS-02 cosmic-ray data.

sions are fairly robust to the exact birth rate of Milky Way pulsars and the exact local ISM assumptions. We still find a preference for larger pulsar birth rates and thicker diffusion zone ISM models.

Finally, when studying the lower energies we noticed that the AMS-02 positron measurements give a spectral feature at $\simeq 12$ GeV. While some of our simulations can explain such a feature, its presence likely suggests a population of positron sources outside the volume of study, or of an entirely different origin. We leave the possible origin of such a feature to future studies.

We have made publicly available our Milky Way pulsars simulations in their pre-fitted format for the entire set. We have also provided the fitted fluxes from simulations that are in agreement with the AMS-02, CALET and DAMPE observations. These files can be found at https://zenodo.org/record/5659004#.YYqnbi-ZNOs.

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