

CHCRUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

Near future MeV telescopes can discover asteroid-mass primordial black hole dark matter Anupam Ray, Ranjan Laha, Julian B. Muñoz, and Regina Caputo Phys. Rev. D **104**, 023516 — Published 15 July 2021

DOI: 10.1103/PhysRevD.104.023516

Closing the gap: Near future MeV telescopes can discover asteroid-mass primordial black hole dark matter

Anupam Ray ^(b), ^{1, a} Ranjan Laha ^(b), ^{2, b} Julian B. Muñoz ^(b), ^{3, c} and Regina Caputo ^(b), ^{4, d}

¹ Tata Institute of Fundamental Research, Homi Bhabha Road, Mumbai 400005, India

²Centre for High Energy Physics, Indian Institute of Science, C. V. Raman Avenue, Bengaluru 560012, India

³Harvard-Smithsonian Center for Astrophysics, 60 Garden St., Cambridge, MA 02138, USA

⁴NASA Goddard Space Flight Center, Greenbelt, MD 20771, USA

Primordial black holes (PBHs), formed out of large overdensities in the early Universe, are a viable dark matter (DM) candidate over a broad range of masses. Ultra-light, asteroid-mass PBHs with masses around 10^{17} g are particularly interesting as current observations allow them to constitute the entire DM density. PBHs in this mass range emit ~ MeV photons via Hawking radiation which can directly be detected by the gamma ray telescopes, such as the upcoming AMEGO. In this work we forecast how well an instrument with the sensitivity of AMEGO will be able to detect, or rule out, PBHs as a DM candidate, by searching for their evaporating signature when marginalizing over the Galactic and extra-Galactic gamma-ray backgrounds. We find that an instrument with the sensitivity of AMEGO could exclude non-rotating PBHs as the only DM component for masses up to 7×10^{17} g at 95% confidence level (C.L.) for a monochromatic mass distribution, improving upon current bounds by nearly an order of magnitude. The forecasted constraints are more stringent for PBHs that have rotation, or which follow extended mass distributions.

I. INTRODUCTION

Unequivocal evidence of a non-baryonic form of matter, known as dark matter (DM), as a dominant component of the Universe has been confirmed by numerous astrophysical and cosmological observations [1–3]. Experimental searches for the elusive DM have thus far shown no firmly preferred model [4–6]. Primordial black holes (PBHs), possibly formed via gravitational collapse of large overdensities in the early universe or via other exotic mechanisms, are one of the earliest proposed and well-motivated DM candidates [7–10]. PBHs have a wide range of masses and can constitute a large fraction or even the entirety of the DM density [11-17]. The idea of PBH DM has recently received renewed attention with the first detection of a BH merger by the LIGO-Virgo collaboration [18], argued to have a PBH rather than astrophysical origin [19–21]. Several techniques have been implemented to probe the DM fraction of PBHs over a wide mass range. These have resulted in a multitude of observational constraints [13, 14, 22–57], along with several future projections [11, 29, 58–72] along a broad range of PBH masses.

Due to their Hawking emission, extremely light PBHs would have evaporated by today, setting a lower limit on the mass of ~ 5×10^{14} g for non-rotating PBHs (or ~ 7×10^{14} g if maximally rotating) [73–75]. PBHs heavier than that still evaporate, and act as decaying DM. Ultra-light PBHs with masses in between 5×10^{14} g – 2×10^{17} g, are typically probed via searches of their

Hawking radiation. Non-observations of such Hawkingproduced photons [22, 29, 30, 56], neutrinos [14], and electrons/positrons [14, 26–28, 76–79] provide the leading constraints on ultra-light PBHs. Additional constraints in this mass range are also obtained via precise observations of the cosmic microwave background and Big Bang Nucleosynthesis [23, 80–82]. PBHs in the mass range of ~ 2×10^{17} g -10^{23} g, often known as the asteroidmass range¹, are currently allowed to compose the entirety of the DM [11–13]. Unlike solar-mass BHs, these ultra-light BHs cannot be produced by any known astrophysical processes (even with the continued accumulation of asymmetric DM particles in compact objects [83, 84]), and thus would be a smoking gun of new physics, be it during the early Universe or in a complex dark sector [85].

In this work, we propose a technique to decisively probe a part of the parameter space for PBH DM in the asteroid-mass range. We show that observation of the Galactic Center by future MeV telescopes, such as an instrument with the sensitivity of AMEGO [86], can probe the DM fraction of asteroid-mass PBHs. AMEGO can exclude non-rotating (maximally rotating) PBHs as the sole component of DM up to $\sim 7 \times 10^{17}$ g ($\sim 4 \times 10^{18}$ g), at 95% C.L., assuming no signal is present in the data and a monochromatic mass function of PBHs. Assuming that PBHs follow an extended mass distribution (log-normal distribution with width $\sigma = 0.5$), AMEGO can probe further into an entirely unexplored mass window, improving our current constraints by nearly an order of magnitude and pushing us closer to probe the entire asteroidmass PBH window. Ref. [56], which appeared as our paper was near completion, performs a similar study for non-rotating PBHs with a monochromatic mass distri-

^a anupam.ray@theory.tifr.res.in

^b ranjanlaha@iisc.ac.in

 $^{^{\}rm c}$ julianmunoz@cfa.harvard.edu

^d regina.caputo@nasa.gov

¹ https://nssdc.gsfc.nasa.gov/planetary/factsheet/asteroidfact.html

bution. Our work differs from Ref. [56] in several key aspects (e.g., the inclusion of the extra-Galactic astrophysical background, and a different region of interest in the Galactic Center), chief among them is our usage of Fisher analysis to derive the projected exclusion limits on the DM fraction of ultra-light PBHs including marginalization over the astrophysical parameters.

II. PARTICLE EMISSION FROM EVAPORATING BLACK HOLES

BHs evaporate via Hawking radiation [8]. An uncharged and rotating BH of mass $M_{\rm BH}$ and angular momentum $J_{\rm BH}$ radiates at a temperature [73–75, 87, 88]

$$T_{\rm BH} = \frac{1}{4\pi G_N M_{\rm BH}} \frac{\sqrt{1 - a_*^2}}{1 + \sqrt{1 - a_*^2}}, \qquad (1)$$

where G_N denotes the gravitational constant and $a_* = J_{\rm BH}/(G_N M_{\rm BH}^2)$ is the dimensionless spin parameter. For a given BH mass, the temperature can vary by orders of magnitude as it approaches its maximal spin, $a_* \to 1$, where the BH stops evaporating.

The number of emitted particles from an evaporating BH of mass $M_{\rm BH}$ and dimensionless spin parameter a_* , in the energy interval E and E+dE and in a time interval dt follows a blackbody-like distribution [8, 73–75, 87, 88]

$$\frac{d^2 N}{dEdt} = \frac{1}{2\pi} \frac{\Gamma_s(E, M_{\rm BH}, a_*, \mu)}{\exp\left[E'/T_{\rm BH}\right] - (-1)^{2s}},$$
(2)

where E' denotes the effective energy of the emitted particles including the rotational velocity of the BH. Γ_s denotes the graybody factor which accounts for the departure from an ideal blackbody emission. It depends on the spin of the emitted particle s, rest mass of the emitted particle μ , and the BH mass and spin. In the high energy limit, $G_N M_{\rm BH} E \gg 1$, the graybody factor becomes independent of the spin of the emitted particle species and reaches its geometric saturation value, i.e. $\Gamma_s =$ $27G_N^2 M_{\rm BH}^2 E^2$. In the opposite limit, $G_N M_{\rm BH} E \ll 1$, it strongly depends on the spin of the emitted particle species [73, 87].

For this work, we use the publicly available BlackHawk [89] package to generate the emitted particle spectrum from evaporating BHs. We have verified this numerically obtained emission rate against semi-analytical formulae from Ref. [73, 74, 87].

III. METHODS & RESULTS

Hereafter we focus on primordial black holes. Ultralight PBHs emit significant number of photons of energy comparable to their temperature. More precisely, photon emission peaks at an energy $E \sim 5.77 T_{\text{PBH}}$ [75, 87] for an evaporating PBH with temperature T_{PBH} . The emission of photons is exponentially suppressed for energies exceeding T_{PBH} ($E \gg T_{\text{PBH}}$), and falls off as a power law in the opposite limit ($E \ll T_{\text{PBH}}$).

For a monochromatic mass distribution of PBHs, the Galactic contribution to the differential flux from PBH evaporation is

$$\frac{d\phi_{\text{gal}}}{dE}\Big|_{\text{mono}} = \frac{f_{\text{PBH}}}{4\pi M_{\text{PBH}}} \frac{d^2 N}{dEdt} \int_0^{s_{\text{max}}} \rho\left[r(s,l,b)\right] ds \, d\Omega \,, \tag{3}$$

where f_{PBH} denotes the DM fraction of PBHs. DM profile of the Milky Way (MW) is denoted by $\rho [r(s, l, b)]$, where r is the Galacto-centric distance, s is the distance from the observer, l and b denote the Galactic longitude and latitude respectively, and $d\Omega = \cos[b] dl db$ is the differential solid angle under consideration. The upper limit of the line of sight integral, s_{max} , depends on the size of the MW DM halo, Galactic longitude, and Galactic latitude:

$$s_{\max} = r_{\odot} \cos[b] \cos[l] + \sqrt{r_{\max}^2 - r_{\odot}^2 \left(1 - \cos^2[b] \cos^2[l]\right)}$$
(4)

where $r_{\rm max}$ denotes the maximum size of the MW halo, and r_{\odot} is the Galacto-centric distance of the Sun.

The extra-Galactic contribution to the differential flux for a monochromatic mass distribution of PBHs is

$$\frac{d\phi_{\rm eg}}{dE}\Big|_{\rm mono} = \frac{\Delta\Omega}{4\pi} \frac{f_{\rm PBH} \,\rho_{\rm DM}}{M_{\rm PBH}} \int_{z=0}^{\infty} \frac{dz}{H(z)} \, \frac{d^2N}{dEdt}\Big|_{E\to[1+z]E},\tag{5}$$

where $\Delta\Omega$ denotes the total solid angle under consideration, $\rho_{\rm DM}$ is the average DM density of the Universe at the present epoch, and H(z) = $H_0 \sqrt{\Omega_{\Lambda} + \Omega_m (1+z)^3 + \Omega_r (1+z)^4}$ is the Hubble expansion rate at redshift z. The Hubble expansion rate at the present epoch is H_0 ; Ω_{Λ} , Ω_m , and Ω_r denote the current dark-energy, matter, and radiation densities of the Universe, respectively. For numerical values of all cosmological parameters, we use the latest Planck 2018 measurements [1].

In addition to a monochromatic mass distribution for PBHs, we also consider a log-normal mass distribution, as predicted by various inflationary models

$$\frac{dN_{\rm PBH}}{dM_{\rm PBH}} = \frac{1}{\sqrt{2\pi\sigma}M_{\rm PBH}} \exp\left[-\frac{\ln^2\left(M_{\rm PBH}/\mu_{\rm PBH}\right)}{2\sigma^2}\right],\tag{6}$$

where $\mu_{\rm PBH}$ and σ are the mean mass and width of the distribution. For an extended mass distribution of PBHs, the (extra-)Galactic contribution to the differential flux is

$$\frac{d\phi_{\rm gal,eg}}{dE}\Big|_{\rm ext} = \int dM_{\rm PBH} \frac{dN_{\rm PBH}}{dM_{\rm PBH}} \frac{d\phi_{\rm gal,eg}}{dE}\Big|_{\rm mono}.$$
 (7)

For non-rotating PBHs, the mass integral runs from $M_{\rm min} = 5 \times 10^{14}$ g to $M_{\rm max} = \infty$. For PBHs approaching to their maximal rotation, the mass integral runs from

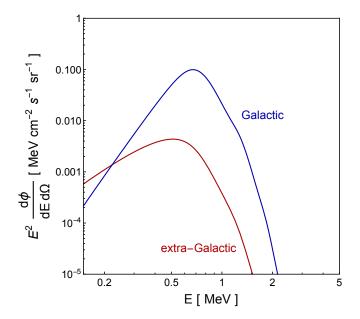


FIG. 1. The Galactic and extra-Galactic photon contributions from Hawking evaporation off a non-rotating PBHs of mass 10^{17} g. It is assumed that PBHs make up the entirety of DM and follow an NFW density profile. The blue and red lines correspond to the Galactic and extra-Galactic contributions in the region of interest ($|l| \leq 5 \deg$ and $|b| \leq 5 \deg$) respectively.

 $M_{\rm min} = 7 \times 10^{14}$ g to $M_{\rm max} = \infty$, as the maximal rotation increases the minimum evaporation mass $M_{\rm min}$ by enhancing the Hawking emission rate. Note that, the minimum PBH mass only matters for extended PBH distributions with low averages.

Fig. 1 shows the Galactic and extra-Galactic contributions to the total evaporation flux from PBHs of mass 10^{17} g in Galactic Center, defined to have: $|l| \leq 5 \text{ deg}$ and $|b| \leq 5 \text{ deg}$. Since this region of interest resides in a DM-dominated environment, the extra-Galactic contribution to the evaporation signal is always subdominant. Galactic emission peaks at around ~ 0.6 MeV as the temperature of a 10^{17} g PBH is 0.1 MeV. The extra-Galactic signal peaks at a slightly lower energy as it is redshifted.

Of course, PBHs are not the only possible source of gamma-rays in the cosmos. In particular, there are well-known astrophysical backgrounds, which we ought to marginalize over to unearth a possible PBH signal. Fig. 2 shows the Galactic and extra-Galactic astrophysical backgrounds used in this analysis. We have adapted the Galactic astrophysical background $\phi_{\text{gal}}^{\text{bkg}}$ from Ref. [90]:

$$\phi_{\rm gal}^{\rm bkg}(E) = A_{\rm bkg} \left(\frac{E}{1\,{\rm MeV}}\right)^{-\alpha} \exp\left[-\left(\frac{E}{E_c}\right)^{\gamma}\right], \quad (8)$$

in units of MeV⁻¹ cm⁻² s⁻¹sr⁻¹, which contains four parameters: an amplitude $(A_{\rm bkg})$, power-law index (α) , exponential cut-off energy (E_c) , and the index within the exponential (γ) . Their best fit values are $A_{\rm bkg} =$

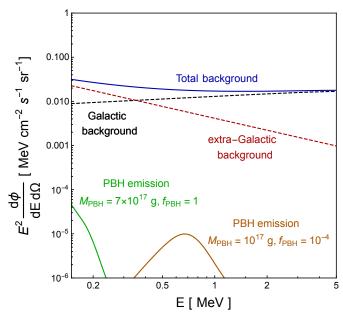


FIG. 2. Galactic and extra-Galactic astrophysical backgrounds are shown as a function of the emitted photon energy. Dashed black line corresponds to the Galactic background which is adapted from Ref. [90]. Dashed red line corresponds to the extra-Galactic background which is a single power law fit to the Cosmic X-ray background measurements. Total background, sum of the Galactic and extra-Galactic backgrounds, is shown by the solid blue line. Evaporation signals from non-rotating PBHs of mass 10^{17} g with dark matter fraction of 10^{-4} and a non-rotating PBH of mass 7×10^{17} g with dark matter fraction of unity are shown for comparison.

 $0.013 \,\mathrm{MeV}^{-1} \,\mathrm{cm}^{-2} \,\mathrm{s}^{-1} \mathrm{sr}^{-1}$, $\alpha = 1.8$, $E_c = 20 \,\mathrm{MeV}$, and $\gamma = 2$, respectively. We have checked that this formula provides an adequate fit to the data obtained by COMP-TEL [93–95]. For the extra-Galactic background, $\phi_{\mathrm{eg}}^{\mathrm{bkg}}$, we have considered a single power law which fits the cosmic X-ray background spectrum measured by various experiments [96–100] in the energy range 150 keV to 5 MeV [29]:

$$\phi_{\rm eg}^{\rm bkg}(E) = A_{\rm bkg}^{\rm eg} \left(\frac{E}{1\,{\rm MeV}}\right)^{-\alpha^{\rm eg}} \tag{9}$$

also in MeV⁻¹ cm⁻² s⁻¹sr⁻¹. Our power-law model for the extra-Galactic background contains two parameters, its amplitude $(A_{\rm bkg}^{\rm eg})$, and the power law index $(\alpha^{\rm eg})$, with best-fit values of $A_{\rm bkg}^{\rm eg} = 0.004135 \,{\rm MeV^{-1} \, cm^{-2} \, s^{-1} sr^{-1}}$, and $\alpha^{\rm eg} = 2.8956$.

We consider photons in the energy range 0.15-5 MeV for this analysis. The lower end of the energy range is determined by the sensitivity of AMEGO, whereas, the higher end of the energy range is determined by the evaporation signal. For PBHs of mass 2×10^{16} g (minimum mass considered for this analysis), evaporation signal peaks at around 3 MeV, and falls off exponentially with increase in photon energy. Moreover, the single

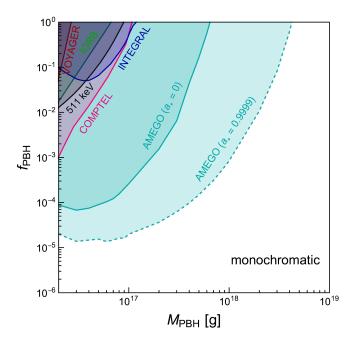


FIG. 3. Projected upper limit (95% C.L.) on the DM fraction of PBHs, f_{PBH} , from near future MeV telescope AMEGO. The plot corresponds to a monochromatic mass distribution of PBHs. Results for non-rotating PBHs $(a_* = 0)$ and PBHs approaching to their maximal spin $(a_* = 0.9999)$ are shown by the solid line and the dashed line respectively. The constraints are derived by considering an NFW density profile of the ultra-light PBHs. The existing exclusions on ultra-light nonspinning PBHs from Voyager-1 measurement of positron flux (shaded red) [26], extra-Galactic gamma ray emission(shaded green) [22, 29, 91], SPI/INTEGRAL 511 keV emission line with 1.5 kpc positron annihilation region & isothermal DM profile (shaded black) [14, 27, 28] and INTEGRAL, COMP-TEL Galactic Center MeV flux (shaded blue, shaded magenta) [30, 56] are also shown for comparison. For reference, there are no existing exclusion limits to the right of the plot until $M_{\rm PBH} \sim 10^{23}$ g [11–13, 92].

power-law fit to the extra-Galactic background in Eq.(9) is valid only up to ~ 5 MeV [29].

We have applied Fisher forecasting [101–103] with marginalization over all astrophysical background parameters to compute the projected upper limits at 95% C.L. The exclusion limits are derived by assuming no evaporation signal is present in the data. The Fisher information matrix (\mathcal{F}) is a $N \times N$ matrix, where N denotes the total number of parameters $\vec{p} = \{p_1, p_2, ..., p_N\}$ and is defined as [90]

$$\mathcal{F}_{ij} = \int_E \int_\Omega \frac{\partial_i \phi(E,\Omega) \,\partial_j \phi(E,\Omega)}{\phi(E,\Omega)} \,T_{\rm obs} \,A_{\rm eff}(E) \,d\Omega \,dE \,, \tag{10}$$

where $\phi(E, \Omega) = \left(\phi_{\text{gal}} + \phi_{\text{eg}} + \phi_{\text{gal}}^{\text{bkg}} + \phi_{\text{eg}}^{\text{bkg}}\right)$ is the total flux, T_{obs} is the observation time, and $A_{\text{eff}}(E)$ is the effective area. We conservatively ignore the extra-Galactic PBH emission, as it is subdominant in our region of interest. The effective area for AMEGO is adapted from

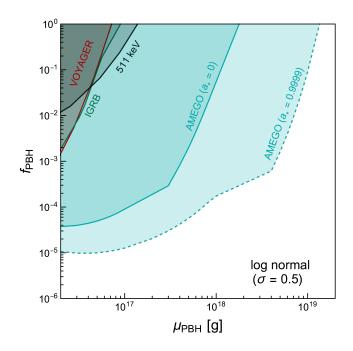


FIG. 4. Projected upper limit (95% C.L.) on the DM fraction of PBHs, $f_{\rm PBH}$, from near future MeV telescope AMEGO. Log-normal mass distribution with a width $\sigma = 0.5$ is considered in this plot. Results for non-rotating PBHs ($a_* = 0$) and maximally rotating PBHs ($a_* = 0.9999$) are shown by the solid line and the dashed line respectively. The constraints are derived by considering an NFW density profile of the ultra-light PBHs. The existing constraints on ultra-light nonspinning PBHs from Voyager-1 measurement of positron flux (shaded red) [26], extra-Galactic gamma ray emission(shaded green) [22, 29, 91], and SPI/INTEGRAL 511 keV emission line with 1.5 kpc positron annihilation region & isothermal DM profile (shaded black) [14, 27, 28] are also shown for comparison.

Ref. [86]² and a uniform sky coverage $T_{\rm obs}$ of 1 year is considered for this analysis. We use a sufficiently dense binning in order to capture all the spectral variations in the Fisher information matrix. We have considered 2000 logarithmically spaced bins between the energy interval of 0.15 - 5 MeV.

For this work, there is only one signal parameter, the fraction $f_{\rm PBH}$ of the DM that is composed of PBHs for each mass we study, plus the 6 astrophysical parameters introduced in Eqs. (8) and (9). Hence, the Fisher information matrix (\mathcal{F}) used in our analysis is a 7 × 7 symmetric matrix. The projected upper limit on the signal parameter $f_{\rm PBH}$ at 95% C.L. is [90]

$$f_{\rm PBH}^{\rm UL} = 1.645 \sqrt{\left(\mathcal{F}^{-1}\right)_{11}}$$
. (11)

Because of the relatively large region of interest, our results are almost insensitive to different choices of DM

² https://asd.gsfc.nasa.gov/amego/technical.html

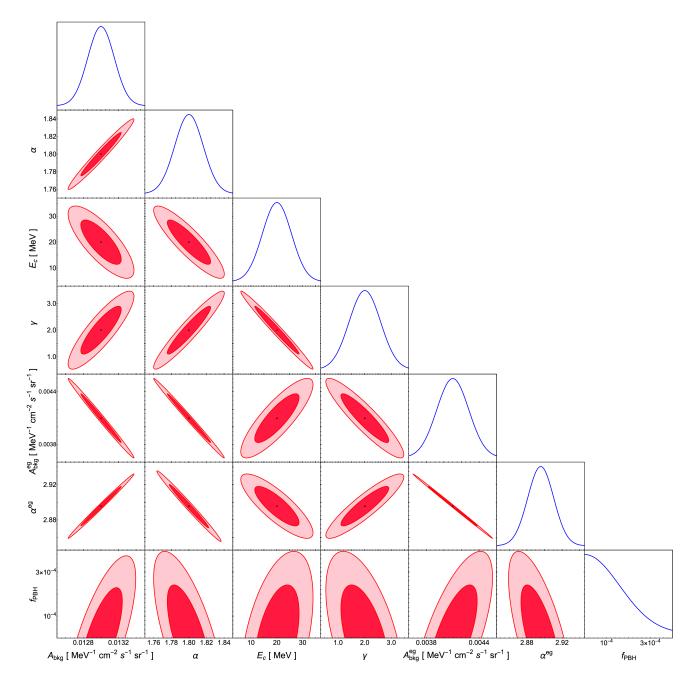


FIG. 5. Confidence ellipses at 68.3% C.L. (1- σ , dark red) and 95% C.L. (2- σ , light red) for all background and signal parameters. A larger correlation between parameters appears as a more tilted confidence ellipse. For this corner plot we have assumed non-rotating and uncharged PBHs with a monochromatic mass distribution centered at 10¹⁷ g, following a NFW density profile. Black dots represent best-fit (i.e., our chosen fiducial) values of the background parameters, and we assume a fiducial $f_{PBH} = 0$. The predicted posteriors for all parameters are shown by the Gaussian curves in blue.

density profiles. For this work, we assume that the density distribution of ultra-light PBHs in MW halo follows a Navarro-Frenk-White (NFW) profile [104]. However, we have tested our results with other density profiles such as with a cored isothermal profile [105] and with a cored NFW profile with a core radii of 2 kpc [30]. We find that due to the different choices of DM density profiles, our results alter by as far as a factor of two (degrades by a factor of ~ 1.69 for a cored isothermal profile and by a factor of ~ 1.55 for a cored NFW profile with a core radii of 2 kpc). We have also checked that a somewhat larger region of interest around the Galactic Center, say $|l| \leq 30 \deg$ and

 $|b| \leq 10 \text{ deg}$, increases the Hawking evaporated photons as well as background photons by a factor of 6.81 and 12 respectively, indicating a putative improvement of the projections by a factor of $(S/\sqrt{N}) \sim 1.96$ (which, however, may be reduced by marginalization with the Fisher matrix).

Fig. 3 shows the projected upper limits (at 95% C.L.) on DM fraction of PBHs, f_{PBH} , that can be derived from future AMEGO observations by assuming that no DM signal is present in the data. Monochromatic mass distribution of the PBHs is assumed in this plot. The solid/dashed lines correspond to non-rotating $(a_* =$ 0)/approaching maximal rotation ($a_* = 0.9999$) PBHs. Note that, we take the maximum value of spin as 0.9999 because BlackHawk can not go beyond that. The limits are derived by assuming an NFW density profile of the PBHs. As the PBHs become maximally rotating, their temperatures as well as the effective energy of the emitted photons fall off rapidly, and as a result maximally rotating PBHs probe higher mass window than their non-spinning counterparts. Because of the lower energy reach and larger effective area, AMEGO is able to probe into asteroid-mass windows compared to the previous gamma-ray observatories such as INTEGRAL [106], Fermi [107], and CRGO [108] for both non-rotating and maximally rotating PBHs. The projected upper limit from AMEGO excludes non-rotating (maximally rotating, $a_* = 0.9999$) PBHs as the sole component of DM upto 7×10^{17} g (4 × 10¹⁸ g). The kinks in the exclusion limits for both non-rotating and maximally rotating PBHs are due to finite number of mass point samplings. Our exclusion limits start from 2×10^{16} g as lighter PBHs mostly evaporate to higher-energy photons, outside of our considered energy range. Quantitatively, for a nonrotating PBH of mass 10^{16} g (2×10¹⁶ g), ~ 30% (~ 97%) of the evaporation spectrum resides in our considered energy interval, explaining the choice of 2×10^{16} g as the minimum PBH mass for this analysis.

Fig. 4 shows the projected upper limits (95% C.L.) on DM fraction of PBHs, f_{PBH} , that can be derived from future MeV telescope AMEGO by assuming no signal present in the data for an extended mass distribution. Log-normal mass distribution of PBHs, a motivated scenario from several inflationary models, with a width of $\sigma = 0.5$ is considered to derive the exclusion limits. The density profile of PBHs are assumed to be NFW. however, the result degrades by at most a factor of two for cored density profiles. The solid (dashed) lines correspond to non-rotating (maximally rotating) PBHs. For this particular mass distribution, our projections exclude upto $\sim 2 \times 10^{18}$ g ($\sim 10^{19}$ g) for non-rotating (approaching maximal rotation $a_* = 0.9999$) PBHs. Similar to the monochromatic mass distributions, here also, AMEGO probes better than other proposed MeV telescopes because of its lower energy reach and larger effective area. Similar to Fig.3, here also, the kinks in the exclusion limits at around 3×10^{17} g for non-rotating PBHs, and at $\sim 3 \times 10^{18}$ g for maximally rotating PBHs are due to

finite number of mass point samplings.

Fig. 5 shows the confidence ellipses at 68.3% C.L. and 95% C.L. for all signal and background parameters. Nonrotating PBHs with a monochromatic mass distribution centered at 10^{17} g and an NFW density profile is assumed for this figure. The confidence ellipses show degeneracies among all of the parameters and the parameters of the ellipses are computed from [109]. For example, amplitude of the Galactic background (A_{bkg}) , amplitude of the extra-Galactic background (A_{bkg}^{eg}) , and the exponential cutoff energy for the Galactic background (E_{cut}) are correlated with the signal parameter, DM fraction of PBHs $(f_{\rm PBH})$. However, power law index of the Galactic background (α) , power law index of the extra-Galactic background (α^{eg}) , and index of the exponential cutoff energy in the Galactic background (γ) are anti-correlated with $f_{\rm PBH}$. From the confidence ellipses, it is also evident that the correlation coefficient $r_{ij} (= \mathcal{F}_{ij}^{-1} / \sqrt{\mathcal{F}_{ii}^{-1} \mathcal{F}_{jj}^{-1}})$ between $A_{\rm bkg}^{\rm eg}$ and $f_{\rm PBH}$ (r = 0.697) is much stronger than the correlation between E_{cut} and f_{PBH} (r = 0.468). In Fig. 5, we also show the best fit values of all background parameters as well as their corresponding error bars by the mean and variance of the blue Gaussian curves.

IV. SUMMARY AND CONCLUSIONS

PBHs in the asteroid-mass range, $\sim 10^{17} - 10^{23}$ g, can make up the entire DM density and it is very important to conclusively probe these candidates. We propose a strategy to decisively probe a part of this parameter space. At the lower end of this mass range, PBHs with masses $\sim 10^{17}$ g $- 10^{18}$ g have Hawking temperatures in the range of 0.01 MeV to 0.1 MeV, implying that substantial evaporated photons are produced by them around these energy scales. Near-future soft gamma-ray telescopes like AMEGO, with its large effective area and improved background rejection capabilities, can search for these photons and investigate this hard-to-probe parameter space. The most efficient search strategy involves observations of the region around the Galactic Center. We include the Galactic astrophysical background produced by cosmic-rays and the measured extra-galactic gammaray background in our projected search strategy. Our projections show that AMEGO can exclude non-rotating PBHs as the sole component of DM upto $\sim 7 \times 10^{17}$ g. We demonstrate that maximal rotation as well as extended mass distribution of the PBHs allow us to explore larger ranges of PBH masses. We also predict that the projected exclusions on PBH DM in the mass range \sim $10^{16} - 10^{17}$ g will be much stronger than the existing limits. The projections presented in this work are robust to the different choices of DM density profiles. At higher PBH masses in this range, the Hawking radiation flux gets smaller and thus much larger instruments need to be built in order to detect the evaporation signature. In

the absence of much larger telescopes, other techniques need to be developed in order to probe the complete parameter space of asteroid-mass PBHs.

V. ACKNOWLEDGMENTS

We thank Basudeb Dasgupta and Thomas Edwards for discussions and useful suggestions. We especially thank

- PLANCK collaboration, N. Aghanim et al., *Planck 2018 results. VI. Cosmological parameters, Astron.* Astrophys. 641 (2020) A6 [1807.06209].
- [2] K. Pardo and D. N. Spergel, What is the price of abandoning dark matter? Cosmological constraints on alternative gravity theories, Phys. Rev. Lett. 125 (2020) 211101 [2007.00555].
- [3] L. E. Strigari, Galactic Searches for Dark Matter, Phys. Rept. 531 (2013) 1 [1211.7090].
- [4] T. R. Slatyer, Indirect Detection of Dark Matter, in Theoretical Advanced Study Institute in Elementary Particle Physics: Anticipating the Next Discoveries in Particle Physics, pp. 297–353, 2018, 1710.05137, DOI.
- [5] T. Lin, Dark matter models and direct detection, PoS 333 (2019) 009 [1904.07915].
- [6] A. Boveia and C. Doglioni, Dark Matter Searches at Colliders, Ann. Rev. Nucl. Part. Sci. 68 (2018) 429 [1810.12238].
- [7] Y. B. Zel'dovich and I. D. Novikov, The Hypothesis of Cores Retarded during Expansion and the Hot Cosmological Model, Astronomicheskii Zhurnal 43 (1966) 758.
- [8] S. Hawking, Gravitationally collapsed objects of very low mass, Mon. Not. Roy. Astron. Soc. 152 (1971) 75.
- [9] B. J. Carr and S. W. Hawking, Black holes in the early Universe, Mon. Not. Roy. Astron. Soc. 168 (1974) 399.
- [10] G. F. Chapline, Cosmological effects of primordial black holes, Nature 253 (1975) 251.
- [11] A. Katz, J. Kopp, S. Sibiryakov and W. Xue, Femtolensing by Dark Matter Revisited, JCAP 1812 (2018) 005 [1807.11495].
- [12] P. Montero-Camacho, X. Fang, G. Vasquez, M. Silva and C. M. Hirata, *Revisiting constraints on* asteroid-mass primordial black holes as dark matter candidates, JCAP **1908** (2019) 031 [1906.05950].
- [13] N. Smyth, S. Profumo, S. English, T. Jeltema, K. McKinnon and P. Guhathakurta, Updated Constraints on Asteroid-Mass Primordial Black Holes as Dark Matter, Phys. Rev. D 101 (2020) 063005 [1910.01285].
- [14] B. Dasgupta, R. Laha and A. Ray, Neutrino and positron constraints on spinning primordial black hole dark matter, Phys. Rev. Lett. **125** (2020) 101101 [1912.01014].
- [15] B. Carr, K. Kohri, Y. Sendouda and J. Yokoyama, Constraints on Primordial Black Holes, 2002.12778.
- [16] A. M. Green and B. J. Kavanagh, Primordial Black Holes as a dark matter candidate, 2007.10722.
- [17] B. Carr and F. Kuhnel, Primordial Black Holes as Dark Matter: Recent Developments, Ann. Rev. Nucl.

Tracy R. Slatyer for early discussions which led to this work. JBM is supported by a Clay Fellowship at the Smithsonian Astrophysical Observatory.

Part. Sci. 70 (2020) 355 [2006.02838].

- [18] LIGO SCIENTIFIC, VIRGO collaboration, B. P. Abbott et al., Observation of Gravitational Waves from a Binary Black Hole Merger, Phys. Rev. Lett. 116 (2016) 061102 [1602.03837].
- [19] S. Bird, I. Cholis, J. B. Muñoz, Y. Ali-Haimoud, M. Kamionkowski, E. D. Kovetz et al., *Did LIGO detect dark matter?*, *Phys. Rev. Lett.* **116** (2016) 201301 [1603.00464].
- [20] S. Clesse and J. Garcia-Bellido, The clustering of massive Primordial Black Holes as Dark Matter: measuring their mass distribution with Advanced LIGO, Phys. Dark Univ. 15 (2017) 142 [1603.05234].
- [21] M. Sasaki, T. Suyama, T. Tanaka and S. Yokoyama, Primordial Black Hole Scenario for the Gravitational-Wave Event GW150914, Phys. Rev. Lett. 117 (2016) 061101 [1603.08338].
- [22] A. Arbey, J. Auffinger and J. Silk, Constraining primordial black hole masses with the isotropic gamma ray background, Phys. Rev. D 101 (2020) 023010 [1906.04750].
- [23] S. Clark, B. Dutta, Y. Gao, L. E. Strigari and S. Watson, *Planck Constraint on Relic Primordial Black Holes*, *Phys. Rev. D* 95 (2017) 083006 [1612.07738].
- [24] S. Wang, Y.-F. Wang, Q.-G. Huang and T. G. F. Li, Constraints on the Primordial Black Hole Abundance from the First Advanced LIGO Observation Run Using the Stochastic Gravitational-Wave Background, Phys. Rev. Lett. **120** (2018) 191102 [1610.08725].
- [25] H. Poulter, Y. Ali-Haimoud, J. Hamann, M. White and A. G. Williams, CMB constraints on ultra-light primordial black holes with extended mass distributions, 1907.06485.
- [26] M. Boudaud and M. Cirelli, Voyager 1 e[±] Further Constrain Primordial Black Holes as Dark Matter, Phys. Rev. Lett. **122** (2019) 041104 [1807.03075].
- [27] W. DeRocco and P. W. Graham, Constraining Primordial Black Hole Abundance with the Galactic 511 keV Line, Phys. Rev. Lett. 123 (2019) 251102 [1906.07740].
- [28] R. Laha, Primordial Black Holes as a Dark Matter Candidate Are Severely Constrained by the Galactic Center 511 keV γ -Ray Line, Phys. Rev. Lett. 123 (2019) 251101 [1906.09994].
- [29] G. Ballesteros, J. Coronado-Blázquez and D. Gaggero, X-ray and gamma-ray limits on the primordial black hole abundance from Hawking radiation, Phys. Lett. B 808 (2020) 135624 [1906.10113].

- [30] R. Laha, J. B. Munoz and T. R. Slatyer, INTEGRAL constraints on primordial black holes and particle dark matter, Phys. Rev. D 101 (2020) 123514 [2004.00627].
- [31] MACHO collaboration, R. Allsman et al., MACHO project limits on black hole dark matter in the 1-30 solar mass range, Astrophys. J. Lett. 550 (2001) L169 [astro-ph/0011506].
- [32] EROS-2 collaboration, P. Tisserand et al., Limits on the Macho Content of the Galactic Halo from the EROS-2 Survey of the Magellanic Clouds, Astron. Astrophys. 469 (2007) 387 [astro-ph/0607207].
- [33] H. Niikura, M. Takada, S. Yokoyama, T. Sumi and S. Masaki, Constraints on Earth-mass primordial black holes from OGLE 5-year microlensing events, Phys. Rev. D 99 (2019) 083503 [1901.07120].
- [34] M. Oguri, J. M. Diego, N. Kaiser, P. L. Kelly and T. Broadhurst, Understanding caustic crossings in giant arcs: characteristic scales, event rates, and constraints on compact dark matter, Phys. Rev. D 97 (2018) 023518 [1710.00148].
- [35] M. Zumalacarregui and U. Seljak, Limits on stellar-mass compact objects as dark matter from gravitational lensing of type Ia supernovae, Phys. Rev. Lett. 121 (2018) 141101 [1712.02240].
- [36] LIGO SCIENTIFIC, VIRGO collaboration, B. Abbott et al., Search for Subsolar Mass Ultracompact Binaries in Advanced LIGO's Second Observing Run, Phys. Rev. Lett. **123** (2019) 161102 [1904.08976].
- [37] B. J. Kavanagh, D. Gaggero and G. Bertone, Merger rate of a subdominant population of primordial black holes, Phys. Rev. D 98 (2018) 023536 [1805.09034].
- [38] T. D. Brandt, Constraints on MACHO Dark Matter from Compact Stellar Systems in Ultra-Faint Dwarf Galaxies, Astrophys. J. Lett. 824 (2016) L31 [1605.03665].
- [39] S. M. Koushiappas and A. Loeb, Dynamics of Dwarf Galaxies Disfavor Stellar-Mass Black Holes as Dark Matter, Phys. Rev. Lett. 119 (2017) 041102 [1704.01668].
- [40] M. A. Monroy-Rodriguez and C. Allen, The end of the MACHO era- revisited: new limits on MACHO masses from halo wide binaries, Astrophys. J. 790 (2014) 159 [1406.5169].
- [41] P. D. Serpico, V. Poulin, D. Inman and K. Kohri, Cosmic microwave background bounds on primordial black holes including dark matter halo accretion, Phys. Rev. Res. 2 (2020) 023204 [2002.10771].
- [42] A. Hektor, G. Hutsi, L. Marzola, M. Raidal, V. Vaskonen and H. Veermae, *Constraining Primordial Black Holes with the EDGES 21-cm Absorption Signal*, *Phys. Rev. D* **98** (2018) 023503 [1803.09697].
- [43] J. Manshanden, D. Gaggero, G. Bertone, R. M. Connors and M. Ricotti, *Multi-wavelength* astronomical searches for primordial black holes, *JCAP* 06 (2019) 026 [1812.07967].
- [44] A. Hektor, G. Hutsi and M. Raidal, Constraints on primordial black hole dark matter from Galactic center X-ray observations, Astron. Astrophys. 618 (2018) A139 [1805.06513].
- [45] M. Raidal, V. Vaskonen and H. Veermäe, Gravitational Waves from Primordial Black Hole Mergers, JCAP 09 (2017) 037 [1707.01480].
- [46] M. W. Sammons, J.-P. Macquart, R. D. Ekers, R. M. Shannon, H. Cho, J. X. Prochaska et al., *First*

Constraints on Compact Dark Matter from Fast Radio Burst Microstructure, Astrophys. J. **900** (2020) 122 [2002.12533].

- [47] P. Lu, V. Takhistov, G. B. Gelmini, K. Hayashi,
 Y. Inoue and A. Kusenko, *Constraining Primordial Black Holes with Dwarf Galaxy Heating*, 2007.02213.
- [48] A. H. Nitz and Y.-F. Wang, Search for Gravitational Waves from High-Mass-Ratio Compact-Binary Mergers of Stellar Mass and Subsolar Mass Black Holes, Phys. Rev. Lett. **126** (2021) 021103 [2007.03583].
- [49] A. H. Nitz and Y.-F. Wang, Search for gravitational waves from the coalescence of sub-solar mass and eccentric compact binaries, 2102.00868.
- [50] R. Laha, P. Lu and V. Takhistov, Gas Heating from Spinning and Non-Spinning Evaporating Primordial Black Holes, 2009.11837.
- [51] H. Kim, A constraint on light primordial black holes from the interstellar medium temperature, 2007.07739.
- [52] M. H. Chan and C. M. Lee, Constraining Primordial Black Hole Fraction at the Galactic Centre using radio observational data, Mon. Not. Roy. Astron. Soc. 497 (2020) 1212 [2007.05677].
- [53] A. Dolgov, A. Kuranov, N. Mitichkin, S. Porey, K. Postnov, O. Sazhina et al., On mass distribution of coalescing black holes, JCAP 12 (2020) 017 [2005.00892].
- [54] K. W. K. Wong, G. Franciolini, V. De Luca, V. Baibhav, E. Berti, P. Pani et al., Constraining the primordial black hole scenario with Bayesian inference and machine learning: the GWTC-2 gravitational wave catalog, Phys. Rev. D 103 (2021) 023026 [2011.01865].
- [55] G. Hütsi, M. Raidal, V. Vaskonen and H. Veermäe, Two populations of LIGO-Virgo black holes, 2012.02786.
- [56] A. Coogan, L. Morrison and S. Profumo, Direct Detection of Hawking Radiation from Asteroid-Mass Primordial Black Holes, 2010.04797.
- [57] A. Halder and M. Pandey, Investigating the Effect of PBH, Dark Matter – Baryon and Dark Matter – Dark Energy Interaction on EDGES in 21cm Signal, 2101.05228.
- [58] J. B. Munoz, E. D. Kovetz, L. Dai and M. Kamionkowski, *Lensing of Fast Radio Bursts as a Probe of Compact Dark Matter*, *Phys. Rev. Lett.* **117** (2016) 091301 [1605.00008].
- [59] R. Laha, Lensing of fast radio bursts: Future constraints on primordial black hole density with an extended mass function and a new probe of exotic compact fermion and boson stars, Phys. Rev. D 102 (2020) 023016 [1812.11810].
- [60] A. Katz, J. Kopp, S. Sibiryakov and W. Xue, Looking for MACHOs in the Spectra of Fast Radio Bursts, Mon. Not. Roy. Astron. Soc. 496 (2020) 564 [1912.07620].
- [61] S. Jung and C. S. Shin, Gravitational-Wave Fringes at LIGO: Detecting Compact Dark Matter by Gravitational Lensing, Phys. Rev. Lett. **122** (2019) 041103 [1712.01396].
- [62] F. Kuhnel, A. Matas, G. D. Starkman and K. Freese, Waves from the Centre: Probing PBH and other Macroscopic Dark Matter with LISA, Eur. Phys. J. C 80 (2020) 627 [1811.06387].
- [63] R.-g. Cai, S. Pi and M. Sasaki, Gravitational Waves Induced by non-Gaussian Scalar Perturbations, Phys.

Rev. Lett. **122** (2019) 201101 [1810.11000].

- [64] S. Jung and T. Kim, Gamma-ray burst lensing parallax: Closing the primordial black hole dark matter mass window, Phys. Rev. Res. 2 (2020) 013113 [1908.00078].
- [65] Y. Bai and N. Orlofsky, Microlensing of X-ray Pulsars: a Method to Detect Primordial Black Hole Dark Matter, Phys. Rev. D 99 (2019) 123019 [1812.01427].
- [66] Y.-F. Wang, Q.-G. Huang, T. G. Li and S. Liao, Searching for primordial black holes with stochastic gravitational-wave background in the space-based detector frequency band, Phys. Rev. D 101 (2020) 063019 [1910.07397].
- [67] J. A. Dror, H. Ramani, T. Trickle and K. M. Zurek, Pulsar Timing Probes of Primordial Black Holes and Subhalos, Phys. Rev. D 100 (2019) 023003 [1901.04490].
- [68] H.-K. Guo, J. Shu and Y. Zhao, Using LISA-like Gravitational Wave Detectors to Search for Primordial Black Holes, Phys. Rev. D 99 (2019) 023001 [1709.03500].
- [69] B. Dutta, A. Kar and L. E. Strigari, Constraints on MeV dark matter and primordial black holes: Inverse Compton signals at the SKA, 2010.05977.
- [70] A. Kusenko, M. Sasaki, S. Sugiyama, M. Takada, V. Takhistov and E. Vitagliano, Exploring Primordial Black Holes from the Multiverse with Optical Telescopes, Phys. Rev. Lett. **125** (2020) 18 [2001.09160].
- [71] S. Sugiyama, V. Takhistov, E. Vitagliano, A. Kusenko, M. Sasaki and M. Takada, *Testing Stochastic* Gravitational Wave Signals from Primordial Black Holes with Optical Telescopes, Phys. Lett. B 814 (2021) 136097 [2010.02189].
- [72] N. Bhaumik and R. K. Jain, Stochastic induced gravitational waves and lowest mass limit of primordial black holes with the effects of reheating, 2009.10424.
- [73] D. N. Page, Particle Emission Rates from a Black Hole: Massless Particles from an Uncharged, Nonrotating Hole, Phys. Rev. D13 (1976) 198.
- [74] D. N. Page, Particle Emission Rates from a Black Hole. 2. Massless Particles from a Rotating Hole, Phys. Rev. D14 (1976) 3260.
- [75] J. H. MacGibbon, B. J. Carr and D. N. Page, Do Evaporating Black Holes Form Photospheres?, Phys. Rev. D78 (2008) 064043 [0709.2380].
- [76] P. N. Okele and M. J. Rees, Observational consequences of positron production by evaporating black holes, Astronomy and Astrophysics 81 (1980) 263.
- [77] P. Okeke, The primary source and the fates of galactic positrons, Astrophysics and Space Science **71** (1980) 371.
- [78] J. H. MacGibbon and B. J. Carr, Cosmic Rays from Primordial Black Holes, Astrophysical Journal 371 (1991) 447.
- [79] C. Bambi, A. D. Dolgov and A. A. Petrov, Primordial black holes and the observed Galactic 511-keV line, Phys. Lett. B670 (2008) 174 [0801.2786].
- [80] P. Stöcker, M. Krämer, J. Lesgourgues and V. Poulin, Exotic energy injection with ExoCLASS: Application to the Higgs portal model and evaporating black holes, JCAP 03 (2018) 018 [1801.01871].

- [81] S. K. Acharya and R. Khatri, CMB and BBN constraints on evaporating primordial black holes revisited, JCAP 06 (2020) 018 [2002.00898].
- [82] C. Keith, D. Hooper, N. Blinov and S. D. McDermott, Constraints on Primordial Black Holes From Big Bang Nucleosynthesis Revisited, Phys. Rev. D 102 (2020) 103512 [2006.03608].
- [83] C. Kouvaris, P. Tinyakov and M. H. Tytgat, NonPrimordial Solar Mass Black Holes, Phys. Rev. Lett. 121 (2018) 221102 [1804.06740].
- [84] B. Dasgupta, R. Laha and A. Ray, Low Mass Black Holes from Dark Core Collapse, 2009.01825.
- [85] S. Shandera, D. Jeong and H. S. G. Gebhardt, Gravitational Waves from Binary Mergers of Subsolar Mass Dark Black Holes, Phys. Rev. Lett. **120** (2018) 241102 [1802.08206].
- [86] J. McEnery, A. van der Horst, A. Dominguez, A. Moiseev, A. Marcowith, A. Harding et al., All-sky Medium Energy Gamma-ray Observatory: Exploring the Extreme Multimessenger Universe, in Bulletin of the American Astronomical Society, vol. 51, p. 245, Sept., 2019, 1907.07558.
- [87] J. H. MacGibbon and B. R. Webber, Quark and gluon jet emission from primordial black holes: The instantaneous spectra, Phys. Rev. D41 (1990) 3052.
- [88] J. H. MacGibbon, Quark and gluon jet emission from primordial black holes. 2. The Lifetime emission, Phys. Rev. D44 (1991) 376.
- [89] A. Arbey and J. Auffinger, BlackHawk: A public code for calculating the Hawking evaporation spectra of any black hole distribution, Eur. Phys. J. C 79 (2019) 693 [1905.04268].
- [90] R. Bartels, D. Gaggero and C. Weniger, Prospects for indirect dark matter searches with MeV photons, JCAP 1705 (2017) 001 [1703.02546].
- [91] B. Carr, K. Kohri, Y. Sendouda and J. Yokoyama, New cosmological constraints on primordial black holes, Phys. Rev. D 81 (2010) 104019 [0912.5297].
- [92] H. Niikura et al., Microlensing constraints on primordial black holes with Subaru/HSC Andromeda observations, Nat. Astron. 3 (2019) 524 [1701.02151].
- [93] A. W. Strong, K. Bennett, H. Bloemen, R. Diehl, W. Hermsen, D. Morris et al., Diffuse continuum gamma rays from the Galaxy observed by COMPTEL., Astronomy and Astrophysics 292 (1994) 82.
- [94] A. Strong, H. Bloemen, R. Diehl, W. Hermsen and V. Schoenfelder, Comptel skymapping: A New approach using parallel computing, Astrophys. Lett. Commun. 39 (1999) 209 [astro-ph/9811211].
- [95] FERMI-LAT collaboration, A. Strong, Interstellar gamma rays and cosmic rays: new insights from Fermi-LAT AND INTEGRAL, in ICATPP Conference on Cosmic Rays for Particle and Astroparticle Physics, pp. 473–481, 1, 2011, 1101.1381, DOI.
- [96] K. Watanabe, D. H. Hartmann, M. D. Leising, L. S. The, G. H. Share and R. L. Kinzer, *The Cosmic γ-ray Background from supernovae*, in *Proceedings of the Fourth Compton Symposium* (C. D. Dermer, M. S. Strickman and J. D. Kurfess, eds.), vol. 410 of *American Institute of Physics Conference Series*, pp. 1223–1227, May, 1997, DOI.
- [97] Y. Fukada, S. Hayakawa, M. Ikeda, I. Kasahara, F. Makino and Y. Tanaka, *Rocket Observation of Energy Spectrum of Diffuse Hard X-Rays, Astrophysics*

and Space Science **32** (1975) L1.

- [98] D. Gruber, J. Matteson, L. Peterson and G. Jung, The spectrum of diffuse cosmic hard x-rays measured with heao-1, Astrophys. J. 520 (1999) 124 [astro-ph/9903492].
- [99] R. L. Kinzer, G. V. Jung, D. E. Gruber, J. L. Matteson, Peterson and L. E., *Diffuse Cosmic Gamma Radiation Measured by HEAO 1*, Astrophysical Journal 475 (1997) 361.
- [100] G. Weidenspointner et al., The comptel instrumental line background, AIP Conf. Proc. 510 (2000) 581 [astro-ph/0012332].
- [101] T. D. P. Edwards and C. Weniger, A Fresh Approach to Forecasting in Astroparticle Physics and Dark Matter Searches, JCAP 02 (2018) 021 [1704.05458].
- [102] T. D. P. Edwards and C. Weniger, swordfish: Efficient Forecasting of New Physics Searches without Monte Carlo, 1712.05401.
- [103] M. DOORNHEIN, Uses and Limitations of Fisher Forecasting in Setting Upper Limits on the Interaction Strength of Dark Matter, 2018.

- [104] J. F. Navarro, C. S. Frenk and S. D. M. White, A Universal density profile from hierarchical clustering, Astrophys. J. 490 (1997) 493 [astro-ph/9611107].
- [105] K. C. Y. Ng, R. Laha, S. Campbell, S. Horiuchi, B. Dasgupta, K. Murase et al., *Resolving small-scale* dark matter structures using multisource indirect detection, Phys. Rev. D 89 (2014) 083001 [1310.1915].
- [106] C. Winkler et al., The INTEGRAL mission, Astron. Astrophys. 411 (2003) L1.
- [107] FERMI-LAT collaboration, W. B. Atwood et al., The Large Area Telescope on the Fermi Gamma-ray Space Telescope Mission, Astrophys. J. 697 (2009) 1071 [0902.1089].
- [108] V. Schoenfelder, H. Aarts, K. Bennett, H. de Boer, J. Clear, W. Collmar et al., Instrument Description and Performance of the Imaging Gamma-Ray Telescope COMPTEL aboard the Compton Gamma-Ray Observatory, Astrophysical Journal, Supplement 86 (1993) 657.
- [109] D. Coe, Fisher Matrices and Confidence Ellipses: A Quick-Start Guide and Software, 0906.4123.