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1	Neutron-Neutron Angular Correlations in Spontaneous Fission of
2	$^{252}\mathbf{Cf} \ \mathbf{and} \ ^{240}\mathbf{Pu}$
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Abstract

Background: Angular anisotropy has been observed between prompt neutrons emitted during the fission process. Such an anisotropy arises because the emitted neutrons are boosted along the direction of the parent fragment.

Purpose: To measure the neutron-neutron angular correlations from the spontaneous fission of ²⁵²Cf and ²⁴⁰Pu oxide samples using a liquid scintillator array capable of pulse shape discrimination. To compare these correlations to simulations combining the Monte Carlo radiation transport code MCNPX with the fission event generator FREYA.

Method: Two different analysis methods were used to study the neutron-neutron correlations with varying energy thresholds. The first is based on setting a light output threshold while the second imposes a time-of-flight cutoff. The second method has the advantage of being truly detector independent.

Results: The neutron-neutron correlation modeled by FREYA depends strongly on the sharing of the excitation energy between the two fragments. The measured asymmetry enabled us to adjust the FREYA parameter x in ²⁴⁰Pu, which controls the energy partition between the fragments and is so far inaccessible in other measurements. The ²⁴⁰Pu data in this analysis was the first available to quantify the energy partition for this isotope. The agreement between data and simulation is overall very good for ²⁵²Cf(sf) and ²⁴⁰Pu(sf).

Conclusions: The asymmetry in the measured neutron-neutron angular distributions can be predicted by FREYA. The shape of the correlation function depends on how the excitation energy is partitioned between the two fission fragments. Experimental data suggest that the lighter fragment is disproportionately excited.

9 I. INTRODUCTION

Spontaneous fission is characterized by the emission of bursts of neutrons. These bursts are in turn amplified by the surrounding multiplying fissile materials to form fission chains. This unique fission chain signature has been used for many decades to detect and authenticate nuclear materials. Typically ³He tubes record the arrival times of neutrons from fissile sources. Unfortunately the cross section for neutron capture in ³He is only large enough for neutrons that have been thermalized in a moderating material. Scintillators, on the other hand, can directly detect unmoderated fission neutrons because inelastic scattering of neutrons on hydrogen results in the emission of a recoil proton, ionizing the scintillator material, enabling detection on a nanosecond time scale.

Because scintillators measure unmoderated prompt emission of neutrons from spontaneous fission, detection of nuclear materials such as plutonium becomes possible by measurements of the angular anisotropy between two neutrons. Almost all of the neutron emission in spontaneous and low energy fission comes from the fully accelerated fission fragments whose back-to-back motion is imprinted on the neutron directions in the laboratory frame. Thus whose small angle correlations are expected from neutrons emitted from the same fragment, whereas large angle correlations arise from opposite fragments. ²⁴⁰Pu is a key isotope of plutonium because of its high spontaneous fission rate. In addition, its low average neutron multiplicity rsuggests that it should exhibit a rather strong angular anisotropy. Thus such measurements ²⁸ in ²⁴⁰Pu(sf) could provide valuable information for identifying the composition of materials.

²⁹ Neutron-neutron angular correlations have been measured in the past for ²⁵²Cf(sf) [1–5], ³⁰ ²⁴⁰Pu(sf) [6] and ²³⁵U($n_{\rm th}$,f) [7]. These measurements were previously employed to search ³¹ for evidence of scission neutrons, emitted from the nucleus prior to fission. These neutrons ³² would be emitted isotropically in the laboratory frame. Discrepancies in the measured n-n³³ angular correlations relative to simulations could be due to scission neutrons. No evidence ³⁴ was seen for an isotropic neutron source in Ref. [8]. However, those simulations using the ³⁵ FREYA code, also employed here, were not coupled to a model of the detector system via ³⁶ a neutron transport code and were thus not a comprehensive comparison. We can thus ³⁷ improve on the analysis in Ref. [8] with a full simulation of our detector. In addition, as ³⁸ was also shown in Ref. [8], the neutron-neutron angular correlation is most sensitive to the ³⁹ excitation energy sharing between the two fragments. Currently this sharing is modeled ⁴⁰ in FREYA by a single-valued parameter x. For ²⁵²Cf(sf), x was fixed by comparing to the ⁴¹ neutron multiplicity as a function of the fragment mass. No such measurement is available to ⁴² fix x for ²⁴⁰Pu(sf). Thus a comparison between the *n*-*n* correlations measured here for this ⁴³ isotope with FREYA simulations could fix the x parameter for this case, as we discuss later.

In most measurements, the method for constructing correlations is based on setting different thresholds on the scintillation light output, leading to an energy dependent set de of correlations. Unfortunately, this method is detector dependent because the detector materials, sizes, and data acquisition systems affect these measurements. For example, in large detectors, neutrons will produce more scintillation light by scattering and transferring denergy to multiple proton recoils than in a smaller detector.

In this paper we propose a new method, based on neutron time-of-flight, to construct the s1 kinetic energy of the measured neutron rather than relying on the recoil proton. To form s2 correlations, we select neutrons with kinetic energies above a threshold, resulting in a truly s3 detector independent correlation measurement.

The paper is organized as follows. We first describe the detector setup, discussing two 54 ⁵⁵ methods to determine the dependence of the scintillator light yield function on proton ⁵⁶ recoil energy. We then describe the method used in Refs. [4–6] for determining correlations ⁵⁷ based on detector energy thresholds, including some of its shortcomings. Subsequently, we ⁵⁸ introduce an analysis based on the neutron time-of-flight to determine a detector-independent ⁵⁹ correlation function. Next, we introduce the fission model FREYA and describe how the 60 measured correlations are simulated by incorporating FREYA into neutron transport codes. Our results are then compared to previous ${}^{252}Cf(sf)$ and ${}^{240}Pu(sf)$ data using the same energy 61 thresholds to validate our method. The dependence of the results on detector size is also 62 ⁶³ discussed. Next, we describe how we employ our simulations to eliminate detector cross talk. ⁶⁴ Finally, we compare Monte Carlo simulations using MCNPX with FREYA to the experimental 65 data and describe how the neutron-neutron correlations could be used to determine the ⁶⁶ FREYA parameter governing the excitation energy sharing between the fragments when no ⁶⁷ other data exists. Finally we draw our conclusions.

68 II. DETECTOR SETUP AND EXPERIMENTAL METHOD

Figure 1 shows the geometrical configuration of the detector array used to measure the ro neutron-neutron correlations. The array consists of seventy-seven scintillator detectors. Each r1 detector in the array is cylindrical in shape, 10.16 cm diameter by 7.62 cm deep and filled with r2 EJ-301 scintillating material [9]. Thirteen detectors sit over a cavity formed by an octagonal r3 array underneath. Each arm of the octagon is a vertical tower made of eight scintillators. r4 The measurement cavity is also octagonal, with 60 cm between the faces of opposite towers, r5 and stands 50 cm tall. The tightly-packed system has 2π solid angle coverage, resulting in r6 an overall geometric efficiency of 50%.

⁷⁷ Each of the 77 scintillators is individually read out by a photomultiplier tube. Data is



 $_{^{78}}$ FIG. 1. (Color online) Photograph of the 77 liquid scintillator array on low mass floor.

79

⁸⁰ acquired using a VME-based pulse digitizer for pulse-shape discrimination (PSD) and list ⁸¹ mode data acquisition. The counter uses Struck SIS3316 fast ADC digitizers with a 160 ⁸² MHz sampling rate and a 12-bit dynamic range. The digitizers have an input voltage range ⁸³ of ± 1 V. The digitizers allow sub-nanosecond timing of time-stamped physics events and ⁸⁴ allow the streaming of processed and compressed PSD information to reduce the overall data ⁸⁵ burden. The detector was originally designed for fast multiplicity counting and assaying of ⁸⁶ fissile material because the few nanosecond decay time of the scintillator material allows ⁸⁷ faster count rates than ³He well counters.

A. Energy calibration

⁸⁹ The energy calibration of the liquid scintillators was performed using a ¹³⁷Cs source placed ⁹⁰ in the middle of the detector array. Each gamma interaction in the scintillator produces ⁹¹ scintillation light, which is recorded by the photomultiplier tube (PMT) as an electric pulse. ⁹² The pulse is digitized by an analog to digital converter (ADC) and the integral of the counts ⁹³ under the pulse is I_{ADC} . In a well calibrated detector, a photon of energy E_{γ} (keV) depositing ⁹⁴ all its energy in the scintillator produces a value of I_{ADC} which can be mapped back to E_{γ} . ⁹⁵ However, in a large array of detectors, the PMTs, scintillators, photocathodes, digitizers ⁹⁶ are not identical, and the integrals I_{ADC} will vary from detector to detector, for identical ⁹⁷ photon energy deposition. The mapping between I_{ADC} and E_{γ} is thus not unique across all ⁹⁸ detectors. To account for these differences, we use detector response functions DRF(I_{ADC}) ⁹⁹ to convert the integral I_{ADC} into a scintillation light output LO which has units of keVee. ¹⁰⁰ With these detector-dependent functions, photons with identical energies map onto the same ¹⁰¹ LO, independently of the detector. The detector response functions have the following form:

$$\text{DRF}_{\gamma}(I_{\text{ADC}}) = aI_{\text{ADC}}(E_{\gamma}) \quad [\text{keVee}] ,$$
 (1)

¹⁰² where the coefficient a depends on the scintillator/PMT assembly and is in units of ¹⁰³ keVee/(integral of ADC counts). The value of a is chosen so that, for a photon of en-¹⁰⁴ ergy E_{γ} transferring all its energy to electrons to eventually produce light, the value of the ¹⁰⁵ light output LO is equal to E_{γ} . These response functions are used to reconstruct the photon ¹⁰⁶ spectrum from the integrals I_{ADC} recorded by the PMT pulse digitizer. In Ref. [10] the ¹⁰⁷ detector response functions were shown to be linear in E_{γ} within 1%. Figure 2 shows the ¹⁰⁸ measured ¹³⁷Cs scintillation light spectrum for all 77 scintillators. The Compton edge for ¹⁰⁹ ¹³⁷Cs, at 477 keV, was detected by an algorithm described in Ref. [11] and was employed to ¹¹⁰ set the values of the coefficients a for each individual detector.



FIG. 2. (Color online) Energy calibration of the 77 liquid scintillators using a ¹³⁷Cs source. The energy spectra is given for each channel number.

111 B. Pulse shape discrimination

¹¹² Neutron-photon pulse separation was achieved by simultaneous measurement of the charge ¹¹³ in the PMT current, in the peak of the pulse, and the charge in the tail of the pulse, the ¹¹⁴ so-called slow component. The method of pulse-shape discrimination (PSD) is described in ¹¹⁵ Ref. [12].

Figure 3 shows neutron scores computed by the PSD algorithm for different detection 117 events as a function of the electron-equivalent energy deposited by the event. The neutron 118 score for digitized pulses is the ratio of the area under the tail to the area under the peak of 119 the pulse. We can clearly distinguish two bands: the upper one, filled with neutrons, and the lower one, with photons. The magenta (light gray) outline in this plot defines a region where events are most likely neutrons and will be tagged as such by the data acquisition 122 123 system. The black outline defines a region where events are tagged as photons. The two ¹²⁴ outlines can be referred to as neutron and photon acceptance regions from a PSD classifier ¹²⁵ perspective, and extend down to 100 keVee, below which PSD was not attempted. The ¹²⁶ PMT biases were optimized to get good PSD for high-energy neutrons because our focus was ¹²⁷ not on the lowest energy neutrons. For electron-equivalent energies greater than 1 MeVee. ¹²⁸ the two bands do not overlap significantly, leading to good neutron-photon discrimination.



FIG. 3. (Color online) Pulse shape discrimination for one of the liquid scintillators. The regions of neutron (magenta or light gray outline) and photon (black outline) identification are shown. From a PSD classifier perspective, they can be referred to as the neutron and photon acceptance regions.

¹²⁹ Below 1 MeVee, discrimination slowly worsens and it becomes more difficult to distinguish ¹³⁰ neutrons from photons. In that energy region, photons encroaching on the neutron band ¹³¹ push the outline of the positive neutron identification region upwards and lead to a number ¹³² of neutrons that cannot be identified as such using the PSD classification algorithm. Shown ¹³³ in Fig. 4, the acceptance of neutron pulses degrades rapidly from 94% at 300 keVee down to ¹³⁴ 80% at 200 keVee and 30% at 100 keVee. At these low light outputs, the reduced acceptances ¹³⁵ not only depends on the PSD classifier but also on the reduced detector sensitivities to ¹³⁶ neutrons (see Figs. 2 and 7). Thus there is significant degradation in neutron acceptance ¹³⁷ below 300 keVee. Our data was corrected for these neutron acceptances by adjusting the ¹³⁸ contributions of the *n*-*n* coincidences.

The ²⁵²Cf source used for calibration emitted so few neutrons above 5 MeVee that it was difficult to define regions of positive neutron identification with great confidence above that neutrons. Because only 0.3% of the neutrons from ²⁵²Cf(sf) have enough kinetic energy to produce proton recoils that can generate 5 MeVee of light output, this upper cutoff was deemed appropriate for these measurements. Events lying outside of these two bands, with equivalent energies of less than 100 keVee and greater than 5 MeVee, are treated as particles of



FIG. 4. (Color online) Acceptance of neutron pulses as a function of scintillation light output and averaged over all detector channels. Bars indicate the dispersions around the means, from channel-to-channel variations.

¹⁴⁵ unknown type. The region of positive photon identification slowly curves up above 5 MeVee.
¹⁴⁶ This effect is attributed to saturation effects in the electronics. Indeed, large enough pulses
¹⁴⁷ run into the dynamic range limit of the digitizers. This causes either the PMTs to saturate
¹⁴⁸ or the tops of the digitized pulses to be flattened or chopped off and the corresponding charge
¹⁴⁹ does not get integrated. For these high energies, the detector response loses its linearity.
¹⁵⁰ This is not critical for our experiment because we only consider electron-equivalent energies
¹⁵¹ below 5 MeVee. One of the seventy-seven scintillators was not properly connected and acted
¹⁵² erratically. It was turned off for the data analysis.

The neutron misidentification rate for this array of liquid scintillators was computed in ¹⁵³ Ref. [13]. The number of events midentified as neutrons decreases with equivalent energy: it ¹⁵⁵ is on the order of 20 ± 4 ppm for a 100 keVee energy threshold; 13 ± 4 ppm for 200 keVee; ¹⁵⁶ 11 ± 3 ppm for 300 keVee; 9 ± 3 ppm for 400 keVee; and 7 ± 3 ppm for 500 keVee. The ¹⁵⁷ number of events misidentified as photons was not estimated because it is of limited relevance ¹⁵⁸ for this analysis.

¹⁵⁹ C. Synchronization between detectors

It is essential that the liquid scintillators be synchronized with each other to accurately 160 measure time intervals between detections in different detectors. Because neutron kinetic 161 energies are computed from time-of-flight, the resolution of the time intervals has a direct 162 impact on the resolution of the neutron kinetic energy. The liquid scintillators were syn-163 chronized using Compton scattering between detectors. The method use to synchronize 164 the scintillators is described in Ref. [14]. We use the same 137 Cs data used for the energy 165 calibration to synchronize the time interval between detectors. Photons emitted from ¹³⁷Cs 166 167 will occasionally Compton scatter in one detector and register a second count in an adjacent detector, resulting in a time interval between detection equal to the photon time-of-flight 168 between the two count locations. If the chronological order of the counts is reversed, the 169 ¹⁷⁰ time interval between the counts will have the same amplitude but will be negative. The centers of adjacent detectors are approximately 10 cm apart, corresponding to a photon 171 ¹⁷² time-of-flight of 330 ps center-to-center. For infinite time resolution, we could thus expect two broad peaks ~ 330 ps apart with long tails on both sides because photons will Compton scatter in different locations within the detectors. The time interval distribution between 174 counts is shown in Fig. 5 for our detector setup. 176

Because adjacent detectors are both large and close together, the two peaks are indistin-¹⁷⁷ guishable and have merged into a single peak. Fitting this peak with a Gaussian distribution, ¹⁷⁹ the standard deviation is 650 ps. Accounting for the photon time-of-flight, one can estimate ¹⁸⁰ the time resolution to be close to 500 ps.

181 D. Light output function

The emitted neutrons generate charged particles in the scintillator (mainly recoil protons) ¹⁸² which produce light pulses. In addition, γ -radiation creates photo or Compton electrons. ¹⁸⁴ However, protons and electrons of the same energy give light pulses of different amplitudes. ¹⁸⁵ Because the detector energy calibration is carried out with photon sources, the relation ¹⁸⁶ between proton and electron energies is determined employing the light output function.

The light output scale is defined in terms of the equivalent electron energy LO which is the light output for an electron depositing the corresponding energy inside the scintillator;



FIG. 5. (Color online) Distribution of time intervals between counts in adjacent detectors.

¹⁸⁹ i.e. a proton of the energy E_p gives the same light output LO as an electron of the equivalent ¹⁹⁰ energy LO.

¹⁹¹ Cecil's exponential model [15] is chosen as the functional form of $LO(E_p)$,

$$LO(E_p) = aE_p - b\left(1 - \exp\left(-cE_p^d\right)\right) \quad [keVee]$$
(2)

¹⁹² The coefficients a, b, and c were determined by fitting time-of-flight spectra with different ¹⁹³ light output thresholds. For a given scintillation light output LO, Eq. (2) can be used to ¹⁹⁴ determine the recoil proton energy E_p necessary to produce the same amount of light as an ¹⁹⁵ electron of energy LO keVee would.

Figure 6 shows the time-of-flight distributions using 16 detectors at the same distance from the ²⁵²Cf(sf) source and setting a 100 keVee threshold on the light output. The blue (top) curve shows the distribution of time intervals between any two detections in the array before PSD is applied to distinguish neutrons from photons. Thus this distribution also includes all the events outside of the black and magenta (light gray) outlines in Fig. 3, explaining time area in the second second



FIG. 6. (Color online) Distribution of time intervals between counts for the $^{252}Cf(sf)$ source measured with a subset of the liquid scintillator array. A light output threshold of 100 keVee is applied.

²⁰³ intervals between photon detections, and the red (middle curve at 15 ns) curve is the time ²⁰⁴ interval for a photon detection followed by a neutron. The maximum proton recoil energy can be determined from a precise measurement of the time difference between the signals and 205 particle identification through the observed signal shape. The maximum proton recoil energy 206 for a given scintillation light output threshold is determined from fitting the red (middle 207 curve at 15 ns) curve in Fig. 6 while accounting for the background. This method, described 208 in Ref. [16], enabled us to determine the coefficients of Cecil's exponential model in Eq. (2). 209 As an alternative to this conventional time-of-flight approach, we can use the measured 210 scintillation light pulse height distribution (PHD) to determine the light output as a function 211 of the proton recoil energy [17, 18]. Indeed, employing the MCNPX 2.7.0 Monte Carlo code, 212 we can accurately model sources and detectors and simulate the collision of each source 213 neutron with hydrogen atoms in each individual detector. To construct the scintillation light 214 ²¹⁵ produced by the simulated proton recoils from a source neutron, we apply Cecil's law to the ²¹⁶ proton recoil energies and sum up the light to form an individual light pulse. This method is ²¹⁷ repeated for all source neutrons to obtain a scintillation light PHD.

Our constructed scintillation light PHD can be compared to the measured one to fix the parameters of the exponential expression for the light output and thus reconstruct the measured PHD. We note that if we assume that neutrons only collide once per detector, it would be straightforward to construct the proton recoil PHD by considering the contributions of each source neutron to this distribution and converting it to a scintillation light PHD using the exponential form. However, due to the nonlinearity of the light output function, the single scattering assumption is only valid if the neutrons generate one single proton recoil per detector, i.e for small detectors.

The optimization yielded the parameters a = 0.81, b = 6.3, c = 0.09 and d = 1 in Eq. (2). The results in terms of PHD are shown in Fig. 7.

In the range 200 keV to 3.5 MeV, the differences between simulated and experimental PHD vary from 0 to 18% with an average of 5%. Except for small discrepancies likely due to insufficient model details in the simulation, the simulated PHD, shown in Fig. 7, is consistent with the one measured experimentally. The jagged structure at low light outputs comes



FIG. 7. (Color online) Measured (black) and simulated (red or light gray) pulse height distributions produced by a ²⁵²Cf(sf) source recorded by the scintillators.

232 233

²³⁴ from neutron rejection by the neutron identification algorithm (see Fig. 3). This results in ²³⁵ reduced detector efficiencies for low neutron energies. The detection sensitivity to epithermal ²³⁶ neutrons, which varies from detector to detector, is reduced as well because the high-voltage ²³⁷ biases on the photomultiplier tubes require a minimum light pulse height close to 100 keVee. ²³⁸ Also note that the measured pulse height spectrum is truncated at 5 MeVee because PSD is ²³⁹ no longer reliable above that energy in our configuration.

240 E. Neutron detection efficiency

The overall neutron detection efficiency of the scintillators is 7.8%. In Table. I, the average neutron detection efficiency is given as a function of the threshold applied to the scintillation light output. A light output threshold is dialed to filter out neutrons with low light output

TABLE I. Average neutron detection efficiency of the scintillators as a function of the scintillation light output threshold LO.

LO (MeVee)	Efficiency $(\%)$
0.1	7.8
0.2	6.7
0.3	4.8
0.4	3.5
0.5	2.5
0.6	1.9
0.7	1.5
0.8	1.2
0.9	0.95
1.0	0.75
1.5	0.29
2.0	0.12

244 245

²⁴⁶ and to compute a LO-dependent neutron detection efficiency.

As an alternative, the detection efficiency can be determined as a function of the neutron kinetic energy using Eqs. (4)-(5) of the time-of-flight approach described in Sec. III B. In this case, the neutron detection efficiency can be inferred from the strength and spectral ²⁵⁰ properties of the spontaneous fission source. Figure 8 shows the average neutron detection ²⁵¹ efficiency of the scintillators for neutrons of kinetic energies varying from 400 keV to 10 MeV. ²⁵² This plot is important as it shows the sensitivity of the detectors to neutrons of various ²⁵³ kinetic energies, and in particular to neutrons emitted by ²⁵²Cf(sf) and ²⁴⁰Pu(sf). The



FIG. 8. Average neutron detection efficiency as a function of kinetic energy, for a scintillation light output threshold of 100 keVee.

254 255

detector efficiency peaks at 2.6 MeV. For neutrons with kinetic energy lower than 2 MeV. 256 the efficiency drops with decreasing energy because fewer and fewer proton recoils yield 257 enough scintillation light to be within the bounds of the neutron acceptance region shown 258 in Fig. 3. For kinetic energies greater than 8 MeV, the efficiency increases artificially. To 259 understand this increase, see the curve labeled 'neutrons following photons' in Fig. 6. This 260 contribution should vanish for time intervals smaller than ~ 5 ns because the only neutrons 261 that can travel to the detectors in less than 4.5 ns are neutrons with energies greater than 262 20 MeV. Instead of vanishing, there are a finite number of events in this region. These events 263 can be attributed to high energy neutrons that inelastically scatter off the detector and 264 ²⁶⁵ surrounding materials. Inelastic scattering reactions generate secondary photons. These ²⁶⁶ photons are delayed by the travel time of the spontaneous fission neutrons to the detectors ²⁶⁷ and are detected on a time scale comparable to that of neutrons originating from the same

²⁶⁸ spontaneous fission. The quasi-coincidences of these photon-neutron pairs fill the region of ²⁶⁹ short time intervals in Fig. 6. In addition, the neutrons in these photon-neutron pairs are ²⁷⁰ erroneously tagged as high energy neutrons, resulting in the artificial increase in neutron ²⁷¹ efficiency for neutrons with kinetic energies greater than 8 MeV in Fig. 8. Fortunately, the ²⁷² fraction of misidentified high energy neutrons is < 2%.

The detector efficiencies are implicitly taken into account in the simulations by using the real neutron energy-dependent cross sections from the data libraries.

275 III. ANALYSIS METHOD

Two different methods are presented to measure the angular correlations between fission reutrons. The first, using detector thresholds as a neutron filter, has been rather widely used in these analyses. Thus, even though it has some shortcomings, as we discuss, we will use it to compare our measurements to previous data. The other, using neutron time of flight to filter neutrons, resulting in a detector independent analysis, is introduced here for the first time. Since it is a new approach, we only show results using this method at the end of this paper, after comparison to previous data and simulations.

A. Detector thresholds as a neutron filter

The first method uses the detection threshold of the scintillators to filter low energy neutrons. This method was used in Gagarski [4] and Pozzi [5] to measure the angular distribution of correlated spontaneous fission neutrons emitted by ²⁵²Cf, and by Marcath [6] for ²⁴⁰Pu. To validate our experimental measurements and methodology, we will compare our data to their results.

Two neutrons are assumed to arise from the same spontaneous fission if they are detected within 40 ns of each other. These neutrons are correlated. Two detected neutrons are uncorrelated if the second neutron is at least 100 μs away in time from the first neutron. A time window opens 100 μs after the first neutron to count uncorrelated neutrons. The duration of this time window depends on the neutron source strength. It is 1 ms for our 294 252 Cf(sf) source and 100 ms for the weaker 240 Pu(sf) source. The ratio of correlated to uncorrelated event rates is proportional to the probability of detecting two spontaneous ²⁹⁶ fission neutrons in some angular bin.

²⁹⁷ While the angular distributions produced by this method are useful, there are some ²⁹⁸ disadvantages that we now discuss.

Although the neutron energy deposition in a scintillator is proportional to the kinetic energy of the incident neutron, it also depends on its scattering angle via elastic scattering. Some high energy neutrons might scatter on hydrogen with a grazing angle, not depositing enough energy to register a count, whereas some lower energy neutrons could register a count with a head-on collision on hydrogen. As a result, the neutron detection threshold imposed on the scintillators does not map onto a single incident neutron kinetic energy threshold.

The probability for the resulting light yield to be above the threshold is a function of the detector volume. For a given threshold, the population of incident neutrons counted in a small detector will be of considerably higher energy than the population in a larger one. Indeed, the number of times a neutron scatters in a volume is a function of the detector volume. In a small detector, a neutron of a given energy will scatter fewer times than in a larger detector, transferring thus less energy to recoil protons.

The selected energy threshold is measured along a scale graduated against gamma-rays. To find out the equivalent neutron kinetic energy, it is necessary to determine the light output function. A survey of the literature [17, 19, 20] indicates that the neutron light output depends on the scintillating material, detector geometry, hardware settings, etc. Measuring it requires a separate, dedicated experiment.

³¹⁶ B. Time-of-flight as a neutron filter

Instead of using a detection threshold to filter low energy neutrons, we propose to use time-of-flight as an alternate approach. Here a photon from spontaneous fission is used to open a time-of-flight measurement window and a neutron is employed to close it.

We assume a spontaneous fission source, located at $(x_{\rm src}, y_{\rm src}, z_{\rm src})$, emits neutrons and photons. One of the photons is detected in a scintillator. This first detection serves as a trigger. Employing this trigger and the distance from the detector to the source, it is possible to determine how much time has passed since the spontaneous fission occurred. Next, one of the spontaneous fission neutrons is detected. The time-of-flight of that spontaneous fission to the neutron detection. The ³²⁶ time interval between the gamma ray detection at $(x_{\gamma}, y_{\gamma}, z_{\gamma})$ and the neutron detection at ³²⁷ (x_n, y_n, z_n) is

$$\Delta t = \frac{1}{v_n} \sqrt{(x_{\rm src} - x_n)^2 + (y_{\rm src} - y_n)^2 + (z_{\rm src} - z_n)^2} - \frac{1}{c} \sqrt{(x_{\rm src} - x_\gamma)^2 + (y_{\rm src} - y_\gamma)^2 + (z_{\rm src} - z_\gamma)^2}$$
(3)

³²⁸ where c is the veolcity of the photon (the speed of light) and v_n is the velocity of the neutron. ³²⁹ The expression above for the time interval can be used to determine the velocity v_n ,

$$v_n = \frac{\sqrt{(x_{\rm src} - x_n)^2 + (y_{\rm src} - y_n)^2 + (z_{\rm src} - z_n)^2}}{\Delta t + \frac{1}{c}\sqrt{(x_{\rm src} - x_\gamma)^2 + (y_{\rm src} - y_\gamma)^2 + (z_{\rm src} - z_\gamma)^2}} .$$
(4)

 $_{330}$ Once v_n is determined, the neutron kinetic energy can be calculated as

$$E_{\rm kin} = \frac{1}{2} m_n v_n^2 \ . \tag{5}$$

³³¹ Inversely, the measured time interval Δt can be calculated as a function of the neutron ³³² kinetic energy. Several values of Δt are listed in Table II for some representative neutron ³³³ kinetic energies. Assuming a threshold $E_{\rm kin}^{\rm thr}$ for the neutron kinetic energy, Eqs. (3)-(5),

TABLE II. Time interval Δt for a given neutron kinetic energy determined by neutron time-of-flight method. Uncertainty $\Delta E_{\rm kin}$ on neutron kinetic energy $E_{\rm kin}$ given the finite detector time resolution of 500 ps. A source to detector distance of 30 cm is assumed.

$E_{\rm kin}$ (MeV) Δt (ns) Δ	$\Delta E_{\rm kin} \ ({\rm keV})$
0.5	29.67	16
1	20.68	48
2	14.34	136
3	11.52	256
4	9.844	396
5	8.700	558

334 335

³³⁶ makes it possible to filter all neutrons with $E_{\rm kin} < E_{\rm kin}^{\rm thr}$.

For all neutrons with $E_{\rm kin} \ge E_{\rm kin}^{\rm thr}$, two neutron detections are assumed to stem from the same spontaneous fission if both occur within a time interval $\Delta t + {\rm TOF}_{\gamma}$. (Recall that this time interval depends on the threshold $E_{\rm kin}^{\rm thr}$, as shown in Table II where ${\rm TOF}_{\gamma}$ is the photon ³⁴⁰ time-of-flight.) Two such neutrons are likely correlated with the spontaneous fission unless ³⁴¹ the two counts arise from the same neutron (neutron cross talk), which is discussed later.

As in the case for using detection thresholds as a filter, the ratio of correlated to uncorrelated event rates is proportional to the probability of detecting two spontaneous fission at neutrons in some angular bin.

We can also determine the uncertainties on the neutron kinetic energy given the finite time resolution of the detector using Eqs. (3)-(5). We assume that the distance between the source and the detectors is uniformly 30 cm. For neutrons of kinetic energy 500 keV, the 500 ps resolution leads to an uncertainty of 16 keV on the neutron kinetic energy. Table II sets the uncertainties on the neutron kinetic energies given the 500 ps resolution of the scintillators.

³⁵¹ A larger uncertainty on the neutron kinetic energy arises from the depth of the detectors. ³⁵² Indeed, neutrons can scatter anywhere in the detector volume, resulting in an uncertainty of ³⁵³ approximately 7.62 cm on its travel distance or a variance $\sigma^2 = (2.2 \text{ cm})^2$ in the numerator ³⁵⁴ of Eq. (4) assuming a rectangular function for the location of interaction within the source. ³⁵⁵ This variance translates into a relative standard deviation of 13% on the kinetic energy of ³⁵⁶ the neutron.

Now the neutron kinetic energies are calculated based on time-of-flight and not on the 357 energy deposited in the scintillators. They are thus independent of the neutron kinematics 358 in the scintillators. We note that, with the PMT voltage setting used in the experiment, a 359 neutron transferring less than 100 keVee to a recoil proton is unlikely to be detected. The 360 population of these neutrons is reduced as the neutron kinetic energy threshold is raised. 361 This method enables us to determine neutron-neutron angular distributions with different 362 kinetic energy thresholds by filtering out incident neutrons based on kinetic energy rather 363 than energy deposition. This method thus has the advantage of forming truly detector 364 ³⁶⁵ independent correlation measurements.

Another advantage of the time-of-flight approach to measure n-n angular correlations is that the type of particle associated with a detection can be determined using a combination of PSD and time-of-flight. Indeed, photons and neutrons can be discriminated based on their relative velocity. We will see in Sec. VII that the neutron detection efficiency can be substantially increased using both of these quantities for particle classification.

371 IV. SIMULATIONS

General-purpose Monte Carlo codes such as MCNP6[®] [21], TRIPOLI-4[®] [22, 23], TART [24], ara and COG [25] are available for modeling neutron transport. They have traditionally employed are "average fission models" for modeling fission, characterized by uncorrelated secondary particle are emission, sampling from the same probability density functions. This approximation is are sufficient for the calculation of average quantities such as flux, energy deposition and multiplication. However, correlations are important, for example, for modeling neutron are multiplicity counters, because determinations of the multiplication and mass of unknown are objects are based on measuring time-correlated neutrons.

To address these deficiencies, analog fission physics was added to Monte Carlo codes over 380 the years. MCNP-DSP [26] was the first code to include full neutron multiplicity distributions 381 from fission. MCNPX-PoliMi [27, 28] followed suit and included full neutron and gamma ray 382 multiplicity distributions from fission. Later, the LLNL Fission Library [29], integrated 383 into MCNPX2.7 [30] and Geant 4.9 [31], featured time-correlated sampling of neutrons and 384 photons from neutron-induced fission, photofission and spontaneous fission. Several of these 385 codes have been used and validated for multiplicity counting systems [32–34]. The correlation 386 capabilities for these codes are, however, limited as they sample outgoing particles from 387 average fission distributions instead of sampling them from individual realizations of a fission 388 process. 389

In recent years, various treatments have addressed fluctuations of and correlations between 390 fission observables. In particular, a Monte Carlo approach was developed for the sequential 391 ³⁹² emission of neutrons and photons from individual fission fragments in binary fission [35, 36]. The more recent event-by-event fission model, FREYA, has been specifically designed for producing large numbers of fission events in a fast simulation [8, 37–42]. Employing nuclear data for fragment mass and kinetic energy distributions, using statistical evaporation models for neutron and photon emission, and conserving energy, momentum, and angular momentum 396 throughout, FREYA is able to predict a host of correlation observables, including correlations 397 in neutron multiplicity, energy, and angles, and the energy sharing between neutrons and 398 ³⁹⁹ photons. FREYA can currently handle neutron-induced fission of ²³³U, ²³⁵U, ²³⁸U, ²³⁹Pu, ²⁴¹Pu, $_{400}$ as well as the spontaneous fission of 238 U, 238 Pu, 240 Pu, 242 Pu, 244 Cm and 252 Cf.

⁴⁰¹ The latest version of FREYA 2.0.2 [43], coupled to the LLNL Fission Library for ease

⁴⁰² of incorporation, can be called from transport codes. In particular, the LLNL Fission ⁴⁰³ Library/FREYA 2.0.2 has been implemented in the latest release of MCNP 6.2. The com-⁴⁰⁴ bination of MCNP 6.2 and LLNL Fission Library/FREYA 2.0.2 enables users to directly ⁴⁰⁵ model fission event-by-event and transport fission secondaries through complex detector ⁴⁰⁶ geometries while keeping them fully correlated from generation to detection.



FIG. 9. (Color online) MCNPX 2.7.0 model of the liquid scintillator array. Scintillators are in yellow (light gray), PMTs in green (dark gray).

To simulate the experimental angular correlation, we used a simplified MCNPX 2.7.0 [30] 408 model developed for the large array of liquid scintillators shown in Fig. 1. A number of 409 elements were not included in this simplified model, shown in Fig. 9: the low mass floor; 410 the room walls and ceiling, which were 5 meters away; the low-density foam holding the 411 liquid scintillators and PMTs; the detector walls; etc. Additional simulations showed that 412 the inclusion of these details made no difference in our analysis. Using a customized [44] 413 version of MCNPX 2.7.0 with the LLNL Fission Library/FREYA [29, 43, 45] turned on, we 414 ran simulations to study neutron-neutron angular correlations.

415 V. COMPARISON TO PREVIOUS DATA USING DETECTOR THRESHOLDS

$_{416}$ A. 252 Cf(sf) measurements

⁴¹⁷ The ²⁵²Cf source used for our measurements was manufactured in 1997. Its initial intensity ⁴¹⁸ was 3.694×10^7 neutrons/s. The casing of the source has a small effect on the outgoing ⁴¹⁹ neutrons from fission. The source contains some contamination from ²⁵⁰Cf. Because the ⁴²⁰ half-life of ²⁵⁰Cf is longer than that of ²⁵²Cf, the fraction of fission neutrons originating from ⁴²¹ ²⁵⁰Cf increases with time. Based on the initial composition and branching ratios for these ⁴²² sources, 1.9% neutrons originate from spontaneous fission of ²⁵⁰Cf. The data analyzed here ⁴²³ were collected by placing the 230 μ Ci ²⁵²Cf source in the center of the detection system for ⁴²⁴ 30 minutes.

The open circles in Fig. 10 show our anisotropic angular distributions as a function of the angle between two spontaneous fission neutrons for different energy thresholds. The variance the angle of correlation, governed by the size of the scintillators and the distance to the area source, is $\sigma^2 = (5.8^{\circ})^2$. The large number of data points in Fig. 10 arises because we have 76 active detectors, and thus 76×75 pairs of detectors with as many angular separations between detectors. Using a large array of detectors has a major advantage: one can measure the area correlation function over a large range of angles with small separations in a single experiment. It is noteworthy that the experiment took only 30 minutes, whereas the Gagarski experiment advantage below with only two detectors took 50 days. Given the size of each detector and the PMT assembly, the smallest angular separation between detectors that could be achieved the 15°. The largest separation angle achievable, aside from diametrically opposed detectors that result in ~ 180°, is approximately 165°.

Table III lists the number of correlated neutron pairs for all detector pairs as a function439 of ENET.

⁴⁴⁰ Data points from other experiments are more sparse because the detector arrays in these ⁴⁴¹ measurements employed fewer array elements. All data points include error bars. The ⁴⁴² Gagarski experiment had two identical stilbene crystals 40 mm diameter by 60 mm deep and ⁴⁴³ shielded with borated polyethylene and lead to prevent cross talk. The angle between the ⁴⁴⁴ two crystals as seen from the source was varied in steps of 5°-10° in the interval 20°-180° for ⁴⁴⁵ a total of 36 different angles. The crystals were 40 to 70 cm from a ²⁵²Cf source, the greater



FIG. 10. (Color online) Our two-neutron angular correlation for ²⁵²Cf(sf) as a function of the angular separation. The open circles are based on 30 minutes of data taking and were adjusted for neutron acceptance. The Gagarski [4] and Pozzi [5] results are shown by the filled circles and stars, respectively. From the top to the bottom curves: 1600, 1200, 800, 550 and 425 keV.

⁴⁴⁶ distance was necessary due to the dimensions of the detector shielding. The Pozzi *et al.*⁴⁴⁷ experiment employed 14 cylindrical EJ-309 scintillators of dimension 7.62 cm diameter by 5.08
⁴⁴⁸ cm deep. The detectors were on a circle and their locations fixed, the face of each detector
⁴⁴⁹ was 20 cm from the source. Because the detectors were equally spaced, this configuration
⁴⁵⁰ enabled the measurement of 7 different angles in steps of 26°. The error bars are too small
⁴⁵¹ to show for the Pozzi data.

ENET (keV)	neutron pairs
425	18,320,600
550	$16,\!446,\!500$
800	12,499,500
1200	5,734,410
1600	2,594,990

TABLE III. Number of neutron pairs counted for all detector pairs, for the ENET values 425, 550, 800, 1200 and 1600 keV, for 252 Cf.

The data in the two reference experiments were not corrected for cross talk, so for 453 comparison, our data in Fig. 10 is not either. Cross talk explains why Pozzi's data points 454 at 26° are higher than the other data points. Indeed the detectors separated by 26° are 455 neighbors and do not have a large distance nor material between them to minimize the 456 number of neutrons scattering from one detector to the other.

⁴⁵⁷ By setting lower event selection boundaries with respect to the peak integral of PMT ⁴⁵⁸ signals in the offline analysis, we obtained the experimental dependence of the neutron-neutron ⁴⁵⁹ coincidence counts on the angle between the emitted neutrons for the equivalent neutron ⁴⁶⁰ energy thresholds (ENET) published in Ref. [4]: 425, 550, 800, 1200 and 1600 keV. When ⁴⁶¹ ENET increases, fewer correlated neutrons are counted. This explains why the uncertainties ⁴⁶² on the data points increase for larger ENET values.

Some remarks about the ENETs are in order. For a 425 keV neutron to register a count above the 425 keV ENET, it would take a single head-on collision with hydrogen. Any other scattering angle would result in the collision not being counted. Assuming neutrons could above the proton recoil and could thus be referred to as a proton recoil energy threshold. However, simulations show that most neutrons scatter multiple times within a single detector. Accounting for multiple collisions, the ENET could be reached by adding up the light output are produced by the different proton recoils. (Note that the sum of the light output is a nonlinear function of the proton recoil energy.) Therefore, we refer to this threshold as the equivalent are neutron energy threshold, and not as proton recoil energy threshold. ⁴⁷³ Previous measurements [1, 3] indicate a quasi-symmetric angular distribution. However, ⁴⁷⁴ our data, shown in Fig. 10, has a distribution that peaks at angles close to 0°. This peak is ⁴⁷⁵ the result of multiple scattering between detectors. Indeed, while neutrons are captured in ⁴⁷⁶ ³He tubes, they survive their scattering with protons in liquid scintillator cells and may be ⁴⁷⁷ recorded a second or even a third time in neighboring detectors, even though this probability ⁴⁷⁸ decreases as they lose energy [13].

Except for the region where neutron cross talk is important (angles close to 0°), the agreement between our measurements and the measurements of Gagarski [4] and Pozzi [5] tis reasonable. The differences can be attributed to the sensitivity of the neutron-neutron correlations analyzed by this method to the detector material and geometry, a sensitivity which plagues this method of measuring neutron-neutron correlations. They could also be related to differences in detector sensitivities, which are shown here in Fig. 8 but are not given in Refs. [4, 5]. The agreement of our data with the results of Refs. [4, 5] validates our data taking and analysis.

We note that the data shown in Fig. 10 is the raw data, not accounting for cross talk between detectors. The correction for cross talk will be studied in Sec. V.C.

489 B. Detector volume effects

In this section, we study the sensitivity of neutron-neutron correlations to detector volume. Here Because the detector volumes used in our analysis differs from those employed by Gagarski and Pozzi it is important to understand the sensitivity of the measurements to this effect. Here I to detector shielding, scintillation and the measurements and other parameters, but this is beyond the scope of this work.

It is obvious that neutrons will scatter fewer times in smaller detectors than in larger ones. As a result, for a given equivalent neutron energy threshold, the population of neutrons counted in a smaller detector (à la Gagarski) will be, on average, higher energy than the population of detected neutrons in a larger detector. To study the effect of detector size, we halved the dimensions of the detectors (5.08 cm diameter by 3.81 cm deep, instead of the 10.16 cm diameter by 7.62 cm deep used in the experiment) in our Monte Carlo simulations. Figure 11 shows the ratio of the resulting neutron-neutron angular correlations, where we arbitrarily set the ratio to 1 for a separation angle of 90°. The graphs show saddles



FIG. 11. (Color online) The ratio of two-neutron angular correlations for 252 Cf(sf) in a small detector relative to a large detector. Ratio arbitrarily set to 1 at 90°. The ratio shows the sensitivity of the correlations to the detector size based on FREYA simulations.

with local minima around 90°. Small (~ 35°) and large (~ 163°) separation angles lead to neutron-neutron correlations 8% larger than at 90°. This increase follows from the higher average energy of the neutron population detected by smaller detectors. Indeed, neutrons will scatter fewer times within a small detector than within a larger one. The scintillation light produced will thus be lower. For a given scintillation light threshold, some neutrons that produce enough light to be detected in a large detector will be below the threshold ⁵¹⁰ in a small detector and therefore pass through undetected. For angular separation below ⁵¹¹ 35°, neutron cross talk dominates and strongly depends on the distances between nearby ⁵¹² detectors.

Figure 11 shows that the size of the detector has an effect on the neutron-neutron angular 514 correlations. The distribution curvature will thus vary with detector size, making this method 515 detector-sensitive. Because this method is sensitive to detector geometry, differences between 516 the three results shown in Fig. 10, which all used different scintillator materials and different 517 size detectors, can be expected.

518 C. ²⁴⁰Pu(sf) measurements and cross talk correction

In this section, we describe our angular correlation measurement of ²⁴⁰Pu(sf), discuss our 519 $_{520}$ cross talk correction, and compare our results with earlier data measured by Marcath et⁵²¹ al. [6]. The measurements were carried out using a 4.5 gm sample of ²⁴⁰Pu (98% pure). Its initial intensity was 4,590 neutrons/s. Other plutonium isotopes accounted for less than 2%522 of the plutonium weight. The fraction of fission neutrons originating from these isotopes is 523 negligible, because of their relatively low spontaneous fission yields. Because the sample is 524 oxidized, ~ 14% of the neutrons emitted are from (α, n) reactions. However these neutrons 525 are emitted individually and thus do not generate correlations, except for contributions due 526 to neutron cross talk, which has been removed via the correction method described here. The 527 data analyzed here were collected by placing the ²⁴⁰Pu source in the center of the detection 528 ⁵²⁹ system for 23 hours.

The thresholds used in this analysis are not the equivalent neutron energy thresholds ⁵³⁰ required for our comparison to the Gagarski and Pozzi data but are, instead, electron ⁵³² equivalent energy thresholds E_{γ} to compare to the ²⁴⁰Pu(sf) measurements by Marcath [6]. ⁵³³ We will use electron equivalent thresholds in the remainder of this section.

Figure 12 shows the raw two-neutron angular correlation for ²⁴⁰Pu(sf). No neutron cross talk correction has yet been applied. There is a prominent peak at 0°. Table IV lists the number of correlated neutron pairs for all detector pairs as a function of the light output threshold LO.

⁵³⁸ We now discuss how we have tried to simulate and remove cross talk, essential for a ⁵³⁹ comparison to the Marcath data. There is no reliable experimental analysis that could



FIG. 12. (Color online) The two-neutron angular correlation for 240 Pu(sf) as a function of the angular separation before cross talk correction and for several light output thresholds. The data points are based on 23 hours of data taking and were adjusted for neutron acceptance.

⁵⁴⁰ isolate counts due to cross talk on an event-by-event basis. However, simulations can be ⁵⁴¹ used to remove integral cross talk counts from the experimental coincidences [6, 46, 47]. To ⁵⁴² study the effect of multiple scattering in our array, we modified the simulation so that, at ⁵⁴³ most, one fission neutron is emitted per spontaneous fission $P(\nu) = 0$ for $\nu \ge 2$, suppressing ⁵⁴⁴ coincidences originating from the simultaneous emission of multiple spontaneous fission ⁵⁴⁵ neutrons. The only coincidences in this case are due to individual neutrons registering ⁵⁴⁶ multiple counts in adjacent detectors. It is possible for two neutrons emitted from two

LO	(keVee) ne	eutron pairs
	100	1,993,380
	150	1,760,670
	200	$1,\!515,\!750$
	300	$762,\!531$
	400	$383,\!142$
	500	203,012

TABLE IV. Number of neutron pairs counted for all detector pairs, as a function of the light output threshold, for 240 Pu.

⁵⁴⁷ different spontaneous fissions to be counted in coincidence. However, even for our strong ⁵⁴⁸ californium source, the probability for such events is ~ 0.01 accidental coincidences in a 30 ⁵⁴⁹ minute measurement interval.

For these simulations, we collect the rates of false coincidences due to neutron cross talk for each pair of detectors. These rates are compared to the rates when full multiplicity distributions are modeled for spontaneous fission. The ratio of the single neutron rates to the rates with the full $P(\nu)$ gives the fraction of coincidences that contaminate the true neutron correlations.

The simulated cross talk contribution is shown in Fig. 13 as a function of the detector separation angle, as seen from the source. In the data, it is important to account for the sor scintillation light-dependent neutron detection efficiency of the detectors (see Sec. II B). Because of the energy-dependent PSD rejection and detector sensitivity to neutrons, the efficiency for detecting neutrons tends to decrease for lower scintillation light output. Neutron cross talk at large angles is not as strong here as in the Marcath data [6], due to the presence of large masses of low-Z materials around each detector in the array which effectively shields them from each other. For angles smaller than 30°, however, the correction is large, 37% to 68%, depending on LO.



FIG. 13. (Color online) Fraction of coincidences attributed to neutron cross talk as a function of the detector separation angle and for several light output thresholds.

Figure 14 shows our results for 240 Pu(sf) after correcting for cross talk. (Note the different scale on the *y*-axis relative to Fig. 12.) We also now compare to the Marcath data. At scale angles, less than 30°, the neutron-neutron correlation measurements appear to be scale slightly different from the Marcath data. This can be attributed to differences in detector



FIG. 14. (Color online) The cross talk and neutron acceptance corrected two-neutron angular correlation for ²⁴⁰Pu(sf) as a function of the angular separation and for several light output thresholds. The full circles, squares and triangles are based on 23 hours of data taking. The Marcath [6] measurements are shown with stars.

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⁵⁷¹ sensitivities, shown here in Fig. 8 but not reported in Ref. [6], to inaccurate modeling of ⁵⁷² either the scintillation material or the scintillator geometry for the cross talk correction, or to ⁵⁷³ the sample position uncertainty which affects the simulated cross talk. At low detector angles, ⁵⁷⁴ the cross talk contribution is very sensitive to small changes in the sample position. It could ⁵⁷⁵ also be attributed to an overprediction of the zero degree correlation in the FREYA simulation ⁵⁷⁶ of the neutron cross talk. The overall good agreement between data sets is encouraging ⁵⁷⁷ because our approach is completely independent, including different detectors, experimental ⁵⁷⁸ setups, and analyses.

In the remainder of the paper, multiple scattering corrections are applied to the neutronneutron correlations. To obtain data corrected for cross talk, it suffices to correct each data point by the factors given in Fig. 13.

582 VI. COMPARISON OF THE DATA TO FREYA SIMULATIONS

Using a customized [44] version of MCNPX 2.7.0 with the LLNL Fission Library/FREYA [29, 584 43, 45] turned on, we simulated neutron-neutron angular correlations using the detector 585 threshold to filter low energy neutrons, as done in previous analyses.

The first simulations are shown for the ²⁵²Cf(sf) source. The FREYA calculations are shown with open symbols in Fig. 15 while the full symbols are the data. The number of spontaneous fission events simulated was equivalent to 30 minutes of data taking. The energy-dependent experimental neutron detection efficiency was taken into account (see Fig. 4).

While the results do not match perfectly, FREYA qualitatively reproduces the experimental data. In particular, with the full detector simulation, the agreement with data is better than in Ref. [8] which concluded that there was no evidence for scission neutrons from the data. That conclusion is strengthened here with the most comprehensive ²⁵²Cf(sf) measurement to date.

⁵⁹⁶ Without FREYA turned on the distribution would be flat except for a peak at 0° due to ⁵⁹⁷ neutron cross talk. For light output thresholds below 300 keVee and angles smaller than ⁵⁹⁸ 25°, we observe deviations between measurements and simulations, likely due to the reasons ⁵⁹⁹ stated in Sec. V C, i.e. insufficient model details in the simulation, etc. Table V lists the ⁶⁰⁰ number of correlated neutron pairs for all detector pairs as a function of the light output ⁶⁰¹ threshold LO. The number of detected pairs for ²⁵²Cf is a factor of 9 greater than the number ⁶⁰² of detected pairs for ²⁴⁰Pu (see Table IV), which explains the higher statistics.



FIG. 15. (Color online) The cross talk and neutron acceptance corrected two-neutron angular correlation for $^{252}Cf(sf)$ as a function of the angular separation and for several light output thresholds.

LO (keVee) n	eutron pairs
100	18,595,000
150	15,871,400
200	13,468,700
300	6,916,880
400	$3,\!570,\!520$
500	1,940,640
600	$1,\!109,\!490$
700	662,943
800	412,261

TABLE V. Number of neutron pairs counted for all detector pairs, as a function of the light output threshold, for 252 Cf.

FREYA includes several physics-motivated model parameters. In particular, the parameter c_{04} x describes how the excitation energy is partitioned between the light, L, and heavy, H, c_{05} fission fragments. If the two fragments are in mutual thermal equilibrium, equal temperature, c_{06} $T_L = T_H$, the total excitation energy will, on average, be partitioned as $E_{\text{stat}} = \acute{E}_L^* + \acute{E}_H^*$ c_{07} according to the heat capacities of the fragments. The heat capacities are assumed to be c_{08} proportional to the corresponding Fermi-gas level density parameters a_L and a_H ,

$$\frac{\acute{E}_L^*}{\acute{E}_H^*} = \frac{a_L}{a_H} \,. \tag{6}$$

The observed neutron multiplicities suggest that the light fragment tends to be disproportionately excited [39]. Therefore the average excitation energy is modified in favor of the light fragment,

$$\overline{E}_L^* = x \acute{E}_L^* , \ \overline{E}_H^* = E_{\text{stat}} - \overline{E}_L^* ,$$
(7)

 $_{612}$ where the adjustable model parameter x is expected be larger than unity.

The simulations for ²⁵²Cf(sf) were based on a 'global' fit to a number of data sets: the ⁶¹⁴ Mannhart prompt fission neutron spectrum [48], prompt neutron multiplicity distribution ⁶¹⁵ [49], neutron multiplicity as a function of TKE [3], neutron multiplicity as a function of ⁶¹⁶ fragment mass [50], and average photon energy and multiplicity [51]. In particular, the ⁶¹⁷ neutron multiplicity as a function of fragment mass, $\nu(A)$, is sensitive to the *x* parameter. ⁶¹⁸ In this fit, x = 1.27 was found. This value of *x* means that the excitation energy of the light ⁶¹⁹ fragment is ~ 30% higher than that of the light fragment.

However, fewer data are available for ²⁴⁰Pu(sf) to fix the FREYA parameters. In particular, $\nu(A)$ data are available to tune the x parameter for ²⁴⁰Pu(sf). Therefore a default value $\nu(A)$ data are available to tune the x parameter for ²⁴⁰Pu(sf). Therefore a default value $\nu(A)$ data are available to tune the x parameter for ²⁴⁰Pu(sf). Therefore a default value $\nu(A)$ data are available to tune the x parameter for ²⁴⁰Pu(sf). Therefore a default value $\nu(A)$ data are available to tune the x parameter for ²⁴⁰Pu(sf). Therefore a default value $\nu(A)$ data are available to tune the x parameter for ²⁴⁰Pu(sf). Therefore a default value $\nu(A)$ data are available to tune the x parameter for ²⁴⁰Pu(sf). Therefore a default value $\nu(A)$ data are available to tune the x parameter for ²⁴⁰Pu(sf). Therefore, we can use our data to determine x $\nu(A)$ for ²⁴⁰Pu(sf).

To determine the value of x that agrees best with our ²⁴⁰Pu(sf) data, we compare the data to four different x values between 1.1 and 1.4 in Fig. 16. The number of fissions simulated with FREYA was equivalent to the 23 hours of data taking in the experiment. We see that increasing x effectively shifts and tilts the correlation from approximately equal intensity at 0° and 180° with x = 1.1 to a significantly higher correlation at 0° for x = 1.4. We note also that, in all cases, similarly for ²⁵²Cf(sf), increasing the strength of the correlation as the cutoff energy increases. Both behaviors can be explained by the characteristics of neutron evaporation.

The neutron-neutron correlation arises because, while the neutrons are emitted isotropically in the rest frame of the fragment, the boost to the laboratory frame means that the neutrons will preferentially follow the fragments. Thus if one neutron is emitted from each fragment, the boost the preference of the same fragment, the angular separation is 0° . The 0° correlation includes two parts: both neutrons emitted from the light fragment and both emitted from the heavy fragment. Since the light fragment is higher velocity to conserve momentum, the correlation from two-neutron emission from the light fragment at 0° is larger. The three contributions combine to give peaks at 0° and 180° with a dip at 90° .



FIG. 16. (Color online) The cross talk and neutron acceptance corrected two-neutron angular correlation for 240 Pu(sf) as a function of the angular separation and for several light output thresholds. FREYA calculations with x = 1.1, 1.2, 1.3 and 1.4 are also shown.

The light fragment also emits neutrons with larger kinetic energy on average. Therefore, increasing x, which gives even more excitation energy to the light fragment while removing it from the heavy fragment, increases the correlation at 0° while decreasing it at 180°. Likewise, increasing the neutron energy threshold increases the average energy of the neutrons that remain to form the correlation. Thus the higher the neutron energy threshold, the larger the bias toward emission from the light fragment and the higher the 0° correlation relative to the back-to-back correlation at 180°. In addition, the higher energy cutoff would preferentially select neutrons that were emitted in the direction of the boost rather than those opposite the boost direction which would enhance the correlation as the energy increases.

We note that there are qualitative differences in the ²⁵²Cf(sf) and ²⁴⁰Pu(sf) correlations due 657 658 to the different average neutron multiplicities as well. Since the average neutron multiplicity $_{659}$ of $^{252}Cf(sf)$ is ~ 3.76, each fragment can emit more than one neutron and any two emitted ⁶⁶⁰ neutrons can be used to form the correlation function. On the other hand, the average ⁶⁶¹ neutron multiplicity of ²⁴⁰Pu(sf) is ~ 2.1 so that, on average, the neutron-neutron correlation ⁶⁶² is formed from the only neutrons emitted during the fission. In addition, the average ⁶⁶³ neutron energy of neutrons emitted from ${}^{252}Cf(sf)$ is higher than those from ${}^{240}Pu(sf)$ so that increasing the energy threshold is more likely to result in two peaks of equal strength for ²⁵²Cf(sf) than for ²⁴⁰Pu(sf). These characteristics can be observed in both the simulations ⁶⁶⁶ and the data. The curves in Figs. 15-16, as well as Fig. 18, can be compared to the angular ⁶⁶⁷ correlations obtained by running the standalone FREYA code. Those are shown for ²⁵²Cf(sf) ⁶⁶⁸ and ²⁴⁰Pu(sf) in Fig. 17. With increasing kinetic energy thresholds, we observe that the peak ⁶⁶⁹ at 0° rises whereas the peak at 180° decreases. This is more noticeable for ²⁴⁰Pu(sf) than for ²⁵²Cf(sf) due to the former's lower neutron multiplicity, as discussed above. FREYA is thus 672 consistent with the above observations.

An examination of the results in Fig. 16 shows that x = 1.3 gives the optimal value compared to the ²⁴⁰Pu(sf) angular correlation data. This x value is quite close to the one determined from the global fit to ²⁵²Cf(sf). Figure 18 shows the comparison of our ²⁴⁰Pu(sf) data to FREYA calculations with x = 1.3. The agreement of the model calculations with the data after adjustment of x is quite good. The quality of the comparison of the simulations and the data again leave no room for a scission neutron contribution for this nucleus. Table IV lists the number of correlated neutron pairs for all detector pairs as a function of the light output threshold LO.



FIG. 17. (Color online) The two-neutron angular correlation for 252 Cf(sf) and 240 Pu(sf) as a function of the angular separation, for several neutron kinetic energies. These curves were obtained by running FREYA in standalone mode, without transporting the neutrons and photons to the detectors. A value of x = 1.3 was used for 240 Pu(sf).

⁶⁸¹ We have adjusted x to the measured ²⁴⁰Pu(sf) neutron-neutron angular correlation data ⁶⁸² assuming it is single-valued, an assumption common to all isotopes in FREYA. However, ⁶⁸³ comparison with ²⁵²Cf(sf) data on the neutron multiplicity as a function of fragment mass ⁶⁸⁴ suggests that x should be mass dependent. Modeling x as a function of fragment mass may ⁶⁸⁵ improve the overall comparison of the angular correlation data with the simulations.



FIG. 18. (Color online) The cross talk and neutron acceptance corrected two-neutron angular correlation for 240 Pu(sf) as a function of the angular separation and for several light output thresholds. Simulations with x = 1.3 are shown, see Eq. (7).

686 VII. USING TIME-OF-FLIGHT CUTOFF TO FILTER NEUTRONS

In Secs. III A and V B, we pointed out the disadvantages of using a detector threshold to measure neutron-neutron correlations. This method of filtering out low energy neutrons detector dependent, which impedes direct comparisons between measurements taken using different detectors. In this section, we analyze the correlations using time-of-flight to determine the neutron kinetic energy. This method, described in Sec. III B, to filter neutrons below a kinetic energy threshold is truly detector independent.

In the Monte Carlo simulations shown below, we account for the energy-dependent experimental neutron acceptance shown in Fig. 19. For low light output, the neutron acceptances are larger than in Fig. 4. Indeed, to determine particle type, events are now classified by combining not only PSD but also time-of-flight, so that the neutron identification region (magenta or light gray outline) in Fig. 3 can be broadened: a detection is identified as a neutron based on the time since the last photon was detected and on whether it falls within the positive neutron identification region. Because of the larger positive neutron identification region, the fraction of detections classified as neutrons also rises.



FIG. 19. (Color online) Acceptance of neutron pulses as a function of scintillation light output and averaged over all detector channels. Bars indicate the dispersions around the means, from ₁ channel-to-channel variations.

Analyzing the same 252 Cf(sf) data, we obtain the angular correlation shown in Fig. 20. Table VI lists the number of correlated neutron pairs for all detector pairs as a function of the neutron kinetic energy E_{kin} . For angles smaller than 30°, the correlations obtained by ros simulations are properly corrected for neutron cross talk, which confirms the validity of the ror correction method. However, the distributions measured experimentally are not properly ros corrected, especially at lower neutron kinetic energies. This is likely because the model ros inadequately represents details of the experimental setup, as discussed earlier. Therefore, ruo this angular region cannot be trusted until neutron cross talk can be better modeled.

The correlations in Fig. 20 can be directly compared to the ones in Fig. 17(a) calculated viz using FREYA as a standalone code, i.e. without neutron transport to and through the detectors.

TABLE VI. Number of neutron pairs counted for all detector pairs, as a function of the neutron kinetic energy $E_{\rm kin}$, for ²⁵²Cf.

$E_{\rm kin}$	(keV)	neutron pairs
	400	5,354,740
	600	4,968,180
	900	4,460,580
	1200	3,775,790
	1500	$2,\!928,\!350$
	1800	$2,\!134,\!600$
	2100	$1,\!506,\!130$
	2400	$1,\!047,\!350$
	2700	726,013
	3000	$503,\!140$
	3300	349,751
	3600	244,999

714 **716**



FIG. 20. (Color online) The cross talk and neutron acceptance corrected two-neutron angular correlation for ²⁵²Cf(sf) as a function of the angular separation, for several neutron kinetic energies. The neutron kinetic energy is determined from the neutron time-of-flight using a spontaneous fission photon trigger. FREYA simulations are also shown for the same kinetic energies. $\overset{}{42}$

In Fig. 15, a detector threshold is imposed to set the minimum neutron kinetic energy required for detection. Most neutrons with the specified minimum neutron kinetic energy are, however, not recorded by the detector. Indeed, only those with the rare head-on collisions on hydrogen will produce a proton recoil with enough energy to produce sufficient scintillation light to be detected. For neutrons with twice the specified minimum neutron kinetic energy, light of them will generate enough light to be counted. In Fig. 20 on the other hand, time-of-flight is used to determine the neutron kinetic energy, and many more neutrons close to the specified kinetic energy will thus be detected.

Higher energy neutrons are more strongly correlated than lower energy neutrons. Because r26 the average energy of the neutron population measured by the detector threshold method is r27 higher than that measured by the time-of-flight method, we expect to observe a stronger r28 correlation employing a detector threshold.

Figure 21 directly compares the two methods to filter neutrons. The correspondence r30 between the detector threshold LO and the neutron kinetic energy $E_{\rm kin}$ was taken from r31 Eq. (2). The detector threshold neutron filter produces the curves with the open symbols r32 and the curves with the full symbols result from the data processed with the time-of-flight r33 neutron filter. The former curves exhibit greater curvatures than the latter ones, confirming r34 that the detector threshold method filters out more low energy neutrons to produce a neutron r35 population of higher average energy.

In Figs. 15 and 20, we observe that FREYA agrees well with both ways of filtering neutrons. The agreement with the experimental data is better than in Ref. [8] where FREYA was used as a standalone code. This is because FREYA is embedded in a radiation transport code that accounts for neutron kinematics effects within the detectors, whereas a standalone calculation (740) ignores them.



FIG. 21. (Color online) The cross talk and neutron acceptance corrected two-neutron angular correlation for 252 Cf(sf) as a function of the angular separation, using either light output threshold (LO) or time-of-flight ($E_{\rm kin}$) as a neutron filter.

The ²⁴⁰Pu(sf) data was analyzed using the same time-of-flight method. The results are r42 shown in Fig. 22. Table VII lists the number of correlated neutron pairs for all detector r43 pairs as a function of the neutron kinetic energy $E_{\rm kin}$. Because of the low neutron yield

TABLE VII. Number of neutron pairs counted for all detector pairs, as a function of the neutron kinetic energy $E_{\rm kin}$, for ²⁴⁰Pu.

$E_{\rm kin}$	(keV)	neutron pairs
	400	639,191
	600	605,160
	900	555,991
	1200	469,720
	1500	357,802
	1800	$254,\!164$
	2100	$174,\!199$
	2400	117,258
	2700	78,218

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⁷⁴⁶ of the source, the angular distributions above a neutron kinetic energy 2700 keV were not ⁷⁴⁷ statistically significant. The most scintillation light a 2700 keV neutron can produce is about ⁷⁴⁸ 828 keVee, which lies above the top distributions in Fig. 18. The correlations in Fig. 22 can ⁷⁴⁹ be directly compared to those in Fig. 17(b) calculated using FREYA as a standalone code, i.e. ⁷⁵⁰ without modeling the detector response using MCNPX.



FIG. 22. (Color online) The cross talk and neutron acceptance corrected two-neutron angular correlation for 240 Pu(sf) as a function of the angular separation. The neutron kinetic energy is determined from the neutron time-of-flight using a spontaneous fission photon trigger. FREYA simulations are also shown for the same kinetic energies.

751 VIII. CONCLUSIONS

We have measured the angular distributions of correlated neutrons emitted by spontaneous ⁷⁵² fission of ²⁵²Cf and ²⁴⁰Pu. To validate our experimental results, our ²⁵²Cf(sf) and ²⁴⁰Pu(sf) ⁷⁵⁴ measurements were compared to previous measurements [4–6]. The agreement is overall ⁷⁵⁵ reasonable. Differences can be attributed to the measurement method, which imposes a ⁷⁵⁶ threshold on the scintillation light pulse to reject events. We show that this method depends ⁷⁵⁷ on the detectors geometry and scintillation materials. We propose a second method to ⁷⁵⁸ measure the neutron-neutron angular distributions based on time-of-flight. This method has ⁷⁵⁹ the advantage of being detector independent. Angular distributions of correlated neutrons ⁷⁶⁰ are shown using this time-of-flight approach for both isotopes.

To correct the neutron-neutron angular distributions from neutrons scattering multiple times between scintillators, a neutron cross talk correction is also presented.

The event-by-event fission generator FREYA, together with the LLNL Fission Library, has been integrated into the Monte Carlo codes MCNP6.2 and MCNPX2.7.0. The combination of a physics-based fission event generator and an established radiation transport code leads to new capabilities: the simulation of correlations that conventional neutron Monte Carlo codes ref cannot predict. Using these codes, we were able to reproduce the experimentally-measured distributions.

The asymmetry in the measured neutron-neutron angular distributions can be predicted by FREYA. The shape of the correlation function depends on how the excitation energy is partitioned between the two fission fragments. Experimental data suggest that the lighter fragment is disproportionately excited. The measured asymmetry enabled us to adjust the FREYA parameter x in ²⁴⁰Pu, which controls the energy partition between the fragments and is so far inaccessible in other measurements. In addition, the good agreement between the FREYA simulations and the high quality data of our analysis suggests a negligible contribution from scission neutrons, in agreement with the conclusions of Ref. [8].

Recent advances in scintillating materials have improved discrimination between neutrons and photons for low scintillation light outputs. In the future, the authors plan on using these materials to better capture the full spectra of ²⁵²Cf(sf) and ²⁴⁰Pu(sf).

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