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Y. K. Tanaka *et al.* (η -PRiME/Super-FRS Collaboration)

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Missing-mass spectroscopy of the $^{12}\text{C}(p, d)$ reaction near the η' -meson production threshold

Y. K. Tanaka,^{1,*} K. Itahashi,² H. Fujioka,³ Y. Ayyad,⁴ J. Benlliure,⁵ K.-T. Brinkmann,⁶ S. Friedrich,⁶ H. Geissel,^{6,7} J. Gellanki,⁸ C. Guo,⁹ E. Gutz,⁶ E. Haettner,⁷ M. N. Harakeh,⁸ R. S. Hayano,¹ Y. Higashi,¹⁰ S. Hirenzaki,¹⁰ C. Hornung,⁶ Y. Igarashi,¹¹ N. Ikeno,¹² M. Iwasaki,² D. Jido,¹³ N. Kalantar-Nayestanaki,⁸ R. Kanungo,¹⁴ R. Knoebel,^{6,7} N. Kurz,⁷ V. Metag,⁶ I. Mukha,⁷ T. Nagae,³ H. Nagahiro,¹⁰ M. Nanova,⁶ T. Nishi,² H. J. Ong,⁴ S. Pietri,⁷ A. Prochazka,⁷ C. Rappold,⁷ M. P. Reiter,⁷ J. L. Rodríguez-Sánchez,⁵ C. Scheidenberger,^{6,7} H. Simon,⁷ B. Sitar,¹⁵ P. Strmen,¹⁵ B. Sun,⁹ K. Suzuki,¹⁶ I. Szarka,¹⁵ M. Takechi,¹⁷ I. Tanihata,^{4,9} S. Terashima,⁹ Y. N. Watanabe,¹ H. Weick,⁷ E. Widmann,¹⁶ J. S. Winfield,⁷ X. Xu,⁷ H. Yamakami,³ and J. Zhao⁹

(η -PRiME/Super-FRS Collaboration)

¹*The University of Tokyo, 7-3-1 Hongo, Bunkyo, 113-0033 Tokyo, Japan*

²*Nishina Center for Accelerator-Based Science, RIKEN, 2-1 Hirosawa, Wako, 351-0198 Saitama, Japan*

³*Kyoto University, Kitashirakawa-Oiwakecho, Sakyo-ku, 606-8502 Kyoto, Japan*

⁴*RCNP, Osaka University, 10-1 Mihogaoka, Ibaraki, 567-0047 Osaka, Japan*

⁵*Universidade de Santiago de Compostela, 15782 Santiago de Compostela, Spain*

⁶*Universität Giessen, Heinrich-Buff-Ring 16, 35392 Giessen, Germany*

⁷*GSI Helmholtzzentrum für Schwerionenforschung GmbH, Planckstraße 1, 64291 Darmstadt, Germany*

⁸*KVI-CART, University of Groningen, Zernikelaan 25, 9747 AA Groningen, the Netherlands*

⁹*Beihang University, Xueyuan Road 37, Haidian District, 100191 Beijing, China*

¹⁰*Nara Women's University, Kita-Uoya Nishi-Machi, 630-8506 Nara, Japan*

¹¹*KEK, 1-1 Oho, Tsukuba, 305-0801 Ibaraki, Japan*

¹²*Tottori University, 4-101 Koyamacho-minami, 680-8551 Tottori, Japan*

¹³*Tokyo Metropolitan University, 1-1 Minami-Osawa, Hachioji, 192-0397 Tokyo, Japan*

¹⁴*Saint Mary's University, 923 Robie Street, Halifax, Nova Scotia B3H 3C3, Canada*

¹⁵*Comenius University Bratislava, Mlynská dolina, 842 48 Bratislava, Slovakia*

¹⁶*Stefan-Meyer-Institut für subatomare Physik, Boltzmannsgasse 3, 1090 Vienna, Austria*

¹⁷*Niigata University, 8050 Ikarashi 2-no-cho, Nishi-ku, 950-2181 Niigata, Japan*

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Excitation-energy spectra of ^{11}C nuclei near the η' -meson production threshold have been measured by missing-mass spectroscopy using the $^{12}\text{C}(p,d)$ reaction. A carbon target has been irradiated with a 2.5 GeV proton beam supplied by the synchrotron SIS-18 at GSI to produce η' meson bound states in ^{11}C nuclei. Deuterons emitted at 0° in the reaction have been momentum-analyzed by the fragment separator (FRS) used as a high-resolution spectrometer. No distinct structure due to the formation of η' -mesic states is observed although a high statistical sensitivity is achieved in the experimental spectra. Upper limits on the formation cross sections of η' -mesic states are determined, and thereby a constraint imposed on the η' -nucleus interaction is discussed.

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I. INTRODUCTION

Understanding hadron masses is one of the major subjects in contemporary hadron physics. Studies of the light pseudoscalar mesons are of particular importance, since they have close relations to fundamental symmetries in quantum chromodynamics (QCD). The flavor-octet mesons are considered to be Nambu-Goldstone bosons associated with spontaneous breaking of chiral symmetry, leading to relatively small masses of the π , K , and η mesons. In contrast, the η' meson has an exceptionally large mass of $958 \text{ MeV}/c^2$, which has attracted interest known as the “U(1) problem” [1]. Theoretically,

the large η' mass can be explained by the explicit breaking of $U_A(1)$ symmetry owing to quantum anomaly effects in QCD [2, 3]. This anomaly effect on the η' mass is expected to manifest itself under the presence of chiral symmetry breaking [4, 5].

In finite baryon density, properties of the mesons may be modified from those in the vacuum due to partial restoration of chiral symmetry [6–8]. For the η' meson, the reduction of the mass is expected through a weakening of the anomaly effect [5] and also predicted in various theoretical models. For example, about $150 \text{ MeV}/c^2$ reduction at the nuclear saturation density is predicted by the Nambu–Jona-Lasinio (NJL) model [9, 10], $80 \text{ MeV}/c^2$ by the linear sigma model [11], and $37 \text{ MeV}/c^2$ by the quark meson coupling (QMC) model [12]. Investigation of such a modification would yield novel insights into the mechanism of the meson mass generation as well as the vacuum structure of QCD.

* E-mail: y.tanaka@gsi.de; Present address: GSI Helmholtzzentrum für Schwerionenforschung GmbH, Planckstraße 1, 64291 Darmstadt, Germany

Meson-nucleus bound states open a unique possibility of directly probing in-medium meson properties. A well-established example of such systems is the deeply-bound π^- states in heavy nuclei, where a π^- meson is bound near the nuclear surface by the superposition of the attractive Coulomb interaction and the repulsive s -wave strong interaction. These states have been discovered and studied in missing-mass spectroscopy of the $(d, {}^3\text{He})$ reaction [13–15]. A large overlap between a π^- meson and a nucleus in well-defined quantum bound states allows the extraction of information on a modification of the isovector part of the s -wave pion-nucleus potential, leading to a quantitative evaluation of partial restoration of chiral symmetry at finite nuclear density [16–19].

In the case of neutral mesons [8], bound states may be formed only via the strong interaction, if the attraction between a meson and a nucleus is strong enough. In-medium meson properties, the mass shift $\Delta m(\rho_0)$ and width $\Gamma(\rho_0)$ at the nuclear saturation density ρ_0 , are incorporated in the meson-nucleus potential as $U(r) = (V_0 + iW_0)\rho(r)/\rho_0$ by relations $V_0 = \Delta m(\rho_0)$ and $W_0 = -\Gamma(\rho_0)/2$, where $\rho(r)$ denotes the nuclear density distribution. A small imaginary potential compared with the real part, i.e., $|W_0| < |V_0|$, is required for the existence of bound states as discrete levels. This condition may be satisfied for the η' meson, as described below.

Very limited information on the η' -nucleus interaction is currently available. On the theoretical side, the predictions for the η' -mass reduction [9–12] suggest the real part of the potential V_0 in the range from -150 MeV to -37 MeV. On the experimental side, the CBELSA/TAPS collaboration deduced the real part as $V_0 = -(39 \pm 7(\text{stat}) \pm 15(\text{syst}))$ MeV from η' momentum distributions and excitation functions in η' photo-production on nuclear targets [20, 21]. They also evaluated the imaginary part of $W_0 = -(13 \pm 3(\text{stat}) \pm 3(\text{syst}))$ MeV by measuring transparency ratios as a function of the mass number of the target nuclei [22] and as a function of η' momentum [23]. Such a small imaginary part relative to the real part implies the possibility of observing a bound state as a distinct peak structure. In the meantime, the real part of the scattering length for the η' -proton interaction has been extracted from measurements of the $pp \rightarrow pp\eta'$ reaction close to its threshold to be 0.00 ± 0.43 fm [24], corresponding to an η' -nucleus potential depth of $|V_0| < 38$ MeV at the nuclear density of 0.17 fm^{-3} within the low-density approximation.

Experimental programs to search for η' -mesic nuclei have recently been started, aiming at directly studying the in-medium properties of the η' meson. A one-nucleon pickup reaction, for example (p, d) or (γ, p) , at forward angles is preferable to produce the η' -nucleus bound states, because the momentum transfer of such a reaction can be rather small. Spectroscopy experiments of the ${}^{12}\text{C}(\gamma, p)$ reaction [25] using high-energy photon beams were proposed by the LEPS2 collaboration at the SPring-8 facility [26] and by the BGO-OD collaboration at the ELSA accelerator [27]. The results of these exper-

iments are thus far not available.

We proposed an experimental search for η' -mesic nuclei with missing-mass spectroscopy of the ${}^{12}\text{C}(p, d)$ reaction near the η' production threshold [28]. The kinetic energy of the proton beam was chosen to be 2.5 GeV, slightly above the threshold energy for the elementary process $n(p, d)\eta'$ of 2.4 GeV. The momentum transfer of this reaction at 0° is moderate (~ 500 MeV/ c) at 2.5 GeV. An inclusive measurement of the forward-emitted deuterons allows the analysis of the overall (p, d) spectrum without any assumption on decay processes of η' -mesic nuclei.

The formation cross section of the η' -mesic nuclei via the ${}^{12}\text{C}(p, d){}^{11}\text{C} \otimes \eta'$ reaction has been theoretically calculated in Ref. [29] for various sets of (V_0, W_0) , the real and imaginary parts of the η' -nucleus potential. Population of η' -mesic states coupling with neutron hole states has been predicted, depending on the assumed potential. Distinct peak structures are expected in the excitation spectra particularly near the η' production threshold because of the enhanced excited states due to the finite momentum transfer of the reaction [29].

Physical background such as quasi-free meson production, $pN \rightarrow dX$ ($X = 2\pi, 3\pi, 4\pi, \omega$), also contributes to the experimental spectrum as a continuum. The cross section of the above background process was estimated to be 2–3 orders of magnitude larger than that of the formation of the η' -mesic states [28]. To overcome such a small signal-to-background ratio, we aimed at achieving an extremely high statistical sensitivity with relative errors of $< 1\%$ in the spectrum. An inclusive simulation has shown that observing peak structures near the threshold is feasible under a realistic experimental condition for a strongly attractive potential $V_0 \lesssim -100$ MeV [28].

We carried out the experiment in 2014. While its results have been briefly reported elsewhere [30], in this paper a full description of the experiment and analysis including discussions based on additional theoretical calculations is presented. First, the experimental method and performed measurements are introduced (Sec. II), and next the data analysis to obtain the excitation-energy spectra is described in detail (Sec. III). The results of a statistical analysis for the obtained spectra are explained (Sec. IV), followed by discussions of the η' -nucleus interaction and future plans for a follow-up experiment with higher sensitivity (Sec. V). Finally, a conclusion is given in Sec. VI.

II. EXPERIMENT

A missing-mass spectroscopy experiment using the ${}^{12}\text{C}(p, d)$ reaction was performed near the η' production threshold at GSI, Darmstadt, Germany. A 2.5 GeV proton beam impinged on a carbon target, and the emitted deuterons at 0° were momentum-analyzed to obtain missing masses in the reaction. In addition, elastic proton-deuteron scattering was measured for the calibration of

the experimental system.

A. Proton beam

Proton beams were supplied by the synchrotron SIS-18. Two kinetic energies were employed: 2499.1 ± 2.0 MeV for the measurement of the $^{12}\text{C}(p,d)$ reaction and 1621.6 ± 0.8 MeV for the calibration with proton-deuteron elastic scattering. These energies were determined by measuring precisely the revolution frequencies of the beams in the synchrotron. The accelerated beams were extracted in a slow extraction mode with a spill length of 4 (1) seconds and a cycle of 7 (4) seconds for 2.5 (1.6) GeV. The beams were focused at the experimental target, where a typical spot size was ~ 1 mm (horizontal) $\times 3$ mm (vertical).

The beam intensity was $\sim 10^{10}/\text{s}$, measured in front of the target by the SEETRAM detector [31] inserted on the beam axis. This detector was used only during a short dedicated measurement for an absolute normalization of the cross sections to avoid unnecessary material near the beam axis. Plastic scintillation counters placed off axis around the target continuously monitored relative changes in the luminosity by counting scattered particles from the target.

B. Target

Three targets were mounted on a movable ladder at the entrance position of the spectrometer. A natural carbon target with an areal density of 4115 ± 1 mg/cm² was used for the measurement of the $^{12}\text{C}(p,d)$ reaction. Deuterated polyethylene (CD₂) targets with areal densities of 1027 ± 2 mg/cm² and 4022 ± 9 mg/cm² were used for the calibration via the proton-deuteron elastic $D(p,d)p$ reaction. These targets had a cylindrical shape with a diameter of 2 cm.

C. Spectrometer and detector system

The fragment separator (FRS) [32] was used as a high-resolution magnetic spectrometer to precisely analyze the momenta of deuterons emitted at 0° in the (p,d) reactions. The FRS has four stages, as schematically depicted in the top panel of Fig. 1. Each stage consists of a 30° -bending dipole magnet, quadrupole doublet and triplet magnets. Such a configuration provides considerable flexibility to realize various ion-optics modes with high momentum resolving powers.

We developed a special ion-optical mode of the FRS, which is momentum-achromatic at the central focal plane (F2) and dispersive at the final focal plane (F4), as illustrated in the middle and bottom panels of Fig. 1. The achromatic section from the target to F2 was used to select particles originating from reactions in the target.

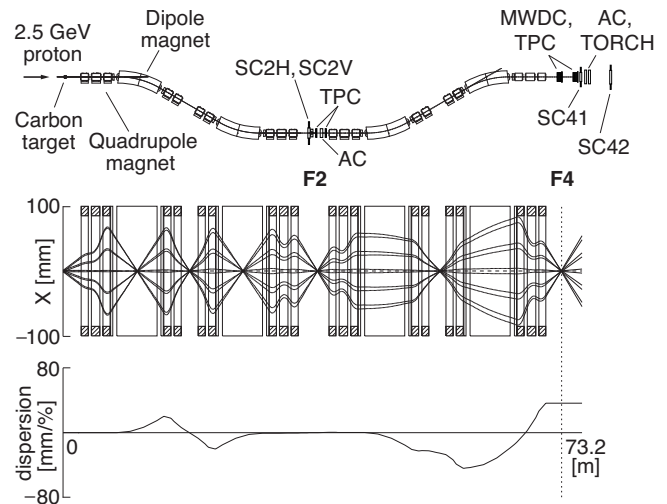


FIG. 1. (Top panel) A schematic view of the experimental setup with the FRS. A 2.5 GeV proton beam impinged on a carbon target. Deuterons emitted in the $^{12}\text{C}(p,d)$ reaction were momentum analyzed at F4 and the tracks were reconstructed from measurements by multi-wire drift chambers (MWDCs). Sets of 5 mm-thick plastic scintillation counters (SC2H, SC2V, and SC41) and a 20 mm-thick one (SC42) were installed at F2 and F4 for time-of-flight (TOF) measurements. Čerenkov detectors (ACs and TORCH) and time projection chambers (TPCs) were installed but not used in the present analysis. (Middle panel) Horizontal beam trajectories with the specially-developed optics mode based on calculated third-order transfer matrices. Initial positions and angles are taken from $\{-1, 1\}$ mm \times $\{-8, -4, 0, 4, 8\}$ mrad, and a momentum at the central value. (Bottom panel) A momentum-dispersion curve of this optics mode.

Secondary background produced by the non-interacting primary beam dumped near the exit of the first dipole magnet was thus rejected. The momenta of the deuterons were then analyzed in the dispersive section from F2 to F4, where a designed momentum resolving power was about 3.8×10^3 . The dispersion was kept relatively small throughout the whole spectrometer to have a wide momentum acceptance. At F4 the dispersion was 35.1 mm/%.

The detection system is depicted in the top panel of Fig. 1. Two sets of multi-wire drift chambers (MWDCs) were installed at F4 to reconstruct the deuteron tracks and obtain their momenta. A MWDC had eight layers of detection planes, each consisting of 48 anode wires with a spacing of 5 mm. The active area of each layer was 24 cm (horizontal) \times 14 cm (vertical). The wires in the first four layers were aligned vertically, while those in the next two and the last two layers were inclined by -15° and $+15^\circ$, respectively. The wire positions in the neighboring layers with the same wire angle were shifted from each other by a half length of the spacing. These MWDCs were operated with a gas mixture of 76% argon, 20% isobutane, and 4% dimethoxymethane. The signals from the anode wires were processed by preamplifier-shaper-

discriminator chips, and the resulting timing information was recorded by time-to-digital converters.

Plastic scintillation counters (SC2H, SC2V, SC41, and SC42) were installed for time-of-flight (TOF) measurements to distinguish signal deuterons with a velocity $\sim 0.84c$ from background protons with $\sim 0.95c$. SC2H and SC2V had an active area of 6 cm (horizontal) \times 6 cm (vertical) and a thickness of 5 mm, whereas SC41 had 24 cm (horizontal) \times 6 cm (vertical) and the same thickness. A plastic scintillator with an area of 50 cm (horizontal) \times 35 cm (vertical) and a thickness of 2 cm was adopted for SC42, which was located at 5.16 m downstream of SC41. Each of these scintillators was equipped with two photomultipliers. The anode signals were recorded by a 1-GHz sampling digitizer, and the discriminated timing information by a time-to-digital converter.

In addition, aerogel Čerenkov detectors (ACs) and a total-reflection Čerenkov detector (TORCH) were installed for confirmation of the particle identification. The ACs had silica aerogel with a refractive index of 1.17 [33] as a radiator, corresponding to a threshold velocity of $0.85c$. TORCH was equipped with a quartz radiator with a refractive index of 1.5, hence the maximum detection velocity of $\sim 0.89c$ due to designed insensitivity to totally-reflected photons [34]. Time projection chambers (TPCs) [35], the standard beam diagnostics devices of the FRS, were also placed at F2 and F4 for the purpose of the online beam tuning. These Čerenkov detectors and TPCs are not used in the offline analysis described in this paper.

D. Trigger condition for data acquisition

In the measurements of the $^{12}\text{C}(p,d)$ reaction, the total rate of charged particles at F4 was ~ 250 kHz. The top panel of Fig. 2 shows a histogram of TOF between SC2H and SC41 versus one between SC41 and SC42 for all particles reaching F4, obtained with a data-acquisition system triggered by the SC41 signal. Concentration of events corresponding to deuterons and protons are seen at the expected locations and clearly identified. The ratio of the number of deuterons to that of protons is about 1 to 200, indicating that the deuteron and proton rates at F4 were ~ 1 kHz and 250 kHz, respectively.

In order to reject the background protons at the hardware level, we employed a TOF-based trigger for the data-acquisition system by requiring a coincidence of the SC2H and SC41 signals within 15 ns around a relative timing of the deuterons. A TOF histogram with this trigger is shown in the middle panel of Fig. 2, demonstrating efficient rejection of the background protons at the trigger level. The main source of the remaining background events was accidental multiple-hit protons at SC2H, which are randomly distributed in TOF between SC2H and SC41. The multiple-hit protons are actually observed in the recorded signal waveforms of SC2H, as

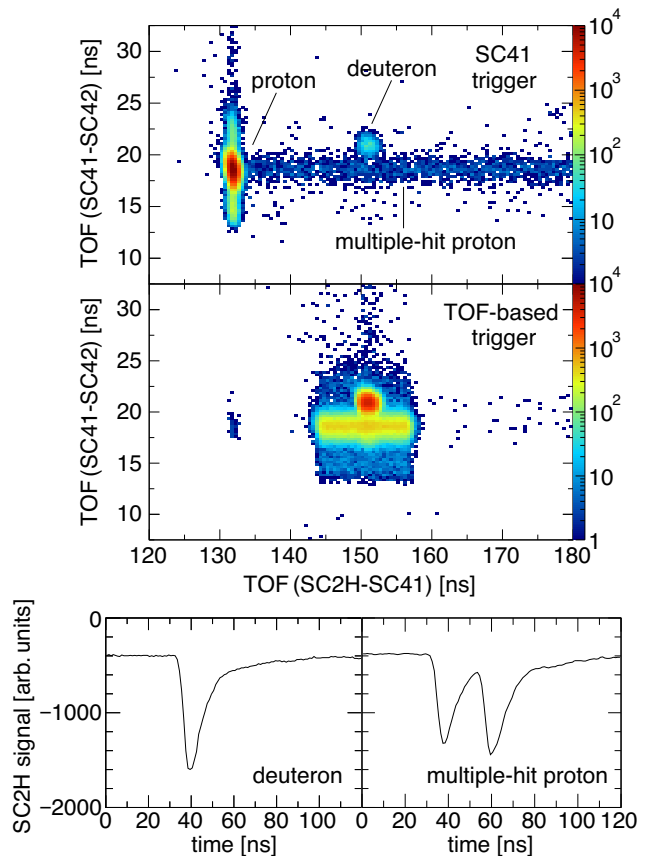


FIG. 2. TOF between SC2H and SC41 and between SC41 and SC42 recorded with a data acquisition system triggered by the SC41 signals (top) and by the TOF-based coincidence between the SC2H and SC41 signals (middle). Typical signal waveforms of SC2H are shown for the deuteron (bottom left) and the multiple-hit proton (bottom right) events based on the TOFs.

shown in the bottom panels of Fig. 2, and are rejected later in the data analysis (Sec. III A). The live rate of the acquisition system varied typically between 30%–40%, and the data were recorded with a rate of about 10^3 events/s.

E. Summary of measurements

The experimental conditions are summarized in Table I. Three types of measurements have been performed, which are explained as follows.

The production measurements of the $^{12}\text{C}(p,d)$ reaction were carried out by using the 2.5 GeV proton beam impinging on the carbon target. The emitted deuterons had a momentum of 2814.4 ± 2.4 MeV/c at the η' production threshold after the energy loss in the target. To cover a wide excitation-energy region, measurements were conducted at seven central momenta of the FRS by scaling the whole magnetic field with factors from $f = 0.980$ to

TABLE I. Experimental conditions of the performed measurements. The first seven rows show production runs of the $^{12}\text{C}(p,d)$ reaction at the proton energy of 2.5 GeV with seven momentum settings of the FRS. The next nine rows are calibrations using the elastic $\text{D}(p,d)p$ reactions at 1.6 GeV with nine FRS settings. One set of the calibration took about 0.5 hours, and the number of repetitions is given in the last column. The last row shows measurements of the elastic $\text{D}(p,d)p$ scattering at 2.5 GeV.

Reaction	Proton energy (MeV)	Target	Central momentum of FRS (MeV/c)	Scaling factor f for magnets	Duration
$^{12}\text{C}(p,d)$	2499.1 ± 2.0	C (4115 ± 1 mg/cm 2)	2771.4	0.980	9.7 hour
			2779.9	0.983	9.3 hour
			2785.6	0.985	9.9 hour
			2799.7	0.990	10.9 hour
			2828.0	1.000	23.0 hour
			2856.3	1.010	5.9 hour
			2884.6	1.020	2.0 hour
$\text{D}(p,d)p$	1621.6 ± 0.8	CD_2 (1027 ± 2 mg/cm 2)	2771.4	0.980	5 set
			2779.9	0.983	2 set
			2785.6	0.985	1 set
			2799.7	0.990	5 set
			2813.9	0.995	1 set
			2828.0	1.000	8 set
			2842.1	1.005	1 set
			2856.3	1.010	3 set
			2884.6	1.020	1 set
$\text{D}(p,d)p$	2499.1 ± 2.0	CD_2 (4022 ± 9 mg/cm 2)	3809.3	1.347	1.2 hour

$f = 1.020$. In particular, a region near the η' production threshold was intensively measured, as distinct narrow structures of η' -mesic states were theoretically predicted most strongly near the threshold [29].

The momentum calibration of the spectrometer was performed by measuring the elastic $\text{D}(p,d)p$ reaction at 1.6 GeV using a CD_2 target. Nearly monochromatic deuterons with the momentum of 2828.0 ± 1.0 MeV/c were emitted from the target, which defined the central momentum of the FRS at $f = 1.000$. These deuterons were measured with various scale factors to analyze the ion-optical response of the FRS. One calibration run took about half an hour, and it was repeated every ~ 8 hours to check the stability of the whole spectrometer system.

The elastic $\text{D}(p,d)p$ scattering was measured with a CD_2 target and a proton beam of 2.5 GeV in order to crosscheck the normalization of the differential cross section. The obtained value was then compared with those reported in Ref. [36], as explained in Sec. III D. During a part of the measurement, solid angles were tightly limited to 2.35×10^{-2} msr and 3.94×10^{-2} msr by using slits directly behind the target. A comparison of the yields with and without the slits provided the effective solid angle covered by the FRS.

III. ANALYSIS

The goal of the data analysis described in this section is to obtain excitation-energy spectra of ^{11}C near the η' production threshold. The analysis procedure consists of the following steps. First, the deuteron events are

identified (Sec. III A), and next the deuteron momenta are reconstructed from the measured tracks (Sec. III B). The excitation energies of ^{11}C are then kinematically calculated (Sec. III C), and finally the normalization of the cross section is performed (Sec. III D).

A. Selection of deuteron events

Data of the plastic scintillation counters are analyzed in order to identify deuterons at the F4 focal plane. As explained in Fig. 2, major background particles in the recorded data are the accidental multiple-hit protons at F2. Thus, signal waveforms of photomultipliers reading SC2H are firstly analyzed to select single-hit events at F2. TOF between F2 and F4 is analyzed as well to further reject remaining background protons. SC42 is not used in the following analysis to avoid position-dependent transmission from SC41 to SC42 caused by material inhomogeneity found in the Čerenkov detectors behind SC41.

The waveforms of SC2H signals are fitted by an empirical function

$$f(t) = p_0 + p_1 t - p_2 \cdot \exp\left(-\frac{(t - p_3)^2}{2(p_4 + p_5 t)^2}\right), \quad (1)$$

where the first two terms represent a baseline and the third a pulse with a negative polarity. Signals are fitted within a time window of 70 ns around a typical deuteron time, treating p_1, \dots, p_5 as free parameters. The sum of the squared residual (SSR) given by the fit is then used to quantify the multiplicity of the particles. Figure 3 shows SSR against the height parameter p_2 obtained for both

two photomultipliers (left and right) of SC2H. Single-hit events are clearly identified around $SSR \approx 100$. By taking into account the correlation between SSR and p_2 , events in the regions indicated by the arrows are selected as single-hit events and used in the following analyses.

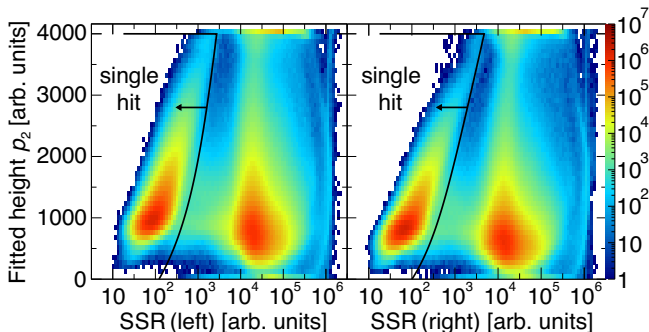


FIG. 3. Fit results of SC2H waveforms with a single-pulse function. SSR and the height parameter p_2 obtained in the fit are plotted for both of the two photomultipliers (left and right) of SC2H. The solid curves are used as boundaries to select single-hit events.

Next, TOF between F2 and F4 is analyzed, by introducing corrections for time-walk effects and dependence on ion-optical variables. The corrected TOF spectrum for the data set at the scaling factor $f = 0.980$ is presented in Fig. 4 as an example. The unshaded spectrum shows the total recorded events, where a peak for the deuteron is observed above a constant component due to the multiple-hit proton background. The achieved time resolution for the deuteron peak is $\sigma = 1.7 \times 10^2$ ps. The shaded spectrum displays the single-hit events selected by the waveform analysis, demonstrating efficient rejection of the multiple-hit background by 2–3 orders of magnitude. Finally, events within the dashed lines ($\pm 5\sigma$ region around the peak) are selected as deuteron events to further reject remaining proton background.

The efficiency of the deuteron identification is discussed in three steps as follows. First, properly measured times and pulse heights of the SC2H and SC41 signals and reconstructed tracks at F4 are required for the analysis of the particle identification. This first condition leads to 0.6–0.9% rejection of the deuteron. Second, rejection of the deuteron by selecting the single-hit waveform is considered using a TOF spectrum for those events rejected in the waveform selection. The spectrum shows a small enhancement at the TOF value for the deuteron, indicating 2–3% rejection. Third, probability of deuteron rejection by the TOF selection is estimated to be 0.2–0.3% from the tail structure of the deuteron peak observed in the TOF spectrum. The longer tail on the right side is due to accidental particles almost coincident with the deuteron at F2 where the timing information measured by a leading-edge discriminator deviated only to the earlier side. Combining the above three contributions, the deuteron identification efficiency is evaluated

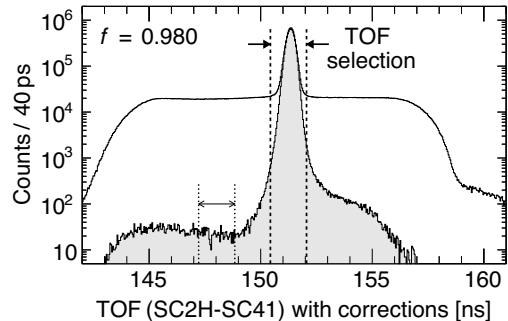


FIG. 4. Corrected TOF spectra between F2 and F4 at the FRS scale factor of $f = 0.980$. The unshaded histogram shows the total number of events, while the shaded one corresponds to the single-hit events selected by the SC2H waveforms. The dashed lines indicate the $\pm 5\sigma$ region around the deuteron peak used for the TOF selection. The region between the dotted lines is used to estimate the proton contamination fraction.

to be 96–97% for all the data sets of the $^{12}\text{C}(p,d)$ reaction.

The contamination of background protons in events with identified deuteron is evaluated in the TOF spectrum with the single-hit selection. The spectrum shows an almost constant background on the shorter TOF side of the deuteron peak, where a tail structure of the peak is not significant. The amount of the contamination in the TOF window (dashed lines) can be estimated by integrating the constant region between the dotted lines with the same interval. The contamination fraction thus evaluated is $\sim 2 \times 10^{-4}$, making only a negligible contribution in the subsequent spectral analysis.

B. Momentum analysis

The deuteron momentum is obtained from the reconstructed track by MWDCs at the F4 dispersive focal plane. The momentum P_d can be written as

$$P_d = P_{\text{FRS}}(1 + \delta), \quad (2)$$

where δ denotes a momentum deviation relative to the FRS central momentum, $P_{\text{FRS}} = f \cdot 2828.0$ MeV/c. The deviation δ can be derived from the horizontal track (position X and angle X') regardless of the scaling factor f , since ion-optical properties remain unchanged by scaling the central momentum in a small range.

In order to obtain a calibration function converting a track (X, X') to δ , the mono-energetic deuteron from the elastic $D(p,d)p$ reaction at the proton energy of 1.6 GeV is analyzed. A deuteron emitted in this reaction has a momentum of 2828.0 MeV/c, corresponding to a deviation of $\delta = 1/f - 1$ for the FRS scaling factor f . Thus, the ion-optical response for δ between -2% and 2% can

be evaluated from the calibration settings listed in Table I. Examples of the reconstructed horizontal position X and angle X' are shown in the left panel of Fig. 5, overlaid for $f = 0.980, 0.990, 1.000, 1.010, 1.020$. An elastic-scattering locus for each scaling factor is observed above a continuum from reactions with carbon. We fit the position X by a polynomial function of both X' and δ using all the data sets, and thereby construct a calibration function for δ , as demonstrated in the right panel.

An uncertainty associated with the calibration of δ is derived from deviations between the repeated measurements. Thus the estimated systematic error of δ is 0.02% in a region of $|X'| < 18$ mrad, which is later used in the analysis of the $^{12}\text{C}(p,d)$ reaction.

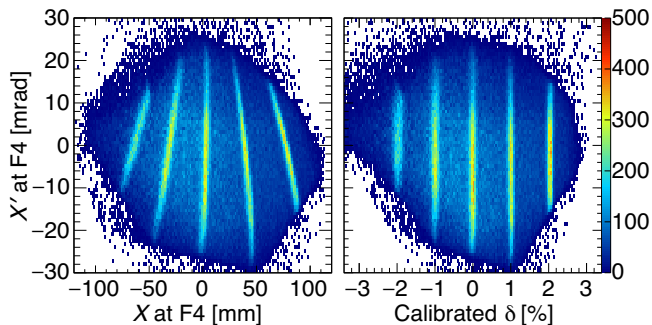


FIG. 5. Calibration data with the elastic proton-deuteron scattering for the FRS scale factors $f = 0.980, 0.990, 1.000, 1.010, 1.020$. (Left panel) Horizontal position X and angle X' at F4 reconstructed by MWDCs. (Right panel) Calibrated δ , the momentum deviation relative to the FRS central momentum, is shown against the angle X' .

C. Excitation energy

1. Calculation

The excitation energy of ^{11}C has been calculated from the proton kinetic energy T_p and the deuteron momentum P_d . First, the relativistic energies of the proton (E'_p) and the deuteron (E'_d) are calculated at the center of the reaction target, after correcting the energy losses, as

$$E'_p = T_p + M_p c^2 - \Delta E_p, \quad (3)$$

$$E'_d = \sqrt{P_d^2 c^2 + M_d^2 c^4} + \Delta E_d. \quad (4)$$

ΔE_p and ΔE_d represent the energy losses in half of the target thickness based on a calculation with ATIMA [37]. The missing mass M_X in the $^{12}\text{C}(p,d)X$ reaction is then obtained by

$$M_X = \sqrt{\left(M_{^{12}\text{C}} + \frac{E'_p - E'_d}{c^2}\right)^2 - \left(\frac{P'_p - P'_d}{c}\right)^2}, \quad (5)$$

where $M_{^{12}\text{C}}$ is the mass of ^{12}C , and P'_p and P'_d are the proton and deuteron momenta corresponding to E'_p and E'_d ,

respectively. Here, the reaction angle is assumed to be 0° because of the ion-optical restrictions on angle reconstruction. Finally, the excitation energy E_{ex} is defined relative to the η' production threshold $E_0 = 957.78$ MeV as

$$E_{\text{ex}} - E_0 = (M_X - M_{^{11}\text{C}} - M_{\eta'}) c^2, \quad (6)$$

where $M_{^{11}\text{C}}$ and $M_{\eta'}$ denote the ^{11}C and η' masses, respectively.

2. Systematic error

The systematic errors in the excitation-energy calculation have been evaluated by considering the following three sources.

(a) *Beam energy.* Uncertainties in the absolute beam energies (2499.1 ± 2.0 MeV and 1621.6 ± 0.8 MeV) cause systematic errors of 1.9 MeV and 0.8 MeV in the excitation energy, respectively. Note here that the lower beam energy also affects the excitation energy, as the deuteron momentum in the $\text{D}(p,d)p$ calibration at 1.6 GeV is used to define the FRS central momentum. Considering that the two errors are mostly correlated because of their common source in the circumference of the SIS-18 synchrotron, we obtain the combined systematic error of 1.4 MeV in the excitation energy.

(b) *Reaction angle.* A systematic error originating in the uncertainty of the reaction angle, which is assumed to be 0° in the kinematical calculation of the production and calibration reactions, is evaluated to be 0.8 MeV in the excitation energy. The possible maximum systematic error caused by neglecting the finite reaction-angle distribution ($\lesssim 1^\circ$) in the acceptance of the FRS is adopted.

(c) *Optics calibration.* The systematic error of the relative momentum deviation δ has been evaluated to be 0.02%. This corresponds to an error of 0.5 MeV in the scale of the excitation energy.

By taking a square root of the quadratic sum of all the above contributions, a total systematic error in the excitation energy is estimated to be 1.7 MeV.

3. Experimental resolution

The experimental resolution is evaluated using the mono-energetic deuterons in the $\text{D}(p,d)p$ calibration at 1.6 GeV. Figure 6 shows a spectrum of the deuteron momentum at the FRS scaling factor of $f = 1.000$ analyzed in the same procedure as the production runs. The spectrum is fitted well with a function given by the gray solid line, summing a Gaussian function for the elastic peak (dotted line) and a second-order polynomial for the carbon contribution (dashed line). The Gaussian component yields the overall momentum resolution of 2.79 ± 0.09 MeV/c (σ), where the uncertainty includes deviations between the different data sets.

This resolution corresponds to an energy resolution of $\sigma_{\text{cal}} = 2.20 \pm 0.07$ MeV in the scale of E_{ex} shown in the lower axis.

In order to evaluate the experimental resolution in the production runs from the above estimate for the calibration runs, two corrections for the different target and beam energy in the calibration measurements are necessary. First, a Monte-Carlo simulation based on ATIMA [37] shows that the energy straggling in the targets makes contributions of $\sigma_{\text{prod}}^{\text{targ}} = 1.15$ MeV and $\sigma_{\text{cal}}^{\text{targ}} = 0.39$ MeV in the production and calibration runs, respectively, in the scale of E_{ex} . Second, an estimated relative momentum spread of the beams of $\leq 1.7 \times 10^{-4}$ accounts for resolutions of $\sigma_{\text{prod}}^{\text{beam}} \leq 0.52$ MeV in the production runs and $\sigma_{\text{cal}}^{\text{beam}} \leq 0.34$ MeV in the calibration in the scale of E_{ex} . By introducing the corrections quadratically *i.e.*, $\sigma_E^2 = \sigma_{\text{cal}}^2 + \{(\sigma_{\text{prod}}^{\text{beam}})^2 - (\sigma_{\text{cal}}^{\text{beam}})^2\} + \{(\sigma_{\text{prod}}^{\text{targ}})^2 - (\sigma_{\text{cal}}^{\text{targ}})^2\}$, the excitation-energy resolution in the production measurements is obtained as $\sigma_E = 2.4\text{--}2.6$ MeV.

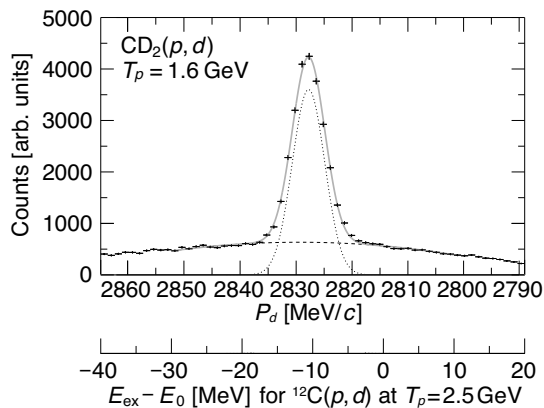


FIG. 6. Momentum spectrum of deuterons in the $\text{CD}_2(p, d)$ calibration measurement with the 1.6 GeV proton beam. The lower axis shows the excitation energy for the production run corresponding to the deuteron momentum. The gray solid line displays a fit with a function consisting of a Gaussian peak (dotted line) and a second-order polynomial (dashed line).

D. Normalization of spectra

Excitation-energy spectra need to be corrected for the acceptance of the spectrometer, which can be expressed as a function of the momentum parameter δ . For spectral analysis, events with the horizontal angle at F4 in $|X'| < 18$ mrad and δ in $0\% \leq \delta \leq 1.5\%$ are selected, where the acceptance curve is assumed to be linear. The slope of the acceptance function is then deduced by two methods: (i) measuring the δ -dependence of deuteron yields at one fixed absolute momentum by scaling the FRS magnetic fields, and (ii) a Monte Carlo simulation of the ion-optical transport in the FRS using the code MOCADI [38]. These two estimations result in a consistent acceptance curve of

$A(\delta) \propto 1 + (0.07 \pm 0.03)\delta/\%$, and the excitation spectra at the seven FRS settings are thus corrected with this function.

To normalize the absolute scale of the double differential cross section, we analyze a short production run with the SEETRAM detector directly monitoring the beam intensity. The double differential cross section is calculated by

$$\left(\frac{d^2\sigma}{d\Omega dE} \right)_{\text{lab}} = \frac{(dY/dE)_{\text{ref}}}{N_p \cdot n_t \cdot \Delta\Omega_{\text{ref}} \cdot \varepsilon} \quad (7)$$

at one reference energy $E_{\text{ex}} - E_0 = -7.0$ MeV, where the solid angle covered by the FRS is separately evaluated as $\Delta\Omega_{\text{ref}} = 1.16 \pm 0.13$ msr. $(dY/dE)_{\text{ref}}$ is the measured yield density per unit excitation energy at the reference, N_p is the number of the incident protons obtained by SEETRAM, and n_t is the number density of the target. ε denotes the overall efficiency estimated to be $(25.2 \pm 0.1)\%$, taking into account the trigger efficiency (26.2%), the deuteron identification efficiency (96–97%), and the tracking efficiency (99.8–99.9%). As a result, the double differential cross section of $5.4 \pm 0.7 \mu\text{b}/(\text{sr MeV})$ is obtained at the reference energy.

Spectral normalization is then performed as follows. First, the acceptance-corrected excitation spectrum at the FRS scale factor of $f = 0.990$ is normalized, according to the analyzed cross section at the reference energy $E_{\text{ex}} - E_0 = -7.0$ MeV. Next, the spectra at the neighboring FRS settings ($f = 0.985$ and 1.000) are scaled so that they have consistent overlap in the common energy region with the $f = 0.990$ spectrum. Spectra at the other settings are sequentially normalized in the same manner.

The differential cross section of the elastic $\text{D}(p, d)p$ reaction at 2.5 GeV is analyzed as well in a similar way in order to confirm the analyses on the beam intensity at this energy and on the normalization of the cross section. The obtained value is $0.98 \pm 0.11 \mu\text{b}/\text{sr}$ in the center-of-mass frame, which is consistent with known cross sections around this energy, $1.10 \pm 0.10(\text{stat}) \pm 0.09(\text{syst}) \mu\text{b}/\text{sr}$ at 2.4 GeV and $1.18 \pm 0.03(\text{stat}) \pm 0.09(\text{syst}) \mu\text{b}/\text{sr}$ at 2.55 GeV [36], within the experimental errors.

IV. RESULTS

Excitation-energy spectra of ^{11}C obtained with the $^{12}\text{C}(p, d)$ reaction are presented in Fig. 7 for the seven momentum settings of the spectrometer. The excitation energy E_{ex} relative to the η' production threshold $E_0 = 957.78$ MeV is shown in the lower horizontal axis, while the scale of the corresponding deuteron momentum is given in the upper one. The systematic error associated with the excitation energy has been estimated to be 1.7 MeV. The ordinate gives the double differential cross section, with an uncertainty of $\pm 13\%$ on the absolute scale.

These seven spectra are combined into one spectrum by averaging the data points of different FRS settings

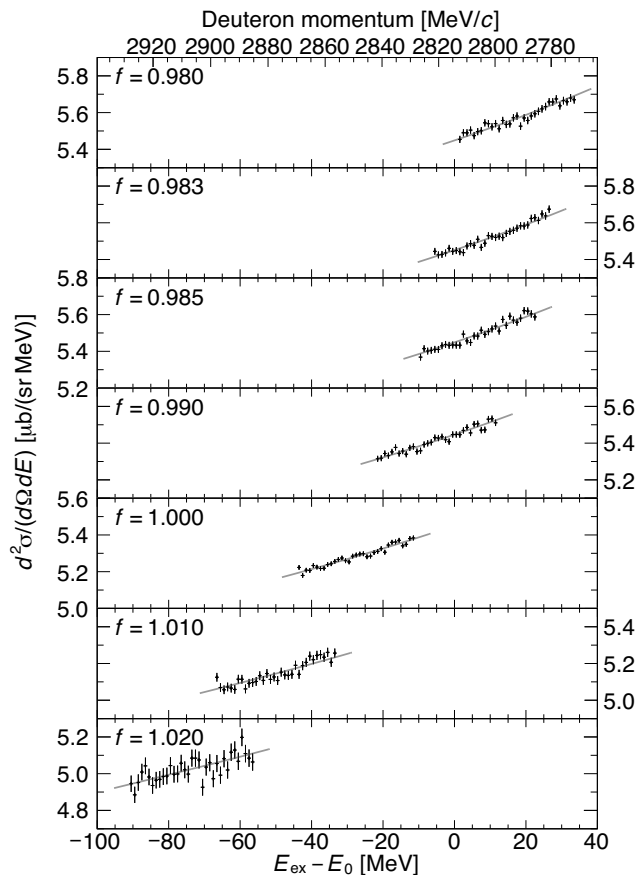


FIG. 7. Excitation-energy spectra of ^{11}C measured in the $^{12}\text{C}(p,d)$ reaction with seven momentum settings ($f = 0.980$ – 1.020) of the FRS. The lower abscissa is the excitation energy E_{ex} relative to the η' production threshold $E_0 = 957.78$ MeV, and the upper axis shows the corresponding deuteron momentum. The gray solid curves display a third-order polynomial simultaneously fitted to the seven spectra.

at each excitation energy. The resulting excitation spectrum is shown in Fig. 8 (top panel). Note that this averaging reduces the degrees of freedom originating in the relative spectral normalization between the neighboring settings. Therefore, the following analyses are performed for both the individual spectra (Fig. 7) and the combined one (Fig. 8), where only minor differences are found as shown later.

The obtained spectra show no distinct narrow structure, although a good statistical sensitivity at a level of $< 1\%$ is achieved together with a sufficiently good experimental resolution of $\sigma_E = 2.4$ – 2.6 MeV. The spectra exhibit a smooth increase from about 4.9 to 5.7 $\mu\text{b}/(\text{sr MeV})$ in the measured region of the excitation energy. This continuous component can be understood within an order of magnitude by quasi-free meson production processes $pN \rightarrow dX$ ($X = 2\pi, 3\pi, 4\pi, \omega$), where N denotes a nucleon in the target nucleus, as simulated in Ref. [28].

The spectra are fitted by a third-order polynomial function over the whole measured energy region. The

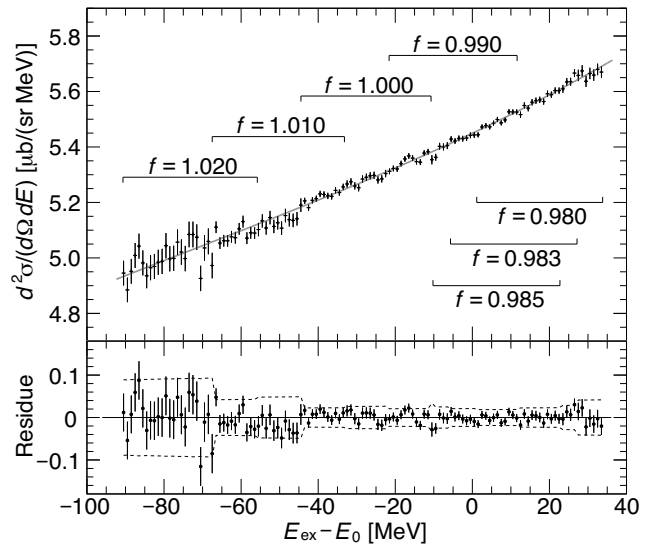


FIG. 8. (Top panel) Combined spectrum of the ^{11}C excitation energy E_{ex} near the η' production threshold $E_0 = 957.78$ MeV. A third-order polynomial fit is given by the solid gray curve. The horizontal bars indicate excitation-energy regions covered by each FRS momentum setting. (Bottom panel) Residues of the polynomial fit. The dashed lines display envelopes of 2 standard deviations.

seven spectra in Fig. 7 are simultaneously fitted, by sharing the polynomial parameters between the settings. In addition, a multiplying factor is introduced as a free parameter to each spectrum except for the one at $f = 0.990$ in order to take into account a possible error correlation with the relative normalization of the spectra. The fit results are shown by the gray solid curves in both Figs. 7 and 8. $\chi^2/(\text{n.d.f.})$ is $221/225$ in Fig. 7 and $125/121$ in Fig. 8, where n.d.f. denotes the number of degrees of freedom. Residues of the fit are also displayed in Fig. 8 (bottom panel) with envelopes of 2 standard deviations.

We determine upper limits for the formation cross section of η' -mesic nuclei. Here, a Lorentzian function at an excitation energy E_{ex} with a width Γ (FWHM) is tested as a signal shape. The measured spectrum is assumed to be described by the following function:

$$f(E; E_{\text{ex}}, \Gamma) = \left(\frac{d\sigma}{d\Omega} \right) \cdot \text{Voigt}(E; E_{\text{ex}}, \Gamma, \sigma_E) + (p_0 + p_1 E + p_2 E^2 + p_3 E^3). \quad (8)$$

The first term includes a Voigt function, which is the Lorentzian function folded by a Gaussian function accounting for the experimental resolution (σ_E). The signal cross section to be tested is represented by $(\frac{d\sigma}{d\Omega})$. The second term is the third-order polynomial accounting for the continuous component. The combined spectrum (Fig. 8) is fitted by this function within a region of ± 35 MeV around the Lorentzian center, by treating both the signal cross section and the polynomial coefficients as free

parameters. The upper limit of the cross section at the 95% confidence level is then determined by assuming a Gaussian probability density function based on the fit result and normalizing it in the physical non-negative region ($\frac{d\sigma}{d\Omega} \geq 0$).

In order to obtain the upper limit as a function of the Lorentzian position E_{ex} and width Γ , the above analysis has been repeated for each set of $(E_{\text{ex}} - E_0, \Gamma)$ in $\{-60, -59, \dots, +20\} \times \{5, 10, 15\}$ MeV. In Fig. 9, the fitted values and errors of the Lorentzian cross section are shown by the solid dots, and the resulting upper limits are summarized by the solid curves. These values are given in the differential cross section $d\sigma/d\Omega$ by the left ordinate and in the Lorentzian peak height $d^2\sigma/(d\Omega dE)$ by the right one. Moreover, analysis based on simultaneous fitting of the seven spectra (Fig. 7) is conducted in order to check effects of possible error correlations with the relative normalization of the spectra. Thus evaluated limits are given by the dashed curves, exhibiting no significant difference between the two analysis methods.

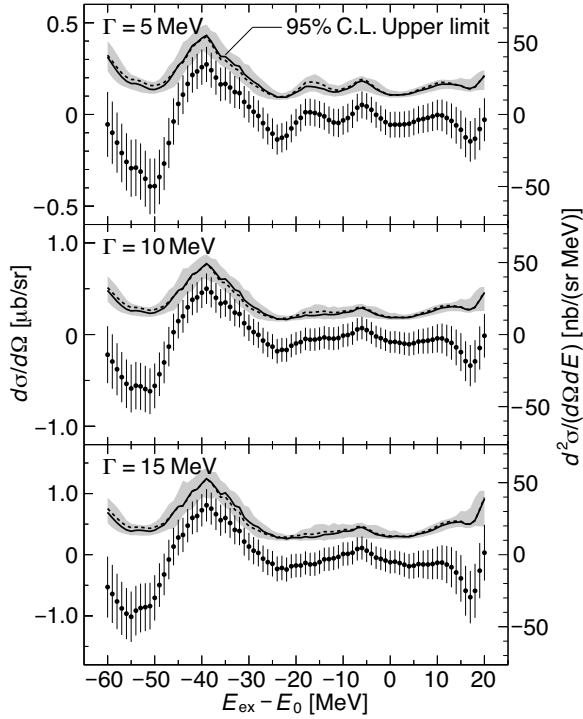


FIG. 9. Fitted values (solid dots) and resulting 95% C.L. upper limits (solid curves) of the Lorentzian-shaped formation cross section of η' -mesic nuclei plotted as a function of the assumed peak position E_{ex} for the widths of $\Gamma = 5, 10, 15$ MeV. Upper limits evaluated by simultaneous fitting of the seven spectra (Fig. 7) are shown by the dashed curves. The shaded areas indicate the systematic errors on the upper limits.

To evaluate systematic errors on the upper limits, the following contributions are considered: (1) the systematic error on the absolute scale of the measured cross section ($\pm 13\%$), (2) the systematic error in the excitation-energy

calculation (± 1.7 MeV), (3) the uncertainty in the slope of the momentum acceptance, (4) the uncertainty in the experimental resolution, (5) different fit regions (10 MeV wider or narrower), and (6) a choice of fitting of the combined spectrum (Fig. 8) or simultaneous fitting of the seven spectra (Fig. 7). The upper limit is analyzed by changing each of these conditions, and then the total systematic error on the limit is evaluated by taking the square root of the sum of the squared deviations. In Fig. 9, the thus-evaluated systematic errors are displayed by the shaded areas.

V. DISCUSSION

The 95% C.L. upper limits for the formation cross section of η' -mesic nuclei have been obtained as a function of the position and width of the assumed Lorentzian peak. The upper limits are particularly stringent near the η' production threshold: $0.1\text{--}0.2 \mu\text{b/sr}$ for $\Gamma = 5$ MeV, $0.2\text{--}0.4 \mu\text{b/sr}$ for $\Gamma = 10$ MeV, and $0.3\text{--}0.6 \mu\text{b/sr}$ for $\Gamma = 15$ MeV. These are as small as ~ 20 nb/(sr MeV) in the Lorentzian peak height, and therefore exclude the existence of prominent peak structures theoretically expected near the threshold for strongly attractive potentials, like a peak with ~ 40 nb/(sr MeV) for $V_0 = -150$ MeV shown in Fig. 10 (top) [29]. On the other hand, the obtained limits are not in conflict with small peak structures predicted for shallow potentials, as in Fig. 10 (bottom) for $V_0 = -50$ MeV where a peak height is < 10 nb/(sr MeV).

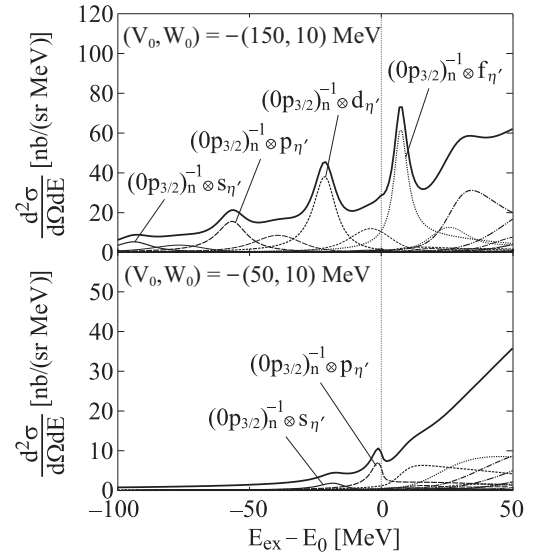


FIG. 10. Theoretically-calculated spectra of the $^{12}\text{C}(p, d)^{11}\text{C} \otimes \eta'$ reaction at 2.5 GeV [29]. The η' -nucleus potential parameters are taken as $(V_0, W_0) = (-150, -10)$ MeV (top) and $(-50, -10)$ MeV (bottom). Total formation cross sections are shown by the thick lines, and major configurations of the η' -mesic states $\ell_{\eta'}$ coupling with the neutron hole states $(nl_j)_n^{-1}$ are shown by the thin lines.

In order to make further quantitative comparisons with

the theoretical predictions, we evaluate constraints on the scales for the theoretically-calculated formation spectra. Here, the following function is assumed to describe the measured excitation spectrum,

$$F(E; V_0, W_0) = \mu \cdot S(E; V_0, W_0, \sigma_E) + (p_0 + p_1 E + p_2 E^2 + p_3 E^3), \quad (9)$$

where $S(E; V_0, W_0, \sigma_E)$ denotes the theoretical formation spectrum (e.g., Fig. 10) [29, 39] for the real and imaginary potentials of (V_0, W_0) folded by the Gaussian function for the experimental resolution (σ_E). The parameter μ is introduced to test an allowed scale for $S(E; V_0, W_0, \sigma_E)$. The remaining term is a third-order polynomial for the continuous part of the spectrum. A 95% C.L. upper limit of μ for given (V_0, W_0) is analyzed in the similar procedure, by fitting the measured spectrum with this function within the region of $-40 \text{ MeV} \leq E_{\text{ex}} - E_0 \leq +30 \text{ MeV}$ and assuming a Gaussian probability density function of μ in the physical region ($\mu \geq 0$).

The analysis has been repeated for the potential parameter sets listed in Table II, including $W_0 = -25 \text{ MeV}$ where theoretical spectra were newly calculated [39]. Fitted values and resultant 95% C.L. upper limits of the scale parameter μ are given by μ_{fit} and μ_{95} , respectively. For each (V_0, W_0) , the existence of the theoretically-calculated peak structure with the strength multiplied by μ_{95} is excluded at the 95% C.L. The upper limits μ_{95} are then linearly interpolated between the calculated potentials, and presented as a contour plot on the real and imaginary potential plane (V_0, W_0) in Fig. 11. Smaller μ_{95} is deduced for larger $|V_0|$ and smaller $|W_0|$. Systematic errors on μ_{95} are estimated by taking into account the same six sources as for the Lorentzian upper limits. A band of the systematic error on the $\mu_{95} = 1$ contour is shown by the dashed curves.

In Fig. 11, one can exclude a region of the potential-parameter set giving $\mu_{95} \leq 1$ at the 95% C.L. within the present comparison with the theoretical calculations. Note here that the magnitude of the theoretically-calculated spectra has an estimated uncertainty of a factor ~ 2 [30, 40], originating in the assumed cross section of $30 \mu\text{b}/\text{sr}$ for the elementary reaction $pn \rightarrow d\eta'$ [28]. Thus, if the theoretical cross sections were overestimated by a factor of 2, for example, one can reject a potential region with $\mu_{95} \leq 1/2$ at the 95% C.L.

Figure 12 summarizes the obtained constraint and currently known information on the η' -nucleus potential. The shaded region shows the excluded region ($\mu_{95} \leq 1$) in the present analysis. The rectangular box displays an evaluated region by the η' photoproduction experiments: the real part of $-(39 \pm 7(\text{stat}) \pm 15(\text{syst})) \text{ MeV}$ from the excitation function and the η' momentum distribution [20, 21], and the imaginary part of $-(13 \pm 3(\text{stat}) \pm 3(\text{syst})) \text{ MeV}$ from the transparency ratios [22, 23]. Theoretical expectations with the NJL model ($V_0 = -150 \text{ MeV}$) [9, 10], the linear sigma model ($V_0 = -80 \text{ MeV}$) [11], the QMC model ($V_0 = -37 \text{ MeV}$) [12], and the chiral unitary approach [41] are shown by the

TABLE II. Fitted values (μ_{fit}) and resulting 95% C.L. upper limits (μ_{95}) for the scale of the theoretical formation spectra. The analysis is performed at the listed sets of the real and imaginary potentials (V_0, W_0).

V_0 (MeV)	W_0 (MeV)	μ_{fit}	μ_{95}
-50	-5	0.04 ± 1.44	2.85
-50	-10	0.22 ± 2.88	5.78
-50	-15	1.07 ± 5.29	11.10
-50	-20	3.10 ± 9.11	20.01
-50	-25	6.74 ± 14.75	33.69
-60	-5	0.36 ± 0.79	1.80
-60	-10	0.75 ± 1.54	3.55
-60	-15	1.49 ± 2.83	6.61
-80	-5	0.13 ± 0.36	0.79
-80	-10	0.20 ± 0.63	1.38
-80	-15	0.19 ± 1.09	2.26
-100	-5	-0.24 ± 0.20	0.27
-100	-10	-0.32 ± 0.35	0.50
-100	-15	-0.43 ± 0.56	0.86
-100	-20	-0.60 ± 0.90	1.41
-100	-25	-0.85 ± 1.39	2.22
-150	-5	-0.01 ± 0.10	0.18
-150	-10	0.01 ± 0.15	0.31
-150	-15	0.03 ± 0.23	0.48
-150	-20	0.06 ± 0.35	0.72
-150	-25	0.09 ± 0.51	1.06
-200	-5	-0.05 ± 0.07	0.11
-200	-10	-0.04 ± 0.11	0.20
-200	-15	-0.03 ± 0.16	0.30
-200	-20	-0.03 ± 0.23	0.43
-200	-25	-0.04 ± 0.31	0.59

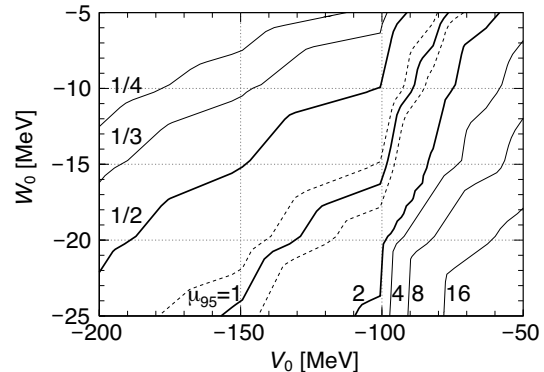


FIG. 11. A contour plot of μ_{95} (solid curves), the 95% C.L. upper limit of the scale parameter μ for the theoretical formation spectra, on the real and imaginary potential plane (V_0, W_0) . The limits have been analyzed at the potential sets listed in Table II and linearly interpolated in-between. The systematic errors on the $\mu_{95} = 1$ contour are shown by the dashed curves. The region with $\mu_{95} \leq 1$ is excluded by the present analysis. See the text for further explanation.

dashed lines.

Here, a strongly attractive potential of the order of

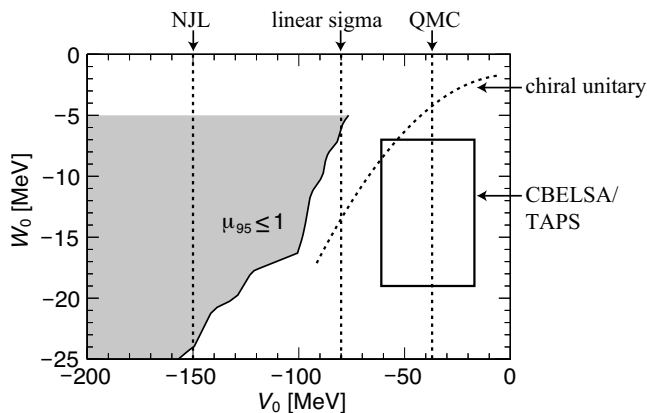


FIG. 12. Obtained constraint and currently known information on the η' -nucleus potential ($V_0 + iW_0$) at normal nuclear density. The shaded region ($\mu_{95} \leq 1$) represents the region excluded within the present analysis. The rectangular box shows real and imaginary potentials evaluated in η' photoproduction experiments by the CBELSA/TAPS collaboration [20–23]. Theoretical predictions based on the NJL model [9, 10], the linear sigma model [11], the QMC model [12], and the chiral unitary approach [41] are indicated by the dashed lines.

$V_0 \approx -150$ MeV, as predicted by the NJL model, is rejected within the present analysis for the region of the imaginary potential of $|W_0| \leq 24$ MeV. The current experiment has very limited sensitivity in a shallower potential region where some small peak structures are predicted in the theoretical formation spectra [29], as shown in Fig. 10 (bottom), for example. Therefore, an improvement of the experimental sensitivity is necessary for further investigating the existence of η' -mesic nuclei.

One of the possible approaches for the next step is a semi-exclusive measurement by simultaneously detecting the forward deuteron in the $^{12}\text{C}(p, d)$ reaction for missing-mass spectroscopy and decay particles from η' -mesic nuclei for event selection. A large amount of the continuous background dominating the present spectrum in Fig. 8, which is understood as quasi-free multi-pion production, will be suppressed by tagging the decay particles. As discussed in Ref. [42], major decay modes of the η' -mesic nuclei are expected to be one- and two-nucleon absorption: $\eta'N \rightarrow \eta N$, $\eta'N \rightarrow \pi N$, and $\eta'NN \rightarrow NN$. Among them the two-nucleon absorption process has a distinguishing feature in the emitted proton (or neutron) energy of ~ 300 – 600 MeV, as simulated in Fig. 13 assuming the Fermi motion of nucleons in the nucleus [43]. A simulation based on an intra-nuclear cascade model [44] has shown that the signal-to-background ratio will be increased by two orders of magnitude compared to the present experiment by selecting energetic protons in the backward angular range ($\theta_p^{\text{lab}} \geq 90^\circ$) in the laboratory [45].

The semi-exclusive measurement will be performed in the near future. This experiment is feasible with the FRS at GSI and the next-generation Super-FRS [46] at

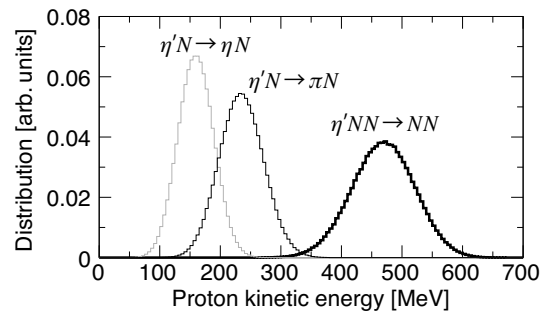


FIG. 13. Simulated kinetic energy distributions of protons emitted in the decay of η' -mesic nuclei. Three decay modes are considered: $\eta'N \rightarrow \eta N$ (thin gray), $\eta'N \rightarrow \pi N$ (thin black), and $\eta'NN \rightarrow NN$ (thick). The integral of each distribution is normalized to unity.

FAIR, as the excellent performance of the FRS for the forward (p, d) spectroscopy has been demonstrated in the present experiment. A large-acceptance detector, such as the WASA central detector [47, 48], will be additionally installed surrounding the reaction target. An experimental setup combining the FRS and the WASA systems is illustrated in Fig. 14. We will also consider possibilities of using other reaction channels such as the (π, N) reaction.

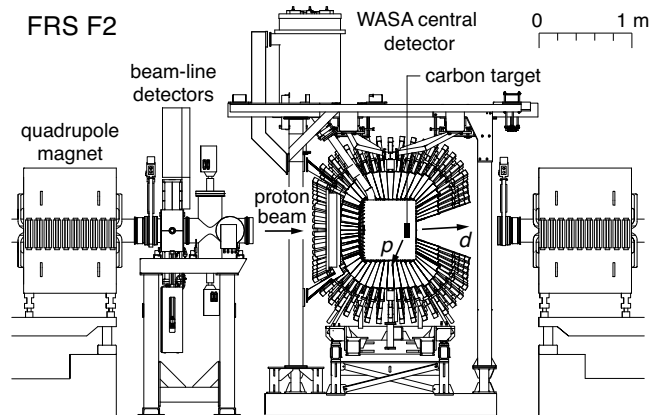


FIG. 14. A schematic view of an experimental setup for the semi-exclusive measurement. A 2.5 GeV proton beam impinges on a carbon target. The forward deuteron is momentum-analyzed by the downstream FRS section. The proton emitted backward in the decay of η' -mesic nuclei is identified by the WASA central detector [47, 48].

VI. CONCLUSION

A missing-mass spectroscopy experiment of the $^{12}\text{C}(p, d)$ reaction was performed at a proton energy of 2.5 GeV aiming at the search for η' -mesic nuclei. The excitation-energy spectra of ^{11}C nuclei were successfully obtained around the η' -meson production threshold with high statistical sensitivity and sufficient experimental res-

olution. As no distinct peak structure has been observed in the excitation-energy spectra, upper limits on the formation cross sections of the η' -mesic nuclei have been determined. A comparison with theoretically-predicted formation spectra sets a stringent constraint on the η' -nucleus potential.

The present work has established the applicability of the missing-mass spectroscopy of the (p,d) reaction for studying in-medium properties of the η' meson. The application to other mesons will be considered. The experimental search for η' -mesic nuclei will further proceed with the semi-exclusive measurement by simultaneously detecting the decay particles.

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