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# Measurement of target and double-spin asymmetries for the e[over]p[over] $\rightarrow e\pi^{+}(n)$ reaction in the nucleon resonance region at low Q^{2}

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## <sup>1</sup> Measurement of Target and Double-spin Asymmetries for the $\vec{e}\vec{p} \rightarrow e\pi^+(n)$ Reaction in the Nucleon <sup>2</sup> Resonance Region at Low $Q^2$

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We report measurements of target- and double-spin asymmetries for the exclusive channel  $\vec{ep} \rightarrow e\pi^+(n)$  in the nucleon resonance region at Jefferson Lab using the CEBAF Large Acceptance Spectrometer (CLAS). These asymmetries were extracted from data obtained using a longitudinally polarized NH<sub>3</sub> target and a longitudinally polarized electron beam with energies 1.1, 1.3, 2.0, 2.3 and 3.0 GeV. The new results are consistent with previous CLAS publications but are extended to a low  $Q^2$  range from 0.0065 to 0.35 (GeV/c)<sup>2</sup>. The  $Q^2$  access was made possible by a custom-built Cherenkov detector that allowed the detection of electrons for scattering angles as low as 6°. These results are compared with the unitary isobar models JANR and MAID, the partial-wave analysis prediction from SAID and the dynamic model DMT. In many kinematic regions our results, in particular results on the target asymmetry, help to constrain the polarization-dependent components of these models.

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## I. PHYSICS MOTIVATION

The perturbative nature of the strong interaction at small 69 distances - often referred to as "asymptotic freedom" - was 70 established more than 30 years ago and provided strong sup-71 port for Quantum Chromodynamics (QCD) to be accepted as 72 he correct theory for strong interactions [1, 2]. On the other 73 hand, calculations at long-distances are still beyond reach be-74 cause of the non-perturbative nature at this scale. As a re-75 sult, we are still far away from being able to describe the 76 strong force as it manifests itself in the structure of baryons 77 and mesons [3][4]. 78

A fundamental approach to resolve this difficulty is to de-79 velop accurate numerical simulations of OCD on the Lattice, 80 for recent reviews see [5, 6]. However Lattice QCD methods 81 are difficult to apply to light-quark systems such as the nu-82 cleon. Alternatively, hadron models with effective degrees of 83 freedom have been constructed to interpret data. One example 84 is the chiral perturbation theory [7, 8], which is constrained 85 only by the symmetry properties of QCD. The constituent 86 quark model, though not fully understood, is one success-87 ful example that works almost everywhere from hadron spec-88 troscopy to deep inelastic scattering [9, 10]. Predictions for 89 the scattering amplitudes and polarization-dependent asym-90 metries exist for many resonances within the framework of 91 <sup>92</sup> the relativistic constituent quark model (RCQM) [11] and the single quark transition model (SQTM) [12]. 93

The comparison between these predictions and experimental results, on the other hand, is not straightforward. This because the experimentally measured cross sections and asymmetries are usually complicated combinations of resonant and non-resonant amplitudes and couplings, and their

<sup>99</sup> interference terms. To compare with theories, partial wave analyses are often used to extract these amplitudes and reso-100 nance couplings from data. Once comparisons can be made, 101 data are used to provide inputs for constructing or adjusting 102 meson production mechanisms in theories and models, such 103 104 as proper treatment of the hadronic final state and implementation of the non-resonant part of the meson production am-105 plitude. These mechanisms are usually not included in quark 106 models. Examples of phenomenological partial wave analyses 107 that can benefit from more data are MAID [13], JANR [14], 108 <sup>109</sup> SAID [15], and the DMT [16] models. Electron-scattering <sup>110</sup> data used to test these calculations include primarily  $N - N^*$ 111 transition form factors and response functions for meson pro-112 duction reactions obtained from Jefferson Lab (JLab), MAMI 113 and MIT-Bates. Recently, polarization observables such as double spin asymmetries and target spin asymmetries for pion 114 115 electro-production from the proton have made the beam- and 116 target-helicity response functions accessible [17-20], provid-117 ing a new approach to testing models and to a greater under-118 standing of the baryon resonance structure. As an example, 119 the MAID model was based mostly on unpolarized data and 120 is only recently being tested extensively against double po-121 larization asymmetries. In general, polarization observables 122 provide an important constraint on the understanding of the <sup>123</sup> underlying helicity response functions or interference terms 124 in  $N \to \Delta$  and  $N \to N^*$  resonances.

Compared to the proton, existing data on neutron excitation were particularly sparse. Neutron data have recently become available from JLab [21, 22], which make it possible to test the isospin structure of models such as RCQM and SQTM. The neutron data will be valuable to the development of many phenomenological analyses as well because they need to incorporate double polarization asymmetry data for all pion production channels from both the proton and the neutron in order to perform the full isospin decomposition.

In addition, data at very low  $Q^2$  values are often desired for testing the chiral perturbation theory and to study the transition from virtual photons to the real photon point ( $Q^2 = 0$ ). Here,  $Q^2$  is defined as  $Q^2 \equiv -q^2$ , where  $q \equiv (\nu, \vec{q})$  is the

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138 four-momentum transferred from the incident electron to the 139 target and

$$\nu \equiv E - E' \tag{1}$$

141 with E and E' the incident and the scattered elec-142 tron's energies, respectively. At low energy transfers < 2 GeV the most prominent resonances are the  $_{144} \Delta(1232)3/2^+$ ,  $N(1520)3/2^-$  and  $N(1680)5/2^+$  [11]. For 145 the  $N(1520)3/2^-$  and  $N(1680)5/2^+$ , their amplitudes at <sup>146</sup> large  $Q^2$  are determined by perturbative QCD and hadron he-<sup>147</sup> licity conservation. It is expected in this region that  $A^N \rightarrow 1$ , where  $A^N$  is the virtual photon helicity asymmetry defined as:

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$$A^{N} = \frac{|A_{1/2}|^{2} - |A_{3/2}|^{2}}{|A_{1/2}|^{2} + |A_{3/2}|^{2}}, \qquad (2)$$

150 with  $A_{1/2,3/2}$  the scattering amplitudes and the subscripts in-151 dicate the total spin projection of the virtual photon and the 152 nucleon target along the virtual photon's momentum. How-153 ever, data using real photons show a strong helicity-3/2 dominduce and  $A^{N} \rightarrow -1$  [23]. This indicates that  $A^{N}$  for these two resonances must cross zero at some intermediate  $Q^2$  and 155 there have been calculations for the  $Q^2$ -dependence of  $A^N$ 156 from various models [11, 12, 24]. For pion electroproduc-<sup>158</sup> tion, the double spin asymmetry is dominated by  $A^N$  [17] and thus data on this observable will allow us to test a possible 159 sign flip for the  $N(1520)3/2^-$  and  $N(1680)5/2^+$  resonances. 160 Data on the double spin asymmetry of pion photoproduc-161 tion have recently become available from the CBELSA/TAPS 162 Collaboration [25] and are also expeced from JLab experiments [26][27][28], all used the frozen spin target with a lon-164 gitudinal polarization and a circularly polarized photon beam. 165 These photoproduction data will futher test the transition to 193 166 167 the real photon point.

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#### Formalism for Pion Electroproduction Α.

Figure 1 shows the kinematics of single pion production in 169 170 the Born approximation: the electron transfers a virtual photon  $\gamma^*$  of four-momentum  $q \equiv (\nu, \vec{q})$  to the target nucleon N 171 which forms a nucleon resonance. The resonance then decays 172 into a pion and another particle X. Two planes are used to de-173 scribe this process: the scattering (leptonic) plane defined by 174 the incoming and outgoing electrons' momenta  $\vec{k}$  and  $\vec{k'}$ , and 175 the reaction (hadronic) plane defined by the momentum of the 176 virtual photon  $\vec{q}$  and the momentum of the outgoing pion  $\vec{p}_{\pi}$ . 177 The reaction is usually described in terms of  $Q^2$ , the invari-178 179 ant mass W of the  $\gamma^* N$  system (which is also the  $\pi X$  system), 180 and two angles  $\theta^*$  and  $\phi^*$ . Here,  $\theta^*$  is the angle formed by  $\vec{q}$ <sup>181</sup> and  $\vec{p}_{\pi}$ , and  $\phi^*$  is the angle formed by rotating the leptonic <sup>207</sup> <sup>182</sup> plane to the hadronic plane. If one defines the  $\gamma^* N$  center 184 then  $\theta^*$  and  $\phi^*$  are the polar and the azimuthal angles of the 209 trons in the laboratory frame. The  $Q^2$  can be calculated as 185 emitted pion. The energy transfer is related to  $Q^2$  and W via



186 
$$\nu = \frac{W^2 + Q^2 - M^2}{2M} , \qquad (3)$$



FIG. 1. Kinematics of single pion electro-production. The Lorentz boost associated with the transformation from the laboratory to the CM frame of the  $\gamma^* N$  system is along the momentum transfer  $\vec{q}$ , where the coordinates  $\hat{x}, \hat{y}, \hat{z}$  of the CM frame are defined in this picture.

 $_{187}$  with M the nucleon mass. The differential cross section for <sup>188</sup> the reaction  $\vec{e}\vec{N} \rightarrow e\pi(X)$  with longitudinally polarized beam 189 and target can be written in the following form

$$\frac{d^{5}\sigma_{h}}{dE_{e'}d\Omega_{e'}d\Omega_{\pi}^{*}} = \Gamma \frac{d\sigma_{h}}{d\Omega_{\pi}^{*}} , \qquad (4)$$

191 with

192

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$$\frac{d\sigma_h}{d\Omega_\pi^*} = \frac{d\sigma_0}{d\Omega_\pi^*} + P_b \frac{d\sigma_e}{d\Omega_\pi^*} + P_t \frac{d\sigma_t}{d\Omega_\pi^*} + P_b P_t \frac{d\sigma_{et}}{d\Omega_\pi^*}$$
(5)

where  $P_b$  and  $P_t$  are respectively the polarizations of the elec-<sup>194</sup> tron beam and the target along the beam direction,  $\sigma_0$  is the <sup>195</sup> unpolarized cross section, and  $\sigma_e$ ,  $\sigma_t$  and  $\sigma_{et}$  are the polarized 196 cross section terms when beam, target, and both beam and tar-<sup>197</sup> get are polarized. Note that the differential cross sections on <sup>198</sup> the right-hand side of Eq. (5) are defined in the CM frame of <sup>199</sup> the  $\gamma^* N$  system, as indicated by the asterisk in the pion's solid angle. The virtual photon flux is 200

$$\Gamma = \frac{\alpha k_{\gamma}^{\text{lab}}}{2\pi^2 Q^2} \frac{E'}{E} \frac{1}{1-\epsilon} , \qquad (6)$$

where  $\alpha$  is the electromagnetic coupling constant,  $k_{\alpha}^{\text{lab}} =$  $_{203}$   $(W^2 - M^2)/2M$  is the photon equivalent energy in the labo-<sup>204</sup> ratory frame, i.e. the energy needed by a real photon to excite  $_{205}$  the nucleon to an invariant mass W. The virtual photon polar-206 ization is given by

$$\epsilon = \left[1 + \frac{2|\vec{q}|^2}{Q^2} \tan^2 \frac{\theta_e}{2}\right]^{-1},$$
 (7)

$$Q^2 = 4EE'\sin^2\frac{\theta_e}{2}.$$
 (8)

To evaluate the pion's kinematics in the CM frame of the 250 211  $_{212} \gamma^* N$  system, we relate a laboratory-frame 4-momentum vec-

<sup>213</sup> tor  $p^{\mu}$  to the CM-frame  $p^{\mu}_{cm}$  via a Lorentz boost with  $\vec{\beta} = {}_{251}$ 214  $\hat{z}|\vec{q}|/(\nu+M)$  and  $\gamma = (\nu+M)/W$ :

$$p_{\rm cm}^0 = \gamma p^0 - \gamma \beta p^z$$
 ,

$$p_{\rm cm}^x = p^x \; ,$$

$$p_{\rm cm}^y = p^y$$
 ,

$$p_{\rm cm}^z = -\gamma \beta p^0 + \gamma p^z$$
 .

<sup>219</sup> Specifically, we have for the virtual photon:

220 
$$|\vec{q}_{\rm cm}| = \frac{M}{W} |\vec{q}|$$
, (13) 260

$$u_{
m cm}=rac{
u M-Q^2}{W}\,.$$

222 For the pion

$$E_{\rm cm,\pi} = \gamma \left( E_{\pi} - \beta | \vec{p}_{\pi} | \cos \theta_{\pi} \right) , \qquad (15)$$

$$p_{z,\mathrm{cm},\pi} = \gamma \left( \left| \vec{p}_{\pi} \right| \cos \theta_{\pi} - \beta E_{\pi} \right) , \qquad (16)$$

where  $\theta_{\pi} = \arccos[(\vec{q} \cdot \vec{p}_{\pi})/(|\vec{q}||\vec{p}_{\pi}|)]$  is the angle between the <sup>226</sup> pion momentum and  $\vec{q}$  in the laboratory frame, and  $E_{\pi}$  is the 227 pion energy again in the laboratory frame. The polar angle of <sup>228</sup> the pion in the CM frame is given by

$$\theta^* = \arccos\left[\frac{p_{z,\mathrm{cm},\pi}}{\sqrt{E_{\mathrm{cm},\pi} - m_{\pi}^2}}\right]$$
(17)

 $_{230}$  where  $m_{\pi}$  is the pion mass. The azimuthal angle of the pion  $_{276}$ <sup>231</sup> is the same in the laboratory and the CM frame, given by

$$\phi^* = \arccos\left[\frac{\vec{a} \cdot \vec{b}}{|\vec{a}||\vec{b}|}\right] \tag{18}$$

with  $\vec{a} \equiv \vec{q} \times \vec{k}$  and  $\vec{b} \equiv \vec{q} \times \vec{p}_{\pi}$ . In this paper, the range of  $\phi^*$ is defined from 0 to  $2\pi$ , i.e. a shift of  $2\pi$  is added to  $\phi^*$  if the 235 result from Eq. (18) is negative.

The beam, target and double beam-target asymmetries are 236

$$A_{LU} = \frac{\sigma_e}{\sigma_0} , \qquad (19)$$

 $A_{UL} = \frac{\sigma_t}{\sigma_0} \; ,$ 238

$$A_{LL} = -\frac{\sigma_{et}}{\sigma_0} \quad , \tag{21}$$

where each cross section  $\sigma$  stands for the  $d\sigma/d\Omega_{\pi}^*$  of Eq. (5). 241 Note that we have adopted an extra minus sign in the defini- 292 <sup>242</sup> tion of  $A_{LL}$  to be consistent with Eq. (2) and previous CLAS <sup>293</sup> used to detect scattered particles [36]. Figure 2 shows the ba-243 publications [17–19].

244 245 extracted from the JLab CLAS EG4 [29, 30] data. The beam 296 the measurement of multi-particle final states in a large mo- $_{246}$  asymmetry  $A_{LU}$  was also extracted from the data, but was  $_{297}$  mentum region. The detector design is based on a toroidal 247 used only as a cross-check of the beam helicity and is not 298 magnet made by six superconducting coils arranged around <sup>248</sup> presented here. These results are available for download from <sup>299</sup> the beam line to produce a field pointing primarily in the az-249 the CLAS database.

### B. Previous Data

The first double-spin asymmetry for the  $\pi^+ n$  channel was 252 published based on the CLAS EG1a data with a 2.6 GeV <sup>253</sup> beam, for a  $Q^2$  range from 0.35 to 1.5 (GeV/c)<sup>2</sup> [17, 18]. The <sup>(9)</sup>  $_{254} \vec{e}\vec{p} \rightarrow e'p(\pi^0)$  channel was analyzed for the  $\Delta(1232)3/2^+$ (10) 255 region using the same dataset [19]. Similar analysis using the (11) <sup>256</sup> CLAS EG1b data has been completed [20, 22], in which the (12)  $^{257}$  target and the double spin asymmetries were extracted from <sup>258</sup> both the  $\vec{e}\vec{p} \rightarrow e'\pi^+(n)$  and  $\vec{e}\vec{n} \rightarrow e'\pi^-p$  channels using 1.6 <sup>259</sup> to 5.7 GeV beams with  $Q^2$  as low as 0.1 (GeV/c)<sup>2</sup>.

## II. THE JLAB CLAS EG4 EXPERIMENT

(14) 261 The main physics goal of the CLAS EG4 experiment [29, 262 30] was to measure the inclusive spin structure functions on 263 the proton and the deuteron, and to extract the generalized 264 Gerasimov-Drell-Hearn (GDH) sum near the photon point. <sup>265</sup> The original GDH sum rule [31, 32], defined for real photons, is a fundamental prediction on the nucleon's spin structure 266 that relates the helicity-dependent total photo-absorption cross 267 section to the nucleon anomalous magnetic moment. The def-268 269 inition of the GDH sum has been generalized to virtual pho-270 tons [33, 34], and the value of the generalized GDH sum at  $_{271}$  low  $Q^2$  has been predicted in the chiral perturbation theory. 272 Similar to the pion production results presented here, the goal 273 of the EG4's inclusive analysis is to test the chiral perturba-274 tion theory prediction and to compare the extrapolation to the  $_{275} Q^2 = 0$  point with the GDH sum rule of the real photon.

The experiment was carried out in 2006 in experimental 277 Hall B of JLab. Inclusive data were collected in the range  $_{278} 1 < W < 2 \text{ GeV}/c^2$  and  $Q^2$  down to 0.015 (GeV/c)<sup>2</sup> [35], 279 using six beam energies (1.1, 1.3, 1.5, 2.0, 2.3, 3.0 GeV) on <sup>280</sup> a polarized NH<sub>3</sub> target and two energies (1.3, 2.0 GeV) on a polarized ND<sub>3</sub> target. The average polarizations of NH<sub>3</sub> and <sup>282</sup> ND<sub>3</sub> typically ranged within (75 - 90)% and (30 - 45)%, <sup>283</sup> respectively. For the exclusive channel, only NH<sub>3</sub> data with <sup>284</sup> beam energies of 1.1, 1.3, 2.0, 2.3, and 3.0 GeV were analyzed with the lowest  $Q^2$  being 0.0065 (GeV/c)<sup>2</sup>. The 1.5 GeV en-286 ergy data were excluded because they were taken for run com-<sup>287</sup> missioning purpose and had limited statistics. For ND<sub>3</sub> data, <sup>288</sup> the target spin direction was not flipped during the run, which 289 makes it impossible to extract  $A_{UL}$  nor the complete informa-(20)  $_{290}$  tion on  $A_{LL}$  from the exclusive channel.

#### A. The CLAS Detector

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The CEBAF Large Acceptance Spectrometer (CLAS) was 294 sic structure of CLAS during EG4 with the polarized target In this paper, we report on results of both  $A_{UL}$  and  $A_{LL}$  295 installed. CLAS is an almost hermetic detector, optimized for 300 imuthal direction. The field direction can be set such that 301 the scattered negatively-charged particles can be either bent away from the beamline ("electron outbending") or towards it ("electron inbending"). The detector itself is composed of six 303 independent magnetic spectrometers, referred to as six "sec-304 tors", with a common target, trigger, and data acquisition sys-305 tem. Each sector is equipped with a three-layer drift cham-306 ber system (DC) for momentum and tracking determination, a 307 time-of-flight (TOF) counter, a Cherenkov Counter (CC) and 308 a double-layer Electromagnetic Calorimeter (EC). The TOF, 309 CC and the EC systems are primarily used for determining 310 311 the particle type.

In order to reach very low  $Q^2$  while retaining the high beam 312 energy needed to measure the GDH sum, a small scattering 313 angle was necessary. This was achieved by running the CLAS 314 torus magnet in the electron-outbending configuration. Al-315 though the standard CLAS Cherenkov detector geometrically 316 reaches an 8° scattering angle [37], its structure is not ideal 317 for collecting the Cherenkov light for outbending electrons. 318 Therefore, for the EG4 experiment, a new Cherenkov detector 319 was built by the INFN-Genova group and installed in sector 6, 320 as shown in Fig. 2. It was designed to reach 6° scattering angle 321 by optimizing the light collection for the electron-outbending 322 configuration. Due to the very high counting rates at such low 323 scattering angles, instrumenting only one CLAS sector was 324 sufficient for the experiment. The new Cherenkov detector 325 used the same radiator gas  $(C_4F_{10})$  and the gas flow control 326 system used in the standard CLAS Cherenkov. It consisted 327 of 11 segments, each equipped with a pair of light-weight spherical mirrors, see Fig. 3. The mirrors were constructed 329 following [38], by shaping a plexiglass layer onto a spheri-330 cal mould, then gluing onto it a sandwich of carbon fiber and 331 <sup>332</sup> honeycomb, and finally evaporating a thin layer of aluminum 333 onto the plexiglass. Each mirror reflected the light towards a 334 light collector made of two pieces, an entrance section with the approximate shape of a truncated pyramid and a guiding 335 section cylindrical in shape such as to match the circular pho-336 tocathode. Each light collector was made of plexiglass with 337 aluminum evaporated on the internal surface. The entrance 338 section was built by a no-contact technique, where the plex-339 iglass sheet was heated and pushed against a mould with the 340 desired shape, then the bottom of the obtained object was cut 341 <sup>342</sup> to permit the free passage of light. The cylindrical section was <sup>343</sup> obtained by cutting a plexiglass tube. The two sections were then glued together before evaporating the reflective layer. For 344 the PMTs, the Photonis XP4508B with quartz window were 345 346 chosen. The photoelectron yield was greater than  $\approx 10$  within the kinematic region of the experiment, thereby yielding a 347 high electron detection efficiency down to a scattering angle 348 of about 6°. Signals from the new Cherenkov were built into 349 the main electron trigger during EG4. Consequently only 1/6 350 of the full azimuthal acceptance of CLAS was used to detect 351 352 and identify forward-angle scattered electrons.

#### 354

#### The Polarized Electron Beam В.

355 356 a strained GaAs photocathode with circularly polarized light. 363 tainties, data were taken for two different beam helicity con-



FIG. 2. (Color online) CLAS during EG4 showing the polarized target and the detector arrangement. A new Cherenkov detector consisting of 11 segments was installed in place of the original Cherenkov in sector 6. It provided the ability of detecting scattered electrons in the outbending configuration with scattering angles as small as  $6^{\circ}$ (dashed-line track).



FIG. 3. (Color online) The new Cherenkov detector designed and built by the INFN-Genova group. It consists of 11 pairs of mirrors with spherical curvature, which reflect the Cherenkov light to corresponding photo-multiplier tubes (PMTs). Only one of the two support planes for the PMTs is shown here. The solid blue lines show simulated particle trajectories originated from the CLAS center and the reflection of the Cherenkov light towards the PMT.

357 The helicity of the electron beam was selected from a pseudorandom sequence, and followed a quartet structure of either "+--+" or "-++-", with each helicity state lasting 33 ms. <sup>360</sup> The helicity sequence controlled the trigger system, and peri-361 ods of beam instability due to helicity reversal were rejected The polarized electron beam was produced by illuminating 362 from the data stream. To reduce possible systematic uncer<sup>364</sup> figurations, with the beam insertable half-wave plate (IHWP) 365 inserted (in) and removed (out), respectively. The polariza-366 tion of the electron beam was measured by both a Møller and 367 a Mott polarimeter.

#### 368

#### C. **The Polarized Targets**

The polarized targets used for EG4 were the frozen <sup>15</sup>NH<sub>3</sub> 369 <sup>370</sup> and <sup>14</sup>ND<sub>3</sub> targets dynamically polarized at 1 K with a 5-Tesla field. These were the same as the targets used for pre-371 vious CLAS double-polarization measurements [39]. The tar-372 get material was irradiated with 20 MeV electrons prior to the 373 experiment to impart the paramagnetic radicals necessary for 374 dynamic polarization. It was subsequently stored in liquid ni-375  $_{376}$  trogen (LN<sub>2</sub>) until needed for the experiment. The material, <sup>377</sup> in the form of 1-2 mm sized granules, was then removed from 378 the LN<sub>2</sub> storage dewars and loaded into two cylindrical containers on the target insert. The structure of the target insert is 379 shown in Fig. 4. The containers were either 1.0 cm or 0.5 cm 380 in length, hereafter referred to as the long and short cells, re-381 spectively. The insert was then quickly placed into the target 382 'banjo", a 1-2 liter vessel of 1-K liquid helium at the center of a 5-T superconducting split coil magnet. A complete descrip-384 <sup>385</sup> tion of the polarized target can be found in Ref. [40].



FIG. 4. (Color online) Target insert used during the EG4 experiment. A 1.0-cm long NH<sub>3</sub> and the 0.5-cm long NH<sub>3</sub> targets were installed in the Long and Short NH<sub>3</sub> positions during the first half of the NH<sub>3</sub> run period. They were called the "long NH<sub>3</sub> top" and the "short NH<sub>3</sub>" targets, respectively. During the second half of the NH<sub>3</sub> run, two 1.0-cm long NH<sub>3</sub> targets were installed in the Long and the Short positions; they were called the "long NH<sub>3</sub> top" and the "long NH<sub>3</sub> bottom" targets, respectively. For the ND<sub>3</sub> run period only one 1.0cm long ND3 target was installed in the Short position. The five 416 target positions are labeled A, B, C, D, and E, as shown.

386 387

388 389 390 391 TABLE I. Targets used during EG4 along with their target lengths and densities. The target ID was the value recorded in the data. ID 10 was not used. The target position refers to the physical location on the target insert defined in Fig. 4.

Target	Target type	Target	length	Density
ID		position	(cm)	$(g/cm^3)$
1	long NH <sub>3</sub> top	А	1.0	0.917 <sup>a</sup>
2	long $ND_3$	В	1.0	1.056 <sup>a</sup>
3	empty cell with helium	Е	1.0	0.145 <sup>b</sup>
4	long carbon	С	$1.0, 0.216^c$	2.166 <sup>d</sup>
5	short NH <sub>3</sub>	В	0.5	0.917 <sup>a</sup>
6	short carbon	D	$0.5, 0.108^c$	$2.166^{d}$
7	long carbon no helium	С	$1.0, 0.216^c$	$2.166^{d}$
8	empty cell without helium	Е	1.0	
9	short carbon without helium	D	0.5	2.166 <sup>c</sup>
11	long NH <sub>3</sub> bottom	В	1.0	0.917 <sup>a</sup>

<sup>a</sup> For polarized NH<sub>3</sub> or ND<sub>3</sub> the densities are the density of the frozen polarized material beads.

<sup>b</sup> Helium density.

<sup>c</sup> The first and the second length values correspond to the cell length and the carbon foil thickness, respectively.

<sup>d</sup> Carbon density.

not be directly measured. The fraction of the target filled by 392 frozen polarized material is called the "packing factor" and is 393 394 typically extracted by comparing the yield from the polarized target to those from carbon and "empty" targets. For the car-395 bon target, a carbon foil with known thickness was placed in 396 397 an empty target cell and filled with liquid <sup>4</sup>He. There were two carbon targets, labeled "long" and "short" carbon, of which 398 both the cell length and the foil thickness match those of the 399 long and the short NH<sub>3</sub> targets, respectively. Empty targets 400 refer to target cells with no solid material inside. Empty tar-401 gets can either be filled with liquid <sup>4</sup>He, or the <sup>4</sup>He can be 402 completely pumped out. There was only one empty cell dur-<sup>404</sup> ing EG4 to physically host the empty targets, which was 1.0 cm in length. 405

During EG4 the polarized target was placed 1.01 m up-406 407 stream from the CLAS center to increase the acceptance at  $_{408}$  low  $Q^2$  by reducing the minimum angle for the scattered elec-409 trons. The following targets were used: two 1.0-cm long and <sup>410</sup> one 0.5-cm long NH<sub>3</sub> target, one 1.0-cm long ND<sub>3</sub> target, one 0.216-cm and one 0.108-cm thick <sup>12</sup>C target, and one empty 412 target. The target types during EG4 are defined in Table I. Un-<sup>413</sup> less specified otherwise, "empty target" refers to target type 3 [empty cell with helium (1 cm)] hereafter. 415

An NMR system was used to monitor the polarization of 417 the target during the experiment, but was subject to three sys-418 tematic uncertainties that limited its suitability for data anal-Due to the presence of gaps between the frozen crystals 419 ysis. First, the NMR coils were wrapped around the outside inside the target cell, even if the length of the target cell or 420 of the 1.5-cm diameter target cells, while the electron beam the banjo could be determined precisely, the exact amount of 421 was only rastered over the central 1.2 cm portion of the target. polarized materials interacting with the electron beam could 422 The NMR signal was thus dominated by the material at the

423 edges of the cell, and lacked sensitivity to the beam-induced depolarization of the material at the center. This uncertainty is 424 difficult to estimate, as the effect depends on the accumulated 425 dose. Second, for the EG4 experiment the two polarized target 426 cells were adjacent to one another on the insert, as shown in 427 428 Fig. 4, and cross-talk was observed between the cells' NMR 429 circuits. Tests performed at the end of the experiment indi-430 cate that cross-talk could contribute an uncertainty of about  $_{431}$  5-10% to the polarization measurement due to its effect on <sup>432</sup> the thermal-equilibrium calibration of the NMR signal. Third, 433 calibration of the NMR system itself is normally subject to a 4-5% uncertainty. These three effects added up to a large 434 systematic uncertainty to the target polarization measured by 435 NMR. Therefore, it was decided that the asymmetries of ep 436 elastic scattering would be used to extract the product of the 437 beam and target polarizations  $P_b P_t$  needed for the exclusive 438 channel analysis reported here. The methods and results for 439 <sup>440</sup> the elastic  $P_b P_t$  extraction will be described in Section III D. 441 For NH<sub>3</sub>, the use of  $^{15}$ N has the advantage that only one unpaired proton can be polarized, while all neutrons are paired 442 <sup>443</sup> to spin zero. The polarized proton in the <sup>15</sup>N does however affect the measured asymmetry by a small amount, as discussed 444 445 in Section III G.

446

#### III. DATA ANALYSIS

447

## A. Exclusive Event Selection

Exclusive events  $\vec{e}\vec{p} \rightarrow e'\pi^+(n)$  were identified by detect-448 ing the final state electron in coincidence with a pion and us-449 ing a missing mass cut to select the undetected neutron. For 450 each event, we required that two particles be detected with 451 the correct charges (-1 for the electron and +1 for the  $\pi^+$ ). 452 Each particle was required to have valid information from 453 DC and TOF, and have reconstructed momentum greater than 454 0.3 GeV/c (0.1 GeV/c higher than the momentum acceptance 455 of CLAS [36]). 456

For particle identification, EC and CC signals were used 457 to identify electrons. Cuts were applied on the EC:  $E_{tot} >$ 458  $(p-0.3) \times 0.22, E_{in} > (0.14p-0.8E_{out}) \text{ and } E_{in} > 0.035p,$ 459 where  $E_{in}$  and  $E_{out}$  are the energy deposited in the inner and 460 461 the outer layers of the EC, respectively;  $E_{tot} = E_{in} + E_{out}$ and p is the particle momentum in GeV/c. These cuts were 462 selected to optimize the separation of electrons (that pro-463 duce electromagnetic showers) from pions (that deposit en-464 ergy mostly through ionizations). We also required there to 487 465 466 from the EC and the TOF in both hit position and timing. 467

468 469 470 471 472 473 474 475 clearly selected pions out of other particle background.

For each event, a vertex z was used. Here z is defined as 498 on the asymmetries will be described in Sec. III H. 476



FIG. 5.  $\beta$  vs. p for all positively charged particles, with (red) and without (black) TOF cut for pions. The red, green and blue curves correspond to reconstructed masses of 0.3, 0.7 and 1.2 GeV/ $c^2$ , respectively, which are typical cut-off values used to distinguish between pions and kaons, kaons and protons, and protons and heavier particles. As can be seen, the positively charged particles detected consist of significant fractions of protons and heavier particles and a small fraction of kaons, but the  $\pm 1.0$  ns TOF cut is quite effective in selecting pions. These data were collected on the long top NH<sub>3</sub> target during the 3 GeV run period.

pointing along the beam direction with the origin coincides 477 478 with the CLAS center. The polarized target was positioned 479 upstream of the CLAS center during EG4 (see Fig. 2), and the 480 center of the target was determined from empty target data to <sub>481</sub> be at z = -101 cm. The z cut was optimized to be

$$-106 \text{ cm} < z < -96 \text{ cm}$$
, (22)

483 where the range was determined using empty target data to <sup>484</sup> exclude as much material outside the target as possible. See <sup>485</sup> Fig. 7 in Section IIIC for a detailed presentation of the vertex z distribution. 486

Acceptance cuts, also called "fiducial cuts", were applied be only one hit in the CC, with its signal consistent with those 488 on both electrons and pions using reconstructed DC variables. 489 These acceptance cuts exclude regions where the detector ef-Pions were determined from a mass cut of 0.01 < m < 490 ficiency is not well understood, which often happens on the  $0.30 \text{ GeV}/c^2$  and a TOF cut  $|t_{TOF} - t_{\text{expected}}^{\pi}| < 1.0 \text{ ns.}^{491}$  edge of the detectors, but could also include regions where The expected flight time of the pion,  $t_{\text{expected}}^{\pi}$ , was calculated  ${}^{492}$  certain parts of the detectors malfunctioned. Moreover, befrom the particle's momentum in combination with the timing 493 cause the main purpose of EG4 was measurement of the GDH of the electron. Figure 5 shows the effect of the TOF cut on 494 sum, which only requires detection of inclusively-scattered the  $\beta \equiv v/c$  vs. momentum p distributions, where v is the 495 electrons, not all six DC sectors were turned on during the velocity amplitude (speed) of the particle. The TOF cut used  $_{496}$  run. This caused a variation in the  $\phi^*$  acceptance of the exclu-<sup>497</sup> sive channel. Determination of the acceptance and its effects

## **B.** Beam Properties

As described in the previous section, the helicity of the elec-500 <sup>501</sup> tron beam followed a quartet structure. For EG4, the beam <sup>502</sup> helicity of each event was delayed by 8 pulses (2 quartets) <sup>503</sup> and then recorded in the data stream. This delayed recording helped to avoid cross-talk between the helicity signal and the 504 electronics or data acquisition system in the hall. In the data 505 analysis, the delay of the helicity sequence was corrected to 506 match each event to its true beam helicity state. During this 507 process, events with inconsistent recording of the helicity se-508 quence were rejected. 509

A helicity dependence of the integrated beam charge causes 510 first-order correction to the measured physics asymmetry, 511 а <sup>512</sup> and thus it is desired to keep the charge asymmetry as small as possible. The beam charge asymmetry was calculated using 513 the charge measured by the Faraday cup. It was found to be 514 below the percent level throughout the EG4 experiment, and 515 or most runs had stable values at or below the  $10^{-3}$  level. 516

Different methods for deriving the beam energy were used 517 during EG4. The exact energies were 1.054, 1.338, 1.989, 518 2.260 and 2.999 GeV. The beam polarization was determined 519 using a Møller polarimeter [36] in Hall B that measured the 520 asymmetry in elastic electron-electron scattering. The re-521 sults are shown in Fig. 6. Typically, Møller measurements 522 were performed as soon as a change to the beam configu-523 ration was made, and then intermittently throughout the run 524 period. Therefore, the beam polarization from each Møller 553 The beam position was then used to re-calculate the vertex po-525 526 527 528 529 530 531 532 ter results were consistent with those from Møller measure- 561 vertex position randomly for each particle. 533 ments. The absolute beam helicity was determined using the 562 534 535 537 538 539 540 541 543 544 larimeter.

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#### С. **Kinematic Corrections**

Various corrections were applied to the kinematic variables 577 546 547 reconstructed from the detectors [47]. The first is the raster 578 the energy loss due to passage through material enclosed in 548 549 550 of the magnet current were recorded in the data stream and 582 the ionization loss. 551 <sup>552</sup> were used to calculate the beam position (x, y) at the target. <sup>583</sup>



FIG. 6. Beam polarization from Møller measurements vs. run number for the whole EG4 experiment. The grey bands represent extrapolations of the beam polarization to the corresponding range of runs as described in the text.

measurement was applied retroactively to runs that immedi- 554 sition along the beam direction z. After the raster correction ately follow such configuration changes, and to runs that fol- 555 was applied, the average value of the z positions of all partilow the Møller measurement until the next valid measure- 556 cles in the same event was taken as the true vertex position of ment is available. Two additional measurements were done 557 the event, see Fig. 7 [47]. The polar and the azimuthal angles using a Mott polarimeter [41–44], which is located near the 558  $\theta$  and  $\phi$  of each particle were also corrected using the new injector where the beam electrons have reached 5 MeV in en- 559 beam and vertex positions. This procedure took into account ergy but before entering the first linac. The Mott polarime- 560 the multiple scattering effect that affected the reconstructed

Due to uncertainties in our knowledge of the drift chamber  $\sin \phi^*$ -weighted moment of the beam asymmetry  $A_{LU}$  in the 563 positions and of the shape and location of the torus coils, a  $\Delta(1232)3/2^+$  region and comparing with results from previ- 564 systematic shift of the particle momentum was present. To ous experiments [45, 46]. Using the  $A_{LU}$  method, it was de- 565 correct for this shift, the magnitude of the reconstructed partermined that when the beam IHWP is inserted, for beam ener- 566 ticle momentum p and the polar angle  $\theta$  were adjusted usgies 1.3 and 2.3 GeV, the positive DAQ helicity corresponds to 567 ing sector-dependent parameters. The detailed method for the the true negative helicity of the beam electron, while for other 568 momentum correction is described in Ref. [48] and results for energies the postive DAQ helicity corresponds to the true posi- 569 this experiment are given in Ref. [47]. For sector 6 equipped tive electron helicity. These results are consistent with the sign 570 with the new Cherenkov counter, inclusive elastic ep scatterchange of the beam polarization measured with the Møller po- 571 ing events were used to optimize the correction based on the  $_{572}$  invariant mass W position of the elastic peak. For the other 573 sectors, electron triggers were not available and hadrons from signal exclusive events such as  $ep \to e'p'X$ ,  $ep \to e'\pi^+\pi^-X$ , and 575 exclusive events  $ep \rightarrow e'p'\pi^+\pi^-$  were used to optimize the 576 corrections.

Finally, the momentum of each particle was corrected for correction: in order to avoid the electron beam overheating the 579 the target banjo and the target windows. For electrons a single target, the beam was rastered in a circular pattern during EG4 580 value  $dE/dx = 2.8 \text{ MeV/(g/cm^2)}$  was used, while for other using four magnets located upstream of the target. The values 581 particles the Bethe-Bloch equation [49] was used to calculate

Figure 8 shows the effect on the missing mass spectrum for



FIG. 7. Electrons' vertex z position before (dashed) and after (solid) <sup>604</sup> raster corrections, taken with the empty target with the 3 GeV beam. While the beam line exit window (at z = -78.3 cm) can be seen both before and after the correction, the banjo windows (at z = -100 and 605 where  $N_{R(L)}^{el}$  and  $Q_{R(L)}$  are the elastic event yield and the foils (aluminum or aluminumized mylar, between z = -90.5 and -94.1 cm), become visible only after the raster correction. The vertex z cut, Eq. (22), corresponds to slightly more than  $3\sigma$  in the target thickness [47].

the  $ep \to e'\pi^+(X)$  channel from kinematic corrections.



FIG. 8. Missing mass spectrum for the  $e + p \rightarrow e' \pi^+(X)$  channel 620 before (dashed) and after all kinematics corrections (solid), from six 3.0-GeV long top NH3 target runs. After all corrections, the peak center is closer to the expected value (the neutron mass). 585

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587

#### **D.** Elastic Scattering for Extracting $P_b P_t$

588 589 is needed to directly correct the exclusive channel asymme- 630 GeV data sets. For lower beam energies, the proton's scatter-<sup>590</sup> tries. During EG4, the target polarization  $P_t$  was measured by <sup>631</sup> ing angle was typically greater than 49°, and was blocked by

<sup>591</sup> NMR and the beam polarization  $P_b$  by the Møller polarimetry. However, due to reasons described in Section IIC, the NMR 592 measurements had large uncertainties and an alternate method 593 had to be used. For EG4 we extracted  $P_b P_t$  for all beam en-594 ergies by comparing the double spin asymmetry of elastic ep 595 events to the expected value:

$$P_b P_t = \frac{A_{\rm meas}^{el}}{A_{\rm th}^{el}} \,, \tag{23}$$

where the measured elastic asymmetry was extracted from 598 599 data using

$$A_{\rm meas}^{el} = \frac{A_{\rm raw}^{el}}{f_{el}},\tag{24}$$

with  $f_{el}$  the elastic dilution factor to account for the effect of 602 events scattered from unpolarized material in the target. The 603 raw asymmetry was evaluated as

$$A_{\rm raw}^{el} = \frac{\frac{N_{R}^{el}}{Q_{R}} - \frac{N_{L}^{el}}{Q_{L}}}{\frac{N_{R}^{el}}{Q_{R}} + \frac{N_{L}^{el}}{Q_{L}}},$$
(25)

-102 cm), the 4 K heat shield (14  $\mu$ m aluminum at z = -121.0 cm), 606 beam charge for the right- (left-)handed beam electrons, resome target structure at  $z \approx -112$  cm, and several insulating 607 spectively. The expected elastic-scattering asymmetry  $A_{\rm th}^{el}$ 608 was calculated using

$$A_{\rm th}^{el} = -2\sqrt{\frac{\tau}{1+\tau}}\tan\frac{\theta_e}{2}$$

$$\times \frac{\left[\sqrt{\tau\left(1+(1+\tau)\tan^2\frac{\theta_e}{2}\right)}\cos\theta_e + \sin\theta_e\frac{G_E^p}{G_M^p}\right]}{\left[\frac{(G_E^p/G_M^p)^2 + \tau}{1+\tau} + 2\tau\tan^2\frac{\theta_e}{2}\right]} (26)$$

611 with  $\tau = Q^2/(4M^2)$ . The proton form factor fits from 612 Ref. [50] were used:

$$G_E^p = 1/[1+0.62Q+0.68Q^2+2.8Q^3+0.83Q^4] (27)$$

614 and

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616

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610

$$G_M^p = 2.79 / \left[ 1 + 0.35Q + 2.44Q^2 + 0.5Q^3 + 1.04Q^4 + 0.34Q^5 \right]$$
(28)

617 with  $Q \equiv \sqrt{Q^2}$  in GeV/c. Using a more updated fit of the 618 proton form factors than Ref. [50] would change the asymmetry value by less than 2% relative. 619

Elastic events were identified using two methods: 1) in-621 clusive elastic events where only the scattered electron was detected and a cut on the invariant mass W near the pro-622 623 ton peak was applied; and 2) exclusive elastic events where 624 both the scattered proton and electron were detected and cuts 625 were applied to the electron and the proton azimuthal angles:  $_{626} |\phi_e - \phi_p - 180^\circ| < 3^\circ$ , the polar angles of the proton and 627 the electron's momentum transfer  $\vec{q}$ :  $|\theta_p - \theta_q| < 2^\circ$ , and the  $_{628}$  missing energy  $E_{
m miss}~<~0.15$  GeV. The exclusive analysis The product of the beam and the target polarizations  $P_b P_t$  629 had limited statistics and only worked for the 3.0 and the 2.3

 $_{632}$  the polarized target coils. Therefore the  $P_bP_t$  value extracted from exclusive elastic events was only used as a cross-check of the  $P_h P_t$  from inclusive events. 634

The presense of unpolarized material reduces the measured 635 636 asymmetry, and this effect is described as a dilution factor 637 in the analysis. The dilution factor for the inclusive elastic 638 events,  $f_{el}^{\text{incl}}$ , was extracted by comparing the invariant mass W spectrum of the polarized target to that computed for the 639  $_{640}$  unpolarized material. The beam-charge-normalized W spec-641 trum for the unpolarized material in the polarized target, de-<sup>642</sup> noted as  $\frac{N_{\rm N \ in \ NH_3}}{Q_{\rm NH_3}}$ , was calculated using the spectra of the 643 carbon and the empty target, the known thickness and density 644 of the carbon and the empty target, and the polarized target's  $_{645}$  packing factor  $x_{\rm NH_3}$  defined as the absolute length of the po-646 larized material in the polarized target:

647 
$$\frac{N_{\rm N \ in \ NH_3}}{Q_{\rm NH_3}} = r_C \frac{N_{\rm ^{12}C}}{Q_{\rm ^{12}C}} + r_{\rm empt} \frac{N_{\rm empt}}{Q_{\rm empt}} , \qquad (29)$$

648 where  $N_{\rm ^{12}C(empt)}$  and  $Q_{\rm ^{12}C(empt)}$  are the yield and the beam 649 charge of the carbon (empty) target data. The scaling factors 650 are

$$r_{C} = \frac{\left(B_{\rm NH_{3}}\rho_{\rm NH_{3}}x_{\rm NH_{3}} + B_{w}\rho_{w}x_{w}\frac{x_{\rm NH_{3}}}{l}\right)}{B_{12}C\rho_{12}Cx_{12}C + B_{w}\rho_{w}x_{w}\frac{x_{12}C}{l}}, \quad (30)$$

$$r_{\rm empt} = \left(1 - \frac{x_{\rm NH_3}}{l}\right) - \left(1 - \frac{x_{\rm 1^2C}}{l}\right) r_C , \qquad (31)$$

 $_{653}$  where  $x_{^{12}C}$  is the thickness of the carbon foil in the carbon target,  $x_w$  is the sum of thicknesses of other unpolarized material  $_{687}$  exclusive channel. Figure 10 illustrates the variation of  $P_b P_t$  $_{655}$  in the target, l is the target banjo length (1.0 cm for the long  $_{688}$  during the experiment. 656 target and 0.5 cm for the short target), and  $B_{12C,w} = 1$  are the 689 bound-nucleon fractions of the carbon target and other unpo-657 658 the various materials are given in Table II. The bound-nucleon 659 660 <sup>661</sup> of bound nucleons and a correction for the extra neutron in the 662  $\sigma_{p,n}$  are the calculated elastic cross sections for the proton and 664 the neutron, respectively.

666 known, the dilution factor was calculated using

667 
$$f_{el}^{\text{incl}} = \frac{N_{\text{p in NH}_3}}{N_{\text{NH}_3}} = \frac{N_{\text{NH}_3} - N_{\text{N in NH}_3}}{N_{\text{NH}_3}},$$
 (32)

669 get. The dilution correction to the elastic asymmetry was then 670 applied using Eq. (24). In the present analysis, elastic events 705  $_{671}$  below  $Q^2 = 0.156$  (GeV/c)<sup>2</sup> could not be used because of  $_{706}$  parison between inclusive and exclusive elastic events, the  $_{672}$  electrons scattered elastically from nuclei in the target, such  $_{707}$   $en \rightarrow e'\pi^-(p)$  channel was also used to check  $x_{\rm NH_3}$  because  $_{673}$  as <sup>4</sup>He and nitrogen. These low  $Q^2$  bins were rejected in the  $_{708}$  these events come primarily from the unpolarized neutrons of 674  $P_b P_t$  analysis.

675 676  $_{677}$  low  $Q^2$  bin (top) is to illustrate the effect of the nuclear elastic  $_{712}$  the  $x_{\rm NH_3}$  values in Table III were indeed consistent with zero. scattering and these bins were rejected from the  $P_bP_t$  analysis. <sup>713</sup> As a last check, the run-by-run values of  $P_bP_t$  were compared est extracted are considered reliable. After the  $P_b P_t$  value was 715 during the experiment, and were found to be consistent with est extracted for individual  $Q^2$  bins, the results were checked to 716 the physical changes of the target.

TABLE II. Material used for the EG4 target and their locations in increasing order of z, in the range z = (-120, -80) cm. The ratios Z/A were used in the dilution factor analysis of the exclusive channel, see Sec.IIIF.

location $z$ (cm)	Material	Density (g/cm <sup>3</sup> )	Thickness	Z/A
-101.9	banjo entrance window, Al	2.7	$71 \ \mu \mathrm{m}$	13./26.982
varies	target entrance window, kapton	1.42	$25~\mu{ m m}$	0.51264
varies	$NH_3$	0.917	$x^a$	7/18
varies	long <sup>12</sup> C	2.166	$2.16{\pm}0.05~\mathrm{mm}$	6/12
varies	liquid <sup>4</sup> He	0.145	$l - x^a$	2/4
varies	target entrance window kapton	1.42	$25~\mu{ m m}$	0.51264
-99.6	banjo exit win- dow Al	2.7	$71~\mu{ m m}$	13./26.982

<sup>a</sup> l is the banjo length and x is either the packing factor (for  $NH_3$ ) targets) or the carbon foil thickness (for carbon targets).

 $_{682}$  ensure there was no systematic  $Q^2$ -dependence, which would imply a problem with the analysis. The  $P_b P_t$  results were then ) <sub>684</sub> averaged over all  $Q^2$  bins above 0.156 (GeV/c)<sup>2</sup>. This was  $_{685}$  done for each individual run and the run-by-run,  $Q^2$ -averaged  $_{686}$   $P_bP_t$  results were used to correct the asymmetries from the

The uncertainty of the packing factor  $x_{\rm NH_3}$  used in the 690 analysis was checked using the W spectrum below W =larized material in the target, respectively. The values of x for  $_{691}$  0.9 (GeV/ $c^2$ ), since an incorrect normalization would yield 692 an over- or an under-subtraction of the yield from unpolarized fraction for the NH $_3$  target takes into account both the fraction  $_{693}$  material. For the 2.3 and 3.0 GeV data the value of  $x_{\rm NH}_3$  was <sup>694</sup> confirmed by comparing the  $P_h P_t$  value extracted from the <sup>15</sup>N:  $B_{\rm NH_3} = (14 + \sigma_n/\sigma_N)/18$  with  $\sigma_N = (\sigma_p + \sigma_n)/2$  and <sub>695</sub> inclusive to that from the exclusive elastic events. The pack-696 ing factor and its uncertainty also affect the dilution analysis <sup>697</sup> of the exclusive channel, to be described in the next sections, After the contribution from the unpolarized material was  $_{698}$  thus the final results on  $P_bP_t$  for each combination of beam <sup>699</sup> energy and polarized target type are shown together with the <sup>700</sup> exclusive channel dilution results in Table III. The relatively ) 701 larger error bar for the 1.1 GeV NH<sub>3</sub> long bottom target is 702 because most of the data were affected by the nuclear elastic <sup>668</sup> where  $N_{\rm NH_3}$  is the total number of events from the NH<sub>3</sub> tar-<sup>703</sup> scattering and there are very limited  $Q^2$  bins available for the <sup>704</sup> elastic  $P_b P_t$  analysis.

In addition to checking the W spectrum and the com-<sup>709</sup> the nitrogen in the target and thus should have a dilution fac-Figure 9 shows the W spectrum decomposition for 1.1 and  $^{710}$  tor of zero. The  $e'\pi^-(p)$  events were analyzed for all beam 3.0 GeV inclusive elastic scattering data for two  $Q^2$  bins. The 711 energies and it was found the dilution factors calculated using The high  $Q^2$  bin (bottom) shows no such effect and the  $P_b P_t$  <sup>714</sup> with the numerous target material and configuration changes



FIG. 9. W-spectrum for dilution calculation for inclusive elastic  $P_bP_t$  analysis. Top: 1.1 GeV data on NH<sub>3</sub> long bottom target in the  $Q^2 = (0.054, 0.092)$  (GeV/c)<sup>2</sup> bin; bottom: 3.0 GeV data on  $\mathrm{NH}_3$  long top target in the  $Q^2 = (0.266, 0.452) (\mathrm{GeV}/c)^2$  bin. For each panel, histograms from the carbon target (blue) and empty target (green) were scaled using Eqs. (30-31) using a packing factor of 0.75 cm for 1.1 GeV and 0.65 cm for 3.0 GeV respectively, and their sum gave the estimated contribution from unpolarized material in the NH<sub>3</sub> target (magenta). This unpolarized background was then subtracted from the NH<sub>3</sub> spectrum (black) to estimate the contribution from polarized protons in the target (red). The calculated elastic dilution factors are shown for each set of data with their uncertainties in the brackets. The W cuts used to select elastic events are shown as the two red vertical lines. Note that the scaled empty target spectrum (green) is negative, indicating that for the chosen packing factor we have scaled up the carbon data and then subtracted the extra helium to reproduce the unpolarized background in NH<sub>3</sub>. For  $Q^2$  bins below  $0.156 (\text{GeV}/c)^2$ , the nuclear elastic event contaminates the ep elastic peak and the extraction of the dilution factor is not reliable. For this reason, data with  $Q^2 < 0.156 (\text{GeV}/c)^2$  were rejected from the elastic  $P_b P_t$  analysis.

#### 717 E. Extraction of Exclusive Channel Asymmetries

To extract the exclusive channel asymmetries, the  $e'\pi^+(n)$ rig channel events were divided into four-dimensional bins in W, red  $Q^2$ ,  $\cos \theta^*$  and  $\phi^*$  and then the asymmetries were extracted ref from the counts in each bin. The event counts for the four



FIG. 10. Magnitude of  $P_b P_t$  extracted from inclusive elastic scattering events for all runs used in the present analysis that were taken on the polarized NH<sub>3</sub> target. For illustration purposes, results from adjacent runs that shared the same beam insertable half-wave plate status were combined and are shown as one data point here. The error bars shown are statistical uncertainties determined by the number of available elastic events.

r22 combinations of beam helicities and target polarization can ber23 written, based on Eq. (5), as

$$N_{\uparrow\uparrow\uparrow} = D_1 \left[ \sigma_0 + P_b^{\uparrow\uparrow} \sigma_e + f_{\rm dil}^{\pi} P_t^{\uparrow\uparrow} \sigma_t + P_b^{\uparrow\uparrow} f_{\rm dil}^{\pi} P_t^{\uparrow\uparrow} \sigma_{et} \right] \tag{33}$$

$$N_{\downarrow\uparrow\uparrow} = D_2 \left[ \sigma_0 - P_b^{\scriptscriptstyle \parallel} \sigma_e + f_{\rm dil}^{\scriptscriptstyle \pi} P_t^{\scriptscriptstyle \parallel} \sigma_t - P_b^{\scriptscriptstyle \parallel} f_{\rm dil}^{\scriptscriptstyle \pi} P_t^{\scriptscriptstyle \parallel} \sigma_{et} \right]$$
(34)

$$N_{\uparrow\downarrow\downarrow} = D_3 \left[ \sigma_0 + P_b^{\downarrow} \sigma_e - f_{\mathrm{dil}}^{\pi} P_t^{\psi} \sigma_t - P_b^{\downarrow} f_{\mathrm{dil}}^{\pi} P_t^{\psi} \sigma_{et} \right] (35)$$

$$N_{\downarrow\downarrow\downarrow} = D_4 \left[ \sigma_0 - P_b^{\downarrow\downarrow} \sigma_e - f_{\rm dil}^{\pi} P_t^{\downarrow\downarrow} \sigma_t + P_b^{\downarrow\downarrow} f_{\rm dil}^{\pi} P_t^{\downarrow\downarrow} \sigma_{et} \right]$$
(36)

where the arrows in the subscripts of N are for the beam he-729 licities ( $\uparrow$  or  $\downarrow$ ) and the target spin directions ( $\uparrow$  or  $\Downarrow$ ), respec- $_{730}$  tively, with  $\uparrow$  and  $\uparrow$  being positive helicity or parallel to the 731 beam direction and  $\downarrow$  and  $\Downarrow$  being negative helicity or antiparallel to the beam direction. The parameters  $P^{\uparrow}$  and  $P^{\downarrow}$  are 732 the statistically-averaged target or beam polarizations when 733 the target spin is aligned and anti-aligned to the beamline, re-734 735 spectively. The dilution factor  $f_{
m dil}^{\pi}$  for the exclusive channel 736  $\vec{e}\vec{p} \rightarrow e'\pi^+(n)$  is defined as the fractional yield from the po-737 larized proton in the NH<sub>3</sub> target, which effectively changes the target polarization. The four parameters  $D_{1,2,3,4}$ , relating 738 739 event counts to cross sections, are related to the total beam 740 charge, target thickness, spectrometer acceptance, and detec-741 tor efficiencies for each configuration. For stable running pe-<sup>742</sup> riods with no significant change in the target cell, the spec-<sup>743</sup> trometer setting and the detector status, the D factor is strictly 744 proportional to the accumulated beam charge in each setting. <sup>745</sup> From Eqs. (33–36), one can form the asymmetries as:

$$A_{LU} = \frac{1}{P_b^{\uparrow} P_b^{\Downarrow}} \times$$

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$${}^{747} \qquad \left[ \frac{\left(\frac{N_{\uparrow\downarrow\downarrow}}{D_3} - \frac{N_{\downarrow\downarrow\downarrow}}{D_4}\right) P_b^{\uparrow\uparrow} P_t^{\uparrow\uparrow} + \left(\frac{N_{\uparrow\uparrow\uparrow}}{D_1} - \frac{N_{\downarrow\uparrow\uparrow}}{D_2}\right) P_b^{\downarrow\downarrow} P_t^{\downarrow\downarrow}}{\left(\frac{N_{\uparrow\uparrow\uparrow}}{D_1} + \frac{N_{\downarrow\uparrow\uparrow}}{D_2}\right) P_t^{\downarrow\downarrow} + \left(\frac{N_{\uparrow\downarrow\downarrow}}{D_3} + \frac{N_{\downarrow\downarrow\downarrow}}{D_4}\right) P_t^{\uparrow\uparrow}} \right] , (37)$$

$$A_{UL} = \frac{1}{f_{\text{dil}}^{\pi}} \frac{\left(\frac{N_{\uparrow\uparrow\uparrow}}{D_1} + \frac{N_{\downarrow\uparrow\uparrow}}{D_2}\right) - \left(\frac{N_{\uparrow\downarrow\downarrow}}{D_3} + \frac{N_{\downarrow\downarrow\downarrow}}{D_4}\right)}{\left(\frac{N_{\uparrow\uparrow\uparrow}}{D_1} + \frac{N_{\downarrow\uparrow\uparrow}}{D_2}\right) P_t^{\downarrow\downarrow} + \left(\frac{N_{\uparrow\downarrow\downarrow}}{D_3} + \frac{N_{\downarrow\downarrow\downarrow}}{D_4}\right) P_t^{\uparrow\uparrow}}$$
(38)

 $A_{LL} = \frac{1}{P_h^{\uparrow\uparrow} P_h^{\downarrow\downarrow} f_{dil}^{\pi}} \times$ 749  $\begin{bmatrix} \left(\frac{N_{\uparrow\downarrow\downarrow}}{D_3} - \frac{N_{\downarrow\downarrow\downarrow}}{D_4}\right) P_b^{\uparrow\uparrow} - \left(\frac{N_{\uparrow\uparrow\uparrow}}{D_1} - \frac{N_{\downarrow\uparrow\uparrow}}{D_2}\right) P_b^{\downarrow\downarrow} \\ \hline \left(\frac{N_{\uparrow\uparrow\uparrow}}{D_2} + \frac{N_{\downarrow\uparrow\uparrow}}{D_2}\right) P_t^{\downarrow\downarrow} + \left(\frac{N_{\uparrow\downarrow\downarrow}}{D_2} + \frac{N_{\downarrow\downarrow\downarrow}}{D_4}\right) P_t^{\uparrow\uparrow} \end{bmatrix}$ .(39) 750

#### **Dilution Factor for the Exclusive Channel** E. 751

In contrast to the dilution for inclusive  $P_b P_t$  analysis that 752 has only  $Q^2$  dependence (Section IIID), the dilution for ex-753 clusive pion production could vary with all four kinematic 754 variables  $W, Q^2, \cos \theta^*$  and  $\phi^*$  [51]. To evaluate the dilution factor for all 4-dimensional bins of  $(W, Q^2, \cos\theta^*, \phi^*)$ , 756 757 the yield from the unpolarized material inside the polarized 758 NH<sub>3</sub> target was constructed using the missing mass spectra 759 from the carbon and the empty targets. Scaling factors for 760 the carbon and empty target data were calculated following 761 a prescription similar to Eqs. (29-31), but with the bound-<sup>762</sup> nucleon fraction B replaced by the ratio Z/A (Table II) for 763 the  $ep \to e'\pi^+(n)$  [(1-Z/A) for the  $en \to e'\pi^-(p)$ ] chanref nel. For NH<sub>3</sub> one should use  $\frac{Z_{\rm NH_3}}{A_{\rm NH_3}} = 7/18$  to account for 765 only unpolarized protons. We obtain

$$\frac{N_{\rm N \ in \ NH_3}}{Q_{\rm NH3}} = a \left(\frac{N_{^{12}\rm C}}{Q_{^{12}\rm C}}\right) + b \left(\frac{N_{\rm empt}}{Q_{\rm empt}}\right) ,\qquad(40)$$

767 where

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$$a = \frac{\left(\frac{Z_{\rm NH_3}}{A_{\rm NH_3}}\rho_{\rm NH_3}x_{\rm NH_3}\right) + \left(\frac{Z_w}{A_w}\rho_w x_w\right)\frac{x_{\rm NH_3}}{l}}{\left(\frac{Z_{\rm 12_C}}{A_{\rm 12_C}}\rho_{\rm ^{12}C}x_{\rm ^{12}C}\right) + \left(\frac{Z_w}{A_w}\rho_w x_w\right)\frac{x_{\rm 12_C}}{l}}, \quad (41)$$

769 
$$b = \left(1 - \frac{x_{\rm NH_3}}{l}\right) - \left(1 - \frac{x_{^{12}\rm C}}{l}\right)a$$
. (42)

Similar to elastic analysis, the value of b from Eq. (42) could 770 be either positive or negative depending on the input packing 771 772 factor. Figure 11 shows the dilution factor evaluation for the 3.0 GeV data using the  $NH_3$  long top target. 778

From Eqs. (38-39) one can see that the uncertainties in  $P_b P_t$ 775 776 and  $f_{\rm dil}^{\pi}$  should be evaluated at the same time because both depend on the packing factor. Table III shows all  $P_b P_t$  and 777 dilution results for the packing factor range used in the elastic 778  $P_b P_t$  analysis. For each setting of beam energy and target, we 779 varied the packing factor by one standard deviation and eval-<sup>781</sup> uated  $P_b P_t$  and  $f_{dil}^{\pi^+}$ . We used the observed difference in the <sup>782</sup> product  $P_b P_t f_{dil}^{\pi^+}$  as the uncertainty due to the packing fac-<sup>783</sup> tor, labeled as  $P_b P_t f_{dil}^{\pi^+} \pm (p.f.)$ . For the total uncertainty <sup>792</sup> ied within its uncertainty. The resulting total uncertainties on  $\frac{\Delta(P_bP_tf_{dil})}{P_bP_tf_{dil}}$  (total), we added the following terms in quadra- $\frac{\Delta(P_bP_tf_{dil})}{P_bP_tf_{dil}}$  (total), we added the following terms in quadra- $\frac{1}{793}$   $P_bP_tf_{dil}^{\pi^+}$  were used for the evaluation of the uncertainty of res ture: 1) statistical uncertainty of inclusive elastic events used  $\frac{1}{794}$  the double-spin asymmetry  $A_{LL}$ . For the target asymmetry



FIG. 11. Missing mass  $M_X$  spectrum for deriving the dilution factor for the  $ep \rightarrow e'\pi^+(n)$  channel. Top: missing mass below the neutron mass peak; bottom: missing mass around the neutron mass peak. The data shown are for the 3.0 GeV run period using the NH<sub>3</sub> long top target. Here, the  $M_X$  spectrum for the nuclear material (magenta) in the polarized NH3 target was constructed using the spectra for the carbon target (blue), the empty target (green), with an input packing factor x = 0.65 cm. The nuclear contribution was then subtracted from the NH<sub>3</sub> target spectrum (black) to give the polarizedproton spectrum (red). The dilution factor was evaluated using the region around the neutron peak and is shown in the bottom panel with the uncertainty in the bracket. The histogram and the dilution uncertainties include both statistical uncertainties and the uncertainty in the scaling or packing factors. Note that the empty target (green) spectrum is negative, indicating we have scaled up the carbon data and then subtracted the extra helium (empty target) to reproduce the unpolarized background in NH3. Results for the dilution factor is shown in the bottom plot. The  $M_X$  cuts (0.90, 0.98) GeV/ $c^2$  used in the dilution and the asymmetry analysis are shown by the two red vertical lines.

<sup>786</sup> in the  $P_b P_t$  analysis; 2) statistical uncertainty of the carbon 787 and empty target counts used to calculate the dilution factor 788 for inclusive elastic events; 3) statistical uncertainty in the exreg clusive  $ep \rightarrow e'\pi^+(n)$  channel due to limited statistics of car- $_{\rm 790}$  bon and empty target data  $f_{\rm dil}^{\pi^+} \pm ({\rm stat.});$  and 4) the observed

795  $A_{UL}$ , the uncertainty was evaluated by combining the uncer-<sup>796</sup> tainty of  $P_b P_t f_{dil}^{\pi^+}$  and the uncertainty of the Møller measure-<sup>797</sup> ments on the beam polarization. The uncertainty from the polarizations and the dilution is the largest systematic uncer-798 tainty of the present analysis. 799

The uncertainty in the input packing factor of Table III was 800  $_{801}$  checked using not only the W spectrum of elastic events (as described in Section IIID), but also the dilution factor of the 802  $en \rightarrow e'\pi^-(p)$  channel analyzed using a similar prescription 803 as Eqs. (40-42). The dilution factor of the  $\pi^{-}(p)$  channel 804 should be consistent with zero in all kinematic bins. Overall, the lower bound in the packing factor was cross-checked 806 between the  $en \to e'\pi^-(p)$  dilution result and the elastic W 807 spectrum, and the upper bound in the packing factor was de-808 termined always by the elastic W spectrum. 809

The kinematics dependence of the dilution factor on  $Q^2$ , W810 and the pion center-of-mass angles  $\theta^*$  and  $\phi^*$  have been stud-812 ied, and multi-dimensional fits of the dependence were per-813 formed. The limited statistics of the carbon and the empty target data prevented fitting the  $(Q^2, W, \cos \theta^*, \phi^*)$  dependence 814 815 simultaneously. Instead, two bi-dimensional fits were used, sie one for the  $(Q^2, W)$  dependence and one for the  $(\cos \theta^*, \phi^*)$ <sup>817</sup> dependence, with the following ad-hoc parameterizations:

<sup>818</sup> 
$$f_1 = p_0 \left[ 1 + p_1 (Q^2) + p_2 (Q^2)^2 \right]$$
  
<sup>819</sup>  $\times \left[ 1 + p_3 (W - 1.8) + p_4 (W - 1.8)^2 \right]$   
<sup>820</sup>  $\times \left[ 1 + \frac{p_5}{(W^2 - 1.50^2)^2 + 1.50^2 \times 0.05^2} \right]$ 

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$$\times \left[ 1 + \frac{p_6}{(W^2 - 1.68^2)^2 + 1.68^2 \times 0.05^2} \right]$$
(43)

where W is in  $\text{GeV}/c^2$  and

$$f_{2} = p'_{0} \times \left[1 + \frac{p_{7}}{1 - \cos \theta^{*}}\right] \times \left[1 + p_{8} \sin \phi^{*} + p_{9} \cos \phi^{*}\right]. \tag{44}$$

The resulting two fits were then multiplied to give the over-825 <sup>826</sup> all  $2 \times 2$ -dimensional fit for  $f_{dil}^{\pi}(W, Q^2, \cos \theta^*, \phi^*)$ . To check <sup>827</sup> the validity of the fit, the results from  $f_{dil}^{\pi}(W, Q^2, \cos \theta^*, \phi^*)$ 828 were integrated over 3 of the 4 variables, and then com-829 pared with the dilution extracted directly from data binned <sup>830</sup> in the 4th variable. This comparison is shown in Fig. 12. 831 One can see that the dilution factors obtained from this  $_{\rm 832}$  method agree with data very well. The  $2\times2\text{-dimensional}$ ss fit  $f_{
m dil}^{\pi}(W,Q^2,\cos{ heta^*},\phi^*)$  was used to correct the asymme-<sup>834</sup> tries  $A_{UL}$  and  $A_{LL}$  for the specific  $W, Q^2, \cos \theta^*, \phi^*$  bin us-836 ing Eqs. (38-39).

#### G. Effect of Nitrogen Polarization on the Asymmetry 837

838 <sup>839</sup> measured asymmetry. In this section we estimate this effect <sup>846</sup> the proton, respectively, B is the magnetic field of the target, k  $_{840}$  and show that it is negligible. Therefore no correction was  $_{847}$  is the Boltzmann constant and  $T_S$  is the spin temperature that <sup>841</sup> made to the extracted exclusive channel asymmetries.



FIG. 12. Dependence of dilution on: (a)  $Q^2$ , (b) W, (c)  $\cos \theta^*$  and (d)  $\phi^*$ , for the 3.0 GeV NH<sub>3</sub> long top target,  $ep \to e'\pi^+(n)$  channel, obtained directly from the data (open squares) and from multiplying the two 2D fits of Eqs. (43-44) then integrating over 3 of the 4 variables (solid circles). The error bars for the dilution extracted from data are statistical only.

The nitrogen polarization in <sup>15</sup>NH<sub>3</sub> can be estimated based 842 on the Equal Spin Temperature (EST) prediction [39]: 843

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$$P(^{15}N) = \tanh \frac{\mu_{^{15}N}B}{kT_S}, P(H) = \tanh \frac{\mu_p B}{kT_S},$$
 (45)

The  ${}^{15}N$  in the NH<sub>3</sub> target is polarizable and can affect the  ${}^{845}$  where  $\mu_{{}^{15}N}$  and  $\mu_p$  are the magnetic moments of the  ${}^{15}N$  and 848 describes the Boltzmann distribution of spins inside the target.

TABLE III. Dilution factor  $f_{dil}^{\pi^+}$  and the product  $P_b P_t f_{dil}^{\pi^+}$  for the exclusive  $\pi^+$  channel. The  $P_b P_t$  results extracted from inclusive elastic scattering, described in section IIID, and their uncertainties are also shown. For  $P_b P_t$ , the three errors are due to statistical uncertainty of the elastic events, the statistical uncertainty of the carbon and empty target counts used to calculate the dilution factor for inclusive elastic analysis, and the uncertainty of the packing factor.  $P_b P_t$  values from Møller and NMR measurements are shown for comparison, although the NMR measurements are unreliable as decribed in section II C. The products  $P_b P_t f_{dil}$  are used to correct the exclusive channel asymmetries. The total uncertainties in  $P_b P_t f_{dil}$  include uncertainties of  $P_b P_t$ , statistical uncertainties of  $f_{dil}^{\pi^+}$ , and the uncertainties due to the packing factor (p.f.), all added in quadrature. These total uncertainties will be used as systematic uncertainties on the extracted exclusive channel asymmetries.

$E_{\rm beam}$	Target	p.f.	$(P_bP_t)_{el}$	Møller	$f_{\rm dil}^{\pi^+} \pm (\text{stat.}) \pm (\text{p.f.})$	$P_b P_t f_{\rm dil}$	$\frac{\Delta(P_b P_t f_{\rm dil})}{P_b P_t f_{\rm dil}}$
(GeV)	$(NH_3)$	(cm)		$\times$ NMR			(total)
3.0	top	$0.65\pm0.05$	$0.614 \pm 0.006 \pm 0.015 \pm 0.045$	0.620	$0.424 \pm 0.021 \pm 0.013$	0.260	7.0%
23	top	$0.65\pm0.05$	$0.597 \pm 0.006 \pm 0.021 \pm 0.028$	0.551	$0.476 \pm 0.021 \pm 0.011$	0.284	6.2%
2.5	short	$0.30\pm0.05$	$0.560 \pm 0.009 \pm 0.026 \pm 0.067$	0.601	$0.322 \pm 0.017 \pm 0.021$	0.180	9.0%
2.0	top	$0.65\pm0.05$	$0.605 \pm 0.004 \pm 0.016 \pm 0.030$	0.545	$0.495 \pm 0.020 \pm 0.010$	0.299	5.7%
2.0	bottom	$0.65\pm0.05$	$0.636 \pm 0.019 \pm 0.016 \pm 0.031$	0.560	$0.484 \pm 0.021 \pm 0.010$	0.308	6.4%
	top	$0.70\pm0.05$	$0.571 \pm 0.003 \pm 0.009 \pm 0.033$	0.509	$0.494 \pm 0.019 \pm 0.010$	0.282	5.7%
1.3	bottom	$0.70\pm0.05$	$0.535 \pm 0.003 \pm 0.010 \pm 0.028$	0.458	$0.493 \pm 0.019 \pm 0.010$	0.264	5.5%
	short	$0.30\pm0.05$	$0.552 \pm 0.010 \pm 0.030 \pm 0.060$	0.581	$0.383 \pm 0.016 \pm 0.014$	0.211	10.2%
1.1	bottom	$0.75\pm0.10$	$0.568 \pm 0.002 \pm 0.007 \pm 0.080$	0.563	$0.496 \pm 0.020 \pm 0.020$	0.282	11.1%

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and H of the ammonia molecule by several experiments start-  $_{879}$  counts  $N_{\uparrow \uparrow, \uparrow \downarrow, \downarrow \uparrow, \downarrow \downarrow}$ , where each event counts as 1, we first 851 ing with the Spin Muon Collaboration [52]. The SLAC E143 880 divided 1 by the acceptance of that particular event, then the <sup>852</sup> collaboration performed an empirical fit and showed [53]:

$$P_{15} N = 0.136 |P_p| - 0.183 |P_p|^2 + 0.335 |P_p|^3 , \quad (46)$$

856 by the unpaired proton and its effect relative to the three free 886 data. When integrating the theoretical calculations, we ex-857 protons in NH<sub>3</sub> is

$$\Delta P = \frac{1}{3} \left( -\frac{1}{3} \right) P(^{15}N) ,$$
 (47)

where the additional factor of -1/3 comes from the wave- $_{860}$  function of the unpaired proton in the  $^{15}N$  [54]. The effect on <sup>861</sup> the asymmetry due to the polarized proton in the <sup>15</sup>N is thus at the (1-2)% level, and is negligible compared to the statistical <sup>863</sup> uncertainty of the asymmetry and the systematic uncertainty 864 due to the polarizations and the dilution factor.

H. Acceptance Corrections

in Section IV.

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#### When studying how the asymmetries vary with very small 866 bins in all four kinematic variables – the electron's $Q^2$ , W 867 and the pion's center-of-mass angles $\theta^*$ and $\phi^*$ – the effect of 868 the detector acceptance and efficiency in principle cancel and 869 therefore do not affect the interpretation of the asymmetry re-870 sults. The effect of acceptance only becomes relevant when 871 integration of the asymmetry over a subset of these four vari-872 873

875 876 ceptance of each bin based on acceptance cuts for both elec- 904 Other non-neglible systematic uncertainties include a relative

<sup>849</sup> The EST prediction has been demonstrated to apply to the <sup>15</sup>N <sup>878</sup> on an event-by-event basis: instead of using the measured sum was taken and used as  $N_{\uparrow\uparrow,\uparrow\downarrow\downarrow,\downarrow\uparrow,\downarrow\downarrow\downarrow}$  in the formula from 882 Section IIIE, Eqs. (37-39). The asymmetries extracted this 883 way were integrated over certain kinematic ranges and comwhich gives  $P_{^{15}N} \approx -15\%$  when  $P_p = 90\%$  and  $P_{^{15}N} \approx {}^{884}$  pared directly with theoretical predictions. Zero-acceptance when  $P_p = 70\%$ . The  ${}^{15}N$  polarization is carried  ${}^{885}$  bins could not be corrected this way when integrating the 887 cluded bins where there were no data, and thus removed the <sup>888</sup> zero-acceptance bins from the theory curves as well.

## I. Radiative Corrections

Radiative corrections were calculated for both  $A_{UL}$  and 891  $A_{LL}$  using the code EXCLURAD [55] and the MAID2007 <sup>892</sup> model [13]. It was found that overall the correction is fairly small and typically no larger than 0.03. Considering the size of the statistical uncertainty of the measurement, radiative cor-895 rections were not applied to the asymmetries, but rather are guoted as a systematic uncertainty of  $\Delta A = \pm 0.03$  through-897 out the accessed kinematics.

#### J. Summary of All Systematic Uncertainties

The systematic uncertainty of the  $\vec{e}\vec{p} \rightarrow e'\pi^+(n)$  exclusive channel is dominated by that from the product  $P_b P_t f_{dil}^{\pi^+}$ , ables is necessary, which is the case for all results presented  $_{901}$  shown in Table III. The uncertainty of  $P_b P_t f_{dil}^{\pi^+}$  takes into <sup>902</sup> account the uncertainties in the target packing factor, as well For results presented in Section IV, we evaluated the ac- 903 as the thickness and density of various materials in the target.  $_{877}$  trons and pions. The acceptance correction was then applied  $_{905} \pm (1-2)\%$  due to the  $^{15}$ N in NH<sub>3</sub> and a  $\pm 0.03$  due to radia-

TABLE IV. Summary of systematic uncertainties due to the target and beam polarizations and the dilution factor for different beam and target combinations. The (1-2)% relative uncertainty due to  $^{15}\mathrm{N}$ be added in quadrature to the values here to obtain the total system- 945 will present some representative results. atic uncertainty.

$E_{\rm beam}$	Target	$\Delta A_{UL}/A_{UL}$	$\Delta A_{LL}/A_{LL}$
(GeV)	$(NH_3)$	(syst)	(syst)
3.0	top	7.0%	7.0%
23	top	6.2%	6.3%
2.5	short	9.0%	9.0%
2.0	top	5.7%	5.8%
13	top	5.7%	5.9%
1.5	bottom	5.5%	5.7%
1.1	bottom	11.1%	11.2%

<sup>906</sup> tive corrections. Adding these uncertainties in quadrature, we 907 arrive at Table IV for our asymmetry results. For the asym- $_{908}$  metry  $A_{UL}$ , one does not need to normalize by  $P_b$ . We relied  $_{909}$  on the elastic  $P_b P_t$  results and combined in quadrature their 910 uncertainties with the uncertainty in the Møller polarization to  $_{912}$  obtain the uncertainty on  $P_t$  alone.

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#### IV. ASYMMETRY RESULTS

Results for the target asymmetry  $A_{UL}$  and the double-spin  $_{969}$ 914  $_{915}$  asymmetry  $A_{LL}$  are available on a 4-dimensional grid of  $Q^2$ ,  $_{970}$  (1.58, 1.82) GeV/ $c^2$  region, only the MAID2007 (solid) and 917 spaced between 0.00453 and 6.45 (GeV/c)<sup>2</sup>, 38 W bins be- 972 and MAID2007 approximates the data better than the other is referred to as "asymmetry bins". To allow a meaningful  ${}^{975}$  1.58 GeV/ $c^2$  region throughout the  $Q^2$  range shown. 920 comparison with theoretical calculations, we integrated the 921 data over 3  $Q^2$  bins, 8 W bins, 5  $\phi^*$  bins and 5  $\cos \theta^*$  bins. 922 These will be referred to as "combined bins" hereafter. The 976 923 resulting combined W bins are (1.1, 1.34), (1.34, 1.58) and 924 (1.58, 1.82) GeV/ $c^2$ , allowing an examination of the first, the <sub>977</sub> 926 927 928 929 930 931 932  $_{334}$  try bin was summed, and used as the combined  $N_{\uparrow\uparrow\uparrow,\uparrow\downarrow\downarrow,\downarrow\uparrow\uparrow,\downarrow\downarrow\downarrow}$   $_{986}$  comparable statistics as Fig. 13 but are not shown here for 995 to evaluate the asymmetries for the combined bin. Using this 987 brevity. Overall the data agree very well with all four cal- $_{936}$  method, the integrated asymmetries are direct reflections of  $_{988}$  culations. For all  $\phi^*$  bins, the sign of  $A_{LL}$  in the region of  $_{937}$  the ratio of the physical cross sections integrated over the  $_{989}$  the  $N(1520)3/2^-$  and the  $N(1680)5/2^+$  is positive in the <sup>938</sup> combined bin except for regions that had zero acceptance. <sup>930</sup> high  $Q^2$ , but start to cross or approach zero in the lower  $Q^2$  $_{999}$  To compare with theory, we calculated the cross sections  $_{991}$  bin, within (0.0919, 0.156) (GeV/c)<sup>2</sup> for  $N(1520)3/2^{-}$  and

941 cross sections over combined bins except for asymmetry bins <sup>942</sup> where there was no data (zero acceptance). The ratio of the summed cross sections [Eqs. (20-21)] was taken as the calcuand the  $\pm 0.03$  absolute uncertainty due to radiative corrections must <sup>944</sup> lated asymmetry for the combined bin. In the following we

#### A. Results on Target Asymmetry $A_{UL}$

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Figure 13 shows, in increasing  $Q^2$  ranges, the  $A_{UL}$  results as a function of W for three  $\phi^*$  bins (120°, 180°), 948  $(180^{\circ}, 240^{\circ}), (240^{\circ}, 300^{\circ}),$  and integrated over 0.5 < 949  $\cos \theta^* < 1.0$ . Results for the  $\phi^* = (0^{\circ}, 60^{\circ})$  and  $(300^{\circ}, 360^{\circ})$ have less statistics and are not shown. Results for the  $\phi^* =$ 951  $(60^{\circ}, 120^{\circ})$  bin have comparable statistics as Fig. 13 but are 952 not shown here for brevity. In general, we see that the agree-<sup>954</sup> ment between these  $A_{UL}$  results and the four calculations, MAID2007 (solid) [13], JANR (dashed) [14], SAID (dashdotted) [15], and DMT2001 (dotted) [16], is very good in the W < 1.5 (GeV/ $c^2$ ) region, but for the region 1.5 < W <957  $_{958}$  1.8 (GeV/ $c^2$ ), all four calculations differ from each other and none agrees well with data, although the MAID2007 curve (solid) approximates the data better than the other three. 960

To study these results further for different W regions, we <sub>962</sub> show in Fig. 14  $A_{UL}$  results as a function of  $\phi^*$  for three  $_{\rm 963}~W$  ranges and between  $Q^2~=~0.0187$  and  $0.452~({\rm GeV/}c)^2.$ Results for lower  $Q^2$  ranges, down to 0.00646 (GeV/c)<sup>2</sup>,  $_{965}$  are available from the 1.1 GeV data but only cover 1.2 < $_{966} W < 1.5 (\text{GeV}/c^2)$  and thus are not presented here.  $_{967}$  From Fig. 14, for the lower two W bins (1.12, 1.34) and  $_{968}$  (1.34, 1.58) GeV/ $c^2$ , the four calculations provide similar predictions and all agree with data. But for the W =W,  $\cos \theta^*$  and  $\phi^*$ . There are 42  $Q^2$  bins logarithmically 971 the DMT2001 (dotted) calculations provide the correct sign, tween 1.1 and 2.21 GeV/ $c^2$ , 30  $\phi^*$  bins between 0 and 360°, 973 three although it does not agree with data perfectly. It is and 20  $\cos \theta^*$  bins between -1 and 1. This binning scheme  ${}^{974}$  clear that all four calculations can be improved in the W >

#### **B.** Results on the Double-Spin Asymmetry A<sub>LL</sub>

Figure 15 shows the double-spin asymmetry  $A_{LL}$  results second, and the third nucleon resonance regions, respectively. 978 as a function of W for eight  $Q^2$  bins, three  $\phi^*$  bins, and The method of integrating the data for the combined bins  $_{979}$  integrated over  $\cos \theta^* = (0.5, 1.0)$ . These results are comwas built upon the acceptance correction described in Sec- 980 pared with four calculations: MAID2007 (solid) [13], JANR tion III H: to correct for the acceptance, each event in the 981 (dashed) [14], SAID (dash-dotted) [15], and DMT2001 (dotasymmetry bin was divided by the acceptance of that particu-  $_{992}$  ted) [16]. Note that our definiton for  $A_{LL}$  has opposite lar event, then summed to be used as  $N_{\uparrow\uparrow\uparrow,\uparrow\downarrow\downarrow,\downarrow\uparrow\downarrow,\downarrow\downarrow\downarrow}$  in Eqs. (37- 983 sign from theories, see Section IA. Results for the  $\phi^*$  = 39). To integrate from asymmetry bins into combined bins, 984 (0°, 60°) and (300°, 360°) bins have less statistics and are these acceptance-corrected  $N_{\uparrow\uparrow\uparrow,\uparrow\downarrow\downarrow,\downarrow\uparrow\uparrow,\downarrow\downarrow\downarrow}$  from each asymme- 985 not shown. Results for the  $\phi^* = (60^\circ, 120^\circ)$  bin have  $\sigma_{t.et,0}$  for each asymmetry bin, then summed the calculated  $\gamma_{22}$  within  $Q^2 = (0.266, 0.452)$  (GeV/c)<sup>2</sup> for  $N(1680)5/2^+$ , re $_{993}$  spectively. This is in agreement with the suggestion in Sec-  $_{1010}$  W > 1.58 GeV/ $c^2$  where predications from various models <sup>994</sup> tion I that  $A_{LL}$  turns to positive at high  $Q^2$  values due to <sup>1011</sup> differ significantly. <sup>995</sup> helicity conservation, but may become negative near the real

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996 photon point.

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## V. SUMMARY

998 <sup>999</sup> metry  $A_{UL}$  and  $A_{LL}$  on the  $e\vec{p} \rightarrow e\pi^+(n)$  channel using data <sup>1016</sup> work was supported by: the U.S. Department of Energy taken on a polarized NH<sub>3</sub> target, from the EG4 experiment us- 1017 (DOE), the U.S. National Science Foundation, the U.S. Jef-1000 ing CLAS in Hall B of Jefferson Lab. These data have reached 1018 fress Memorial Trust; the United Kingdom's Science and 1001 a low  $Q^2$  region from 0.0065 to 0.35 (GeV/c)<sup>2</sup> that was not ac- 1019 Technology Facilities Council (STFC) under grant num-1002 cessed previously. They suggest a transition in  $A_{LL}$  from pos- 1020 bers ST/L005719/1 and GR/T08708/01; the Italian Istituto 1003 itive at higher  $Q^2$  to negative values below  $Q^2 \approx 0.1$  (GeV/c)<sup>2</sup> 1021 Nazionale di Fisica Nucleare; the French Institut National de 1005 in the region  $1.5 < W < 1.7 \text{ GeV}/c^2$ , in agreement with 1022 Physique Nucléaire et de Physique des Particules, the French 1006 both previous data from CLAS (high  $Q^2$ ) [20, 22] and the real 1023 Centre National de la Recherche Scientifique; and the Naphoton data at  $Q^2 = 0$ . Our results show that while all model 1024 tional Research Foundation of Korea. Jefferson Science As-1008 calculations agree well with  $A_{LL}$ , in general there is room 1025 sociates, LLC, operates Jefferson Lab for the U.S. DOE under 1009 for improvements for  $A_{UL}$  in the high-mass resonance region 1026 U.S. DOE contract DE-AC05-060R23177.

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FIG. 13. Results on the target spin symmetries  $A_{UL}$  for the  $\vec{ep} \rightarrow e\pi^+(n)$  channel as a function of the invariant mass W in GeV/ $c^2$ , integrated over  $\cos \theta^* = (0.5, 1.0)$ , in increasing  $Q^2$  ranges and three  $60^\circ \phi^*$  bins. From top to bottom the  $Q^2$  bins are (0.00646, 0.0110) and (0.0110, 0.0187) (1.1 GeV NH<sub>3</sub> long bottom target), (0.0187, 0.0317) and (0.0317, 0.054) (1.3 GeV NH<sub>3</sub> long top target), (0.054, 0.0919)(2.0 GeV NH<sub>3</sub> long top target), (0.0919, 0.156), (0.156, 0.266), and (0.266, 0.452) (GeV/ $c^2$  (3.0 GeV NH<sub>3</sub> long top target). From left to right the  $\phi^*$  bins are  $\phi^* = (120^\circ, 180^\circ)$ ,  $(180^\circ, 240^\circ)$  and  $(240^\circ, 300^\circ)$ . In each panel, the horizontal scale is from 1.1 to 2 GeV/ $c^2$ in W and the vertical scale is from -1 to 1. Data are compared to four calculations: MAID2007 (solid) [13], JANR (dashed) [14], SAID (dash-dotted) [15], and DMT2001 (dotted) [16].



FIG. 14. Results on  $A_{UL}$  for the  $\vec{ep} \rightarrow e\pi^+(n)$  channel as a function of azimuthal angle  $\phi^*$ , integrated over  $\cos \theta^* = (0.5, 1.0)$ , for six  $Q^2$  bins and three W bins. From top to bottom the six  $Q^2$  bins are:  $Q^2 = (0.0187, 0.0317)$  [1.3 NH<sub>3</sub> long target for W = (1.12, 1.34) and (1.34, 1.58) GeV/ $c^2$ , and 2.0 NH<sub>3</sub> long top target for W = (1.58, 1.82) GeV/ $c^2$ ]; (0.156, 0.266) and (0.266, 0.452) (GeV/ $c^2$  (2.0 GeV NH<sub>3</sub> long top target); (0.0919, 0.156), (0.156, 0.266) and (0.266, 0.452) (GeV/ $c^2$  (3.0 GeV NH<sub>3</sub> long top target); from left to right the W bins are: W = (1.12, 1.34), (1.34, 1.58), (1.58, 1.82) GeV/ $c^2$ . In each panel, the horizontal scale is from 0 to 360° in  $\phi^*$  and the vertical scale is from -1 to 1. Data are compared to four calculations: MAID2007 (solid) [13], JANR (dashed) [14], SAID (dash-dotted) [15], and DMT2001 (dotted) [16].



FIG. 15. Results on the double-spin symmetries  $A_{LL}$  for the  $\vec{e}\vec{p} \rightarrow e\pi^+(n)$  channel as a function of the invariant mass W in GeV/ $c^2$ , integrated over  $\cos\theta^* = (0.5, 1.0)$ , for increasing  $Q^2$  ranges and three  $60^\circ \phi^*$  bins. From top to bottom the  $Q^2$  bins are (0.00646, 0.011) and (0.011, 0.0187) (1.1 GeV NH<sub>3</sub> long bottom target), (0.0187, 0.0317) and (0.0317, 0.054) (1.3 GeV NH<sub>3</sub> long top target), (0.054, 0.0919)(2.0 GeV NH<sub>3</sub> long top target), (0.0919, 0.156), (0.156, 0.266), and (0.266, 0.452) (GeV/ $c^2$  (3.0 GeV NH<sub>3</sub> long top target). From left to right the  $\phi^*$  bins are  $\phi^* = (120^\circ, 180^\circ)$ ,  $(180^\circ, 240^\circ)$  and  $(240^\circ, 300^\circ)$ . In each panel, the horizontal scale is from 1.1 to 2 GeV/ $c^2$ in W and the vertical scale is from -1 to 1. Data are compared to four calculations: MAID2007 (solid) [13], JANR (dashed) [14], SAID (dash-dotted) [15], and DMT2001 (dotted) [16].

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