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Measurement of nuclear effects in neutrino interactions with minimal dependence on neutrino energy

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We present a phenomenological study of nuclear effects in neutrino charged-current interactions, using transverse kinematic imbalances in exclusive measurements. Novel observables with minimal dependence on neutrino energy are proposed to study quasielastic scattering, and especially resonance production. They should be able to provide direct constraints on nuclear effects in neutrinoand antineutrino-nucleus interactions.

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I. INTRODUCTION

The study of neutrino interactions presents unique challenges. Unlike for its electroweak counterpart, the charged lepton, the energy of a neutrino is generally difficult to measure. Existing accelerator technologies are able to provide a neutrino beam with a well defined direction, and yet the beam energy spectrum, which is of critical importance in neutrino oscillation analyses [1, 2], is not well known. With a nuclear target, where neutrinos interact with bound nucleons, uncertainties from various nuclear effects arise. With accelerator neutrinos in the GeV regime, individual bound nucleons are resolved. Their momenta, due to Fermi motion ranging up to $p_{\rm F} \sim 200 \ {\rm MeV}/c$, need to be considered; the energy required to release one of them (binding energy) causes further fluctuations in the initial kinematics. Moreover, multinucleon correlations have recently been conjectured to contribute significantly to the measured cross sections in this energy regime, evoking a reexamination of the long-used impulse approximation [3, 4]. Because the hadronic final states are produced inside a nuclear medium—the nucleus containing nucleons undergoing Fermi motion—they experience final-state interactions (FSIs) before exiting and therefore both their kinematics and identity can be altered. In response to this, the nucleus can be excited or it can break up, emitting nucleons, pions and photons—collectively known as nuclear emission. These effects further modify the final states from the *basic* neutrino-nucleon interaction, which could have already been biased by multinucleon correlations, and introduce ambiguities, in both measurements and calculation, to efforts to identify the interaction channel. The highly convoluted nature of the problem is made manifest by the fact that these nuclear effects are all present in different channels for all nuclei except

hydrogen [5].

Experimental efforts to understand charged-current (CC) neutrino-nucleus interactions, on which spectrum measurements of accelerator neutrinos are based, have been focused on inclusive and semi-inclusive observables, such as total cross sections and lepton kinematics, which depend strongly on the neutrino energy and cannot be directly compared across experiments because the neutrinos are produced in wideband fluxes. To interpret the data, theories of the basic interactions and nuclear effects have to be folded into approximated neutrino energy spectra. Therefore, on one hand, accessing the nuclear effects precisely is difficult, while on the other hand, understanding the nuclear effects helps determine the spectra. For example, Ref. [5] shows that, with moderate FSIs, the calorimetric approach of neutrino energy reconstruction outperforms kinematic methods; yet models of FSIs have not been extensively tested because of the lack of measurements of the final-state hadrons.

In this work, we propose to measure nuclear effects via the transverse kinematic imbalance between the charged lepton and the primary final-state hadron in an exclusive CC channel, such as quasielastic scattering (QE) and resonance production (RES). The measurement in RES is especially important for a better understanding of nuclear effects in both neutrino and antineutrino interactions. Our discussion starts with the impulse approximation. We will first demonstrate the minimal dependence of hadronic variables on the neutrino energy, and describe the nuclear medium response to FSIs. Then we illustrate how these variables are affected by Fermi motion and FSIs. Subsequently the issue with respect to multinucleon correlations and an extension of the technique to electron-nucleus scattering will be addressed briefly.

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II. NUCLEAR MEDIUM RESPONSE

Consider a CC interaction on a nucleus. At the basic level the neutrino ν interacts with a bound nucleon N which then transits to another hadronic state N':

$$\nu + N \to \ell' + N',\tag{1}$$

where ℓ' is the charged lepton. In the rest frame of the nucleus, the bound nucleon is subject to Fermi motion with momentum $\vec{p}_{\rm N}$, and an energy-momentum (ω, \vec{q}) carried by a virtual W-boson (W^*) is transferred to it as the neutrino scatters. In characterizing the interaction, the virtuality $Q^2 \equiv q^2 - \omega^2$ and the invariant mass W of N' are used. Following energy-momentum conservation (the binding energy is neglected compared to the initial nucleon energy [6]), the energy transfer reads

$$\omega = \frac{Q^2 + W^2 - m_{\rm N}^2 + 2\vec{q} \cdot \vec{p}_{\rm N}}{2\sqrt{m_{\rm N}^2 + p_{\rm N}^2}},\tag{2}$$

$$\sim \frac{Q^2 + W^2 - m_{\rm N}^2}{2\sqrt{m_{\rm N}^2 + p_{\rm N}^2}},\tag{3}$$

where $m_{\rm N}$ is the mass of N, and the last line follows from averaging out the direction of $\vec{p}_{\rm N}$ in Eq. 2, which is a first order approximation because the *polarization* term ~ $\vec{q} \cdot \vec{p}_{\rm N}$ with opposite orientations of $\vec{p}_{\rm N}$ for a give \vec{q} does not exactly cancel as the W*-N cross section is slightly different with the varying center-of-mass energy [7]. Below the deeply inelastic scattering (DIS) region—especially in QE and RES where W equals the nucleon and dominantly the $\Delta(1232)$ resonance mass, respectively—the cross section is suppressed when Q is larger than the nucleon mass. The hadron momentum in these channels, as indicated by Eq. 3, "saturates" if the neutrino energy is above the scale $Q^2/2m_{\rm N} \sim \mathcal{O}(0.5 \text{ GeV})$ beyond which the charged lepton retains most of the increase of the neutrino energy.

Once the final state hadron N' is produced, it starts to propagate through the nuclear medium [8]. Under the assumption that the basic interaction (Eq. 1) and the in-medium propagation are uncorrelated (i.e., are *factorized*), the momentum of N', which depends weakly on the neutrino energy, completely determines the medium response, including the in-medium interaction probability $\tau_{\rm f}$ [9] and the energy-momentum transfer $(\Delta E, \Delta \vec{p})$ to the medium (if N' decays inside the nucleus, the total effect of all decay products is considered). It is the latter that leads to nuclear excitation [10] or break-up and consequently nuclear emission. The nuclear emission probability, $P(\Delta E, \Delta \vec{p})$, correlates the medium response to the in-medium energy-momentum transfer [11]. The factorization assumption suggests that $P(\Delta E, \Delta \vec{p})$ is independent of the neutrino energy E_{ν} , which is consistent with the implementation in the NuWro [12, 13] simulation shown in Fig. 1. In addition, as the neutrino energy increases, the predicted FSI strength saturates, as is indicated by $\tau_{\rm f}$ in the figure.



FIG. 1. Nuclear emission probability as a function of the in-medium momentum transfer, simulated by NuWro [12] for ν_{μ} CC QE on carbon—nuclear state modeled as relativistic Fermi gas (RFG) [14]—at neutrino energy of 0.6, 1, 3 and 6 GeV. Multinucleon correlations are ignored. The in-medium interaction probability $\tau_{\rm f}$ (extracted from the simulation output throughout this work) is shown in the legend.

III. SINGLE-TRANSVERSE KINEMATIC IMBALANCE

To make a neutrino energy-independent measurement of nuclear effects, the in-medium energy-momentum transfer (ΔE , $\Delta \vec{p}$) would be the ideal observable; this however is not experimentally accessible because of the unknown initial nucleon momentum and the initially unknown neutrino energy. Instead, $\Delta \vec{p}$ can be directly inferred from the following single-transverse kinematic imbalance (Fig. 2):

$$\delta \vec{p}_{\rm T} \equiv \vec{p}_{\rm T}^{\ell'} + \vec{p}_{\rm T}^{\rm N'},\tag{4}$$

$$\delta \alpha_{\rm T} \equiv \arccos \frac{-\vec{p}_{\rm T}^{\ell'} \cdot \delta \vec{p}_{\rm T}}{p_{\rm T}^{\ell'} \delta p_{\rm T}},\tag{5}$$

where $\vec{p}_{\rm T}^{\,\ell'}$ and $\vec{p}_{\rm T}^{\,\rm N'}$ are the projections of the extra-nucleus final-state momenta transverse to the neutrino direction. In particular, $-\vec{p}_{\rm T}^{\,\ell'} = \vec{q}_{\rm T}$, the transverse component of \vec{q} .

If the initial-state nucleon were static and free, $\delta p_{\rm T}$ would be zero—a feature that is not possessed by other experimentally accessible variables such as the final-state momenta. If FSIs could be switched off, $\delta \vec{p}_{\rm T}$ and $\delta \alpha_{\rm T}$ would be the transverse projection of $\vec{p}_{\rm N}$ and of the angle between $\vec{p}_{\rm N}$ and \vec{q} , respectively. Accordingly, to first approximation, the distribution of $\delta \vec{p}_{\rm T}$ would be independent of the neutrino energy, and that of $\delta \alpha_{\rm T}$ would be flat due to the isotropy of Fermi motion. The FSI acceleration (deceleration) of the propagating N' adds in a smearing to $\delta p_{\rm T}$ and pushes $\delta \vec{p}_{\rm T}$ forward (backward) to $(-)\vec{q}_{\rm T}$, making $\delta \alpha_{\rm T} \to 0$ (180) degrees.

Second order effects that lead to the dependence on the neutrino energy include the previously discussed polarization (see text after Eq. 2), Pauli blocking, and the



FIG. 2. Schematic illustration of the single-transverse kinematic imbalance— $\delta \phi_{\rm T}$, $\delta \vec{p}_{\rm T}$ and $\delta \alpha_{\rm T}$ —defined in the plane transverse to the neutrino direction.

transverse projection. The combined effect determines the evolution of the $\delta \alpha_{\rm T}$ distribution with $p_{\rm T}^{\ell'}$. An example predicted by NuWro is shown in Fig. 3. At $p_{\rm T}^{\ell'} \lesssim p_{\rm F}$, the cross section for $\delta \alpha_{\rm T}$ at 180 degrees is suppressed in QE interactions due to Pauli blocking, which leads to a forward peak in the distribution of $\delta \alpha_{\rm T}$ at small $p_{\rm T}^{\ell'}$. As $p_{\rm T}^{\ell'} \to E_{\nu}$, the cross section for $\delta \alpha_{\rm T}$ at 0 degrees is suppressed by the conservation of the longitudinal momentum. Even though the fractions of events in both extremes of the $p_{\rm T}^{\ell'}$ spectrum change with the neutrino energy, they are insignificant for the few GeV neutrino interactions. As a result, the $\delta p_{\rm T}$ and $\delta \alpha_{\rm T}$ distributions are largely independent of E_{ν} , as is shown in Fig. 4, where the evolution of the distributions with the neutrino energy is dominated by variations in the strength of the FSIs.

The transverse momentum imbalance $\delta p_{\rm T}$ has been used by the NOMAD experiment to enhance the purity of the selected QE [15], while the "transverse boosting angle" $\delta \alpha_{\rm T}$ is proposed here for the first time. Experimental data on $\delta \alpha_{\rm T}$ will reveal the accelerating/decelerating nature of FSIs. Its dependence on $p_{\rm T}^{\ell'}$, measured in a detector that has a low momentum threshold, will additionally provide constraints on Pauli blocking.

Besides the transverse momentum imbalance and boosting angle, another single-transverse variable can be defined (Fig. 2):

$$\delta\phi_{\rm T} \equiv \arccos \frac{-\vec{p}_{\rm T}^{\ell'} \cdot \vec{p}_{\rm T}^{\rm N'}}{p_{\rm T}^{\ell'} p_{\rm T}^{\rm N}},\tag{6}$$

which measures the deflection of N' with respect to \vec{q} in the transverse plane. If the initial-state nucleon were static and free, $\delta \phi_{\rm T}$ would be zero; with nuclear effects,



FIG. 3. Conditional probability density function of $\delta \alpha_{\rm T}$ as a function of the muon $p_{\rm T}$ without FSIs (each slice of $p_{\rm T}^{\mu}$ is normalized in such a way that the maximum is 1; the renormalized density is shown on the z-axis), predicted by NuWro for ν_{μ} CC QE on carbon (RFG) at neutrino energy of 1 GeV with FSIs switched off.

the deflection caused by $\Delta \vec{p}$ adds in a smearing to the initial distribution of $\delta \phi_{\rm T}$ that is determined by $\vec{p}_{\rm N}$. Experiments have measured the $\delta \phi_{\rm T}$ distribution in QE-like events [16] and used it to enhance the QE purity [15, 17]. However, the trigonometric relation illustrated by Fig. 2 shows that $\delta \phi_{\rm T}$ scales with $\delta p_{\rm T}/p_{\rm T}^{\ell'}$ and therefore depends on the lepton kinematics which are sensitive to the neutrino energy. The energy dependence of $p_{\rm T}^{\ell'}$ counteracts the FSI deflection and the uncertainties from the nuclear effects and neutrino flux become convolved. The distribution of $\delta \phi_{\rm T}$ by NuWro is shown in Fig. 5 for different neutrino energies. In contrast to the expected evolution with the FSI strength, the distribution becomes narrower at higher energy because of the increase of $p_{\rm T}^{\ell'}$. This serves as an example of how the neutrino energy dependence can bias a measurement of nuclear effects. Because of the $p_{\rm T}^{\ell'}$ dependence, the single-transverse variables all suffer to some extent from a dependence on the neutrino energy even after kinematic saturation is reached. Nevertheless, the study of nuclear effects can be performed by restricting $p_{\rm T}^{\ell'}$.

IV. MODEL PREDICTIONS

In the previous discussion, an equivalence is established between the nuclear effects in neutrino-nucleus interactions and the transverse kinematic imbalance. Initial and final-state effects can be directly observed via $\delta \vec{p}_{\mathrm{T}}$, as can be seen by rewriting Eq. 4 into

$$\delta \vec{p}_{\rm T} = \vec{p}_{\rm T}^{\rm N} - \Delta \vec{p}_{\rm T},\tag{7}$$

where $\vec{p}_{\rm N}$ is the momentum of the initial nucleon. In this section we present the latest predictions of the single-transverse variables. Interactions of neutrinos from the



FIG. 4. Probability density function of $\delta p_{\rm T}$ (upper) and $\delta \alpha_{\rm T}$ (lower) predicted by NuWro for different neutrino energy.



FIG. 5. Probability density function of $\delta \phi_{\rm T}$.

NuMI (on-axis) beam line [18] on a carbon target are simulated by NuWro (version 11q) [12] and GENIE (version 2.10.0) with the hA FSI model [19]. Since the neutrino energy is well above the saturation scale $\mathcal{O}(0.5 \text{ GeV})$, the minimal energy dependence of the transverse kinematic imbalance applies. Interesting features of the implemented nuclear effects in the models are therefore maximally preserved and readily identified as shown be-



FIG. 6. NuWro predictions for $\delta p_{\rm T}$ with different nuclear states: relativistic Fermi gas (RFG) [14], relativistic Fermi gas with the Bodek-Ritchie modifications (BR-RFG) [20], local Fermi gas (LFG) [21] and spectral function (SF) [22]. The NuMI [18] on-axis flux shape is used to simulate the neutrino energy distribution.

low.

The NuWro prediction for $\delta p_{\rm T}$ in QE is shown in Fig. 6. Four models of the nuclear state—relativistic Fermi gas (RFG) [14], relativistic Fermi gas with the Bodek-Ritchie modifications (BR-RFG) [20], local Fermi gas (LFG) [21] and spectral function (SF) [22]—are compared. The deformation of the $p_{\rm T}^{\rm N}$ shape due to FSI, which results in the long tail towards the upper end of the $\delta p_{\rm T}$ distribution, is limited by the FSI strength quantified by $\tau_{\rm f}$. For finite $\tau_{\rm f}$, as is the case predicted by NuWro (see e.g. Fig. 1), the $\delta p_{\rm T}$ shapes largely preserve the Fermi motion distributions—a useful technique for understanding novel target materials in future experiments such as DUNE [1].

The NuWro and GENIE predictions for $\delta \alpha_{\rm T}$ and $\delta \phi_{\rm T}$ in QE are shown in Fig. 7. When FSI is switched off in both simulations, consistent distributions are observed. With the nominal settings, the two predictions significantly differ in the $\vec{q}_{\rm T}$ -collinear regions— $\delta \alpha_{\rm T} \sim 0, 180$ degrees and $\delta \phi_{\rm T} \sim 0$ degrees—where GENIE predicts a much enhanced probability. While the NuWro distributions show *normal* evolution when the FSI is switched on as one would expect from the in-medium deflection and deceleration caused by FSI, the GENIE distributions show an *inverted* tendency. Motivated by this observation, the GENIE Collaboration suggested to investigate the effect of the *elastic interaction* of the hA FSI model. In the nominal GENIE simulation for QE on carbon, events with protons that undergo this FSI interaction amount to about 40% at the NuMI beam energy. After removing these events, the GENIE prediction is more consistent with the NuWro nominal one, as is shown in Fig. 7. Further investigation taking into account the dependence on $p_{\rm T}^{\ell'}$ (in a similar approach to Fig. 3) shows that in $\delta \alpha_{\rm T}$ the collinear enhancement is of an appearant acceleration feature at low $q_{\rm T}$ ($\lesssim 200 \text{ MeV}/c$ at NuMI



FIG. 7. NuWro and GENIE predictions for $\delta \alpha_{\rm T}$ (upper) and $\delta \phi_{\rm T}$ (lower). Nominal distributions are compared to the cases where FSI is disabled. Further comparison is made by removing nominal GENIE events that experienced proton elastic FSI (see text for exact definition).

energy), and deceleration at high $q_{\rm T}$.

V. DISCUSSION

The definitions of the transverse kinematic imbalance require an exclusive measurement of the primary finalstate particles. In RES, the imbalance is defined between the charged lepton and the $p\pi^{+(-)}$ -system with a ν ($\bar{\nu}$) beam. Transverse kinematic imbalance in RES, proposed for the first time, should provide information on the resonance and pion FSIs. As an example, the NuWro and GENIE predictions for $\delta p_{\rm T}$ in Δ^{++} (p π^+) production is shown in Fig. 8. In the NuWro predictions, the deformation of the $p_{\rm T}^{\rm N}$ shape is severer in RES than in QE because of the additional FSI from the pion final state; for GENIE, both the proton and pion hA elastic interaction contribute to an *inverted* deformation of the $p_{\rm T}^{\rm N}$ shape towards the lower end of the $\delta p_{\rm T}$ distribution. Because all simulations use the same nuclear state (BR-RFG), a stronger FSI in GENIE can be inferred by its more pronunced upper tail in the distribution.

Another interesting example from the transverse kine-



FIG. 8. NuWro and GENIE predictions for $\delta p_{\rm T}$ in QE and Δ^{++} (p π^+) production. Nominal GENIE events that experienced proton and pion elastic FSI are removed stepwise to separate the effects; similar features are also exhibited in the p π^- and p π^0 channels.

matic imbalance in RES is the Pauli blocking of the resonance decay product. If it does not affect the resonance momentum—this is expected since the polarization of the decay product alone can vary to fulfill Pauli blocking—the $\delta \alpha_{\rm T}$ distribution at small $p_{\rm T}^{\ell'} (\leq p_{\rm F})$ will not be suppressed at 180 degrees, different from the QE case.

So far the discussion only considers the in-medium energy-momentum transfer and nuclear emission that are induced by FSIs. In reality, multinucleon correlations in the initial state could have significant impact in both processes that are however non-distinguishable from being FSI-induced on an event-by-event basis. Their contribution to the kinematic imbalance results in an additional convolution to each of the single transverse variables. The $\delta p_{\rm T}$ and $\delta \alpha_{\rm T}$ distributions—especially in the regions beyond the Fermi momentum and around the backward peak, respectively—may therefore provide a kinematic constraint on the multinucleon correlations. Furthermore, because the nuclear emission probability is enhanced, its correlations against the single transverse variables may be of interest to provide sensitive signatures.

In general, samples of QE and RES can be produced by selecting events with at least one proton and no pion, and at least one proton and one pion, respectively, in a CC inclusive sample. Neutrino energy-dependent contamination comes from other channels where incomplete final states are selected. In addition, because of their intrinsic kinematic imbalance, such non-exclusive backgrounds mimic the exclusive signals that experience FSIs and/or multinucleon correlations. However, quantitatively they may behavior differently: because of the characteristic strengths of the imbalance, one would expect that the single-transverse variables from the background, the signal with FSIs, and that with multinucleon correlations form a certain ordering, based on which it might be possible to perform efficient channel purification and nuclear effect identification.

The observation of the transverse kinematic imbalance relies on the momentum reconstruction of both leptonic and hadronic final states. Since the $\delta \vec{p}_{\rm T}$ distributions reveal nuclear effects including Fermi motion, deflection and acceleration/deceleration in FSI. efforts in improving the momentum and angular resolution, as well as in understanding the momentum scales of the final-state lepton, proton and pion might be needed for current experiments. Experiments with trackers, for example T2K [23] and MINER ν A [24], might be capable to perform pioneering measurements to validate the different model predictions presented in the previous section. The prospect in MINER ν A with its multiple-type nuclear targets is of special interest because the transverse kinematic imbalance would directly show the evolution of the nuclear effects as the target type varies.

Throughout this work, it is emphasized that the equivalence between nuclear effects and transverse kinematic imbalance is invariant with the neutrino energy. In fact this equivalence is invariant with *all* physics at the neutrino-nucleon interaction level. In analogue to the minimal neutrino energy dependence, transverse kinematic imbalances are also minimally influenced by nucleon level model uncertainties, such as the details of the nucleon form factors (Fig. 9). This further reduces the uncertainties in measuring nuclear effects.

Even though this work is motivated for neutrino interactions, the technique can be used in electron-nucleus scattering to probe nuclear effects in general. In such a case, as the electron beam energy is well known, the energy imbalance between the initial and final states can also be studied.

VI. SUMMARY

In this work, for a measurement of nuclear effects independent of the neutrino energy, transverse kinematic imbalance has been systematically examined. Its novel application to the resonance production is important for experiments with high energy neutrinos produced in the NuMI and LBNF [1] beam lines because of the significant production cross section; it is also unique for the study of nuclear effects in antineutrino interactions where the final-state neutrons in quasielastic scattering cannot usually be measured. An extension of the singletransverse kinematics in the resonance production is the double-transverse momentum imbalance [5, 25], which is defined on the axis perpendicular to both the neutrino and charged lepton momenta, with a sensitivity to the difference between the proton and pion FSIs. A comprehensive description of nuclear effects in neutrino interactions should be attainable from future measurements of the single- and double-transverse kinematic imbalance on various nuclear targets in different interaction channels.



FIG. 9. Comparison of $\delta p_{\rm T}$ (upper), $\delta \alpha_{\rm T}$ (middle) and the final-state proton momentum $p_{\rm p}$ (lower) in QE for different values of the axial mass $M_{\rm A}^{\rm QE}$: 0.8, 1.2 (nominal) and 1.6 GeV. It shows that the transverse kinematic imbalances are much less sensitive to the variation of $M_{\rm A}^{\rm QE}$.

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- [9] The in-medium interaction probability is a functional of the nucleon momentum distribution in the nucleus.
- [10] For simplicity, the nucleus excitation during the basic interaction is not discussed here.
- [11] To be precise, the nuclear emission considered here is from the deexcitation within a detection time window. In practice, slow emission with a longer transition time

is effectively seen as no emission. Another way the inmedium energy-momentum transfer is carried away is via the nucleus recoil.

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