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Precise measurement of α_K and α_T for the 150.8-keV E3 transition in ^{111}Cd : Test of internal-conversion theory

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We have measured the K-shell and total internal conversion coefficients, α_K and α_T , for the 150.8-keV E3 transition in ¹¹¹Cd to be 1.449(18) and 2.217(26) respectively. The α_K result agrees well with Dirac-Fock calculations in which the effect of the K-shell atomic vacancy is accounted for; it extends our precision tests of α_K calculations to Z=48, the lowest Z yet measured. However, the result for α_T disagrees by about two standard deviations from the calculated α_T value, whether or not the atomic vacancy is included.

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I. INTRODUCTION

Over the past decade we have published a sequence of papers [1–7], in which we reported measurements of K-shell Internal Conversion Coefficients (ICCs) for E3 and M4 transitions in 6 nuclei with a precision of $\pm 2\%$ or better. The motivation has been to test ICC theory, in particular its treatment of the K-shell vacancy left behind by the emitted electron. What makes such precise measurements possible for us is our having an HPGe detector whose relative efficiency is known to $\pm 0.15\%$ ($\pm 0.20\%$ absolute) over a wide range of energies: See, for example, Ref. [8]. By detecting both the K x rays and the γ rays from a transition of interest in the same well-calibrated detector at the same time, we can avoid many sources of error.

By 2008, our early results from this program influenced a reevaluation of ICCs by Kibédi $et\ al.\ [9]$, who also developed BrIcc, a new data-base obtained from the basic code by Band $et\ al.\ [10]$ but, in conformity with our conclusions, it employed a version of the code that incorporates the vacancy in the "frozen orbital" approximation. The BrIcc data-base has been adopted by the National Nuclear Data Center (NNDC) and is available on-line for the determination of ICCs. Our experimental results obtained since 2008 continue to support that decision and have included transitions in nuclei that cover the range 50 < Z < 78.

We report here a measurement that extends the range down to Z=48. We have measured the α_K and α_T values for the 150.8-keV E3 transition in ¹¹¹Cd to precisions of $\pm 1.7\%$ and $\pm 0.8\%$, respectively. These results are interesting not so much in distinguishing between

models to account for the atomic vacancy – the difference in calculated ICCs between models that do and do not include the vacancy is rather small – but in testing whether either model comes close to describing the experimental data at all. Previous measurements of α_K and α_T for this transition [11–13] have been inconsistent with one another, scattering widely, but generally being significantly lower than the corresponding calculated values. Since the transition is hindered by $\sim 10^4$ relative to the Weisskopf limit [12, 14], the discrepancy has been associated with ICC anomalies observed for some other strongly hindered transitions. However, we have previously demonstrated [3] that the α_K for the 127.5-keV E3 transition in ¹³⁴Cs, a similarly hindered case [14], agrees well with calculations. Is the transition in ¹¹¹Cd really discrepant and, if so, does the disagreement with theory extend to both α_K and α_T values?

II. MEASUREMENT OVERVIEW

In our previous measurements we were dealing with decay schemes dominated by a single transition that can convert in the atomic K shell. Under those conditions, if a spectrum of K x rays and γ rays is recorded, then the K-shell ICC for the transition is given by

$$\alpha_K = \frac{N_K}{N_\gamma} \cdot \frac{\epsilon_\gamma}{\epsilon_K} \cdot \frac{1}{\omega_K},\tag{1}$$

where ω_K is the fluorescence yield; N_K and N_{γ} are the total numbers of observed K x rays and γ rays, respectively; and ϵ_K and ϵ_{γ} are the corresponding photopeak detection efficiencies.

The fluorescence yield for cadmium has been measured several times, with a weighted average quoted to $\pm 2.1\%$ [15]. Furthermore, world data for fluorescence yields have also been evaluated systematically as a function of Z [16] for all elements with $10 \le Z \le 100$, and ω_K values have been recommended for each element in this range. The recommended value for cadmium, Z = 48, is 0.842(4),

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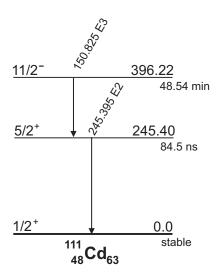


FIG. 1: Decay scheme for the 48.5-min isomer in ¹¹¹Cd. The data are taken from Ref. [17].

which is consistent with the average measured value but has a smaller relative uncertainty, $\pm 0.5\%$. We use this value.

The decay scheme of the 48.5-min isomer in 111 Cd is shown in Fig. 1. It does not have a single dominant transition but rather a cascade of two, both of which can convert in the K shell. Thus, to extract the α_K value for the 150.8 keV transition, we must use a modified version of Eq. 1:

$$\alpha_{K150} = \frac{N_K}{N_{\gamma 150}} \cdot \frac{\epsilon_{\gamma 150}}{\epsilon_K} \cdot \frac{1}{\omega_K} - \alpha_{K245} \cdot \frac{N_{\gamma 245}}{N_{\gamma 150}} \cdot \frac{\epsilon_{\gamma 150}}{\epsilon_{\gamma 245}}, (2)$$

where the subscripts 150 and 245 on a quantity denote the transition – either the 150.8-keV or 245.4-keV one – to which that quantity applies. Note that the result we are seeking for α_{K150} now depends on α_{K245} but since the 245.4-keV transition is pure E2 and has higher energy, its K-conversion coefficient is about an order of magnitude smaller, so the dependence of α_{K150} on α_{K245} is rather weak and does not seriously degrade the precision with which the former can be determined.

Having a second transition in cascade with the 150.8-keV transition also offers an advantage: It allows the determination of α_{T150} via the equation

$$(1 + \alpha_{T150}) \cdot \frac{N_{\gamma 150}}{\epsilon_{\gamma 150}} = (1 + \alpha_{T245}) \cdot \frac{N_{\gamma 245}}{\epsilon_{\gamma 245}}.$$
 (3)

In this case, the fact that α_{T245} is much smaller than 1 (~0.06) and α_{T150} is greater than 1 (~2.2), the experimental result obtained for α_{T150} is rather insensitive to the calculated value used for α_{T245} .

Note that in Eqs. (1-3) all the N values have to incorporate corrections for coincidence summing, which for the two gamma rays must also include the effect of the angular correlation between them. For N_K , the contributions from impurities must also be removed.

In our experiments, we detect the γ rays and the K x rays in the same HPGe detector, a detector whose efficiency has been meticulously calibrated [8, 18, 19] to subpercent precision, originally over an energy range from 50 to 3500 keV but more recently extended [6] down to 22.6 keV, the average energy of silver K x rays. Over this whole energy region, precise measured data were combined with Monte Carlo calculations from the CYLTRAN code [20] to yield a very precise and accurate detector efficiency curve. In our present study, the γ rays of interest at 150.8 and 245.4 keV are well within the energy region for which our efficiencies are known to a relative precision of $\pm 0.15\%$. The cadmium K x rays lie between 23 and 27 keV, just within our extended region of calibration so the detector efficiency for them can only be quoted to a relative precision of $\pm 1\%$.

III. EXPERIMENT

We used the same experimental method and setup as in our previous measurements [1–7]. Only those details not covered in previous publications will be described here.

A. Source Preparation

We produced $^{111}\mathrm{Cd}$ by neutron activation of a thin layer of 95.88%-enriched $^{110}\mathrm{CdO}$ electroplated onto a 10- $\mu\mathrm{m}$ -thick foil of 99.999% pure aluminum. The source material was obtained as cadmium metal powder from Trace Sciences International, which itemized its chemical and isotopic impurities. The former totaled less than 250 ppm and, of the latter, only $^{106}\mathrm{Cd}$ (0.01%), $^{108}\mathrm{Cd}$ (0.02%), $^{114}\mathrm{Cd}$ (0.84%) and $^{116}\mathrm{Cd}$ (0.16%) are of potential relevance to our post-activation γ -ray spectrum.

Two samples were prepared, each from ~ 0.9 mg of the enriched metal foil. Each foil was dissolved in 100 μ L of 2-molar HNO₃ and evaporated to dryness under argon gas to convert the metal into the nitrate form. The sample was then reconstituted with 5-10 μ L of 0.1-molar HNO_3 and ~ 12 mL of anhydrous isopropanol. We then transferred this solution to an electrodeposition cell, and electrochemically deposited the $^{110}\text{Cd}(\text{NO}_3)_2$, using the molecular plating technique [21, 22], onto a 10- μ m-thick, 99.999%-pure Al backing (purchased from Goodfellow USA). The deposition voltage was 350-700 V with a current density of $\sim 2 \text{ mA/cm}^2$. Deposition times ranged from 40 to 60 min. After deposition, each target was rinsed in acetone for 5 min and baked in atmosphere at 200° C for 30 min to convert the 110 Cd(NO₃)₂ to 110 CdO. The plating efficiencies were between 95 and 100%.

We used identically made ^{nat}CdO targets to characterize the products instead of ¹¹⁰CdO because the analysis techniques led to destruction of the targets. Since the conditions for molecular plating were carefully controlled and are highly reproducible, we expect that the chemical and physical properties of the natural and isotopically

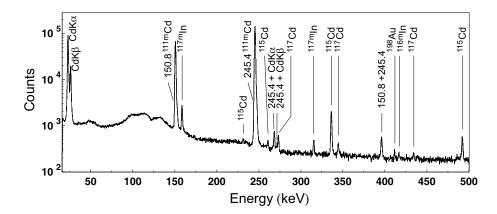


FIG. 2: Portion of the x- and γ -ray energy spectrum measured for 15 min with source S2. Room background has been subtracted. The background was recorded before and after the source data were measured; and was normalized to the same live-time. Peaks are labeled by their β -decay parent; the γ -ray peaks associated with 111m Cd decay also have their energies in keV marked.

enriched targets were very similar. The $^{\rm nat}{\rm CdO}$ targets were analyzed with scanning-electron microscopy (SEM) and atomic-force microscopy (AFM) to examine the surface and ensure uniformity. The average variation in the thickness was ${\sim}0.1\,\mu{\rm m}$ as determined by AFM; and the images taken via SEM showed a mostly smooth, uniform layer of $^{\rm nat}{\rm CdO}$ with few cracks or other irregularities. Finally, an energy-dispersive x-ray-spectrometry analysis confirmed that the $^{\rm nat}{\rm CdO}$ targets did indeed have a 1:1 cadmium-to-oxygen atomic ratio and that no major contaminants were introduced during the molecular plating process.

One of the 110 CdO targets (S1) had an areal density of $435(8)~\mu g/cm^2$; the other (S2) had $475(8)~\mu g/cm^2$. Both were 1.7 cm in diameter. The sources were activated, one month apart, for 2h in a neutron flux of $\sim 7 \times 10^{12}~n/(cm^2~s)$ at the TRIGA reactor in the Texas A&M Nuclear Science Center. After removal from the reactor each sample was conveyed to our measurement location, where counting began approximately 4h after the end of activation. The initial activity from 111m Cd was determined to be $\sim 80~k$ Bq.

B. Radioactive decay measurements

We acquired spectra with our precisely calibrated HPGe detector and with the same electronics used in its calibration [8]. Our analog-to-digital converter was an Ortec TRUMP TM -8k/2k card controlled by MAESTRO TM software. We acquired 8k-channel spectra at a source-to-detector distance of 151 mm, the distance at which our calibration is well established. Each spectrum covered the energy interval 10-2000 keV with a dispersion of about 0.25 keV/channel.

With source S1 we acquired 14 spectra over a two-week period; with S2 we acquired 10 spectra in one week. Since 111m Cd has a half-life of only 49 min, all but the first few spectra recorded in each case were used solely as an aid in identifying contaminant activities. All subsequent analysis was based on only two spectra – the first 9-min spectrum taken from S1 and the first 15-min spectrum from S2 – where the 111m Cd activity was most dominant. It is the results from these two spectra that are reported

here.

IV. ANALYSIS

A portion of the S2 spectrum is presented in Fig. 2: It includes the x- and γ -ray peaks of interest from the decay of 111m Cd, as well as a number of weak peaks from contaminant activities. In our analysis of the data, we followed the same methodology as we did with previous source measurements [1–7]. We first extracted areas for essentially all the x- and γ -ray peaks in the background-subtracted spectrum. Our procedure was to determine the areas with GF2, the least-squares peak-fitting program in the RADWARE series [23]. In doing so, we used the same fitting procedures as were used in the original detector-efficiency calibration [8, 18, 19].

Once the areas (and energies) of peaks had been established, we could identify all impurities in the 111m Cd spectrum and carefully check to see if any were known to produce x or γ rays that might interfere with the cadmium K x rays or either of the two γ -ray peaks of interest, at 150.8 and 245.4 keV. As is evident from Fig. 2, even the weakest peaks were identified. In all, we found 5 weak activities that contribute to the cadmium x-ray region; these are listed in Table I, where the contributions are given as percentages of the total cadmium x rays recorded. No impurities interfere in any way with either of the γ -ray peaks.

The spectra in Fig. 3 show expanded versions of the

TABLE I: The contributions of identified impurities to the energy region of the cadmium K x-ray peaks.

| Source | Contaminant | Contribution to spectrum (%) | | |
|---|--|---|--|--|
| | | S1 | S2 | |
| ^{115}Cd ^{117}Cd ^{117}In ^{117m}In ^{116m}In | In K x rays In K x rays Sn K x rays In+Sn K x rays In K x rays | 1.81(8) 0.113(12) 0.18(3) 0.603(9) 0.010(2) | 2.71(6) 0.125(9) 0.21(3) 0.484(5) 0.006(1) | |

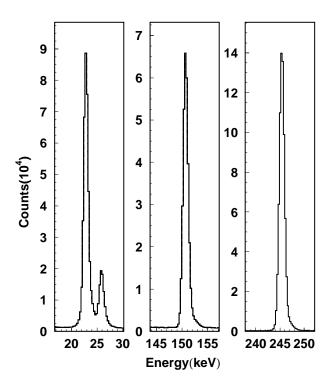


FIG. 3: Spectra for the three energy regions of interest in this measurement. From left to right are shown the cadmium K x rays, and the γ rays at 150.8 and 245.4 keV. These correspond to the full spectrum presented in Fig. 2

energy regions of interest for this measurement: they include the cadmium K x rays and the γ rays at 150.8 and 245.4 keV. In all cases, the peaks lie cleanly on a flat background. The count total recorded in the energy region of the cadmium K_{α} and K_{β} x rays appears for each source in the top row of Table II. The impurity totals, derived from the percentage breakdowns listed in Table I, are given in the second row of Table II. Three more corrections need to be applied at this stage: The first relates to the shape of the x-ray peaks. As explained in our previous papers (see, for example, Ref. [1]) we use a special modification of the GF2 program that allows us to sum the total counts above background within selected energy limits. To account for possible missed counts outside those limits, the program adds an extrapolated Gaussian tail. This extrapolated tail does not do full justice to x-ray peaks, whose Lorentzian shapes reflect the finite widths of the atomic levels responsible for them. To correct for this effect we compute simulated spectra using realistic Voigt functions to generate the x-ray peaks, and we then analyze them with GF2, following exactly the same fitting procedure as is used for the real data, to ascertain how much was missed by this approach. The resultant correction factor appears as a percent in Table II.

The second correction takes account of truecoincidence summing. Because the two transitions from $^{111m}\mathrm{Cd}$ occur in rapid succession, there is a finite possibility that two γ rays, or a γ ray from one transition and an x ray from the other, can appear essentially simultaneously in our detector and thus be recorded with an apparent energy that differs from 150.8 or 245.4 keV or from the K x-ray energy. If not corrected for, these summing processes would falsely deplete the counts in the peaks of interest. We can easily calculate the effects of this true-coincidence summing (as distinct from random summing, which is negligible in our case) because the efficiency of our HPGe detector and the total-to-peak ratio of its response function are both well known as a function of γ -ray energy [19]. The resultant correction factor for the x ray appears as a percent in the table.

The third correction arises from the finite thickness of our samples, which leads to some additional attenuation of the K x rays relative to the higher-energy γ rays, over and above the calibrated relative efficiencies of the HPGe detector. These percentage corrections are also listed in the table, and the values for N_K , corrected for impurities, the Lorentzian shape, summing and relative attenuation, are given on the line below.

The counts recorded in the two γ -ray peaks also appear in Table II. They require no corrections for impurities or shape but they are subject to summing corrections, so these are also given in the table. In evaluating these corrections, we have taken account of the calculated angular correlation between the two γ rays, which favors small angles and thus serves to increase the summing probability slightly. The corrected values for $N_{\gamma 150}$ and $N_{\gamma 245}$ are shown for both sources immediately below the summing

TABLE II: Corrections to the 111m Cd K x rays and the 150.8-and 245.4-keV γ rays, as well as the additional information required to extract a value for α_{K150} .

| Quantity | Value | | |
|---|-------------------------|-------------------------|--|
| | S1 | S2 | |
| $\operatorname{Cd}(K_{\alpha}+K_{\beta})$ x rays | | | |
| Total counts | $1.979(6) \times 10^5$ | $4.695(9) \times 10^5$ | |
| Impurities | $-5.39(14)\times10^3$ | $-1.66(3)\times10^4$ | |
| Lorentzian correction | +0.12(2)% | +0.12(2)% | |
| Summing correction | +0.99(6)% | +0.99(6)% | |
| Attenuation correction | +0.27(2)% | +0.29(2)% | |
| Corrected counts, N_K | $1.952(6) \times 10^5$ | $4.593(10) \times 10^5$ | |
| $^{111}\mathrm{Cd}\ 150.8\text{-keV}\ \gamma\ \mathrm{ray}$ | | | |
| Total counts | $1.303(11)\times10^{5}$ | $3.064(25)\times10^5$ | |
| Summing correction | +1.29(6)% | +1.29(6)% | |
| Corrected counts, $N_{\gamma 150}$ | $1.320(12)\times10^5$ | $3.104(25)\times10^5$ | |
| $^{111}\mathrm{Cd}\ 245.4\text{-keV}\ \gamma\ \mathrm{ray}$ | | _ | |
| Total counts | $3.024(22)\times10^5$ | $7.082(45)\times10^5$ | |
| Summing correction | +0.86(3)% | +0.86(3)% | |
| Corrected counts, $N_{\gamma 245}$ | $3.050(22)\times10^5$ | $7.143(45) \times 10^5$ | |
| $N_K/N_{\gamma 150}$ | 1.479(14) | 1.480(12) | |
| $N_{\gamma 245}/N_{\gamma 150}$ | 2.311(27) | 2.301(24) | |

correction.

In anticipation of their use in Eqs. (2) and (3), the ratios $N_K/N_{\gamma 150}$ and $N_{\gamma 245}/N_{\gamma 150}$ also appear in Table II, where it can be seen that the results from both sources are entirely consistent with one another. Consequently, we use the weighted average of results from the two sources for all subsequent analysis: viz.

$$N_K/N_{\gamma 150} = 1.479(10)$$

 $N_{\gamma 245}/N_{\gamma 150} = 2.305(18)$ (4)

We deal next with the efficiency ratios, $\epsilon_{\gamma 150}/\epsilon_{\gamma 245}$ and $\epsilon_{\gamma 150}/\epsilon_K$, also required by Eqs. (2) and (3). The former can be obtained from our well-established detector efficiency curve obtained via CYLTRAN Monte Carlo calculations [8]. The latter requires a multi-step process. Following the same procedure as the one we used in analyzing the decay of 119m Sn [6], we employ as low-energy calibration the well-known decay of ¹⁰⁹Cd, which emits 88-keV γ rays and silver K x rays. The latter are very close in energy to the cadmium K x rays observed in the current measurement. Note that we are not distinguishing between K_{α} and K_{β} x rays. Scattering effects are quite pronounced at these energies and they are difficult to account for with an HPGe detector when peaks are close together, so we have chosen as before to use only the sum of the K_{α} and K_{β} x-ray peaks. For calibration purposes, we consider each sum to be located at the intensity-weighted average energy of the component peaks¹—23.62 keV for cadmium and 22.57 keV for silver.

We obtain the required ratio, $\epsilon_{\gamma 150}/\epsilon_{K23.6}$ from the following relation:

$$\frac{\epsilon_{\gamma 150}}{\epsilon_{K23.6}} = \frac{\epsilon_{\gamma 88.0}}{\epsilon_{K22.6}} \cdot \frac{\epsilon_{\gamma 150}}{\epsilon_{\gamma 88.0}} \cdot \frac{\epsilon_{K22.6}}{\epsilon_{K23.6}},\tag{5}$$

where here we have identified the K x rays by their centroid energy for clarity. We take the ratio $\epsilon_{\gamma 88}/\epsilon_{K22.6} = 1.069(8)$ from our previously reported measurement [6]. The ratio $\epsilon_{\gamma 150}/\epsilon_{\gamma 88.0} = 0.8707(13)$ is determined from our known detector efficiency curve calculated with the CYLTRAN code [8], while $\epsilon_{K22.6}/\epsilon_{K23.6} = 0.9849(9)$ comes from a CYLTRAN calculation as well but in an energy region with higher uncertainty. Nevertheless, the energy span is so small that the uncertainty on the ratio is also very small ($\sim 0.1\%$).

The two efficiency ratios required by Eqs. (2) and (3) are thus:

$$\frac{\epsilon_{\gamma 150}}{\epsilon_{\gamma 245}} = 1.3123(14)$$

$$\frac{\epsilon_{\gamma 150}}{\epsilon_{K}} = 0.917(7).$$
(6)

V. RESULTS AND DISCUSSION

The K-shell ICCs for the two transitions from 111m Cd can be related to one another if we substitute the measured ratios from Eqs. (4) and (6) into Eq. (2); the result is

$$\alpha_{K150} = 1.610(18) - 3.025(24) \ \alpha_{K245}. \tag{7}$$

Because α_{K245} is about an order of magnitude smaller than α_{K150} , its contribution to this equation is minor. Nonetheless its value must be calculated in order to obtain a value for α_{K150} . Our ICC calculations are made within the Dirac-Fock framework with the option either to ignore the K-shell vacancy or to include it in the "frozen orbital" approximation [10]. For α_{K245} the two different calculations yield values that differ by less than 1%: 0.05309 (no vacancy) and 0.05343 (vacancy included). So as not to prejudice our result for the 150.8-keV transition, we adopt the value 0.05326(17), which encompasses both possibilities. Substituting this value into Eq. (7) we obtain the result:

$$\alpha_{K150} = 1.449(18),\tag{8}$$

where the uncertainty in α_{K245} makes a negligible contribution to the α_{K150} uncertainty.

Next, the total ICCs for the two transitions can be related to one another by substitution of Eqs. (4) and (6) into Eq. (3); in this case the result is

$$\alpha_{T150} = 3.025(24) (1 + \alpha_{T245}) - 1.$$
 (9)

The total ICC for the 245.4-keV transition is calculated to be 0.06333 if the vacancy is ignored and 0.06368 with the vacancy included, so again we choose the average with an assigned uncertainty that encompasses both values: 0.06351(17). Substituting this value into Eq. (9) we obtain:

$$\alpha_{T150} = 2.217(26). \tag{10}$$

As with the K-shell ICCs, the uncertainty in α_{T245} has no impact on the uncertainty attached to α_{T150} .

There has been only one previous measurement of α_{K150} , by Németh and Veres [13], who also used an HPGe detector to record both the x and γ rays. Their result, 1.29(11), is statistically consistent with ours but is a factor of 6 less precise – see Eq. (8).

The situation is more complicated for α_{T150} , of which there have been three previous measurements. The earliest, by Lu [11], is from 1960: It was performed with a source placed in the well of a large NaI(Tl) scintillator, and produced a result, averaged over two independent runs, of 2.286(9), with an astonishing $\pm 0.4\%$ uncertainty. The two more-recent measurements, which both appeared in the 1980s, employed HPGe detectors to obtain the values 1.76(8) [12] and 1.98(5) [13]. All three of these references were included in the 2002 survey of internal conversion coefficients published by Raman et al.[25],

¹ To establish the weighting, we used the intensities of the individual x-ray components from Table 7a in Ref. [24].

TABLE III: Comparison of the measured α_K and α_T values for the 150.853(15)-keV E3 transition from 111m Cd with calculated values based on two different theoretical models, one that ignores the K-shell vacancy and one that deals with it in "frozen orbital" (FO) approximation [10]. Shown also are the percentage deviations, Δ , from the experimental value calculated as (experiment-theory)/theory. For a description of the various models used to determine the conversion coefficients, see Ref. [1].

| Model | α_K | $\Delta(\%)$ | α_T | $\Delta(\%)$ |
|-------------|------------|--------------|------------|--------------|
| Experiment | 1.449(18) | | 2.217(26) | |
| Theory: | | | | |
| No vacancy | 1.425(1) | +1.7(12) | 2.257(1) | -1.8(12) |
| Vacancy, FO | 1.451(1) | -0.1(12) | 2.284(1) | -2.9(12) |

but the Lu result appeared there as 2.29(3), the survey authors having decided to increase its uncertainty. Finally Raman *et al.* "adopt" 2.12(11) as the recommended value for α_{T150} . Strikingly, none of the three previous measurements agree with one another or with our new result, which appears in Eq. (10); however, our result does agree with the value adopted in the 2002 survey [25] and has an uncertainty smaller by a factor of 4.

In Table III, our measured α_K and α_T results for the 150.8-keV E3 transition are each compared with two theoretical values, one that was calculated without accounting for the atomic vacancy and one that included the vacancy in the "frozen orbital" (FO) approximation [10]. The percentage deviations given in the table show excellent agreement between our α_K measurement and the calculation that includes provision for the atomic vacancy. This outcome is consistent with our previous five precise α_K measurements on E3 and M4 transitions in ¹¹⁹Sn [6, 7], ¹³⁴Cs [3, 4], ¹³⁷Ba [3, 4], ¹⁹³Ir [1, 2] and ¹⁹⁷Pt [5], all of which agreed well with the FO calculations, and disagreed – some by many standard deviations – with the no-vacancy calculations.

Our α_T result does not lead to such a simple conclusion: It is lower than both calculations, with the worst disagreement ($\sim 2.5\sigma$) being with the FO calculation. One possible explanation arises from the fact that the 150.8-keV transition is hindered by a factor of 10^4 relative to the single-particle Weisskopf estimate [14]. Under such conditions, one could expect to encounter "penetration", which is a dynamic effect associated with the change from transition electromagnetic potentials used for a point nucleus to transition potentials required for a realistic finite-sized nucleus [26]. For unhindered electric transitions, the penetration effect is not significant, but it may reach several percent for magnetic transitions. The effect is included in our ICC calculations by an ap-

proximation based on the surface-current model [25] but it is done uniformly with all nuclei and all transitions. For strongly hindered transitions, the penetration effect can become more important, giving rise to non-negligible nuclear matrix elements in the expressions for the ICCs. In this way these particular ICCs become dependent on nuclear structure details and nuclear transition dynamics.

Calculations of penetration factors for specific nuclei were attempted decades ago, but mainly for M1 and E1 transitions (see for example Refs. [26–29]). To our knowledge, there are no convincing theoretical results for E3 transitions. Nevertheless, we may speculate that the discrepancy we observe between experiment and theory for α_T is likely due to penetration. Is it reasonable that the effect is evident for α_T and not for α_K ? Yes, Krpić and Aničin [29] argue (for M1 transitions) that under certain conditions the penetration can be "hidden" by a cancellation that only affects one atomic shell and not the others. It is plausible that this can explain our results; certainly no more definitive explanation is possible.

VI. CONCLUSIONS

Our measurement of the K-shell internal conversion coefficient for the 150.8-keV E3 transition from ^{111m}Cd has yielded a value, $\alpha_K=1.449(18)$, that agrees with a version of the Dirac-Fock theory that includes the atomic vacancy. It disagrees (by $\sim 1.5\sigma$) with theory if the vacancy is ignored. This result is consistent with the conclusion reached from our previous five precise ICC measurements, and extends the validity of that conclusion down to Z=48.

Our result for the total ICC of this transition, $\alpha_T = 2.217(26)$, is lower than theory by several percent. Although we cannot draw any definitive conclusion as to the cause of this discrepancy, we suggest that it may be due to penetration effects that have become noticeable because the transition is particularly hindered.

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