This is the accepted manuscript made available via CHORUS. The article has been published as:

## Upscattering of ultracold neutrons from gases

S. J. Seestrom et al. (UCNt Collaboration)

Phys. Rev. C 92, 065501 — Published 14 December 2015 DOI: 10.1103/PhysRevC.92.065501

# Upscattering of Ultracold Neutrons from Gases 

Revised 11/13/15 7:41 PM

S. J. Seestrom ${ }^{1}$, E. R. Adamek², D. Barlow ${ }^{1}$, L. J. Broussard ${ }^{1}$, N. B. Callahan², S. M. Clayton ${ }^{1}$, C. CudeWoods², S. Currie ${ }^{1}$, E. B. Dees ${ }^{4}$, W. Fox², P. Geltenbort ${ }^{4}$, K. P. Hickerson ${ }^{5}$, A. T. Holley ${ }^{2}$, C.-Y. Liu², M. Makela ${ }^{1}$, J. Medina ${ }^{1}$, D. J. Morley ${ }^{1}$, C. L. Morris ${ }^{1}$, J. Ramsey ${ }^{1}$, A. Roberts ${ }^{1}$, D. J. Salvat ${ }^{112}$, A.<br>Saunders ${ }^{1}$, E. I. Sharapov ${ }^{6}$, S. K. L. Sjue ${ }^{1}$, B. A. Slaughter ${ }^{2}$, B. VornDick ${ }^{3}$, P. L. Walstrom ${ }^{1}$, Z. Wang ${ }^{1}$, T. L. Womack ${ }^{1}$, and A. R. Young ${ }^{3,1}$<br>${ }^{1}$ Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA<br>${ }^{2}$ Indiana University, Bloomington, Indiana 47405, USA<br>${ }^{3}$ North Carolina State University, Raleigh, North Carolina 27695, USA<br>${ }^{4}$ Institut Laue Langevin, 38042 Grenoble, France<br>${ }^{5}$ University of California Los Angeles, Los Angeles, California 90095, USA<br>${ }^{6}$ Joint Institute for Nuclear Research, 141980, Dubna, Russia


#### Abstract

We present measurements of the upscattering cross sections of ultracold neutrons (UCN) from room temperature hydrogen, deuterium, neon, argon, xenon, $\mathrm{C}_{4} \mathrm{H}_{10}, \mathrm{CF}_{4}$ and air. The values of these cross sections are important for estimating the loss rate of trapped neutrons due to residual gas, and are therefore of importance for neutron lifetime measurements using UCN. Cross sections were obtained from a combined analysis of the UCN attenuation in a gas cell and direct measurement of the neutrons upscattered in the cell. The effects of the UCN velocity and path-length distributions were accounted for using a Monte Carlo transport code. Results are compared with measurements at higher neutron energy as well as with calculations.


Keywords: Ultracold neutrons, scattering and capture cross sections, noble gases, LANL UCN source, etc.

PACS: 25.40.Fq, 25.40.Kv, 28.20.Ka

## I. INTRODUCTION

The UCN $\tau$ Collaboration has built a large volume, $0.6 \mathrm{~m}^{3}$, magneto-gravitational trap that will be used to measure the lifetime of the free neutron.[1] In order to investigate possible systematic effects that could impact our measurement of the neutron lifetime, the collaboration is using the LANSCE ultracold neutron source[2]. One source of systematic errors comes from absorption and upscattering due to residual gas. Here we report measurements of the cross section for upscattering of UCN by potential residual gases that could be found within the UCN $\tau$ apparatus. Residual gas in the trap can absorb or upscatter the stored UCN to cold or thermal energies, thus introducing a potential source of UCN loss in the experiment. Recent neutron lifetime measurements using material bottles have corrected for this effect. Arzumanov et al. [3, 4] introduce a 0.2 s uncertainty (but no correction) in their determination of $\tau_{n}$ for a trap pressure of $1 \times 10^{-6}$ to $5 \times 10^{-6}$ torr. Pichlmaier et al. [5] introduce various corrections depending on the observed vacuum pressure and composition, ranging from 0.7 to 1.4 s . The larger corrections were due to the outgassing of Fomblin oil that was observed with a mass spectrometer and fine pressure gauge. Thereafter the pressure was stable at $3.8 \times 10^{-6}$ torr, and the dominant residual gas that can cause upscattering was water vapor. All corrections quoted a 0.4 s uncertainty stated to be due to the location of the measurement devices. Serebrov et al. [6] corrected for this effect by measuring the storage time of the trap at two pressures $P=3.8 \times 10^{-6}$ and $P=6 \times 10^{-4}$ torr, and the loss rate $\tau_{g}^{-1} \propto P$ was determined the difference between from these two measurements, giving a $0.4 \pm 0.024$ correction to the measurement of the neutron lifetime. However, the size of the correction and its uncertainty are expected to depend strongly on the species of residual gas and stability of vacuum conditions. These various approaches motivate the measurements shown here, as they can be used to place limits on the amount of these gases that can be tolerated in our system to meet the goal of a measurement with sub 1-second accuracy.

The thermal and cold neutron total cross sections for scattering from gases have been the subject of earlier investigations for molecular [7] [8] and noble gases [9] and found in agreement with theoretical expectations. Recently the ultracold neutron scattering cross section for deuterium gas was measured[10] for better understanding of the mechanism of ultracold neutron production in gases, liquids and solids. Figure 1 presents a spectrum from a residual gas analyzer connected to the vacuum system of our neutron trap. The dominant contaminants in our system were water vapor (including both $\mathrm{H}_{2} \mathrm{O}$ and OH ), $\mathrm{N}_{2}$ and $\mathrm{O}_{2}$. Hydrocarbon gases that are frequently used as detector gases are potential contaminants. For the measurements presented here, we chose a set of gases that included potential contaminants and spanned a range of mass. The molecular gases are of interest both as potential contaminants and also to test theoretical predictions. [11-13] We further chose a set of Noble gases whose cross sections should be straightforward to calculate and therefore could be used as a test of our experimental method.

In subsequent sections we describe our UCN measurements.

## II. DESCRIPTION OF EXPERIMENT

The experimental configuration is shown in Figure 2. UCN enter from the UCN source[2] (left). The experimental set-up contained three detectors: a ${ }^{3} \mathrm{He}$ filled multi-wire proportional chamber to provide a relative UCN fluence monitor [14] ( $M$ in Fig. 2), a commercial High Purity Germanium gamma ray detector (HPGe in Fig. 2), and a ${ }^{3} \mathrm{He}$-filled drift tube neutron detector (HE in Fig. 1). The UCN pass through a gate valve (GV, open for these measurements) and a 6 T solenoidal
polarizing magnet ( P ). A curved, electropolished stainless steel guide elbow ( 7.6 cm in diameter with a 30.5 cm bending radius) leads downward to a cylindrical gas cell (G). The vertical distance from the center of the main beamline guide to the entrance of the gas cell is 1 m . The gas cell is 7.6 cm long by 7.6 cm in diameter with a 0.127 mm aluminum window separating the cell from the guide system. This cell was developed as a detector for UCN and it was lined with a thin layer of ${ }^{10}$ B. [15] Here, instead of being used as a detector, the cell was used as a neutron-absorbing and scattering cell to hold the gases to be studied (the target). The cell was filled with different gas species, and each was measured over a range of pressures $0<P<1000 \mathrm{mbar}$. The temperature was $25 \pm 1$ C over the course of the experiment.

In the cell, neutrons that reach the wall without being upscattered have a high probability (near $100 \%$ ) of being captured via ${ }^{10} \mathrm{~B}(\mathrm{n}, \alpha)^{7} \mathrm{Li}^{*}$. This reaction results in a prompt 0.478 MeV decay $\gamma$-ray with a probability of $94 \%$. The detector $H P G e$ is used to detect this $\gamma$-ray; a spectrum is shown in Figure 3. The attenuation of the ${ }^{10} \mathrm{~B}$ capture signal by the gas is readily apparent. Upscattered neutrons can also interact with material, generating $\gamma$-rays that subsequently generate a signal in this detector through Compton scattering; this results in the increased background visible above the 0.511 MeV peak in the measurement at a pressure of 821 mb .

Upscattered UCN were directly detected in detector $H E$. This detector is a 5 cm diameter, 31.8 cm drift tube filled with 1.8 bar of ${ }^{3} \mathrm{He}$. Spectra from this neutron detector are shown in Figure 4. The counts at low pulse height in Figure 4 are due to neutrons that capture near the walls of the drift tube, for which only part of the full energy contained in the proton and triton from ${ }^{3} \mathrm{He}$ plus a neutron is detected.

For these measurements, the source was operated in a pulsed mode, with a pulse chain occurring every 5 seconds (see ref. [2] for a detailed description of the source operation). The UCN are extracted from the source through the bulk shielding using a transfer line with a chicane into the very low background experimental area. This results in many bounces as the UCN pass through the guide and thus provides very effective filtering of the neutron velocity spectrum. The neutron potential of the stainless steel guides ( 189 neV ) corresponds to a maximum $609 \mathrm{~cm} / \mathrm{sec}$ velocity for neutrons incident normally. There are few neutrons above this energy. Spectra were calculated using the Monte Carlo code "UCN"[16], yielding an average velocity at beam height outside the bulk shield of $486 \mathrm{~cm} / \mathrm{sec}$. The benchmark simulations presented in Reference 2 have established the validity of this code. Calculated spectra for neutrons inside the solid ${ }^{2} \mathrm{H}\left(\mathrm{SD}_{2}\right)$ volume in which they are produced, neutrons at beam height, and neutrons after dropping the 1 m into the gas cell are plotted in Figure 5. Data were acquired for 500 seconds at each pressure, and the monitor detector ( M ) was used to normalize each measurement. No appreciable background is observed in this detector, and the monitoring rate is not affected by the presence of gas in the cell. The UCN source was stable within the statistical sensitivity of these measurements.

## Data Analysis

## Model

Each detector measured a quantity sensitive to the upscattering cross section: the HPGe was primarily sensitive to the UCN that did not interact in the gas, while the He neutron detector was sensitive only to those UCN that did upscatter in the gas.

The yield of upscattered neutrons measured in the upscattered neutron detector was normalized to the counts in a detector (M) located near the gate valve ( $N_{G V}$ ). Backgroundsubtracted yields were calculated by subtracting the yield obtained combining target empty runs that were taken just before and just after the gas sample measurements. In the hypothetical case of a well defined path length and single neutron energy, yields can be connected to upscattering cross section via:

$$
\begin{equation*}
Y_{\exp }(P)=\frac{\sigma_{u p}}{\sigma_{T}} F \Omega \varepsilon\left[1-\exp \left(-\rho_{\text {volume }} \sigma_{T} l\right)\right] \tag{1}
\end{equation*}
$$

Here $l$ is the cell thickness, $\Omega$ is the solid angle of the neutron detector, $\varepsilon$ is the detection efficiency for the neutron detector $H E$, and $F$ is the neutron fluence $\varphi_{n}$ per count $N_{G V}$ in the beam monitor detector M:

$$
\begin{equation*}
F=\frac{\varphi_{\text {neutron }}}{N_{G V}} \tag{2}
\end{equation*}
$$

and

$$
\begin{equation*}
\sigma_{T}=\sigma_{\text {absorption }}+\sigma_{u p} \tag{3}
\end{equation*}
$$

where $\rho_{\text {volume }}$ is the number density of the target gas for a gas temperature of 25 C is given by:

$$
\begin{equation*}
\rho_{\text {volume }}=2.43 \cdot 10^{16} \cdot P(\text { mbar })\left(\frac{\text { atoms }}{\mathrm{cm}^{3} \mathrm{mbar}}\right) \tag{3}
\end{equation*}
$$

The detection efficiency $\varepsilon$ includes the efficiency of the neutron detector $H E$ itself and the attenuation due to absorption of the upscattered neutrons in the stainless steel wall of the gas cell and in the ${ }^{10} \mathrm{~B}$ coating on the cell. All these factors depend on the energy of the upscattered neutrons. This energy was not measured and is expected to be different for each gas sample. The neutron detector data also requires a normalization of the flux-solid angle product $F \Omega$.

The transmission ratio at pressure $P$ is defined in terms of the yield of 478 keV gamma rays $Y_{\gamma}(P)$ and can be written as follows:

$$
\begin{equation*}
T_{n}(P)=\frac{Y_{\gamma}(P)}{Y_{\gamma}(P=0)}=\frac{F \Omega_{\gamma} \varepsilon_{\gamma}\left[\exp \left(-\rho_{v o l} \sigma_{T} l\right)\right]}{F \Omega_{\gamma} \varepsilon_{\gamma}}=\exp \left(-\rho_{v o l} \sigma_{T} l\right) \tag{4}
\end{equation*}
$$

In this case there is no need to determine an efficiency or absolute neutron fluence normalization. For this reason, it is preferable to extract the upscattering cross section from this data if possible.

Because of the distribution of neutron energies and angles entering the cell, there is a range of different mean-free-paths for UCN within the cell. We have accounted for this using the results of the Monte Carlo Transport program "UCN" [16] which has been benchmarked previously for the characterization of the LANSCE UCN source [2]. Ultimately, the quality of the description of the transmission ratio data at high pressures is a good validation of the simulation. In the simulation performed here, neutrons are transported from the solid deuterium source to the gas cell in a simplified geometry that accounts for the velocity shift due to the $\mathrm{SD}_{2}$ potential, the UCN transport through the guide system, and transmission into the gas cell window. In this simulation the ${ }^{10} \mathrm{~B}$ coated gas cell wall was taken to be $100 \%$ absorptive for UCN. Neutrons in the volume of the gas cell are absorbed with a lifetime $\tau$, which is a variable in the simulation. To a good approximation both absorption and upscattering result in UCN lifetimes that are independent of velocity, because for both processes the first order cross sections are given by $\sigma_{0}=\sigma(v) \cdot v$ where $v$ is the UCN velocity, $\sigma(v)$ is the cross section and $\sigma_{0}$ is a constant. The lifetime is related to the total cross section:

$$
\begin{equation*}
\tau=\frac{1}{\rho \sigma_{T} v} \tag{5}
\end{equation*}
$$

where $\rho$ is the number density of the cell, given by Eqn.4. and $\sigma_{T}$ is the total cross section.
The total cross section is the sum of the upscattering cross section and the absorption cross section. The absorption cross section is taken from the thermal neutron value in the NIST tables [17] and scaled to the appropriate neutron velocity using a $1 / v$ dependence.

The average neutron velocity in the cell, $\bar{v}$, and path length to the wall, $\bar{l}$, were calculated from the Monte Carlo to be $660 \mathrm{~cm} / \mathrm{s}$ and 5.3 cm respectively. The average neutron velocity is higher than that at beam height because of the $\sim 1$ meter drop to the gas cell. From the number of neutrons interacting in the gas, $N_{i}$, and absorbing on the wall $N_{w}$, an average transmission, $T_{n}(\tau)=N_{w} /\left(N_{i}+N_{w}\right)$, was calculated for a range of values for the lifetime $\tau$. This is plotted as a function of the inverse lifetime in Figure 6. Also shown (dashed line in the figure) is a simple exponential obtained using $\bar{v}$ and $\bar{l}$ from the Monte Carlo. Although this describes the data well for long lifetimes, it fails for short lifetimes and larger attenuation because of the broad UCN spectrum incident upon the cell. To achieve a better description of the Monte Carlo results, we have fitted a three-exponential model to the transmission as shown as the solid line in figure 6:

$$
\begin{equation*}
T_{n}=a_{1} e^{-\left(k_{1} / \tau\right)}+a_{2} e^{-\left(k_{2} / \tau\right)}+a_{3} e^{-\left(k_{3} / \tau\right)} \tag{6}
\end{equation*}
$$

Here the amplitudes, $a_{1}+a_{2}+a_{3}=1$, and values of $k_{1}, k_{2}$, and $\mathrm{k}_{3}$ (where $k=l / v$ ) were chosen to give a good fit to the Monte Carlo prediction of transmission. The use of three values of $l / v$ is similar to the practice in which a limited number of neutron groups are used to approximate a complex neutron spectrum in many Monte Carlo applications.

## Fitting

The function in Eqn. 7 can be used to fit the transmission ratio $T_{n}(P)$ defined in (4) (varying the upscattering cross section, and hence $\tau$ ) measured with the HPGe $\gamma$ detector as a function of pressure to extract a $\sigma_{u p}$. The total cross section $\sigma_{T}$ is the sum of the upscattering cross section and the absorption cross section. The absorption cross section is taken from the thermal neutron value in the NIST tables [17] as described above.

The upscattered neutron yield $Y_{\text {exp }}$ data can be fitted with the following related function:

$$
\begin{equation*}
Y_{\exp }(P)=\frac{\sigma_{u p}}{\sigma_{T}} F \Omega \varepsilon\left[1-\left(a_{1} e^{-k_{1} / \tau}+a_{2} e^{-k_{2} / \tau}+a_{3} e^{-k_{3} / \tau}\right)\right] \tag{7}
\end{equation*}
$$

The lifetime $\tau$ is related to the pressure through Equation (4) and (6) with $v$ determined to be the average UCN energy $\bar{v}=660 \mathrm{~cm} / \mathrm{sec}$.

The detection efficiency in detector HE is given by:

$$
\begin{equation*}
\varepsilon=\varepsilon_{3 H e} \cdot T_{B} \cdot T_{S S} \tag{8}
\end{equation*}
$$

$T_{B}$ is the transmission through the ${ }^{10} \mathrm{~B}$ layer and $T_{S S}$ is the transmission through the stainless steel walls of the gas cell. The neutron detector efficiency as a function of neutron energy was taken from a calculation using the LANL MCNP code[18] that modeled the detector. The transmissions though the boron and stainless were calculated from the NIST thermal neutron cross section tables [17], scaled to the expected upscattered energy using the expected $1 / v$ dependence. For stainless, the atomic composition of 304 stainless was used to calculate a stainless cross section from the atomic cross sections in the NIST table. The thickness of the stainless steel was fixed at the known value. The ${ }^{10} \mathrm{~B}$ was applied by a sprayed on powder coating, with thickness estimated[15] to be $1.5 \pm 0.5 \mu \mathrm{~m}$. We let the ${ }^{10} \mathrm{~B}$ thickness be a variable parameter in our fits. Note that the upscattering cross sections extracted from the transmission ratio data are relatively insensitive to the ${ }^{10} \mathrm{~B}$ thickness because it impacts only the contributions of the upscattered neutrons to the transmission data described below. UCN interacting with the ${ }^{10} \mathrm{~B}$ are $100 \%$ absorbed for any reasonable values of the ${ }^{10} \mathrm{~B}$ thickness and therefore the effective target length is not impacted by the value of the ${ }^{10} \mathrm{~B}$ thickness.

We must account for the contribution to the transmission ratio $T_{n}$ from neutrons that upscatter and subsequently are captured in the ${ }^{10} \mathrm{~B}$ layer as they exit the gas cell. To model this we added a term relating the number of upscattered neutrons multiplied by $\left(1-T_{B}\right)$, the probability that an upscattered neutron is captured in the ${ }^{10} \mathrm{~B}$ layer. The resulting fitting function for the transmission ratio data is:
$T_{n}(P)=\left[a_{1} e^{-k_{1} / \tau}+a_{2} e^{-k_{2} / \tau}+a_{3} e^{-k_{3} / \tau}\right]+\left(1-T_{B}\right) \frac{\sigma_{u p}}{\sigma_{T}}\left[1-\left(a_{1} e^{-k_{1} / \tau}+a_{2} e^{-k_{2} / \tau}+a_{3} e^{-k_{3} / \tau}\right)\right]$

The fitted parameters used to describe the transmission data are the upscattering cross sections and the thickness of the ${ }^{10} \mathrm{~B}$ layer inside the gas cell. Hence, it is this data alone that is
used to determine the upscattering cross section. To describe the upscattering yield from the neutron detector, a value for the flux-solid angle must be fitted, using the cross sections and ${ }^{10} \mathrm{~B}$ thickness determined from the fits to the transmission data. As mentioned previously, the energy of the upscattered neutrons is required to determine both the neutron detector efficiency and the transmission through the ${ }^{10} \mathrm{~B}$ and stainless steel. The theoretical calculations described in section III provide a reasonable estimate for the outgoing energies for cold neutrons from upscattering from the noble gases, $\mathrm{H}_{2}$ and ${ }^{2} \mathrm{H}_{2}\left(\mathrm{D}_{2}\right)$. For $\mathrm{C}_{4} \mathrm{H}_{10}, \mathrm{CF}_{4}$, and air this energy was treated as a variable parameter. The upscattered energies are in the range of 25 meV (thermal) down to $\sim 1 \mathrm{meV}$ (for the heaviest gas Xe). The overall detection efficiency (calculated for the best-fit ${ }^{10} \mathrm{~B}$ layer thickness of 1.5 micron), $\mathrm{T}_{\mathrm{B}}, \mathrm{T}_{\mathrm{ss}}$ and the ${ }^{3} \mathrm{He}$ detector efficiency as a function of energy are plotted in Figure 7. The fitting procedure resulted in rather large upscattered energies for $\mathrm{C}_{4} \mathrm{H}_{10}, \mathrm{CF}_{4}$ and air $(25,25$, 18 meV respectively); a limit of 25 meV was imposed to avoid physically unreasonable values. It is likely that this suspiciously large value of $v$ acts to account for some inadequacy in the model for the neutron yield at the gas pressures for which most neutrons are upscattered. This could include for example, the use of only 3 neutron groups to describe the UCN spectrum or a dependence of the solid angle of the detector $H E$ on the location at which the upscattering occurs in the target.

Because of the additional uncertainties in extraction of upscattering cross sections from the direct upscattered neutron measurements, we have chosen to extract the cross sections from the transmission data only where possible. This is true for the polyatomic gases, which exhibit a significant decrease in transmission as a function of pressure. For these gases, we simultaneously fitted all transmission data, varying only the individual upscattering cross sections and the ${ }^{10} \mathrm{~B}$ layer thickness (which determines $T_{B}$ in Eqn. 9 and 10). For these gases the $\frac{\chi^{2}}{D o F} \sim 1$. We then obtained the best description possible for the direct neutron upscattering data by varying only the flux solid angle product $F \Omega$ and the upscattered energy for $\mathrm{C}_{4} \mathrm{H}_{10}, \mathrm{CF}_{4}$, and air as a consistency check. In this case, $\frac{\chi^{2}}{D o F} \sim 20$. In contrast, it is the direct neutron upscattering data that are most sensitive to the upscattering cross-sections for Ne and Ar , because those cross sections are quite small (and hence result in very little attenuation). For Xe, the transmission data are dominated by the very large absorption cross section. Therefore, for all three of these noble gas samples we fitted each upscattering cross section simultaneously to the transmission and upscattering data, while keeping $F \Omega$ and the ${ }^{10} \mathrm{~B}$ thickness fixed at the best fit values previously determined for the polyatomic gases. For these fits, $\frac{\chi^{2}}{D o F} \leq 1$.

The data and resulting fits are shown in Figures 8-11. The extracted upscattering cross sections are listed in Table I. The uncertainties in the Table include the statistical uncertainties and the uncertainty due to the fitting procedure. We made an initial estimate of the fitting uncertainties by varying the cross section to change the $\chi^{2}$ by 1 , and then scaled the resulting cross section change by the square root of the reduced $\chi^{2}$. Different approaches to the fitting resulted in extracted cross sections that were outside that estimated uncertainty. For this reason, we estimate an overall uncertainty of $20 \%$, which encompasses different indistinguishable fits. In particular, we have looked at the dependence of the extracted cross section on the ${ }^{10} \mathrm{~B}$ thickness for values between 1 and 2 microns; for this range of thickness the change in extracted cross
sections are of order $10 \%$, within the quoted $20 \%$ fitting uncertainty. Argon has smallest measured cross section in the presence of a larger absorption cross section; we increased the uncertainty to $30 \%$ to account for the range of fits that gave what appear to the eye to be equivalent fits.

In addition to the uncertainties due to statistical and fitting we have considered the following potential systematic errors: errors due to 1) uncertainty in the length of the gas cell, 2) uncertainty in the neutron velocity (and hence $1 / v$ ), and 3) the uncertainty in gas pressure. The uncertainty in the size of the gas cell is estimated to be $\sim 5 \mathrm{~mm}$, due to possible bowing of the windows. We estimate the uncertainty in velocity to be due to an uncertainty of 2 cm in the vertical drop. We have estimated a $1 \%$ uncertainty in the gas pressure. The overall systematic uncertainty is $7 \%$ - the dominant uncertainty coming from the uncertainty in the length of the gas cell. The cross sections for $\mathrm{N}_{2}$ and Air were measured in a slightly different configuration. These data require different flux normalization in the direct upscattering data; for this reason only the transmission data are presented Figure 8.

Table I: Upscattering cross sections determined in this work. Also presented are the absorption cross sections from NIST, the predicted upscattering cross section, and the lifetime correction (for a neutron lifetime of 880 sec ) of neutrons in the gas calculated in $10^{-6} \mathrm{Torr}$ of gas corresponding to the total cross section listed in the table (all cross sections scaled to $660 \mathrm{~cm} / \mathrm{sec}$ ). For $\mathrm{H}_{2}$ and $\mathrm{D}_{2}$ the measured values from ref. [7] have been scaled to our energy; for $D_{2}$ the measurements with UCN have been scaled from $20 \mathrm{~K}_{2}$ temperature. We estimated the upscattering cross section for air by scaling the results for $\mathrm{O}_{2}$ and $\mathrm{N}_{2}$ in Ref. [7] to our energies, and adding these according to the partial pressures of these gases in air.

| Molecule | $\sigma_{\text {up }}$ (this work) <br> (barns) | Scaled $\sigma_{\text {up }}$ <br> from [7] <br> and [10] | $\sigma_{\text {up }}$ <br> (Calculated) | $\sigma_{\text {absorption }}$ <br> (NIST) | $\sigma_{\text {total }}$ <br> (barns) | Correction <br> to $\tau_{\mathrm{n}}$ <br> (10.6 Torr) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{H}_{2}$ | $20,000(4,000)$ | 18,000 | 16,000 | 220 | 20,000 | 0.3 |
| $\mathrm{D}_{2}$ | $3,500(700)$ | 3,200 | 2,400 | 0.35 | 3,500 | 0.1 |
| Ne | $250(50)$ |  | 200 | 13 | 260 | 0.0 |
| Ar | $70(20)$ |  | 40 | 220 | 300 | 0.0 |
| Xe | $190(40)$ |  | 200 | 8,000 | 8,200 | 0.1 |
| $\mathrm{CF}_{4}$ | $3,300(660)$ |  |  | 14 | 3,300 | 0.1 |
| $\mathrm{C}_{4} \mathrm{H}_{10}$ | $74,000(15,000)$ | 96,000 | 87,000 | 1,100 | 75,000 | 1.2 |
| Air | $3,400(700)$ | 4,600 |  | 990 | 4,400 | 0.1 |
| $\mathrm{~N}_{2}$ | $3,000(600)$ |  | 2700 | 1,300 | 4,800 | 0.1 |

## III. THEORETICAL CONSIDERATIONS

When scattering from a monatomic gas at temperature T, energy is transferred to a cold neutron via atomic recoil, and expressions for the differential and total scattering cross sections for gases have been derived by Zemach and Glauber[19]. In the limit of low incident neutron energy (as is the case for UCN) these expressions are greatly simplified. For the total upscattering cross section of UCN, it is convenient to use expressions from Turchin[20] :

$$
\begin{equation*}
\sigma_{u p}=\sigma_{\text {free }} \frac{2}{v \sqrt{\pi}} \sqrt{\frac{2 k T}{M}}=\sigma_{\text {free }} \frac{w}{v} \tag{10}
\end{equation*}
$$

Here $\sigma_{\text {free }}$ is the total scattering cross section for a free atom at rest [21] (related to the bound cross section $\sigma_{b}$ by $\sigma_{b}=\sigma_{\text {free }}(1+m / M)^{2}, v$ is the initial neutron velocity and $w$ is the average velocity of gas atoms with mass $M$. The origin of the $1 / v$ behavior of the scattering cross-section for gases at low energy is a consequence of the folding of the constant in center of mass cross section with the Maxwell-Boltzmann velocities of the gas atoms in lab system. Defining $A=M / m$, the average energy $\mathrm{E}_{\text {avg }}$ of an upscattered UCN is:

$$
\begin{equation*}
E_{\text {avg }}=\frac{4 A k T}{(A+1)^{2}} \tag{11}
\end{equation*}
$$

This follows from the exponential dependence of the differential cross section on the neutron final energy $E$ considered, for example, in the book by Ignatovich [22]. The calculated upscattering cross sections and average energies for the noble gases are shown in Table I for an initial neutron velocity of $660 \mathrm{~cm} / \mathrm{s}$.

In the case of polyatomic gases, molecular degrees of freedom also contribute to the cross section. To predict the upscattering of UCN from molecular gases, we must in principle incorporate all translational, rotational, and vibrational motions into a calculation of the dynamical structure function for the gas species in question. In practice, the molecular species measured here are in different regimes with regard to this general prescription, and different approximations and models are therefore necessary.

A rigorous quantum mechanical treatment of slow neutron scattering from hydrogen and deuterium was performed by Young and Koppel[23]. For gas at room temperature, we can neglect the population or excitation of vibrational modes, but must incorporate the first several rotational states. Following Young and Koppel, including only the vibrational ground state and including the six lowest rotational states, we compute $\sigma_{\text {up }}$ for hydrogen and deuterium weighted by their ortho/para concentrations. We also adopt this prescription to calculate the $\mathrm{N}_{2}$ cross section. Accounting for the differences in mass, scattering length, and spin statistics, we calculate the cross section including the lowest twenty rotational transitions. The values are shown in Table I.

Due to the relatively high mass and high hydrogen content of isobutane $\left(\mathrm{C}_{4} \mathrm{H}_{10}\right)$, we use the mass-tensor approximation of Sachs and Teller[12] and the monatomic scattering law as applied by Krieger and Nelkin[13]. The mass-tensors for the constituent hydrogen atoms can be computed from the principle of reduced moments of inertia and bond structure reported in [24]. The total upscattering cross section was calculated using an effective mass for constituent H nuclei of approximately 3 amu which follows from the reduced moments of inertia due to the torsional vibration of $\mathrm{CH}_{3}$ groups in the molecule. The small rotational constant for rigid-body rotation (i.e.
using the principle moments) leads to a much larger effective mass, and smaller energy transfers which would be below our neutron detection threshold. It thus seems reasonable to rely on the reduced moments to determine the average upscattered neutron energy.

We can also estimate the polyatomic cross sections by scaling the known experimental inelastic scattering cross sections for $\mathrm{H}_{2}$ and $\mathrm{C}_{4} \mathrm{H}_{10}$ starting from 2.5 meV (the lowest energy point in Ref.[7] and using the $1 / v$ dependence. The same was performed for air using the $N_{2}$ and $O_{2}$ data from [7] and used the result to estimate the cross section for air. For $D_{2}$ gas, scattering cross sections have been measured down to UCN energies at 25 K [10], and we scale this to 300 K assuming that the cross section scales as $\sqrt{T}$. The inelastic scattering cross sections for the $\mathrm{CF}_{4}$ gas in the meV region are unknown. The estimated values for the other gases are shown in Table I. The cross section values are per one atom (noble gases) or per one molecule (others).

## IV. CONCLUSIONS

The agreement between the extracted cross sections and the predictions for these gases are quite reasonable for all gases. The calculations for Ar and $\mathrm{D}_{2}$ are somewhat lower than the measured cross sections. However, the measured upscattering cross section for $\mathrm{D}_{2}$ is in good agreement with the value scaled from [10]. This gives us confidence to the use the upscattering cross sections determined from the polyatomic gases to place limits on the contribution of upscattering from these gases to UCN losses in our lifetime measurement.

In order to make an $\sim 1$ second measurement of the lifetime one would prefer a correction of no more than .1 sec . This implies a partial pressure of a heavy hydrocarbon like $\mathrm{C}_{4} \mathrm{H}_{10}$ of no more than $10^{-7}$ mbar. The requirements for a 0.1 second measurement are even more challenging. However, the most likely contaminants have substantially smaller cross sections, and so this systematic is easily controlled for a 1 second measurement. In future experiments we will measure the upscattering cross section for water vapor. We also plan to repeat the measurements described here with multiple ${ }^{3} \mathrm{He}$ tubes at different pressures so that we can obtain an experimental estimate of the upscattered neutron velocities. In order to fully evaluate the systematics at the level needed for sub 1-second measurement of the lifetime, it will be necessary to characterize the residual gases in the UCN trap, which should be maintained at a high vacuum.

## V. REFERENCES

[1] D. J. Salvat, et al., Physical Review C 89, 052501 (2014).
[2] A. Saunders, et al., The Review of scientific instruments 84, 013304 (2013).
[3] S. Arzumanov, et al., Physics Letters B 483, 15 (2000).
[4] S. S. Arzumanov, L. N. Bondarenko, V. I. Morozov, Y. N. Panin, and S. M. Chernyavsky, Jetp Letters 95, 224 (2012).
[5] A. Pichlmaier, V. Varlamov, K. Schreckenbach, and P. Geltenbort, Physics Letters B 693, 221 (2010).
[6] A. Serebrov, et al., Physics Letters B 605, 72 (2005).
[7] E. Melkonian, Physical Review 76, 1750 (1949).
[8] G. L. Squires and A. T. Stewart, Proceedings of the Royal Society of London Series a-Mathematical and Physical Sciences 230, 19 (1955).
[9] R. Genin, H. Beil, C. Signarbieux, P. Carlos, R. Joly, and M. Ribrag, J. Phys. Radium 24, 21 (1963).
[10] F. Atchison, et al., Phys Rev Lett 95, 182502 (2005).
[11] E. P. W. Wigner, J.E., in Atomic Energy Commision Report (Oak Ridge National Laboratory, Oak Ridge, 1944).
[12] R. G. Sachs and E. Teller, Physical Review 60, 18 (1941).
[13] T. J. Krieger and M. S. Nelkin, Physical Review 106, 290 (1957).
[14] C. L. Morris, et al., Nuclear Instruments \& Methods in Physics Research Section a-Accelerators Spectrometers Detectors and Associated Equipment 599, 248 (2009).
[15] D. J. Salvat, et al., Nuclear Instruments \& Methods in Physics Research Section a-Accelerators Spectrometers Detectors and Associated Equipment 691, 109 (2012).
[16] C. L. Morris and A. Roberts, in Los Alamos National Laboratory Report (Los Alamos National Laboratory, LANL, 2014), Vol. LA-UR-14-23816.
[17] V. F. Sears, Neutron News 3, 26 (1992).
[18] J. F. Briesmeister, Version 4C, LA-13709-M, Los Alamos National Laboratory (2000).
[19] A. C. Zemach and R. J. Glauber, Physical Review 101, 118 (1956).
[20] V. F. Turchin, Slow neutrons (Israel program for scientific translations, 1965).
[21] S. F. Mughabghab, Atlas of Neutron Resonances: Resonance Parameters and Thermal Cross Sections. Z=1-100 (Elsevier, 2006).
[22] V. K. Ignatovich, The Physics of Ultracold Neutrons (Clarendon Press, Oxford, 1990).
[23] J. A. Young and J. U. Koppel, Physical Review 135, A603 (1964).
[24] S. S. Chen, R. C. Wilhoit, and B. J. Zwolinski, Journal of Physical and Chemical Reference Data 4, 859 (1975).


Figure 1: RGA spectrum. The main contaminants appear at Mass 17, 18, 28, and 32 corresponding to $\mathrm{OH}, \mathrm{H}_{2} \mathrm{O}, \mathrm{N}_{2}, \mathrm{O}_{2}$. Peaks at large mass are likely Ar (mass 40) and heavy hydrocarbons.


Figure 2: Schematic of the experimental set-up (not to scale). The curved guide is 7.6 cm diameter electropolished stainless steel with a 30.5 cm bending radius. The vertical guide is 7.6 cm electropolished stainless steel. The total distance from the center of the beam height to the cell window is 1 meter. M is a ${ }^{3} \mathrm{He}$-filled MWPC permanently installed at the UCN source, used to monitor the UCN production. G is the boron-lined gas cell. The HPGe detector is used to detect $\gamma$-rays from capture on the boron layer. " He " is the ${ }^{3} \mathrm{He}$ filled drift tube used to detect up-scattered neutrons from the cell. GV is a gate valve and $P$ is a polarizing magnet.


Figure 3: Gamma ray spectra measured for two different pressures of $\mathrm{C}_{4} \mathrm{H}_{10}$ in the cell. The dotted line corresponds to a gas target cell pressure of 821 mb ; the solid line is for an empty target. The peak labeled 0.478 MeV is from the decay of ${ }^{7} \mathrm{Li}$. The peak labeled 0.511 MeV is from pair production by room background. The larger counting rates above the 0.511 MeV peak are due to Compton $\gamma$-ray events induced by captured neutrons in the detector or surrounding materials.


Figure 4: Spectra from the upscattered neutron detector for two different pressures of $\mathrm{C}_{4} \mathrm{H}_{10}$ in the cell. The finite peak measured with the empty cell is due to the ambient thermal neutron background. The peak near channel 200 is when the energy from both the proton and triton from neutron capture on ${ }^{3} \mathrm{He}$ is deposited in the gas; the lower energy counts correspond to event for the energy is partially deposited in the wall.


Figure 5: Spectra showing number of neutrons as a function of neutron velocity generated using the Monte Carlo code UCN for neutrons inside the source solid ${ }^{2} \mathrm{H}\left(\mathrm{SD}_{2}\right)$ (circles), for neutrons at beam height near the gas cell (solid line), and inside the gas cell (dashed line).


Figure 6: Fits to the Monte Carlo data, where the points are for different UCN lifetimes in the gas cell, using a simple exponential (dotted line) and a triple exponential function (solid line).


Figure 7: The energy dependent correction (solid line) , $\varepsilon$, which is the product of the efficiency of the ${ }^{3} \mathrm{He}$ detector (dashed line), the transmission through the Boron layer in the gas cell (dot-dashed line), and transmission through the stainless steel of the gas cell (dotted line) as a function of upscattered neutron energy.


Figure 8: Transmission Ratio data and fits for the polyatomic gas samples $\mathrm{H}_{2},{ }^{2} \mathrm{H}_{2}\left(\mathrm{D}_{2}\right), \mathrm{C}_{4} \mathrm{H}_{10}, \mathrm{CF}_{4}$, $\mathrm{N}_{2}$ and air. The transmission ratio is calculated by taking the ratio of the $0.478 \mathrm{MeV} \gamma$ line with and without gas in the measurement cell.


Figure 9: Upscattering yields from ${ }^{3} \mathrm{He}$ upscattered neutron detector and fits for the polyatomic gas samples $\mathrm{H}_{2},{ }^{2} \mathrm{H}_{2}\left(\mathrm{D}_{2}\right), \mathrm{C}_{4} \mathrm{H}_{10}$, and $\mathrm{CF}_{4}$.


Figure 10: Transmission Ratio data and fits for the noble gas samples.


Figure 11: Upscattering yields from ${ }^{3} \mathrm{He}$ detector and fits for the polyatomic gas samples

