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Electron capture decay of 58-min ${}^{229}_{92}$ U and levels in ${}^{229}_{91}$ Pa

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Abstract

Electron capture decay of ²²⁹U has been investigated by measuring the γ -ray and conversion electron spectra of mass separated and unseparated ²²⁹U sources with high-resolution germanium and silicon detectors, respectively. Gamma-gamma coincidence measurements were also performed using germanium detectors. These studies provide level energies and level ordering in ²²⁹Pa. Singleparticle assignments have been made to these levels which are in agreement with the systematics in this region and also with theory. In a previous study, we reported the observation of a $5/2\pm$ parity doublet in the ²²⁹Pa ground state which is a signature of octupole deformation. The present analysis of the data still shows a splitting of 60 ± 50 eV, but with this large uncertainty the existence of the doublet is not certain.

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I. INTRODUCTION

Incipient octupole deformation was predicted in 1980 by Chasman [1] in the ground state of ²²⁹Pa. Its signature is a parity-doublet consisting of two almost degenerate states with the same spin but opposite parity, and a large octupole matrix element between the connecting states. The existence of the parity doublet in ²²⁹Pa was also found in later calculations [2]. Experiments performed [3] on the level structure of 229 Pa indicated the presence of a ground-state parity doublet. In these studies the 231 Pa(p,t) reaction was used to determine the excitation energy of the I, $K^{\pi} = 3/2, 1/2^{-530}$ single-particle state by measuring the energies of the outgoing tritons with a magnetic spectrometer. [Note that the use of Nilsson quantum numbers is not strictly appropriate when there is strong octupole correlation or octupole deformation in the nucleus. These quantum numbers should be understood as signifying the main single-particle component of the wavefunction.] The 231 Pa(p,t) reaction gave the energy of the $3/2, 1/2^-$ level as 128 ± 15 keV. In the electron capture (EC) decay of ²²⁹U, we observed a strong 122.5-keV M1 transition, suggesting a level at 122.5 keV. Since the two energies are close, the 122.5-keV level was identified as the same state as populated in the (p,t) reaction and was given the $3/2, 1/2^{-}[530]$ assignment. The ground state of ²²⁹Pa was established [4] as $5/2^+$ [642] on the basis of its EC and α decay. The M1 character of the 122.5-keV transition indicates a negative parity state near ground, which we assigned to the $5/2^{-1}$ Nilsson state, establishing a parity doublet. The energy difference between the $5/2^-$ and the $5/2^+$ states was deduced from closed cycles of γ rays as 150 ± 100 eV.

The experiment in Ref. [3] was performed using the Argonne FN tandem Van de Graaff accelerator and the Enge split-pole magnetic spectrometer, measuring absolute energies of the outgoing tritons from the ²³¹Pa(p,t) reaction. Later, several careful experiments were performed at other laboratories to deduce the level structure of ²²⁹Pa. In one experiment [5], the energies of tritons from the ²³¹Pa(p,t) reaction were measured with a Q3D magnetic spectrometer which gave the energies of the members of the $1/2^{-}$ [530] band directly. The Qvalue to the $3/2^{-}$ level in ²²⁹Pa was measured as -4145±3 keV and the Q-value between the ground states was calculated from known atomic masses [6] as -4126±9 keV. The difference of the two Q-values gave an excitation energy of 19 ± 9 keV for the $3/2^{-}$ state. Using the recent mass table [7], we calculate the Q value between the ground states as -4133 keV, which gives an excitation energy 12 ± 5 keV for the $3/2^{-}$ level in ²²⁹Pa. In other experiments [8, 9], γ rays from the ²³¹Pa(p,t γ) and ²³⁰Th(p,2n γ) reactions were measured. These measurements gave the same level scheme as in Ref. [3] but the levels were given different single-particle assignments. The excitation energy of the 3/2,1/2⁻[530] state was measured [10] directly by particle-gamma coincidence using the ²³¹Pa(p,t γ) reaction. An 11.6 ±0.3-keV γ ray was observed in coincidence with the tritons which was absent in the spectrum gated by protons or deuterons. This γ ray was assigned to the 1/2,3/2⁻ \rightarrow 5/2,5/2⁺ decay with an E1 multipolarity. In our experiments we do not see any γ ray or a difference between two γ rays of this energy. However, we observe several pairs of γ rays with an energy difference of 12.20±0.04 keV.

The measured value of 19 ± 9 keV for the $3/2, 1/2^{-530}$ level in Ref. [5] is clearly in disagreement with the value of 128 ± 15 keV reported in Ref. [3]. Although we could not find any error in our (p,t) reaction measurements, it is possible that the calibration of the spectrometer changed before the time of the (p,t) reaction measurement. During the investigation of the 229 Pa level scheme in 1982, a large set of data was collected on the decay properties of ²²⁹U which did not fit in the level scheme proposed in Ref. [3]. These data included measurements of higher-energy γ rays, electron spectra in coincidence with Pa K x rays, and γ - γ coincidence measurements. All these spectra have now been analyzed in detail and have been used to construct a new level scheme for ²²⁹Pa. By removing the constraint of the assignment of the $3/2, 1/2^{-530}$ configuration to the 122.71-keV level in Ref. [3], we have been able to construct a new reasonable level scheme which includes the original level scheme but with different spin-parity assignments. We still find a positive number in the 211.06-(122.52+88.43) closed cycle but detailed analysis shows that the 211.06-keV γ ray is a doublet. One component is the (122.52+88.43) -0.0 = 210.95 keV γ ray and the other component is the 241.80 - 30.67 = 211.13 keV γ ray. The measured energy of 211.06 keV represents the energy of the mixed peak. Hence, this closed cycle can not be used to determine the energy of the $5/2^{-}$ level. However, the 241.84-(122.52+119.26) = 60 ± 50 eV closed cycle still gives a positive difference.

The level scheme of ²²⁹Pa is best studied by measuring the radiations associated with the EC decay of the 58-min ²²⁹U as was done in Ref. [3]. However, it is quite difficult to produce sufficient quantity of mass-separated ²²⁹U because of the safety issues associated with radioactive targets. For this reason, no measurement on the ²²⁹U EC decay has been published since our experiments in 1980s. In this article we present new experimental results on the ²²⁹U EC decay which are quite extensive and well established.

II. SOURCE PREPARATION

The nuclide ²²⁹U was produced by the ²²⁹Th(⁴He,4n) and ²³⁰Th(³He,4n) reactions. Milligram quantities of Th targets were irradiated with microampere currents of ⁴He and ³He ions at the Argonne 152-cm cyclotron. The uranium produced in the reaction was chemically isolated and run through the Argonne electromagnetic isotope separator [11]. For some measurements, where a large quantity of ²²⁹U was needed, the chemically purified uranium fraction without mass separation was used. These sources had ²³⁰Th and Pa isotopes as impurities because these elements could not be completely removed from the source due to the fast chemical separation needed for the short-lived ²²⁹U. Mass separation reduced the ²²⁹U activity produced at the end of irradiation by a factor of 100; a factor of 10 due to the ~10% isotope separator efficiency and a factor of ~8 due to the decay.

III. EXPERIMENTAL METHODS AND RESULTS

A. γ -ray spectroscopy

Gamma rays in the EC decay of ²²⁹U were measured with a 5-cm²×10-mm low energy photon spectrometer (LEPS) and a 15% coaxial Ge(Li) detector, both placed in a very low-background shield. Both, mass separated and unseparated ²²⁹U sources were used in these studies. The LEPS detector had a resolution [full width at half maximum (FWHM)] of 600 eV at 122-keV energy. With this resolution, energies of low-energy strong γ rays were measured with an accuracy of ±10 eV. In the measurement before the publication of our article [3], we did not make efforts to achieve high precision in γ -ray energies. It was during the data analysis that it was realized that a parity doublet energy of 0.2 keV could be derived from closed cycles of γ rays. We, therefore, analyzed the γ -ray spectra more carefully later and determined the energies with higher precision. We checked the precision of our measurement by comparing the energies of Pa K x-ray lines with the precise energies measured with a curved crystal spectrometer [12]. We find that the difference between our measured K x-ray energies and those listed in the literature is, on the average, less than 10 eV. For all the well defined lines below 250 keV, the uncertainties are less than 40 eV.

Several γ -ray spectra of mass-separated and unseparated ²²⁹U sources were used to determine energies and intensities. A γ -ray spectrum measured with the 5-cm²×10-mm LEPS detector is shown in Fig. 1. The source for this spectrum was chemically purified after the mass separation. In this spectrum, in addition to the Pa K x-ray lines, Pa K x ray-Pa K x ray sum peaks are present. This shows that the ²²⁹U decay generates large intensities of K conversion electrons which cause the production of Pa K x rays. Additional evidence for their being sum peaks comes from the fact that the intensities of these peaks relative to that of the $K_{\alpha 1}$ peak are smaller in the spectrum measured with the more efficient 15% Ge(Li) detector than those obtained from the spectrum measured with the LEPS detector. A spectrum of an unseparated ²²⁹U source measured with the 15% Ge(Li) detector is displayed in Fig. 2. This spectrum has much higher counts in the peaks than the spectrum measured with the LEPS detector and was used to determine the energies of weaker transitions and higher energy γ rays. There are several γ rays with energies around 240 keV. These γ rays are better resolved in the spectrum measured with the LEPS detector, shown in Fig. 3. The uncertainties in the energies of γ rays measured with the LEPS detector are between 20-40 eV and those measured with the Ge(Li) detector are between 50 and 300 eV. The γ -ray singles spectra also contained γ rays from the ²²⁹U decay products. Gamma rays from the EC decay daughter ²²⁹Pa (1.5 d) have been studied in Ref. [4] and are too weak to be observed in the measured spectra. Gamma rays in the decay of the α -decay daughter ²²⁵Th (8.72 min) and the granddaughter ²²¹Ra (28 s) have been reported in Ref. [13]. Gamma rays were assigned to the ²²⁹U EC decay on the basis of their presence in the spectrum of a mass-separated $^{229}\mathrm{U}$ source, their presence in the spectrum measured in coincidence with Pa K x rays, and their half-lives, and in Tables I and II, they are denoted by the letters m, c, and d, respectively. For some very weak γ rays, listed at the end of Table I, half-lives could not be determined. They may belong to the ²²⁹U EC decay because they did decay with a short half-life of ~ 1 hour.

The energies of the ²²⁹Pa γ rays in keV produced in the EC decay of ²²⁹U and their intensities in % per ²²⁹U EC decay are given in Table I. Absolute intensities were obtained by normalizing the sum of all EC decays to 100%. These intensities depend on the assumed multipolarities of transitions and thus on the spin-parity assignments to the ²²⁹Pa levels. Gamma rays associated with the decays of ²²⁵Th and ²²¹Ra are listed in Table II. Those γ rays were not present in the spectrum measured in coincidence with Pa K x rays indicating that they do not belong to the EC decay of 229 U. The energies and intensities of these γ rays are in excellent agreement with the published values [13].

B. γ - γ coincidence measurements

A γ - γ coincidence measurement was performed with an unseparated ²²⁹U source, and a 5-cm²×10-mm and a 20% LEPS detectors. The coincidence events were recorded in eventby-event mode and γ -ray spectra were later generated by gating on γ -ray peaks. A γ -ray spectrum produced by placing the gate on the Pa K x rays is displayed in Fig. 4. In this spectrum, K x ray-K x ray sum peaks are absent and hence peaks near 200 keV can be easily identified. Also, the Th K x rays from ²²⁹Pa EC decay, and the γ rays following the α decays of ²²⁹U and its daughters are absent in this spectrum. Since most of ²²⁹U γ rays have low intensities, only strong γ rays were seen in the gated spectra.

C. Electron spectroscopy

Internal conversion electron lines in the EC decay of ²²⁹U have low intensities; the strongest line (122.5 L₁ line) has an intensity of only 5.5% per ²²⁹U EC decay. The source activity at the beginning of the measurement was only ~0.5% of the original activity at the end of the irradiation due to the mass separation and the time required to cool the Si(Li) detector. Hence, only strong transitions were observed in the electron spectrum. An advantage of using electron spectra is that, because the γ -ray energies are known, energies of their conversion electron lines are also known. Thus, one knows where to look for the peaks in the spectrum and consequently, even the limit on the intensity can be used to determine the transition multipolarity. The conversion-electron spectrum of a mass-separated ²²⁹U source was measured with a cooled Si(Li) detector [14] and the γ -ray spectrum of the same source was measured with a LEPS detector. The conversion coefficients of strong transitions in ²²⁹U EC decay were determined by using a ⁵⁷Co source as a standard whose electron and γ -ray spectra were measured with the same detectors and at the same solid angles as the ²²⁹U source.

Th electron singles spectrum was also measured with an unseparated 229 U source. This source had an order of magnitude more 229 U activity than the mass-separated source but it contained impurities as mentioned earlier. Electron lines belonging to ²²⁹U decay were identified by using a spectrum obtained by subtracting a later spectrum from an early one. This difference spectrum, shown in Fig. 5, contains only lines which have decayed in the 3hour time interval between the measurements of the two spectra. Although the 198.8 K and 122.5 L lines stand out, the rest of the spectrum is quite complex. The region between 86 and 100 keV contains K x rays. The Si(Li) detector has ~1 % efficiency for 100-keV photons and the electrons at this energy lose ~ 2 keV in the source and the detector window. For this reason, K x-ray peak energies were ~2 keV higher than their real values relative to the electron energy. Th 98.0-keV peak which has the right energy for the 211.0 K electron line also has the correct energy for the Pa $K_{\alpha 1}$ peak. Since we could not determine the contribution of the K x ray component to the peak counts, the 98.0-keV peak was not used for the determination of the conversion coefficient.

In the spectrum shown in Fig. 5(b), the 246.0 K line of ²²¹Ra and the 149.1 L and M lines of ²¹⁷Rn are clearly visible. The multipolarities of these transitions are known [13] to be M1 and E2, respectively. As Fig. 3 shows, the 240.50-, 241.84-, and 247.80-keV γ rays have higher intensities than the 246.02-keV γ ray. Hence, if these transitions were M1, we would see their K electron lines as intense as the 246.0 K line. We do not see the K lines of these γ rays which indicates that these are not M1 transitions. They could have E1 or E2 multipolarity. In heavy nuclei, E2 transitions between single-particle states are slower than E1 transitions. Hence, we assign E1 multipolarity to the 240.50-, 241.84, and 247.80-keV transitions.

The electron spectrum of a mass-separated ²²⁹U source was also measured in coincidence with Pa K α x rays which is displayed in Fig. 6. Although this spectrum has low counts, it is very clean and all strong ²²⁹U electron lines seen in the singles spectrum are clearly visible. The intensities obtained from this spectrum have larger uncertainties but they agree with the values obtained from the singles spectrum. The 98.0-keV line, seen in the singles electron spectrum, is present in this spectrum also, but as mentioned earlier we can not use it to determine the multipolarity of the 211.0-keV transition because it contains Pa K x-ray line. There is an electron line at 89.8 keV in the spectrum which is assigned to the 110.9-keV transition between the 210.95 and 100.1 keV levels. This γ ray is masked by the Pa K_{β2} line and hence its intensity was not measured. The electron intensities from all these spectra and conversion coefficients deduced from them are given in Table III along with the theoretical conversion coefficients [15]. From the upper limit on the intensities of electron lines we deduce the multipolarity of 66.24- and 88.43-keV transitions as E1. Also included in the Table are electron intensities and conversion coefficients for transitions in the α decays of ²²⁵Th and ²²¹Ra, and these are in agreement with literature values [13]. These electron intensities are normalized to the intensity of the 321.35-keV γ ray as 100.

IV. DISCUSSION

A. Level scheme

In electron capture or β^- decay, level energies in the daughter nucleus are deduced from sums and differences of energies of the observed γ -ray transitions. In the absence of coincidence and transition multipolarity information, different level sequences can be postulated as was done by us [3, 16]. However, with γ - γ coincidence information, one can generally determine the correct level orderings. We have used the criterion that an energy level is established only when two observed γ rays are associated with that level, either deexciting it or populating it.

By balancing the total EC, γ -ray, and internal conversion electron intensities feeding each level, and the γ -ray and conversion electron intensities deexciting it, we determine $40\pm3\%$ EC population to the ²²⁹Pa ground state and nearby states. Using the measured M1 multipolarity for the 122.52-keV transition, we deduce its transition intensity as $32\pm3\%$, which leaves only 28% intensity for the remaining γ rays. The γ -ray transitions in coincidence with the 122.52-keV γ ray have total intensity of < 5% and hence the 122.52-keV transition must decay to the ground state or to a nearby state. We interpret the 122.52-keV γ ray deexciting a 122.52-keV level to the ground state because, as we show later, with this assignment all γ -ray transitions fit in a level scheme. In coincidence with the 122.52-keV γ ray, we observe 88.43- and 119.26-keV γ rays establishing levels at 210.95 and 241.80 keV, shown in Fig. 7. A gate placed on the 88.43-keV peak shows the presence of the 122.52- and a 247.80-keV γ ray, indicating that the 210.95-keV level is fed by a 247.80-keV γ -ray transition. In coincidence with the 241.84-keV γ ray we observe a 216.90-keV γ ray, suggesting that the 241.80-keV level is populated by a 216.90-keV γ ray. By gating on the 247.80-keV γ -ray peak, we observe 66.24, 88.43-, 198.77-keV, and 211.06-keV γ rays. By placing a gate on the 66.24-keV γ -ray peak we observe 114.03-, 132.52-, 144.70-, and 247.80-keV γ rays. Since the 66.24-keV γ ray originates at the 210.95-keV level, these coincidence γ rays define levels at 144.70, 12.20, and 30.67 keV. The presence of the 12.20-keV level is further supported by the observation of other pairs of γ rays with this energy difference. Thus, the coincidence measurements establish levels at 0.0, 12.20, 30.67, 122.52, 144.70, 210.95, 241.80, and 458.75 keV.

B. Spin-parity and configuration assignment

The ground-state spin of ²²⁹Pa has been established as 5/2 on the basis of its EC and α decay [4], and the β^- decay of ²²⁵Ra. The log ft values of ²²⁹Pa EC transitions and the level spacings in the rotational bands of ²²⁵Ac favor a $5/2^+$ [642] assignment. However, the $5/2^-$ [523] single-particle assignment is also possible.

The ground-state spin of ²²⁹U is most likely 3/2, with the configuration $3/2^+[631]$ as determined from its α decay [13, 17]. Since $\Delta K=0, \pm 1$ and $\Delta I=0, \pm 1$ EC transitions have the highest decay rates, only states with spin 1/2, 3/2, and 5/2 in ²²⁹Pa are expected to receive measurable EC population. The decay data establish a level at 12.20 keV. We assign it to the $3/2,1/2^-[530]$ configuration because this energy is very close to the energy of 12 ± 5 keV measured by the ²³¹Pa(p,t) reaction [5] and theory [1] predicts its 1/2 member at 40 keV. The 3/2 - 1/2 and 5/2 - 3/2 energy differences for this band were measured as 15.1 ± 0.4 keV and 87.7 ± 0.3 keV in the (p,t) reaction [8]. From the decay of the $1/2^+$ and $3/2^+$ states at 252.7 and 304.7 keV (Fig. 8), we deduce these energy differences as 14.5 ± 0.1 and 87.9 ± 0.1 keV, respectively, in excellent agreement with the (p,t) reaction data.

Coincidence relationship establishes a level at 210.95 keV which decays to the 12.20keV level by a 198.77-keV M1 transition. Thus the parity of the 210.95-keV level must be negative. We assign a $3/2^-$ spin-parity to this state and a configuration of $3/2^-$ [532]. The 241.80-keV level is interpreted as the $5/2^-$ member of this band because of the similarity of the level spacing in this band to the spacing in the $3/2^-$ band of ²²⁵Ac [4] and ²³¹Pa [18]. The 210.95-keV level decays to the 122.52- and 144.70-keV levels by 88.43- and 66.24-keV E1 transitions, respectively and hence these two states should have positive parity. We tentatively assign these levels to the 3/2 and 5/2 members of the $3/2^+$ [651] band. The level spacing in this band is comparable to the spacing in the $3/2^+$ band in ²²⁵Ac. The M1 multipolarity of the 122.52- and 144.70-keV transitions establishes positive parity for the ground state and we assign it to the $5/2^{+}[642]$ single-particle configuration.

The 30.67-keV level, populated by the 114.03-keV γ ray, could be either the 5/2^{-[523]} single-particle state or the $7/2^+$ member of the ground-state band. The latter assignment is more likely because this level is expected around this energy and the intensity of the 114.03keV γ ray is in agreement with the value calculated by the Alaga rules [19]. A measurement of the 114.03-keV transition multipolarity is needed to confirm this assignment. The transition energy from the 241.80-keV to the 30.67-keV level is 211.13 keV whereas the energy from the 210.95-keV level to the ground state is 210.95 keV. These two γ rays are indistinguishable and the 211.06-keV peak in the γ singles spectrum contains both transitions. The contribution from each transition was determined from the coincidence data. In Fig. 9, are shown two spectra gated by the 198.77- and 211.06-keV γ rays. The spectra have large amount of Pa K x rays because the detector efficiency at the K x-ray energy is ~ 4 times the efficiency at 200 keV and the background spectrum was not subtracted. If there were only one γ -ray transition of 210.95 keV, both spectra would be identical because both, the 198.77- and 210.95-keV γ rays originate at a common level at 210.95 keV. However, the two spectra are quite different. The data show that $\sim 70\%$ of the 211.06-keV peak counts arise from the decay of the 241.80-keV level. For this reason the measured energy of the γ -ray peak in the spectrum is higher than 210.95 keV, giving the positive number in the $211.06 \cdot (122.52 + 88.43)$ cycle.

Other levels are deduced from the γ - γ coincidence measurements and γ rays listed in Table I. In coincidence with the 88.43-keV peak we observe 247.80-, 279.1- and 350.80-keV γ rays which require levels at 458.75, 490.05, and 561.72 keV. The multipolarity of the 247.80-keV γ ray has been measured as E1 and hence, the 458.75-keV level should have positive parity. We assign 458.75- and 490.05- keV levels to the 3/2 and 5/2 members of the 3/2⁺[402] band which is calculated [1] to be at 460 keV. The 561.72-keV level is given a tentative assignment of the 3/2⁻[521] particle state because this level was observed in ²³¹Pa [20] at 604 keV. The 1/2⁺[400] state, which is predicted [1] to be at 200 keV, was observed by Levon *et al.* [8] at 240.3±0.5 keV relative to the energy of the 1/2,3/2⁻ level and its 3/2 and 5/2 members were identified at 291.4±0.3 and 272.5±0.3 keV. We have observed a 240.50-keV γ ray which gives the energy of the 1/2⁺ level as 252.7 keV. A 226.00-keV γ ray is observed which is interpreted as the 252.7→26.7 transition, the 26.7-keV level being the 1/2 member of the 1/2⁻[530] band. Three γ rays of energy 204.60, 278.0, and 292.8 keV define a level at 304.7 keV, which is interpreted as the 3/2⁺ member of the 1/2⁺[400] band. Also, a weak 273.5-keV γ ray was observed which has been assigned to the 285.7 \rightarrow 12.2 decay, the 285.7-keV level being the 5/2⁺ member of the 1/2⁺[400] band. The measured E1 multipolarity of the 240.50-keV transition further supports this assignment.

A level at 745.2 keV is proposed on the basis of γ rays connecting it to lower levels. This level decays predominantly to the $1/2,3/2^-$ level at 12.20 keV and also to the $3/2^+$ and $5/2^+$ levels. This level could therefore be either 1/2 or 3/2 member of the $1/2^+$ [651] rotational band or the 0⁺ state built on the $1/2,3/2^-$ level. The β band is known in the neighboring ²²⁸Th at 832 keV [21]. Three weakly populated levels at 799.3, 884.2, and 1058.2 keV are also shown as dashed lines in the level scheme. Their tentative spins and parities are shown in the figure.

The level scheme deduced in this work is compared with the predictions of Chasman [1] in Fig. 10. The observed level ordering is, in general, in good agreement with theory, providing additional support for the proposed level scheme. The energy levels in 229 Pa are compared with the energy levels in 231 Pa in Fig. 11. Since both isotopes contain 91 protons, their level structures should be similar. However, there is big change in the two nuclei; the $5/2^+$ level drops drastically in 229 Pa indicating difference in the structures of the two nuclei, in agreement with theory.

C. Gamma-ray transition probabilities

One of the observed properties associated with octupole correlations or octupole deformation is the enhancement of E1 transition rates. Since the center of charge and the center of mass in octupole shape do not coincide, they give rise to dipole and octuple moments which result in enhanced B(E1) and B(E3) values. It has been shown in nuclei in the Z~90 region with octupole correlations that E1 rates between the members of the parity doublet are enhanced [22] over the respective values in Pu and heavier nuclei which have no octupole correlations. In nuclei with no octupole correlations, M1 transitions are found to be the fastest transitions. In ²²⁹Pa, there are several enhanced E1 transitions (see Fig. 7). The ratio of the intensities of the 88.43- and 198.77-keV γ rays indicate that the energyindependent E1 rate is 10 times the energy-independent M1 rate. Similarly the intensities of the 247.80- and 336.23-keV γ rays indicate that the E1 rate is 18 times the M1 rate. In the case of the 1/2⁺ band at 252.7 keV, we observe only E1 transitions. These enhanced E1 transition rates provide evidence for large octupole correlations in ²²⁹Pa.

According to the Alaga rules [19], relative intensities of γ rays from any level to the members of a rotational band are proportional to the squares of the appropriate Clebsch-Gordan coefficients. Using the assignments in Figs. 7 and 8, we have calculated the relative intensities of γ rays de-exciting several levels. The excellent agreement between the measured and calculated relative intensities further supports the single-particle assignments in Figs. 7 and 8.

D. Splitting energy of the $5/2\pm$ doublet

So far the $5/2^-$ member of the parity doublet has not been identified. In this work we have established many excited states which would decay to the $5/2^-$ level expected below 80 keV from the systematics. The fact that we have placed all observed transitions in the level scheme presented here, leaves no γ -ray transition which could be attributed to the decay to the $5/2^-$ level. From these observations we conclude that the $5/2^-$ level is almost degenerate with some level below 80 keV, possibly the ground state. The $5/2^{\pm}$ doublet in ²²⁹Pa was identified in Ref. [3] from two closed cycles of γ rays. One of the closed cycles, 211.09-(122.51+88.43), can not be used because the 211.06-keV γ ray is a doublet. The other closed cycle 241.84-(122.52+119.26) = 60 ± 50 eV still gives a positive number that makes $5/2^-$ the ²²⁹Pa ground state. However, the large uncertainty in the energy difference makes the assignment of the $5/2^-$ level uncertain.

E. Summary

We have presented a large set of data on the ²²⁹U EC decay which establishes a detailed level scheme for ²²⁹Pa. The decay scheme is constructed on the basis of γ - γ coincidence data and conversion electron measurements. The energy levels presented here are well supported by the data and single-particle assignments are in agreement with theoretical predictions. The fact that the 5/2⁺[642] single-particle state is the ground state in ²²⁹Pa, as predicted by theory [1], and the E1 transition rates are enhanced suggests large octupole correlations in ²²⁹Pa. The presence of large octupole correlations in ²²⁹Pa is also supported by the near equality of the decoupling parameters for the $1/2^-$ band (a = -1.63) and the $1/2^+$ band (a = +1.53) [8], as predicted by theory [2]. However, the $5/2^-$ [523] level, the other member of the parity doublet, has not been located. The data reported in this article make it possible to search for the $5/2^-$ member of the parity doublet. Since many γ rays have been shown to belong to the ²²⁹U EC decay, mass separation is not necessary for detailed spectroscopy. A ²²⁹U sample can be produced by the irradiation of a ²²⁹Th target with α particles or by the irradiation of a ²³⁰Th target with a ³He beam. Chemical purifications can produce quite pure ²²⁹U sample, free of fission products and other actinide elements. The only other uranium isotope produced in the reactions which generates γ rays is the 4.2-d ²³¹U. However, transitions in ²³¹U decay are known [23] and can be easily distinguished from ²²⁹U transitions because of their low intensities and long ²³¹U half-life. Use of high-efficiency Ge detectors can improve the γ -ray sensitivity. Measurements that can be used to determine the energy of the $5/2^{-}[523]$ level include:

a) A precise measurement of γ -ray energies with a LEPS detector or a microcalorimeter so that the energy difference between the $5/2^-$ and $5/2^+$ levels, if there is a ground-state doublet, could be measured with higher precision.

b) Measurement of electron spectrum. The multipolarity of the 114.03-keV transition will determine whether the 30.67-keV level is $7/2^+$ or $5/2^-$. The energy of the 12.2 M conversion line for M1 transition is ~0.4 keV less than for E1 multipolarity. The M1 multipolarity will provide evidence for the $5/2^-$ state near ground., The low-energy conversion electrons could be detected with a high-resolution cooled 100- μ m thick silicon detector or with a magnetic spectrometer.

c) A measurement of the lifetime of the 12.20-keV level. If a $5/2^{-}$ level is near the ground state, the lifetime of the 12.20-keV level will be short, otherwise it will be in the microsecond range.

d) Study of the α decay of the 36.2-min ²³³Np which has a small α -decay branch of ~0.001%. Even when 5/2⁺ and 5/2⁻ levels in ²²⁹Pa are degenerate, their 7/2 members will have different energies and will receive measurable α population.

ACKNOWLEDGMENTS

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TABLE I: Gamma-rays in ²²⁹Pa from EC decay of ²²⁹U measured in the present work. Letters m, c, and d indicate that the γ ray was observed in mass-separated source, in coincidence with Pa K x rays, and decayed with ~1 hour half-life, respectively.

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Energy	Intensity ^{a}	Transition	Remark
keV		Initial (keV) \rightarrow Final (keV)	
$66.24 {\pm} 0.03$	$0.58{\pm}0.07$	$210.95 {\rightarrow} 144.70$	m,c,d
$88.43 {\pm} 0.02$	$2.10 {\pm} 0.20$	$210.95 {\rightarrow} 122.52$	m,c,d
$92.28 {\pm} 0.01$	34 ± 2	Pa K α_2	m,c,d
$95.86{\pm}0.01$	53 ± 3	Pa K α_1	m,c,d
$107.59 {\pm} 0.02$	$6.2 {\pm} 0.4$	Pa K β_3	m,c,d
$108.42 {\pm} 0.02$	$12.0{\pm}0.7$	Pa K β_1	m,c,d
$111.50 {\pm} 0.02$	$4.6 {\pm} 0.3$	Pa K β_2	m,c,d
$112.37 {\pm} 0.03$	$1.8 {\pm} 0.2$	Pa $\mathrm{KO}_{2,3}$	m,c,d
$114.03 {\pm} 0.03$	$0.50 {\pm} 0.04$	$144.70 { ightarrow} 30.67$	m,c,d
$119.26 {\pm} 0.03$	$0.26 {\pm} 0.02$	$241.80 {\rightarrow} 122.52$	m,c,d
$122.52 {\pm} 0.02$	$2.60 {\pm} 0.13$	$122.52 \rightarrow 0.0$	m,c,d
$132.52{\pm}0.03$	$0.38{\pm}0.03$	$144.70 \rightarrow 12.20$	m,c,d
$144.70 {\pm} 0.03$	$0.42 {\pm} 0.03$	$144.70 \rightarrow 0.0$	m,c,d
$184.2 {\pm} 0.2$	$0.20{\pm}0.05$	$210.95 {\rightarrow} 26.7$	С
$198.77 {\pm} 0.03$	$2.30 {\pm} 0.13$	$210.95{\rightarrow}12.20$	m,c,d
$204.60 {\pm} 0.03$	$0.65{\pm}0.05$	$304.7 { ightarrow} 100.1$	m,c,d
$211.06 {\pm} 0.04$	\sim 0.13 b	$210.95 \rightarrow 0.0$	m,c,d
	~ 0.32 b	$241.80 { ightarrow} 30.67$	m,c,d
$216.90 {\pm} 0.04$	$0.65{\pm}0.05$	$458.75 \rightarrow 241.80$	m,c,d
$226.00 {\pm} 0.04$	$0.34 {\pm} 0.03$	$252.7 \rightarrow 26.7$	m,c,d
$229.60 {\pm} 0.04$	$0.26 {\pm} 0.02$	$241.80 \rightarrow 12.20$	m,c,d
$240.50 {\pm} 0.04$	$0.80{\pm}0.06$	$252.7 \rightarrow 12.20$	m,c,d
$241.84{\pm}0.04$	$0.59{\pm}0.05$	$241.80 {\rightarrow} 0.0$	m,c,d

			D1
Energy	Intensity ^a	Transition	Remark
keV		itial (keV) \rightarrow Final (ke	,
247.80 ± 0.04	$1.54 {\pm} 0.10$	$458.75 \rightarrow 210.95$	m,c,d
273.5 ± 0.2	~ 0.10	$285.7 \rightarrow 12.2$	
$278.0 {\pm} 0.1$	$0.42 {\pm} 0.04$	$304.7 \rightarrow 26.7$	m,c,d
$279.1 {\pm} 0.1$	$0.42 {\pm} 0.04$	$490.05 {\rightarrow} 210.95$	m,c,d
286.2 ± 0.1	$0.12{\pm}0.01$	$745.2 \rightarrow 458.75$	c,d
$292.8 {\pm} 0.1$	$0.15{\pm}0.02$	$304.7 \rightarrow 12.20$	$^{\rm c,d}$
$314.0 {\pm} 0.1$	$0.11{\pm}0.02$	$458.75 {\rightarrow} 144.70$	$^{\rm c,d}$
$336.23 {\pm} 0.06$	$0.22{\pm}0.02$	$458.75 {\rightarrow} 122.52$	m,c,d
$340.2{\pm}0.3$	$0.027 {\pm} 0.007$	$799.3 { ightarrow} 458.75$	
$345.2{\pm}0.1$	$0.08{\pm}0.01$	$490.05 {\rightarrow} 144.70$	d
$350.80 {\pm} 0.10$	$0.21{\pm}0.02$	$561.72 {\rightarrow} 210.95$	m,c,d
$425.7 {\pm} 0.3$	$0.12{\pm}0.012$	$884.2 \rightarrow 458.75$	d
$446.60 {\pm} 0.08$	$0.16{\pm}0.02$	$458.75 {\rightarrow} 12.20$	m,c,d
$458.82{\pm}0.10$	$0.05{\pm}0.01$	$458.75 {\rightarrow} 0.0$	
$477.89 {\pm} 0.10$	$0.05{\pm}0.01$	$490.05 {\rightarrow} 12.20$	d
$490.07 {\pm} 0.10$	$0.032{\pm}0.008$	$490.05 \rightarrow 0.0$	
$497.2 {\pm} 0.3$	$0.031 {\pm} 0.008$	$1058.2 {\rightarrow} 561.72$	
$534.3 {\pm} 0.2$	$0.04{\pm}0.01$	$745.2 \rightarrow 210.95$	d
$549.50 {\pm} 0.10$	$0.52{\pm}0.05$	$561.72 { ightarrow} 12.20$	m,c,d
$557.1 {\pm} 0.3$	$0.04{\pm}0.01$	$799.3 \rightarrow 241.80$	
$600.5{\pm}0.2$	$0.09{\pm}0.01$	$745.2 \rightarrow 144.70$	$^{\rm c,d}$
$622.6{\pm}0.2$	$0.22{\pm}0.02$	$745.2 \rightarrow 122.52$	m,c,d
$644.9 {\pm} 0.3$	$0.027 {\pm} 0.007$	$745.2 \rightarrow 100.1$	d
$654.7 {\pm} 0.3$	$0.030 {\pm} 0.008$	$799.3 \rightarrow 144.70$	
$733.0{\pm}0.2$	$1.23 {\pm} 0.10$	$745.2 \rightarrow 12.20$	m,c,d
$761.2{\pm}0.3$	$0.031 {\pm} 0.008$	$884.2 \rightarrow 122.52$	d
$787.2 {\pm} 0.3$	$0.016 {\pm} 0.003$	$799.3 \rightarrow 12.20$	

TABLE I: (continued)

Energy	Intensity ^{a}	Transition	Remark
keV		Initial (keV) \rightarrow Final (keV)	
799.6±0.3	$0.05 {\pm} 0.01$	$799.3 { ightarrow} 0.0$	d
$847.1 {\pm} 0.3$	$0.09{\pm}0.02$	$1058.2 \rightarrow 210.95$	d
884.2 ± 0.3	$0.07{\pm}0.01$	$884.2 \rightarrow 0.0$	d
$1058.6 {\pm} 0.3$	$0.06{\pm}0.01$	$1058.2 { ightarrow} 0.0$	d
$414.5{\pm}0.4$	$0.05{\pm}0.01$	not placed in level scheme	d
$433.6 {\pm} 0.4$	$0.04{\pm}0.01$	not placed in level scheme	d
$465.8 {\pm} 0.4$	$0.03 {\pm} 0.01$	not placed in level scheme	
$543.3 {\pm} 0.4$	$0.08{\pm}0.01$	not placed in level scheme	d
$552.6 {\pm} 0.4$	$0.07{\pm}0.01$	not placed in level scheme	d
$663.0 {\pm} 0.4$	$0.03 {\pm} 0.01$	not placed in level scheme	
$689.0 {\pm} 0.4$	$0.04{\pm}0.01$	not placed in level scheme	
$712.4 {\pm} 0.4$	$0.04{\pm}0.01$	not placed in level scheme	
$717.1 {\pm} 0.4$	$0.06 {\pm} 0.01$	not placed in level scheme	
$749.4 {\pm} 0.4$	$0.03 {\pm} 0.01$	not placed in level scheme	

TABLE I: (continued)

 a % per $^{229}\mathrm{U}$ EC decay.

 $^b {\rm The}$ total intensity of the 211.06-keV γ ray is 0.45±0.04 % per $^{229}{\rm U}$ EC decay.

10	decayed with ~58 mm. nan-me.							
	Energy	Intensity	Transition	Remark				
	keV		Initial (keV) \rightarrow Final (keV)					
	53.2 ± 0.1	$7.5{\pm}0.6$	$53.14 { ightarrow} 0.0$	m				
	$56.3 {\pm} 0.1$	$4.8{\pm}0.6^a$	$149.18 { ightarrow} 93.02$	217 Rn, m				
	$146.82 {\pm} 0.08$	$3.4{\pm}0.3$	$146.81 { ightarrow} 0.0$	m,d				
	$149.12 {\pm} 0.03$	35 ± 3	$149.18 { ightarrow} 0.0$	$^{217}\mathrm{Rn},\mathrm{m,d}$				
	$174.28 {\pm} 0.08$	$5.8{\pm}0.6$	$174.3 { ightarrow} 0.0$	$^{217}\mathrm{Rn},\mathrm{m,d}$				
	$177.27 {\pm} 0.08$	$4.9{\pm}0.5$	$299.16{\rightarrow}121.95$	m,d				
	$246.02 {\pm} 0.05$	18 ± 2	$299.16 {\rightarrow} 53.14$	m,d				
	$299.29 {\pm} 0.10$	$5.8{\pm}0.6$	$299.16{\rightarrow}0.0$	d				
	$305.85 {\pm} 0.08$	18 ± 2	$359.02 {\rightarrow} 53.14$	m,d				
	$321.35 {\pm} 0.08$	100 (norm)	$321.37 {\rightarrow} 0.0$	m,d				
	$359.05 {\pm} 0.08$	20 ± 2	$359.02 \rightarrow 0.0$	m,d				
	$382.00 {\pm} 0.10$	2.5 ± 0.3	$485.40 { o} 103.60$	d				
	$485.7 {\pm} 0.1$	$0.9{\pm}0.2$	$485.40 \rightarrow 0.0$					

TABLE II. ²²¹Ra γ rays from the α decay of ²²⁵Th measured in the present work. The letter m indicates that the γ ray was observed in the spectrum of a mass-separated ²²⁹U source and d denotes that it decayed with ~58 min. half-life.

 a This intensity is higher than the value given in Ref. [13].

Transition	Shell	Electron	Conversion	Theoretical	conversion	coefficient	Multipolarity
energy (keV)		intensity $(\%)$	coefficient	E1	E2	M1	
66.2	L_1+L_2	<3.0	<5	0.19	36	10.4	E1
88.4	L_1+L_2	<3.0	< 2	0.09	9.4	4.5	E1
110.9 $^{\rm a}$	L_1+L_2	~ 1.0	-	0.054	3.4	2.3	M1
122.5	L_1+L_2	$5.0{\pm}0.5$	$1.9{\pm}0.2$	0.042	2.2	1.75	M1
	$M_1 + M_2$	$1.6{\pm}0.2$	$0.6{\pm}0.1$	0.013	0.97	0.43	
	N+O	$0.30 {\pm} 0.04$	$0.12{\pm}0.02$	0.013	0.97	0.43	
144.7	Κ	$2.3 {\pm} 0.6$	5.5 ± 1.5	0.16	0.24	5.7	M1
198.8	Κ	$5.5 {\pm} 0.7$	$2.40{\pm}0.33$	0.077	0.158	2.3	M1
	L_1+L_2	$1.0{\pm}0.2$	$0.43 {\pm} 0.09$	0.013	0.28	0.44	
149.1 (221 Ra)	L_1+L_2	16 ± 4	$0.46{\pm}0.12$	0.006	0.55	0.61	E2
149.1 (221 Ra)	L_3	12 ± 3	$0.34{\pm}0.09$	0.005	0.35	0.004	E2
246.0 (225 Th)	Κ	15 ± 2	$0.83 {\pm} 0.14$	0.044	0.11	0.99	M1
$305.9~(^{225}\text{Th})$	Κ	~ 14	~ 0.8	0.027	0.068	0.64	M1
$321.4~(^{225}\text{Th})$	Κ	44 ± 5	$0.44 {\pm} 0.05$	0.025	0.062	0.47	M1
359.1 (225 Th)	Κ	~ 8	~ 0.4	0.019	0.049	0.35	M1

TABLE III. Summary of 229 Pa electron lines in the EC decay of 229 U. The high intensity of the 122.5 M line could be due to the presence of 229.60 K line.

 $^{\rm a}$ The 110.9-keV transition is 210.95 ${\rightarrow}100.1$ transition. No $\gamma\text{-ray seen.}$ FIG. 1. γ -ray spectrum of a mass-separated ²²⁹U source measured with a 5-cm²×10-mm LEPS detector. γ -ray energies in keV are indicated on the peaks. The symbol * denotes γ rays belonging to ²²⁵Th or ²²¹Ra α decay.

FIG. 2. γ -ray spectrum of an unseparated ²²⁹U source measured with a 15% Ge(Li) detector. A set of Cu and Al absorbers was used to reduce the counts in the low-energy γ -ray and x-ray peaks thus reducing γ - γ summing. γ -ray energies in keV are indicated on the peaks. Counting was started \sim 2 hours after the end of the irradiation. The symbol * denotes γ rays belonging to ²²⁵Th or ²²¹Ra α decay.

FIG. 3. γ -ray spectrum of an unseparated ²²⁹U source measured with a 5-cm²×10-mm LEPS detector showing γ rays in the 240-keV region. A set of Cu and Al absorbers was used to reduce the counts in the low-energy γ -ray and x-ray peaks thus reducing γ - γ summing. γ -ray energies in keV are indicated on the peaks. Counting was started ~2 hours after the end of the irradiation. The symbol * denotes γ ray belonging to ²²⁵Th α decay.

FIG. 4. γ -ray spectrum of an unseparated ²²⁹U source measured with a 5-cm²×10-mm LEPS detector in coincidence with Pa K α x rays. γ -ray energies in keV are indicated on the peaks. The K α x rays were detected with a 20% LEPS spectrometer.

FIG. 5. Electron spectrum of an unseparated ²²⁹U source measured with an 80-mm²×3-mm cooled Si(Li) spectrometer with a resolution(FWHM) of 1.0 keV at 100-keV electron energy. The spectrum was generated by subtracting a later spectrum from an early spectrum. Strong electron lines from ²³⁰Th and ²²⁹Pa were present in both spectra. Electron and/or transition energies in keV are indicated on the peaks. The symbol * denotes electron lines belonging to ²²⁵Th or ²²¹Ra α decay.

FIG. 6. Electron spectrum of a mass-separated ²²⁹U source measured with a cooled Si(Li) spectrometer in coincidence with Pa K α x rays. Electron and/or transition energies in keV are indicated on the peaks.

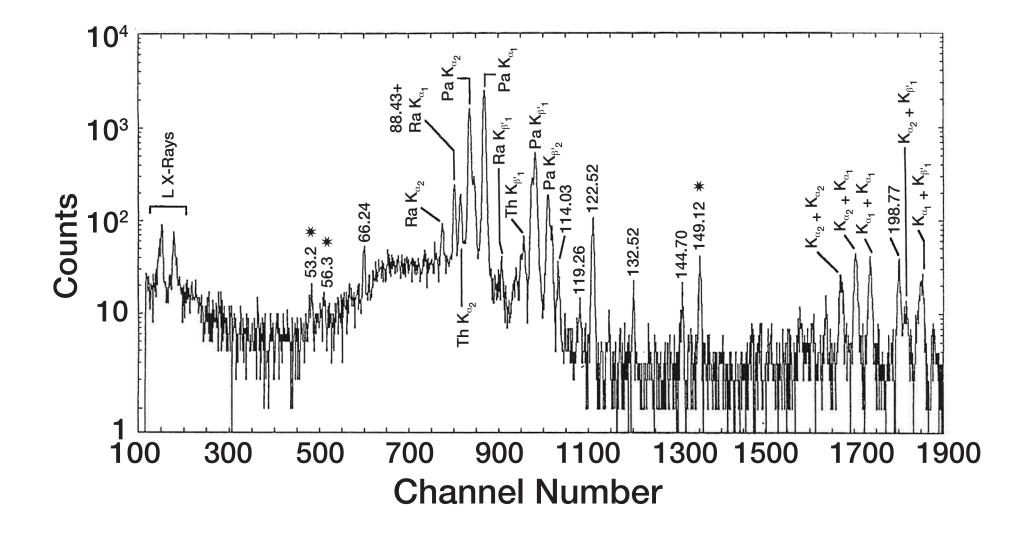
FIG. 7. (Color online) Low-energy portion of the ²²⁹Pa level scheme. γ -ray energies are given in keV and γ -ray intensities in % per ²²⁹U EC decay are given in parenthesis. The half-life in the figure was measured during the course of this work. Red lines represent the band heads.

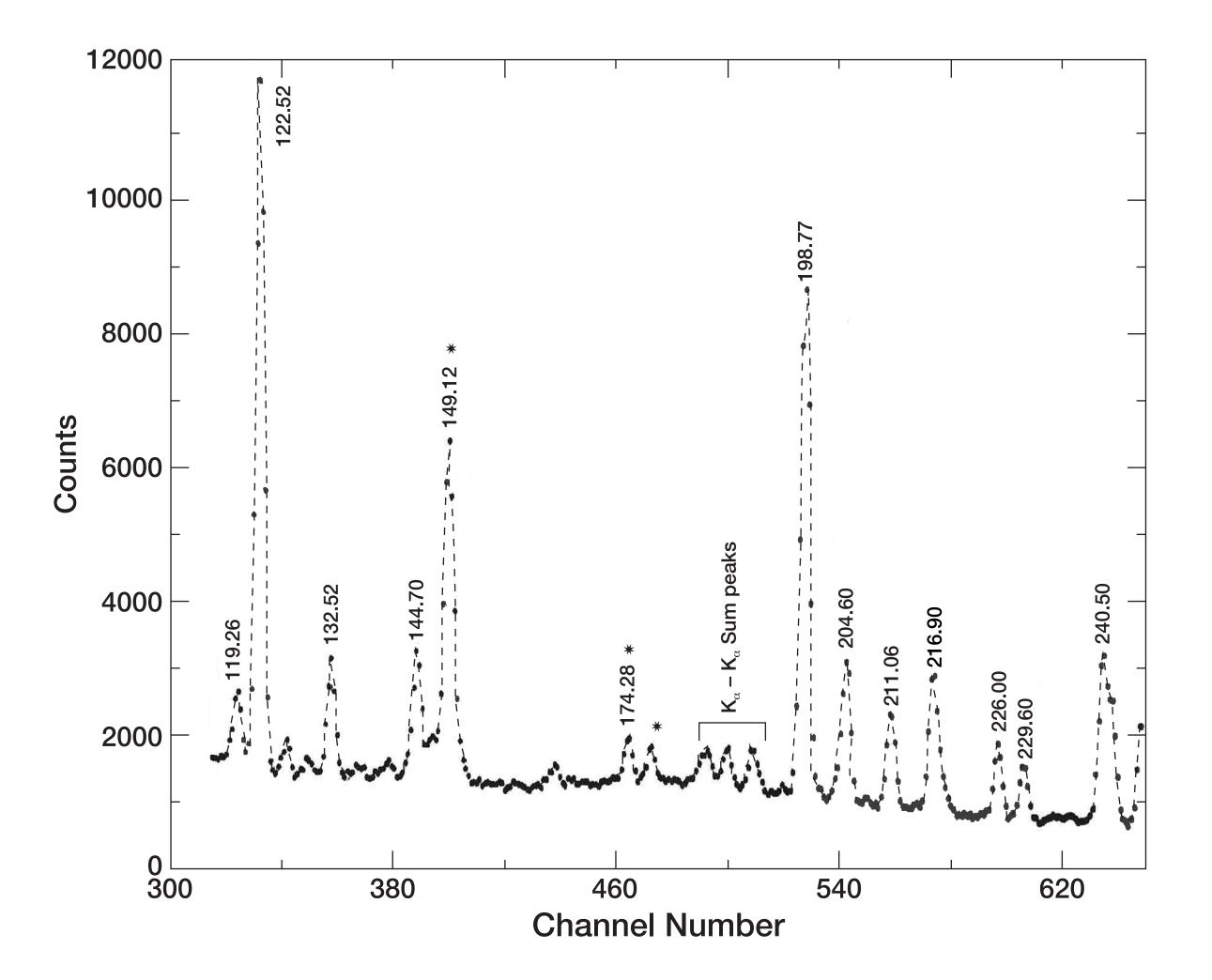
FIG. 8. (Color online) High-energy portion of the partial EC decay scheme of ²²⁹U deduced in the present work. Red lines represent the band heads.

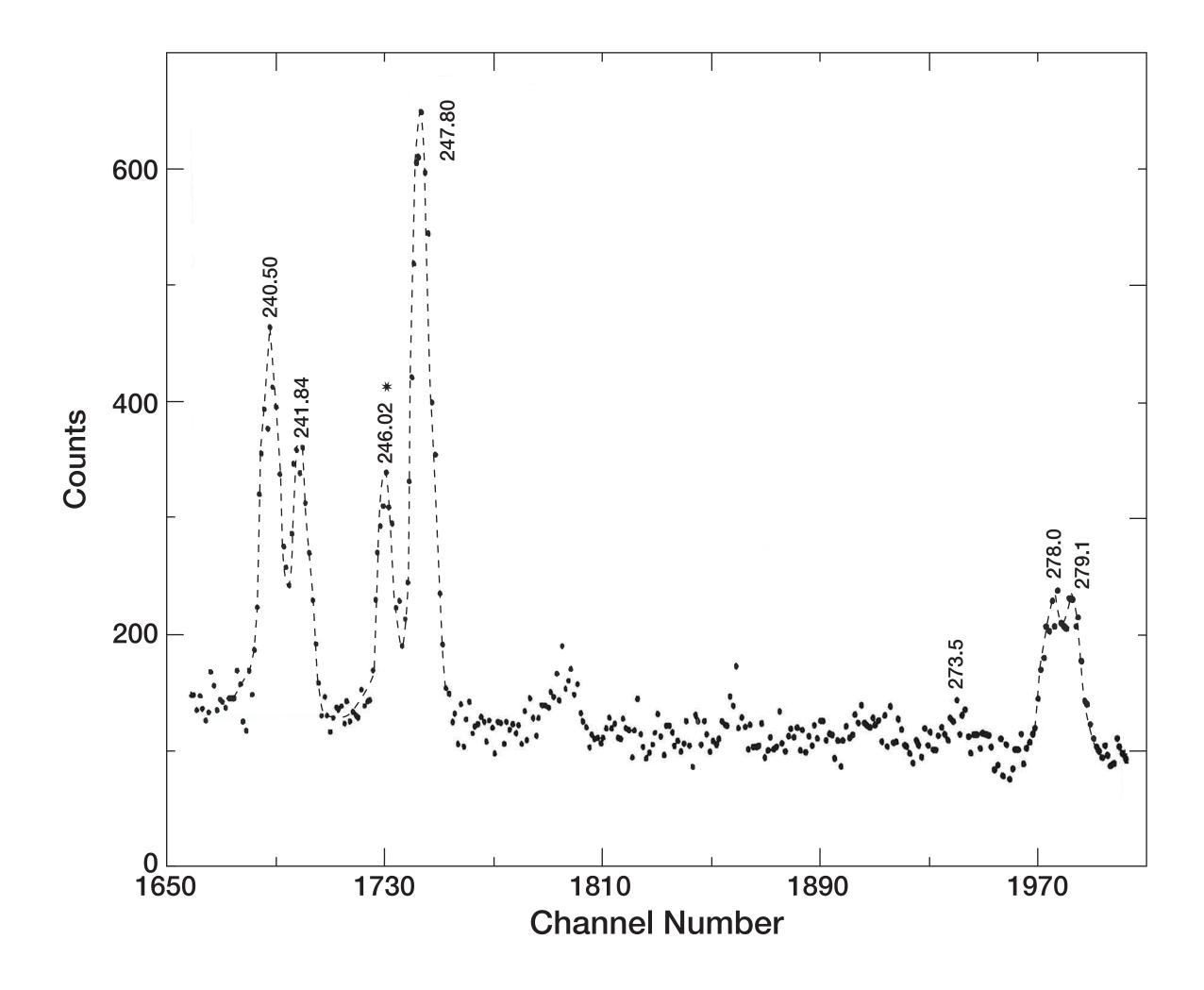
FIG. 9. γ -ray spectra of a ²²⁹U source measured in coincidence with 211.0-keV (top) and 198.8-keV (bottom) γ rays. γ -ray energies in keV are indicated on the peaks. The upper spectrum shows that most of the 211.0-keV γ -ray intensity originates at the 241.80-keV level (see Fig. 7).

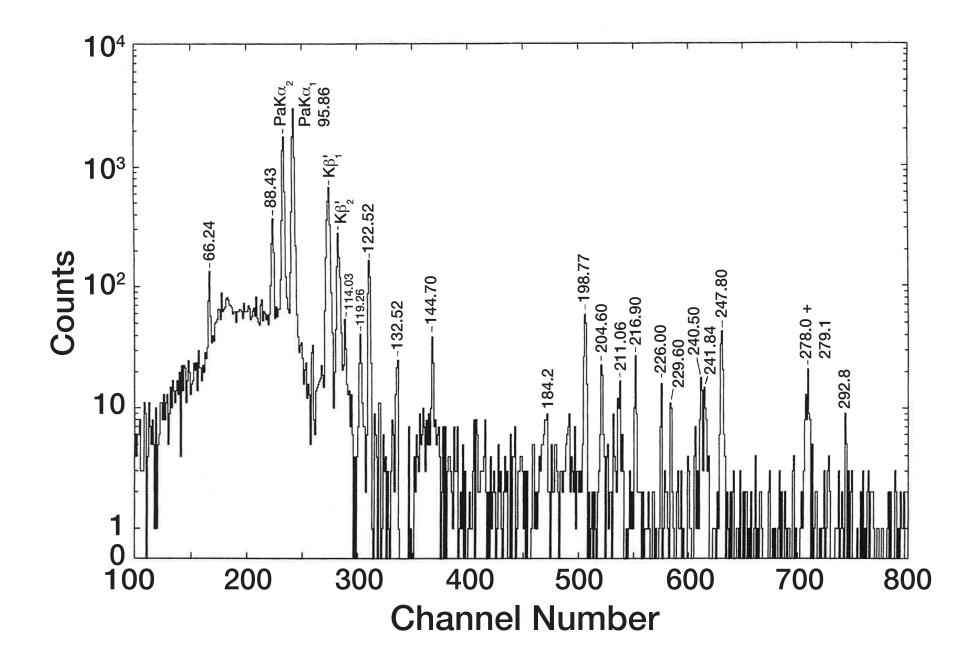
FIG. 10. A comparison of the ²²⁹Pa energy levels deduced in the present work with the prediction of Chasman [1]. In Ref. [2], the energies of the $5/2^+$ [642], $5/2^-$ [523], and $1/2^-$ [530] single-particle states were calculated to be 0.0, 0.4, and 56 keV, respectively.

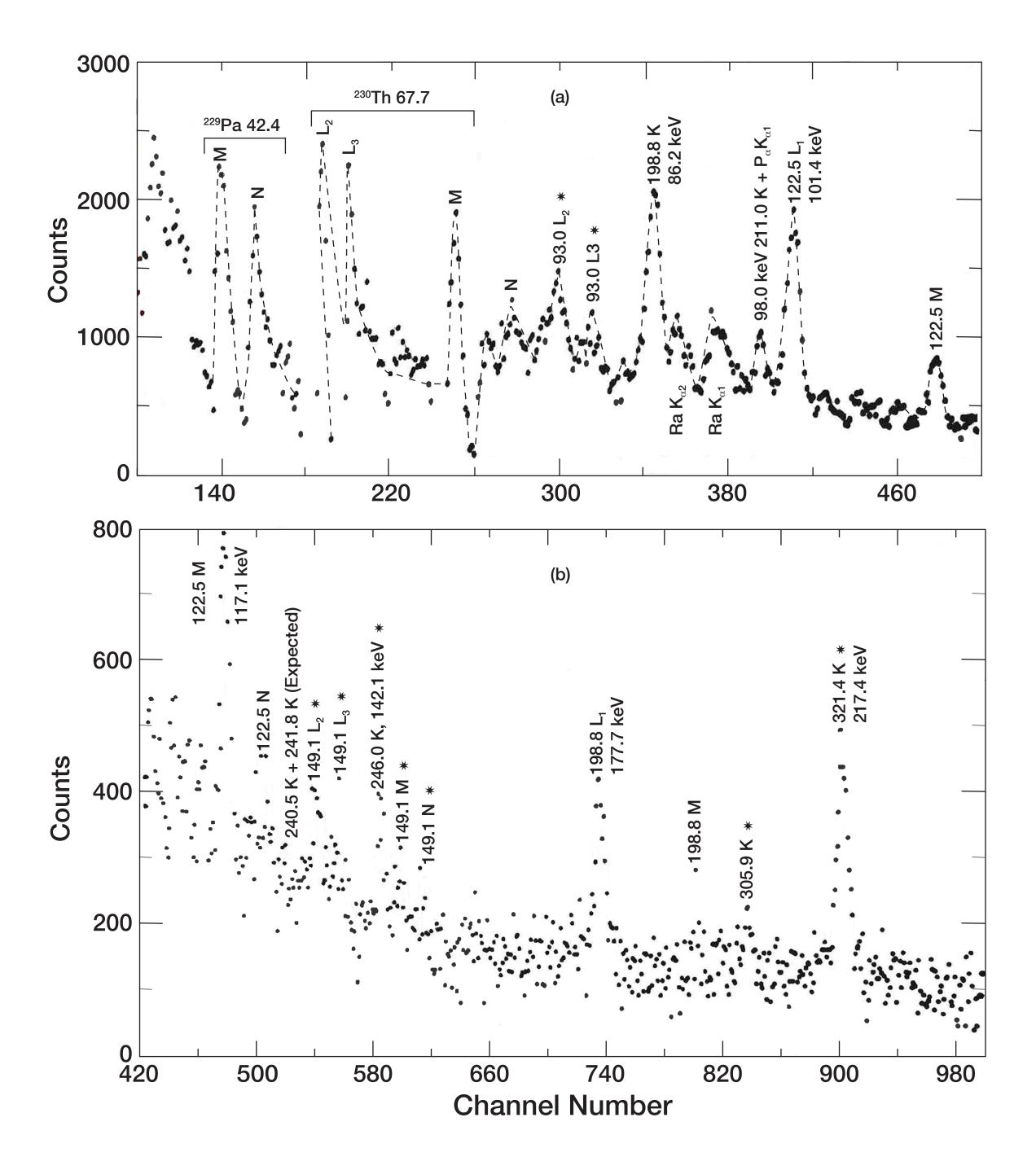
FIG. 11. A comparison of the experimental ²²⁹Pa and ²³¹Pa energy levels. The figure shows that despite both nuclei having 91 protons, their structures are quite different.

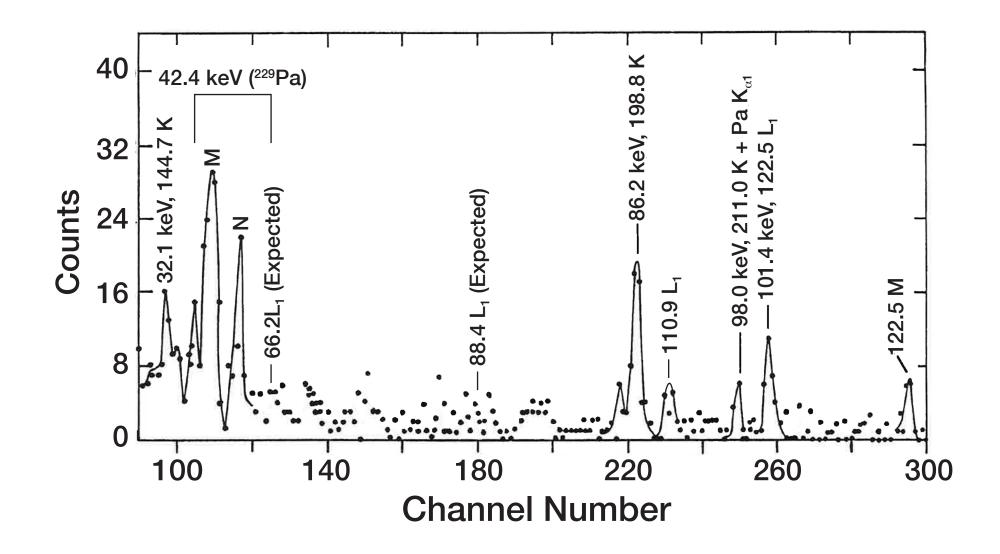


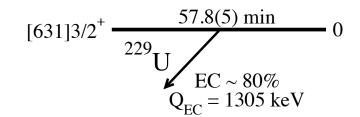


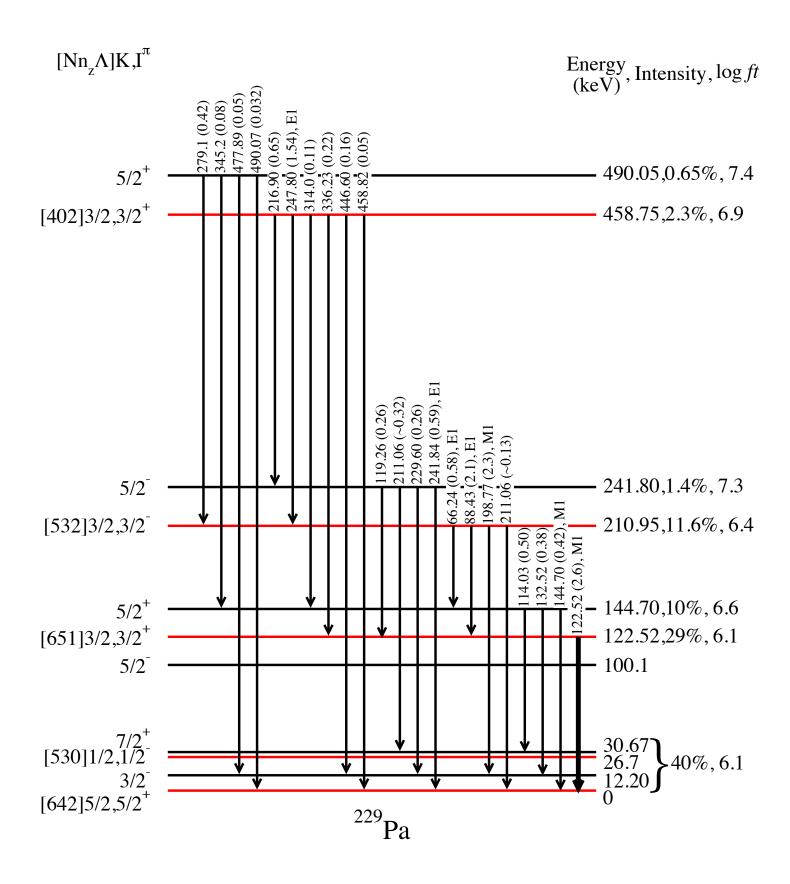


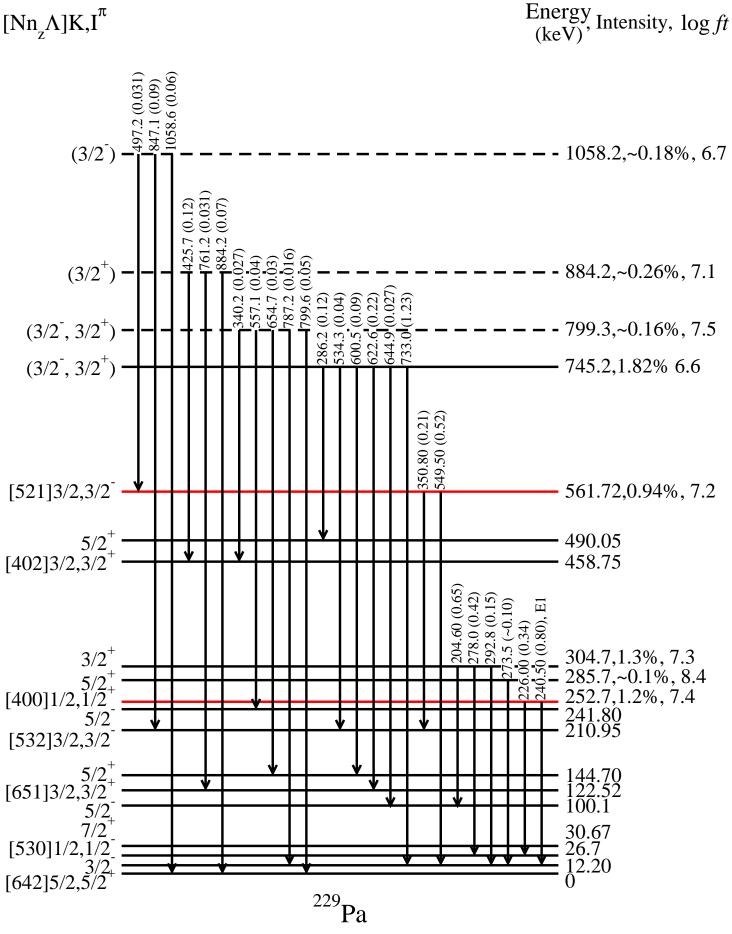




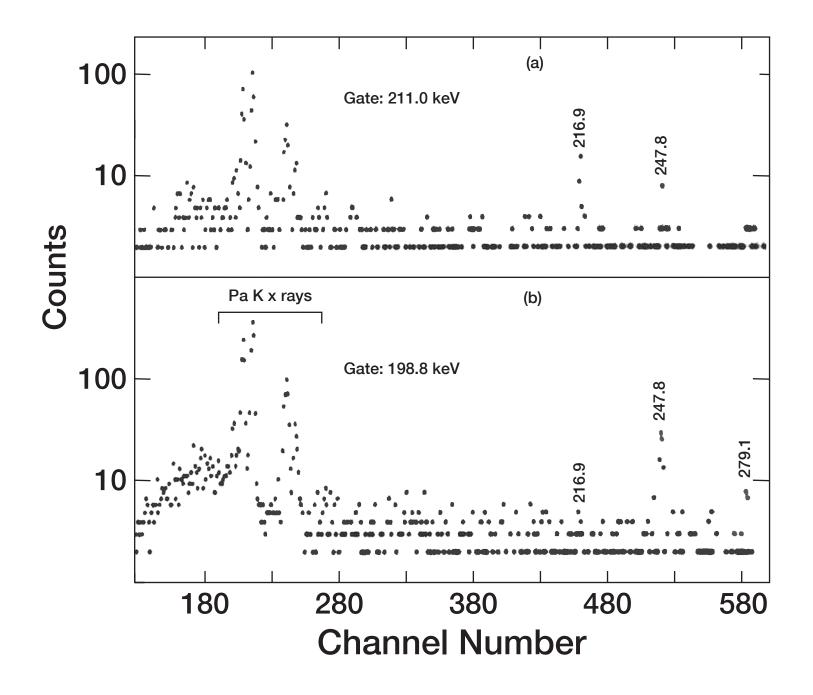


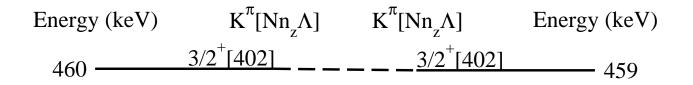


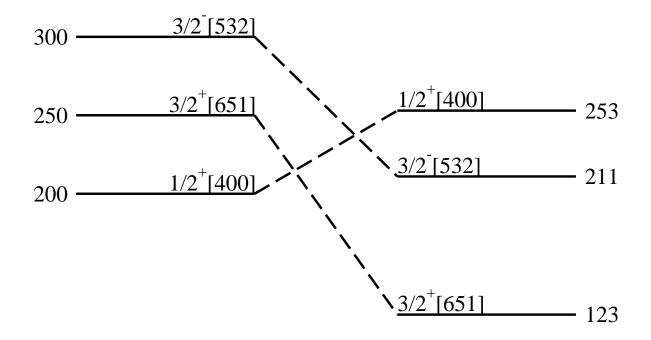


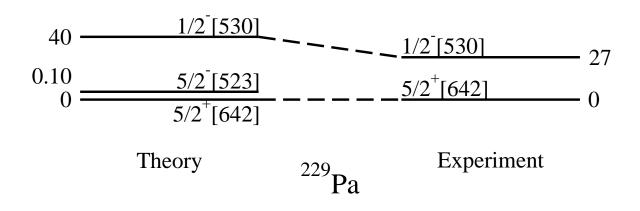


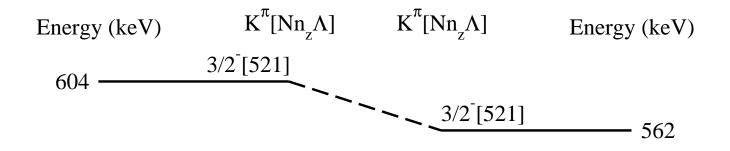
 $[Nn_{z}\Lambda]K,I^{\pi}$











$$\frac{3/2^{+}[402]}{459}$$

