Spin alignment of excited projectiles due to target spin-flip interactions
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Spin alignment of excited projectiles due to target spin-flip interactions.

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The sequential breakup of E/A=65.5-MeV $^7$Be and E/A=36.6-MeV $^6$Li projectiles excited through inelastic interactions with $^9$Be target nuclei have been studied. For events where the target nucleus remained in its ground state, significant alignment of the excited projectile’s spin axis parallel or anti-parallel to the beam direction was observed. This unusual spin alignment was found largely independent of the projectile’s scattering angle and it was deduced that the target nucleus has a significant probability of changing its spin orientation during the interaction. It is proposed that the unusual spin alignment is a consequence of the molecular structure of the $^9$Be nucleus.

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I. INTRODUCTION

Fragments produced in many nuclear reactions often have a preferred alignment of their spins in some reference frame. Spin alignment is found in a diverse number of reactions including inelastic scattering [1–6], deep elastic scattering [7–10], projectile fragmentation [11–18], fission [19, 20], Coulomb excitation [21] and other direct reactions [22–28]. For peripheral reactions, the dominant angular momentum in the reaction is the initial orbital angular momentum between the projectile and target which is perpendicular to both the beam axis and the reaction plane. It is therefore not surprising that many fragments have their spin aligned, on average, parallel to this direction [7, 11, 12, 21–23, 27]. However, there are some cases where different alignments are found [13–16, 18].

Measurement of a fragment’s spin alignment can be deduced from its decay products, including $\beta$ particles through NMR techniques [11, 12], from the recoil induced by gamma-ray decay [23, 24], gamma-ray angular distributions [3, 6, 7, 29], or from the angular distributions of the emitted particles [3, 4, 7, 9, 13, 22, 25–28] or fission fragments [10].

The theory of spin alignment is most tractable in simple direct reactions. Most studies often consider further simplification of the theory, by choosing zero-spin projectile and target nuclei, and zero-spin decay products of the excited projectile. This selection leads to restrictions on the mechanism for producing the spin alignment, i.e., any induced projectile spin must be accompanied by changes in the orbital angular momentum in order to conserve the total angular momentum. However, if the projectile and target nuclei have non-zero spins, then angular momentum conservation can be achieved from changes in the orientation of these spins. Until now, only evidence for small contributions from changes in spin orientation have been found [1].

In this work we examine the spin alignment of $^6$Li and $^7$Be projectiles excited via inelastic interactions with a $^9$Be target. Both projectile and target spins are non-zero; $^6$Li ($J^\pi=1^+$), $^7$Be ($J^\pi=3/2^-$) and $^9$Be ($J^\pi=3/2^-$). We will show that the alignment of the excited projectile’s spin axis is quite different from other direct reactions, with a preferred orientation parallel, or anti parallel, to the beam axis. In order to conserve angular momentum, the change in the projectile’s spin state is balanced by a flip in the spin orientation of the target nucleus.

Details of the experiment will be discussed in Sec. II and the theory of spin alignment for these direct reactions is given in Sec. III. The results of the experiment and their interpretation with the theory are given in Sec. IV. The experimental observations are discussed in terms of target spin flip in Sec. V and finally the conclusions of this work are listed in Sec. VI.

II. EXPERIMENTAL METHOD

The experimental data presented in this work come from a previously published experiment [30, 31] performed at the National Superconducting Cyclotron Laboratory at Michigan State University using the HiRA array [32] to detect projectile-breakup products. Here we
The sum over all $\ell$ assumes there is no net polarization of the spins of the beam or target nuclei. The spins (spin projections) of the lighter and heavier decay products with projection $m$ are denoted as $s$ and $s'$, respectively. The spins (spin projections) of the heavier and lighter decay products with projection $m$ are denoted as $t$ and $t'$, respectively, and $\ell$ is the relative orbital angular momentum of the decay fragments with projection $m$. To simplify the theory in this study, where the heavier decay fragment of the projectile is an $\alpha$ particle, we assume in the following that $s_h = m_h = 0$ and also that the decay of the projectile proceeds through a single value of $\ell$.

### III. SEQUENTIAL-DECAY THEORY

Consider a direct binary reaction between a projectile and target with spins (spin projections) of $s_p$ ($m_p$) and $s_t$ ($m_t$), respectively. This reaction produces an excited projectile nucleus scattered to an element of solid angle $d\Omega^*$ located at the polar angles $\theta^*$ and $\phi^*$ in the reaction center-of-mass frame. The spin and spin projection of the scattered projectile nucleus are $s^*$ and $m^*$ while those of the scattered target nucleus are $s'_t$ and $m'_t$. In the center-of-mass frame of the decaying projectile, its lighter decay product is emitted to an element of solid angle $d\Omega$ located at the polar angles $\psi$ and $\chi$. See Fig. 1 for a schematic giving the definition of the various angles.

The spins (spin projections) of the lighter and heavier decay products are $s_t$ ($m_t$) and $s_h$ ($m_h$), respectively, and $\ell$ is the relative orbital angular momentum of the decay fragments with projection $m$. To simplify the theory in this study, where the heavier decay fragment of the projectile is an $\alpha$ particle, we assume in the following that $s_h = m_h = 0$ and also that the decay of the projectile proceeds through a single value of $\ell$.

For clarity and completeness, the relevant theory is presented here in the distilled form needed for the present analysis. The angular correlation summed over all spin projections is [33]

$$
\frac{d^4\sigma}{d\Omega^*d\Omega} \propto \sum_{m_p,m_t,m'_t,m_l} \left| \sum_{m=\pm \ell} \alpha_{m_p,m_t,m'_t,m_l}^{m,\ell}(\theta^*,\phi^*)Y^m_{\ell}(\psi,\chi) \right|^2 .
$$

The sum over all $m_p$ and $m_t$ assumes there is no net polarization of the spins of the beam or target nuclei. The spherical harmonics are defined as

$$
Y^m_{\ell}(\psi,\chi) = (-1)^m \sqrt{\frac{2\ell + 1}{4\pi}} d^\ell_{m,0}(\psi) e^{im\chi}
$$

FIG. 1. (Color online) Schematic showing the definition of the angles $\theta^*$, $\phi^*$, $\psi$, and $\chi$ in terms of the reaction-center-of-mass velocity vectors of the projectile ($V_{\text{projectile}}$) and target ($V_{\text{target}}$) nuclei and those of the light ($V_{\text{light}}$) and heavy ($V_{\text{heavy}}$) decay products of the projectile. The experimental angular correlations were analyzed with the $z$ axis aligned along the beam axis and the $x$ axis in the reaction plane.

present data from the breakup of $^6$Li and $^7$Be secondary beams on a 1-mm-thick $^9$Be target with the same experimental arrangement. Both beams were produced by fragmenting a primary $E/A=150$-MeV $^{16}$O beam with a $^9$Be target and were separated from other reaction products using the A1900 separator with a momentum acceptance of $\pm 0.5\%$. The $^6$Li beam, with an energy $E/A=36.6$ MeV in the center of the target, was actually a “contaminant” beam of $\sim 35\%$ relative intensity in conjunction with the desired $^8$C beam. Reactions produced with these two beams were separated using the time of flight measured from the A1900 separator to HiRA. The $^7$Be beam with $E/A=65.2$ MeV in the center of the target was $\sim 90\%$ pure. As these secondary beams are produced in fragmentation reactions it is possible they have some small alignment of their spins, but we do not expect this important (see Appendix B).

In these experiments, the HiRA array, consisting of 14 Si-CsI(Tl) $\Delta E - E$ telescopes and located 90 cm downstream from the target, was arranged around all sides of the beam axis to cover the polar angular range from $1.4^\circ$ to $13^\circ$. The double-sided 1.5-mm-thick Si $\Delta E$ detectors have 32 strips on both front and back faces thus giving excellent angular resolution for detected fragments. More details of the experimental apparatus and the energy calibrations of the Si and CsI(Tl) detectors can be found in Refs. [30, 31]. In the following section, measured quantities will be presented which have been corrected for the detector bias that has been determined from Monte Carlo simulations (see Appendix A).
where Wigner's little-d matrix is

\[ d_{m,0}^\ell(\psi) = \sqrt{\frac{(\ell - m)!}{(l + m)!}} P_{\ell}^m(\cos \psi), \quad d_{-m,0}^\ell(\psi) = (-1)^m d_{m,0}^\ell(\psi), \] (3)

and \( P_{\ell}^m(\cos \psi) \) are the associated Legendre polynomials.

The coefficients \( \alpha_{m_1, m_1', m_1''}^{m_2, m_2', m_2''} \) are given by [33]

\[ \alpha_{m_1, m_1', m_1''}^{m_2, m_2', m_2''}(\theta^*, \phi^*) \propto T_{m_1, m_1'}^{m_2, m_2'}(\theta^*, \phi^*) \langle s_1 m_1, \ell m | s^* m_1 + m \rangle \] (4)

where \( T_{m_1, m_1'}^{m_2, m_2'}(\theta^*, \phi^*) \) is the formation amplitude for the creation of the excited projectile fragment.

For simplicity we replace the projections \( m_p, m_t, m_t', m_t, m_h \) by a single index \( i \) in the following. Expanding Eq. (1) we obtain

\[ \frac{d^4 \sigma}{d\Omega^* d\Omega} \propto \frac{2\ell + 1}{4\pi} \sum_{m=-\ell}^{\ell} C_{m,m}(\theta^*, \phi^*) |d_{m,0}^\ell(\cos \psi)|^2 + \sum_{m_1, m_2 \text{ such that } m_1 > m_2} I_{m_1, m_2}(\theta^*, \phi^*, \psi, \chi) \] (5)

where the latter terms are interference terms between the different \( m \) projections defined as

\[ I_{m_1, m_2}(\theta^*, \phi^*, \psi, \chi) = \sum_i \alpha_{m_1}^{i}(\theta^*, \phi^*) \left[ \alpha_{m_2}^{i}(\theta^*, \phi^*) \right]^* Y_{\ell}^m(\psi, \chi) \chi \] (6)

\[ = \frac{2\ell + 1}{4\pi} \sum_{m=-\ell}^{\ell} C_{m,m}(\theta^*, \phi^*) |d_{m,0}^\ell(\cos \psi)|^2 + \sum_{m_1, m_2 \text{ such that } m_1 > m_2} I_{m_1, m_2}(\theta^*, \phi^*, \psi, \chi) \] (7)

where

\[ C_{m_1, m_2}(\theta^*, \phi^*) = \sum_i \alpha_{m_1}^{i}(\theta^*, \phi^*) \left[ \alpha_{m_2}^{i}(\theta^*, \phi^*) \right]^* \] (8)

and the following symmetry relations are valid

\[ I_{m_2, m_1}(\theta^*, \phi^*, \psi, \chi) = I_{m_1, m_2}(\theta^*, \phi^*, \psi, \chi), \quad C_{m_2, m_1}(\theta^*, \phi^*) = C_{m_1, m_2}(\theta^*, \phi^*). \] (9)

The density matrix for the decay orbital angular momentum is a normalized version of the \( C_{m_1, m_2} \) matrix [34], i.e.,

\[ \rho_{m_1, m_2}^\ell(\theta^*, \phi^*) = \frac{C_{m_1, m_2}(\theta^*, \phi^*)}{\text{tr} [C_{m_1, m_2}(\theta^*, \phi^*)]} \] (10)

where the real diagonal elements give the \( m \)-substate probability distribution and the complex non-diagonal elements determine the magnitude and phase of the interference between the different \( m \) substates.

As we are free to choose any quantization axis, it is useful to make a choice that simplifies the problem. One such choice is to define the \( z \) axis as the beam axis and the \( x \) axis is taken to be in the reaction plane, i.e., \( \phi^* = 0 \). With this choice we find from symmetry considerations [35],

\[ T_{m_1, m_1'}^{m_2, m_2'}(\theta^*, \phi^*) = (-1)^{m_1'} m_1 - m_2 - m_p T_{m_1, m_1'}^{m_2, m_2'}(\theta^*), \] (11)

\[ \alpha_{m_1, m_1'}^{m_2, m_2'}(\theta^*, \phi^*) = (-1)^{m_1'} m_1 - m_2 - m_p \alpha_{m_1, m_1'}^{m_2, m_2'}(\theta^*). \] (12)

From these we obtain

\[ C_{m_1, m_2}(\theta^*) = (-1)^{m_1 + m_2} C_{m_1, m_2}(\theta^*), \] (13)

For \( m_2 \neq -m_1 \), the interference terms can be combined to cancel the \( \sin(m_1 - m_2)\chi \) terms of Eq. (7), i.e.,

\[ I_{m_1, m_2}(\theta^*, \psi, \chi) + I_{m_2, -m_1}(\theta^*, \psi, \chi) = \frac{2\ell + 1}{4\pi} \sum_{m=-\ell}^{\ell} C_{m_1, m_2}(\theta^*) \chi \] (14)
While for \( m_1 = m = -m_2 \neq 0 \) the \( \sin(m_1, m_2) \) term is zero as, to satisfy both Eq. (9) and Eq. (13), we require \( \text{Im} [C_{m,-m}(\theta^\ast)] = 0 \). In general, the angular correlation for \( \ell > 0 \) is

\[
\frac{d^4 \sigma}{d \Omega^\ast d \Omega} \propto \frac{2 \ell + 1}{4 \pi} \left\{ C_{0,0}(\theta^\ast)|d_{0,0}(\psi)|^2 + 2 \sum_{m=1}^\ell |d_{m,0}(\psi)|^2 [C_{m,m}(\theta^\ast) + (-1)^m C_{m,-m}(\theta^\ast) \cos 2m\chi] \right. \\
+ \left. 4 \sum_{1 \leq m_1 \geq \ell \atop -m_1 > m_2 > m} \text{Re}[C_{m_1,m_2}(\theta^\ast)] (-1)^{m_1+m_2} d_{m_1,0}(\psi) d_{m_2,0}(\psi) \cos(m_1 - m_2)\chi \right\}
\]  

(15)

In summary with the chosen quantization axis, the angular correlations are determined by the \( C_{m_1,m_2} \) matrix or alternatively the density matrix \( \rho_{m_1,m_2}^\ell \). Only real matrix elements enter Eq. 15, or where the matrix elements are complex, only the real components are needed. Information on the imaginary components would require a polarized beam or target.

A. Projections

As \( \int_0^{2\pi} \cos m\chi \, d\chi = 0 \) for \( m \neq 0 \), if we project the correlation distribution on the \( \psi \) axis, then all the interference terms will drop out and the projected distribution will be given by

\[
W(\psi) \propto \frac{2 \ell + 1}{2} \left[ \rho_{0,0}^\ell(\theta^\ast) + 2 \sum_{m=1}^\ell \rho_{m,m}^\ell(\theta^\ast) \right] .
\]  

(16)

As \( \int_0^{2\pi} d_{m_1,0}(\psi) d_{m_2,0}(\psi) \sin \psi \, d\psi = 0 \) for \( m_1 - m_2 = \text{odd} \), then by projecting on the \( \chi \) axis, only the \( \cos m\chi \) terms with even \( m \) will survive. The projected \( \chi \) correlations can then be written as

\[
W_{\text{even}}(\chi) = \int_0^{\pi} \frac{d^4 \sigma}{d \Omega^\ast d \Omega} \sin \psi \, d\psi \\
= A_0 + A_2 \cos 2\chi + \ldots + A_{2\ell} \cos 2\ell\chi.
\]  

(18)

If \( \ell \) is not known, then the highest order term in Eq. (18) needed to fit a measured distribution can give a lower limit to this quantity. To see the odd-\( m \cos m\chi \) terms, we construct the quantity

\[
W_{\text{odd}}(\chi) = \int_0^{\pi/2} \frac{d^4 \sigma}{d \Omega^\ast d \Omega} \sin \psi \, d\psi - \int_{\pi/2}^{\pi} \frac{d^4 \sigma}{d \Omega^\ast d \Omega} \sin \psi \, d\psi \\
= A_1 \cos \chi + \ldots + A_{2\ell-1} \cos(2\ell - 1)\chi
\]  

(20)

IV. EXPERIMENTAL RESULTS

A. \( ^7\text{Be} \) Breakup

The \( ^7\text{Be} \) nucleus has a strong \( ^3\text{He}+\alpha \) cluster structure and large \( ^3\text{He}+\alpha \) breakup yield. The distribution of target excitation energy \( E_\ast^\text{t} \) for all detected \( ^3\text{He} + \alpha \) events, determined from conservation of energy and momentum, is displayed in Fig. 2(a). A strong peak at \( E_\ast^\text{t} \sim 0 \) MeV is very prominent in this spectrum with a FWHM of around 12 MeV. This width is consistent with the expected resolution as demonstrated by the smooth curve in Fig. 2(a) which is a simulated distribution for \( E_\ast^\text{t} = 0 \). Thus the experimental peak in this figure predominantly contains events where the target remains in its ground state, however one cannot rule our some contribution from low-lying excited states in \( ^9\text{Be} \). In the following we will only consider the events in the \( E_\ast^\text{t} = 0 \) peak as the high-energy tail does not exhibit strong alignment of the projectile.

The \( ^8\text{Be} \) excitation-energy distribution (corrected for the energy-dependent detector efficiency) is shown in Fig. 2(b). This excitation energy, \( E_\ast^\text{p} \), is determined from the invariant mass of the detected \( ^3\text{He} + \alpha \) pair minus the ground-state mass of \( ^7\text{Be} \) and the simulated resolution is 245 keV FWHM at \( E_\ast^\text{p} = 4.6 \) MeV. This distribution shows a very prominent peak associated with the second excited state (\( s^\ast = 7/2^- \)) of \( ^7\text{Be} \) at \( E_\ast^\text{p} = 4.57 \) MeV. The third excitation state (\( s^\ast = 5/2^- \)) at \( E_\ast^\text{p} = 6.73 \) MeV is present, but weakly populated.

The angular distribution (corrected for the detector acceptance) for the \( 7/2^- \) state is displayed in Fig. 2(c) and shows diffraction oscillations typically expected for inelastic excitations. To accurately define the reaction plane and the breakup angle \( \chi \), we restrict further analysis to \( \theta^\ast_{\text{lab}} > 2^\circ \), unless specified.

The raw experimental 2-dimensional \( \cos \psi - \chi \) angular correlations for the \( 7/2^- \) state are shown in Fig. 3(a), while the simulated detection efficiency is displayed in Fig. 3(b). The efficiency-corrected correlation obtained from dividing the raw data by this efficiency is shown in Fig. 3(c). It contains well-defined modulations which can be related to the interference between different \( m \) projections.

From angular-momentum and parity conservation, the decay of this \( ^7\text{Be} \) level must be \( \ell = 3 \) and the theoretical correlation of Eq. (15) can be defined by 16 unique \( C_{m_1,m_2} \) parameters or the equivalent density matrix \( \rho_{m_1,m_2}^\ell \) [see Eq. (10)]. These include 7 real matrix elements \( \rho_{0,0}^\ell, \rho_{1,1}^\ell, \rho_{2,2}^\ell, \rho_{3,3}^\ell, \rho_{1,-1}^\ell, \rho_{2,-2}^\ell, \text{ and } \rho_{3,-3}^\ell \) and the real parts of 9 complex matrix elements. Figure 3(d) shows a fit obtained by varying these 16 pa-
If we define the reduced matrix elements as experimental angular correlations quite well. This fit reproduces the basic features of the parameters. This fit reproduces the basic features of the experimental angular correlations quite well.

The fitted density matrix elements are listed in Table I. If we define the reduced matrix elements as

$$c_{m1,m2} = \frac{\rho_{m1,m2}^I}{\sqrt{\rho_{m1,m1}^I \rho_{m2,m2}^I}},$$

then, from the Cauchy-Schwarz inequality

$$|\sum_i a_i b_i|^2 \leq \sum_i |a_i|^2 + \sum_i |b_i|^2,$$

it is easy to show that $|\text{Re} \left[c_{m1,m2}\right]| \leq 1$. The real components of the reduced matrix elements are also listed in Table I and their magnitudes are indeed less than unity and thus consistent with theory.

To examine the angular correlations in more detail, let us look at the projections discussed in Sec. III A. The experimental correlation projected on the $\cos \psi$ axis, shown in Fig. 4(a), depends only on the real matrix elements $\rho_{m,m}^\ell$. Surprisingly, this distribution peaks at $\psi=90^\circ$ ($\cos \psi=0$), i.e., the sequential decay of the $^7$Be $s^*=7/2^-$ level is dominated by transverse emissions to the beam axis.

The fitted projection is indicated in Fig. 4(a) by the solid curve, together with the contributions from the different $|m|$ values (dashed curves). The fitted $\rho_{m,m}^\ell$ values give the probability distribution of the various $m$ projections, also known as the magnetic-substrate population. Note from Eq. (13), the distribution is symmetric around $m=0$, i.e., $\rho_{m,-m}^\ell = \rho_{m,m}^\ell$. This probability distribution is displayed in Fig. 4(b) and is dominated by the $|m|=\ell$ components, i.e., in classical terms, the alignment is mostly parallel or antiparallel to the beam axis a result which is consistent with the strongly transverse decay pattern. This alignment distribution is very unusual in inelastic scattering and this is the most important result of this work.

The $\rho_{m1,m2}^\ell$ density matrix gives information on the alignment of the orbital angular momentum produced in the decay of the excited projectile. However, it would be more interesting to deduce the alignment of the spin of the excited projectile itself. This is described by the

<table>
<thead>
<tr>
<th>parameter</th>
<th>fitted value</th>
<th>reduced value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\rho_{0,0}$</td>
<td>0.028(1)</td>
<td>1</td>
</tr>
<tr>
<td>$\rho_{1,1}$</td>
<td>0.051(1)</td>
<td>1</td>
</tr>
<tr>
<td>$\rho_{2,2}$</td>
<td>0.122(2)</td>
<td>1</td>
</tr>
<tr>
<td>$\rho_{3,3}$</td>
<td>0.312(2)</td>
<td>1</td>
</tr>
</tbody>
</table>

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\[ \frac{\rho_{m1,m2}}{\sqrt{\rho_{m1,m1} \rho_{m2,m2}}} \]
density matrix \[34\]

\[
\rho_{m_1, m_2}^{s}(\theta^*) = \frac{\sum_{m_p, m_t, m'_t} T_{m_p, m_t}^{m_1, m'_t}(\theta^*) \left[ T_{m_p, m_t}^{m_2, m'_t}(\theta^*) \right]^*}{\text{tr} \left[ \sum_{m_p, m_t, m'_t} T_{m_p, m_t}^{m_1, m'_t}(\theta^*) \left[ T_{m_p, m_t}^{m_2, m'_t}(\theta^*) \right]^* \right]},
\]

(25)

Although it is not possible to constrain all elements of this matrix from our measured data, the real diagonal elements which give the \(m\)-substate distribution can be determined from the diagonal elements of \(\rho_{m, m}^{s}\). From Eqs. (4,10,23) we obtain

\[
\rho_{3,3}^{s}(\theta^*) = \rho_{\pm \frac{1}{2}, \pm \frac{1}{2}}^{s}(\theta^*) + \frac{1}{7} \rho_{\pm \frac{3}{2}, \pm \frac{1}{2}}^{s}(\theta^*),
\]

(24)

\[
\rho_{2,2}^{s}(\theta^*) = \frac{6}{7} \rho_{\pm \frac{1}{2}, \pm \frac{1}{2}}^{s}(\theta^*) + \frac{2}{7} \rho_{\pm \frac{3}{2}, \pm \frac{1}{2}}^{s}(\theta^*),
\]

(25)

\[
\rho_{1,1}^{s}(\theta^*) = \frac{5}{7} \rho_{\pm \frac{1}{2}, \pm \frac{1}{2}}^{s}(\theta^*) + \frac{3}{7} \rho_{\pm \frac{3}{2}, \pm \frac{1}{2}}^{s}(\theta^*),
\]

(26)

\[
\rho_{0,0}^{s}(\theta^*) = \frac{8}{7} \rho_{\pm \frac{1}{2}, \pm \frac{1}{2}}^{s}(\theta^*)
\]

(27)

where the coefficients of each term are the square of Clebsch-Gordan coefficients. After solving for \(\rho_{m, m}^{s}\), the \(m\)-substate distribution for the \(s^*\) spin alignment is plotted in Fig. 4(c). It also shows the alignment is mostly parallel or antiparallel to the beam axis.

An alternative way of specifying the \(m\)-substate distribution is via the statistical or polarization tensor \(\rho_{kq}\) (or \(B_k^{q}\) in some studies) \[34\]. The \(\rho_{k0}\) terms just depend on the diagonal elements of the density matrix and only even \(k\) values are non-zero when \(\rho_{m^*, m^*}^{s} = \rho_{-m^*, -m^*}^{s}\).

The \(\rho_{00}\) term is just the normalization of the \(m\)-substate distribution, and the lowest-order term of interest is \(\rho_{20}\). However, additional terms, \(\rho_{40}\) and \(\rho_{01}\), are necessary to fully describe the distributions in Figs. 4(b) and 4(c) and \(q > 0\) terms are needed to describe the off-diagonal elements. An alignment parameter,

\[
A = \frac{\rho_{20}}{\rho_{20}^{\text{max}}} = \sum_{m^*} \frac{3m^2 - s^*(s^* + 1)}{s^*(2s^* - 1)} \rho_{m^*, m^*}^{s},
\]

(28)

is often defined where \(\rho_{20}^{\text{max}}\) is the maximum value of \(\rho_{20}\) when only the \(|m^*| = s^*\) elements are non-zero. Negative alignment would correspond to a preponderance of the small \(|m^*|\) values. The alignments associated with spin of the excited state and decay orbital angular momentum in this case can be shown to be identical from Eqs. (24-27). We obtain an alignment of \(A = 49(1)\)% from the experimental data. This is quite large. In comparison typical positive alignments of the order of 10% or less have been found in projectile fragmentation reactions when the projectile remnants at the peak of their momentum...
These two distributions were corrected for their individual detection efficiencies and subtracted. This final distribution clearly has a very strong $\cos \chi$ component and a smaller, but still significant, $\cos 3\chi$ component. A fit with Eq. (20) is indicated by the solid curve and the fitted components are again plotted as the dashed curves. No significant $\cos 5\chi$ component is needed in this fit.

Both the $W_{\text{even}}$ and $W_{\text{odd}}$ distributions of Fig. 5 clearly show the presence of many interference terms. The density matrix elements in Table I indicate that the detected events are not associated with just a single projection of $\ell$, but contain admixtures of different $m$ values. These admixtures are not just between neighboring values of $m$ ($\cos \chi$ terms), and in particular the $\cos 4\chi$ terms in Table I are quite strong. The latter correspond to admixtures for $m$ values separated by 4 units.

B. Scattering-Angle Dependence

The dependence of the angular correlations on the scattering angle $\theta^{*}$ is quite small. To demonstrate this, we have subdivided the events into two approximately equal groups, one with $2^{\circ} < \theta_{\text{lab}}^{*} < 4.5^{\circ}$ and the other for larger angles. The two efficiency-corrected angular correlations are plotted in Fig. 6. The result for $\theta_{\text{lab}}^{*} > 4.5^{\circ}$ has a number of “holes” where the efficiency is zero. However apart from these “holes”, the two correlations look very similar with the same dominant features.

For a more quantitative comparison, the $m$-substate distributions determined from the fitted $\rho_{m,m}^{\ell}$ matrix elements are compared in Fig. 7. In addition to the previously defined $\theta^{*}$ angular range, we also consider events for $\theta^{*} < 2^{\circ}$. Even though it is problematic to define a $\chi$ angle for such events, the $\psi$ angle is still well defined and the $\rho_{m,m}^{\ell}$ matrix elements can be determined from Eq. (16).

The $m$-substate distributions for both data sets with $\theta^{*} > 2^{\circ}$, which account for most of the events, are similar. The events for $\theta^{*} < 2^{\circ}$ again show qualitatively similar behavior with the $|m| = \ell$ components still dominant, but now the $m=0$ component is somewhat more prominent. Again note that these events account for only a small fraction of the total. Overall there is very little dependence on the scattering angle $\theta^{*}$ and even the changes at very small angles are minor.

C. $^6$Li breakup

Similar spin alignment is also observed from the $d+\alpha$ breakup of $^6$Li. Detected $d+\alpha$ events are again found to have a prominent component with $E_i^{*}=0$. The projectile excitation-energy distribution for this component is shown in Fig. 8(a). This spectrum shows a dominant peak associated with the $E_p^{*}=2.186$-MeV, $s^{*}=3^{+}$ first excited state and a smaller peak associated with the $E_p^{*}=4.31$-MeV, $s^{*}=2^{+}$ third excited state. For the $s^{*}=3^{+}$

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig5}
\caption{(Color online) Projected (a) $W_{\text{even}}$ and (b) $W_{\text{odd}}$ correlation distributions for the $s^{*}=7/2^{+}$ excited state of $^7$Be. The solid curves show fits with Eqs. (18) and (20) while the dashed curves give individual the $\cos m\chi$ components where each curve is labeled by the value of $m$.}
\end{figure}
peak, the angular distribution of the scattered projectile is plotted in Fig. 8(b). It has similar features to that found for the $^7$Be$^{7/2-}$ level in Fig. 2(c).

For the $s^*=3^+$ state, $\ell=2$ and $\ell=4$ components are both possible. In the following we will assume only the $\ell=2$ decay occurs. The $\ell=4$ decay could generate interference terms up to order $\cos 8\chi$, but no indication of such higher-order interference terms were observed in the experimental correlations.

The efficiency-corrected angular correlation for the $s^*=3^+$ state, shown in Fig. 9(a), is qualitatively similar to the results for $^7$Be [Fig. 3(c)]. Again the fitted distribution shown in Fig. 9(b) reproduced the major features of the experimental distribution. The fitted matrix elements are listed in Table II and again the real reduced matrix elements (third column) have magnitudes less than unity as expected.

The projected $\cos \psi$ distribution for the $s^*=3^+$ state is displayed in Fig. 10(a) and again shows a predominance for traverse decay. The extracted $m$-substate distribution is plotted in Fig. 10(b) and shows strong alignment with the $|m|\leq\ell$ components again having the largest probability. Thus they are also consistent with an alignment mostly parallel or antiparallel to the beam axis. The alignment obtained from this distribution is $A=51(1)\%$, very similar to the $A=49(1)\%$ value obtained for the $s^*=7/2^-$ state in $^7$Be.

The $W_{even}(\chi)$ and $W_{odd}(\chi)$ projected distributions for the $s^*=3^+$ state are plotted in Fig. 11 and again are qualitatively similar to the results for $^7$Be in Fig. 4.

V. DISCUSSION

These sequential breakup reactions are peripheral and are expected to be confined to a narrow window of incoming and outgoing orbital angular momentum, $L_{in}$ and $L_{out}$, respectively [36]. A number of experimental studies have looked at spin alignment in reactions where the spins of the initial and final products are zero [22, 25–28]. While this greatly simplifies the theory of spin alignment, it also forces a certain type of spin alignment as the spin of the excited projectile can only be obtained from changes in the orbital angular momenta, i.e., by
FIG. 8. (Color online) (a) Efficiency-corrected projectile excitation-energy distribution determined from detected \( d + \alpha \) events for \( E_t^* = 0 \) with the \(^6\text{Li}\) beam. (b) Angular distribution of the scattered projectile extracted for the \( s^* = 3^+ \) level.

Angular-momentum conservation, \( s^* = |L_{\text{in}} - L_{\text{out}}| \) and the observed average spin alignment is typically normal to the reaction plane (parallel to \( L_{\text{in}} \)). If \( m_{\text{out}} \) is the projection of \( L_{\text{out}} \) and as different values of \( m_{\text{out}} \) peak at different scattering angles \( \theta^* \), then by gating on \( \theta^* \), one is selecting a different \( m_{\text{out}} \) distribution. If all the spins of the initial and final particles are zero, then \( m^* = -m_{\text{out}} \), and the alignment is strongly coupled to the scattering angle [25]. This explains the strong correlations between \( \psi \) and \( \theta^* \) observed in many reactions.

In contrast in this work where, the spins of the initial fragments are nonzero and one of the exit-channel fragments has finite spin, we find only a very weak dependence of the \( \psi \) distributions on \( \theta^* \) and the observed alignment is mostly parallel or antiparallel to the beam axis. These observations suggest that changes in the orbital angular momentum play a significantly smaller role in these reactions. In fact if \( \Delta \ell = |L_{\text{in}} - L_{\text{out}}| = 0 \), then there is only one projection, i.e. \( m_{\text{out}} = 0 \), and the angular correlations would be independent of scattering angle \( \theta^* \).

For \( \Delta \ell = 0 \), the increased spin of the projectile during the reaction could be compensated by changes in the spin projection of the target. For example, if the \(^9\text{Be}\) target’s spin \( (3/2 \hbar) \) is fully flipped, then this changes the angular momentum by \( 3 \hbar \), enabling the excited \(^7\text{Be}\) projectile’s spin to obtain values between \( 1/2^- \) to \( 9/2^- \). For the \(^6\text{Li}\), this spin flip of the target would enable the excitation of states with spin from \( 0^+ \) to \( 4^+ \). For both projectiles, these spin ranges allow for the production of the excited states observed in Figs. 2(b) and 8(a).

Additional evidence for significant \( \Delta \ell = 0 \) contribution can be obtained from the \( \theta^* \) angular distributions in Figs. 2(c) and 8(b). Only for \( \Delta \ell = 0 \), do the angular distributions have a peak at \( \theta^* = 0 \) [36] as observed in these experimental distribution. Thus we have presented a number of pieces of evidence that point to changes in the target’s spin orientation, rather than changes in the orbital angular momentum, as the most important source of the increased spin of the excited projectile. Although spin flip in inelastic scattering has been observed before, it only contributed to a small fraction of the total yield (\(~1\%\) [1]), in contrast in this study it appears to be the dominant contribution.

There is still the question: Why does this spin-flip mechanism produce the strong alignment of the projectile spin parallel or antiparallel to the beam axis observed in this work? We propose an answer to this question that
rest on the peculiar structure of the $^9$Be target nucleus. This nucleus is loosely bound (breakup threshold of only 1.5 MeV) with a very large deformation [37] and strong $\alpha$-particle structure. It is often modeled as two separated $\alpha$ particles with the valence neutron in a molecular orbit. The ground state corresponds to a spin projection on the symmetry axis of $K=3/2$ with the valence neutron in the $\pi_{3/2}^-$ orbital, with a degeneracy of two [38].

For the relatively higher-energy reactions studied in this work, one may consider the orientation of the $^9$Be deformation to remain fixed during the collision. Therefore in flipping the target’s spin one is just moving the valence neutron to the other unoccupied member of the $\pi_{3/2}^-$ orbital with opposite angular-momentum projection. This change in spin projection must be facilitated by the interactions of the projectile with the valence neutron, but to prevent this fragile nucleus from breaking up (and keeping it in its ground state), interactions of the projectile with the $\alpha-\alpha$ core should be minimized. This requirement may select certain orientations of the $^9$Be symmetry axis and thus lead to the strong alignment of the spin of the excited projectiles observed in this work.

VI. CONCLUSION

The sequential breakup of $^7$Be and $^6$Li projectiles following inelastic interactions with a $^9$Be target have been studied. For events where the target nucleus remained in its ground state, we have observed strong alignment of the spin axis for the $J^\pi=7/2^-$, second excited state of $^7$Be determined from the angular correlations of the $t-\alpha$ decay products. Similar alignment was also determined for the $J^\pi=3^+$, first excited state of $^6$Li in $d-\alpha$ decay.

The measured angular correlations of the decay products showed strong modulations due to interference between different angular-momentum projections. In addition, both projectiles decay predominantly in the transverse direction corresponding to spin alignments which
orbital angular momentum. It must be accompanied by changes in the projectile-target orientation, i.e., a target spin flip. The alignments observed in this work are quite different to most other alignment studies in direct reactions where the projectile and target do not change. This is further confirmed by the angular distribution of the excited projectiles which peak at zero angle. If the orbital angular momentum does not change, then the change in the projectile's spin from its ground-state value, must be accompanied by a change in orientation of the target's spin alignment, i.e., a target spin flip. The alignments observed in this work are quite different to most other alignment studies in direct reactions where the projectile and target are usually chosen to have zero ground-state spin. In these cases, one often observes alignment perpendicular to the beam axis as changes in the projectile spin must be accompanied by changes in the projectile-target orbital angular momentum.

It is speculated that the strong alignment observed in this work is associated with the structure of $^9$Be which is very deformed and has a strong $\alpha$-cluster structure where the valence neutron occupies a $\pi$ molecular orbit. If the target symmetry axis is aligned with the beam direction, the projectile could more easily interact with the valence neutron, causing the spin flip, without exciting the $\alpha$-$\alpha$ core. This idea can be tested using the same beams but with a zero-spin target where spin flip is not possible.

**Appendix A: Monte Carlo Simulations**

The measured correlations, angular distributions and energy spectra were corrected for detector acceptance and resolution using Monte Carlo simulations similar to those discussed in Refs. [30, 31]. In these simulations, the reaction was assumed to occur at a random depth in the secondary target. Energy loss and small-angle scattering of the projectile and the decay products in the target material were then calculated from Refs. [39, 40]. Simulated events were kept if both decay fragments were “detected” in a HiRA telescope. The angles and energies of the “detected” fragments where then smeared by the detector resolutions before being analyzed in the same manner as the experimental events. The acceptance of the HiRA array is governed only by the angular location of the telescopes, which were measured very accurately with a Coordinate Measurement Machine (CMM) arm. Otherwise the energies of the $t$, $^6$He, and $\alpha$ decay products from the projectile were located well within the low and high-energy thresholds for detection and identification.

The simulations also included the effects of the beam-spot size and the beam divergence at the target. These quantities were not measured, but a range of reasonable values based on past experiments and predictions were used, and the uncertainties associated with these was included to the error bars of the final efficiency-corrected distributions.

The efficiency as a function of $\theta^*$, used for determining the angular distributions of the scattered projectiles in Figs. 2(c) and 8(b), has a small dependence on the $\psi - \chi$ correlations assumed in the simulation of projectile decay. Similarly the efficiency as functions of $\psi$ and $\chi$ as shown in Fig. 3(b) has a small dependency on the projectile angular distribution assumed in the simulations. We therefore employed an iterative approach, starting with an initial guess for both the angular distributions and correlations and then progressively adjusting them both to reproduce the measured distributions. Final efficiencies as a function of the various angle were then calculated from the simulated events and used to correct the experimental distributions.

**Appendix B: Spin Alignment of Secondary Beams**

Given the unexpected nature of the result, it useful to examine other assumptions made in the analysis. We have assumed that the $^6$Li and $^7$Be secondary beams are unpolarized with uniform distributions of their magnetic substates. Fragmentation products can show net polarization and alignment depending on the selected angular and momentum regions [11, 12, 14–18]. Information on the magnetic substate distribution of the beam is contained in a density matrix for beam $\rho_{n_{p1}m_{p2}}$. The secondary beams in this work were produced in a fragmentation of the primary $^{16}$O beam and zero-degree products were selected by the A1900 separator. As we expect symmetry about the beam axis, the density matrix should be diagonal [34]. As fully stripped $^7$Be and $^6$Li fragments were selected, there was no loss of their polarization or alignment due to the hyperfine interaction during the passage to the secondary target, however, some rotation of the alignment axis will occur due to their passage through the dipole magnets between the primary and sec-
ond targets [41].

If there is any net polarization of the beams, then our assumption that $p_{m,m}^l = p_{-m,-m}^l$ for the excited projectile is not valid and the cancellation of the $\sin(m_1 - m_2)\chi$ terms in Eq. (14) will not occur. Therefore we have refitted the $\cos\psi - \chi$ correlation plots including these $\sin(m_1 - m_2)\chi$ terms but found their magnitudes to be consistent with zero at the 2$\sigma$ level and thus consistent with zero polarization.

Even if there is no polarization, there may be some alignment, i.e., the magnetic substate distribution is not uniform but $p_{m,m}^l = p_{-m,-m}^l$. Such effects in projectile fragmentation have been probed via $g$-factor measurements of isotomers with the Time-Dependent Perturbed Anglar Distribution (TDPAD) method [15–18, 41]. In Ref. [18], the spin alignment is described in a simple model as the net contribution from ablated nucleons removed from a localized region on the surface of the projectile. In this model, the alignment [Eq. (28)] changes from positive to negative as one goes from the peak to the wings of the momentum distribution of the fragmentation products. This is consistent with the limited available data [14–16].

The largest positive alignment has observed from high-spin isotomers, e.g., $A \sim 35\%$ for the $I=19/2^-$ isomer in $^{43}$Sc [15]. This is not unexpected, as in such cases the ablated nucleons must act in unison in order to achieve high spins. However for lower-spin isotomers, significantly smaller alignments are observed, i.e., for isotomers of spin $2 \leq I < 9/2$, only alignments of 9% or less have been observed at the peak of the momentum distribution [14, 16, 18]. In addition, for the low spins the ablation of large numbers of nucleons is expected to further attenuate the alignment as the angular momenta removed by individual nucleons do not have to add, but can cancel. For example an alignment of $A=8(1)\%$ was measured for the $I=4^+ 32$Al isomer from the fragmentation of a $^{32}$Al beam compared to a limit of $A < 0.8\%$ from the fragmentation of a $^{48}$Ca beam.

Our $^6$Li and $^7$Be secondary projectiles have smaller spins than any of these isomer studies and involved significant nucleon loss from the primary $^{16}$O projectile. As such we do not expect any appreciable alignment, at most just a few percent. Fragments at the peak of the momentum distribution were selected for the $^7$Be beam in order to maximize its intensity. Therefore any alignment should be positive. On the other hand, the $^6$Li beam was a “contaminant” and its yield was far from maximized with a momentum cut away from the peak value. Therefore the expected beam alignment should be even smaller or perhaps negative. However both beams produce alignment of $A \sim 50\%$ for their excited states thus suggesting the initial beam alignment was unimportant.

Even if our beams were strongly aligned for some unknown reason, one still needs to transfer more aligned angular momentum to the projectile to obtain the larger spin values of the excited states. Clearly if this transfer comes from changes in the projectile’s orbital angular moment it is not appropriately aligned in contrast to the proposed target spin-flip mechanism. Thus we conclude that the possible presence of some non-uniformity in the projectile’s magnetic-substate distribution is likely to be small and irrelevant.

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