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Neutron angular correlations in spontaneous and neutroninduced fission

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Phys. Rev. C **90**, 064623 — Published 30 December 2014

DOI: 10.1103/PhysRevC.90.064623

Study of neutron angular correlations in spontaneous and neutron-induced fission

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 (Dated: November 24, 2014)

Background Neutron emission is correlated in fission events because, on average, more than one neutron is emitted per fission. Measurements of these correlations, couple with studies of more inclusive observables such as neutron multiplicity, provide sensitive information about the fission mechanism. Neutron-neutron angular correlations have been studied both in spontaneous fission of ²⁵²Cf and neutron-induced fission of ²³⁵U. These correlations, until recently incalculable in most available simulations of fission, can now be calculated in event-by-event simulations of fission.

Purpose Phenomenological studies of fission are of interest both for basic science and for practical applications. Neutronneutron angular correlations are characteristic of the fissioning isotope and could be used in material identification.

Method We use our model of complete fission events, FREYA, to first study the sensitivity of two-neutron angular correlations to the model inputs and then compare to available data. We also compare our simulations to neutron-fragment angular correlations.

Results We find that the correlations calculated with FREYA are fairly robust with respect to the input parameters. Any strong deviations in the correlations result in poor agreement with measured inclusive neutron observables such as neutron multiplicity as a function of fragment mass and the neutron multiplicity distribution. The agreement of FREYA with the present set of correlation data is found to be good.

Conclusions FREYA can be used to reliably predict neutron-neutron angular correlations and could then be used to identify materials.

I. INTRODUCTION

Neutron-neutron correlations as a function of the angle between the two emitted neutrons, θ_{nn} , are an observable studied early in the history of fission measurements. These correlations do not require simultaneous measurement of the fission fragments. Another early observable that does depends on detecting both a neutron and the fission fragment is the study of the angular correlation between emitted neutrons and the light fission fragment, θ_{nL} . Taken together, these two observables are sensitive to the characteristics of neutron emission and are useful for testing models of neutron emission.

The first of the neutron-neutron angular correlation measurements dates as far back as 1948, by DeBenedetti et al. [1]. They bombarded a ²³⁵U source with fast neutrons. The neutrons were detected by proportional counters placed at different angles around the source. The also took a calibration measurement of the ratio of neutron coincidences at 90° and 180°. They tried to account for cross correlations between detectors due to rescattering where a neutron producing a recoil in one counter is scattered into an adjacent detector. To do this, they used a Pb-Be source emitting single neutrons so that all observed neutron coincidences arise from only one neutron. They assumed that the same number of rescattering coincidences from the Pb-Be source also arise from the ²³⁵U source. With this assumption, they found a flat correlation for $\theta_{nn} < 90^{\circ}$ and an increase above 90° . They concluded that the neutrons are preferentially emitted in opposite directions by opposite fragments. Since most later experiments have observed a finite signal at $\theta_{nn} = 0^{\circ}$, they may have overestimated this background for their source.

Neutrons are generally assumed to be emitted isotropically in the rest frame of the decaying fragment. When boosted to the laboratory frame, where observations are made, the neutrons thus move in the same direction as the fragments. If one neutron is emitted from each of the two fragments, the correlation is back-to-back, $\theta_{nn} = 180^{\circ}$, because energy-momentum conservation requires the fragments to move in opposite directions after scission. If both neutrons come from the same fragment, then they appear at $\theta_{nn} = 0^{\circ}$. These are the only neutron sources if one assumes neutrons are emitted only from the fully-accelerated fragments and not before. However, there is also a possibility that neutrons are emitted from the nucleus before scission [2–5] or during acceleration of the fragments [6]. A number of the later experiments measuring neutron-neutron angular correlations were motivated by the search for these scission neutrons.

The measured correlations have been simulated assuming the existence of these scission neutrons. Thus they assume three neutron sources: the scissioning nucleus and the light and heavy fission fragments. Scission neutrons are emitted isotropically in the rest frame of the nucleus undergoing scission, equivalent to the laboratory frame in this case. There is then no boost and the correlation between two neutrons emitted at scission is independent of θ_{nn} . This is also the case if one of the neutrons comes from a fragment and the other is a scission neutron. This additional neutron source then leads to a flatter correlation than assuming no scission neutrons [7]. Previous simulations of these correlations assume a 0-20% contribution to the neutron multiplicity from scission neutrons. They also assume, in addition to isotropic neutron emis-

sion in the emitter rest frame, that the neutron energy spectrum is the same for all neutrons and is independent of the number of neutrons emitted from a given fragment. The two fragments are assumed to have a common temperature for neutron emission and all emission is assumed to be independent and thus uncorrelated.

Another neutron-related angular correlation is that between a neutron and the light fragment. While the identity of the light fragment can be determined with fragment detectors, it is unknown whether the detected neutron comes from the light or the heavy fragment. Nonetheless measurements show a strong peak at $\theta_{nL} = 0^{\circ}$. The first such measurement was by Bowman *et al.* [2] and, more recently, by Gagarski *et al.* [7] in 2008.

For the first time, with our model FREYA, these angular correlations are calculated with a complete event-byevent Monte Carlo with a temperature that changes with each neutron emitted. The fission model FREYA (Fission Reaction Event Yield Algorithm) incorporates the relevant physics with a few key parameters determined by comparison to data [8–10]. It simulates the entire fission process and produces complete fission events with full kinematic information on the emerging fission products and the emitted neutrons and photons, incorporating sequential neutron and photon evaporation from the fission fragments. The event-by-event nature of FREYA makes it straightforward to extract the angular correlation between two evaporated neutrons [1, 7, 14–16] and between an evaporated neutron and the light fission fragment [2], neither of which can be addressed with standard fission models.

We describe the inputs to FREYA that could affect the shape of these correlations in Sec. II. We then discuss the sensitivity of the neutron-neutron angular correlation result to these inputs in Sec. III. In Sec. IV we make comparison to available data on neutron-neutron angular correlations (Sec. IV A) and neutron-light fragment angular correlations (Sec. IV B). We summarize our findings in Sec. V.

II. INPUTS

FREYA relies on data-related inputs of the fission yields, Y(A), as a function of energy (for neutron-induced fission) and total fragment kinetic energy, TKE. Additionally, the Gaussian widths of the fragment charge distributions depend on previous measurements [10]. There are some universal inputs including ground-state masses, taken from data [17] and supplemented by theory [18] when required; fission barrier heights; and pairing energies and shell corrections. FREYA also has several input parameters that can depend on the identity of the fissile nucleus. These include:

dTKE, the shift of the measured TKE required to match the average neutron multiplicity;

 e_0 , the asymptotic level density parameter;

- x, the advantage in excitation energy given to the light fragment;
- c, the relative thermal fluctuations in the fragment temperature distribution;
- Q_{\min} , the energy above the neutron separation energy where photon emission begins to dominate over neutron emission; and
- c_S , the ratio of the 'spin temperature' to the scission temperature.

In the remainder of this section, we introduce these inputs more fully and describe the consequences of varying these inputs on neutron observables.

We use a parameterization of the level density parameter based on the back-shifted Fermi gas (BSFG) model [19],

$$\tilde{a}_i(E_i^*) = \frac{A_i}{e_0} \left[1 + \frac{\delta W_i}{U_i} \left(1 - e^{-\gamma U_i} \right) \right] \tag{1}$$

where $U_i = E_i^* - \Delta_i$ and $\gamma = 0.05$ [20]. The pairing energy of the fragment, Δ_i , and its shell correction, δW_i , are tabulated in Ref. [19] based on the mass formula of Koura et~al. [21]. We take e_0 as a model parameter in both cases. We note that if the shell corrections are negligible, $\delta W \approx 0$, or the available energy, U, is large, then this renormalization is immaterial and the BSFG level-density parameter is proportional to the mass, $\tilde{a}_i \sim A_i/e_0$. In Ref. [10], we found $e_0 \sim 10/\text{MeV}$ which we use in these studies for all fissile actinides. To test the effect of the choice of e_0 on the neutron angular correlations, we will vary e_0 by 20%, between 8/MeV and 12/MeV.

If the two fragments are in mutual thermal equilibrium, $T_L = T_H$, the total excitation energy will, on average, be partitioned in proportion to the respective heat capacities which in turn are proportional to the level density parameters, i.e. $\overline{E}_i^* \sim \tilde{a}_i$. FREYA therefore first assigns average excitation energies based on such an equipartition,

$$\acute{E}_{i}^{*} = \frac{\tilde{a}_{i}(\tilde{E}_{i}^{*})}{\tilde{a}_{L}(\tilde{E}_{L}^{*}) + \tilde{a}_{H}(\tilde{E}_{H}^{*})} \overline{\text{TXE}} , \qquad (2)$$

where $\tilde{E}_i^* = (A_i/A_0)\overline{\text{TXE}}$. Subsequently, because the observed neutron multiplicities suggest that the light fragments tends to be disproportionately excited, the average values are adjusted in favor of the light fragment

$$\overline{E}_L^* = x \acute{E}_L^* \ , \ \overline{E}_H^* = \overline{\text{TKE}} - \overline{E}_L^* \ , \tag{3}$$

where x is an adjustable model parameter expected be larger than unity. We find x=1.3 agrees well with $\nu(A)$ for $^{252}\mathrm{Cf}(\mathrm{sf})$ while x=1.2 is used for $^{235}\mathrm{U}(n,\mathrm{f})$ [11]. To test the effect of the choice of x on the correlation observables, we will vary x for $^{252}\mathrm{Cf}$ by $\sim 30\%$, between 1 and 1.6. We also test the effect of taking x<1, using

x = 0.75. Since this parameter has a strong effect on the calculated $\nu(A)$, we also show how this observable changes with x.

After the mean excitation energies have been assigned, FREYA considers the effect of thermal fluctuations. In Weisskopf's statistical model of the nucleus, which considers the excited nucleus as a degenerate Fermi gas, the mean excitation of a fragment is related to its temperature T_i by $\overline{E}_i^* = \tilde{a}_i T_i^2$ [22–24] and the associated variance in the excitation is $\sigma_{E_i}^2 = -\partial^2 \ln \rho_i(E_i)/\partial E_i^2 = 2\overline{E}_i^* T_i$. Therefore, for each of the two fragments, we sample a thermal energy fluctuation δE_i^* from a Gaussian distribution of variance $2c\overline{E}_i^*T_i$ and modify the fragment excitations accordingly, arriving at

$$E_i^* = \overline{E}_i^* + \delta E_i^* , i = L, H. \tag{4}$$

Due to energy conservation, there is a compensating opposite fluctuation in the total kinetic energy, so that

$$TKE = \overline{TKE} - \delta E_L^* - \delta E_H^* . \tag{5}$$

The factor c multiplying the variance can, in principle, be tuned to the neutron multiplicity distribution $P(\nu)$. As a default value, used in our previous work, we take c=1.0. We vary c by 20%, between 0.8 and 1.2. Since $P(\nu)$ is also sensitive to this quantity, we will show the effect of changing c on $P(\nu)$ for 252 Cf(sf).

We generally assume that neutron emission continues until no further neutron emission is energetically possible, i.e. when $E_d^* < S_n + Q_{\min}$, where S_n is the neutron separation energy in the prospective daughter nucleus, $S_n = M(^{A_d}Z_d) - M(^{A_d-1}Z_d) - m_n$. We have chosen $Q_{\min} = 0.01$ MeV so that neutrons can be emitted even if the energy is very close to the neutron separation energy. We will take this as the default and raise it to 1 MeV to see how the correlations are affected.

In Ref. [13], we introduced the possibility for the fissile nucleus to have some initial angular momentum. In addition to the rigid rotation of the dinuclear configuration prior to scission, assumed to be inherited by the fragments, the fragments also acquire fluctuations around the rigid rotation axis. Of these fluctuations, the wriggling and bending modes, with rotating in the same or opposite sense around an axis perpendicular to the dinuclear axis. We assume that these fluctuations are statistically excited during scission. Thus, in each event, the values of s_{\pm} , the spin of the normal modes (the plus refers to wriggling modes (with parallel rotations) while the minus refers to bending modes (with opposite rotations)) are being sampled from distributions of the form

$$P_{\pm}(\mathbf{s}_{\pm} = (s_{+}^{x}, s_{+}^{y}, 0)) ds_{+}^{x} ds_{+}^{y} \sim e^{-s_{\pm}^{2}/2\mathcal{I}_{\pm}T_{S}} ds_{+}^{x} ds_{+}^{y}, (6)$$

where the "spin temperature" T_S is regarded as a global but somewhat adjustable parameter. We take $T_S = c_S T_{\rm sc}$ where $T_{\rm sc}$ is the scission temperature. As the default value, we use $c_S = 1$ which corresponds to assuming that the spin degrees of freedom are fully equilibrated at

scission. This value of c_S yields $\overline{S}_L \sim 6.2\hbar$, $\overline{S}_H \sim 7.6\hbar$ in rather good agreement with the average energy of photons emitted in fission. As an alternative, we have also employed $c_S = 0.1$ to dial down the photon multiplicity; this yields $\overline{S}_L \sim 1.8\hbar$, $\overline{S}_H \sim 2.2\hbar$, eliminating most of the collective yrast photons. See Ref. [13] for details.

The moments of inertia, \mathcal{I}_{\pm} , depend on the moments of inertia of the light and heavy fragments, \mathcal{I}_L and \mathcal{I}_H , as well as the moment of inertia of the relative fragment motion, \mathcal{I}_R . We use the rigid rotator moment of inertia, $\mathcal{I} = (c_I/5)MR^2$ where M and R are the mass and radius of the fragment, $R = r_0 A^{1/3}$. We use the commonly accepted value of $c_I = 0.5$ [12, 13] and leave it fixed since it only affects the photon observables.

III. SENSITIVITY OF NEUTRON-NEUTRON ANGULAR CORRELATIONS TO INPUTS

We first study the robustness of the correlation observable by changing the input parameters one at a time from their default values of x = 1.3, $e_0 = 10/\text{MeV}$, $c_S = 1$, $Q_{\min} = 0.01 \text{ MeV}$ and $c = 1 \text{ for } ^{252}\text{Cf(sf)}$. We do not change dTKE from its value of 0.5 MeV with $c_S = 1$ because most of the changes we make do not strongly affect the calculated $\overline{\nu}$. We also do not change c_I because changing c_I only has an effect on the photon observables, the effect on the neutron observables is negligible. The results are shown in Fig. 1 for neutrons emitted during spontaneous fission of ²⁵²Cf. We choose ²⁵²Cf(sf) because these correlations have been studied most for this system. We employ a minimum neutron energy of $E_n = 0.5 \text{ MeV}$ for both emitted neutrons. Increasing the minimum neutron energy tends to enhance correlation at $\theta_{nn} = 0^{\circ}$ while giving only a negligible change at $\theta_{nn} = 180^{\circ}$, see Ref. [11].

Figure 1(a) shows the sensitivity of the correlation to the parameters most closely related to the photon observables, c_S and Q_{\min} . Changing c_S from 1 to 0.1 reduces the initial spin from $\sim 7\hbar$ to $\sim 2\hbar$. The higher value, $c_S = 1$, is most compatible with previous extractions of fragment spins at scission [13]. The two calculations effectively coincide, thus the correlation is insensitive to this parameter. Changing the minimum energy for neutron emission relative to the separation energy, $S_n + Q_{\min}$, from $Q_{\min} = 0.01$ MeV, effectively allowing neutron emission to dominate down to $\sim S_n$, to 1 MeV has a small effect on the correlation, reducing the value at $\theta_{nn} = 180^{\circ}$ somewhat and making the correlation slightly more symmetric around $\theta_{nn} = 90^{\circ}$. The higher value of Q_{\min} is more compatible with the energy spectra of photon emission, see Ref. [12]. Therefore, while these parameters do not have a strong effect on the neutron-neutron angular correlation, they do have an important effect on photon observables.

The most striking effect on the shape of the neutronneutron angular correlation is the partition of the excitation energy between the light and heavy fragments.

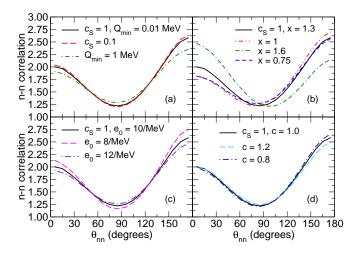


FIG. 1: (Color online) The angular correlation between two neutrons emitted from ²⁵²Cf(sf) as a function of the opening angle between the two neutrons, θ_{nn} . The FREYA results are shown for neutron kinetic energies E > 0.5 MeV. The results of different parameter choices in FREYA are compared to the default results: $c_S = 1$, $Q_{\min} = 0.01$ MeV, x = 1.3, $e_0 = 10/\text{MeV}$, and c = 1. (a) Parameters affecting photon emission are varied. The dashed red curve is with $c_S = 0.1$, $Q_{\min} = 0.01$ MeV while the dot-dashed green curve is with $c_S = 1$, $Q_{\min} = 1$ MeV. (b) The parameter affecting the relative excitation energy of the light fragment, x, is varied. The dot-dot-dashed red curve is the result for x = 1, equal partition between the light and heavy fragments. The dotdashed-dashed green curve shows the result when giving the light fragment even more energy, x = 1.6, while the dashed blue curve shows a result with x = 0.75, with more excitation given to the heavy than to the light fragment. (c) The parameter governing the level density is varied. The dashed magenta curve is with $e_0 = 8/\text{MeV}$ while the dot-dashed maroon curve is with $e_0 = 12/\text{MeV}$. (d) The parameter governing thermal fluctuations is varied with c = 1.2 (dashed turquoise curve) increasing the width of the fluctuation while c = 0.8(dot-dashed blue) decreases it.

Changing x while keeping $x \ge 1$ has a somewhat larger effect at $\theta_{nn} = 0^{\circ}$ than changing Q_{\min} but the difference is not large. the difference is not large. The small-angle enhancement for neutrons coming from the same fragment is larger for those emitted by the light fragment because of its higher velocity from the Coulomb repulsion at scission. Furthermore, the relative magnitude of the small-angle and large-angle enhancements evolves at the energy sharing is changed, due to the change in the origin of the emitted neutrons. Thus, for x = 1.6 when the light fragment has a large excess energy, the peak at $\theta_{nn} = 0^{\circ}$ is higher than the peak at $\theta_{nn} = 180^{\circ}$, and the angular correlation function tilts steadily in favor of the 180° peak as x is decreased. Such a large dependence on x should appear also in other observables and may provide a bound on how much x can be varied and still agree with data on other observables.

In Fig. 2, we show $\nu(A)$ for the same values of x as in Fig. 1(b), x = 0.75, 1, 1.3 and 1.6. For the default value

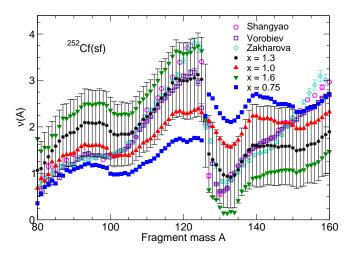


FIG. 2: (Color online) The variation of $\nu(A)$ with the parameter governing the partition of the excitation energy between the two fragments, x, is compared to data [25–27]. The default result, black stars, including bars representing the variance in A for fragment Z, is shown by the magenta stars. The results with x=1 (solid red, upward triangles), x=1.6 (solid green, downward facing triangles), and x=0.75 (blue stars) do not show the variances.

of x = 1.3, we also show the variance in $\nu(A)$ over the range of possible Z values for each A for FREYA. We also show several sets of recent data which agree well with each other. The agreement of our default calculations with these data are quite good for 105 < A < 145, covering the symmetric region and the A range where the yields are highest. To improve the overall agreement, we would have to introduce an A dependent temperature distribution, as has been done in some other calculations [28, 29] or point-by-point yields for each fragment pair [30]. Increasing x to 1.6 increase $\nu(A)$ for the light fragment to well above the data while underestimating the neutron multiplicity for the heavy fragment. It enhances the difference in neutron emission between A = 120 and 132. Taking x=1 decreases the variation of $\nu(A)$ considerably. While it actually improves agreement with the data for A < 100, the edge of the sawtooth is not sufficiently sharp. Finally, x = 0.75 actually inverts the sawtooth shape, significantly underestimating the yield below symmetry while overestimating the neutron multiplicity for the heavy fragment. Thus while we can see some dependence of the correlation function on x, these variations can be ruled out by the data on $\nu(A)$.

Next, we show the dependence of the neutron-neutron angular correlation on the asymptotic value of the level density parameter, e_0 , in Fig. 1(c). Changing e_0 by $\pm 2/\text{MeV}$ modifies the correlation somewhat but generally less than changing Q_{\min} in Fig. 1(a). While the chosen range of e_0 is within the range of acceptable values, it is constrained by the shape of the prompt fission neutron spectrum, see e.g. Ref. [10].

Finally, we check the sensitivity of our results to the

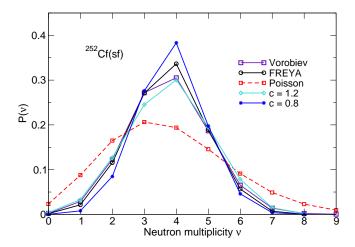


FIG. 3: (Color online) The variation in the neutron multiplicity distribution obtained from varying the thermal fluctuations, c. The data [31] (violet squares) are compared to the default (labeled FREYA) result as well as that with c=1.2 (turquoise diamonds) and c=0.8 (blue stars). The corresponding result for a Poisson distribution with the same average multiplicity is shown by the red dashed curve.

variance of the thermal fluctuations in Fig. 1(d). These fluctuations can modify the intrinsic excitation energy and thus the neutron multiplicity distribution, $P(\nu)$, see Fig. 3. While changing c has a negligible effect on the correlation function, it has a stronger effect on $P(\nu)$. Increasing c to 1.2 broadens $P(\nu)$ relative to the data while decreasing it to 0.8 narrows the multiplicity distribution relative to the data. Thus significant changes of c can be ruled out.

IV. COMPARISON TO DATA

Here we take our default values for FREYA, shown as the solid black curve in Fig. 1 for neutron-neutron angular correlations in ²⁵²Cf(sf), and compare to available data. We first compare to existing neutron-neutron angular correlation data in Sec. IV A. We focus on ²⁵²Cf(sf) data from Pringle and Brooks [15] and then from Gagarski et al. [7]. Our calculations have also been compared to the recent ²⁵²Cf(sf) data of Pozzi et al. and appear in Ref. [16]. Therefore we do not reproduce them again here but rather refer the reader to their work. We also compare to the $^{235}\mathrm{U}(n_{\mathrm{th}},f)$ data of Franklyn et al. [14]. In Sec. IVB, we compare our calculations of neutronlight fragment angular correlations to ²⁵²Cf(sf) data from Bowman et al. [2] and Gagarski et al. [7]. Some of these early data have also been compared to Monte Carlo studies albeit not with complete events [32].

A. Neutron-Neutron Angular Correlation Data

As we have already discussed, prompt neutrons from fission tend to be either forward or backward correlated. We have considered three separate neutron sources: both neutrons from the light fragment, both from the heavy fragment, and one neutron emitted from each fragment. We do not include scission neutrons as a source. In Ref. [33], we analyzed $^{239}Pu(n_{\rm th},f)$ for $\nu=2$ and found a significant correlation at $\theta_{nn} = 0^{\circ}$ when both neutrons are emitted from the same fragment, with a higher peak when both neutrons are emitted from the light fragment, due to its higher velocity. On the other hand, when one neutron is emitted from each fragment, there is a peak at $\theta_{nn} = 180^{\circ}$. The overall result is a stronger backward correlation because emission from both fragments is most likely. Indeed, the backward correlation is strongest when the overall neutron multiplicity is low since large multiplicities reduce the angular correlation [11]. This is because larger overall neutron multiplicities make it likely that more than one neutron is emitted by each fragment.

As we will see, the agreement of our calculations with the data is quite good without requiring a contribution from scission neutrons.

1.
252
 Cf(sf)

An early neutron-neutron angular correlation measurement was performed by Pringle and Brooks in 1975 [15]. They used two liquid scintillator neutron detectors and employed pulse-shape discrimination to reject photon events. One detector was fixed in the horizontal plane with the source while the second detector was rotated around the vertical axis. At $\theta_{nn} < 45^{\circ}$ the distance between the detector and the source was increased and shielding was inserted to reduce neutron rescattering. The minimum detected neutron energy was 0.7 MeV [15].

The more recent measurement by Gagarski et al. [7] was published in 2008. They used a similar setup of two neutron detectors with varying angular difference around the source. The detectors were stilbene crystals with photomultiplier tubes surrounded by shielding. They used time-of-flight to separate neutrons from photons. They showed that they could achieve neutron and photon separation with the photomultiplier tubes down to the detector threshold. By changing the event selection boundaries, they were able to employ several different neutron detection thresholds: 0.425, 0.55, 0.75, 0.8, 1.2 and 1.6 MeV [7].

The Gagarski measurement for the 0.75 MeV neutron threshold was compared to the Pringle and Brooks measurement at 0.7 MeV in Ref. [7]. They found relatively good agreement between the two measurements at $\theta_{nn} < 90^{\circ}$ but the Gagarski result shows a stronger backto-back threshold than that of Pringle and Brooks, see Fig. 4. The difference between the two measurements was

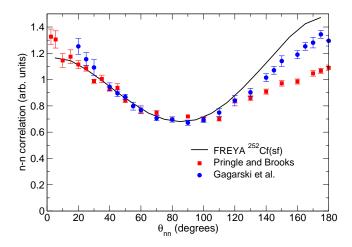


FIG. 4: (Color online) The default FREYA calculations are compared to ²⁵²Cf(sf) two-neutron angular correlation data from [15] (red squares) and [7] (blue circles) for neutron kinetic energies greater than 0.7 MeV.

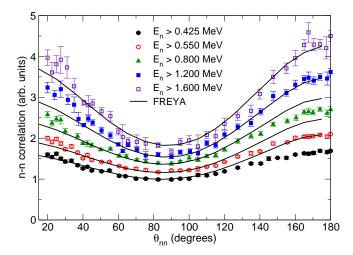


FIG. 5: (Color online) The default FREYA calculations are compared to 252 Cf(sf) two-neutron angular correlation data from [7] for neutron kinetic energies greater than 0.425, 0.55, 0.8, 1.2 and 1.6 MeV.

noted in Ref. [7] but no reason for the discrepancy was proposed. The 0.05 MeV difference in energy thresholds is too small to account for it.

Figure 4 also shows the FREYA result. The calculation agrees well with both data sets at $\theta_{nn} < 90^{\circ}$ but overestimates the back-to-back correlation at larger angles. Our calculation is relatively close to the Gagarski result although it is slightly above. Given that increasing Q_{\min} was seen to decrease the calculated correlation at $\theta_{nn} \to 180^{\circ}$, taking a higher Q_{\min} would improve our agreement with the data.

Our results are compared to the Gagarski et al. data with their other energy thresholds in Fig. 5. We again see that the agreement between the calculation and the data is very good for $\theta_{nn} < 90^{\circ}$ while the calculation

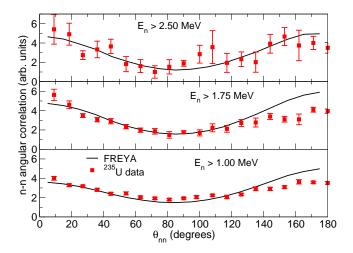


FIG. 6: (Color online) The default FREYA calculations are compared to $^{235}\mathrm{U}(n_{\mathrm{th}},f)$ two-neutron angular correlation data from [14] for neutron kinetic energies greater than 1.0 MeV (bottom), 1.75 MeV (center) and 2.5 MeV (top).

overestimates the back-to-back peak for neutrons with kinetic energies less than 1 MeV. The improvement of the agreement between the calculations and the data at higher neutron energy thresholds suggests that the dependence of the correlation on Q_{\min} may diminish with neutron energy.

2.
$$^{235}U(n,f)$$

In 1978 Franklyn, Hofmeyer and Mingay [14] studied neutron-neutron angular correlations in $^{235}\text{U}(n_{\rm th},f)$. They used two stilbene neutron detectors and employed pulse-shape discrimination to reject photon events. The used boron-loaded shadow shields to suppress neutron rescattering effects at low θ_{nn} . They obtained correlation results for minimum neutron energies of 1.0, 1.75 and 2.5 MeV. The lower limit on the neutron kinetic energy was imposed by the pulse-shape discriminator [14].

These data are compared to our default FREYA calculations for $^{235}\mathrm{U}(n_{\mathrm{th}},\mathrm{f})$ in Fig. 6. The agreement is generally rather good for $\theta_{nn}<140^\circ$ with $E_n\geq1.0$ and 1.75 MeV where our results again overestimate the backto-back correlation somewhat. For $E_n\geq2.5$ MeV, the agreement is good over all θ_{nn} , again suggesting that we should employ a larger value of Q_{\min} .

B. Neutron-light fragment angular correlations

In 1962 Bowman *et al.* made the first measurement of correlations between neutrons and light fragments [2]. Their setup consisted of two neutron detectors and two fission fragment detectors, both plastic scintillators of different thickness, mounted around a steel drum of 2 m diameter. A 252 Cf(sf) source was placed at the center of

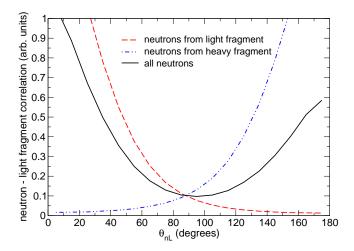


FIG. 7: (Color online) The default FREYA calculations are shown for ²⁵²Cf(sf) neutrons correlated with the light fragment. The neutrons emitted from the light fragment (dashed red) and those emitted from the heavy fragment (dot-dot-dashed blue) are compared to the correlation of all neutrons with the light fragment. All neutrons have a minimum kinetic energy of 0.5 MeV.

the drum and put under vacuum. The fragment detectors were mounted on opposite sides of the drum, at 180° from each other. One neutron detector was held fixed at $\theta_{nn}=11.25^{\circ}$ while the other was moved through angles 22.5° to 90° with respect to one fragment detector (111.5° to 180° relative to the other fragment detector). Time of flight was used to detect one neutron in coincidence with two fission fragments as well as to separate the light and heavy fragments from each other. They presented the angular correlation between all measured neutrons and the identified light fragment. While the correlation is made with the light fragment, it was not possible to determine which fragment emitted the neutron [2].

In Fig. 7, we show how the neutron-light fragment angular correlation is built up in FREYA. The dashed curve shows the result if all neutrons come from the light fragment. There is a strong peak at $\theta_{nLF}=0$ with essentially no signal in the opposite direction. If all detected neutrons arise from the heavy fragment, the correlation is effectively reflected around $\theta_{nLF}=90^{\circ}$. The shape of the correlation from all emitted neutrons retains the largest peak at zero degrees while, in the backward direction, the signal is reduced. This is because more neutrons are emitted by the light fragment because it gets more intrinsic excitation energy.

We compare the measurements of Bowman $et\ al.$ [2] and also Skarsvag and Bergheim [3] (reproduced in

Gagarski et al. [7]) to our FREYA results in Fig. 8. The agreement of our correlation with the shape of the data is very good.

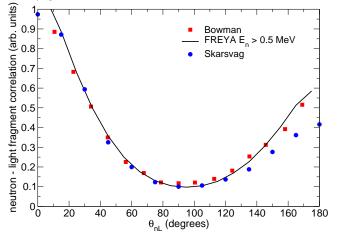


FIG. 8: (Color online) The default FREYA calculations are compared to ²⁵²Cf(sf) neutron-light fragment angular correlation data from [2] (red squares) and [3] (blue circles). The minimum kinetic energy of the neutrons is 0.5 MeV.

V. SUMMARY

We have shown that event-by-event models of fission, such as FREYA, provide a powerful tool for studying fission neutron angular correlations. The calculations are robust, being relatively insensitive to the input parameters which can be constrained by other data. The agreement of our calculations with the available data is good and does not lend strong support for the requirement of scission neutrons to explain the correlations. However, further data on these correlations based on fission of other isotopes and, for neutron-induced fission, at higher incident neutron energies would be welcome to help verify these results.

Acknowledgments

We wish to acknowledge helpful discussions with J. Lestone and S. Pozzi. This work was supported by the Office of Nuclear Physics in the U.S. Department of Energy's Office of Science under Contracts No. DE-AC02-05CH11231 (JR) and DE-AC52-07NA27344 (RV). We also gratefully acknowledge the Department of Energy, National Nuclear Security Administration, NA-22, for support.

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