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Azimuthal anisotropy in a jet absorption model with fluctuating initial geometry in heavy ion collisions

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The azimuthal anisotropy due to path-length dependent jet energy loss is studied in a simple jet absorption model that include event by event fluctuating Glauber geometry. Significant anisotropy coefficients $v_n$ are observed for $n = 1.2$ and $3$, but they are very small for $n > 3$. These coefficients are expected to result in a “ridge” for correlations between two independently produced jets. The correlations between the orientation of the $n$th-order anisotropy induced by jet absorption ($\Phi_{QP}$) and the $n$th-order participant plane ($\Phi_{PP}$) responsible for harmonic flow are studied. Tight correlations are observed for $n = 2$ in mid-central collisions, but they weaken significantly for $n \neq 2$. The correlations are positive for $n < 3$, but become negative in central collisions for $n > 3$. The dispersion between $\Phi_{QP}$ and $\Phi_{PP}$ is expect to break the factorization of the Fourier coefficients ($v_n$) into the single particle $v_n$, and has important implications for the high-$p_T$ ridge phenomena.

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\section{I. INTRODUCTION}

Recently, a lot of attentions are focused on the study of the azimuthal anisotropy of the particle production in heavy ion collisions at the Relativistic Heavy Ion Collider (RHIC) and the Large Hadron Collider (LHC). This anisotropy is usually expanded into a Fourier series:

$$\frac{dN}{d\phi} \propto 1 + 2 \sum_{n=1}^{\infty} v_n \cos n(\phi - \Phi_n)$$

with $v_n$ and $\Phi_n$ represent the magnitude and direction of $n$th-order anisotropy, respectively. At low $p_T$, $v_n$ is thought to be driven by the anisotropic pressure gradient associated with the initial spatial asymmetries, with more particles emitted in the direction of largest gradients \cite{1}. Asymmetries giving rise to non-zero $v_n$ are associated with either average shape (for $n = 2$) or shapes arising from spatial fluctuations of the participating nucleons \cite{2,3}. They can be characterized by a set of multipole components (also known as “eccentricities”), calculated from the participating nucleons at $(r, \phi)$ \cite{2}:

$$e_n = \sqrt{(r^2 \cos n \phi)^2 + (r^2 \sin n \phi)^2}.$$ 

The orientations of the minor axis for each moment $n$, also known as the participant plane (PP) are given by

$$\Phi_{PP} = \text{atan} 2((r^2 \sin n \phi), (r^2 \cos n \phi)) + \frac{\pi}{n}$$

When fluctuations are small and linearized hydrodynamics is applicable, each $v_n$ is expected to be independently driven by $e_n$ along $\Phi_{PP} \neq \Phi_n$ \cite{2}. This may not be true when the fluctuations are large, as the non-linear effects may lead to significant mixing between harmonic flow of different order \cite{2}. In this paper, linear hydrodynamics are assumed ($\Phi_{PP} = \Phi_n$) in order to facilitate the study of the correlations between $\Phi_n$ of different physics origins.

At high $p_T$ ($p_T \gtrsim 10$ GeV), the $v_n$ is thought to be driven by the path-length dependent energy loss of jets traversing the medium, with more particles emitted along the direction of shortest path-length, $\Phi_{QP}$ (QP stands for “quenching plane”, the direction of minimal jet attenuation) \cite{4,5}. Since jet quenching is influenced by the same geometry for flow, the direction of smallest jet attenuation is expected to be correlated with the direction of largest pressure gradient for flow. In fact, these two directions are often implicitly assumed to be the same in many theoretical calculations \cite{4,5-1}. An explicit study of the correlation between these directions can help clarifying this assumption.

In this paper, we estimate the high-$p_T$ anisotropy coefficients $v_n$ and $\Phi_{QP}$ using a jet absorption model with event by event fluctuating Glauber geometry. In multi-jet events with multiple hard-scattering processes, we show that the attenuation of jet yield lead to collimation of jet pairs at small relative angles and result in a near-side “ridge” in two-particle correlations (2PC) at high $p_T$. We study the correlations between $\Phi_{PP}$ and $\Phi_{QP}$, and show explicitly that these two angles are not the same. We explain how this angle mis-alignment influence the relation between the high-$p_T$ ridge and high-$p_T$ $v_n$. The experimental prospect for measuring the high-$p_T$ ridge is discussed in our model framework.

\section{II. MODEL}

We use a simple jet absorption/Glauber model of Ref. \cite{15} to calculate $v_n$ and $\Phi_{QP}$. This model has been used previously to study the centrality and path-length dependence of single particle suppression $R_{AA}$, dihadron
The suppression $I_{AA}$ and $v_2$. Back-to-back jet pairs are generated according to the binary collision density profile $(\rho_c)$ in the transverse $(xy)$ plane with random orientation. They are then propagated through the medium, whose density is given by the participant density profile $(\rho_p)$. Both profiles are generated with a Monte Carlo Glauber model with event by event fluctuation of positions of nucleons in Au ions [10]. The nucleons are sampled from a Woods-Saxon distribution with a radius of 6.38 fm and diffuseness of 0.535 fm, with a nucleon-nucleon cross-section of $\sigma = 42$ mb. In order to have smooth distributions for $\rho_c$ and $\rho_p$, the nucleons are assumed to have a Gaussian profile in transverse plane with a width of $r_0 = 0.4$ fm in $x$ and $y$ direction similar to Ref [10]. The value of $r_0$ is varied from 0.2-0.4 fm, and the nucleon is also assumed to be a uniform disk with a radius of $\sqrt{\sigma_{nn}/\pi}/2 = 0.58$ fm. However the final results are found to be insensitive to the details of the nucleon shape, except in peripheral collisions.

The jet quenching is implemented via exponential attenuation $f = e^{-\kappa I}$ for mid-rapidity, where the matter integral $I$ is calculated as:

$$ I_m = \int_0^\infty dl \frac{l^m}{l+l_0} \rho(\mathbf{r} + (l+l_0) \mathbf{v}) $$  \hspace{1cm} (4)

$$ \approx \int_0^\infty dl l^{m-1} \rho(\mathbf{r} + l \mathbf{v}), \quad m = 1, 2. \hspace{1cm} (5) $$

for jet generated at $\mathbf{r} = (x, y)$ and propagated along direction $\mathbf{v}$ with the same speed. They corresponds to $l^{m+1}$ dependence of absorption ($\propto l^m dl$) in a longitudinal expanding or 1+1D medium (x, $1/(l_0 + l)$ or 1D Hubble expansion) with a thermalization time of $l_0 = c\tau_0$. The $l_0$ is fixed to 0 by default, but we have checked the $v_n$ do not change much for $l_0 < 0.3$ fm [10]. The two cases, $m = 1$ and $m = 2$, are motivated for the $l$ dependence expected for radiative and AdS/CFT energy loss in 1+1D medium [17, 18], respectively.

The absorption coefficient $\kappa$ controls the jet quenching strength and is the only parameter in this calculation. It is tuned to reproduce $R_{AA} = \langle e^{-\kappa l_m} \rangle \sim 0.19$ for 0-5% $\pi^0$ data at RHIC after averaging over many Glauber events [10]. This leads to a value of $\kappa = 0.1473$ fm$^{-1}$ and 0.0968 fm$^{-2}$ for $m = 1$ and 2, respectively.

### III. RESULTS

The original impact parameter of the event is aligned along the $x$-axis.
centrality interval. Panels (a) and (b) shows the density profile for \( p_t \) and \( \rho_c \), respectively. Panel (c) shows the normalized probability distribution of \( I_1; P(I_1(\phi)) \), which is obtained by calculating \( I_1 \) over all possible di-jet production point \( \rho_c \) and jet propagation direction \( \phi \). This distribution exhibit characteristic high density and low density regions in \( (I_1, \phi) \) space, presumably reflecting spatial correlation between the \( \rho_c \) and \( p_t \) profiles. Panel (d) shows the normalized probability distribution of the attenuation \( e^{-\kappa L} \). Panel (e) shows the \( (e^{-\kappa L_1}) \) averaged along the \( y \)-axis in Panel (d) as a function \( \phi \), which is precisely the azimuthal angle dependent suppression \( R_{AA}(\phi) \). A clear anti-correlation can be seen between the peak magnitude of the \( R_{AA}(\phi) \) and breadth of the \( I_1 \) distribution in Panel (c). This distribution can also be obtained by randomly generating many di-jet pairs according the \( \rho_c \) and propagating them through \( p_t \) via Eq. [6] We expand it into a Fourier series:

\[
R_{AA}(\phi) = R_{AA}^0(1 + 2 \sum_{n=1}^{\infty} v_n^{QP} \cos(n(\phi - \Phi_n^{QP}))) , \tag{6}
\]
where \( R_{AA}^0 \) represents the average suppression, \( v_n^{QP} \) and \( \Phi_n^{QP} \) represent the magnitude and direction of \( n^{th} \)-order harmonic of emission probability distribution, respectively. Similar studies of \( R_{AA}(\phi) \) were pursued before in Ref. [12] for a pQCD energy loss in a event by event hydrodynamic underlying event. However it focused primarily on the influence of fluctuations on the event-averaged \( R_{AA}(\phi) \) distribution relative to the 2nd-order event plane (EP).

Figure 4 (f) shows a distribution calculated from \( \epsilon_n \) and \( \Phi_n^{QP} \):

\[
\epsilon(\phi) = 1 + 2 \sum_{n=1}^{\infty} \epsilon_n \cos(n(\phi - \Phi_n^{QP})) . \tag{7}
\]

It visualizes the shape of the initial geometry that is transformed into the final momentum anisotropy via either flow or jet quenching. A good alignment is seen between \( \Phi_n^{PP} \) and \( \Phi_n^{QP} \) for \( n \leq 3 \). It also shows that the large \( \epsilon_n \) for \( n > 3 \) are strongly damped after jet absorption, leading to very small values of \( v_n^{QP} \) for \( n > 3 \).

The study shown in Fig. 4 can be repeated for many events. We divide the simulation data into 5% centrality intervals, each containing about 2500 events. Figure 2 shows the distribution of \( \Phi_n^{PP} - \Phi_n^{QP} \) for two centrality intervals. Strong positive correlations are observed for \( n = 1, 2 \) and 3, while the correlations are rather weak or even become negative for \( n > 3 \).

In heavy ion collisions at RHIC and LHC, the \( v_n \) is usually measured from particle distribution relative to \( \Phi_n^{PP} \) via Eq. [11] [20]. However it has also been derived from the Fourier coefficients of two-particle correlation in relative azimuthal angle \( \Delta \phi = \phi - \phi_n^{QP} \) [21]:

\[
\frac{dN_{\text{pairs}}}{d\Delta \phi} \propto 1 + 2 \sum_{n=1}^{\infty} v_{n,n}(p_t^1, p_t^2) \cos n \Delta \phi , \tag{8}
\]

\( v_{n,n}(p_t^1, p_t^2) = v_n(p_t^1) v_n(p_t^2) . \tag{9} \]

The fact that the quenching plane and participant plane do not align exactly with each other implies that the \( v_n \), measured relative to \( \Phi_n^{QP} \), is not the same as those contributing to the 2PC in Eq. [8]. In other words, it is possible that the \( v_n \) obtained from single particle analysis is only a fraction of the true anisotropy resulting from jet quenching:

\[
v_n = v_n^{QP} \cos n(\Phi_n^{PP} - \Phi_n^{QP}) \tag{10}
\]

Since what is measured in experiment is the event plane not the PP, it is important to check whether the event plane align with QP or not, for example in a hydrodynamic model calculation.

Figure 3 (a) and (c) summarize the centrality dependence of \( v_n \) with \( n = 1–6 \) and for \( I_1 \) and \( I_2 \), respectively. Significant \( v_n \) signals are observed for \( n \leq 3 \), while higher-order \( v_n \) are usually smaller than 1%. The \( v_2^{QP} \) and \( v_4^{QP} \) all show strong centrality dependence, while the \( v_2^{QP} \) and \( v_3^{QP} \) show little centrality dependence for \( N_{\text{part}} > 100 \). Interestingly, the value of the \( v_1^{QP} \) is consistently larger than that for \( v_3^{QP} \), and it even exceeds \( v_2^{QP} \) value in most central collisions. This behavior suggest that the path-length dependence of energy loss and initial dipole asymmetry from fluctuations combine to produce a large \( v_1^{QP} \). This large \( v_1^{QP} \) is expect to contribute to the high-\( p_t \) \( v_1 \) signal observed by the ATLAS Collaboration [21]. Figure 3 also shows that the \( I_2 \) type of path-length dependence induces significantly larger \( v_n \) than that for \( I_1 \); the increase is almost a factor of two for \( n = 1 \) and \( n = 3 \). This is also observed in other studies before [11, 12].

Figure 4 (b) and (d) summarize the centrality dependence of \( \cos n(\Phi_n^{PP} - \Phi_n^{QP}) \) with \( n = 1–6 \) and for \( I_1 \) and \( I_2 \), respectively. As indicated by Eq. [10] this represents the reduction factor of the \( v_n \) when it is measured.
relative to the $\Phi_{PP}$.

The large anisotropy coefficients $v_i^{QP}$ also has important consequences for the "ridge" observed in two-particle correlations [21, 22]. This "ridge" is thought to be the result of the constructive contribution of harmonics at $\Delta \phi \sim 0$. In the literature, it is referred to as either the "soft-ridge" [21, 23] for soft-soft correlation or "hard-ridge" [22, 24] for soft-hard correlation, respectively. Here we show that the correlation between two independently produced high-$p_T$ jets can also produce the "ridge"-like structure. This "hard-hard ridge" can be calculated on a probability basis event-by-event by simply self-convoluting the $R_{AA}(\phi)$ distribution like Fig. 1 (c). Examples of these structures are shown in Fig. 3 for two representative events in both 0-5% and 20-25% centrality intervals. The magnitude of the ridge, as well as the away-side shape changes dramatically from event to event. They also changes a lot between the $I_1$ and $I_2$ types of path-length dependence jet absorption.

Figure 5 show the long-range structures (solid lines) obtained from the jet absorption model, averaged over many events. The ridge magnitude increases with centrality to about 1.5% (4%) for $I_1$ ($I_2$) path-length dependence in mid-central collisions. This signal should be measurable with the large statistics dataset from LHC. The dashed lines in Fig. 5 show the 2PC predicted...
This suggests the difference between the measured ridge and those predicted by the event plane method could be large and measurable.

IV. CONCLUSION

The anisotropy of high-p_T particle is studied in a simple jet absorption framework with event by event fluctuating geometry. The harmonic coefficients v_n are found to be significant for n = 1 - 3 (> 1%) but become very small for n > 3. The correlation between the quenching plane and participant plane are studied. A strong de-correlation is found for n = 2 in central collisions and for n = 1 and 3 over the full centrality range. The correlations become negative for n > 3 in central collisions. This de-correlation, if also confirmed between the event plane and the quenching plane (e.g via hydrodynamic model that has dijets embedded), is expected to break the global factorization of the two particle Fourier coefficient v_{n,n} into the v_n for the two single particles. It would also imply that the high-p_T v_n measured relative to the event plane could be significantly smaller than the true anisotropy from path-length dependent jet energy loss. These jet quenching v_n also give rise to long range “ridge” structure in two-particle correlations. The predicted ridge amplitudes is on the order of 0.5-4% depending on the centrality and functional form of the l dependence of the energy loss, and should be measurable at the LHC using the correlations between two high-p_T particles with a large rapidity separation. Our study bear some similarities to Ref. [14]. However, Ref. [14] uses a cumulant expansion framework instead of Monte Carlo Glauber model for initial geometry, and that it focus on the soft-hard ridge instead of the hard-hard ridge in our case.

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FIG. 5: (Color online) The expected long-range structures for correlations between two high p_T particles from two independent hard-scattering processes (solid lines) and those calculated from single particle v^{QP}_n relative to participant planes (dashed lines) for various centrality intervals. They are averaged distribution over many events for a given centrality intervals. The thick (thin) lines denote the I_1 (I_2) type of path-length dependence.

from the v_n measured relative to Φ^{PP}. Clearly the mis-alignments between Φ^{QP} and Φ^{PP} reduces the ridge magnitude. The reduction is almost 50% in most central collisions, but decrease to about 20% in mid-central collisions.