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# Electromagnetic transition rates in the N=80 nucleus $_{58}^{138}Ce$

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The half-life of the  $I^{\pi} = 6^+$  yrast state at  $E_x=2294$  keV in <sup>138</sup>Ce has been measured as  $T_{1/2}=880(19)$  ps using the fast-timing gamma-ray coincidence method with a mixed LaBr<sub>3</sub>(Ce)-HPGe array. The excited states in  $^{138}$ Ce have been populated by the  $^{130}$ Te( $^{12}$ C,4n) fusionevaporation reaction at an incident beam energy of 56 MeV. The extracted  $B(E2;6^+_1 \rightarrow 4^+_1) =$ 0.101(24) W.u. value is compared with the predictions of truncated basis shell model calculations and with the systematics of the region. This shows an anomalous behaviour compared to the neighbouring isotonic and isotopic chains. Half-lives for the yrast  $5^-$ ,  $11^+$  and  $14^+$  states in <sup>138</sup>Ce have also been determined in this work.

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#### INTRODUCTION I.

Electromagnetic transition rates in nuclei in the vicinity of closed shells can be used as a precision test of the restricted basis shell model and also provide information on the effective charges used as inputs to such calculations. The N=80 isotonic chain allows a consistent test of shell model predictions for proton numbers above the Z=50shell closure where the near-yrast states in such nuclei can be associated largely with configurations of well defined proton-particle/neutron-hole make up. The N=80isotonic chain exhibits yrast  $I^{\pi} = 10^+$  isomeric states in all its even-Z members from  $^{130}_{50}$ Sn up to  $^{148}_{68}$ Er [1–6], with this structure in the lighter isotones being associated with a predominantly  $\nu(h_{11/2})_{10^+}^{-2}$  maximally aligned configu-ration. In the case of the Z=56 [7] system, <sup>136</sup>Ba, the lower lying yrast states have been characterised by either negative parity states from neutron  $(h_{11/2} \otimes d_{3/2})$ or  $(h_{11/2} \otimes s_{1/2})$  configurations or positive parity from proton  $(d_{5/2})^2$ ,  $(g_{7/2})^2$  or  $(d_{5/2} \otimes g_{7/2})$  states. Both restricted basis shell model calculations and pair truncated shell model calculations [8] suggest a significant change in structure between the  $6^+$  and  $4^+$  yrast states in  $^{136}$ Ba, which gives rise to a relatively low  $B(E2; 6^+ \rightarrow 4^+)$  value in this nucleus [9].

The current paper investigates the yrast states of the N=80 isotone, <sup>138</sup>Ce and in particular focuses on the measurement of the yrast  $I^{\pi} = 6^+ \rightarrow 4^+$  reduced transition probability, which is used as a direct comparison for shell model calculations in the region. The decay halflives for other, yrast excited states of <sup>138</sup>Ce have also been established.

#### II. EXPERIMENTAL DETAILS

The fusion-evaporation reaction  $^{130}\text{Te}(^{12}\text{C},4\text{n})$  at a beam energy of 56 MeV was used to populate the excited states of  $^{138}$ Ce. The beam was provided by the Tandem van de Graaff accelerator at the National Institute for Physics and Nuclear Engineering, Bucharest, Romania. The target consisted of a  $1~{\rm mg/cm^2}$  thick enriched  $^{130}{\rm Te}$ foil on a 20 mg/cm<sup>2</sup> <sup>208</sup>Pb backing. The experiment was performed using a continuous DC beam over a period of 2.5 days, with an average on-target beam current of approximately 10 pnA. The production cross-section for the  ${}^{130}\text{Te}({}^{12}\text{C},4\text{n}){}^{138}\text{Ce}$  reaction was estimated using the PACE4 code [10] to be  $\sim 650$  mb.

The de-exciting  $\gamma$  rays were detected by an array of eight  $LaBr_3(Ce)$  scintillator detectors and eight hyperpure germanium detectors (HPGe) [11]. One of the HPGe detectors had an active Compton suppression shield while the other seven were unsuppressed. The HPGe detectors were placed in three angular rings; five detectors at backward angle  $\sim 143^{\circ}$  relative to the beam direction, two at  $\sim 90^{\circ}$  and one at a forward angle of ~43°. The LaBr<sub>3</sub>(Ce) detectors were positioned above (three) and below (five) the target-chamber at angles of ~45° with respect to the beam direction. The targetdetector distance was measured to be ~20 cm for all detectors. Three different sizes of LaBr<sub>3</sub>(Ce) crystal were used in the present work, having crystal dimensions of (a) (three) 2" × 2" cylindrical; (b) (three) 1.5" × 1.5" cylindrical and (c) (two) 1" × 1.5" conical. Typical full width at half maximum (FWHM) energy resolutions at 1.33 MeV were 2.2–2.8 keV and 30 keV for the HPGe detectors and LaBr<sub>3</sub>(Ce) detectors, respectively [12].

Data were collected in triple coincidence mode, such that (i) Ge-Ge-Ge or (ii)  $\text{LaBr}_3(\text{Ce})\text{-LaBr}_3(\text{Ce})\text{-Ge} \gamma$ -ray energy coincidences were measured. The coincidence master gate time window was ~50 ns. A total of ~4×10<sup>8</sup> LaBr<sub>3</sub>(Ce)-LaBr<sub>3</sub>(Ce)-Ge coincidences were recorded during the experiment for subsequent offline analysis.

#### III. DATA ANALYSIS

The data were sorted offline into a range of  $\gamma$ -ray energy and time difference coincidence matrices and cubes, such as those described in Ref. [11]. These were then interrogated offline using different,  $\gamma$ -ray energy conditions and analyzed with the GASPWARE [13] and RADWARE [14] packages. In order to correct for instrumental drifts of the  $LaBr_3(Ce)$  detectors, a run-by-run gain matching procedure was applied. Energy and efficiency calibrations for the response of the detectors in the array were performed using standard <sup>152</sup>Eu, <sup>137</sup>Cs and <sup>60</sup>Co point sources placed at the target position. The instrument time response for each  $LaBr_3(Ce)$  detector and constant fraction discriminator (CFD) combination in the mixed array required an offline correction for the low-energy time walk. In order to achieve this, the method described by Märginean *et al.* [11] was used.

Two-dimensional LaBr<sub>3</sub>(Ce)  $(E_{\gamma}-E_{\gamma})$  matrices and  $E_{\gamma 1}-E_{\gamma 2}-\Delta T$  cubes were created during the offline analysis. A 2D matrix (energy vs time difference) was constructed for the HPGe detectors and was used as offline software gating conditions for the LaBr<sub>3</sub>(Ce)  $E_{\gamma 1}$ - $E_{\gamma 2}$ - $\Delta T$  cubes. The  $I^{\pi} = 10^+$ ,  $T_{1/2} = 81(2)$  ns isomeric state in <sup>138</sup>Ce [15] provided discrete reference energy peaks in the 2D matrix. A condition that the LaBr<sub>3</sub>(Ce) ( $E_{\gamma}$ - $E_{\gamma}$ ) coincidence should be anticipated before the signal from the HPGe detectors was used to isolate  $LaBr_3(Ce)$  $(E_{\gamma}-E_{\gamma})$  coincidences associated with transitions below the  $I^{\pi} = 10^+$  isomeric state in <sup>138</sup>Ce. LaBr<sub>3</sub>(Ce) ( $E_{\gamma}$ - $E_{\gamma}$ ) coincidence signals arriving after that of the HPGe detectors were similarly used for transitions above the  $I^{\pi} = 10^+$  isomeric state. Figure 1 shows an example of this 2D matrix for one of the HPGe detectors. The software conditions applied to clean the LaBr<sub>3</sub>(Ce)  $E_{\gamma 1}$ - $E_{\gamma 2}$ - $\Delta T$  cubes are also indicated.

For the half-life measurements, two different techniques were used: (i) the centroid shift method [16, 17]

and (ii) a fit with a single exponential decay and a prompt response convolution for decays which are significantly longer than the LaBr<sub>3</sub>(Ce) timing resolution. The centroid shift method, as first introduced by Bay [18] was used in the present work in cases where the lifetime of the nuclear state was significantly shorter than the time resolution (full width at half-maximum) for the LaBr<sub>3</sub>(Ce) coincidences.

# IV. RESULTS

The partial level scheme of <sup>138</sup>Ce deduced in the current work is shown in Fig. 2. This is consistent with that reported by Bhattacharjee et al. [19]. Relative gammaray intensities have been measured and normalized with respect to the 789 keV  $(2^+ \rightarrow 0^+)$  transition. The total projection spectra of the  $E_{\gamma}$ - $E_{\gamma}$  coincidence matrices from the  $^{130}\text{Te}+^{12}\text{C}$  fusion-evaporation reaction are shown in Fig. 3 (a) where the black line is the total projection from HPGe detectors and the red line is the equivalent spectrum from the  $LaBr_3(Ce)$  detectors. Figure 3 (b) shows the total projection from the  $LaBr_3(Ce)$ detectors  $(E_{\gamma}-E_{\gamma})$  matrix with an anticipated HPGe timing gate for transitions below the  $I^{\pi} = 10^+$  isomer. The energy spectra shown in Figures 3 (c) and (d) were obtained by gating with the 815- and 77 keV transitions on the symmetric LaBr<sub>3</sub>(Ce)  $(E_{\gamma}-E_{\gamma})$  coincidence energy matrix, respectively, with an anticipated HPGe timing gate.

Figure 4 shows the half-life measurements obtained using the centroid shift method by gating on feeding and deexciting transitions across levels of interest in the sorted  $E_{\gamma 1}$ - $E_{\gamma 2}$ - $\Delta T$  cubes with additional timing conditions in the HPGe selecting  $\gamma$ -rays below or above the  $I^{\pi} = 10^+$  isomer in <sup>138</sup>Ce.

Figure 4 (a) presents the time spectra associated with the decay of the yrast  $I^{\pi} = 5^{-}$  state in <sup>138</sup>Ce. An extracted experimental half-life of  $T_{1/2}=450(30)$  ps was obtained from the centroid shift of the time distribution of (77, 390) (black line) and (390, 77) (red line) gates in the  $LaBr_3(Ce)$  detectors. Figure 4 (b) shows the time spectra of the  $I^{\pi} = 11^+$  yrast state which give a value of  $T_{1/2}=140(11)$  ps obtained from the centroid shift of the time distribution associated with the (418, 403) and (403, 403)418) coincident transitions. Figure 4 (c) shows the extracted half-life for the decay of the yrast  $I^{\pi} = 14^+$  state. A measured half-life of  $T_{1/2}=80(9)$  ps was obtained using the centroid shift for the two difference distributions gated on the (254, 338) and (338, 254) transitions. Figure 4 (d) corresponds to a prompt coincidence between the (1038, 789) and (789, 1038) pair and shows no measurable shift. The  $I^{\pi} = 2^+$  state half-life was measured previously to be 2.06(14) ps [20]. The FWHM time resolution of 460(10) ps was obtained by a Gaussian fit for the (1038, 789) coincidence. Figures 4 (e) and (f) show the time distributions associated with the  $I^{\pi} = 4^+$  and  $8^+$  yrast states. No measurable shift was observed which



FIG. 1: (Color Online) Two-dimensional energy vs time matrix for one of the HPGe detectors. The software gates used to select transitions below and above the  $I^{\pi} = 10^+$  isomeric state are also indicated.

indicates that the half-lives for the  $I^{\pi} = 4^+$  and  $8^+$  yrast states are shorter than 50 ps.

Figure 5 shows the measurement of the half-life of the yrast  $I^{\pi} = 6^+$  state, resulting from the time differences between (a) 815- and 467 keV (b) 815- and 165 keV and (c) 815-165 keV. The time difference spectra in (a) and (b) were fitted with an exponential decay convoluted with a Gaussian (FWHM=460(10) ps) and gave values of the half-life of the  $I^{\pi} = 6^+$  state of (a)  $T_{1/2}=860(60)$  ps and (b)  $T_{1/2}=920(25)$  ps respectively. Figure 5 (c) shows the time distributions for the decay of the  $I^{\pi} = 6^+$  state using the centroid shift method. The time distribution, which is plotted as a black line, is obtained with a (815, 165) energy gate, while the symmetric, time-reversed (165, 815) gate is plotted in red. The resulting half-life is consistent with that obtained from the exponential decay component. The measured half-lives of the  $I^{\pi} = 6^+$  yrast state are plotted versus the gating gamma-ray energy in Fig. 6. The solid line corresponds to the weighted average of these half-lives which has a value of  $T_{1/2} = 880(19)$  ps.

# V. DISCUSSION

The nucleus  ${}^{138}_{58}$ Ce<sub>80</sub> has eight valence protons outside the closed Z=50 shell and two neutron holes with respect to N=82. Table I summarises the decay half-lives obtained from the present work in  ${}^{138}$ Ce. These are discussed individually below:

# A. Half-life of the $6^+$ state at 2294 keV

The 2294 keV level has been previously identified in  $^{138}\text{Ba}(\alpha,4n\gamma)$  studies [21, 22] and has a well established spin and parity of  $I^{\pi} = 6^+$  [23] from angular distribution measurements. The state de-excites to the  $I^{\pi} = 5^-$  state



FIG. 2: The partial level scheme of  $^{138}$ Ce observed in the present work. The width of the arrows connecting the levels is proportional to the  $\gamma$ -ray intensities.

via an E1 transition with an energy of 77 keV. It also decays directly to the yrast  $I^{\pi} = 7^{-}$  state via another E1with a transition energy of 165 keV. A third decay branch from the yrast  $I^{\pi} = 6^{+}$  state is observed via a 467 keV E2 transition to the yrast  $I^{\pi} = 4^{+}$  state in <sup>138</sup>Ce. Also, it decays to the  $I^{\pi} = 4^{+}_{2}$  state via an E2 transition with an energy of 156 keV (see Fig. 2). Müller *et al.* [24] suggested that the  $I^{\pi} = 6^{+}$  state consists mainly of a  $\pi(d_{5/2} \otimes g_{7/2})$ or  $\pi(g_{7/2})^{2}$  configuration. The extracted half-life from the current work gives a B(E2)=0.101(24) W.u. for the 467 keV transition, B(E2)=9.5(25) W.u. for the 156 keV transition,  $B(E1)=3.2(8)\times10^{-5}$  W.u. for the 165 keV transition and  $B(E1)=1.1(4)\times10^{-4}$  W.u. for the 77 keV transition. E1 transitions are typically hindered by a factor of  $10^{4} - 10^{5}$  compared to their Weisskopf estimate.

The plot of the systematics of the  $B(E2; 6_1^+ \rightarrow 4_1^+)$  values for cerium and barium isotopes, shown in Fig. 7, indicates that the E2 transition to the  $I^{\pi} = 4_1^+$  level is more hindered than the corresponding B(E2) value for the N=82, magic nucleus <sup>140</sup>Ce.

A similar situation has been reported in <sup>136</sup>Ba [7] where  $B(E2; 6_1^+ \to 4_1^+) < B(E2; 6_1^+ \to 4_2^+)$ . This was interpreted by assuming that the  $I^{\pi} = 6^+$  and the  $I^{\pi} = 4_2^+$ states have similar configurations dominated by  $\pi(g_{7/2})^2$ and  $\nu(h_{11/2})^{-2}$  excitations [7].



FIG. 3: (Color Online) (a) Total projection for all HPGe and LaBr<sub>3</sub>(Ce) detectors. (b) Total projection for all LaBr<sub>3</sub>(Ce) detectors with "anticipated" HPGe timing gate. (c) and (d)  $\gamma$ -ray spectra obtained by gating with the 815 keV and 77 keV transitions in the symmetric LaBr<sub>3</sub>(Ce) ( $E_{\gamma}$ - $E_{\gamma}$ ) coincidence energy matrix with the "anticipated" HPGe timing gate.



FIG. 4: (Color Online) Time difference spectra for yrast states in <sup>138</sup>Ce, obtained using the centroid shift method showing the time difference between: (a) 77- and 390 keV, (b) 418and 403 keV, (c) 254- and 338 keV, (d) 1038- and 789 keV, (e) 390- and 1038 keV and (f) 430- and 815 keV transitions. Time difference spectra plotted with black lines, are gated on  $(E_{\gamma 1}, E_{\gamma 2})$ , while the red lines shows the reverse gating.

# B. Half-life of the $5^-$ state at 2217 keV

The two low-lying negative parity states (the isomer state  $I^{\pi} = 7^{-}$  at 2129 keV and  $I^{\pi} = 5^{-}$  at 2217 keV) shown in Fig. 2 are reported previously by Ludziejew-ski [22] who suggested that the  $I^{\pi} = 5^{-}$  state arises from the neutron configuration  $(d_{3/2}^{-1} \otimes h_{11/2}^{-1})$  with a  $(s_{1/2}^{-1} \otimes h_{11/2}^{-1})$  admixture which decays by E1 to the 4<sup>+</sup>



FIG. 5: (Color Online) Time spectra obtained in <sup>138</sup>Ce from the LaBr<sub>3</sub>(Ce)  $E_{\gamma 1}$ - $E_{\gamma 2}$ - $\Delta T$  cube with an anticipated HPGe gate showing the time difference between: (a) 815and 467 keV (b) 815- and 165 keV (c) (815, 165) and reversed (165, 815) energy gates using the centroid shift method. The continuous lines in (a) and (b) are Gaussian exponential convolution fits to the spectra. The dashed curve is a Gaussian prompt distribution (PRF) with FWHM=460(10) ps.



FIG. 6: (Color Online) The three measurements of the halflife of the  $I^{\pi} = 6^+$  yrast state from the time difference between 815 keV  $\gamma$ -ray and 77-, 165- and 467 keV  $\gamma$ -rays. The horizontal solid line indicates the weighted average of the three values and the dashed lines are the uncertainty.

state. The extracted B(E1) strength for the  $5^- \rightarrow 4^+$  transition is  $7.4(8) \times 10^{-6}$  W.u.

### C. Half-lives of higher-spin states

Bhattacharjee *et al.* [19] assigned the  $I^{\pi} = 11^+$  yrast state at an excitation energy of 3942 keV to decay by a mixed (M1 + E2) multipolarity transition with an energy of 403 keV based on angular distribution measurements. Since the exact value for the mixing ratio is unknown for this transition, the reduced transition probabilities assuming the limiting values of either pure M1or pure E2 have been calculated. A previous study [33]



FIG. 7: (Color Online) Systematics of  $B(E2; 6_1^+ \to 4_1^+)$  values for cerium and barium isotopes, <sup>126</sup>Ce [25], <sup>128</sup>Ce [26], <sup>130,132,134</sup>Ce [27], <sup>140</sup>Ce [28], <sup>126</sup>Ba [29], <sup>128</sup>Ba [30], <sup>130</sup>Ba [31], <sup>136</sup>Ba [7], <sup>138</sup>Ba [32]. The <sup>138</sup>Ce data point is obtained from the current work.

placed a half-life limit on the  $I^{\pi} = 11^+$  state of  $T_{1/2} \leq 1.5$  ns. The measured half-life of  $T_{1/2} = 140(11)$  ps from this work gives  $B(M1)=2.34(19)\times10^{-3}$  W.u. and B(E2)=8.2(7) W.u. for this transition.

The  $I^{\pi} = 14^+$  state at an excitation energy of 5312 keV is populated via a  $\Delta I = 1$  transition of 254 keV from the  $I^{\pi} = 15^+$  state. This state de-excites to the  $I^{\pi} = 13^+$ state via 338 keV transition. It also decays by a 98 keV transition to the  $I^{\pi} = 13^-$  state. In Ref. [19] the 338 keV transition was assigned to have pure *M*1 character. A half-life of  $T_{1/2} = 80(9)$  ps was obtained for the  $I^{\pi} = 14^+$  state using the centroid shift method in the current work (see figure 4). The resulting reduced transition strengths for the 338 keV and 98 keV transitions were calculated to be  $B(M1)=3.1(19)\times10^{-3}$  W.u. assuming a pure *M*1 multipolarity and  $B(E1)=1.9(4)\times10^{-3}$  W.u. respectively.

# VI. SHELL MODEL CALCULATIONS

Shell model calculations have been performed for <sup>138</sup>Ce and the closed shell system nucleus <sup>140</sup>Ce in the current work. These calculations used the NuShellX@MSU code [34], with the jj55pn model space and SN100PN interaction [35]. The SN100PN interaction was originally applied to magnetic moments near <sup>132</sup>Sn, obtaining good agreement with experiment for the N=80 isotones <sup>132</sup>Te and <sup>134</sup>Xe. The model space spans N, Z = 50 - 82, comprising the  $1g_{7/2}, 2d_{5/2}, 2d_{3/2}, 3s_{1/2}$  and  $1h_{11/2}$  orbitals. The proton single-particle energies, taken from states in <sup>133</sup>Sb, were -9.68, -8.72, -7.24, -7.34 (estimated) and -6.88 MeV for the  $1g_{7/2}, 2d_{5/2}, 2d_{3/2}, 3s_{1/2}, 1h_{11/2}$  states respectively. Similarly, the neutron single-hole energies were taken from states in <sup>131</sup>Sn, being -9.74, -8.97, -7.31, -7.62, and -7.38 MeV for the  $1g_{7/2}, 2d_{5/2}, 2d_{3/2}, 3s_{1/2}$ ,  $1h_{11/2}$  states respectively. The large number of valence nucleons for <sup>138</sup>Ce (8 protons, 2 neutron holes) necessitates a truncation of the full model space. This was done by forcing the proton  $1g_{7/2}$  orbit to contain a minimum of 4 protons. The remaining 4 protons and 2 neutron holes were unconstrained. Calculations for electromagnetic transition rates used the "standard" effective charges of  $e_{\pi} = 1.5e$  and  $e_{\nu} = 0.5e$ .

The calculated energy levels of the excited states are compared with experimental data in Fig. 8. At low energies the shell model calculations are in reasonable agreement with the experimental spectrum; the ordering and spacing of levels below the  $10^+$  state are in good agreement, though states above the yrast  $2^+$  are typically 100 keV lower than their experimental counterparts. The measured and calculated transition rates are summarised in Table I.

The wave functions for the states of interest are summarised in Table II and are found to be strongly mixed, with leading-order partitions typically contributing at the level of ~ 10 - 20%. This will be in part due to the large number of valence nucleons. For the transitions between the first  $I^{\pi} = 6^+$  state and the first and second  $I^{\pi} = 4^+$  states, there is disagreement with experiment. The shell model calculations predict the yrast transition is unhindered, with  $B(E2; 6^+ \rightarrow 4_1^+) = 0.967$  W.u., whereas the experimentally derived value is 0.101(24) W.u.. Conversely, the calculations in this shell model space predict the transition to the second  $4_2^+$  state is strongly hindered, with  $B(E2; 6^+ \rightarrow 4_2^+) = 0.008$  W.u., in contrast to the experimental value of 9.5(25) W.u.

For the corresponding yrast  $6^+$  to  $4^+$  transition in  $^{140}\mathrm{Ce},$  a similar, albeit smaller in absolute magnitude, overestimation of the B(E2) is found. Here the experimental transition strength is B(E2) = 0.29(6) W.u., whereas the shell model calculations in the same space as those for  $^{138}$ Ce yield 0.89 W.u.. In this case, the second  $4^+$  is at higher energy than the yrast  $6^+$ , which it does not directly decay to. Since the shell model calculations for  $N = 82^{-140}$ Ce only involve valence protons, a calculation in the unrestricted space is possible. A recent study by Srivastava et al. [37] using the full jj55pn model space reports a value of 0.15 W.u. for the yrast  $6^+ \rightarrow 4^+$  transition in <sup>140</sup>Ce, close to the experimental value of 0.29 W.u.. This suggests that the truncations applied to the model space in the present work, both for <sup>140</sup>Ce and <sup>138</sup>Ce, are (at least partially) responsible for the disagreement between the shell model predictions and experimental results for the B(E2) values in these isotopes.

#### VII. CONCLUSIONS

In summary, the half-life of the  $I^{\pi} = 6^+$  yrast state in <sup>138</sup>Ce has been measured to be 880(19) ps which corresponds to a rather hindered transition with  $B(E2; 6_1^+ \rightarrow 4_1^+) = 0.101(24)$  W.u. Unusually, the mea-

Nucleus	$E_x \text{ (keV)} \ J_i{}^{\pi} \rightarrow J_f{}^{\pi}$		$L_c^{\pi}$	$E_{\rm e}~(\rm keV)$	$T_{1/2}$ (ns)	$L\lambda$	Branch (%)*	$B(\lambda L)$ (W.u.)		
Trucicus			$L\gamma$ (KCV)	1/2 (ps)		Dranch (70)	Expt.	SM		
<sup>138</sup> Ce	789	$2^+ \rightarrow$	$\rightarrow 0^+$	789	$2.06(14)^*$	E2	100	21.2(14)	15.5	
	1827	$4^+ \rightarrow$	$\rightarrow 2^+$	1038	$<\!50$	E2	100	>0.23	21.2	
	2217	$5^- \rightarrow$	→ 4 <sup>+</sup>	390	450(30)	E1	78.9	$7.4(8) \times 10^{-6}$	-	
	2294	$6^+ \rightarrow$	$\rightarrow 4^+$	467	880(19)	E2	15	0.101(24)	0.967	
	2294	$6^+ \rightarrow$	$\rightarrow 4_2^+$	156	880(19)	E2	6.5	9.5(25)	0.008	
	2294	$6^+ \rightarrow$	→ 7 <sup>-</sup>	165	880(19)	E1	53	$3.2(8) \times 10^{-5}$	-	
	2294	$6^+ \rightarrow$	→ 5 <sup>-</sup>	77	880(19)	E1	25	$1.1(4) \times 10^{-4}$	-	
	3109	$8^+ \rightarrow$	$\rightarrow 6^+$	815	<50	E2	70	>0.52	7.5	
	3539	$10^+ \rightarrow$	▶ 8 <sup>+</sup>	430	$81(2)^*$ ns	E2	100	0.0110(3)	0.04	
	3942	$11^+ \rightarrow$	$\rightarrow 10^{+}$	403	140(11)	M1	93.8	$2.34(19) \times 10^{-3}$	-	
	5312	$14^+ \rightarrow$	$\rightarrow 13^{+}$	338	80(9)	M1	43	$3.1(19) \times 10^{-3}$	-	
	5312	$14^+ \rightarrow$	→ 13 <sup>-</sup>	98	80(9)	E1	57	$1.9(4) \times 10^{-3}$	-	
<sup>140</sup> Ce	1596	$2^+ \rightarrow$	$\rightarrow 0^+$	1596	$0.0916(19)^*$	E2	100	13.8(3)	10.9	
	2083	$4^+ \rightarrow$	$\rightarrow 2^+$	487	$3.45(3)^*$ ns	E2	100	0.137(4)	1.1	
	2108	$6^+ \rightarrow$	$\rightarrow 4^+$	25	$7.3(15)^* \ \mu s$	E2	100	0.29(6)	0.89	
	3715	$10^+ \rightarrow$	→ 8 <sup>+</sup>	202	$23.1(4)^*$ ns	E2	29	0.46(13)	2.08	

TABLE I: Transition rates for  $\gamma$  decay from excited states in <sup>138</sup>Ce and <sup>140</sup>Ce.

\* Taken from Ref. [36].

- E1 transitions are strictly forbidden in this SM space.

	State	Ang.	mom.	$\pi$ occupancy				$\nu$ occupancy					07	
$I^{\pi}$	$E_x^{Pred}$ (keV)	$\pi$	u	$g_{7/2}$	$d_{5/2}$	$d_{3/2}$	$s_{1/2}$	$h_{11/2}$	$g_{7/2}$	$d_{5/2}$	$d_{3/2}$	$s_{1/2}$	$h_{11/2}$	70
$4^{+}$	1723	$4^{+}$	$0^{+}$	6	2	0	0	0	8	6	2	2	12	7.52
		$2^{+}$	$2^{+}$	6	2	0	0	0	8	6	3	1	12	4.21
$4_{2}^{+}$	1974	$4^{+}$	$0^{+}$	6	2	0	0	0	8	6	2	2	12	11.71
				6	2	0	0	0	8	6	4	0	12	5.95
				6	2	0	0	0	8	6	4	2	10	6.50
$6^{+}$	2194			6	2	0	0	0	8	6	2	2	12	10.98
		$6^{+}$	$0^+$	6	2	0	0	0	8	6	4	0	12	5.84
				6	2	0	0	0	8	6	4	2	10	4.50
8+	2943			5	3	0	0	0	8	6	2	2	12	9.18
		$8^{+}$	$0^+$	5	3	0	0	0	8	6	4	2	10	7.35
				5	3	0	0	0	8	6	4	0	12	5.65
$10^{+}$		$0^{+}$	$10^{+}$	6	2	0	0	0	8	6	4	2	10	18.87
	9549	$0^+$	$10^{+}$	4	4	0	0	0	8	6	4	2	10	10.15
	5545	$2^{+}$	$10^{+}$	6	2	0	0	0	8	6	4	2	10	9.48
		$0^{+}$	$10^{+}$	4	2	0	0	2	8	6	4	2	10	7.81

TABLE II: Shell model wave function compositions for states in <sup>138</sup>Ce.

sured  $B(E2; 6_1^+ \rightarrow 4_1^+)$  value was found to be less in <sup>138</sup>Ce than for the corresponding, neighbouring closed shell N=82 isotope <sup>140</sup>Ce. The half-lives of the yrast  $I^{\pi} = 5^-$ ,  $11^+$  and  $14^+$  states have also been determined in this work for the first time, with limits on the corresponding reduced electromagnetic transition decay probabilities.

Truncated-basis shell model calculations have been carried out to investigate the make-up wavefunction and B(E2) decay strength from the  $I^{\pi} = 6^+$  yrast state in <sup>138</sup>Ce. Comparison with shell model calculations shows a reasonable agreement with the experimental level scheme.

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FIG. 8: Comparison of experimental (Expt.) and shell model (SM) energy levels of  $^{138}{\rm Ce.}$ 

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