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Gamma-ray constraints on the properties of unbound ^{32}Cl levels

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Abstract

Systematic differences between measurements of excitation energies and branching ratios of unbound ^{32}Cl levels near the proton threshold have recently emerged. We investigate these ^{32}Cl properties using independent information by analyzing existing $^{32}\text{Ar}(\beta\gamma)^{32}\text{Cl}$ data and using published values from measurements of the $^{32}\text{S}(^3\text{He}, t\gamma)^{32}\text{Cl}$ reaction. Significant evidence emerges in support of particular values. The results increase the thermonuclear rate of the $^{31}\text{S}(p, \gamma)^{32}\text{Cl}$ reaction by up to a factor of two over the temperature range of 0.4 to 2 GK that is reached during type I x-ray bursts on hydrogen-accreting neutron stars.

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I. INTRODUCTION

Several experimental studies [1–4] of proton-unbound ^{32}Cl levels near the 1581.3(6)-keV threshold [5] have been conducted in recent years that were motivated by the desire to understand the influence of the $^{31}\text{S}(p, \gamma)^{32}\text{Cl}$ reaction on explosive hydrogen burning in astrophysical environments such as accreting compact objects in binary star systems [6]. These levels correspond to resonances in the $^{31}\text{S}(p, \gamma)^{32}\text{Cl}$ reaction that cannot yet be measured directly because a ^{31}S beam of sufficient intensity is not currently available. Consequently, most experimental studies [1–4] of the $^{31}\text{S}(p, \gamma)^{32}\text{Cl}$ reaction have used the $^{32}\text{S}(^3\text{He}, t)^{32}\text{Cl}$ reaction to populate the relevant ^{32}Cl excited states in order to determine the properties of the corresponding resonances.

In the most recent publication on the ^{32}Cl levels of interest [4], excitation energies and proton branching ratios were reported with values that differed systematically from those reported in Refs. [3] and [2]. In the present work, we first use published, independent γ -ray energies from Refs. [2, 5, 7] to resolve the differences between excitation energies. We then use data acquired in a ^{32}Ar β -decay experiment [5] in order to resolve the discrepancies between branching ratios.

II. ^{32}Cl EXCITATION ENERGIES

The excitation energies of unbound ^{32}Cl levels have been measured many times using the $(^3\text{He}, t)$ reaction [1–4, 8, 9]. The two most recent measurements [4, 9] produced values that differed from each other systematically in the region of astrophysical interest by about 4 keV. The earlier measurement [3, 9, 10] carried a combined statistical and systematic uncertainty of ≈ 0.5 keV. The latter measurement [4] carried statistical uncertainties of ≈ 2 keV and a systematic uncertainty of 4 keV. It was emphasized in Ref. [4] that uncertainties in the reaction Q -values or target thicknesses could cause systematic shifts in those $(^3\text{He}, t)$ measurements¹. The authors of Ref. [4] called for an independent measurement of the gamma decays of these levels to determine the excitation energies.

In fact, γ -ray data of sufficient precision already exist for three levels that provide evidence

¹ The calibration method employed in Ref. [3] produced excitation energies that are effectively independent of the $(^3\text{He}, t)$ reaction Q values and target thicknesses because the residual ground-state masses were treated as free parameters.

towards a resolution of this problem. In 1997, measurements of the $^{32}\text{S}(^3\text{He},t\gamma)^{32}\text{Cl}$ reaction were reported [2] in which the gamma decays of two unbound levels were measured. The excitation energies were determined to be 1736(2) and 2130(2) keV. The next two ^{32}Cl excited states are likely to decay predominantly by proton emission, as shown in Section III, so it might be very challenging to measure their energies via their gamma *decays* as proposed in Ref. [4]. However, the gamma-ray *feeding* of the level near 2.2 MeV can be used to constrain its excitation energy instead. Although a value for the excitation energy of this level was not reported explicitly in Ref. [5], the excitation energy can be derived by taking the difference between the precisely measured excitation energy of 5046.3(4) keV for the lowest $T = 2$ level of ^{32}Cl and the 2836(1)-keV energy of the gamma ray transition de-exciting it. The same gamma ray has been observed in another ^{32}Ar -decay experiment [7] and measured to have an energy of 2838(1) keV. Subtracting these energies from the excitation energy [5] of the $T = 2$ level yields $E_x = 2210.3(11)$ keV [5] and $E_x = 2208.3(11)$ keV [7] for the level of interest.

These independent gamma-ray values for excitation energies are compared to the values from Refs. [3] and [4] in Table I. The excitation energies from gamma-ray data are consistent with those from both Ref. [3] and Ref. [4] (if the systematic uncertainty of Ref. [4] is included in the comparison) and also with the values from a 1998 data compilation [11]. However, it appears that the central values of the excitation energies of Ref. [4] are systematically low and that the systematic effect increases in magnitude with increasing excitation energy (this increase may saturate). Such an increase could result from the fact that the lowest excitation energies were strongly influenced by internal ^{32}Cl calibration points and that the calibration gradually became more dependent on external calibration points towards higher energies [4], introducing substantial systematic uncertainties from the dependence on the assumed target properties [3, 9, 10] (primarily) and reaction Q values [9] (secondarily).

III. ^{32}Cl PROTON BRANCHING RATIOS

Two measurements of the decay properties of unbound ^{32}Cl levels near the proton threshold using the $(^3\text{He},t)$ reaction have been reported to date [2, 4]. In both measurements, excited states of ^{32}Cl were tagged by detecting the tritons. In the first measurement [2], gamma rays were detected in coincidence with the tritons using Ge detectors at 90° and 135°

TABLE I. Excitation energies (keV) for unbound ^{32}Cl levels from selected measurements.

J^π	$(^3\text{He}, t\gamma)$ [2]	$\beta\gamma$ [5]	$(^3\text{He}, t)$ [3]	$\beta\gamma$ [7]	$(^3\text{He}, t)$ [4] ^a
3^+	1736(2)		1736.7(6)		1734.2(14)
3^+	2130(2)		2131.1(4)		2127.5(19)
1^+		2210.3(11)	2209.5(5)	2208.3(11)	2203.1(28)
2^+			2283.5(5)		2278.6(25)

^a Statistical uncertainty only shown. Systematic uncertainty was 4 keV for all levels shown.

to determine the γ -ray branching ratios Γ_γ/Γ of levels in the range $1730 \lesssim E_x \lesssim 2300$ keV. In the second measurement [4], protons were detected in coincidence with the tritons in an array of silicon strip detectors subtending angles between 131° and 166° to determine proton branching ratios Γ_p/Γ in the range $2120 \lesssim E_x \lesssim 3900$ keV. Both of these measurements effectively determined the proton branching ratios because γ decay and proton decay are the only open channels (i.e. $\Gamma_p/\Gamma + \Gamma_\gamma/\Gamma = 1$) so the resulting values can be compared directly. As shown in Table II, the two measurements are inconsistent at the energies where they overlap.

We use information from the beta decay of ^{32}Ar [5] to help resolve the systematic discrepancy between branching ratios. As mentioned above, ^{32}Ar decay populates the level at $E_x = 2209.5$ keV both directly [$I = 0.15(3)\%$] and via gamma-decay from the $T = 2$ state [$I = 0.24(3)\%$] [5]. The feeding and decay of the 2209.5-keV state in ^{32}Ar beta decay are peculiar. Usually, low-spin states with higher excitation energy than those decaying by proton emission also decay by particle emission. Here, however, the $T = 2$, $J^\pi = 0^+$ state that lies about 2837-keV above this state has a significant gamma-ray branching ratio of $\Gamma_\gamma/\Gamma = 0.085$ because the proton decay is isospin forbidden. 12.5% of this gamma-ray branching is to the unbound 2209.5-keV state, producing the unusual circumstance of a beta-gamma-proton sequence, which has only been proposed to occur in a few other systems in this mass region [12]. The absolute intensity of the proton emission from the $E_x = 2209.5$ -keV state in ^{32}Ar beta decay has been observed to be $I = 0.385(8)\%$, but this state has never been observed to decay by gamma-ray emission.

We have analyzed the ^{32}Ar beta-delayed gamma-ray spectrum displayed in Figure 12 of Ref. [5] to search for the gamma decay of the 2209.5-keV level. Based on both the

decay properties of the well known mirror level at $E_x = 2230$ keV in ^{32}P and shell model calculations [13], we expect the gamma decay of the 2209.5-keV level in ^{32}Cl to be dominated by a 2119.6-keV transition to the first excited state at $E_x = 89.9$ keV. We estimate this gamma ray to carry 92% of the total gamma-ray branching using the properties of the mirror level. We have searched for gamma rays with energies across the range $2110 < E_\gamma < 2123$ keV and we find no evidence for this transition (Figure 1). Using the upper limit on the intensity of the 2119.6-keV gamma ray, normalizing it to the intensity of the 2837-keV transition [$I = 0.24(3)\%$] that directly feeds the 2209.5-keV level, and employing the ratio of detection efficiencies for these two different gamma-ray energies yields a 90% confidence level (*C.L.*) upper limit on the intensity of the 2119.6-keV gamma ray of $I < 0.084\%$. Dividing this value by the proton-decay intensity, and accounting for 8% of the gamma-ray intensity in other potential branches, this translates into $\Gamma_p/\Gamma_\gamma > 4.2$ (90% *C.L.*), or a limit on the proton branching ratio of $\Gamma_p/\Gamma > 0.81$ (90% *C.L.*). Over the broader energy range of $2110 < E_\gamma < 2123$ keV, we find the weakest limit to be $\Gamma_p/\Gamma > 0.80$ (90% *C.L.*) at $E_\gamma = 2120.3$ keV.

Our limits depend on the gamma-decay branches of the 1^+ , 2.21-MeV level, which were estimated by assuming mirror symmetry with ^{32}P . Isospin symmetry demands that corresponding electromagnetic transition strengths in mirror nuclei ought to be similar and it has been shown empirically [6] that for the general case of pure or mixed M1/E2 transitions this assumption is good to within a factor of 1.7. The shell model [13] suggests that the 2.22-MeV transition (and each of the the strongest competing transitions) from this level is nearly pure *M1* and it should, therefore, be dominated by the isovector component. As a result, we expect the assumption of mirror symmetry for this case to be even better than the empirical factor of 1.7. Upon varying the transition strengths within the expected limits of isospin symmetry, we find that it is difficult to impose enough mirror asymmetry to make our limit on the proton branching ratio consistent with the value in Ref. [4].

Our limit on the proton branching ratios favors the value of Ref. [2] as shown in Table II, suggesting that the values from Ref. [4] might be too low for all three of the unbound levels investigated at excitation energies below 2300 keV. A possible explanation for the low proton branching ratios deduced in Ref. [4] could be the difficulties associated with producing and verifying a sharp, consistent detection threshold for an array of several silicon detectors with sixteen strips apiece. Whether or not there was a problem of this kind with the thresholds in

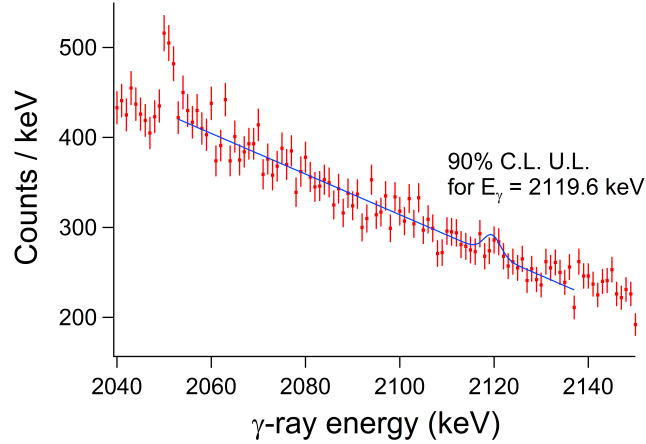


FIG. 1. ^{32}Ar beta delayed gamma-ray spectrum from Figure 12 of Ref. [5], showing a linear background plus the 90% C.L. upper limit on the intensity of a gamma ray with $E_\gamma = 2119.6$ keV. Generalizing this search over the energy range of $2110 < E_\gamma < 2123$ keV, we find the weakest limit at $E_\gamma = 2120.3$ keV, as discussed in the text.

TABLE II. Proton branching ratios Γ_p/Γ for proton-unbound ^{32}Cl levels near threshold.

J^π	E_x (^{32}Cl)	Γ_p/Γ	Γ_p/Γ^a	Γ_p/Γ
	(keV) [14]	($^3\text{He}, t$) [2]	$\beta\gamma$	($^3\text{He}, t$) [4]
3^+	2131.1	0.48 ± 0.28		0.07 ± 0.04
1^+	2209.5	> 0.92	> 0.80	0.54 ± 0.07
2^+	2283.5	> 0.95		0.66 ± 0.13

^a 90% C.L. lower limit deduced in the present work from data in Ref. [5].

Ref. [4], it seems prudent to interpret the proton branching ratios reported therein as lower limits for the time being, given the evidence presented here. We caution that the proton branching ratios reported in Ref. [4] have already been adopted in the most recent $A = 32$ data evaluation [14].

IV. CONCLUSIONS

In order to clarify systematic differences between ($^3\text{He}, t$)-reaction measurements of ^{32}Cl excitation energies and proton branching ratios, we have appealed to independent

$^{32}\text{S}(^3\text{He}, t\gamma)$ and $^{32}\text{Ar}(\beta\gamma)$ data. Our results support the excitation energies reported in Ref. [3] and the branching ratios reported in Ref. [2].

Accurate excitation energies will facilitate direct measurements of the $^{31}\text{S}(p, \gamma)^{32}\text{Cl}$ reaction when sufficiently intense low-energy beams of ^{31}S become available. The higher proton branching ratios favored restore the picture from Ref. [6] where proton emission was estimated to dominate gamma decay for both the 2.21- and 2.28-MeV levels. Assuming a value of Γ_p/Γ near unity [6] for the 2.21-MeV level increases the thermonuclear $^{31}\text{S}(p, \gamma)^{32}\text{Cl}$ reaction rates deduced in Ref. [4] by up to a factor of two over the temperature range $0.4 < T < 2$ GK that is important for type I x-ray bursts on hydrogen-accreting neutron stars.

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