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One-neutron transfer study of 135 Te and 137 Xe by particle- γ coincidence spectroscopy: the $\nu 1i_{13/2}$ state at N=83

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Abstract

New information is reported on single-neutron states above the doubly closed-shell nucleus $^{132}{\rm Sn}$. A radioactive ion beam of $^{134}{\rm Te}(N=82)$ at 565 MeV and a stable ion beam of $^{136}{\rm Xe}(N=82)$ at 560 MeV were used to study single-neutron states in the N=83 nuclei $^{135}{\rm Te}$ and $^{137}{\rm Xe}$, respectively, by ($^{13}{\rm C}$, $^{12}{\rm C}\gamma$) and ($^{9}{\rm Be}$, $^{8}{\rm Be}\gamma$) direct reactions in inverse kinematics. Particle- γ and particle- γ - γ coincidence measurements using CsI and HPGe arrays allowed determination of decay paths, high-precision level energies, multipolarities of transitions, and relative cross sections. One-neutron transfer with heavy ions is employed to gain selectivity to both low- and high-spin single-neutron states above the N=82 shell closure. Results are presented for the $13/2_1^+$ states in the N=83 nuclei $^{135}{\rm Te}$ and $^{137}{\rm Xe}$ at 2108.8(9) keV and 1752.6(3) keV, respectively, and for the 3_1^- collective octupole state observed at 3749(5) keV in $^{134}{\rm Te}(N=82)$ inelastic scattering, all previously unknown. While the $13/2_1^+$ state (or $\nu 1i_{13/2}$ centroid) in $^{133}{\rm Sn}(Z=50,N=83)$ remains unknown, the present results provide the best empirical prediction of its energy available to date.

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The nuclear shell model is the leading foundational model of nuclear physics and it predicts a particular number of single-particle and single-hole states outside of each closed proton and/or neutron shell. Experimental energies of single-particle, single-hole, and core-excited states not only challenge microscopic calculations, they also serve as empirical input to more realistic calculations and enable one to infer the nature of nucleon-nucleon interactions. While the single-particle, single-hole, and core-excited states near the light (16 O, 40 Ca) and heavy (208 Pb) double-magic nuclei are well known [1], those in the radioactive 132 Sn(Z=50, N=82) region remain incomplete. With the advent of radioactive ion beams (RIBs), the study of nuclei far from stability, particularly with respect to shell closures, has become a topic of high interest. In this Rapid Communication, new experimental results are presented for the $13/2_1^+$ states (i.e., $\nu 1i_{13/2}$ candidates) in the N=83 nuclei 135 Te and 137 Xe. New results are also presented for the 3_1^- collective octupole state observed in 134 Te(N=82) inelastic scattering.

Many of the known levels in the radioactive and double-magic ¹³²Sn region have been determined from beta-decay and/or prompt γ -ray studies of actinide fission products (e.g., Refs. [2–7]), which do not offer any particular selectivity to single-particle states. Recently, ¹³²Sn(d,p)¹³³Sn [8] and ¹³⁴Te(d,p)¹³⁵Te [9] studies in inverse kinematics have been executed but the momentum matching for $\ell = 6$ transfer did not favor population of the $1i_{13/2}$ single-neutron state with any significant cross section. While the $2f_{7/2}$, $3p_{3/2}$, $3p_{1/2}$, $2f_{5/2}$, and $1h_{9/2}$ systematics are known for the N = 83 nuclei at, near, and above ¹³³Sn [1], the $1i_{13/2}$ systematics are incomplete. The $1h_{9/2}$ systematics can also be considered incomplete in that they have never been observed in ¹³³Sn or ¹³⁵Te by a direct reaction. The $1i_{13/2}$ systematics for the N = 83, $56 \le Z \le 70$ nuclei are well established in the literature [1]. They are also known to mix with the $13/2^+$, $3^- \otimes 2f_{7/2}$ multiplet member [10–19], which means the observed $13/2_1^+$ energy is different from the unmixed single-neutron energy, $\epsilon_{\text{s.p.}}(1i_{13/2})$. This makes determination of experimental energies in nuclei closer to Z = 50 all the more important.

One-neutron transfer is employed here in conjunction with particle- γ coincidence spectroscopy, using (13 C, 12 C γ) and (9 Be, 8 Be $\rightarrow 2\alpha\gamma$) direct reactions in inverse kinematics ($A_{\rm beam} > A_{\rm target}$), to gain selectivity to the single-neutron states above the N=82 shell closure. Because 8 Be is unbound ($T_{1/2}=8.2\times10^{-17}$ s [1]), two correlated alphas are detected. Scattered target nuclei were measured at forward laboratory angles relative to the

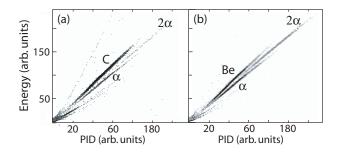


FIG. 1: CsI particle identification maps from the ¹³⁴Te RIB experiment, where the PID parameter on the x-axis is established by integrating the tail of the energy signal (cf. Ref. [26]). (a) ¹³C target data. (b) ⁹Be target data.

beam direction (corresponding to backward angles in the center-of-mass frame) to provide a clean trigger for selecting the γ -ray transitions emitted from the beam-like reaction products. The ¹³C target, with a $\nu 1p_{1/2}$ ($J_{<}=l-1/2$) ground state, and the ⁹Be target, with a $\nu 1p_{3/2}$ ($J_{>}=l+1/2$) ground state, provide different selective populations of single-neutron states (cf. Ref. [20] for a discussion on selective populations of high-J states with heavy-ion reactions). The difference in ground-state Q values for one-neutron transfer reactions on these two targets provide further differences in selectivity; this provides a mechanism for assigning observed levels to specific single-neutron configurations. Preliminary results have been reported using this technique in Refs. [21–25].

A 134 Te RIB at 565 MeV was used on two targets: a 13 C target with a thickness of 1.2 mg/cm^2 and a 9 Be target with a thickness of 2.37 mg/cm^2 . The 134 Te RIB provided by the Holifield Radioactive Ion Beam Facility (HRIBF) had an intensity of approximately 3×10^5 ions/s. Recoiling target nuclei were detected in the "bare" HyBall (BareBall) array [26] (cf. Fig. 1) using the first four rings (lab angles 7°-14°, 14°-28°, 28°-44°, and 44°-60°, relative to the beam direction, with 6, 10, 12, and 12 CsI(Tl) crystals, respectively). Coincident gamma rays were detected by 11 HPGe segmented clover detectors of the CLARION array [27] (cf. Fig. 2) at angles of 90° (5 clovers), 132° (4 clovers), and 154° (2 clovers) at a distance of 21.75 cm from the target with a total efficiency of 2.94(5)% at 1 MeV. The left-middle-right side channels of these segmented clover detectors were used to effectively give 8 segments per clover (2×4 "leaves"). The experimental trigger required either a scaled-down particle singles event or a particle- γ coincidence event.

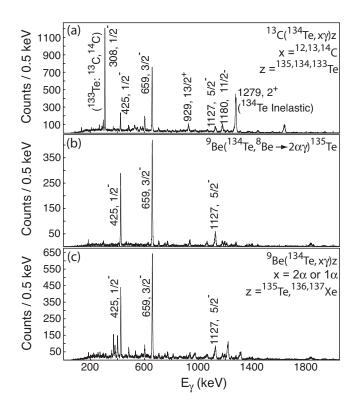


FIG. 2: The particle-gated γ -ray spectra related to 135 Te from the 134 Te RIB experiment. The gating conditions and residual nuclei are indicated in the figure and the peak labels, unless stated otherwise, pertain to transitions in 135 Te.

In a second experiment, a stable ¹³⁶Xe beam at 560 MeV was used on two targets: a ¹³C target with a thickness of 1 mg/cm² and a ⁹Be target with a thickness of 1.25 mg/cm². The Gammasphere [28] and Microball [29] arrays were used for this experiment at the Argonne Tandem Linear Accelerator System (ATLAS) facility.

From the N=83 systematics [1], the most likely decay path (i.e., the only E1 or/and E2 path) of the $13/2_1^+$ state to the $7/2_1^-$ ground state for the 135 Te and 137 Xe nuclei is through the $11/2^-, 2^+ \otimes 2f_{7/2}$ states at 1179.88(9) keV and 1220.07(15) keV, respectively. These $11/2^-$ states are well known in both 135 Te and 137 Xe from their part in a $15/2^- \to 11/2^- \to 7/2^-$ yrast transition sequence following deexcitation of an $19/2^-$ isomer [1, 7, 30-33]. Carbon-gated γ - γ coincidence data from the 13 C(134 Te, 12 C $\gamma\gamma$) 135 Te and 13 C(136 Xe, 12 C $\gamma\gamma$) 137 Xe direct reactions are shown in Fig. 3 and Fig. 4, respectively. Figure 3 shows a strong 928.9(9)-keV γ -ray transition in coincidence with the $11/2^-, 2^+ \otimes 2f_{7/2}$ state of 135 Te; the 929-keV gamma originates from a state at 2108.8(9) keV. Figure 4 shows a strong 532.5(3)-keV γ -ray transition in coincidence with the $11/2^-, 2^+ \otimes 2f_{7/2}$ state of 137 Te;

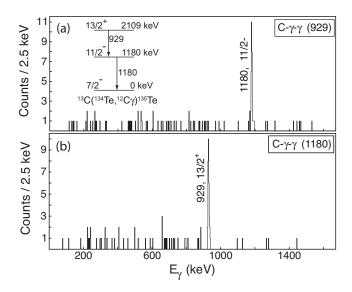


FIG. 3: The carbon-gated γ - γ coincidence data from the $^{13}\text{C}(^{134}\text{Te},^{12}\text{C}\gamma\gamma)^{135}\text{Te}$ direct reaction shows 1180- and 929-keV gamma rays in coincidence with each other. The 1180-keV gamma ray decays from the previously known $11/2^-, 2^+ \otimes 2f_{7/2}$ state at 1179.88(9) keV [1].

the 533-keV gamma originates from a state at 1752.6(3) keV.

The 2108.8(9) keV and 1752.6(3) keV states in 135 Te and 137 Xe, respectively, are likely the $13/2_1^+$ states (i.e., $1i_{13/2}$ candidates). Recently, a $13/2^+$ state in 137 Xe has been reported in an inverse kinematics $(d,p)^{137}$ Xe study (particles only, no gamma rays) by Kay et al. [34]; they report a weak $\ell = 6$ transfer component at ~ 1751 keV with a spectroscopic factor of 0.84. This identification, as acknowledged by the authors in Ref. [34], was guided by preliminary results of the present study through a private communication. The excitation energy is reported here with high precision (in combination with the selectivity of a direct reaction) for the first time. The level is identified as a previously observed but unassigned level in the beta decay of $^{137}I(7/2^+)$ [35], which reported a 532.49(10)-keV gamma ray from a 1752.56(15)-keV level (cf. the present value of 1752.6(3) keV) in coincidence with a 1220.07(15) keV gamma ray.

A $13/2^+$ assignment of a level decaying to an $11/2^-$ state suggests an E1 decay. Figure 5 shows the particle-gamma $\Delta\phi$ angular correlations for three different decays: (a) a stretched E2 decay from the Coulomb excitation of 2_1^+ in 134 Te and subsequent $2_1^+ \to 0_1^+$ decay, (b) a relatively isotropic E2 decay from the direct and indirect population of the $3/2_1^-$ level and subsequent decay to the $7/2^-$ ground state, and (c) a non-isotropic decay from the

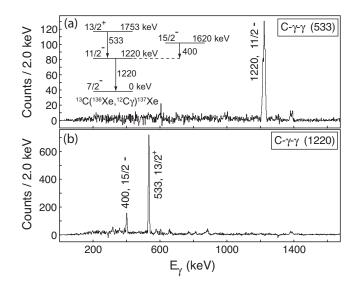


FIG. 4: The carbon-gated γ - γ coincidence data from the $^{13}\mathrm{C}(^{136}\mathrm{Xe},^{12}\mathrm{C}\gamma\gamma)^{137}\mathrm{Xe}$ direct reaction shows 1220- and 533-keV gamma rays in coincidence with each other; a narrow 533-keV gate is used to remove leakage of neighboring γ -ray transitions. The 1220-keV gamma ray decays from the previously known $11/2^-, 2^+ \otimes 2f_{7/2}$ state at 1220.07(15) keV [1]. The 400-keV gamma ray is the previously known $15/2^- \to 11/2^-$ yrast transition [1, 7, 30–32].

direct population of a level at 2108.8(9) keV and subsequent decay to the $11/2_1^-$ state. The particle-gamma angular correlation, cf. Fig. 5(c), is consistent with an E1 decay and a $13/2^+$ assignment; a M1 decay and $13/2^-$ assignment is also consistent but very unlikely since no $13/2^-$ state is expected to be strongly populated in these direct reactions.

A summary of the new levels and γ -ray energies observed in the present study is given in Table I. In addition to the $13/2_1^+$ levels in 135 Te and 137 Xe, new levels at 1854.8(8) keV, 2021.5(10) keV, and 2483.2(12) keV in 135 Te are reported for the first time (cf. Fig. 6 for their γ -ray transitions). These new levels are likely members of multiplets expected from single-neutron-core coupling. The spin assignments of these levels assume E1, M1, or E2 decay; the statistics of these states are too low to determine multipolarities through particle-gamma angular correlations. More importantly, the 3_1^- collective octupole excitation at 3749(5) keV in 134 Te is observed for the first time, cf. Fig. 7. The (13 C, 13 C') and (9 Be, 9 Be') inelastic scattering channels are highly selective of 2_1^+ quadrupole and 3_1^- octupole states [13, 14]. Indeed, the 3_1^- decay to the 2_1^+ level is the second strongest γ -ray transition in the 134 Te and 136 Xe inelastic-scattering channels; the 3_1^- level in 136 Xe was previously known in the literature [1]. The observation of the 3_1^- level in 134 Te completes the systematics for

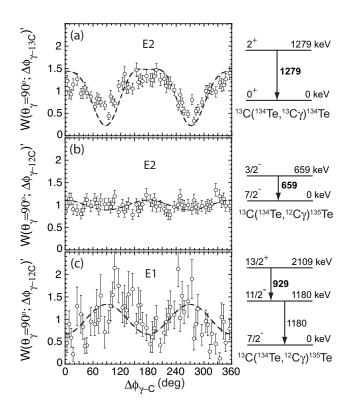


FIG. 5: The carbon- γ $\Delta \phi$ angular correlations, $W(\theta_{\gamma}, \theta_C; \Delta \phi_{\gamma-C})' = W(\theta_{\gamma}, \theta_C; \Delta \phi_{\gamma-C})/W(\theta_{\gamma}, \theta_C)$, where $\theta_C = 28^{\circ}$ to 60° and $\theta_{\gamma} = 90^{\circ}$ in the lab frame, show (a) a stretched E2 decay, (b) a relatively isotropic E2 decay, and (c) a stretched E1 decay. The dashed curves were calculated (cf. Ref. [36]) assuming full alignment.

 $N=82,\,50\leq Z\leq 72$ nuclei and the observation of $13/2^+_1$ in $^{135}{\rm Te}$ and $^{137}{\rm Xe}$ completes the systematics for all but $^{133}{\rm Sn}$ of the $N=83,\,50\leq Z\leq 70$ nuclei.

The relative cross sections are deduced by performing an intensity balance (i.e., total intensity out of a level less the total intensity feeding that level, $\sigma^{rel} \approx \Sigma I_{\text{out}} - \Sigma I_{\text{in}}$) and normalization to the $3/2^-_1$ level ($3p_{3/2}$ candidate); unobserved side feeding could reduce the accuracy of this method. Absolute cross sections can be obtained by normalizing to Rutherford scattering but this was not possible in the present study due to the fact that scattered particles were only measured at "non-safe" backward center of mass angles. The relative cross sections are compared to distorted wave Born approximation (DWBA) calculations performed with the finite-range PTOLEMY code [37] assuming a one-step process and pure single-neutron configurations.

The $1i_{13/2}$ cross section for the (13 C, 12 C) reaction is expected to be large compared to the (9 Be, 8 Be) reaction. The $13/2_{1}^{+}$ to $3/2_{1}^{-}$ cross-section ratio in 135 Te is measured as

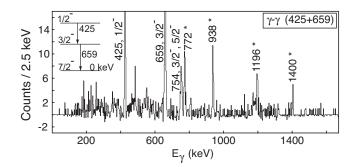


FIG. 6: The 425+659-keV γ -gated γ -ray spectrum of 135 Te from the sum of the carbon and beryllium target data show four new transitions (marked by asterisks). The new 1196-keV transition is observed only in the 659-keV gate component.

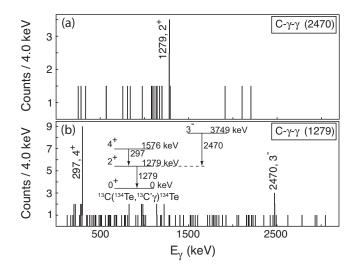


FIG. 7: The carbon-gated γ - γ coincidence data from $^{13}\text{C}(^{134}\text{Te},^{13}\text{C'}\gamma\gamma)^{134}\text{Te}$ inelastic scattering shows 1279 and 2470-keV gamma rays in coincidence with each other.

0.238(12) (cf. 0.294 from DWBA calculations) for the (13 C, 12 C) reaction but only 0.046(10) (cf. 0.054 from DWBA calculations) for the (9 Be, 8 Be) reaction; a $13/2_{1}^{+}$, $0^{+} \otimes 1i_{13/2}$ assignment is supported by the DWBA calculations. A summary of the experimental and calculated relative cross sections for the 13 C(134 Te, 12 C) 135 Te and 9 Be(134 Te, 8 Be) 135 Te reactions are given in Table II. The measured and calculated relative cross sections are in fairly good agreement for the carbon target data but not for the beryllium target data, which could be, in part, due to significant two-step processes from Coulomb excitation, unobserved side feeding, and/or breakup. Preliminary results from a recent (d,p) 135 Te study [9] report a $2f_{5/2}$ candidate at ≈ 1.8 MeV. While the present data are more consistent with the predom-

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TABLE I: New	levels and	1 ∿-rav	energies	trom	narticle- γ -	v coincidence	measurements
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E_x (keV)	J^{π}	$E_{\gamma} \text{ (keV)}$	I_{γ}^{branch}	$E_f (keV)^a$	J_f^{\pia}
134Te					
3749(5)	(3-)	$2470(5)^a$	100	1279.11(10)	2+
$135 \mathrm{Te}$					
1854.8(8)	$1/2^{\pm}, 3/2^{\pm}, 5/2^{-}$	772.1(9)	58(5)	1083.3(4)	$(\frac{1}{2}^{-})$
		1195.7(9)	100(7)	658.65(10)	$(\frac{3}{2}^{-})$
2021.5(10)	$1/2^{\pm}, 3/2^{\pm}, 5/2^{-}$	938.2(9)	100	1083.3(4)	$(\frac{1}{2}^{-})$
2108.8(9)	$(13/2^+)$	928.9(9)	100	1179.88(9)	$(\frac{11}{2}^{-})$
2483.2(12)	$1/2^{\pm}, 3/2^{\pm}, 5/2^{-}$	1399.9(11)	100	1083.3(4)	$(\frac{1}{2}^{-})$
137Xe					
$1752.6(3)^b$	$(13/2^+)$	$532.5(3)^b$	100	1220.07(15)	$(\frac{11}{2}^{-})$

^aTaken from the literature [1].

inant $2f_{5/2}$ component being located at 1127 keV, which is also the adopted assignment in the literature [1], the present data are not inconsistent with a strong $2f_{5/2}$ component at 1837 keV and/or 1855 keV. A future report of spectroscopic factors from the recent (d,p) study [9] or a future (d,p γ) study may be able to clarify this further.

The $7/2_1^-$ (N=83), $13/2_1^+$ (N=83), and 3^- (N=82) core-excited octupole systematics from the present study and literature [1] are shown in Fig. 8. The $13/2_1^+$ level in 133 Sn is the only outstanding unknown, which was predicted [6] to be unbound at an excitation energy of 2694 keV (the neutron-separation threshold is $S_n=2370(24)$ [1]); this is consistent with the extrapolated systematics in Fig. 8, which now include the 135 Te and 137 Xe data. The $1i_{13/2}$ single-neutron states are known to mix with the $13/2^+$ member of the $3^- \otimes 2f_{7/2}$ multiplet [10–19, 34], which means the observed $13/2_1^+$ energy is different from the unmixed single-neutron energy, $\epsilon_{\text{s.p.}}(1i_{13/2})$. The presence of this mixing, as evident in Fig. 8, highlights the importance in obtaining the experimental energies in nuclei closer to Z=50, such as 135 Te and 137 Xe.

The higher-lying $13/2^+$ member of the $3^- \otimes 2f_{7/2}$ multiplet is not known or observed in the present study, which makes an empirical determination of the unmixed single-neutron energy, $\epsilon_{\text{s.p.}}(1i_{13/2})$, and the two-state mixing strength out of reach for 135 Te and 137 Xe. A

^bStrongly observed in γ -ray singles spectrum as 2467.5(8) keV but could be contaminated with $E_{\gamma}(2_2^+ \to 0_1^+) = 2465.3(2)$ keV [1].

^cExists in the literature [1] as an unassigned state from ¹³⁷I decay [35] with $E_x = 1752.56(16)$ keV and $E_{\gamma} = 532.49(10)$ keV.

TABLE II: Measured relative cross sections and DWBA calculations (see text) for the one-neutron transfer study of ¹³⁵Te.

		¹³ C(¹³⁴ Te	$(e^{12}C)^{135}Te$	9 Be(134 Te, 8 Be) 135 Te	
E_x	J^{π}	σ^{rel}	DWBA^{a}	σ^{rel}	DWBA^{a}
0.00	7/2-		1.391		0.333
658.65(10)	$3/2^{-}$	1.000(21)	1.000	1.000(58)	1.000
1083.3(4)	$1/2^{-}$	0.145(11)	0.185	0.478(39)	0.832
1127.06(8)	$5/2^{-}$	0.153(52)	0.152	0.436(39)	0.711
1179.88(9)	$11/2^{-}$	0.095(20)		0.190(20)	
1246.18(10)	$9/2^{-}$	0.035(8)	0.018	0.085(10)	0.108
1380.14(9)	$(7/2^-, 9/2)$	0.056(7)		0.106(12)	
1442.22(10)		0.129(9)		0.078(10)	
1837.19(10)	$(3/2^-, 5/2^-)$	0.064(8)	$(0.152)^b$	0.478(42)	$(0.711)^b$
$1854.8(8)^c$		0.083(8)	$(0.152)^b$	0.302(19)	$(0.711)^b$
2017.88(15)				0.192(17)	
$2021.5(10)^c$				0.185(18)	
$2108.8(9)^c$	$13/2^{+}$	0.238(12)	0.294	0.046(10)	0.057
2193.80(13)		0.084(9)		0.157(19)	
2339.07(22)				0.131(13)	
$2483.2(12)^c$		0.029(5)		0.116(14)	

^aCalculated for $2f_{7/2}$, $3p_{3/2}$, $3p_{1/2}$, $2f_{5/2}$, $1h_{9/2}$, and $1i_{13/2}$.

future experiment with higher statistics could resolve this. Lifetime or g-factor measurements of the first $13/2^+$ state would be of similar value [11, 12] in determining the two-state mixing strength and unmixed single-neutron energy, as would spectroscopic factors from a (d,p) reaction study. Nevertheless, the present data provide valuable constraints on the unmixed $1i_{13/2}$ single-neutron energy.

In summary, the $13/2_1^+$ state $(1i_{13/2} \text{ candidate})$ in $^{135}\text{Te}(Z=52, N=83)$ and the 3_1^- collective octupole state in $^{134}\text{Te}(Z=52, N=82)$ have been observed for the first time by using a ^{134}Te RIB with ^{13}C and ^{9}Be targets. Furthermore, the $13/2_1^+$ state in $^{137}\text{Xe}(Z=54, N=83)$ has been identified with high-precision energy for the first time. These new results were achieved by employing particle- γ coincidence spectroscopy with CsI-HPGe arrays; this technique provides an invaluable tool for future direct-reaction studies of RIBs in inverse kinematics. While the $13/2_1^+$ state (or $1i_{13/2}$ centroid) in $^{133}\text{Sn}(Z=50, N=83)$ remains unknown, the present results provide the best empirical measure of its energy available to date and a path towards a more complete determination in the future.

^bPreliminary (d,p)¹³⁵Te results [9] report $2f_{5/2}$ at ≈ 1.8 MeV.

^cNew levels from present study; other energies from ENSDF [1].

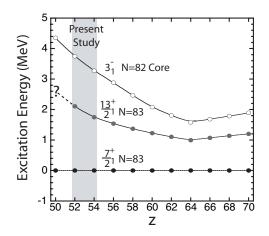


FIG. 8: The $7/2_1^-$ (N=83), $13/2_1^+$ (N=83), and 3^- (N=82) core-excited octupole systematics from the present study and literature [1].

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