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**Longitudinal dependence of two-particle momentum correlations from the hydrodynamic flow model NEXSPHERIO**

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Longitudinal dependence of two-particle momentum correlations from NEXSPHERIO model

Monika Sharma*, Claude Pruneau, and Sean Gavin

Department of Physics and Astronomy, Wayne State University, Detroit, MI 48201 USA

Jun Takahashi, R. Derradi de Souza

Universidade Estadual de Campinas, São Paulo, 13083-970, Brazil

T. Kodama

Universidade Federal do Rio de Janeiro, Rio de Janeiro, 21945-970, Brazil

The rapidity dependence of two-particle momentum correlations can be used to probe the viscosity of the liquid produced in heavy nuclei collisions at RHIC. We reexamine this probe in light of the recent experimental analyses of the azimuthal-angle dependence of number correlations, which demonstrate the importance of initial state fluctuations propagated by hydrodynamic flow in these correlations. The NEXSPHERIO model combines fluctuating initial conditions with viscosity-free hydrodynamic evolution and, indeed, has been shown to describe azimuthal correlations. We use this model to compute the number density correlation $R_2$ and the momentum current correlation function $C$, at low transverse momentum in Au+Au collisions at $\sqrt{S_{NN}} = 200$ GeV. The correlation function $C$ is sensitive to details of the collision dynamics. Its longitudinal width is expected to broaden under the influence of viscous effects and narrow in the presence of sizable radial flow. While the NEXSPHERIO model qualitatively describes the emergence of a near-side ridge-like structure for both the $R_2$ and $C$ observables, we find that it predicts a longitudinal narrowing of the near side peak of these correlation functions for increasing number of participants in contrast with recent observations by the STAR Collaboration of a significant broadening in most central collisions relative to peripheral collisions.

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I. INTRODUCTION

Measurements of elliptic flow indicate that strong collective flow is achieved in nuclear collisions at RHIC [1–5]; see also the reviews [6, 7]. Hydrodynamic models describe many features of the experimental data, indicating that the produced medium behaves as a nearly ideal fluid, i.e. a fluid endowed with a very small shear viscosity per unit of entropy, $\eta/s$. Considerable effort is devoted to using elliptic flow data to measure $\eta/s$; see, e.g., [8, 9], and Refs. therein. However, the interpretation of such measurements has many sources of theoretical uncertainty. The primary uncertainties are: initial conditions, event-by-event fluctuations, and freeze-out [10]. These effects are somewhat outside the scope of hydrodynamics and further theoretical work is required to elaborate a systematic scheme to compute them with quantifiable uncertainties. It is therefore important to explore independent methods to determine $\eta/s$.

One such alternative method was proposed by Gavin et al. based on two-particle transverse momentum correlations [11]. This novel technique relies on the fact that viscous forces impart momentum transfers between different fluid cells. These momentum transfers in turn modify the relative rapidity of correlated particles produced by these cells thereby leading to a longitudinal broadening of transverse momentum two-particle correlation functions. The longitudinal profile of this correlation function, hereafter called $C$, is expected to broaden with increasing collision system lifetime, and for increasing number of collision participants. The measurement strategy proposed by authors of [11] is to measure the $p_T$ correlation function $C$ as a function of collision centrality and seek evidence for its longitudinal broadening in most central collisions. Given its explicit dependence on particle momenta, the correlation function $C$ is sensitive to momentum current correlations and as such constitutes a more suitable observable to measure viscosity than simple two particle (number) correlation functions.

The STAR experiment recently carried an analysis of a differential version of the $p_T$ correlation function $C$. STAR reported that the near-side of the correlation function broadens progressively with increasing collision centrality [12]. The broadening is considerable but translates nonetheless in a rather modest $\eta/s$ consistent with values deduced from comparison of hydrodynamic calculations with $v_2$ measurements. While, this agreement is encouraging, one must however exercise caution in the interpretation of the broadening of the measured correlation function. Indeed, one must assess whether other mechanisms could produce or perhaps mask broadening. Reaction mechanisms and effects

* currently at Vanderbilt University, Nashville, TN 37209 USA
of particular interest include two-particle kinematical focusing associated with radial flow, jet production, and more specifically jet quenching, flux tubes, fluctuations, anisotropic flow, resonances, and momentum conservation. One must also acknowledge that the structure of two-particle correlations observed is not fully elucidated. While differential correlation functions have been previously measured by the STAR [13], PHENIX [14] and PHOBOS [15] experiments, a significant interest lies in studying diverse correlation functions which provide better understanding and sensitivity to various reaction mechanisms. Dihadron correlations have previously been studied containing a high-\(p_T\) “trigger” particle and a low-\(p_T\) “associated” particle. Measurements of near-side enhanced yield - long range correlations - also known as the “Ridge” were reported by the STAR collaboration [16, 17]. Some theoretical models attribute the ridge to jet-medium interactions: particles from jet fragmentations in QCD vacuum result in a peak at \(\Delta \eta \sim 0\) and those affected by the medium are diffused broadly in pseudorapidity, forming a ridge-like structure [18–25]. Other plausible explanations of the ridge formation are given by transverse radial flow models where kinematic focussing of clusters, strings, or color flux tubes is induced by increasing radial flow with centrality [26]. Transverse radial expansion produces strong position-momentum correlations that leads to characteristic rapidity, \(p_T\) and azimuthal correlations among the produced particles. Another interesting and promising interpretation of the near-side ridge observed in both triggered and untriggered correlation functions is based on the notion of initial density fluctuations. Initial density fluctuations in the coordinate space shall lead to fluctuations in the number of locally produced particles. These fluctuations translate, under the influence of hydrodynamical radial expansion, into long range pseudorapidity two-particle correlations. Such long range correlations are well demonstrated in the NEXSPHERIO simulations reported by Takahashi et al.[27]. Other studies based on hydrodynamical and hybrid models have essentially confirmed this important observation [28–32]. Also note that much work is being done to quantitatively understand the connection between initial collision system spatial anisotropies and final state flow coefficients, \(v_n\), of orders \(n = 1\) through 6 [33–37], and to determine the fluid viscosity (see for instance [38, 39]). NEXSPHERIO describes many features of the measured correlations, particularly their azimuthal dependence. It is thus of interest to extend the work of these authors and consider predictions of NEXSPHERIO for transverse momentum two-particle correlations.

The NEXSPHERIO model, the correlation observable of interest, and the analysis technique used in this work are described in the next section. Results are presented in sec. III, and conclusions summarized in sec. IV.

II. NEXSPHERIO MODEL AND ANALYSIS TECHNIQUE

NEXSPHERIO [40, 41] combines the event generator NEXUS [42] and the hydrodynamical code SPHERIO [43] to simulate particle production in \(A + A\) collisions. NEXUS provides for initial parton-parton interactions and energy deposition with lumpy initial conditions (ICs) specified in terms of number density, energy density and baryon density. SPHERIO is then used to simulate the hydrodynamical evolution in each NEXUS event, i.e. thereby including the effect of IC fluctuations in the production of collective flow patterns and correlated particle production. Indeed, the recent studies with NEXSPHERIO show that hydrodynamic expansion of fluctuating ICs lead to the formation of near-side ridge-like structure in \(\Delta \eta\) vs. \(\Delta \phi\) correlation functions [27] while, by contrast, smooth initial conditions do not feature any near-side ridge-like structures. Furthermore, an interesting interpretation of the origin of the away-side double peaked structure of the two particle correlation function was also discussed in the context of the NEXSPHERIO lumpy initial condition in reference [44].

The transverse momentum two-particle correlation \(C\) depends at a basic level on particle number fluctuations and should therefore exhibit the formation of a ridge, in NEXSPHERIO, for central collisions with lumpy initial conditions. \(C\) also depends on actual momentum-momentum correlations. Its magnitude and dependence on \(\Delta \eta\) vs. \(\Delta \phi\) should thus also be influenced by radial hydrodynamical flow brought about by lumpy initial density conditions. However, given SPHERIO is built as an ideal hydrodynamical transport code, there should be no viscous effects: no broadening of the correlation function should arise with increasing collision centrality. Any change in the correlation function profile and width should be due solely to viscous free expansion dynamics.

Our analysis is based on a total of 500,000 simulated \(Au + Au\) collisions events at \(\sqrt{s_{NN}} = 200\) GeV produced with NEXSPHERIO [27]. Events were grouped in four collision centrality classes corresponding to 0-10% (most central), 20-30%, 40-60% and 60-80% (most peripheral) fractions of the total reaction cross-section. Modeling nuclear collisions in ideal hydrodynamics is limited to low \(p_T\) (\(\leq 2.0\) GeV/\(c\)) because it is generally assumed that the equilibrium description fails at high \(p_T\), where particle production may be dominated by hard processes. We therefore focus our analysis on bulk particles, i.e. particles produced in the range \(p_T < 2.0\) GeV/\(c\). This momentum selection is used for both particles in constructing the two particle correlation function \(R_2\), and the momentum dependent correlation function, \(C\), defined below, thereby yielding “untriggered” distributions. We simulate the STAR experiment acceptance and further limit our simulations to particles produced in the pseudorapidity range \(|\eta| < 1.0\) and with \(0.2 < p_T < 2.0\) GeV/\(c\).

We carried an analysis of observables \(R_2\) and \(C\) studied as a function of pseudorapidity \((\Delta \eta)\) and azimuth\((\Delta \phi)\)
differences of particle pairs. These correlation functions are defined as follows:

\[ R_2(\Delta \eta, \Delta \phi) = \frac{\int \rho_2(p_1, \eta_1, \phi_1, p_2, \eta_2, \phi_2) \delta(\Delta \eta - \eta_1 + \eta_2) \delta(\Delta \phi - \phi_1 + \phi_2) dp_1 dp_2 d\eta_1 d\eta_2 d\phi_1 d\phi_2 \rho_1}{\int \rho_1(\eta_1, \phi_1) \rho_2(\eta_2, \phi_2) \delta(\Delta \eta - \eta_1 + \eta_2) \delta(\Delta \phi - \phi_1 + \phi_2) dp_1 dp_2 d\eta_1 d\eta_2 d\phi_1 d\phi_2} - 1 \]  

(1)

\[ C(\Delta \eta, \Delta \phi) = \frac{\int \rho_2(p_1, \eta_1, \phi_1, p_2, \eta_2, \phi_2) \rho_2(p_1, \eta_1, \phi_1, p_2, \eta_2, \phi_2) \delta(\Delta \eta - \eta_1 + \eta_2) \delta(\Delta \phi - \phi_1 + \phi_2) dp_1 dp_2 d\eta_1 d\eta_2 d\phi_1 d\phi_2}{\int \rho_1(\eta_1, \phi_1) \rho_1(\eta_2, \phi_2) \delta(\Delta \eta - \eta_1 + \eta_2) \delta(\Delta \phi - \phi_1 + \phi_2) dp_1 dp_2 d\eta_1 d\eta_2 d\phi_1 d\phi_2} - \langle \rho_1 \rangle \langle \rho_2 \rangle \]

where \( \rho_1 = dN_1/d\eta_1 d\phi_1 \) and \( \rho_2 = dN_2/d\eta_2 d\phi_2 \) correspond to single and two-particle densities, respectively; \( \langle \rho_k \rangle \equiv \langle \sum \rho_{k,i} \rangle / \langle \eta \rangle \) is the average particle momentum. The label \( k=1,2 \) stands for particles being detected at \( (p_{k,i}, \eta_k, \phi_k) \), and the brackets represent event ensemble averages.

III. RESULTS

We present, in Fig. 1, the correlation function \( R_2 \) for (a) 60-80% (most peripheral), (b) 40-60%, (c) 20-30% and (d) 0-10% (most central) collision centralities. Our calculation of \( R_2 \) reproduces the features already reported in [27] for a ‘per trigger’ correlation function. \( R_2 \) exhibits a somewhat narrow near-side peak (i.e. near \( \Delta \eta \approx \Delta \phi \approx 0 \)) and an extended ridge-like structure centered at \( \Delta \phi \approx \pi \) in all collision centralities. The correlation function exhibits a strong \( \cos(2\Delta \phi) \) modulation associated with collective flow in mid-central collisions. This component is minimal in most central collisions but \( R_2 \) exhibits the build up of a narrow ridge at \( \Delta \phi \sim 0 \) which extends over the full \( \Delta \eta \) range of the correlation function.

Figure 2 presents the correlation function \( C \) for the same four collision centrality bins used for \( R_2 \) in Fig. 1. \( C \) exhibits correlation shape dependencies on \( \Delta \eta \) and \( \Delta \phi \) qualitatively similar to those observed for \( R_2 \). It also has a narrow near-side peak at \( \Delta \eta \approx \Delta \phi \approx 0 \) and an extended \( \Delta \eta \) ridge at \( \Delta \phi \approx \pi \) in all collision centralities. Mid-central bins feature strong elliptic flow modulations and the most central bin exhibit a near-side peak atop an extended ridge. Also note that both \( R_2 \) and \( C \) exhibit an overall decrease of the correlation function strength consistent with the increase in the average number of participant nucleons and the decrease of the elliptic flow modulation from 60-80% to 0-5% collision centrality ranges.

![Figure 1](image)

FIG. 1: (Color online) Two-particle correlation function, \( R_2 \), plotted as a function of the particle pair pseudorapidity difference, \( \Delta \eta \), and relative azimuthal angle, \( \Delta \phi \) [rad], for (a) 60-80%, (b) 40-60%, (c) 20-30% and (d) 0-10% collision centralities in Au + Au interactions at \( \sqrt{s_{NN}} = 200 \) GeV calculated with the NEXSPHERIO event generator.

Authors of Ref. [27] showed the initial density (event-by-event) fluctuations present in NEXSPHERIO calculations produce a near-side ridge in ‘triggered correlation functions’. We here find that these initial density fluctuations also produce a near-side ridge in both ‘untriggered’ and transverse momentum correlation functions. Given \( C \) has an
explicit dependence on the particle momenta, one expects measurements of this variable should provide additional
constraints for theoretical models. We further observe that the away-side ridge-like feature evolves significantly from
a broad structure at $\Delta \eta \sim 0$ in most peripheral collisions to a saddle-like shape with a minimum located at $\Delta \eta \sim 0$
in the most central collisions.

The observed build up of a near-side ridge in most central collisions is understood in NEXSPHERIO simulations
to arise from hot spots extending in the longitudinal (i.e. beam) direction. Fluctuations in number and transverse
position of these hot spots generate finite azimuthal anisotropy which one expects to be essentially independent of
pseudorapidity in the acceptance considered in this work. Given that NEXSPHERIO involves ideal hydrodynamical
transport of the energy deposited during the early moments of the collisions, one could thus anticipate that the
longitudinal width of the near-side peak should be essentially unaffected by the production of the near-side ridge. We
verify this assertion by plotting $\Delta \eta$ projections of the $R_2$ and $C$ correlation functions in the range $|\Delta \phi| < 1.0$ radians
in Figures 3 and 4 respectively. We parameterize and fit these distributions using a simple two-component ansatz to
study their evolution with collision centrality.

$$f(b, a, \sigma) = b + a \exp \left(-\frac{\Delta \eta^2}{2\sigma^2}\right)$$

Fit results are presented in Table I and II for observable $R_2$ and $C$ respectively. We first observe that the near-side
peak amplitude of both observables decreases monotonically with increasing collision centrality. We also observe the
emergences of strong azimuthal modulation in mid-central collisions, and the rise of a near-side ridge extending over a
long $\Delta \eta$ range in the most central collisions. These result from the formation and evolution of the medium, with initial fluctuations, and the effects of radial and elliptic flow, embodied in the NEXSPHERIO calculations. We furthermore find that the distribution widths, $\sigma$, exhibit a decreasing trend with increasing collision centrality. Specifically, we find that the $\Delta \eta$ width of $C$ monotonically evolves from $0.72 \pm 0.02$ units of rapidity in peripheral collisions, to $0.54 \pm 0.03$ in most central collisions. $R_2$ exhibits a similar behavior, with an initial width of $0.81 \pm 0.02$ in peripheral collisions, and reduces to $0.63 \pm 0.01$ in 20-30% collisions. It however rises slightly in most central collisions. We also characterized the width of the distributions by calculating their root-mean-square (RMS) above a constant offset evaluated based on the value of the correlation function at $\Delta \eta \sim \pm 2$. The deduced RMS values are listed in Table I and II. They are found to be in agreement, within statistical errors, with the widths, $\sigma$, obtained from the fits.

Table I: Various fit parameters for $R_2$

<table>
<thead>
<tr>
<th>Centrality</th>
<th>Offset</th>
<th>Amplitude</th>
<th>$\sigma$</th>
<th>RMS</th>
<th>$\chi^2$/ndf</th>
</tr>
</thead>
<tbody>
<tr>
<td>60-80%</td>
<td>0.345</td>
<td>0.39</td>
<td>0.81</td>
<td>0.78</td>
<td>0.02</td>
</tr>
<tr>
<td>40-60%</td>
<td>0.156</td>
<td>0.17</td>
<td>0.69</td>
<td>0.01</td>
<td>0.68</td>
</tr>
<tr>
<td>20-30%</td>
<td>0.032</td>
<td>0.038</td>
<td>0.63</td>
<td>0.01</td>
<td>0.63</td>
</tr>
<tr>
<td>0-10%</td>
<td>0.022</td>
<td>0.025</td>
<td>0.74</td>
<td>0.03</td>
<td>0.75</td>
</tr>
</tbody>
</table>

Table II: Various fit parameters for $C$

<table>
<thead>
<tr>
<th>Centrality</th>
<th>Offset</th>
<th>Amplitude</th>
<th>$\sigma$</th>
<th>RMS</th>
<th>$\chi^2$/ndf</th>
</tr>
</thead>
<tbody>
<tr>
<td>60-80%</td>
<td>0.1096</td>
<td>0.126</td>
<td>0.72</td>
<td>0.02</td>
<td>0.71</td>
</tr>
<tr>
<td>40-60%</td>
<td>0.0559</td>
<td>0.063</td>
<td>0.67</td>
<td>0.01</td>
<td>0.66</td>
</tr>
<tr>
<td>20-30%</td>
<td>0.0142</td>
<td>0.017</td>
<td>0.56</td>
<td>0.01</td>
<td>0.59</td>
</tr>
<tr>
<td>0-10%</td>
<td>0.0084</td>
<td>0.0097</td>
<td>0.54</td>
<td>0.03</td>
<td>0.58</td>
</tr>
</tbody>
</table>

Figure 5 shows a comparison of the RMS obtained with NEXSPHERIO (black squares) with those reported by STAR (black circles) for Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV. The RMS predicted by NEXSPHERIO substantially exceeds the value measured by STAR in most peripheral collisions. We find additionally that NEXSPHERIO predicts a progressive narrowing of the correlation function for increasing number of participants, at variance with the observation, by the STAR experiment, of an increasing broadening for larger number of participants [12]. The RMS reported by STAR for most central collisions is in fact almost twice as large as that predicted by the model. In addition, the smaller value of RMS observed in the STAR peripheral data could in part be due to contributions from jet particles that will yield a narrower correlation function.

We thus find that while NEXSPHERIO qualitatively reproduces the azimuthal modulation and near-side ridge observed in experimental data it predicts a narrowing rather than the observed longitudinal broadening of the correlation function $C$. The longitudinal narrowing in NEXSPHERIO is in large part due to the strong transverse flow.
This narrowing effect of transverse flow on rapidity correlations was first discussed in [47, 48]. The narrowing found here is rather modest, however, amounting to approximately 0.13 units of rapidity.

To understand why NEXSPHERIO fails to describe the measured broadening, we ask how broadening may arise in general. In Ref. [11], it was predicted that viscous diffusion can produce a considerable longitudinal broadening of the momentum current correlation function $C$. The idea is that viscous friction acts to reduce the difference in transverse flow velocity between neighboring fluid cells. This can be measured by studying the rapidity dependence of $p_T$ fluctuations, because of the rough correspondence between spatial distance along the beam direction and rapidity. In principle, rapidity broadening can also result if the particle production mechanism varies appropriately with centrality. We speculate that NEXSPHERIO fails to reproduce the measured broadening because neither effects are included.

The STAR Collaboration used their measurement [12] of the broadening of the correlation function $C$ to estimate the viscosity per unit of entropy based on the model presented in [11]. They reported a value of $\eta/s = 0.13 \pm 0.03$ (stat). Their analysis of experimental systematic errors leads to a range $\eta/s = 0.06 - 0.21$. The model however neglects the fact that radial flow may cause a longitudinal narrowing in rapidity of the near side peak in the differential correlation function $C$. We find in this work that the narrowing associated with radial flow effects is relatively modest compared to the sizable broadening reported by STAR. The neglect of radial flow effects in [12] thus appears reasonable, in a first approximation.

IV. CONCLUSIONS

In summary, we presented a study of the centrality dependence of the correlation functions $R_2$ and $C$ in Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV based on the NEXSPHERIO model. We find the two observables exhibit qualitatively similar shapes in $\Delta \eta$ and $\Delta \phi$, and dependence on collision centrality. Quantitative differences however arise from the explicit dependence of $C$ on particle momenta. We find that both observables exhibit a near-side ridge in central collisions owing to event-by-event fluctuations in the initial transverse energy deposition profile. We studied projections of the near-side ($|\Delta \phi| < 1.0$ radians) of these correlation functions and studied their evolution with collision centrality. We found the longitudinal width of $C$ exhibits a small decrease with increasing collision centrality owing to radial expansion dynamics. The magnitude of this reduction is rather modest. It is unlikely that this reduction would mask correlation broadening associated with viscous effects in real systems. Indeed, we find that the RMS reduction observed in this work is rather modest in comparison with the sizable increase of the longitudinal width reported by STAR from their measurement of $C$ in Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV. From this study, it is clear that the observed increase in the width of the longitudinal correlation function $C$ from peripheral to central collisions by the STAR experiment is not due just to variations of flow effects. In fact, our result shows that with an ideal hydrodynamic scenario, the width of the correlation function would decrease, thus suggesting that the broadening caused by other possible effects such as viscosity could be even higher than the observed values.

While NEXSPHERIO does not describe the measured increase in $\Delta \eta$ with increasing centrality, the model does describe the azimuthal dependence of correlations qualitatively well. We envision that extensions of hydro-models
that includes viscous hydrodynamics might describe the $\Delta \eta$ broadening reported by STAR. We surmise that this
is a generic feature of models that derive long range rapidity correlations from the early time behavior followed by
hydrodynamic flow [23, 49–52]. We have not dwelled on the detailed ways in which measurements of beam-energy,
$p_T$, and projectile-mass dependence might ultimately distinguish these models.

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[15] PHOBOS Correlations