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# Investigation of $^{10}\text{B}(p, \alpha)^7\text{Be}$ reaction from 0.8 to 2.0 MeV

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**Background:** A multitude of broad interfering resonances characterize the  $^{10}\text{B}(p, \alpha)^7\text{Be}$  cross section at low energies. The complexity of the reaction mechanism, as well as conflicting experimental measurements, have so far prevented a reliable prediction of the cross section over the energy ranges pertinent for a boron-proton fusion reactor environment.

**Purpose:** To improve the evaluated cross section of the  $^{10}\text{B}(p, \alpha)^7\text{Be}$  reaction, this study targets the proton energy region from 0.8 to 2.0 MeV, where kinematic overlap of the scattered protons and reaction  $\alpha$ -particles have made past measurements very challenging.

**Method:** New detailed studies of the reaction have been performed at the Edwards Accelerator Laboratory at Ohio University and the Nuclear Science Laboratory at the University of Notre Dame using time-of-flight and degrader foil techniques, respectively.

**Results:** Proton and  $\alpha$ -particle signals were clearly resolved using both techniques, and 16 point differential cross sections were measured over an angular range of  $\theta_{\text{lab}} = 45$  and  $157.5^\circ$ . A comprehensive  $R$ -matrix analysis of the experimental data, including data from previous low-energy studies of the  $^{10}\text{B}(p, \alpha)^7\text{Be}$ ,  $^{10}\text{B}(p, p)^{10}\text{B}$ , and  $^{10}\text{B}(p, \gamma)^{11}\text{C}$  reactions, was achieved over the region of measurement. Using a representative set of previous data, the fit was extended to very low energies.

**Conclusions:** On the basis of this data and  $R$ -matrix analysis, a more reliable and consistent description of the  $^{10}\text{B}(p, \alpha)^7\text{Be}$  cross section has been established. The uncertainty over the energy range of this study has been reduced from  $\approx 20\%$  to  $\approx 10\%$ , and the level structure over this region has been clarified considerably.

## I. INTRODUCTION

Aneutronic plasma fusion systems have been increasingly discussed as possible energy sources that would avoid the disadvantage of long-lived radioactive end-products [1]. The most frequently quoted aneutronic sources are the  $^3\text{He}(^3\text{He}, 2p)^4\text{He}$  ( $Q = 12.9$  MeV) and the  $^{11}\text{B}(p, 2\alpha)^4\text{He}$  ( $Q = 8.7$  MeV) reactions, with helium as the primary end-product along with a sufficient amount of energy generation. Of particular interest is the  $^{11}\text{B}(p, 2\alpha)^4\text{He}$  process [2] because, unlike  $^3\text{He}$ , being mostly produced as a decay product of tritium  $^3\text{H}$  [3],  $^{11}\text{B}$  is considered to be a naturally abundant and inexpensive fuel stock. While the  $^{11}\text{B}+p$  fusion system has already been considered earlier as a potential energy source in traditional plasma systems [4, 5], or for colliding beam

reactors [6], recent observations of aneutronic fusion reactions on laser-picosecond plasmas [7] have motivated the discussion of possible applications for  $^{11}\text{B}(p, 2\alpha)^4\text{He}$  in laser-driven, hot-pulsed plasma systems [8–11]. In particular, the development of high power peta-watt laser systems with picosecond durations [12, 13] opens up new windows of application. The optimal energy range for the  $^{11}\text{B}+p$  fusion system is between 200 and 1000 keV because of a broad resonance structure observed at 600 keV center of mass energy [14] that dominates the total cross section of the reaction. Therefore, the efforts of laser-driven fusion studies focus on that energy range [15].

The  $^{11}\text{B}(p, 2\alpha)^4\text{He}$  fusion reaction does not produce any long-lived radioactive products; however, the 19%  $^{10}\text{B}$  abundance in naturally occurring boron fuel material will produce the longer-lived  $^7\text{Be}$  isotope through the  $^{10}\text{B}(p, \alpha)^7\text{Be}$  reaction.  $^7\text{Be}$  decays by electron capture with a laboratory lifetime of 53.2 days under emission of a characteristic 457 keV  $\gamma$ -line from the 10% transition to the first excited state in  $^7\text{Li}$  with subsequent  $\gamma$ -decay to the ground state [16]. The total cross section of the reaction near 600 keV is 10 mb according to the EXFOR data compilation [17]. This value is substantially lower than the 1 barn cross section reported for the  $^{11}\text{B}(p, 2\alpha)^4\text{He}$

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52 reaction [14]. The production of spurious amounts of  
 53  ${}^7\text{Be}$  in a plasma fusion operation with enriched  ${}^{11}\text{B}$  fuel  
 54 may therefore not be a matter of great concern, but the  
 55 observation of  ${}^7\text{Be}$  from a boron-hydrogen plasma burn-  
 56 ing environment, doped with a well know amount of  ${}^{10}\text{B}$ ,  
 57 may provide the means for temperature determination in  
 58 the plasma region.

59 This may provide an independent test for tempera-  
 60 ture analysis in the new generation of laser-driven, hot-  
 61 plasma facilities such as the National Ignition Facility  
 62 (NIF) [18] or OMEGA [19], where recent studies of  $d$ - $t$   
 63 and  $d$ - $d$  fusion signals indicated considerable uncertainty  
 64 in the temperature analysis [20]. Yet, the EXFOR data  
 65 compilation indicates significant differences and uncer-  
 66 tainties between the different data sets for the possible  
 67 transitions to the ground state  ${}^{10}\text{B}(p, \alpha_0){}^7\text{Be}$  and the  
 68 first excited state  ${}^{10}\text{B}(p, \alpha_1){}^7\text{Be}^*$  in  ${}^7\text{Be}$  (see Wiescher  
 69 *et al.* [21]). The ground state transition has been mea-  
 70 sured extensively in the low energy range between 100  
 71 keV and 1 MeV [21–32], with some experiments cover-  
 72 ing a higher energy range up to 2 MeV [24, 26]. More  
 73 recent efforts using the Trojan Horse method (THM)  
 74 have concentrated on the study of very low energies [33–  
 75 36]. The  ${}^{10}\text{B}(p, \alpha_1){}^7\text{Be}^*$  channel has been measured in-  
 76 dependently either by particle spectroscopy [24, 26] or by  
 77  $\gamma$ -ray spectroscopy using the  ${}^{10}\text{B}(p, \alpha_1 - \gamma){}^7\text{Be}$  channel  
 78 [21, 24, 37–39]. The discrepancies are most visible in the  
 79 energy range of interest for the  ${}^{11}\text{B}(p, 2\alpha){}^4\text{He}$  around 600  
 80 keV. To use the  ${}^{10}\text{B}(p, \alpha){}^7\text{Be}$  reaction as a monitor, the  
 81 cross section needs to be known with high accuracy and  
 82 the presently existing uncertainties need to be removed.

83 The very low energies accessed at NIF remain below  
 84 the energy range of accelerator-based measurements, and  
 85 THM measurements have relatively large, model depen-  
 86 dent, uncertainties [36]. Therefore, to determine the low-  
 87 energy cross section, the phenomenological  $R$ -matrix ap-  
 88 proach has often been utilized to extrapolate from higher  
 89 energies that are experimentally accessible [40, 41]. The  
 90 extrapolation is accomplished by constraining the phe-  
 91 nomenological model with higher energy cross section  
 92 data and level information from nuclear structure stud-  
 93 ies. For the  ${}^{10}\text{B}(p, \alpha){}^7\text{Be}$  reaction, this approach is com-  
 94 plicated by inconsistent cross section measurements and  
 95 incomplete level structure information (see Fig. 1). The  
 96 experimental data often have large discrepancies in the  
 97 absolute scale of the cross section and in some cases even  
 98 the energy dependence of data sets are inconsistent, as  
 99 recently highlighted in Wiescher *et al.* [21].

100 One of the main conclusions of Wiescher *et al.* [21] was  
 101 that the current data do not place sufficient constraints  
 102 on the broad resonance contributions in the  $R$ -matrix de-  
 103 scription of the  ${}^{10}\text{B}+p$  reactions. This is emphasized by  
 104 the rather different  $R$ -matrix fits obtained in the recent  
 105 works [21, 31, 32, 36], despite the use of similar experi-  
 106 mental data for the fits. One chief reason for this is that  
 107 the reaction kinematics result in very similar energies for  
 108 the  $\alpha$ -particles and protons from the  ${}^{10}\text{B}(p, \alpha_0){}^7\text{Be}$  and  
 109  ${}^{10}\text{B}(p, p_0){}^{10}\text{B}$  reactions, respectively. With standard res-

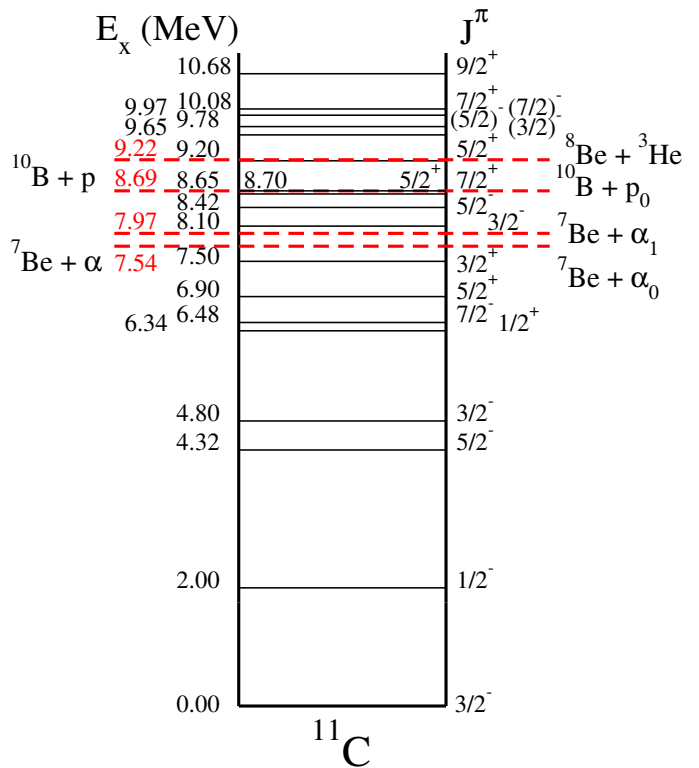


FIG. 1. Level diagram of the  ${}^{11}\text{C}$  system up to  $E_x \approx 11$  MeV as given in the [Evaluated Nuclear Structure Data File \(ENSDF\) evaluation \[42\]](#). The red dashed lines indicate particle separation energies.

110 lution ( $\approx 20$  keV) silicon detectors at room temperature,  
 111 it is very difficult to separate the  $\alpha$ -particle and proton  
 112 peaks from about 0.8 to 2 MeV (see Fig. 2) laboratory  
 113 proton energy ( $E_p$ ). **In addition, the emitted particles**  
 114 **are too low in energy for particle identification through**  
 115 **energy loss techniques, using an  $E$ - $\Delta E$  telescope for ex-**  
 116 **ample. Hence the data available in the literature over**  
 117 **this energy region are quite limited.**

118 In this work, we report new experimental differential  
 119 cross section measurements of the  ${}^{10}\text{B}(p, \alpha_0){}^7\text{Be}$ , and  
 120  ${}^{10}\text{B}(p, \alpha_1){}^7\text{Be}$ , reactions from  $E_p = 0.8$  to 2 MeV. In  
 121 Sec. II two experimental setups at the University of Notre  
 122 Dame and Ohio University are described and in Sec. III  
 123 the experimental yields and absolute cross sections are re-  
 124 ported. The multichannel  $R$ -matrix analysis is discussed  
 125 in Sec. IV and the effect on the reaction rates in Sec. V.  
 126 Summarizing remarks are made in Sec. VI.

## 127 II. EXPERIMENTAL SETUP

128 Two experimental setups, at two different experi-  
 129 mental facilities, were used for new cross section mea-  
 130 surements of the  ${}^{10}\text{B}(p, \alpha_0){}^7\text{Be}$ ,  ${}^{10}\text{B}(p, \alpha_1){}^7\text{Be}$ , and  
 131  ${}^{10}\text{B}(p, p){}^{10}\text{B}$  reactions. Measurements were made at the  
 132 University of Notre Dame (UND) Nuclear Science Lab-

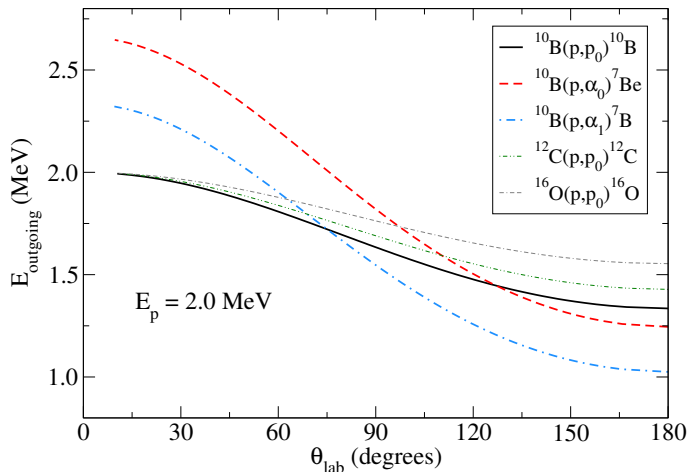


FIG. 2. Energies of outgoing particles for  $^{10}\text{B}+p$  and  $^{12}\text{C}(p,p)$  and  $^{16}\text{O}(p,p)$  reactions at  $E_p = 2.0$  MeV. The similar outgoing particle energies over the central angular range complicates measurements from  $E_p = 0.8$  to 3.0 MeV.

133 oratory (NSL) using a degrader foil method, while those  
 134 at the Edwards Accelerator Laboratory at Ohio Univer-  
 135 sity (OU) were performed using the time-of-flight (ToF)  
 136 technique. Additional details can be found in the Ph.D.  
 137 thesis of Vande Kolk [43].

### A. Notre Dame setup

139 For the experimental measurements at the UND NSL,  
 140 the 5 MV Stable ion Accelerator for Nuclear Astrophysics  
 141 (St. ANA) was used to produce proton beams between  
 142 0.8 and 2.0 MeV. The energy calibration of the beam was  
 143 determined using the energies of well known resonances  
 144 in the  $^{27}\text{Al}(p,\gamma)^{28}\text{Si}$  reaction [44], and was determined  
 145 to better than 1 keV over the energy range of the present  
 146 measurements. Beam intensities between 100 and 150 nA  
 147 were used and read from an electrically isolated beam  
 148 stop. The measurements were made using a 43 cm diam-  
 149 eter ORTEC scattering chamber as shown in Fig. 3. The  
 150 chamber was equipped with a double beam collimator  
 151 just before the entrance to the chamber, which was used  
 152 to define the beam spot on target to  $\approx 1.27$  cm diameter.  
 153 The beam stop was located  $\approx 0.61$  m downstream of the  
 154 target position and the exit port of the chamber was col-  
 155 limated to limit background from back-scattering off the  
 156 beam-stop. Eight S3590 Hamamatsu PIN photodiodes  
 157 (bare chip type,  $10 \times 10$  mm, 300  $\mu\text{m}$  thickness, biased to  
 158 +50 V), placed at  $\theta_{\text{lab}} = 45, 65, 75, 85, 95, 105, 115,$   
 159 and  $135^\circ$  were used for charged particle detection. The  
 160 Hamamatsu particle detectors were mounted in custom  
 161 housings and were doubly collimated. A 0.63 cm collima-  
 162 tor was placed directly in front of the detector, while the  
 163 second, of a smaller diameter, was mounted at the end of  
 164 a conical nose piece of either 0.25 or 0.30 cm in length.  
 165 These collimators were made of varying sizes (ranging

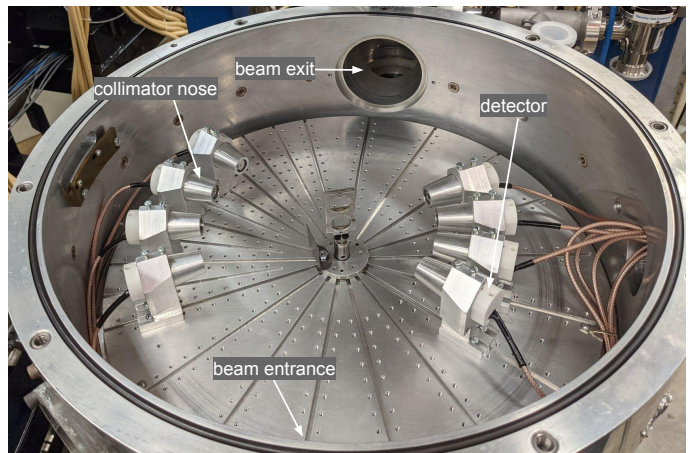


FIG. 3. Notre Dame experimental setup. See text for details.

166 from 0.13 to 0.51 cm), decreasing in diameter from back-  
 167 ward to forward angle, to achieve a similar count rate in  
 168 each detector. The target was placed at a  $45^\circ$  angle re-  
 169 lative to the incoming beam, allowing for the placement  
 170 of a set of detectors at both forward and backward an-  
 171 gles. The more forward set of detectors were placed at a  
 172 distance of 14.3 cm from the target, while those at back-  
 173 ward angles were placed at a distance of 10.7 cm. This  
 174 resulted in detection solid angles ranging from  $6.7 \times 10^{-5}$   
 175 to  $6.5 \times 10^{-4}$  sr.

176 As boron targets of the desired thickness are not self-  
 177 supporting, targets were prepared by evaporating en-  
 178 riched  $^{10}\text{B}$  powder (96%) onto thin ( $\approx 3.6 \mu\text{m}/\text{cm}^2$ ), self-  
 179 supporting, carbon foils. The evaporation was performed  
 180 at the NSL, producing  $^{10}\text{B}$  layers of  $5.0(5) \mu\text{g}/\text{cm}^2$ . The  
 181 carbon foils did provide an additional source of back-  
 182 ground from proton elastic scattering. Additional reac-  
 183 tions on carbon were not energetically allowed.

184 Fig. 2 shows the energies of the scattered protons and  
 185  $\alpha$ -particles from the  $^{10}\text{B}+p$  reactions at  $E_p = 2.0$  MeV  
 186 as well as background reactions from  $^{12}\text{C}(p,p)^{12}\text{C}$  and  
 187  $^{16}\text{O}(p,p)^{16}\text{O}$ . The carbon background comes mainly from  
 188 the thin carbon backing, but also is present from beam  
 189 induced carbon build up on the target. Oxygen contam-  
 190 ination is present from moisture in the carbon foil and  
 191 from oxidization and nitrogen contamination in the boron  
 192 target.

193 In order to separate  $\alpha$ -particle events from those of  
 194 proton produced by elastic scattering, a  $250 \mu\text{m}/\text{cm}^2$   
 195 carbon degrader foil was placed in front of each detec-  
 196 tor. Since the stopping cross section for protons is con-  
 197 siderably less than that of  $\alpha$ -particles in the degrader  
 198 foil, the  $\alpha$ -particle peaks are shifted by a greater amount  
 199 downward in energy. The thickness of  $250 \mu\text{g}/\text{cm}^2$   
 200 chosen as it was found to shift the  $\alpha$ -peaks downward  
 201 enough in energy to separate them from the proton scat-  
 202 tering peaks, but still leave them with enough energy  
 203 to be above the detector thresholds ( $\approx 400$  keV). Exam-  
 204 ple energy spectra for the same incoming beam energy

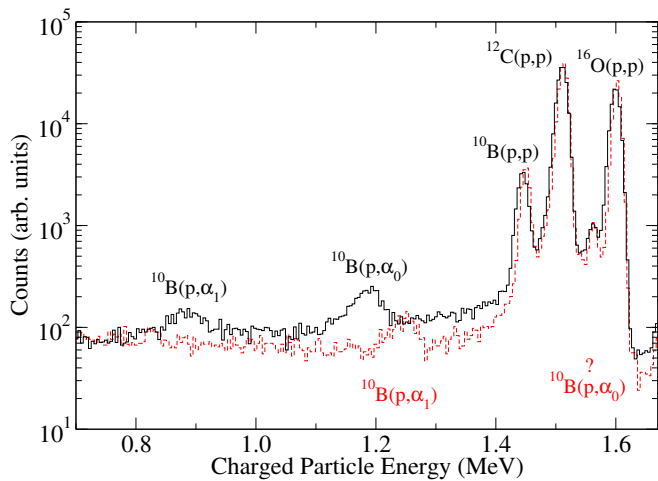


FIG. 4. Example energy spectra for  $E_p = 2.0$  MeV at  $\theta_{\text{lab}} = 115^\circ$  on a boron transmission target with thin self-supporting carbon backing with (solid black line) and without (red dashed line) a  $250 \mu\text{g}/\text{cm}^2$  carbon degrader foil. Without the degrader foil, the  $\alpha$ -particle peak from the  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  reaction is obscured beneath the elastic proton scattering peaks.

( $E_p = 2.0$  MeV) but with and without the degrader foil are shown in Fig. 4.

The electronics for each detector consisted of a Canberra Model 2003B pre-amplifier, an Ortec 671 spectroscopic amplifier (3  $\mu\text{s}$  shaping time), and finally a Canberra 8715 analog-to-digital converter (ADC). The ADCs were read into a FAST ComTec Base Module MPA-3 data acquisition system.

### B. Ohio University setup

Proton beams of between 20 and 100 nA were delivered to the target by the OU 4.5 MeV T-type tandem Pelletron accelerator. The proton beam was produced with 200 ns between bunches. A scattering chamber, customized for ToF-type experiments, was utilized. A detailed description of the chamber can be found in Wheeler [45]. Eight ORTEC silicon detectors (model # (B)U-013-100-100) were used for charge particle detection. In order to achieve sufficient ToF resolution, the three detectors at the most forward angles were placed at a distance of 1.0 m from the target, while the remainder were placed at 0.30 m. This provided sufficient ToF resolution for the proton and  $\alpha$ -particle events to be clearly distinguishable. Detectors were doubly collimated, with the first collimator (diameter of 1.27 cm) located near the edge of the scattering chamber at a distance of 13 cm from the target, while the second collimator (diameter of 1.67 cm) was placed directly in front of the detector. The detectors were positioned at angles of  $\theta_{\text{lab}} = 52.5, 67.5, 82.5, 97.5, 112.5, 127.5, 142.5,$  and  $157.5^\circ$ . Detector solid angles varied from  $2.4 \times 10^{-4}$  to  $3.5 \times 10^{-3}$  sr. For a clear view of the

target with each detector, the target was positioned at an angle of  $30^\circ$  from perpendicular to the incoming beam direction. The experimental setup is shown in Fig. 5.

Boron targets were produced in a similar manner as those described in Sec. II A, but with a higher enrichment of 99% in  $^{10}\text{B}$ . The target thicknesses were determined using an energy loss setup and a radioactive  $\alpha$ -source. Stopping cross sections were taken from SRIM-2013 [46]. In addition, the thickness was also determined during the peak fitting process of the experimental  $^{10}\text{B}(p, \alpha)^7\text{Be}$  yields. A single target was used for all experimental measurements at OU and was found to have a thin carbon backing of  $5.8(3) \mu\text{g}/\text{cm}^2$  and a boron thickness of  $53(3) \mu\text{g}/\text{cm}^2$ .

## III. DATA ANALYSIS

### A. Notre Dame data

Fig. 4 shows a typical spectrum from the measurements at the University of Notre Dame described in Sec. II A. Because of the significant amount of straggling suffered by the protons and  $\alpha$ -particles through the degrader foil, peak yields were determined by modeling the peak shapes with an exponentially-modified Gaussian and linear background term. As discussed in Sec. II A the number of protons that impinged on the target were determined by reading the current from an electrically isolated beam stop. The uncertainty in charge reading was found to be within 3%. The deadtime produced by proton scattering determined the beam intensity limit and was kept below 2%. This allowed a determination of the number of protons that impinged on the target ( $N_p$ ) to within 3% uncertainty.

Target stability studies were performed prior to the experimental data run. From repeated measurements of the yield at the same energy, it was found that very limited target deterioration occurred if beam intensities were kept below 200 nA. Thus, to be conservative, the measurements were performed with beam intensities below 150 nA. However, given the rather thin target (see Sec. II A), a systematic uncertainty of 5% was added to the overall uncertainty budget (see Table I).

The efficiency of each detector in the setup ( $\epsilon$ ) was determined using two methods: geometric measurement and yield measurements from the well known angular distribution of the  $E_p = 1366$  keV resonance in the  $^{27}\text{Al}(p, \alpha_0)^{24}\text{Mg}$  reaction [47]. The reaction produces a nearly isotropic distribution of  $\alpha$  particles (in the center of mass frame), with angular distribution coefficients of  $a_2 = -0.08(2)$  and  $a_4 = 0.00(2)$ . The two methods were found to agree to within uncertainties, giving an uncertainty in the relative angular distributions of 3%. The absolute differential cross section, assuming a thin target, can then be calculated by

$$\frac{d\sigma}{d\Omega_X} = A_X N_p N_B \epsilon, \quad (1)$$

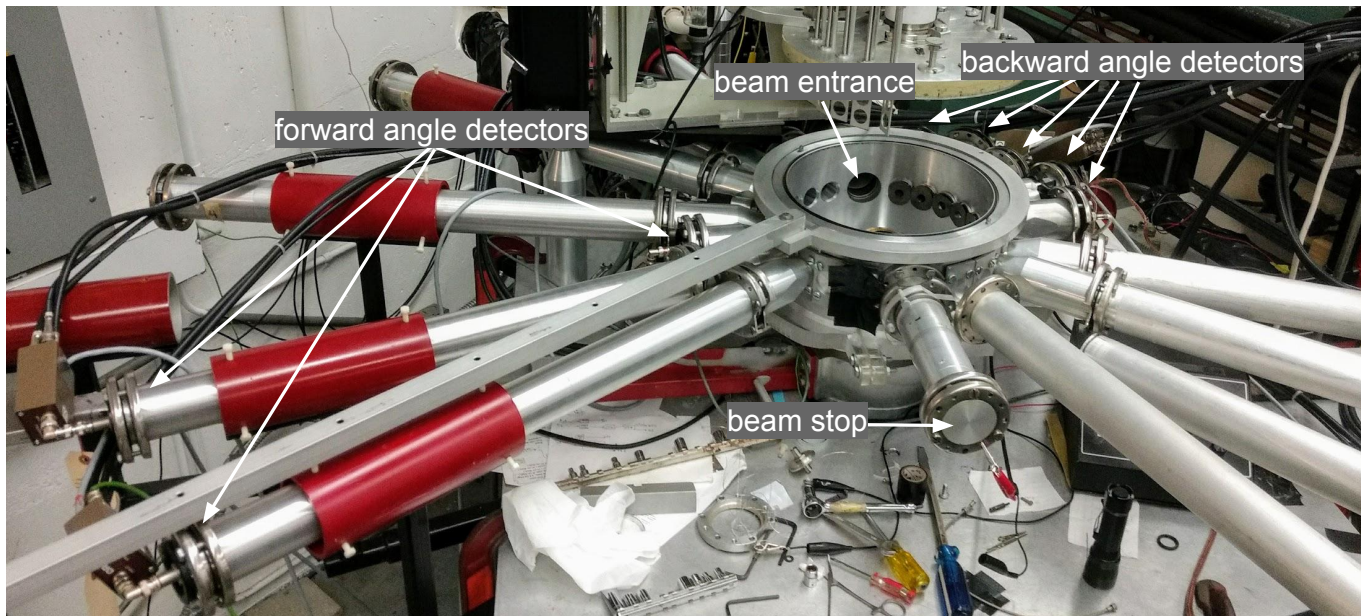


FIG. 5. Ohio University experimental setup. Particle detectors were placed at the end of the extension pipes that have been installed off of the main section of the scattering chamber. The larger distance between detector and target is required in order to provide sufficient resolution for particle identification using ToF. See text for details.

where the index  $X$  denotes either the  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  or  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  reaction,  $\frac{d\sigma}{d\Omega}$  is the differential cross section,  $A$  is the area of the peak from the charged particle spectrum,  $N_p$  are the number of protons made incident on the target,  $N_B$  are the number of boron atoms per unit area in the target, and  $\epsilon$  is the efficiency. Due to the very thin target (see Sec. II A) and the changes in the cross section as a function of energy, energy loss corrections (less than 1.25 keV) were negligible compared with the experimental uncertainties.

## B. Ohio University data

Fig. 6 (a) shows a typical ToF-versus-energy spectrum. As described in Sec. II B, the target-to-detector flight path provided sufficient resolution to distinguish clearly the different types of particles. Starting from the bottom of the figure, the four kinematic curves correspond to protons,  $^3\text{He}$ ,  $^4\text{He}$  and heavy recoils. Gating on the  $\alpha$ -particle curve results in the purple spectrum shown in Fig. 6 (b), while gating on the proton curve results in the blue spectrum shown in Fig. 6 (c). In both cases, the ungated spectrum is also indicated for comparison.

The relative efficiency of the setup was determined by geometric measurement and by comparison with the well-known scattering cross section of the  $^{12}\text{C}(p, p)^{12}\text{C}$  reaction [48]. The phenomenological  $R$ -matrix fit described in Azuma *et al.* [49] was used to interpolate the differential cross section from the angles of measurement by Meyer *et al.* [48] to those of the present experiment. Sensitivity tests found that variations of up to 5% were ob-

served in the calculations, in addition to the 3% systematic uncertainty quoted by Meyer *et al.* [48].

A complication in the measurement arose from unreliable current readings from the beam stop. As the individual scattering peaks were resolvable at most of the energies and angles of measurement, the  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  and  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  differential cross sections were determined relative to the  $^{12}\text{C}(p, p)^{12}\text{C}$  differential cross section, as the thickness of carbon and boron in the targets had been previously measured II B. Taking the uncertainty in the carbon target thickness (5%), the uncertainty in the boron target thickness of (6%), the systematic uncertainty from Meyer *et al.* [48] and an estimated 5% interpolation uncertainty from the  $R$ -matrix calculation, this normalization procedure contributes an estimated 10% to the systematic uncertainty budget.

Targets were tested for deterioration throughout the experiment by making repeated runs at the same energies to check for consistent yields. No measurable target degradation was observed. This was expected as the targets used at Ohio University were about an order of magnitude thicker than those used in the Notre Dame measurement and no degradation was observed. In addition, beam intensities used at Ohio University were less than those used at Notre Dame. As a further check, repeated measurements were made at several energies throughout the experiment, and consistent yields were obtained. Therefore, no additional uncertainty was included for target degradation for this portion of the experiment.

Differential cross sections were determined using the thin target approximation given by Eq. (1). While the

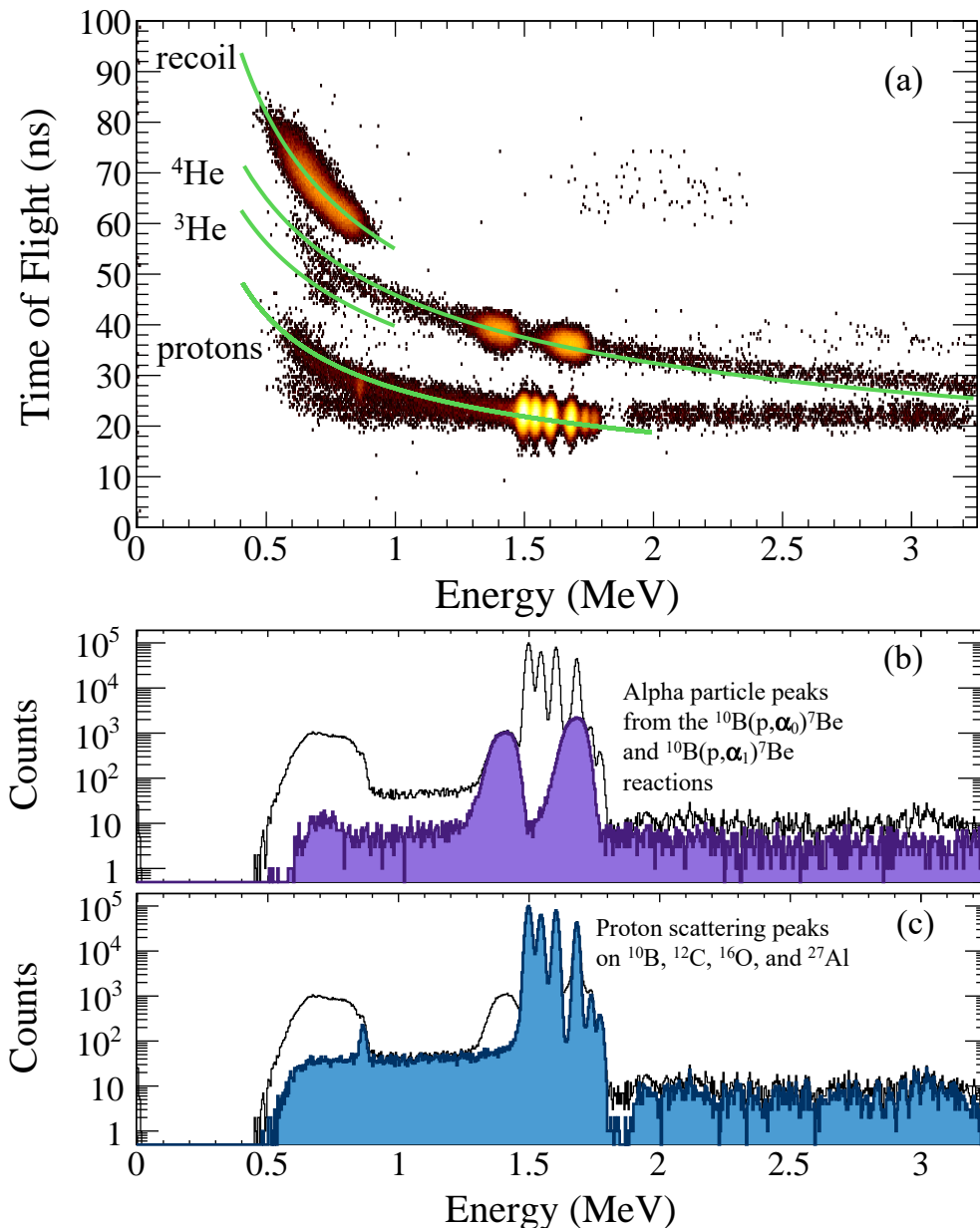


FIG. 6. ToF charged-particle spectra with the setup shown in Fig. 5 for  $E_p = 1.9$  MeV at 82.5 degrees. The green curves in Fig. 6 (a) indicate the kinematic curves for protons,  $^3\text{He}$ ,  $^4\text{He}$ , and heavy recoils. Figs. 6 (b) and (c) indicate the spectra obtained by gating on the  $\alpha$ -particle (purple) and proton (blue) curves. The ungated spectrum is also indicated for comparison. In (b), the two large, broad peaks correspond to the  $\alpha$ -particles coming from the  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  (higher energy) and  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  (lower energy). In (c), the cluster of proton scattering peaks around 1.5 MeV correspond to  $^{10}\text{B}$ ,  $^{12}\text{C}$ ,  $^{16}\text{O}$  and  $^{27}\text{Al}$  (from lowest to highest energy). **The smaller peak at about 0.8 MeV corresponds to inelastic proton scattering from the first excited state of  $^{10}\text{B}$ .** The flat background at higher energies comes from multiple scattering off of upstream beam line components.

348 target used for the Ohio University experiments was ap- 356  
 349 proximately an order of magnitude thicker than that used 357  
 350 for the University of Notre Dame measurements, the thin 358  
 351 target approximation is still a good approximation. The  
 352 proton energy loss through the boron target ranged from  
 353 13 keV at  $E_p = 800$  keV to 7 keV at  $E_p = 2$  MeV. The ex-  
 354 perimental data for both measurements can be found in  
 355 the Supplemental Material [50] and are shown in Figs. 7

and 8. The systematic uncertainties are summarized in  
 Table I.

#### IV. R-MATRIX ANALYSIS

359 One of the main difficulties encountered in the  $R$ -  
 360 matrix fit of Wiescher *et al.* [21], was the lack of con-

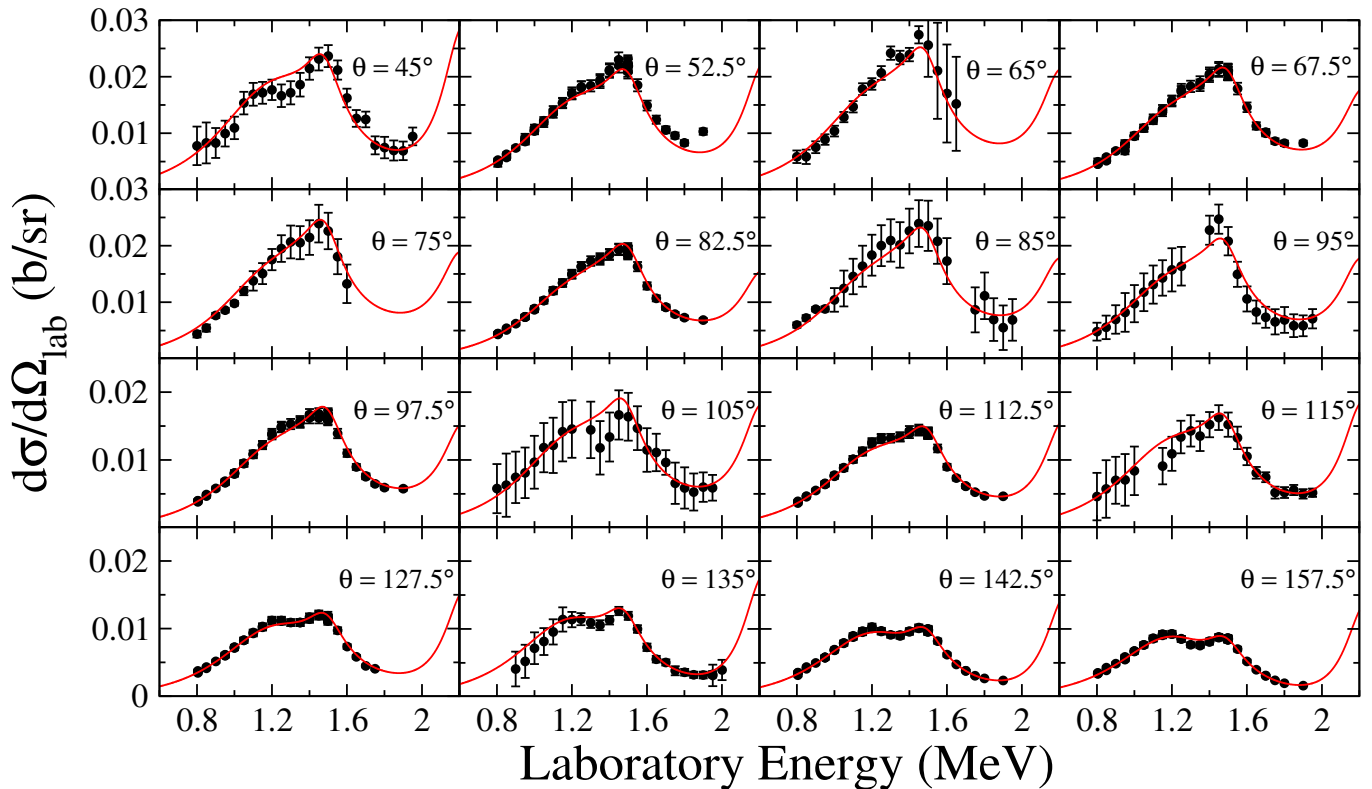


FIG. 7. Experimental measurements of the  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  reaction from the present work. The Notre Dame data were measured at whole angles, while those at OU at half angles. The red solid line indicates the  $R$ -matrix fit described in Sec. IV. All quantities are in the laboratory frame of reference. For comparison with figures later in the text that are given in the center of mass frame, the energy scale should be multiplied by a factor of  $\approx 10/11$ .

TABLE I. Summary of systematic uncertainty estimates.

Systematic Uncertainty Contribution	%
<b>University of Notre Dame</b>	
$^{10}\text{B}$ target thickness	10
Target degradation	5
Beam current reading	3
Total	12
<b>Ohio University</b>	
$^{10}\text{B}$ target thickness	6
$^{12}\text{C}$ target thickness	5
systematic uncertainty from Meyer <i>et al.</i> [48]	3
$R$ -matrix interpolation	5
Total	10

361 straint on the position and width of the broad resonances  
 362 that are the **dominant** contributors to the cross sections  
 363 of the  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  and  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  reactions over the  
 364 range from  $E_{c.m.} \approx 1$  to 2 MeV. The new data presented  
 365 here were measured specifically to remedy this issue, and,  
 366 as will be shown, they largely do so. The  $R$ -matrix fits  
 367 presented here were done in three parts. First, a fit to  
 368 only the data from the present work and the  $^{10}\text{B}(p, p)^{10}\text{B}$   
 369 data of Chiari *et al.* [51] was **performed** in order to **focus**  
 370 on the region from  $E_{c.m.} \approx 1$  to 2 MeV. Then the fit was

371 extended to very low energies using a few representative  
 372 data sets [21, 28, 30, 39] in order find if a consistent fitting  
 373 over the wider energy range could be achieved. Finally,  
 374 the fit was further extended to the  $^{10}\text{B}(p, \gamma)^{11}\text{C}$  data of  
 375 Wiescher *et al.* [52], which has never been previously in-  
 376 cluded in an  $R$ -matrix analysis.

377 In this work, cross sections are reported for the  
 378  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  and  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  reactions as these yields  
 379 were observed to dominate over the entire energy  
 380 range ( $0.8 < E_p < 2.0$  MeV). However, the reactions  
 381  $^{10}\text{B}(p, p_1)^{10}\text{B}$  and  $^{10}\text{B}(p, ^3\text{He})^8\text{Be}$  are also energetically  
 382 possible. Weak proton peaks corresponding to inelastic  
 383 proton scattering were observed in some runs, but since  
 384 their yields were approximately an order of magnitude  
 385 smaller than the  $^{10}\text{B}(p, \alpha)^7\text{Be}$  reactions, the  $p_1$  reaction  
 386 channel is neglected in the  $R$ -matrix analysis. Likewise,  
 387 no yields were observed for the  $^{10}\text{B}(p, ^3\text{He})^8\text{Be}$ , so the  
 388  $^3\text{He}$  channel is also neglected.

389 For the  $R$ -matrix fits presented here, the code  
 390 AZURE2 [49, 53] has been used. The code uses the alter-  
 391 native  $R$ -matrix parameterization of Brune [54] to work  
 392 directly with observed widths and energies and to re-  
 393 move the need for boundary conditions. This only leaves  
 394 the channel radius model parameters, which were chosen  
 395 as 5.0 fm for the proton channels and 5.5 fm for the  $\alpha_0$   
 396 and  $\alpha_1$  channels. Masses and particle separation energies



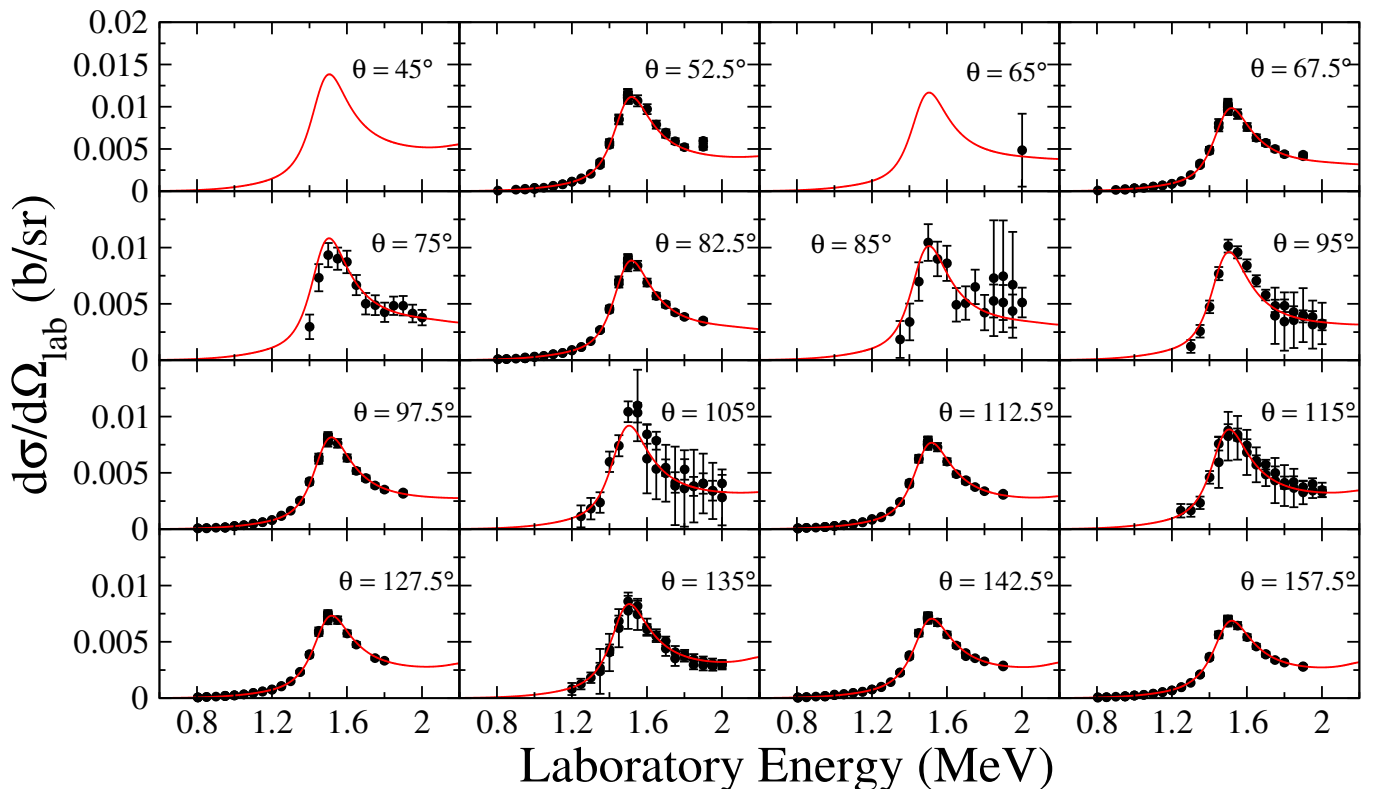


FIG. 8. As Fig. 7, but for the  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  reaction.

397 were taken from the AME mass evaluations [55, 56] and  
 398 were treated as constants. The corrections due to energy  
 399 loss through the target were performed using the exper-  
 400 imental effect routine of AZURE2, where stopping powers  
 401 were taken from the code SRIM-2013 [46].

#### A. Present Data

403 As the present  $^{10}\text{B}(p, \alpha_{0,1})^7\text{Be}$  data and the  
 404  $^{10}\text{B}(p, p_0)^{10}\text{B}$  from Chiari *et al.* [51] provide com-  
 405 prehensive measurements over the energy range from  
 406  $E_p = 0.8$  to  $2.0$  MeV for all of the dominant reaction  
 407 channels, these data sets provide sufficient constraint  
 408 for an initial multichannel  $R$ -matrix fit. Starting from  
 409 the levels and their parameters listed in the most  
 410 recent ENSDF evaluation [42], it was quickly apparent  
 411 that the angular distributions of the  $^{10}\text{B}(p, p_0)^{10}\text{B}$  and  
 412  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  data could be reproduced, but those of  
 413 the  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  data could not.

414 In particular, the  $^{10}\text{B}(p, p_0)^{10}\text{B}$  data can be well  
 415 described by the  $J^\pi = 7/2^+$  level at  $E_x = 10.05$  MeV  
 416 ( $E_{c.m.} = 1.36$  MeV) and the  $9/2^+$  level at  
 417  $E_x = 10.71$  MeV ( $E_{c.m.} = 2.02$  MeV), which are  
 418 clearly visible resonances in the data. In addition, the  
 419 near threshold  $5/2^+$  level at  $E_x = 8.699$  MeV and a  
 420 high energy  $5/2^+$  background level are also needed  
 421 to reproduce the scattering cross sections. For the

422  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  data, the  $7/2^+$  level at  $E_x = 10.05$  MeV  
 423 ( $E_{c.m.} = 1.36$  MeV) dominates the cross section. The  
 424  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  differential cross sections were much more  
 425 challenging to reproduce. From the experimental data  
 426 at backward angles, it is clear that two resonances are  
 427 present, one at  $E_{c.m.} \approx 1.05$  MeV ( $E_x = 9.74$  MeV)  
 428 and another at  $E_{c.m.} \approx 1.36$  MeV ( $E_x = 9.74$  MeV).  
 429 Moving forward in angle, the relative strength of the  
 430  $E_{c.m.} \approx 1.05$  MeV resonance decreases compared to the  
 431  $E_{c.m.} \approx 1.36$  MeV resonance, making the separation of  
 432 the two resonances more difficult to identify. This was  
 433 previously observed in the measurements of Brown *et al.*  
 434 [24] and Cronin [26].

435 The identification of the spin-parity of the levels that  
 436 correspond to these two broad resonances is obfuscated  
 437 by the strong interference between not only these two  
 438 resonances, but also the underlying tails of other broad  
 439 resonances at both higher and lower energies. In particu-  
 440 lar, the interference pattern between the two resonances  
 441 was very challenging to reproduce simultaneously at all  
 442 angles. This is further complicated because the spin of  
 443  $^{10}\text{B}$  is  $3^+$ . This means that there are often multiple chan-  
 444 nel spins ( $s$ ) / relative orbital angular momentum ( $\ell$ )  
 445 channels that are possible for each level and multiple  $J^\pi$   
 446 that are populated with the same  $\ell$  for the  $^{10}\text{B}+p$  par-  
 447 ticle partition. For example, both  $3/2^+$  and  $1/2^+$  levels  
 448 can be populated through  $\ell = 2$ , and for  $3/2^+$ , there  
 449 are two possible channels, for channel spins  $5/2$  and  $7/2$ .

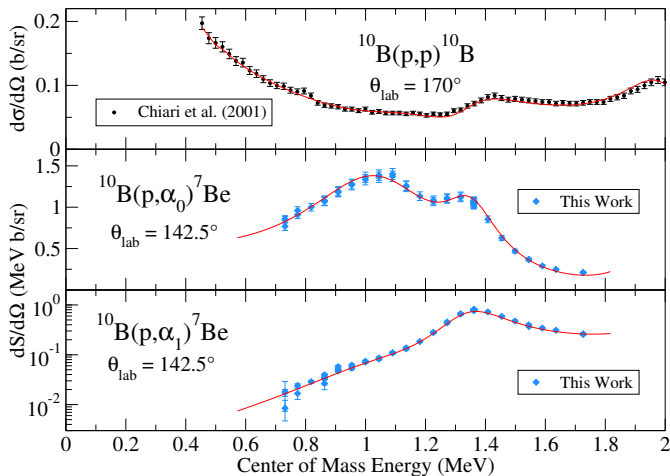


FIG. 9.  $R$ -matrix fit, shown at representative angles, to the present  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  and  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  data as well as the  $^{10}\text{B}(p, p_0)^{10}\text{B}$  data of Chiari *et al.* [51].

450 The fitting is made further challenging because depend-  
 451 ing on the particular channels used, or combinations of  
 452 channels, differences in the angular distributions can be  
 453 produced. These differences are at a level that is often  
 454 similar to the uncertainties in the data, making discern-  
 455 ing the correct solution quite challenging.

## B. Extension to Low Energy

456  
 457 The  $R$ -matrix fit to data of just this work (Sec. IV A)  
 458 was then expanded to the low energy range using a few  
 459 representative data sets [21, 28, 30, 39]. These data were  
 460 found to be generally in agreement with the present mea-  
 461 surements in the region of overlap. The exception are  
 462 the  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  data of Wiescher *et al.* [21], which de-  
 463 viated substantially from the present measurements. At  
 464  $E_{c.m.} > 1.0$  MeV, the data are in excellent agreement  
 465 with the present measurements if they are re-normalized  
 466 by a factor of 0.6. At higher energies, the data become  
 467 suddenly quite inconsistent in their energy dependence  
 468 as well. In light of this discrepancy, a re-examination  
 469 of the data of Wiescher *et al.* [21] found that the data  
 470 were measured at different experimental facilities, which  
 471 may have introduced a systematic error in the high en-  
 472 ergy data taken at the Ohio State CN VdG facility under  
 473 very limited beam current conditions. These energy data  
 474 were therefore discarded from the analysis, as indicated  
 475 in Fig. 11.

476 Unfortunately, these types of data inconsistencies are  
 477 quite common in the literature data, as mentioned in  
 478 Sec. I and as highlighted in Wiescher *et al.* [21]. This  
 479 is why this preliminary fit to higher energies is limited  
 480 to only a few data sets, and even among those, incon-  
 481 sistencies can be seen in some overlapping regions. The  
 482 consistency achieved between the two independent mea-  
 483 surements presented in this work provide additional con-

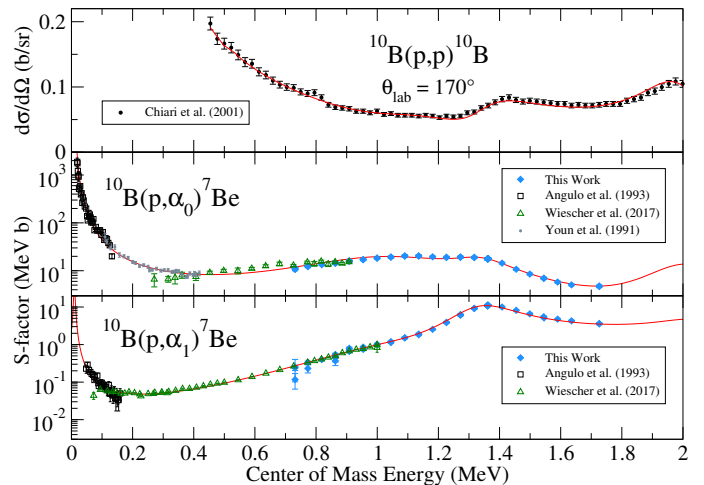


FIG. 10.  $R$ -matrix fit extended to low energy. The fit included the present data for the  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  and  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  reactions as well as the lower energy data sets of Angulo *et al.* [30] Angulo *et al.* [39], Wiescher *et al.* [21], and Youn *et al.* [28], and the  $^{10}\text{B}(p, p_0)^{10}\text{B}$  data of Chiari *et al.* [51]. The fit was made directly to the differential cross section data of the present measurement, but the data were angle integrated for visual comparison with the other angle-integrated data sets.

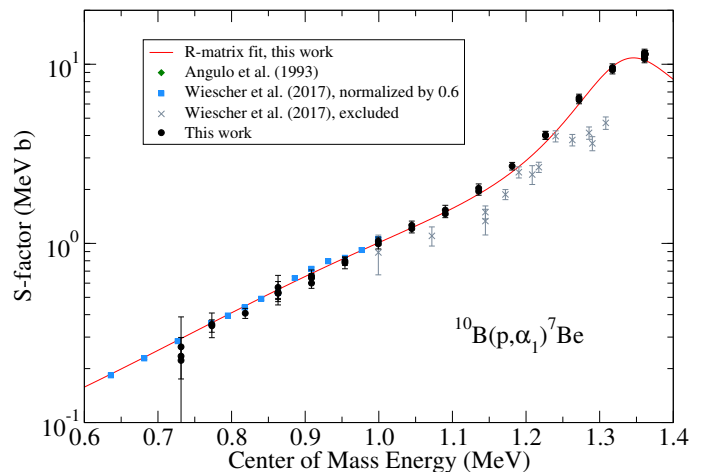


FIG. 11. Comparison of the  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  data (black circles) and  $R$ -matrix fit (red line) from the present work with the data of Wiescher *et al.* [21]. At  $E_{c.m.} < 1.0$  MeV, the data of Wiescher *et al.* [21] are in good agreement with the present measurements if they are re-normalized by a factor of 0.6 (blue squares). At higher energies, it is recommended that the data of Wiescher *et al.* [21] be excluded, as they deviate from the present measurements in energy dependence as well. See text for details.

484 fidence in their accuracy. These issues will be discussed  
 485 further in Sec. V.

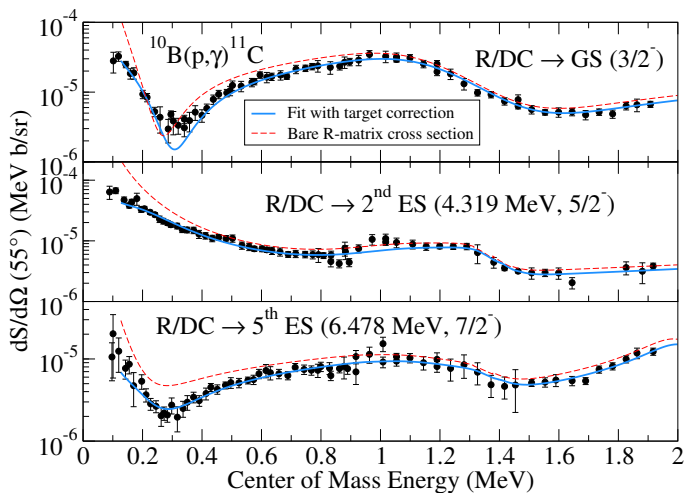


FIG. 12.  $S$ -factors showing the  $R$ -matrix fit to the primary-transition capture data of Wiescher *et al.* [52] that contain significant resonance contributions. The blue solid line represents the  $R$ -matrix  $S$ -factor corrected for the experimental target effects quoted in Wiescher *et al.* [52], while the red dashed line represents the bare  $R$ -matrix  $S$ -factor.

### C. Extension to Capture

In order to check the consistency with the present fit to the radiative capture data of Wiescher *et al.* [52], the primary transition cross sections were investigated. The data were not available in tabular form and were obtained from the EXFOR database [57], where the data had been digitized from Fig. 5 of Wiescher *et al.* [52]. A more limited fit was performed where the particle widths were held fixed to the values obtained from the fit to the particle data, and only the  $\gamma$ -ray partial widths and asymptotic normalization coefficients were allowed to vary. It was found that a good reproduction of the capture data of Wiescher *et al.* [52] could be achieved, but with this more limited set of positive parity levels as shown in Fig. 12. For the data of Wiescher *et al.* [52], target effect corrections were found to be quite significant. Calculations of both the experimental effects corrected and bare  $R$ -matrix  $S$ -factors are shown in Fig. 12.

In this work, only the capture  $S$ -factors for the three transitions that have significant resonance contributions were investigated (ground state, 3<sup>rd</sup>, and 5<sup>th</sup> excited states). It was found that the dominant resonance contributions came from the levels corresponding to the near threshold ( $E_x = 8.699$  MeV,  $E_{c.m.} = 0.01$  MeV) and that at  $E_x = 9.96$  MeV ( $E_{c.m.} = 1.27$  MeV), both of which are  $5/2^+$  levels with incoming angular momentum  $\ell = 0$ . External capture contributions were also found to be significant for all three transitions. The only region of the capture data that was not well fit was in the transition to the third excited state in the energy region around  $E_{c.m.} \approx 1$  MeV ( $E_x \approx 9.69$  MeV) (see Fig. 12), where there seems to be an additional resonance contribution.

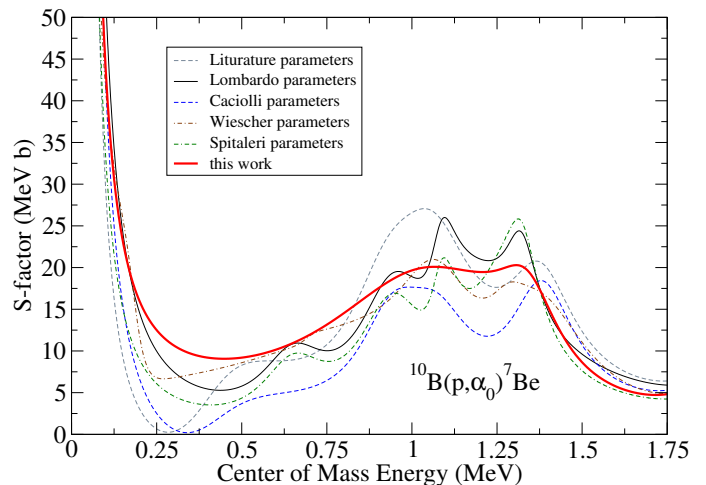


FIG. 13. Comparison of  $S$ -factors determined from recent  $R$ -matrix fits by Lombardo *et al.* [31] (black solid line), Cacioli *et al.* [60] (blue dashed line), and Wiescher *et al.* [21] (brown dotted-dashed line), Spitaleri *et al.* [36] (green dashed-dashed-dotted line) using level parameters from the ENSDF evaluation [42] (grey dashed line) and the present work (red solid line).

Thus, there remains the possibility that an additional level could be present in this region.

## V. DISCUSSION

In Wiescher *et al.* [21] (Fig. 9), the discrepancies between different previous measurements of the  $^{10}\text{B}(p, \alpha)^7\text{Be}$  reaction were highlighted, in particular the ground state transition. It was also shown how these discrepancies led to large variations in the  $R$ -matrix fits reported recently [21, 31, 60]. These previous  $R$ -matrix calculations of the  $S$ -factors are compared in Fig. 13, along with that of the present work.

The present data indicate less underlying structure than previously proposed. In particular, Wiescher *et al.* [52] proposed that three negative parity states are present between the proton threshold and  $E_x = 10$  MeV. The combination of inconsistent  $^{10}\text{B}(p, \alpha)^7\text{Be}$  data and the inclusion of these states, led to an overfitting of the data and to the more oscillatory  $S$ -factors compared to the present calculation as shown in Fig. 13. Table III summarizes the levels reported in the ENSDF evaluation [42] that were not needed to describe the data in the present analysis. This reduction in levels and the improved energy and angular coverage of the present data has led to a significant reduction in the uncertainty of the cross section over the energy range of the present data ( $0.8 < E_p < 2.0$  MeV). Variations of up to 50% have been shown to be present between recent  $R$ -matrix fits that cover this energy range. Compared to the recent evaluation by Wiescher *et al.* [21], deviations as large as 20% exist. The present measurements reduce the uncer-

TABLE II.  $R$ -matrix parameters for the analysis of the  $^{11}\text{C}$  system. The partial widths are in units of keV and excitation energies in MeV. The sign of the partial width indicates the interference sign of the corresponding reduced width amplitude. Parameters that were varied in the fitting are marked in **bold**. The level parameter uncertainties were estimated using codes BRICK [58] and emcee [59]. **Some level parameters have been reported previously in the literature and are compared using the format (this work / ENSDF evaluation [42]).**

$J^\pi$	$E_x$	this work / ENSDF evaluation [42]		$\Gamma_{p0}$	$\Gamma_{\alpha 0}$	$\Gamma_{\alpha 1}$	$\Gamma_{\text{total}}$
		$s$	$l$				
$5/2^+ / 5/2^+$	8.6987/8.699(2)	5/2	0	<b><math>2.5^{+1.2}_{-1.1} \times 10^{-17}</math></b>	15		15(1)
		3/2	1				
		1/2	3				
$(3/2^+) / 5/2^+$	<b><math>9.744^{+0.011}_{-0.008}</math></b> / 9.20(5)	5/2	0	<b><math>13.4^{+4.4}_{-2.5}</math></b>	<b><math>430^{+180}_{-190}</math></b>	<b><math>-17^{+1}_{-1} \times 10^{-3}</math></b>	491.6/500(90)
		3/2	1				
		1/2	3				
$(5/2^+)$	<b><math>9.962^{+0.013}_{-0.006}</math></b>	5/2	0	<b><math>124^{+6}_{-5}</math></b>	<b><math>565^{+27}_{-29}</math></b>	<b><math>-51.2^{+7.5}_{-11.3}</math></b>	740
		3/2	1				
		1/2	3				
$7/2^+ / (7/2^+)$	<b><math>10.0465^{+0.0011}_{-0.0011}</math></b> / 10.083(5)	7/2	0	<b><math>52.6^{+1.7}_{-1.8}</math></b>	<b><math>58.4^{+2.4}_{-2.3}</math></b>	<b><math>51.5^{+2.7}_{-2.6}</math></b>	218/230(20)
		3/2	3				
		1/2	3				
$9/2^+ / (9/2^+)$	<b><math>10.7123^{+0.0015}_{-0.0017}</math></b> / 10.679(5)	5/2	2	<b><math>-34.3^{+8.5}_{-12.4}</math></b> <b><math>-114^{+2.3}_{-2.4}</math></b>	<b><math>72^{+22}_{-18}</math></b>	<b><math>106.7^{+2.0}_{-2.1}</math></b>	250/200(30)
		7/2	2				
		3/2	3				
		1/2	5				
$(7/2^+)^{\text{a}}$	11.44 / 11.44(1)	7/2	0	<b><math>1260^{+60}_{-70}</math></b>			
$5/2^{+\text{a}}$	15	1/2	3			<b><math>-213^{+16}_{-17}</math></b>	
		5/2	0	<b><math>8400^{+400}_{-400}</math></b>	<b><math>533^{+150}_{-160}</math></b>		
		3/2	1				

<sup>a</sup> The  $7/2^+$  and  $5/2^+$  energy levels at 11.44 MeV and 15 MeV, respectively, are background levels.

TABLE III. Summary of levels reported in the ENSDF evaluation [42] but found not to be needed in the  $R$ -matrix description of the present data.

$J^\pi$	$E_x$	$\Gamma_{\text{total}}$
$(3/2^-)$	9.645(50)	210(40)
$(5/2^-)$	9.780(50)	240(50)
$(7/2^-)$	9.970(50)	120(20)

548 tainty in this region to the 10-12% level, that is, that of  
549 the dominant systematic uncertainties (see Table I).

550 In addition to fewer levels, the present fit also fa-  
551 vored a change in the spin-parity assignment for the  
552 low-lying broad resonance from  $5/2^+$  to  $3/2^+$ . While  
553 the width obtained here is similar to that quoted in the  
554 ENSDF evaluation [42], the energy is significantly higher,  
555 as summarized in Table II. For the  $7/2^+$  and  $9/2^+$  levels  
556 at  $E_x = 10.05$  and  $10.7$  MeV, it is suggested that the  
557 tentative spin-parity assignments in the compilation be  
558 changed to firm assignments, as they are uniquely con-  
559 strained by the scattering data of [51]. Different spin-  
560 parity combinations were investigated in the present work  
561 and only the suggested ones were found to reproduce  
562 the angular distributions of both the  $^{10}\text{B}(p, \alpha)^7\text{Be}$  and  
563  $^{10}\text{B}(p, p)^{10}\text{B}$  data simultaneously.

564 For the reasons discussed in Sec. I, there are lim-  
565 ited previous measurements over the energy range of

566 this study that the present data can be compared to di-  
567 rectly. The only two available are those of Brown *et al.*  
568 [24] (1951) and Cronin [26] (1956). As shown in Fig. 14,  
569 the present data are generally consistent with those of  
570 Cronin [26], both the excitation functions and angular  
571 distributions. This is also true for the  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$   
572 data of Brown *et al.* [24], but their  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  have  
573 a somewhat different energy dependence than those of  
574 the present study. The sparsity of both data sets and  
575 the inconsistent data of Brown *et al.* [24] complicated  
576 the fitting described in Wiescher *et al.* [21], motivating  
577 the present measurements.

578 Fig. 15 compares the  $^{11}\text{B}(p, \alpha)^8\text{Be}$  and  $^{10}\text{B}(p, \alpha)^7\text{Be}$   
579 data sets over the energy range pertinent for aneutronic  
580 fusion (see Sec. I). For the  $^{11}\text{B}(p, \alpha)^8\text{Be}$  reaction, the first  
581 excited state transition dominates the total cross section  
582 over this energy range. For the  $^{10}\text{B}(p, \alpha)^7\text{Be}$  reaction, the  
583  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  transition dominates at low energies, but  
584 the  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$  transition begins to make a substantial  
585 contribution to the total at  $E_p \approx 1$  MeV. In Fig. 15,  
586 the sum of the present  $^{10}\text{B}(p, \alpha_0)^7\text{Be}$  and  $^{10}\text{B}(p, \alpha_1)^7\text{Be}$   
587 data have been taken and the total  $^{10}\text{B}(p, \alpha)^7\text{Be}$  cross  
588 section is shown. While the  $^{11}\text{B}(p, \alpha)^8\text{Be}$  cross section is  
589 much larger than that of the  $^{10}\text{B}(p, \alpha)^7\text{Be}$  reaction over  
590 most of the energy range, the two become comparable at  
591  $E_p \approx 1$  MeV.

592 Finally, while the current measurements do not reach  
593 down into the low energy range needed for laser-driven,

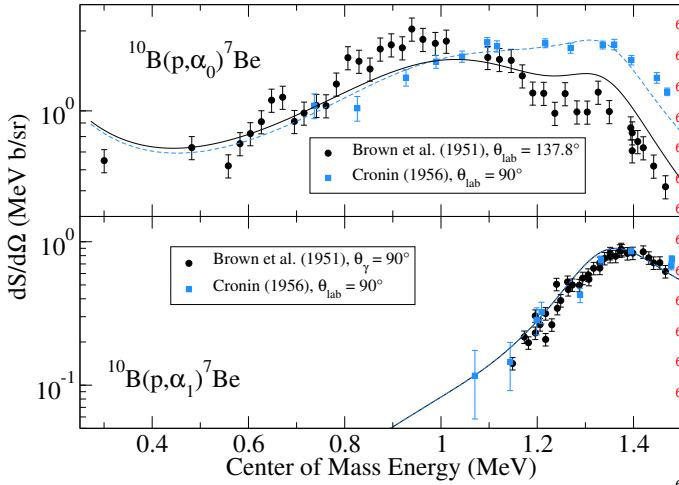


FIG. 14. Comparison of the  $R$ -matrix fit to the data of the present work (solid and dashed lines) to the data of Brown *et al.* [24] and Cronin [26]. Note that the cross sections of Brown *et al.* [24] were determined through the detection of 429 keV isotropic secondary  $\gamma$ -rays, while those of Cronin [26] were through  $\alpha$ -particle detection.

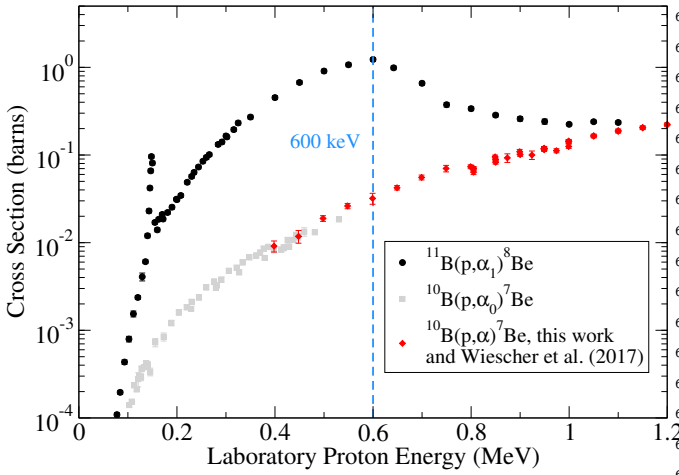


FIG. 15. Comparison of the  $^{11}\text{B}(p,\alpha)^8\text{Be}$  [14] (black circles) and  $^{10}\text{B}(p,\alpha_0)^7\text{Be}$  [21, 28, 30] (grey squares) cross section data over the energy range of interest for aneutronic fusion applications. The present  $^{10}\text{B}(p,\alpha)^7\text{Be}$  total cross section data are indicated by the red diamonds.

hot plasma facilities ( $\approx 10$  keV), they provide much more stringent constraints on the background contributions for future phenomenological  $R$ -matrix analyses that will be used to evaluate lower energy measurements. The present measurements can also provide a check on the overall normalization of these lower energy studies, where an absolute normalization can be more challenging, if they extend high enough in energy to overlap. This is especially important for THM measurements, which have to be normalized to higher energy data, as they lack their own independent normalization. For the  $^{10}\text{B}(p,\alpha)^7\text{Be}$  reaction, the THM measurements [33–36] are the only data

that scan over the near threshold resonance that dominates the low energy cross section. A comprehensive re-evaluation of the very low energy cross section is beyond the scope of this work. While the present data are a step forward in this effort, large inconsistencies are present in the currently available low energy data [21], which means that a re-evaluation with this same data would likely not result in a significant decrease in the uncertainty. Therefore, a consistent set of new low energy measurements is called for, at which point, they can be combined with the present work to produce an improved evaluation of the low energy  $^{10}\text{B}(p,\alpha)^7\text{Be}$  reaction.

## VI. SUMMARY

The  $^{10}\text{B}(p,\alpha)^7\text{Be}$  reaction is a potential diagnostic reaction for aneutronic fusion and laser-driven, hot-plasma facilities. However, despite a large amount of experimental data, the cross section was quite uncertain because of conflicting measurements and a lack of measurements of certain energy and angular ranges. In the present work, new measurements have been performed for the  $^{10}\text{B}(p,\alpha)^7\text{Be}$  reaction, clearly discriminating the  $^{10}\text{B}(p,\alpha_0)^7\text{Be}$  and  $^{10}\text{B}(p,\alpha_1)^7\text{Be}$  yields from the elastic scattering yields using either degrader foil or time-of-flight techniques. The resulting differential cross sections cover an experimentally-challenging energy region from  $E_p = 0.8$  to 2 MeV with greater energy and angular coverage and smaller uncertainties. The new data have enabled a much more confident  $R$ -matrix description of not only the  $^{10}\text{B}(p,\alpha_0)^7\text{Be}$ ,  $^{10}\text{B}(p,\alpha_1)^7\text{Be}$ , and  $^{10}\text{B}(p,p)^{10}\text{B}$  cross sections, resolving discrepancies between previous data sets, but also provided a consistent description of the  $^{10}\text{B}(p,\gamma)^{11}\text{C}$  data for the first time. It was found that the  $^{10}\text{B}(p,\alpha)^7\text{Be}$  and  $^{10}\text{B}(p,\gamma)^{11}\text{C}$  data could be described with only the positive parity states reported previously in the literature, which has shed light on the fitting inconsistencies observed in other recent  $R$ -matrix analyses. The present data thus reduce the uncertainty in the cross section over the energy range important for aneutronic fusion (200 to 1000 keV) and set the stage for a new  $R$ -matrix evaluation of the  $^{11}\text{C}$  system, paving the way for an improved determination of the very low energy ( $\approx 10$  keV) cross-section region needed for laser-driven fusion applications.

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