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Proton branching ratios of math xmlns="http://www.w3.org/1998/Math/MathML">mmultiscripts>mi>Mg/mi>mprescripts>/mprescripts>none>/none> mn>23/mn>/mmultiscripts>/math> levels

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Proton branching ratios of ²³Mg levels

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Abstract

Background: The anomalous 22 Ne abundance measured in certain presolar graphite grains is thought to arise from the decay of 22 Na that was synthesized at high temperatures in core-collapse supernovae. To better interpret this abundance anomaly, the primary destruction mechanism of 22 Na, the 22 Na(p,γ) 23 Mg reaction, must be better understood.

Purpose: Determine proton branching ratios of several ²³Mg excited states that play a role in the high-temperature ²²Na (p,γ) ²³Mg reaction rate.

Methods: Particle decays of 23 Mg excited states populated with the previously reported 24 Mg(p,d) 23 Mg transfer reaction measurement [Kwag et al., Eur. Phys. J. A 56, 108 (2020)] were analyzed to extract proton branching ratios. The reaction was studied using a 31-MeV proton beam from the Holifield Radioactive Ion Beam Facility of Oak Ridge National Laboratory and 24 Mg solid targets.

Results: Proton branching ratios of several ²³Mg excited states in the energy range of $E_x = 8.044$ - 9.642 MeV were experimentally determined for the first time for the p0 and p1' (p1+p2+p3) decay channels.

Conclusions: These new branching ratios for 23 Mg levels can provide an experimental foundation for an improved high-temperature rate of the 22 Na $(p,\gamma)^{23}$ Mg reaction needed to understand production of anomalously high 22 Ne abundance in core-collapse supernovae.

I. INTRODUCTION

The radionuclide 22 Na ($t_{1/2} = 2.6$ y) can be synthesized during nova and supernova explosions. In novae, 22 Na is created via either the 21 Ne(p,γ) 22 Na reaction or the β^+ -decay of 22 Mg [1, 2]. When 22 Na β -decays to the first excited state of 22 Ne, the characteristic 1.275 MeV γ -ray follows. This γ -ray is a target of several current and future space-based γ -ray telescopes including the International Gamma-Ray Astrophysics Laboratory (INTE-GRAL) [3], Advanced Compton Telescope (ACT) [4] and enhanced ASTROGAM [5]. In core-collapse supernovae, 22 Na is mainly created through the 21 Ne(p,γ) 22 Na reaction [6]. A high abundance ratio of 22 Ne in presolar graphite grains is thought to mainly originate

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from core-collapse supernovae. This is the so-called Ne-E(L) anomaly as the abundance is notably different from the solar abundance [6–9]. The 22 Na $(p,\gamma)^{23}$ Mg reaction is believed to play a crucial role in understanding the destruction of 22 Na during both nova and supernova explosions. As the reaction proceeds through resonances in 23 Mg, the spectroscopic information of resonant states located above the proton threshold at 7.581 MeV is required to estimate the 22 Na $(p,\gamma)^{23}$ Mg reaction rate. Owing to this importance, many studies have been conducted on the energy levels of 23 Mg [10–18].

One of the important properties needed to estimate the reaction rate is the proton branching ratio. In recent studies that utilized β -delayed proton emissions of ²³Al, for instance, the proton decay branching ratios of a few ²³Mg levels were obtained at energies near $E_x = 7.8 \text{ MeV}$ [14, 15, 17, 18] which provide critical information for the ²²Na(p,γ)²³Mg reaction rate calculations. As the proton threshold energy of ²³Mg is 7.581 MeV [19], the energy levels studied in those references fall in the Gamow window for T = 0.1 - 0.5 GK, which corresponds to nova temperatures. In Ref. [17], β -delayed proton emission spectra at higher energy regions were obtained. However, as the transition intensities were normalized to that of the 451 keV line, more studies on the proton branching ratios of populated ²³Mg levels are required to estimate the ²²Na(p,γ)²³Mg reaction rate accurately at high temperatures.

In the present work, the proton decay branching ratios of several 23 Mg levels populated from a previously reported 24 Mg(p,d) 23 Mg transfer reaction study [20] were investigated as a follow-up analysis. The reaction was measured to help determine the astrophysical 22 Na(p,γ) 23 Mg reaction rate at nova temperatures. The angular distributions of deuterons from the reaction were extracted to constrain the spins and parities of the populated 23 Mg energy levels. The spin value of $J^{\pi} = 5/2^+$ for the 7.788 MeV level, which is the dominant resonance for the 22 Na(p,γ) 23 Mg reaction at nova temperatures, was adopted in the reaction rate calculations. The result showed that the updated reaction rate was approximately a factor of three smaller than that from the literature at T=0.3 GK. Because many 23 Mg energy levels in the range of $E_x=6.537$ - 9.642 MeV were observed in Ref. [20] through the (p,d) transfer reaction, the current analysis of the proton branching ratios can significantly enhance our knowledge of the high-temperature burning of the radionuclide 22 Na.

II. EXPERIMENT

The experimental setup was described in detail in Ref. [20]. A 31-MeV proton beam at an intensity of ~ 60 pA was produced at the Holifield Radioactive Ion Beam Facility at Oak Ridge National Laboratory. The beam bombarded an isotopically-enriched (> 99.9%) 24 Mg solid target with an areal density of $\sim 520~\mu\mathrm{g/cm^2}$. A large-area Silicon Detector Array (SIDAR, [21]) was placed at forward angles to detect charged particles from the 24 Mg $(p,d)^{23}$ Mg transfer reactions. A thick (9.5 mm) aluminum plate with a 19 mm diameter hole was placed directly in front of the target ladder to protect the fragile silicon detectors from the halo of the intense beam. The SIDAR comprised four trapezoidal wedges of $\Delta E - E$ telescopes. Each telescope was configured with a 100- μ m-thick energy loss (ΔE) detector backed by a 1000- μ m residual energy (E) detector for standard energy loss techniques. The angles covered by the detector array were $16.8^{\circ} \leq \theta_{\text{lab}} \leq 44.8^{\circ}$. The energy response of each silicon strip was calibrated using an α -emitting source composed of 239 Pu (5.157 MeV), ²⁴¹Am (5.486 MeV) and ²⁴⁴Cm (5.805 MeV). The energy resolutions were measured to be approximately 1% for the α particles. Deuterons from the $^{24}{\rm Mg}(p,d)^{23}{\rm Mg}$ reaction were clearly identified using the standard energy loss techniques. To better reconstruct the excitation energies, internal energy calibrations were also performed using six well-known 23 Mg energy levels: the ground state and excited states at $E_x=2.359,\,2.771,\,5.286,\,5.992$ and 9.642 MeV. A total of 17 ²³Mg levels were identified at excitation energies less than approximately 9.7 MeV.

III. RESULTS AND ANALYSIS

A. Coincident events

Events from the proton decay of 23 Mg were identified by requiring coincidence between the deuterons from the 24 Mg $(p,d)^{23}$ Mg reaction and the decay protons. When two charged particles fell within an event window of $\sim 4\mu$ s, the events were considered coincident. Decay protons stopped at the first layer of the detectors (ΔE) were analyzed in present work. A decay proton energy versus coincident reaction deuteron energy plot for all identified events is shown in Fig. 1. By considering the coincidence, only 23 Mg nuclei produced from the 24 Mg $(p,d)^{23}$ Mg reaction could be considered in the present analysis. Proton decays of 23 Mg

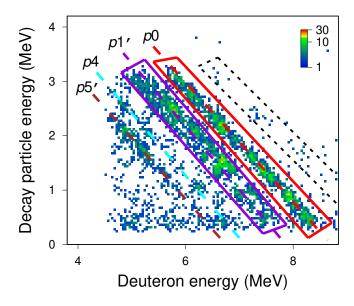


FIG. 1. (Color online) Decay particle energy versus coincident reaction deuteron energy plot for all identified events. Four major diagonal bands labeled as p0, p1', p4, and p5' are evident. Each band represents a proton decay channel. Only the events falling in the red and purple gates were used to determine branching ratios, and are associated with the ground state (p0) and three closely located levels of 22 Na at $E_x = 582.8$, 657.0, and 890.9 keV (p1'), respectively. The weak band in the black dotted gate shows the decay events originated from the impurity of the target.

that originate from other possible reaction mechanisms such as the $^{24}\text{Mg}(p,2n)^{23}\text{Al}$ reaction followed by β -decays of ^{23}Al were excluded by detecting the deuterons instead of the ^{23}Mg recoils.

As shown in Fig. 1, four major diagonal bands are evident. Each diagonal band represents a proton decay channel: the p0 channel for the decay to the ground state of 22 Na; p1' for a combined channel of three closely spaced final levels of 22 Na at $E_x = 582.8$, 657.0 and 890.9 keV (p1, p2, and p3); p4 for the decay to the 22 Na level at 1527.7 keV; and p5', again, for a combined channel of three closely spaced final levels at 1937.0, 1951.7, and 1983.1 keV (p5, p6, and p7). The closely spaced energy levels in the p1' and p5' groups could not be fully resolved in the present analysis. The events located left to the p5' channel are thought to be decay protons from higher proton decay channels overlapped with α decay channels, exhibiting no clear bands. Background events consist of decay protons from the impurities in the target and random coincidences. For instance, a possible proton decay channel of

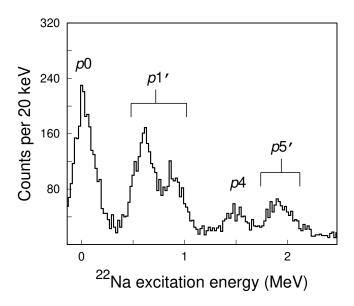


FIG. 2. Reconstructed 22 Na excitation energy spectrum from the proton-deuteron coincidences in Figure 1. The peak-like structures labeled as p1' and p5' are associated with three closely spaced levels each that could not be fully resolved in the present work.

 15 O, which was populated by 16 O(p,d) 15 O, to the ground state of 14 N can be found in Fig. 1 (black dotted box). It did not affect the current analysis as the band is not overlapped with the 23 Mg proton decay channels. The decay protons from the other potential impurities such as 12 C are energetically far away from the energy region of interest. Because some random coincidences were evident at deuteron energies higher than those relevant for the events in the rightmost gate of Fig. 1, where particle decay is energetically forbidden, another gate was implemented in this region to estimate the level of random coincidences. The 22 Na excitation energy was reconstructed using the energies of the coincident particles for each identified event. The results are shown in Fig. 2.

B. Decay-gated spectra and Branching ratios

Fig. 3 (a) shows the deuteron single spectrum obtained from the previous 24 Mg(p,d) 23 Mg measurement [20]. The excitation energies reported in the reference are indicated in MeV for several identified levels in this deuteron energy range. Fig. 3 (b) shows the spectra gated on the p0 and p1' groups in Fig. 1.

For the first step of the branching ratio estimation, each identified peak in Fig. 3 (a) was

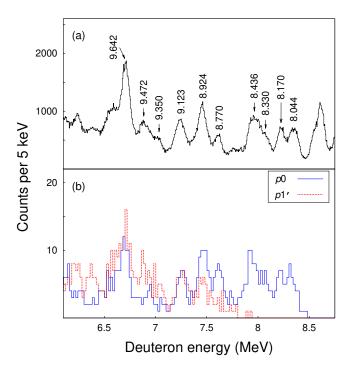


FIG. 3. (Color online) (a) Deuteron energy spectrum obtained from the 24 Mg $(p,d)^{23}$ Mg reaction measurement [20]. Identified 23 Mg levels are labeled with their excitation energies in MeV. (b) Gated spectra of the coincident protons for the p0 (blue solid line) and p1' (red dotted line) channels.

Gaussian-fitted. Then, the corresponding peak in the decay-gated spectra was also fitted to obtain the number of proton decay events using the same parameters such as the centroid and width. The geometric detection efficiency (\sim 2%) obtained by assuming isotropic decay was also used in the branching ratio estimations. A discussion of the isotropy assumption is presented in Sec. III C. By comparing the number of decay-gated events to that of deuteron singles for each identified ²³Mg level in the energy range of $E_x = 8.044 - 9.642$ MeV, the proton branching ratios of several transitions in the p0 and p1' channels could be obtained. The corresponding results are summarized in Table I. The uncertainty due to the isotropic assumption had the largest contribution to the total uncertainty of each branching ratio (see Sec. III C). The statistical uncertainty was less than 10% of the total uncertainty in most cases. The random background contribution was approximately 4% for b_{p0} of $E_x = 8.044$ and 8.170 MeV and $b_{p1'}$ of $E_x = 8.924$ MeV, whereas those for the other branching ratios were negligible. The diagram of the relevant energy levels and decay channels are shown in Fig. 4.

Several peaks apparent in the deuteron singles were not included in the proton branching ratio estimations because of poor statistics. Although the energy levels at $E_x = 9.350$ and 9.472 MeV were clearly identified in Ref. [20], for instance, the corresponding peaks in the decay-gated proton energy spectrum were rather featureless and therefore could not be well fitted. The branching ratios for the p4 and p5' channels were not extracted, as the excitation energies of the 23 Mg levels associated with those channels are higher than those reported in the previous study [20], except for the states at E_x =9.123 and 9.642 MeV. Although these states are located above the thresholds of p4 and p5' channels, the decay energies were so small to observe or no legitimate peak was obtained.

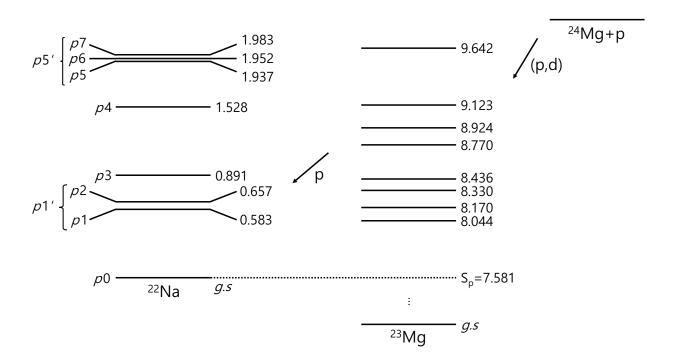


FIG. 4. A diagram of the involved energy levels of 22 Na and 23 Mg along with decay channels. Energies are in units of MeV.

The proton energy spectrum of the coincident events obtained for the p0 channel is shown in Fig. 5 as a black solid line. The excitation energies of 23 Mg associated with several identified peaks are indicated in MeV. The expected proton energy spectrum is also displayed as the red dotted line in the figure. This spectrum was obtained in the following manner. Relativistic kinematics calculations were performed by considering the excitation energies in 23 Mg, angular distributions of deuterons and proton branching ratios extracted in the

TABLE I. Proton branching ratios (b_p) of ²³Mg levels extracted for p0, p1', p1, p2, and p3. The excitation energy values were taken from Ref. [20]. Uncertainties include factors originated from the statistics, backgrounds, and discrepancy between isotropic and anisotropic decay. See Sec. III C for detailed argument on isotropic and anisotropic decay.

| E_x (keV) | b_{p0} | $b_{p1'}$ | b_{p1} | b_{p2} | b_{p3} |
|--------------|-----------------|-----------------|-------------------|-------------------|-------------------|
| 8044 ± 4 | 0.36 ± 0.11 | | | | |
| 8170 ± 4 | 0.36 ± 0.12 | | | | |
| 8330 ± 6 | 0.48 ± 0.15 | | | | |
| 8436 ± 7 | 0.59 ± 0.18 | | | | |
| 8770 ± 8 | 0.86 ± 0.27 | | | | |
| 8924 ± 5 | 0.47 ± 0.15 | 0.26 ± 0.08 | (0.13 ± 0.04) | (0.01 ± 0.01) | (0.12 ± 0.04) |
| 9123 ± 7 | 0.36 ± 0.11 | 0.35 ± 0.11 | (0.06 ± 0.02) | (0.27 ± 0.09) | (0.03 ± 0.01) |
| 9642 | 0.37 ± 0.11 | 0.49 ± 0.15 | (0.14 ± 0.05) | (0.26 ± 0.08) | (0.08 ± 0.03) |

TABLE II. Observed and calculated proton energies and their uncertainties for identified transitions. All proton energies are in keV.

| | p0 (k | æV) | | | | |
|-------------|---------------------|-------------|-------------------------------|----------------------|----------------|--------------|
| | Expected | Measured | Expected | | | Measured |
| E_x (keV) | $E_f = \text{g.s.}$ | | $E_f = 583 \text{ keV } (p1)$ | $657~{\rm keV}~(p2)$ | 891 keV $(p3)$ | |
| 8044 | 498 ± 60 | 510 ± 95 | | | | |
| 8170 | 653 ± 72 | 709 ± 65 | | | | |
| 8330 | 800 ± 29 | 841 ± 15 | | | | |
| 8436 | 899 ± 110 | 940 ± 59 | | | | |
| 8770 | 1289 ± 129 | 1285 ± 98 | | | | |
| 8924 | 1441 ± 36 | 1448 ± 49 | 843 ± 33 | 751 ± 40 | 525 ± 39 | 589 ± 142 |
| 9123 | 1631 ± 130 | 1642 ± 96 | 1051 ± 43 | 975 ± 42 | 726 ± 39 | 1003 ± 120 |
| 9642 | 2180 ± 235 | 2231 ± 15 | 1588 ± 62 | 1513 ± 60 | 1275 ± 56 | 1554 ± 155 |

present work. The production of deuterons through the $^{24}{\rm Mg}(p,d)^{23}{\rm Mg}$ transfer reaction and isotropic proton decay of $^{23}{\rm Mg}$ levels were assumed in the calculations. As shown in

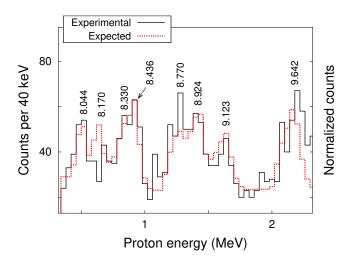


FIG. 5. (Color online) Proton energy spectrum for the coincident events falling in the p0 gate (black solid line). Identified ²³Mg energy levels are labeled with their excitation energies in MeV. The expected proton energy spectrum (displayed as the red dotted line) well reproduces the experimental result.

the figure, the empirical proton energy spectrum can be well reproduced for the p0 channel, indicating that the extracted branching ratio values are well estimated.

Because the p1' channel contains three final states in 22 Na that were not fully resolved in the present work, the expected proton energy spectrum for the channel could not be reconstructed using the same method as that for the p0 channel analysis. As the first approach, the proton energy spectrum was calculated by assuming equal contributions from three levels to the obtained p1' branching ratios summarized in Table I. The calculated spectrum is shown in Fig. 6 (a) with the experimental result. The calculated proton energies, along with the corresponding observed energies, are summarized in Table II for the 11 identified transitions. Three apparent peaks in the experimental spectrum that are located at $E_p = 0.589$, 1.003, and 1.554 MeV are associated with the transitions from 23 Mg levels at $E_x = 8.924$, 9.123 and 9.642 MeV, respectively.

As shown in Fig. 6 (a), some of the expected peaks notably differ from the empirical results at the corresponding proton energy regions. To fit the expected result to the empirical one, the branching ratios of the p1, p2, and p3 channels ($E_f = 0.583$, 0.657, and 0.891 MeV) were parameterized. The best fitting result is shown in Fig. 6 (b). The contributions from the p1, p2, and p3 channels to the p1' branching ratio were determined through the fitting. The

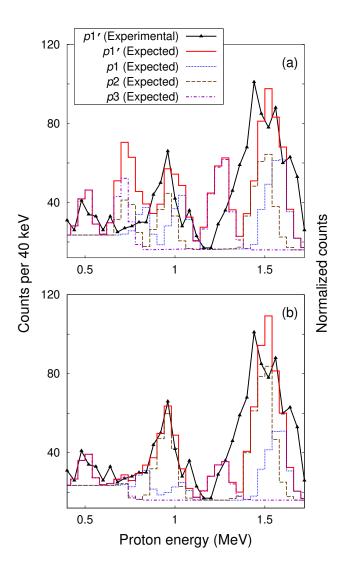


FIG. 6. (Color online) Similar to Fig. 5, the empirical proton energy spectrum for the p1' channel (black solid line). (a) The expected proton energy spectra obtained by assuming equal contributions from three final levels are also shown. (b) The expected spectra after the fit are shown (see text).

results are presented in Table I as individual branching ratios. The uncertainty contribution from statistics was less than 50% in these branching ratios. Results show that the transitions from $E_x = 8.924$ MeV state through p2 channel and the one from $E_x = 9.123$ MeV state through p3 channel are rather weak to have the branching ratios of less than 5%. Strong branches were obtained for the transitions associated with the p2 channel except for the one from $E_x = 8.924$ MeV state.

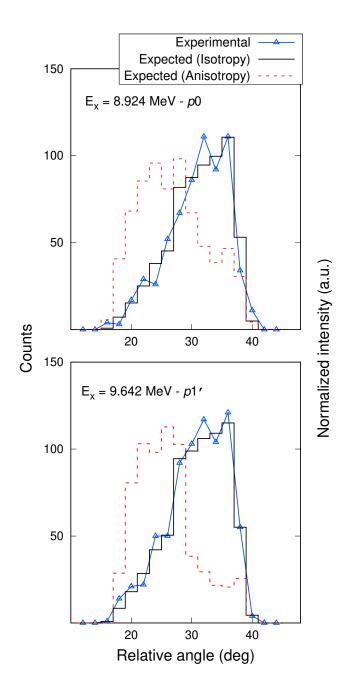


FIG. 7. (Color online) Counts of decay protons from the 8.924 MeV (9.642 MeV) level as a function of relative angle for the p0 (p1') channel is shown in the top (bottom) panel as a blue solid line. The expected distributions assuming isotropic and anisotropic decay of protons are shown as a black solid and a red dotted line, respectively.

C. Isotropic and Anisotropic decay

The relative angle (i.e., the angle between the reaction deuteron and decay proton) was deduced for each identified decay event for the $E_x = 8.924$ (9.642) MeV level through the p0 (p1') decay as shown in the top (bottom) panel of Fig. 7. Because the angular distributions of decay protons could not be sufficiently obtained owing to limited statistics, an isotropic decay in the center of the mass frame was assumed for the branching ratio calculations. Moreover, because the laboratory and the center of the mass frames are similar in the case of normal kinematics, isotropic decay in the laboratory frame could be used instead. As the decay protons are emitted at each angle with the same probability under this assumption, the expected intensity as a function of the relative angle can be derived from the angular distribution of deuterons.

The calculated distributions for $E_x = 8.924$ and 9.642 MeV level are shown as black solid lines in the top and bottom panels of Fig. 7, respectively. While the transitions from unbound levels in 23 Mg would be mostly anisotropic except for l = 0 transfer, the assumption of isotropy resulted in good agreement between the empirical and calculated distributions. As previously done in Refs. [22, 23], a relative angle histogram for anisotropic decay was also considered by assuming a sinusoidal variation, as indicated by the red dashed line in the figure. The results show that assuming the isotropic decays for the observed transitions is reasonable. Nevertheless, the conservative systematic uncertainty of 30% was introduced for the extracted branching ratios to account for any possible discrepancies between isotropic and anisotropic decays, as has been done in Refs. [22, 23].

IV. ASTROPHYSICAL 22 Na $(p,\gamma)^{23}$ Mg REACTION RATE

For novae, states in 23 Mg just above the proton binding energy are dominant resonances for the proton capture reaction 22 Na $(p,\gamma)^{23}$ Mg. Even with the results from direct measurements of the reaction, the reaction rate still remains uncertain [10, 11, 13]. Several previous studies implemented indirect measurements using beta-delayed decay of 23 Al have been performed as well, focusing on the state near $E_x \sim 7.8$ MeV [14, 15, 17, 18]. They measured the proton branching ratio as it is critically concerned with the partial widths of the state $(b_p = \Gamma_p/\Gamma_{tot})$ and, correspondingly, the resonance strength. Most recently, M. Friedman et

al. [18] reported the proton branching ratio value of $6.5(8) \times 10^{-3}$ for the E_x =7.79 MeV level, which is a factor of 5 lower compared to the previous value. This shows the importance of precise estimations on the proton branching ratios of 23 Mg.

For core-collapse supernovae, investigations on the properties of higher lying states are required as they have much higher temperatures compared to novae. For the most part, only the upper limits of the resonance strengths could be deduced through the direct measurements [10, 11]. An indirect study using 22 Na+p resonant scatterings estimated two resonance strengths of E_x =8.793(13) and 8.916(15) MeV by relying on the shell-model calculations [24]. They calculated the strengths by assuming $\Gamma_{p0}/\Gamma_{tot} \approx 1$. If the two states are the same states with the ones at E_x =8.770(8) and 8.924(5) MeV in the current measurements, the resonance strengths will be lowered by factors of 0.86 and 0.47, respectively, which would lower the 22 Na(p,γ) 23 Mg reaction rate from their estimate [24]. The current branching ratios can be useful to calculate the strengths of additional resonances. However, the other critical nuclear properties of the states needed to calculate the partial widths, including spin-parities and half-lives, are mostly unknown. Additional measurements or theoretical model calculations are therefore needed to determine a new proton capture rate on 22 Na at supernova temperatures.

V. CONCLUSION

As a follow-up analysis of previously reported $^{24}\text{Mg}(p,d)^{23}\text{Mg}$ reaction measurements, decay protons from excited states in ^{23}Mg were investigated to obtain proton branching ratios of the populated levels. By detecting the reaction products and decay particles simultaneously, several proton decay branches of ^{23}Mg levels could be identified: the p0 channel for the decay to the ground state of ^{22}Na and the p1' channel for the three closely spaced levels at $E_x = 582.8, 657.0$, and 890.9 keV.

Proton branching ratios for 8 (3) transitions associated with the p0 (p1') channel were obtained for the energy levels in ²³Mg ranging from $E_x = 8.044$ to 9.642 MeV. Isotropic decay in the center of the mass frame was assumed and the geometric detection efficiency was considered in the branching ratio calculations. Proton decay of ²³Mg levels to higher lying states in ²²Na was also observed. However, the corresponding branching ratios could not be extracted because the peaks of interest were not obtained. Excitation energies of the

levels investigated in the present work correspond to $E_{\text{c.m.}} \sim 0.4$ - 2 MeV for the astrophysical $^{22}\text{Na}(p,\gamma)^{23}\text{Mg}$ reaction rate, which is relevant for core-collapse supernova scenarios. The impact of these branching ratios on the high-temperature $^{22}\text{Na}(p,\gamma)^{23}\text{Mg}$ thermonuclear reaction rate will be explored in the future with additional measurements.

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