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Abstract

The aCORN experiment measures the neutron decay electron-antineutrino correlation (*a*-coefficient) using a novel method based on an asymmetry in proton time-of-flight for events where the beta electron and recoil proton are detected in delayed coincidence. We report the data analysis and result from the second run at the NIST Center for Neutron Research, using the high-flux cold neutron beam on the new NG-C neutron guide end position: $a = -0.10758 \pm 0.00136(\text{stat}) \pm 0.00148(\text{sys})$. This is consistent within uncertainties with the result from the first aCORN run on the NG-6 cold neutron beam. Combining the two aCORN runs we obtain $a = -0.10782 \pm 0.00124(\text{stat}) \pm 0.00133(\text{sys})$, which has an overall relative standard uncertainty of 1.7 %. The corresponding result for the ratio of weak coupling constants $\lambda = G_A/G_V$ is $\lambda = -1.2796 \pm 0.0062$.

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16 I. INTRODUCTION

¹⁷ The free neutron decays into a proton, electron, and antineutrino via the charged-current ¹⁸ weak interaction. This is the simplest example of nuclear beta decay. In contrast to beta ¹⁹ decay of most nuclei, the dynamics of neutron decay are undisturbed by nuclear structure ²⁰ effects. Experimental observables can be directly related to fundamental parameters in the ²¹ theory. As a result, neutron decay is an excellent laboratory for studying details of the ²² weak nuclear force and searching for hints of physics beyond the Standard Model (SM). The ²³ important experimental features of neutron decay are described by the formula of Jackson, ²⁴ Treiman, and Wyld [1], which gives the decay probability N of a spin-1/2 beta decay system ²⁵ in terms of the neutron spin polarization \boldsymbol{P} , the beta electron total energy and momentum ²⁶ E_e , \boldsymbol{p}_e , and the antineutrino total energy and momentum E_{ν} , \boldsymbol{p}_{ν}

$$N \propto \frac{1}{\tau_n} E_e |\boldsymbol{p_e}| (Q - E_e)^2 \left[1 + a \frac{\boldsymbol{p_e} \cdot \boldsymbol{p_\nu}}{E_e E_\nu} + b \frac{m_e}{E_e} + \boldsymbol{P} \cdot \left(A \frac{\boldsymbol{p_e}}{E_e} + B \frac{\boldsymbol{p_\nu}}{E_\nu} + D \frac{(\boldsymbol{p_e} \times \boldsymbol{p_\nu})}{E_e E_\nu} \right) \right].$$
(1)

Q = 1293 keV is the neutron-proton mass difference, m_e is the electron mass, and τ_n is the neutron lifetime. Here and throughout velocity is in units with c = 1. The parameters a, A, B, and D are correlation coefficients which are measured by experiment. We note that a, b are parity conserving, A, B are parity violating, and D violates time-reversal symmetry. The Fierz interference parameter b is zero in the SM; it would be generated by the presence of scalar or tensor weak currents. Neglecting recoil order effects, the values of the other coefficients are related to two basic parameters in the theory: the nucleon weak vector and axial vector coupling constants G_V and G_A . Writing their ratio as $\lambda = G_A/G_V$ we have [1]

$$\tau_n = \frac{2\pi^3 \hbar^7}{(G_V^2 + 3G_A^2)m_e^5 f_R} \qquad a = \frac{1 - |\lambda|^2}{1 + 3|\lambda|^2}$$
$$A = -2\frac{\operatorname{Re}\{\lambda\} + |\lambda|^2}{1 + 3|\lambda|^2} \qquad B = -2\frac{\operatorname{Re}\{\lambda\} - |\lambda|^2}{1 + 3|\lambda|^2} \qquad D = 2\frac{\operatorname{Im}\{\lambda\}}{1 + 3|\lambda|^2} \tag{2}$$

35

³⁶ where
$$f_R$$
 is the value of the integral over the Fermi energy spectrum. There are two main
³⁷ motivations for precision measurements of neutron decay observables.

The first is to accurately determine the values of G_V and G_A . These constants appear not only in neutron decay but in many other weak interaction processes involving free neutrons and protons that are important in astrophysics, cosmology, solar physics, and neutrino the detection [2, 3]. The value of G_V gives the first element V_{ud} of the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix: $G_V = G_F V_{ud}$, where G_F is the universal weak ⁴³ coupling constant obtained from the muon lifetime. A very important low energy test of the⁴⁴ Standard Model is the unitarity of the first row of the CKM matrix

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1.$$
(3)

⁴⁵ The term $|V_{ub}|^2$ is small enough to be neglected so in practice this is a precise comparison of ⁴⁶ V_{ud} and V_{us} . A real violation of this unitarity condition would be a clear sign of new physics ⁴⁷ Beyond the Standard Model (BSM) at the low energy, precision frontier. For example ⁴⁸ supersymmetry loop corrections could cause a departure from equation 3 at the few 10^{-4} ⁴⁹ level and reveal new physics that lies beyond present constraints from the Large Hadron ⁵⁰ Collider [4].

The second motivation is to search for small discrepancies in the values of these observ-⁵² ables that could result from BSM physics. We see from equation 2 that a measurement of ⁵³ τ_n and any one of a, A, or B determine the real values of G_V and G_A , but new physics ⁵⁴ could introduce dependencies on additional new parameters. A useful model-independent ⁵⁵ self-consistency test is obtained from the Mostovoy parameters [5]

$$F_1 = 1 + A - B - a = 0$$

$$F_2 = aB - A - A^2 = 0.$$
(4)

⁵⁶ which follow algebraically from the relations in equation 2. Inserting the Particle Data Group ⁵⁷ 2020 (PDG 2020) [6] recommended values we have $F_1 = 0.0056 \pm 0.0041$ and $F_2 = 0.0014 \pm$ ⁵⁸ 0.0028, consistent with the SM expectations. The PDG 2020 experimental uncertainty in ⁵⁹ the *a*-coefficient is the largest contributor to the uncertainties in F_1 and F_2 . We note that ⁶⁰ recoil order corrections will cause F_1 and F_2 to differ from zero at the 10^{-4} level, but those ⁶¹ corrections are calculable. Important model-dependent tests for new physics can be made ⁶² with neutron decay observables. The relative values of *a*, *A*, and *B* can be related to the ⁶³ strength of hypothetical right-handed weak forces and scalar and tensor forces [7, 8]. Gardner ⁶⁴ and Zhang have shown that a comparison of *a* and *A* at the 10^{-3} level can place sharp limits ⁶⁵ on possible conserved-vector-current (CVC) violation and second-class currents [9]. Possible ⁶⁶ extensions to the Standard Model, such as supersymmetry or left-right symmetric models, ⁶⁷ could lead to observable departures from the predictions in equations 2.

Figure 1 summarizes the current experimental results for G_A and G_V . The PDG 2020 recommended value $\lambda = -1.2756 \pm 0.0013$ includes nine measurements of the neutron decay ⁷⁰ coefficients A and a from 1986 to 2019, and the uncertainty is expanded by a factor of ⁷¹ 2.6 due to poor agreement. The most recent and precise results for the beta asymmetry ⁷² A from the PERKEO II,III [10, 11] and UCNA [12] experiments are in good agreement ⁷³ and give a more negative value of λ . The neutron lifetime averages from beam method ⁷⁴ and ultracold storage experiments significantly disagree, see for example [13]. The value of ⁷⁵ $G_V = 1.13625(24) \times 10^{-5} \text{ GeV}^{-2}$ from an evaluation of 222 measurements of 20 superallowed ⁷⁶ beta decay systems [14] agrees moderately with the CKM unitarity requirement (using the ⁷⁷ PDG 2020 V_{us} [6]), differing by 1.2σ . But a 2018 calculation of electroweak box diagram ⁷⁸ contributions to the "universal" radiative correction Δ_R by Seng, *et al.* [15, 16] shifted the ⁷⁹ superallowed result down to $G_V = 1.13570(16) \times 10-5 \text{ GeV}^{-2}$ which would violate CKM ⁸⁰ unitarity by 4.5σ . In a subsequent paper Czarnecki, Marciano, and Sirlin [17] recommend ⁸¹ an intermediate value for Δ_R and hence G_V . The 2018 Seng, *et al.* result is supported by ⁸² new theoretical work within the past year [18, 19].

83 II. EXPERIMENTAL METHOD

The traditional method for measuring the a-coefficient is from the shape of the recoil 84 ⁸⁵ ion energy spectrum. If the beta electron and antineutrino momenta are anticorrelated, the ⁸⁶ average recoil momentum is reduced, which shifts weight to the low-energy part of the spec-⁸⁷ trum. Until recently all measurements of the neutron *a*-coefficient used some variation of this $_{88}$ method and achieved results that were systematically limited at the 5 % level [20–22]. The ⁸⁹ method used by aCORN, first proposed by Yerozolimsky and Mostovoy [23, 24], relies on ⁹⁰ a novel time-of-flight (TOF) asymmetry that does not require precise proton spectroscopy. ⁹¹ The aCORN method is illustrated in figure 2. Assume a pointlike cold neutron source on the ⁹² axis between a set of opposing electron and proton detectors with a uniform axial magnetic ⁹³ field applied throughout. Electron and proton collimators, shown schematically as cylindri-⁹⁴ cal tubes, lie on the axis. When a cold neutron, which is effectively at rest, decays, a beta ⁹⁵ electron, antineutrino, and proton are emitted. Due to their helical motion in the magnetic ⁹⁶ field B, the collimators impose a maximum transverse momentum of $p_{\perp}(\max) = eBr/2$, $_{97}$ where r is the collimator radius, for detected electrons and protons. An electrostatic mir- $_{98}$ ror containing a uniform axial electric field, produced by a pair of grids at ground and +3⁹⁹ kV as shown, causes all neutron decay protons to be accelerated and directed toward the

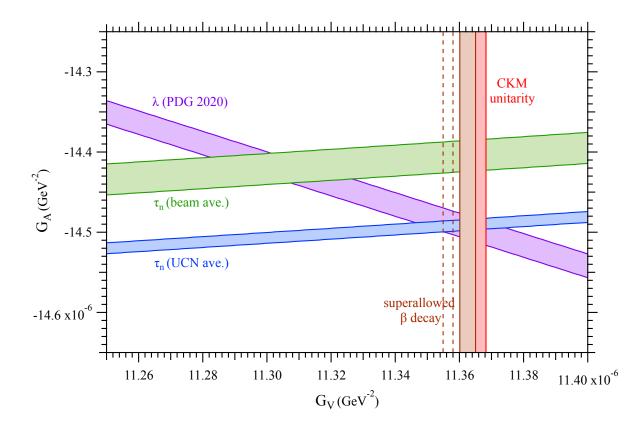


FIG. 1. A summary of experimental constraints on the nucleon weak coupling constants G_A and G_V . The purple band is the PDG 2020 [6] recommended value for λ from neutron decay parameters A and a, including a scale factor of $\sqrt{\chi_{\nu}^2} = 2.6$ to account for poor agreement among experiments. The green (no scale factor) and blue (scale factor $\sqrt{\chi_{\nu}^2} = 1.5$) bands are derived from the neutron lifetime averages for the beam and UCN storage experiments. The brown vertical band shows G_V from superallowed beta decay [14] and the dashed lines indicate the shift due to the calculation of Δ_R by Seng, *et al.* [15]. The red vertical band shows the CKM matrix unitarity condition using the PDG recommended value of V_{us} [6].

¹⁰⁰ proton detector. Electrons in the energy range of interest must be emitted into the right ¹⁰¹ hemisphere to be detected. The momentum acceptances for the electron and proton in this ¹⁰² scheme are shown in figure 2 (middle). These are cylinders in momentum space and the ¹⁰³ proton acceptance extends to both sides of the origin. Now consider the antineutrino mo-¹⁰⁴ mentum acceptance for coincidence-detection events where the electron momentum is $\vec{p_e}$ as ¹⁰⁵ shown. Conservation of momentum requires $\vec{p_{\nu}} = -(\vec{p_e} + \vec{p_p})$ so the antineutrino momentum ¹⁰⁶ acceptance is a cylinder equivalent to the proton acceptance cylinder but displaced from 107 the origin by $-\vec{p_e}$. If we neglect the kinetic energy of the proton (751 eV maximum) the ¹⁰⁸ electron and antineutrino must share the total decay energy Q = 1293 keV and conservation 109 of energy requires $|\vec{p_{\nu}}| = Q - \sqrt{p_e^2 + m_e^2}$. So for the given $\vec{p_e}$ the antineutrino momentum ¹¹⁰ must lie on the intersection of the cylinder and sphere shown in figure 2 (bottom), which ¹¹¹ is indicated by the gray regions marked I and II. Region I (II) antineutrinos are correlated (anticorrelated) with $\vec{p_e}$ and have equal solid angles from the origin. If the *a*-coefficient is ¹¹³ zero, the number of coincidence events associated with regions I and II will be equal. If not there will be an asymmetry. The same is true when we sum over all values of $\vec{p_e}$ for 114 detectable electrons. In reality the neutron source is not a point but a cylindrical beam 115 passing through the electrostatic mirror perpendicular to \vec{E} and \vec{B} , so most decay vertices 116 ¹¹⁷ are off axis. For off-axis decays the proton and electron momentum acceptances are elliptical ¹¹⁸ cylinders and the geometric construction is somewhat more complicated, but the result is essentially the same and solid angles of regions I and II remain equal. 129

In the experiment we measure the beta electron energy and proton TOF, the time between 121 electron and proton detection, for neutron decay events where both were detected. The 122 ¹²³ data form the characteristic wishbone shape shown in figure 3. Region I antineutrinos are correlated with the electron momentum direction, so the associated protons have larger 124 ¹²⁵ momentum and axial velocity and the events lie on the lower wishbone branch (group I). ¹²⁶ Region II antineutrinos are anticorrelated with electron momentum, so the protons have ¹²⁷ smaller momentum and axial velocity and the events lie on the upper wishbone branch (group ¹²⁸ II). The gap between the wishbone branches corresponds to the kinematically forbidden gap between regions I and II in figure 2 (bottom). At beta energy above about 400 keV 129 the regions overlap and the wishbone branches merge. A vertical slice at beta energy E, 130 ¹³¹ depicted in figure 3, contains N^{I} events in the lower branch and N^{II} events in the upper ¹³² branch. Using equation 1 we have

$$N^{I(II)}(E) = F(E) \int \int \left(1 + av \cos \theta_{e\nu}\right) d\Omega_e \, d\Omega_\nu^{I(II)} \tag{5}$$

¹³³ where F(E) is the beta energy spectrum, v is the beta velocity (in units of c), $\theta_{e\nu}$ is the ¹³⁴ angle between the electron and antineutrino momenta, and $d\Omega_e$, $d\Omega_{\nu}^{I(II)}$ are elements of solid ¹³⁵ angle of the electron and antineutrino (group I, II) momenta. The integrals are taken over ¹³⁶ the momentum acceptances shown in figure 2. Since by construction the total solid angle ¹³⁷ products are equal for the two groups: $\Omega_e \Omega_{\nu}^I = \Omega_e \Omega_{\nu}^{II}$, we find that the *a*-coefficient is

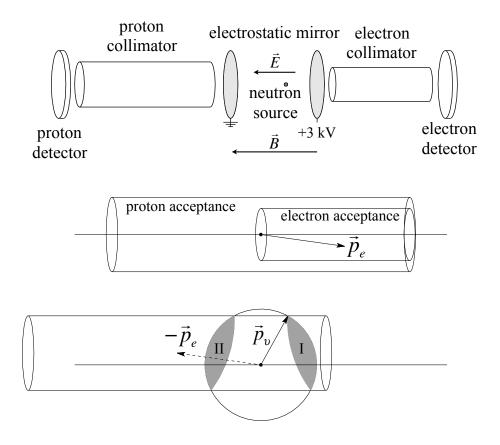


FIG. 2. An illustration of the aCORN experimental method. Top: A neutron source, shown as a point source here, lies on axis between a set of proton and electron detectors. A uniform axial magnetic field \vec{B} is present throughout. Electron and proton collimators act to limit the transverse momenta of detected electrons and protons from neutron decay. An electrostatic mirror produces an approximately uniform electric field \vec{E} in the decay region that accelerates and directs all protons toward the proton detector, but beta electrons in the energy range of interest must be emitted into the right hemisphere to be detected. Middle: A momentum space plot showing the cylindrical momentum acceptances of electrons and protons. Bottom: A momentum space construction of the acceptance for antineutrinos from neutron decay, when the detected electron momentum was $\vec{p_e}$ as shown and the proton was also detected. Conservation of energy and momentum restricts the antineutrino momentum to the shaded regions I and II which have equal solid angle from the source. Region I is correlated with $\vec{p_e}$ and region II is anticorrelated, so the asymmetry in events associated with each region measures the *a*-coefficient.

¹³⁸ related to the wishbone asymmetry X(E) by

$$X(E) = \frac{N^{I}(E) - N^{II}(E)}{N^{I}(E) + N^{II}(E)} = \frac{\frac{1}{2}av\left(\phi^{I}(E) - \phi^{II}(E)\right)}{1 + \frac{1}{2}av\left(\phi^{I}(E) + \phi^{II}(E)\right)}$$
(6)

¹³⁹ The functions $\phi^{I}(E)$ and $\phi^{II}(E)$ are defined as

$$\phi^{I}(E) = \frac{\int d\Omega_{e} \int_{I} d\Omega_{\nu} \cos \theta_{e\nu}}{\Omega_{e} \Omega_{\nu}^{I}} \quad \text{and} \quad \phi^{II}(E) = \frac{\int d\Omega_{e} \int_{II} d\Omega_{\nu} \cos \theta_{e\nu}}{\Omega_{e} \Omega_{\nu}^{II}}, \tag{7}$$

¹⁴⁰ where again the integrals are taken over the momentum acceptances. Equations 7 can ¹⁴¹ be understood as the average value of $\cos \theta_{e\nu}$ for detection regions I and II. These are ¹⁴² geometrical functions that depend only on the transverse momentum acceptances of the ¹⁴³ proton and electron so they can be calculated precisely from the known axial magnetic field ¹⁴⁴ and collimator geometries.

The second term in the denominator of equation 6 has a numerical value less than 0.005 in the energy range of interest (100 keV-380 keV), so we can treat it as a small correction in and write

$$X(E) = af_a(E) [1 + \delta_1(E)] + \delta_2(E)$$
(8)

148 with

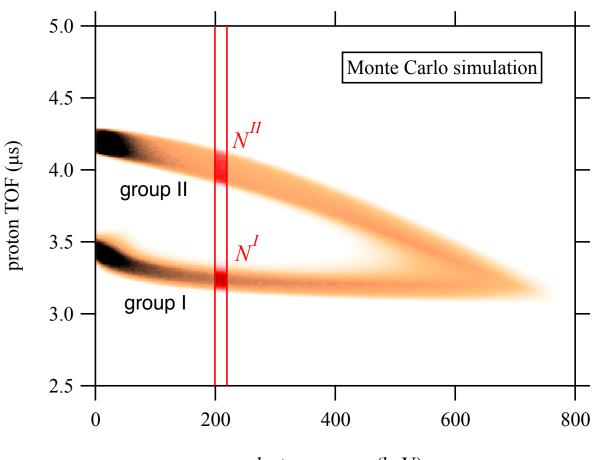
$$f_a(E) = \frac{1}{2}v\left(\phi^I(E) - \phi^{II}(E)\right) \tag{9}$$

149 and

$$\delta_1(E) = -\frac{1}{2}av\left(\phi^I(E) + \phi^{II}(E)\right).$$
(10)

¹⁵⁰ The other small correction $\delta_2(E)$ in equation 8 comes from our neglect of the proton's ¹⁵¹ kinetic energy in the momentum space discussion of figure 2. If we account for this energy, ¹⁵² the antineutrino momentum sphere is slightly oblong and the solid angles of groups I and II ¹⁵³ differ by approximately 0.1 %. This causes a small (about 1 % relative) intrinsic wishbone ¹⁵⁴ asymmetry that is independent of the *a*-coefficient; it is straightforward to compute by ¹⁵⁵ Monte Carlo to the needed precision.

Omitting the small corrections we see that $X(E) = af_a(E)$; the experimental wishbone asymmetry is proportional to the *a*-coefficient and the dimensionless geometric function $f_a(E)$. In analyzing the data we take the approach of assuming a perfectly uniform axial magnetic field and exact collimator configuration, and use the precisely computed $f_a(E)$ shown in figure 4. We then treat nonuniformities and uncertainties in the measured magnetic



electron energy (keV)

FIG. 3. A Monte Carlo simulation of aCORN data, proton TOF vs. beta energy for coincidence events. The fast proton branch (group I) is associated with neutron decays where the antineutrino momentum was in region I in figure 2. The slow proton branch (group II) is associated with decays where the antineutrino momentum was in region II. The sums N^{I} and N^{II} are used to compute the wishbone asymmetry for each beta energy slice.

¹⁶² field magnitude and shape and the collimator geometry as systematic effects applied to the¹⁶³ result.

aCORN runs on a nominally unpolarized neutron beam. If the beam were slightly polife larized, there would be an additional contribution to the wishbone asymmetry from the antineutrino asymmetry correlation B term in equation 1, giving

$$X(E) = af_a(E) + PBf_B(E) \tag{11}$$

168 where P and B are the neutron polarization and B-coefficient, and $f_B(E)$ is a similarly

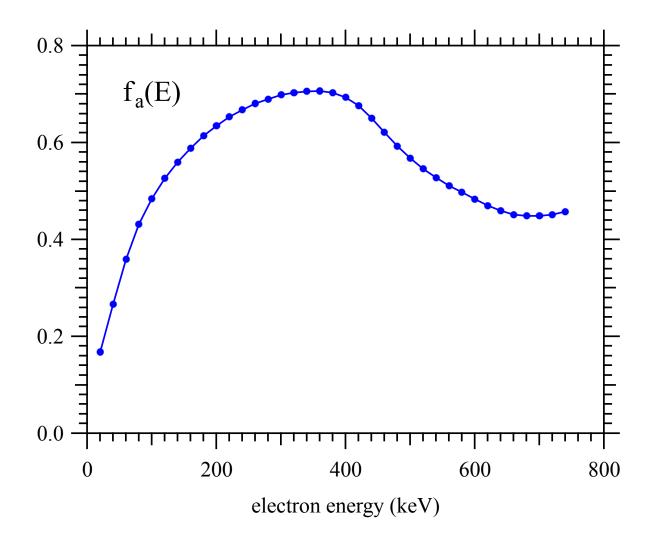


FIG. 4. The dimensionless geometric function $f_a(E)$, computed numerically from the aCORN geometry and a 36.4 mT uniform magnetic field (see equations 8, 9).

¹⁶⁹ calculated geometric function for *PB*. Because neutron polarization is more axially peaked ¹⁷⁰ than $\mathbf{p_e}$, $f_B(E)$ is on average 40 % larger than $f_a(E)$. Also $|B/a| \approx 10$. So even with ¹⁷¹ $P \ll 1$ this can be a significant effect. In the NG-6 aCORN data an observed difference in ¹⁷² X(E) with the magnetic field in the up and down directions was attributed to a neutron ¹⁷³ polarization $P \approx 0.6 \%$ [25].

174 III. THE aCORN APPARATUS

¹⁷⁵ We describe here briefly the main components of the aCORN apparatus. More details ¹⁷⁶ can be found in previous publications [26–28]. Figure 5 shows a cross section view of the 177 aCORN tower.

178 The 36.3 mT axial main magnetic field is produced by a vertical array of 24 individual $_{179}$ flat coils supplied in series. Each coil contains 121 turns of 2 cm \times 0.1 cm copper tape, has an overall diameter of 78.8 cm, and rests on a water-cooled copper plate. Coil assemblies 180 are separated by 8 cm vertical gaps, set by the size of the neutron beam. The full magnet 181 assembly is surrounded by an iron flux return yoke composed of top and bottom circular 182 endplates and four vertical columns. A set of 76 computer controlled trim coils are used to 183 improve the shape of the magnetic field. Each main coil has an attached axial trim coil. 184 Two pairs of large transverse coils cancel the overall environmental transverse field. Twenty-185 four pairs of small transverse trim coils are used to eliminate localized transverse fields and 186 gradients. A robotic magnetic field mapper, attached to precision bearings on the upper and 187 lower iron endplates, is used to map the magnetic field inside the vacuum chamber, both on 188 and off axis. Using the results of these maps, an algorithm computes the trim coil currents 189 needed to meet the magnetic field specifications. The proton and electron collimators, and 190 the electrostatic mirror, are then optically aligned to the axis of the experiment defined by 191 193 the bearings.

The electron collimator is a series of seventeen 0.5-mm thick tungsten discs, each with a 5.5 cm diameter circular aperture. These are unevenly spaced to minimize the probability that an electron will scatter from an edge and reach the active area of the beta spectrometer, as determined by a PENELOPE simulation. The total length of the electron collimator is 48.0 cm. The proton collimator is a monolithic aluminum tube, 140.0 cm long, containing a series of 49 evenly spaced 8.0 cm diameter knife edge apertures cut by a precision lathe on the inner surface. The electron and proton collimators are individually aligned and attached to a rigid aluminum insert structure which is then aligned as a single unit to the experimental axis.

²⁰³ The electrostatic mirror must provide a nearly uniform axial electric field in the cylindrical ²⁰⁴ neutron decay region. This requires differing uniform potentials at the ends and a linearly ²⁰⁵ varying potential on the wall. The neutron beam must also penetrate the mirror wall, which ²⁰⁶ presented a technical challenge. Our solution was to make the wall from a thin (0.25 mm) ²⁰⁷ polytetrafluoroethylene (PTFE) sheet. The inner surface of the sheer was electroplated with ²⁰⁸ a 4.5 μ m layer of copper divided into 63 parallel thin bands by photolithography, produced by

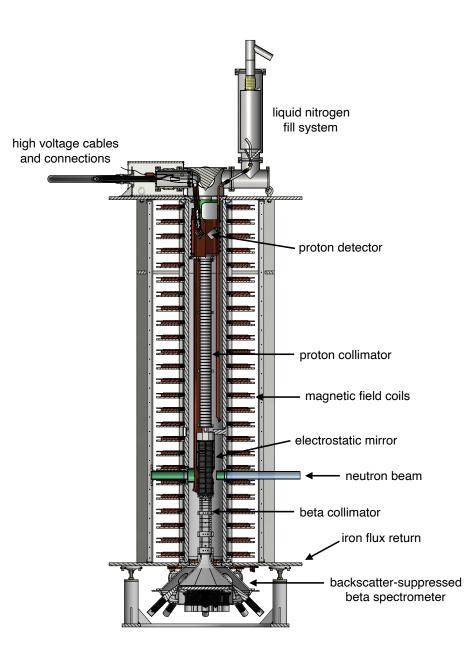


FIG. 5. A cross section view of the aCORN tower showing the arrangement of major components. The neutron beam passes through from right to left.

²⁰⁹ Polyflon¹². These 63 bands were held at potentials established by a chain of equal precision ²¹⁰ resistors to approximate the linear boundary condition. The neutron beam was allowed to

 $_{211}$ pass through the wall on both sides, each side scattering about 1 % of the beam by the

¹ Polyflon Co., Norwalk, CT, USA.

² Certain trade names and company products are mentioned in the text or identified in illustrations in order to adequately specify the experimental procedure and equipment used. In no case does such identification imply recommendation or endorsement by the National Institute of Standards and Technology, nor does it imply that the products are necessarily the best available for the purpose.

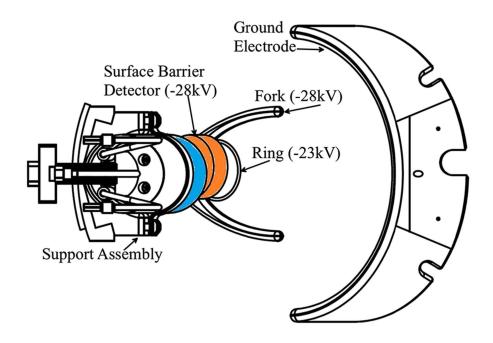


FIG. 6. An overhead view of the proton detector assembly showing the positions of the surface barrier detector and focusing electrodes.

²¹² PTFE and scattering/absorbing about 0.1 % of the beam by the copper. The end potentials ²¹³ were set by grids of 100 μ m wires. The grid on the bottom (electron) side was at +3 kV ²¹⁴ and the grid on the top (proton) side was at ground.

²¹⁵ The proton detector was a 600 mm², 1000 μ m thick surface barrier detector held at -28 ²¹⁶ kV to accelerate protons to a detectable energy. Figure 6 shows an overhead view, looking ²¹⁷ down from the top of the tower. Detector components were located off-axis to prevent ²¹⁸ neutron decay electrons emitted in the upward direction from backscattering on the proton ²¹⁹ detector and returning to the beta spectrometer, where they would be detected with the ²²⁰ wrong energy and wrong sign of $\cos \theta_{e\nu}$. A focusing fork and ring act as a lens to focus ²²¹ all protons exiting the proton collimator onto the active area of the detector. The proton ²²² detector is cooled by a copper panel attached to a liquid nitrogen cooling system.

aCORN employed a novel backscatter-suppressed beta spectrometer, illustrated in cross-225 section in figure 7. The beta energy detector was a 5 mm thick, 280 mm diameter circular 226 slab of Bicron BC-408 plastic scintillator, viewed by 19 Photonis XP3372 8 stage 7.6 cm (3 227 inch) hexagonal photomultiplier tubes (PMT's). Surrounding the energy detector was an 228 array of eight veto detectors, each composed of a 10 mm thick BC-408 plastic scintillator ²²⁹ and adiabatic acrylic light guide viewed by a Burle 8850 12 stage 5.1 cm (2 inch) PMT. The ²³⁰ spectrometer was mounted on the tower below the bottom flux return end plate. The axial ²³¹ magnetic field was high at the entrance to the spectrometer but dropped quickly below it $_{232}$ to about 1 mT at the energy detector. All beta electrons with kinetic energy >100 keV ²³³ that were accepted by the beta collimator passed through the opening at the top of the veto array and struck the active area of the energy detector, as verified by Monte Carlo simula-234 tion. Approximately 5 % were expected to backscatter from the plastic scintillator without 235 depositing their full energy. This may lead to a large systematic effect, discussed in section 236 VIE3. To mitigate this a backscatter veto array was used; the majority of backscattered 237 electrons struck a veto paddle and were vetoed. The overall veto efficiency for backscattered 238 electrons was measured to be (92 ± 5) %. A pair of linear motion vacuum feedthroughs lo-239 cated between the electrostatic mirror and proton collimator held conversion electron sources 240 (¹¹³Sn and ²⁰⁷Bi). During production runs, *in situ* calibration measurements were made at 241 ²⁴² approximately 48 hour intervals to monitor slow gain drifts in the beta spectrometer and enable correction in the data analysis. Details of the design, construction, and characterization 243 of the aCORN beta spectrometer can be found in reference [28]. 245

The main vacuum chamber of aCORN was a vertical aluminum tube 3 m tall and 28 ²⁴⁷ cm inner diameter. It was joined at the top and bottom to the iron endplates by o-ring ²⁴⁸ seals. A 250 l/s turbomolecular pump was mounted on the beta spectrometer chamber and ²⁴⁹ a 370 l/s helium cryopump was attached to the beam dump. A set of three liquid nitrogen ²⁵⁰ cooled copper cryopanels extended from the top of the main chamber to the bottom of the ²⁵¹ proton collimator to provide high conductance pumping of water and volatiles released by ²⁵² the plastic scintillator in the beta spectrometer. During normal operation the pressure at ²⁵³ the top of the electrostatic mirror was about 8×10^{-5} Pa (6×10^{-7} torr).

254 IV. MODIFICATIONS FOR THE NG-C RUN

A previous publication [27] describes the aCORN apparatus as it was used for the first measurement on the NG-6 beamline at the NIST Center for Neutron Research (NCNR) [29] in 2013–2014. The experiment was moved, with some modifications, to the new high-flux beamline NG-C in 2015 for a second run. This section describes those modifications.

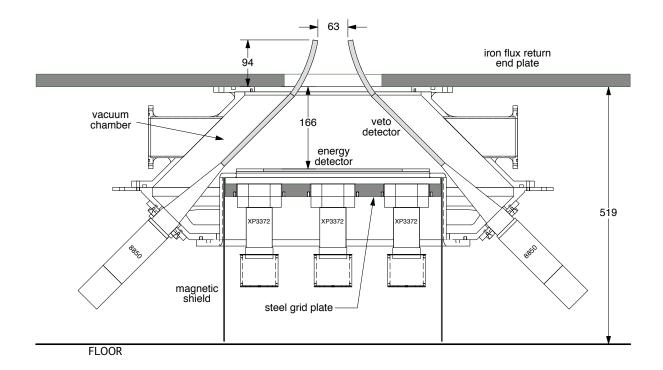


FIG. 7. An interior cross section view of the backscatter-suppressed beta spectrometer. Dimensions are in mm.

259 A. Neutron beam and collimation

In 2013 a second guide hall was commissioned at the NCNR with four new supermirror 260 ²⁶¹ guides. The end position on new guide NG-C was designated for fundamental neutron physics experiments and aCORN was the first experiment to run there. NG-C is a ballistic 262 curved supermirror guide 11 cm \times 11 cm at the exit with a measured capture flux of 8.1×10^9 263 $cm^{-2}s^{-1}$. Details of the design of the NG-C guide and other guides in the new guide hall 264 can be found in [30]. Because NG-C is curved, a bismuth filter is not needed to remove fast 265 neutrons and gammas, which improves neutron transmission to the experiment. A 180-cm 266 long secondary focusing supermirror guide was installed to reduce the beam cross section to 267 a 6 cm \times 6 cm square. This was followed by a neutron collimator, 120 cm long containing 268 four ⁶LiF apertures. Its interior was lined with ⁶Li glass to absorb scattered neutrons. The 269 collimator reduced the beam divergence and delivered a 3.1-cm diameter circular beam to 270 ²⁷¹ the experiment. The capture flux in the neutron decay region of aCORN was measured to $_{272}$ be 6.7×10^9 cm⁻²s⁻¹, about a factor of ten higher than the equivalent measurement with ²⁷³ the experiment installed on NG-6, but with a beam area that was a factor of two smaller, ²⁷⁴ resulting in an overall factor of five increase in the wishbone event rate from neutron decay. ²⁷⁵ At the end of NG-C is a 2.4-m deep pit available to experiments that need part of the ²⁷⁶ apparatus below floor level. For aCORN we constructed a false floor inside the pit at 40 cm ²⁷⁷ below the main floor level for better access to the beta spectrometer and the field mapping ²⁷⁸ apparatus when installed.

279 B. Electrostatic mirror

The departure from a perfectly axial electric field in the vicinity of the upper grounded end 280 grid, where the protons pass through, resulted in the largest systematic correction (5.2 %)281 $_{282}$ and uncertainty (1.1 %) in the result from the NG-6 run [25]. Guided by a 3D COMSOL ³ ²⁸³ model along with a Monte Carlo proton transport simulation, we made some improvements to the upper grid geometry to reduce this effect. We replaced the linear wire upper grid 284 with an electroformed square mesh copper grid containing 100 μ m threads spaced by 2 ²⁸⁶ mm, purchased from Precision Eforming⁴. We also redesigned the upper aluminum support ²⁸⁷ ring to locate it entirely outside the thick PTFE tube, thereby increasing the open inner diameter at the top to 10.9 cm. The new upper grid can be seen in the photo in figure 8. 288 These adjustments reduced the size of the electrostatic mirror correction by more than a 289 $_{290}$ factor of three (see the discussion in section VIE1). The lower +3 kV grid was unchanged; ²⁹¹ protons do not pass close to the lower grid and the electrostatic effect on electrons passing ²⁹³ through it is negligible.

294 C. Data Acquisition

Electronic pulses from the 19 beta energy channels, 8 backscatter veto channels, and the proton detector were sent to two PIXIE-16 modules⁵ which are 12 bit, 100 MSPS multiplexing analog to digital converters. For the NG-C run we made two changes to the PIXIE-16 firmware: i) certain calculations that were not needed, such as constant fraction discrimination ratios, were removed in order to increase throughput; and ii) the energy calculation for all channels was switched from a trapezoidal filter to the charge to digital conversion (QDC)

³ COMSOL, Inc., Burlington, MA, USA.

⁴ Precision Eforming, LLC, Cortland, NY, USA.

⁵ XIA LLC, Newark, CA.

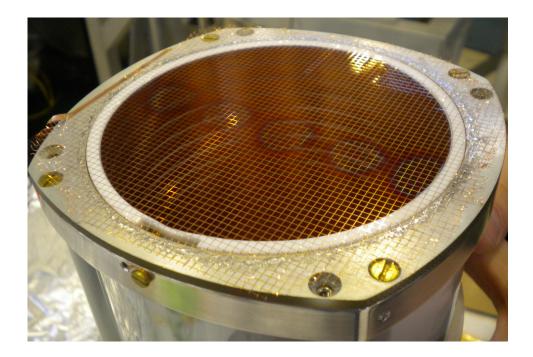


FIG. 8. The redesigned upper end of the electrostatic mirror used in the NG-C run, showing the new square mesh grid and larger open diameter.

mode. In the QDC mode three timings are specified: 1) time before the event trigger to 301 begin saving data (0.6 μ s for electrons, 1 μ s for protons), 2) the pre-pulse time window (0.5 302 μ s for electrons, 0.5 μ s for protons), and 3) the pulse time window (0.3 μ s for electrons, 2 μ s 303 for protons). The energy is then calculated as the average number of counts per channel in 304 the pulse window minus the average number of counts per channel in the pre-pulse window. 305 We found that this switch did not noticeably affect energy resolution or linearity, but it 306 significantly lowered the effective energy threshold which was useful for all channels but was 307 particularly helpful for the proton channel. In the NG-6 data analysis [25] there was a 3 % 308 ³⁰⁹ systematic correction to the *a*-coefficient due to loss of protons below threshold. Such a 310 correction was not needed in the NG-C data analysis.

311 V. THE NG-C RUN

aCORN ran on the NG-C end position at the NCNR from August 2015 to September 2016 and collected a total of 3758 beam hours of neutron decay data. The raw coincidence event are was 171 s^{-1} , The neutron decay wishbone event rate, after background subtraction, was 0.9 s^{-1} , about a factor of three higher than in the previous run on NG-6.

We collected data in both axial magnetic field directions in order to monitor and correct 316 ³¹⁷ for a possible effect due to residual polarization of the neutron beam. The first data run was magnetic field up (B_{up}) , for 1097 beam hours. The second run was magnetic field down 318 (B_{down}) , for 2178 hours. The magnetic field was returned to B_{up} for the final 482 hours. The 319 ³²⁰ following protocol was followed whenever the magnetic field was reversed: 1) the detectors ³²¹ and collimation insert were removed and the field mapper installed; 2) the existing axial and transverse magnetic fields were mapped and compared to the previous maps; 3) the 322 leads to the main magnet supply were reversed and all trim coils were de-energized; 4) the 323 magnetic field was mapped and trimmed to specification in the new direction; 5) the field 324 mapper was removed and the detectors and collimation insert reinstalled and aligned. The 325 entire process of reversing the magnetic field took about two weeks, completed mostly during 326 ³²⁷ NCNR refueling shutdown periods. Figure 9 shows results of on-axis axial and transverse ₃₂₈ field maps made in June 2015, prior to the first production run, and December 2015, just before the first field reversal and with the trim settings unchanged. Drifts in the field shape 329 over the six month span are evident in the plots. We attribute the increase in axial field 330 near the top and bottom of the tower to relaxation of the flux return endplates. Our target 331 uncertainty for the axial field is ± 0.2 mT so this axial drift is not a problem. aCORN is very 332 sensitive to transverse magnetic fields in the proton transport region, *i.e.* the electrostatic 333 mirror and proton collimator, as they can cause a false wishbone asymmetry. As can be 334 seen in figure 9 (bottom) the newly trimmed field in June met our target of $< 4 \ \mu$ T, but in 335 ³³⁶ December the transverse field in a region near the bottom of the proton collimator exceeded ³³⁸ the target. However the associated systematic effect was small (see section VIE2).

Figure 10 shows a transverse field map taken 5.1 cm off-axis. At each z position the field was measured in steps of 30° as the mapper carriage rotated. The data were fit to a Fourier series function: $B_{\text{trans}}(\theta) = b_0 + b_1 \cos(\theta - \theta_1) + b_2 \cos 2(\theta - \theta_2)$. The constant term dominated by the small misalignment angle between the Hall probe and the field axis and is not interesting. The $\cos \theta$ coefficient b_1 gives the uniform transverse field off axis. The $\cos 2\theta$ coefficient b_2 results from a transverse gradient. The parameters θ_1 and θ_2 are constant phase offsets.

Figure 11 shows results of alignment checks of the collimation insert made at various times during the run. Measurements were made using an optical system consisting of a theodolite, appentaprism that rotates the line of sight by 90°, and a series of precision reticules installed

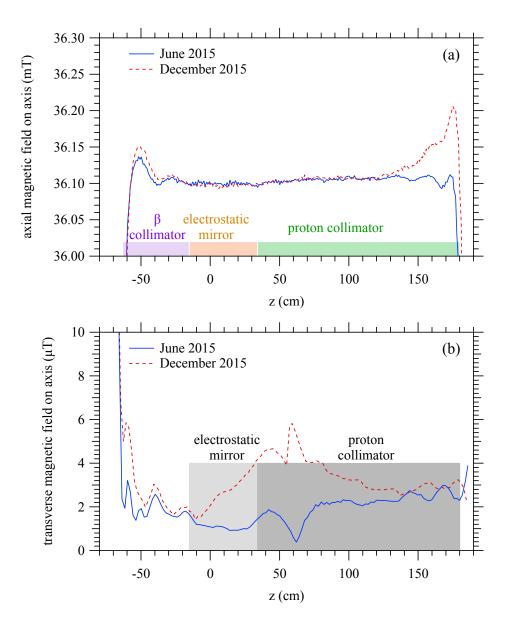


FIG. 9. The axial (a) and transverse (b) magnetic fields measured by the robotic field mapper on axis. The June 2015 maps were made after reversing and trimming the field. The December 2015 maps were made just prior to the next field reversal. The difference shows typical drift over six months with unchanged trim coil settings. Gray shaded regions in the bottom plot indicate the $< 4 \mu$ T target for the transverse field in the electrostatic mirror and proton collimator.

³⁵⁰ in the insert, all in a very well measured geometry. Usually independent measurements were ³⁵¹ made by two people as a double-check. The electrostatic mirror alignment was consistently ³⁵² within our target of 1 mrad. The proton collimator had a much stricter target of 0.1 mrad ³⁵³ which was generally met or slightly exceeded.

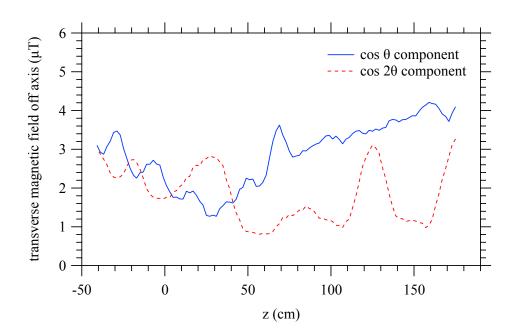


FIG. 10. The transverse field map measured 5.1 cm off axis using the robotic field mapper. At each z position the field is measured at 30° intervals as the mapper rotates. The result is Fourier decomposed into a $\cos \theta$ component that gives the uniform transverse field and a $\cos 2\theta$ that corresponds to a transverse gradient.

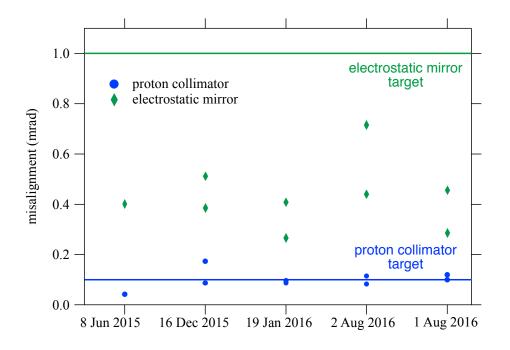


FIG. 11. A summary of optical insert alignment checks made over the course of the run. Multiple points are independent measurements made by two people.

355 VI. DATA REDUCTION AND ANALYSIS

For each aCORN event the PIXIE system recorded the energy and time of 31 signals: 356 19 beta energy PMTs, 8 beta veto PMTs, 2 copies of the proton preamp output, and 2 357 copies of a level-discriminated proton pulse. An event was defined in firmware as any two of 358 the above signals above threshold within a 100 ns time window. Two copies of the proton 359 detector signal were used so that a single proton would produce an event. Most noise and 360 dark current from individual PMTs did not produce events. These raw data were written to 361 disk along with header information containing run parameters at a rate of about 5 TB per day. An online data distiller preprocessed raw data and removed much of the background. 363 The distiller included all events that were within a time window 10 μ s before to 1 μ s after 364 each proton event. Events outside this window could not be a neutron decay coincidence 365 ₃₆₆ and were discarded. Data bottlenecks within the PIXIE could cause events to enter the 367 data stream out of time order, but each event contained an accurate time stamp used by ³⁶⁸ the distiller to correct the time order. The distiller produced distilled data files at a rate of ³⁶⁹ about 8 GB per day (a factor of >600 reduction) that became the archival data. Raw data were not saved, except for a small sample kept each day for diagnostic purposes. 370

A data reducer was then used to convert the distilled data into reduced data files, indi-372 vidual text files each containing 160 s of coincidence event data, for analysis. The reducer 373 combined individual beta PMT events into complete beta energy and time, or discarded 374 them as noise, assigned a veto state to each, and calculated the beta-proton time of flight 375 (TOF) for each proton event within the 11 μ s time window. The reduced data were or-376 ganized into series of up to 1000 files, about two days of data, collected under essentially 377 the same experimental conditions. Each series had an associated beta energy calibration 378 obtained from *in situ* calibration source measurements completed every two days.

Data were divided into groups, each containing several equivalent series totaling approximately 100 beam hours, for analysis. Data were then sorted into a raw wishbone plot, a plot of proton TOF *vs.* beta energy, applying the calibration data for each series separately, with are proton energy cut applied as shown in figure 12. A typical raw wishbone plot is shown in figure 13. Neutron decays are contained in the "wishbone" structure of delayed coincidence events.

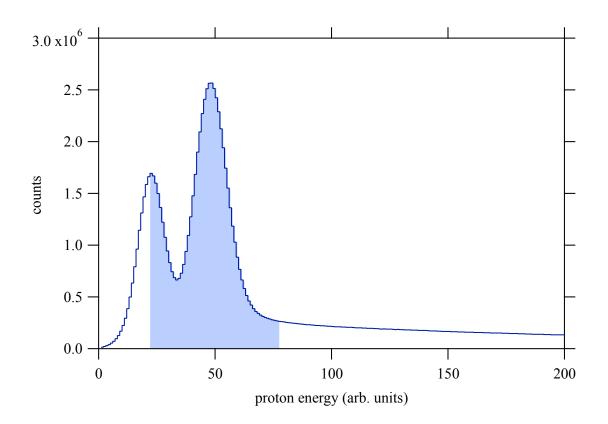


FIG. 12. A typical proton energy singles spectrum. The peak on the right is protons. The noise/background forms a peak on the left due to the soft energy threshold of the PIXIE. The shaded region is the applied proton energy window.

387 A. Data Blinding Strategy

The nature of aCORN does not allow an easy way to add an arbitrary blinding constant to the wishbone data. But the possibility of residual neutron polarization offers a useful data blinding strategy. An unknown neutron polarization would add an offset to the wishbone asymmetry, as shown in equation 11, that is undetectable in the analysis of data from a single magnetic field direction. In the NG-6 run a presumed neutron polarization of only 0.6 % produced an 8.4 % shift in the value of the *a*-coefficient for each field direction [25]. Our blinding strategy was as follows:

A small subset of the aCORN collaboration, the polarimetry group, measured the
 aCORN neutron beam polarization *in situ* using polarized ³He NMR in an auxiliary
 experiment and analyzed the result, which was not revealed to other collaboration
 members.

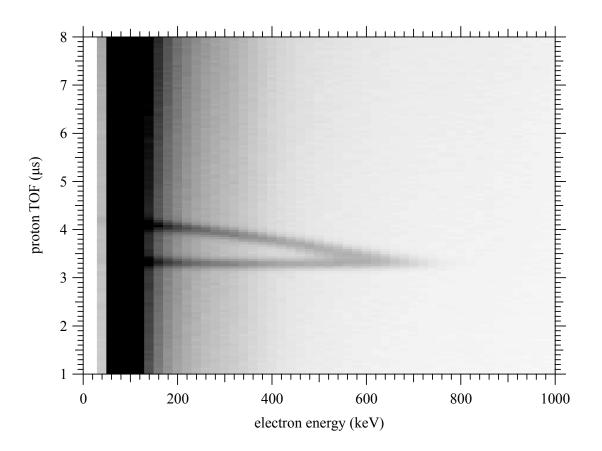


FIG. 13. A typical raw wishbone obtained from approximately 100 hours of reduced data, using the proton energy cut shown in figure 12.

- 2. The magnetic field up (B_{up}) data only were fully analyzed, including all systematic
 corrections and uncertainties, and a result for the *a*-coefficient was obtained and locked.
 The polarimetry group did not participate in this analysis.
- 3. The magnetic field down (B_{down}) data were analyzed using the same procedures and
 corrections, without adjustment.

404
 4. The polarimetry "box" was opened and the result compared to the *a*-coefficients from
 405 the B_{up} and B_{down} analyses.

406 B. Background Subtraction and Dead Time Correction

⁴⁰⁷ The PIXIE system is complicated and exhibits dead time effects at several time scales. ⁴⁰⁸ First there is a dead time for each channel that depends on the time structure of its signal ⁴⁰⁹ pulses. This was 300 ns for beta PMT channels and 3000 ns for proton detector channels. ⁴¹⁰ Because the analog to digital conversion is multiplexed, an additional deadtime of several ⁴¹¹ μ s can occur for a group of channels on a single module when data rates are high. Finally, ⁴¹² when the module memory is full, the entire module of 16 channels is dead for about 3 μ s ⁴¹³ while data is transferred to the host computer. During the NG-6 run the background data ⁴¹⁴ rate (proton detector $\approx 350 \text{ s}^{-1}$, beta detector $\approx 1.1 \times 10^4 \text{ s}^{-1}$) was sufficiently low that ⁴¹⁵ the longer dead times were not apparent in the data, but during the NG-C run (proton ⁴¹⁶ detector $\approx 500 \text{ s}^{-1}$, beta detector $\approx 6.6 \times 10^4 \text{ s}^{-1}$), such affects did appear due to the much ⁴¹⁷ higher data rate. We found that a 4 μ s dead time for all events, applied in the analysis, was ⁴¹⁸ sufficient to remove all nonphysical time correlation effects between channels in the data.

In the NG-6 data analysis described in [25, 27] we were able to treat each electron event within the coincidence time window of a proton (10 μ s before the proton to 1 μ s after) as a separate coincidence event. The same proton could be associated with several different coincidence events, but at most one would be a neutron decay because the neutron decay arate was quite low. Any others were background coincidences where the electron and proton events were uncorrelated in time. As a result, the background in the raw wishbone was completely flat and structureless, lacking the usual exponential shape of a random time spectrum, and background subtraction was relatively simple. Due to the longer time scale are dead time effects observed in the NG-C data, we were unable to use the same method. Instead we kept only the earliest electron in the 11 μ s wide coincidence time window of each proton and discarded any others. This change produced three important effects:

A random background coincidence could preempt a neutron decay event if the background electron event occurred earlier in time. This removed an estimated 20 % of
usable neutron decays from the data with a resulting loss of statistics.

2. Neutron decay protons appear in a coincidence region of $(3-4.5) \mu$ s after the beta electron as can be seen in figure 13. If an event appeared in this region, there could not have been an earlier electron event during the previous 5 μ s, otherwise the coincidence region event would have been preempted. Note that earlier electrons correspond to longer proton TOF in the wishbone plot. This enforced the >4 μ s dead time requirement described above.

⁴³⁹ 3. The random background coincidences now have the usual exponential time structure.

A more intricate method is needed to subtract background and correct for dead time.

We begin with the assumption that the raw wishbone plot contains only neutron decay coincidence events and random background coincidences. This is reasonable because we do at not expect physical correlations in background events in the time range $(1-10) \mu$ s. The vast majority of background comes from gamma rays produced by neutron capture in the electrostatic mirror, collimator, and other nearby materials. The remainder is radioactive decay, at guide hall background, and cosmic rays. Weak decays from neutron capture may produce the correlations, but at much longer times. The others produce only prompt coincidences well within 1 μ s.

Consider a vertical slice of the raw wishbone at a particular beta energy. Let the neutron 450 decay wishbone function be bounded by proton TOF values t_0 and t_1 . For $t < t_0$ the 451 background has an exponential shape

$$B(t < t_0) = c_0 e^{Rt} (12)$$

 $_{452}$ and for $t > t_1$ a similar exponential shape

$$B(t > t_1) = c_1 e^{Rt}.$$
(13)

⁴⁵³ Note that these are positive exponentials because larger t (larger proton TOF) corresponds ⁴⁵⁴ to earlier electron event time. The rate parameter R is the same in both regions; it is the ⁴⁵⁵ random background electron event rate at the energy of this wishbone slice. The constants ⁴⁵⁶ c_0 and c_1 are different; their ratio $c_0/c_1 < 1$ is the probability that no neutron decay electron ⁴⁵⁷ was detected, with proton TOF in the neutron decay window $t_0 < t < t_1$, for a given proton ⁴⁵⁸ event. The values of R, c_0 , and c_1 are found by fitting the data simultaneously in the two ⁴⁵⁹ regions outside the neutron decay window.

Inside the neutron decay window the background shape is more complicated; at each 461 point in t it depends on the probability that a background electron was not preempted by 462 a neutron decay electron prior to that point, *i.e.*

$$B(t_0 < t < t_1) = c(t)e^{Rt}$$
(14)

463 with

$$c(t) = c_1 - (c_1 - c_0) \frac{\int_t^{t_1} N(t') dt'}{\int_{t_0}^{t_1} N(t') dt'}.$$
(15)

Here N(t) is the neutron decay wishbone function that can be obtained by subtracting the background B(t) from the measured spectrum and applying the dead time correction factor $e^{-R(t_1-t)}$. We start with an estimate for N(t) and find the background B(t) using equations $e^{-R(t_1-t)}$. We start with an estimate for N(t) and find the background B(t) using equations using equations $e^{-R(t_1-t)}$. Subtracting B(t) from the measured wishbone slice yields an improved, measured re $e^{-R(t_1-t)}$ and we repeat the process iteratively until the resulting background subtracted wishbone function N(t) is stable (typically three iterations). We note that $c_0/c_1 \approx 0.99$ in the beta energy range of interest (100 keV-400 keV) so the function c(t) in equation 15 e^{-1} affects the background subtraction at the 1 % level. This background subtraction algorithm e^{-1} was extensively tested using pseudodata and it worked very effectively.

Figure 14 shows a 20 keV wide vertical slice (blue) of the raw wishbone (figure 13), 473 474 centered at 100 keV, the lowest beta energy that was used in the final analysis. Also shown 475 is the same slice after background subtraction (green), *i.e.* the measured neutron decay wishbone function N(t). The background outside the neutron decay window is flat and 476 without apparent structure. The bottom plot in the figure is a fit of the same background-477 subtracted slice to a zero-slope line with the neutron decay window $(3-4.6) \mu s$ excluded. 478 The variation in counts is consistent with Poisson statistical fluctations. Figure 15 shows similar plots for a 20 keV wide vertical slice of the raw wishbone (figure 13) centered at 380 keV, the highest beta energy that was used in the final analysis. As can be seen here, the signal to background ratio (S/B) was strongly dependent on beta energy. In the energy range used in the analysis, $E_e = 100 \text{ keV}-380 \text{ keV}$, the average S/B was 0.2. 48**5**

During the experimental run, as a systematic check, we collected 19 hours of beam data 486 with the polarity of the electrostatic mirror reversed. This prevented all neutron decay 487 protons from reaching the proton detector with minimal effect on background coincidences. 488 Data from this run are shown in figure 16, again 20 keV wide slices centered at beta energies 489 100 keV and 380 keV. Other than the expected exponential there is no apparent structure 490 in the background inside or outside the neutron decay window. The green points are after 491 background subtraction using the same algorithm as for the neutron decay data described 492 above, and fitting to a zero-slope line. A full background-subtracted and deadtime-corrected 493 wishbone plot is shown in figure 17, obtained from the data shown in figure 13. Blue points ⁴⁹⁵ are positive and red points are negative (due to background subtraction).

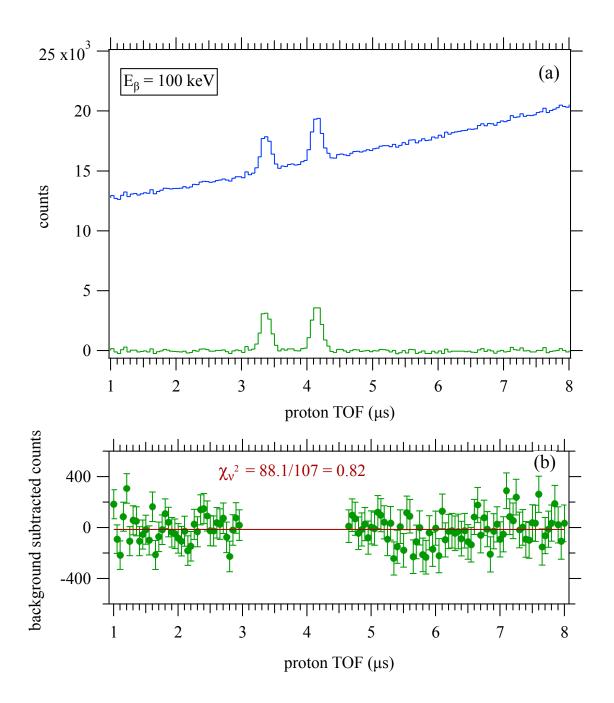


FIG. 14. (a) A 20-keV wide wishbone slice centered at beta energy 100 keV (blue, higher), and the same wishbone slice after subtracting background (green, lower). (b) The same background subtracted slice fit to a horizontal line, excluding the neutron decay region (3–4.6 μ s). Error bars are statistical.

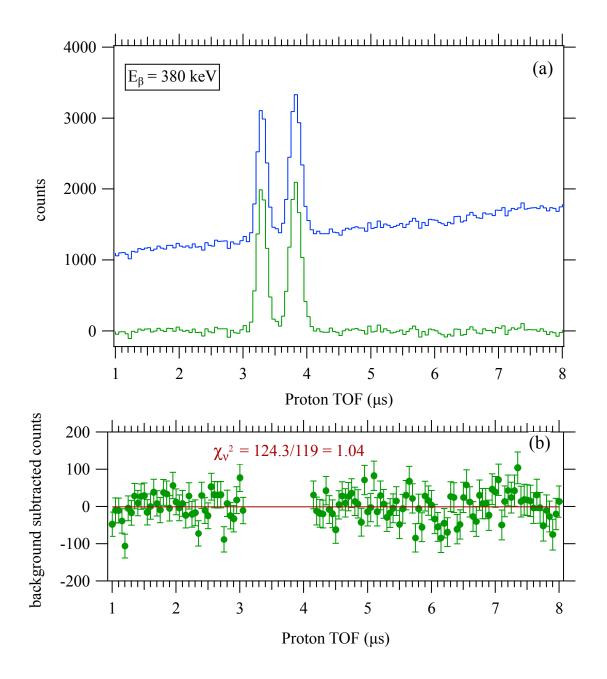


FIG. 15. (a) A 20-keV wide wishbone slice centered at beta energy 380 keV (blue, higher), and the same wishbone slice after subtracting background (green, lower). (b) The same background subtracted slice fit to a horizontal line, excluding the neutron decay region (3–4.6 μ s). Error bars are statistical.

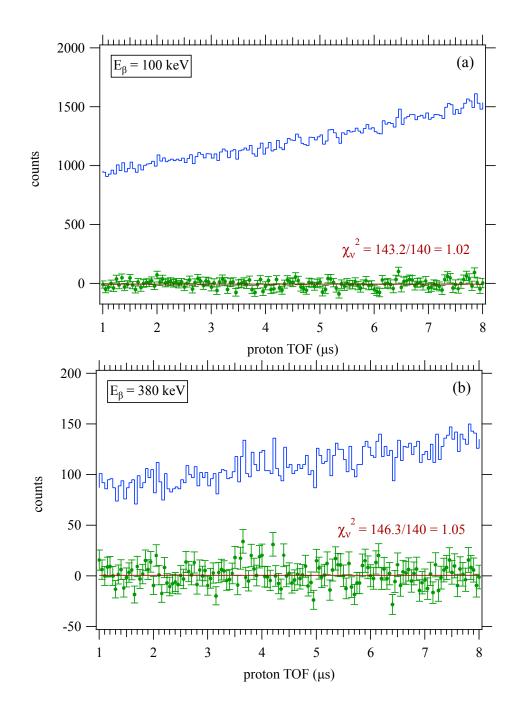


FIG. 16. 20-keV wide wishbone slices centered at (a) 100 and (b) 380 keV for a data series where the polarity of the electrostatic mirror was reversed, so neutron decay protons could not be detected. The upper curve (blue) is the raw wishbone and the lower curve (green) is after subtracting background and fitting to a horizontal line. Error bars are statistical.

497 C. Energy Calibration Fit

The absolute beta energy calibration was monitored during the run by collecting data 498 ⁴⁹⁹ from *in situ* conversion electron sources (¹¹³Sn and ²⁰⁷Bi) 3–4 times per week, interleaved with the neutron decay data series. A more robust and precise energy calibration was obtained 500 ⁵⁰¹ later for each data group using the neutron decay beta spectrum. Figure 18 (a) shows the wishbone energy spectrum, which is the background subtracted wishbone data (figure 17) 502 ⁵⁰³ summed over proton TOF. The corresponding theoretical spectrum is the Fermi beta energy spectrum $F(E_e) = E_e |\mathbf{p}_e| (Q - E_e)^2$ found in equation 1, multiplied by the correction function 505 F(Z = 1, E) [31] that accounts for the Coulomb interaction between the beta electron and ⁵⁰⁶ proton. Other shape effects due to recoil order and radiative corrections are negligible here ⁵⁰⁷ and have been omitted. The spectrum shape is significantly modified by the beta and proton momentum acceptances for coincidence events imposed by the aCORN collimation. 508 The solid curve in figure 18 (top) is this theoretical spectrum computed numerically using 509 ⁵¹⁰ the collimator diameters, axial magnetic field strength, and neutron beam geometry. The ⁵¹¹ theoretical function was fit to the data to minimize chi-squared, with four variable free 512 parameters:

- An overall multiplicative scale factor
- A linear energy calibration slope
- A linear energy calibration offset

• The theoretical function was convoluted with a normalized Gaussian energy response function $G(E, E') = \frac{1}{\sqrt{\pi C E'}} \exp(-(E - E')^2/CE')$, based on the expected \sqrt{E} resolution-width dependence of the scintillator detector. The constant C was a free parameter in the fit.

Acceptable fits were obtained as illustrated in figure 18. With this method the wishbone data were self-calibrating for beta energy. This result also supports the success of the background subtraction, the absence of extraneous structure in the data, and the effectiveness of the backscatter suppression which obviated the need for a low energy tail in the beta response function. We note that the wishbone energy spectrum in figure 18 is insensitive to the wishbone asymmetry and the value of the *a*-coefficient so these fits had no bearing on the suppression which VID), other than to provide the absolute beta energy scale.

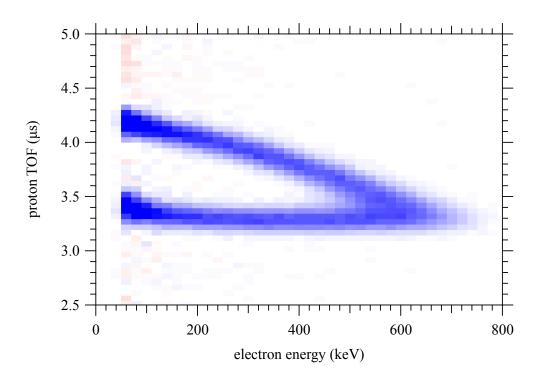


FIG. 17. A background-subtracted wishbone plot (data from figure 13). Blue points are positive and red are negative.

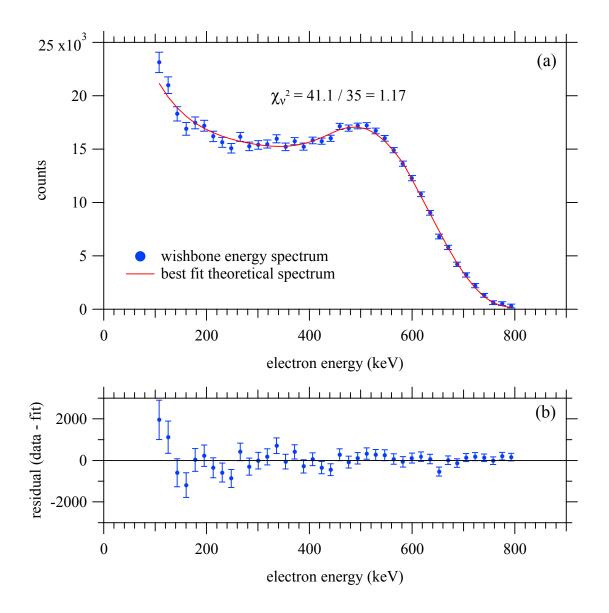


FIG. 18. (a) The wishbone energy spectrum, *i.e.* the background subtracted wishbone (figure 17) summed over proton TOF and the best fit theoretical spectrum. (b) Fit residuals (data minus fit). Error bars are statistical.

527 D. Wishbone Asymmetry Analysis, Magnetic Field Up

To calculate the wishbone asymmetry X(E) for data taken with the magnetic field up ⁵²⁸ direction (B_{up}), we start with 20-keV wide vertical slices of the background-subtracted wish-⁵³⁰ bone plot (figure 17) for each data group. The background-subtracted histograms (green) ⁵³¹ in figures 14, 15 are examples of these. From equation 6 we have

$$X(E) = \frac{N^{I}(E) - N^{II}(E)}{N^{I}(E) + N^{II}(E)}$$
(16)

 $_{532}$ where $N^{I}(E)$ and $N^{II}(E)$ are the counts in the fast (left) and slow (right) peaks, respectively, for each energy slice, summed over all B_{up} data groups. Because the fast and slow peaks 533 tend to overlap a bit, we are faced with the questions of which TOF bin to use to separate 534 them, and how to apportion the counts within that bin. For this we use Monte Carlo data as 535 a guide. We take a high-statistics Monte Carlo wishbone slice for each beta energy, and find 536 the TOF bin and its apportionment that reproduces the exactly correct wishbone asymmetry 537 based on the input value of the *a*-coefficient. This can always be done in spite of the slight 538 overlap of the fast and slow peaks. We expect a systematic uncertainty in this procedure that 539 will be small for low beta energy where the overlap is negligible, and large for beta energy 540 above ≈ 400 keV where the overlap becomes significant. To estimate this uncertainty, we 541 assume that the correct apportionment of the TOF separation bin lies somewhere between 542 $_{543}$ 100 % of its counts to the slow peak and 100 % to the fast peak, and assign this full range 544 a 95 % C.L. ($\pm 2\sigma$). It then follows that the 1 σ systematic uncertainty equals one-half the counts in the separation bin divided by the total counts in the fast and slow wishbone peaks. 545 Figure 19 shows the average systematic uncertainty in the wishbone asymmetry using this 546 prescription, compared to the Poisson statistical uncertainty in X(E) for all B_{up} data. We 547 $_{548}$ restrict the *a*-coefficient analysis to the energy range where this systematic uncertainty is $_{550}$ less than the statistical, *i.e.* up to 380 keV.

The wishbone data for beta energy ≤ 80 keV has a number of issues:

• Beta electrons may have zero axial momentum and still satisfy the transverse momentum acceptance, adding a tail to the wishbone TOF.

• Some beta electrons will miss the active region of the beta spectrometer, as shown by Monte Carlo simulation, complicating the geometric function $f_a(E)$.

• The wishbone signal/background is very poor in this energy region and the background subtraction is imperfect.

⁵⁵⁸ From the above considerations we choose the energy range 100 keV–380 keV for the *a*-⁵⁵⁹ coefficient analysis. The uncorrected wishbone asymmetry X(E) for all B_{up} data is shown ⁵⁶⁰ in figure 20.

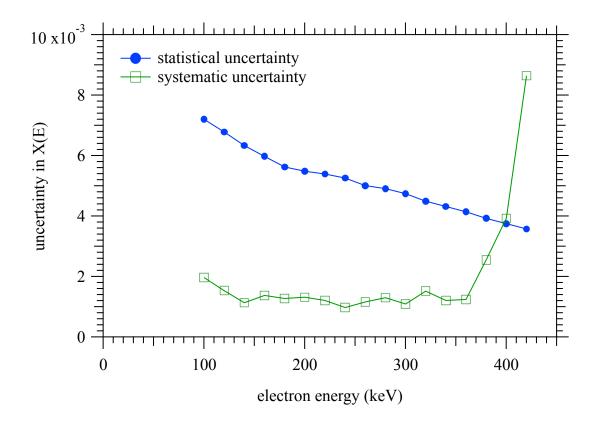


FIG. 19. The estimated systematic uncertainty in computing the wishbone asymmetry X(E) from the data, compared to the Poisson statistical uncertainty.

562 E. Systematic Effects and Corrections

563 1. Electrostatic Mirror

The electrostatic mirror was designed to provide an approximately uniform axial electric field in the proton transport region. Protons associated with group I and II wishbone events tend to have different trajectories inside the mirror so the presence of transverse electric fields will cause a bias in their transmission within the proton collimator. Through Monte Carlo studies we found that a 0.1 % uniform transverse electric field, relative to the axial, produces a 0.5 % false wishbone asymmetry. Due to the precision of its construction and alignment (see figure 11) the uniform transverse field was much smaller than this. However to the upper (grounded) wire grid. In the NG-6 run this effect gave the largest correction to the result: (5.2 ± 1.1) % [25]. For the NG-C run the grid support structure was modified and

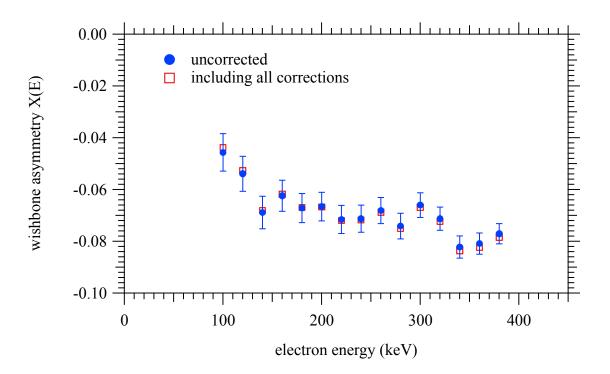


FIG. 20. The wishbone asymmetry X(E) for the combined B_{up} data, uncorrected with statistical error bars, and with all corrections.

⁵⁷⁴ the upper linear grid was replaced with the crossed wire grid shown in figure 8. A detailed ⁵⁷⁵ 3D COMSOL model, depicted in figure 21, was built to calculate the resulting electric field ⁵⁷⁶ shape. This field map was input to the aCORN proton transport Monte Carlo to calculate ⁵⁷⁷ the beta-energy dependent correction shown in figure 22, an overall relative correction to the ⁵⁷⁸ wishbone asymmetry of (1.49 ± 0.30) %. The uncertainty was calculated using a standard ⁵⁷⁹ 20 % relative uncertainty that we chose and assigned to all Monte Carlo corrections in this ⁵⁸⁰ experiment. We regard this uncertainty to be an overestimate as the electric field and proton ⁵⁸⁰ transport calculations are expected to be much more accurate than 20 %.

584 2. Magnetic Field

The proton collimation is affected by both the shape and absolute value of the magnetic field in the proton transport region. In particular, a transverse magnetic field will cause a bias in proton collimation and thence a false wishbone asymmetry. For a radially symmetric transverse field the effect averages out. The absolute value of the magnetic field is used to calculate the geometric function $f_a(E)$; an error in the absolute field will result in a

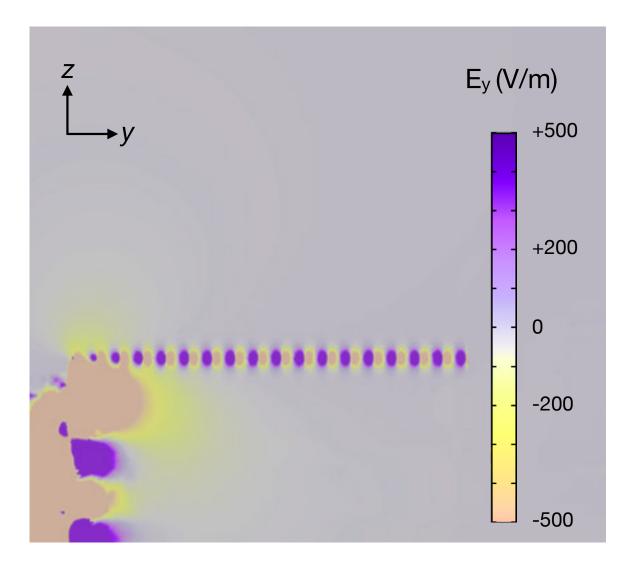


FIG. 21. A COMSOL finite element map of the transverse electric field inside the NG-C electrostatic mirror, in the region near the upper wire grid through which the protons pass.

 $_{590}$ proportional error in the *a*-coefficient result.

Through Monte Carlo analysis we have found that the false asymmetry is proportional to ⁵⁹¹ Through Monte Carlo analysis we have found that the false asymmetry is proportional to ⁵⁹² the average magnitude of the transverse magnetic field in the proton transport region. An ⁵⁹³ average of 4 μ T produces a wishbone asymmetry of $\Delta X = -3.4 \times 10^{-4}$ which is about 0.5 % ⁵⁹⁴ of the *a*-coefficient asymmetry. Based on the field maps, the average transverse field in the ⁵⁹⁵ B_{up} configuration was 1 μ T giving a systematic error in the asymmetry of $\Delta X = -8.5 \times 10^{-5}$ ⁵⁹⁶ and we assign an uncertainty equal to the size of the correction.

⁵⁹⁷ The absolute axial magnetic field was determined from NMR measurements on a glass ⁵⁹⁸ cell filled with spin-polarized ³He that was lowered into the proton collimator from above. ⁵⁹⁹ For B_{up} the result was $B_{axial} = 36.39(11)$ mT, which leads to an uncertainty of 0.3 % in the

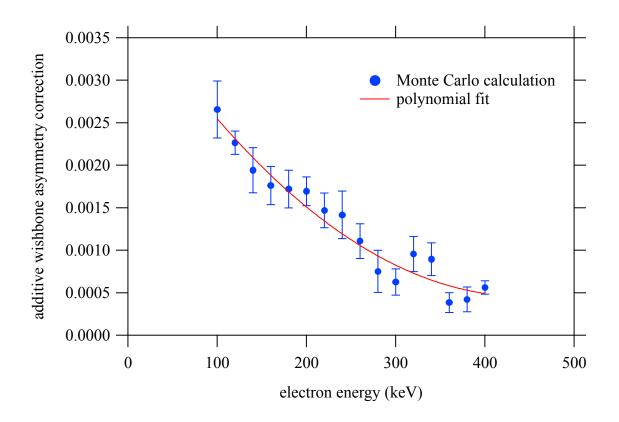


FIG. 22. The electrostatic mirror correction calculated by proton transport Monte Carlo using the 3D COMSOL model of the electric field. The red curve is a smoothed average obtained by fitting the Monte Carlo data to a second order polynomial. Error bars are statistical.

600 calculated $f_a(E)$.

601 3. Electron Backscatter

Approximately 5 % of electrons that strike the active energy detector will backscatter from it and the energy deposited is incomplete, producing a low energy tail in the electron response function. Such backscattered events have two undesirable effects: 1) they tend for to fill in the gap between the wishbone branches (see figure 3) and confound our ability for to cleanly separate group I and group II events; and 2) they systematically shift events from group II into group I, causing a false positive wishbone asymmetry. The backscatter for veto system in the beta spectrometer was used to mitigate this problem. Electrons may also scatter from the beta collimator with similar effect. These cannot be vetoed, but the for the beta spectrometer was designed to limit the probability of a scattered electron to reach the beta ⁶¹¹ spectrometer to 0.3 %, as verified in a PENELOPE simulation. Electron scatter from other ⁶¹² materials or residual gas, and electron Bremsstrahlung, were investigated during the NG-6 ⁶¹³ run and found to be negligible [27].

Our best test for electron backscatter effects was in the wishbone data. We looked for 614 an excess of events in the gap between the wishbone branches and compared to a Monte 615 Carlo wishbone that included a low energy scattering tail. Figure 23 shows a combined 616 $_{617}$ background-subtracted wishbone plot with all B_{up} data. The choice of the gap region, indicated in green, required some optimization. We want to use a large region while avoiding 618 ⁶¹⁹ the tails of the wishbone branches and avoiding low energies where the background subtraction uncertainty is large. A nonzero total of counts in this region can be attributed 620 to non-vetoed backscattered electrons but would also include contributions from electron 621 collimator scattering, electron scattering from the wire grid (section VIE4), and proton 622 collimator scattering (section VIE9). The number of counts in the chosen gap is 62 ± 490 , 623 consistent with zero. The uncertainty is due to the background subtraction. We take the 624 total 62 + 490 = 552 counts to be the 1σ upper limit due to non-vetoed backscattered elec-625 ⁶²⁶ trons, and zero to be the lower limit. We generated Monte Carlo wishbone data, including a ₆₂₇ flat tail in the electron energy response function, and varied the tail area to achieve a count ₆₂₈ rate in the gap region that equals the 1σ upper limit. The resulting tail area was 0.59 % of $_{629}$ the peak, which produces an average false asymmetry of +1.5 %. Therefore our systematic 630 error due to electron backscatter is $(+0.75 \pm 0.75)$ %.

632 4. Electron Energy Loss in Grid

Beta electrons pass through the positive grid at the bottom of the electrostatic mirror. The grid is composed of parallel wires, diameter 100 μ m, made of 2 % beryllium copper with approximately 1 μ m coatings of nickel and gold. The wire spacing is 2 mm, so the geometric probability of striking a grid wire is approximately 5 %. When an electron strikes a wire the main systematic effect comes from energy loss. A beta electron will generally pass through the wire and lose typically about 100 keV. Electrons may also be scattered into a different direction, but to first order the probability of scattering into the collimator acceptance is the same as the probability of scattering out of it, and because the wishbone the wire asymmetry is insensitive to beta collimation this does not create a systematic error. Energy

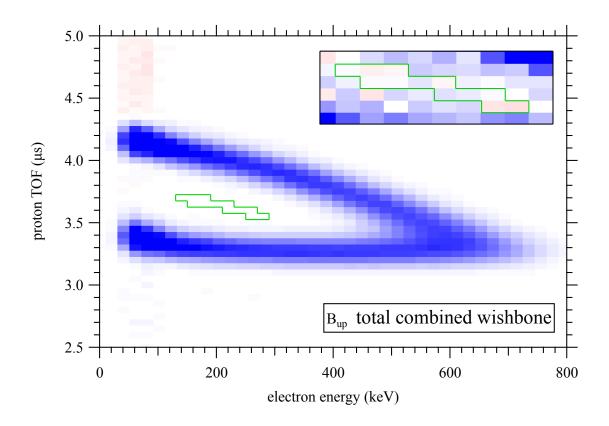


FIG. 23. A combined background-subtracted wishbone plot with all B_{up} data. The event total in the region outlined in green was used to test for the presence of a low energy tail in the detected electron response function due to electron scattering. The inset shows the same green-outlined region with an expanded color scale. Blue points are positive counts, red points are negative due to the background subtraction.

⁶⁴² loss in a grid wire is similar to backscatter from the beta spectrometer in its effect, but ⁶⁴³ instead of producing a broad low energy tail it produces a small low energy shoulder on ⁶⁴⁴ the energy response function, which is less of a problem. Energy loss in the grid and its ⁶⁴⁵ effect on the electron energy response was calculated using the NIST ESTAR data base [32]. ⁶⁴⁶ The associated error in the wishbone asymmetry is $(+1.0\pm0.2)$ %, using our 20 % standard ⁶⁴⁷ Monte Carlo uncertainty.

648 5. Beta Energy Calibration

As discussed in section VIC, the most precise beta energy calibration comes from a fit $_{650}$ to the wishbone data. The combined calibration from all B_{up} data gives an overall energy ⁶⁵¹ uncertainty of $\sigma(E) = \pm 0.48$ %. The corresponding uncertainty in the wishbone asymmetry ⁶⁵² is

$$\sigma(X) = a \frac{\partial f_a(E)}{\partial E} \sigma(E) \tag{17}$$

 $_{653}$ which has an average value of 0.27 % in the energy range 100 keV–380 keV.

654 6. Proton Energy Threshold

Protons associated with group I and II coincidence events differ in kinetic energy by an 655 average of 380 eV. Both groups of protons are preaccelerated by the electrostatic mirror 656 and then, after passing through the proton collimator, accelerated to a final energy of about 30 keV by the proton focusing electrodes and detector. While this difference in energy 658 is a small fraction of the detected energy, protons near threshold nevertheless contain a 659 slightly higher fraction of group II protons. If these are not completely counted, a false 660 negative wishbone asymmetry results. In the NG-6 aCORN run about 1.2 % of protons 661 were excluded by the PIXIE threshold which lead to a 3.0 % false asymmetry [25]. For the 662 NG-C run we significantly lowered the PIXIE energy threshold (see section IV C). Figure 24 663 shows a fit of a typical proton energy spectrum fit to a Gaussian plus a 4th order polynomial 664 ⁶⁶⁵ background function to extract the Gaussian component. The fraction of events excluded $_{666}$ by the threshold is less than 0.02 % and the resulting false asymmetry is negligible.

668 7. Collimator Insert Alignment

A small angular misalignment ϕ_{coll} (radians) of the proton collimator is equivalent to a angular misalignment ϕ_{coll} (radians) of the proton collimator is equivalent to a uniform transverse magnetic field $B_{\text{trans}} = \phi_{\text{coll}} B_{\text{axial}}$. Figure 11 shows a summary of the collimator alignment measurements. The variation in results obtained by two independent by two independent cobservers for the same misalignment strongly suggests that the overall variation is due mostly to measurement error rather than differences in the actual misalignment. Therefore we take the mean misalignment and the standard deviation (square root of variance) from all nine the measurements: $\phi_{\text{coll}} = (0.101 \pm 0.035)$ mrad. Using $B_{\text{axial}} = 0.0364$ T we have $B_{\text{trans}} =$ $\sigma_{76} (3.7 \pm 1.3) \mu$ T. Using the Monte Carlo result described in section VIE2, this results in $\sigma_{77} \Delta X = (-3.1 \pm 1.3) \times 10^{-4}$, where the standard 20 % Monte Carlo uncertainty has been σ_{76} included in quadrature. Note that this effective transverse magnetic field is independent of

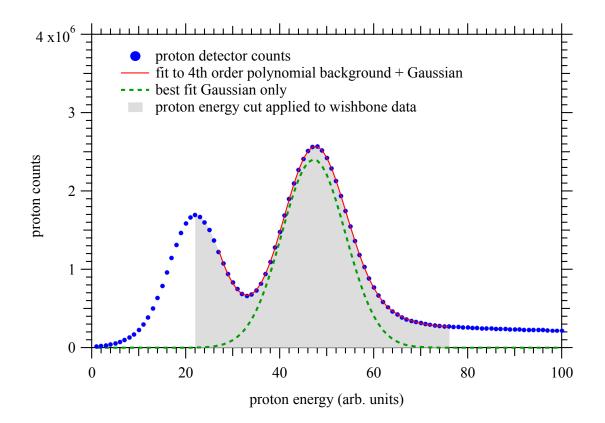


FIG. 24. A typical proton energy spectrum (blue) fit to a 4th order polynomial background function plus a Gaussian (red). The resulting Gaussian alone is shown in green. The soft energy threshold of the PIXIE-16 takes effect below channel 27. The slight loss of protons below threshold has a negligible effect on the wishbone asymmetry.

⁶⁷⁹ that measured by the field mapper as the collimator was not present when the maps were ⁶⁸⁰ made. Therefore we treat the collimator misalignment as an independent source of error.

Similarly, a misalignment of the electrostatic mirror would introduce an approximately uniform transverse electric field. From Monte Carlo analysis we found that a 1 mrad misalignment will produce a false wishbone asymmetry of $\Delta X = -4 \times 10^{-4}$. The mean and standard deviation of the measured values shown in figure 11 is $\phi_{\text{mirror}} = (0.43 \pm 0.13)$ mrad corresponding to $\Delta X = -1.7 \pm 0.6 \times 10^{-4}$.

686 8. Residual Gas Interactions

Protons travel about 2 m from the decay region to the detector. If a proton interacts with residual gas during this trip it may be neutralized or scattered. Neutralized protons cause 669 neutron decay events to be eliminated and they may introduce a false wishbone asymmetry ⁶⁹⁰ due to the slight velocity-dependence of the neutralization probability. Scattered protons ⁶⁹¹ result in a larger TOF in the wishbone plot which may also result in a false wishbone asymmetry. Monte Carlo analyses showed that proton scattering and neutralization have 692 ₆₉₃ opposite-sign effects on the asymmetry, and that their relative probability depends on the ⁶⁹⁴ gas species. We accounted for this effect by collecting data for 134 hours with a deliberately higher pressure in the chamber, effected by partially closing a gate valve to the turbopump. 695 The average pressure in the proton collimator during the high pressure run was 1.79×10^{-3} 696 Pa $(1.34 \times 10^{-5} \text{ torr})$, compared to the normal pressure of 8.0×10^{-5} Pa $(6.0 \times 10^{-7} \text{ torr})$, a 697 factor of 22 higher. Residual gas analyzer (RGA) measurements indicated that the gas was 698 dominated by hydrogen and water (due to outgassing from the beta spectrometer plastic 699 ⁷⁰⁰ scintillator) at both pressures.

⁷⁰¹ Comparing the wishbone asymmetry from the high pressure run, from beta energy 100 ⁷⁰² keV-380 keV, to that of the production B_{up} data, we found an average difference $\Delta X =$ ⁷⁰³ -0.0024±0.0070, consistent with no effect. We therefore estimate the systematic uncertainty ⁷⁰⁴ due to residual gas interaction as $\sigma_X = 0.0070/22 = 3.2 \times 10^{-4}$.

705 9. Proton Scattering from the Collimator

A large number of neutron decay protons strike the aluminum knife edge elements of 706 ⁷⁰⁷ the proton collimator. A SRIM Monte Carlo study showed that for protons with energy in the range 2–3 keV, about 90 % of those will be absorbed in the aluminum, 9.5 % will 708 emerge as neutral hydrogen atoms, and the remaining 0.5 % emerge as bare protons, having 709 $_{710}$ lost an average of 2/3 of their kinetic energy. Many of those will subsequently strike the collimator again and be removed but some fraction will be detected with TOF that is 712 systematically too large. Absorbed and neutralized protons are not detected and cause no 713 systematic effect. Because protons are accelerated by the electrostatic mirror they have a ⁷¹⁴ minimum possible axial momentum while in the collimator. This sets an upper limit on the TOF for unscattered protons in the wishbone plot. Scattered neutron decay protons 715 $_{716}$ would appear beyond this maximum as a broad tail several μ s in width, and we can study ⁷¹⁷ this effect in the wishbone plot. This effect is insensitive to beta energy, so it is useful ⁷¹⁸ to look at relative high beta energy where the statistical uncertainty due to background ⁷¹⁹ subtraction is smaller. We use the beta energy range 400 keV–600 keV. Figure 25 (a) shows ⁷²⁰ the total B_{up} wishbone proton TOF spectrum summed from 400 keV–600 keV compared ⁷²¹ to the equivalent Monte Carlo proton TOF spectrum. Figure 25 (b) is the same with an ⁷²² expanded vertical scale. We choose 1- μ s wide regions just before and after the wishbone ⁷²³ TOF peak where the Monte Carlo counts are zero and take the difference of their sums, post-⁷²⁴ wishbone minus pre-wishbone, which is 2296 ± 2400 counts. As a fraction of the wishbone ⁷²⁵ peak area this is 0.0010 ± 0.0011, consistent with the SRIM estimate but also statistically ⁷²⁶ consistent with zero. Comparing this to a Monte Carlo analysis where a proton scattering ⁷²⁷ TOF tail was included, this corresponds to a systematic error in the wishbone asymmetry ⁷²⁸ of $\Delta X = -0.00036 \pm 0.00038$.

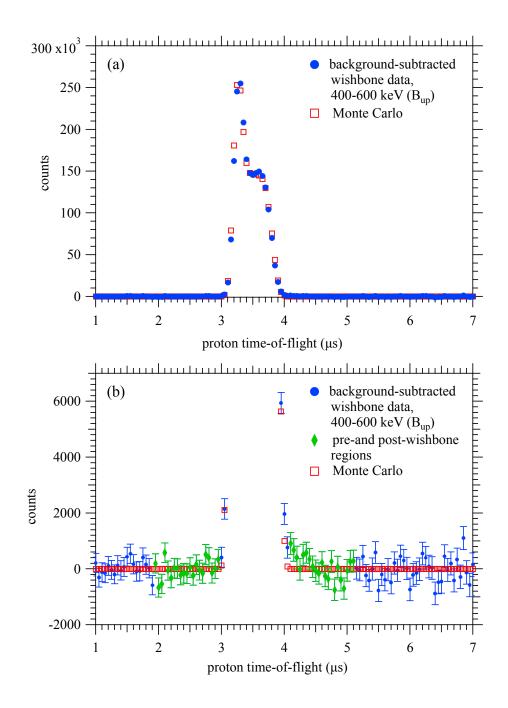


FIG. 25. (a) The total B_{up} wishbone proton TOF spectrum summed from 400–600 keV compared to the equivalent Monte Carlo proton TOF spectrum. (b) The same plot with an expanded vertical scale and statistical error bars. The 1 μ s wide regions pre- and post-wishbone used to estimate the proton scattering tail are shown in green.

730 10. Proton Focusing

The proton detector focusing system was designed to focus all neutron decay protons that were accepted by the proton collimator onto the active region of the surface barrier detector. The focusing efficiency, while very good, was not perfect. A small fraction of protons may strike the focusing electrodes or an inactive region of the detector, or miss the detector entirely. Because the average kinetic energies of the fast (group I) and slow (group protons differ slightly at the exit of the collimator, and the focusing efficiency is expected to depend on kinetic energy, imperfect proton focusing will lead to a systematic error in the wishbone asymmetry. This effect was studied computationally and experimentally.

A simulation of the focusing assembly and related apparatus was developed using the r40 software suite AMaze by Field Precision⁶ The relative positions of the surface barrier proton r41 detector and ring and fork electrodes were accurately measured using a FARO⁷ coordinate r42 measuring device. An auxiliary simulation produced neutron decay protons at the exit of r43 the proton collimator and transported them to the exit of the proton collimator. These r44 proton momenta were then fed into the AMaze simulation to track them to the detector.

We fabricated a set of thin aluminum detector masks that blocked different regions of the 745 ⁷⁴⁶ detector face. One of these (the "R4" mask) blocked a central circle 24.8 mm in diameter, ⁷⁴⁷ leaving a ring of width 3 mm at the outer edge of the active region exposed to detect protons. Neutron decay data were collected with the various masks installed in 1–2 day runs. The 748 749 resulting background-subtracted wishbone event rates were compared to the rates found in ⁷⁵⁰ the simulation using the same mask geometries which enabled us to fix the absolute position ⁷⁵¹ of the detector system in space relative to the neutron beam and collimator. The simulation $_{752}$ then computed the focusing efficiency. Figure 26 shows a simulation of 10^6 neutron decay 753 protons, out of which 146 struck the focusing ring (green circles) and 154 struck the inactive region of the detector (red circles). No protons missed the detector assembly entirely. The 754 resulting focusing efficiency was 99.97 %. A 45-hour run with the R4 mask in place produced 755 a wishbone event rate of $(3.8 \pm 1.9) \times 10^{-3} \text{ s}^{-1}$, or (0.33 ± 0.17) % of the normal unmasked 756 ⁷⁵⁸ rate, consistent with the AMaze simulation.

From the simulation of the B_{up} proton assembly the systematic error in the wishbone asymmetry was determined to be $\Delta X/X = -0.0042 \pm 0.0058$, including a 20 % quadrature

⁶ Field Precision, LLC, Albuquerque, NM, USA.

⁷ FARO Technologies, Lake Mary, FL, USA.

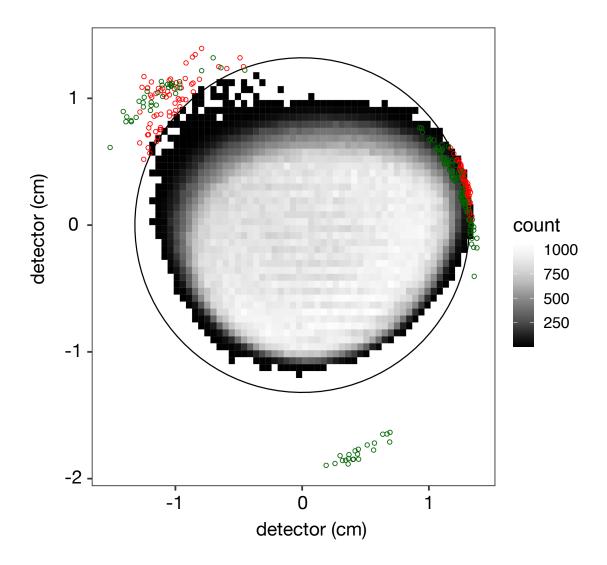


FIG. 26. Results from a proton focusing simulation tracking 1 million neutron decay protons from the proton collimator to the detector. Green and red circles are protons striking the focusing ring and detector inactive region, respectively. The thin black circle indicates the active region of the surface barrier detector.

⁷⁶¹ uncertainty for the Monte Carlo.

Approximately 0.5 % of protons incident on the detector are expected to backscatter 763 without producing a countable signal. This occurs at the full kinetic energy 30 keV, where 764 the relative energy difference between the fast and slow groups (about 380 eV) is small, so 765 the associated systematic error due to proton backscatter is negligible.

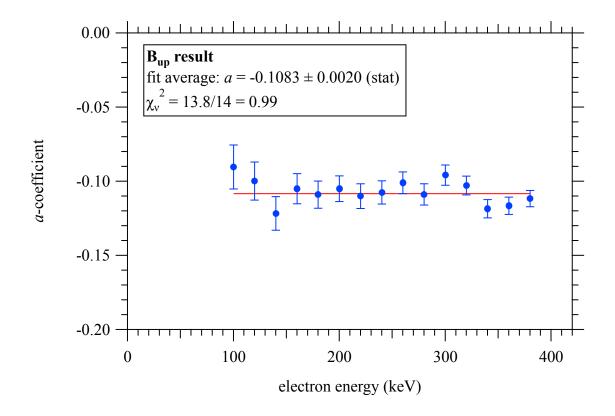


FIG. 27. The corrected B_{up} wishbone asymmetry (see figure 20), divided by the geometric function $f_a(E)$ (see figure 4), giving the measured *a*-coefficient for each beta energy slice. These were fit to a constant to produce the *a*-coefficient result for the B_{up} data. Error bars are statistical.

⁷⁶⁶ F. Wishbone Asymmetry Result, Magnetic Field Up

To produce the corrected wishbone asymmetry, we started with $[X(E) - \delta_2(E)] / [1 + \delta_1(E)]$ (see equation 8) and added the systematic corrections described above. This can be seen in figure 20. The corrected wishbone asymmetry was then divided by the geometric function f_{70} $f_a(E)$ to give the measured value of the *a*-coefficient for each energy slice, shown in figure 771 27. These were then fit to a constant to obtain the overall result

$$a = -0.10834 \pm 0.00197(\text{stat}) \pm 0.00156(\text{sys}) \quad (B_{up}).$$
 (18)

773

⁷⁷⁴ G. Wishbone Asymmetry Analysis, Magnetic Field Down

After finalizing the B_{up} result, we analyzed the B_{down} data in the same way, except that four systematic effects were analyzed independently for B_{down} :

1. Magnetic field shape: In the B_{down} field maps the average transverse magnetic field magnitude was 2 μ T, a factor of two larger than in the B_{up} field maps, so the systematic correction was correspondingly larger, and as before we assign an uncertainty equal to the correction, giving $\Delta X = (-1.7 \pm 1.7) \times 10^{-4}$.

2. Absolute magnetic field: Independent ³He NMR measurements were made in the B_{down} configuration with the result $B_{axial} = 0.03624(11)$ T. Because the geometric function $f_a(E)$ was calculated using $B_{axial} = 0.0364$ T, a correction of (0.4 ± 0.3) % to the wishbone asymmetry was needed.

3. **Proton scattering:** While the effect of proton scattering from the collimator should be the same for B_{up} and B_{down} , it was analyzed independently using the method described in section VIE9. The count rate difference in 1- μ s wide regions just before and after the wishbone TOF peak was smaller, -26 ± 2272 counts, leading to a smaller estimate for the correction: $\Delta X = 0 \pm 0.00034$.

4. Proton focusing: In order to accomodate the change in sign of the $E \times B$ force, a separate proton focusing assembly with slightly different geometry was used for the B_{down} run. The systematic error in the wishbone asymmetry was estimated from the B_{up} analysis to be $\Delta X/X = 0 \pm 0.010$, including a 20 % quadrature uncertainty for the Monte Carlo.

⁷⁹⁵ All other systematic corrections and uncertainties were the same as described in section ⁷⁹⁶ VIE. The wishbone asymmetry X(E) for the combined B_{down} data, both uncorrected (blue ⁷⁹⁷ dots) with statistical error bars, and with all corrections (red squares), are shown in the top ⁷⁹⁸ plot of figure 28. The bottom plot shows the corrected wishbone asymmetry, divided by ⁷⁹⁹ the geometric function $f_a(E)$, giving the measured *a*-coefficient for each beta energy slice. ⁸⁰⁰ These were fit to a constant to produce the overall *a*-coefficient result for B_{down}

$$a = -0.10690 \pm 0.00187(\text{stat}) \pm 0.00180(\text{sys}) \quad (B_{\text{down}}).$$
 (19)

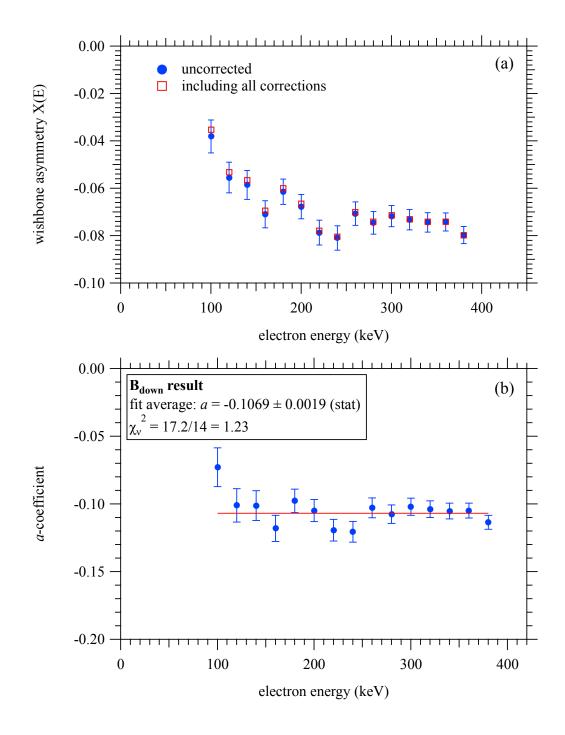


FIG. 28. (a) The wishbone asymmetry X(E) for the combined B_{down} data, uncorrected with statistical error bars, and with all corrections. (b) The corrected B_{down} wishbone asymmetry, divided by the geometric function $f_a(E)$, giving the measured *a*-coefficient for each beta energy slice. These were fit to a constant to produce the *a*-coefficient result for the B_{down} data. Error bars are statistical.

803 VII. RESULT AND DISCUSSION

 $_{804}$ The difference in the results from the B_{up} and B_{down} runs is

$$a(B_{down}) - a(B_{up}) = 0.0014 \pm 0.0027(stat).$$
 (20)

Attributing this difference to a residual neutron polarization gives $P = (5.0 \pm 9.5) \times 10^{-4}$, consistent with zero, using equation 11. At this point in the analysis we unblinded by revealing the directly measured neutron polarization, $P < 4.0 \times 10^{-4}$ (90 % C.L.), an upper limit that confirmed the null polarization. The direct neutron polarization measurement on NG-C is described in detail in another publication [33]. We combine the B_{up} and B_{down} results for the aCORN NG-C run

$$a = -0.10758 \pm 0.00136 (\text{stat}) \pm 0.00148 (\text{sys})$$
 (NG-C combined). (21)

⁸¹¹ The error budget for the combined result is shown in Table I. In producing this table we ⁸¹² used the standard deviation of the mean for the independent systematic uncertainties, *i.e.* ⁸¹³ the enumerated list in section VIG.

This result is in good agreement with the result of the aCORN NG-6 run: $a = -0.1090 \pm$ $a_{15} 0.0030(\text{stat}) \pm 0.0028(\text{sys})$ [25]. We may combine them to obtain an overall result from the a_{16} two completed aCORN physics runs. To combine these two we first compute the weighted a_{17} average value of the *a*-coefficient, using statistical uncertainties only. The only systematic a_{16} correction and uncertainty that was applied equally to both measurements was the effect a_{19} of electron energy loss in the positive grid of the electrostatic mirror; the others were all a_{20} evaluated independently. Therefore we remove the grid uncertainty from both, compute the a_{21} standard deviation of the mean of the two systematics uncertainties, and then add the grid a_{22} uncertainty back in quadrature. The result is

$$a = -0.10782 \pm 0.00124 (\text{stat}) \pm 0.00133 (\text{sys}) \quad (\text{NG-6} + \text{NG-C combined}),$$
(22)

⁸²³ or with the statistical and systematic uncertainties combined in quadrature: $a = -0.10782 \pm$ ⁸²⁴ 0.00181, for a relative uncertainty of 1.7 %. Using equation 2 we can extract a result for ⁸²⁵ $\lambda = G_A/G_V$,

 $\lambda = -1.2796 \pm 0.0062$ (NG-6 + NG-C combined). (23)

Figure 29 shows a summary of four neutron a-coefficient measurements from the past 50 ⁸²⁷ years. The 2020 result from the aSPECT experiment [34], which used an electromagnetic TABLE I. A summary of systematic corrections and uncertainties for the value of the *a*-coefficient in the combined NG-C result. The third column lists the absolute uncertaintes and the fourth column is relative to our final result for |a|. The combined uncertainty is the quadrature sum of statistical and systematic.

systematic	correction	σ uncertainty	relative uncertainty
e scattering	-0.00083	0.00083	0.0077
wishbone asymmetry		0.00064	0.0060
residual gas		0.00048	0.0045
proton scattering		0.00038	0.0035
beta energy calibration		0.00030	0.0028
electrostatic mirror	0.00161	0.00032	0.0030
absolute magnetic field	0.00023	0.00023	0.0022
energy loss in grid	-0.00111	0.00022	0.0020
proton collimator alignment	0.00046	0.00020	0.0019
magnetic field shape	0.00018	0.00011	0.0010
electrostatic mirror alignment	0.00025	0.00009	0.0008
neutron beam density	-0.00045	0.00009	0.0008
proton focusing	0.00036	0.00055	0.0051
total systematic	0.00070	0.00148	0.0137
statistical		0.00136	0.0126
combined uncertainty		0.00201	0.0186

retardation spectrometer to measure the proton energy spectrum, is the most precise. The versal agreement of these is good in spite of the slight tension (1.7σ) between the aSPECT and aCORN results. The weighted average of these is

$$a = -0.10486 \pm 0.00075$$
 (world average). (24)

The effects of the new *a*-coefficient results on the world average for λ are less satisfactory. Figure 30 shows an ideogram, in the style of the Particle Data Group ([6], p. 16), of precise determinations of $\lambda = G_A/G_V$ from the neutron decay beta asymmetry (*A*-coefficient) [10-12, 35-37] and the electron-antineutrino correlation (*a*-coefficient) [34] and this work. Also

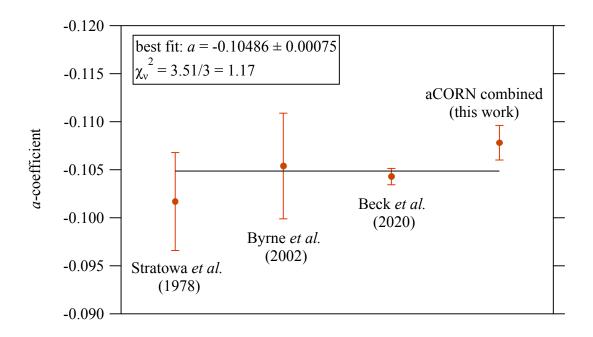


FIG. 29. A summary of neutron a-coefficient measurements from the past 50 years.

included is a determination from the ratio of the A-coefficient to B-coefficient in a combined sr experiment [38]. The distribution is unfortunately bimodal with poor overall agreement $\chi^2_{\nu} = 43.98/8 = 5.37$). The weighted world average is

$$\lambda = -1.2754 \pm 0.0011 \quad \text{(world average)} \tag{25}$$

with the uncertainty expanded by a factor of $\sqrt{5.37} = 2.32$. The aSPECT result adds 839 weight to the more positive number favored by older beta asymmetry experiments. The 841 aCORN result is in better accord with recent beta asymmetry experiments. In particular it 842 ⁸⁴³ is troubling that the most precise results for the A- and a-coefficients [11, 34], both published within the past two years, disagree by 3 standard deviations. In a recent paper Falkowski, et 844 al. [39] show that this difference could be attributed to a non-zero right handed tensor weak 845 current, although an experimental origin seems more likely. New precision experiments, in 846 particular additional measurements of the neutron *a*-coefficient at the <1% level, are needed to address this. The upcoming Nab experiment [40] and a possible future aCORN run at 848 NIST are hoping to achieve such precision. 849

Finally we can update the values of the Mostovoy parameters (equations 4) using the new world average for the a-coefficient (equation 24)

$$F_1 = 1 + A - B - a = 0.0046 \pm 0.0031$$

$$F_2 = aB - A - A^2 = 0.00244 \pm 0.00081.$$
⁽²⁶⁾

⁸⁵² The value of F_2 now exceeds zero by 3σ , a strong deviation, for the first time using this ⁸⁵³ test, from the Standard Model prediction. This follows mainly from the disagreement in the ⁸⁵⁴ value of λ between aSPECT [34] and PERKKEO III [11].

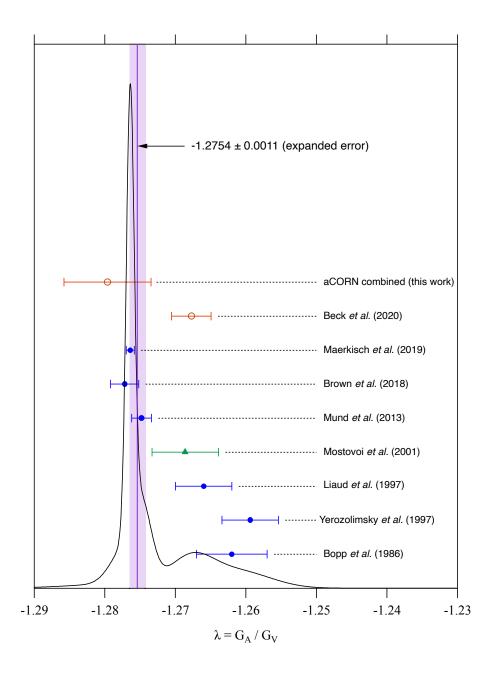


FIG. 30. An ideogram of precision determinations of the neutron decay ratio of axial vector to vector coupling (λ) using the beta asymmetry (A-coefficient, blue circles), the electron-antineutrino correlation (a-coefficient, red open cirles), and the A/B ratio (green triangle). The distribution features two groups of experimental results and the overall agreement is poor. The weighted average is indicated with the uncertainty expanded by a factor of 2.32.

855 VIII. ACKNOWLEDGEMENTS

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- ⁸⁶¹ [1] J. D. Jackson, S. B. Treiman, and H. W. Wyld, Nuclear Physics 4, 206 (1957).
- ⁸⁶² [2] D. Dubbers, Nucl. Phys. **A527**, 239 (1991).
- ⁸⁶³ [3] J. Barranco, G. Miranda, and T. I. Rashba, JHEP **12**, 021 (2005).
- ⁸⁶⁴ [4] S. Bauman, J. Erler, and M. J. Ramsey-Musolf, Phys. Rev. D 87, 035012 (2013).
- 865 [5] Y. Mostovoy and A. Frank, JETP Lett. 24, 38 (1976).
- ⁸⁶⁶ [6] P. A. Zyla, et al. (Particle Data Group), Prog. Theor. Exp. Phys. **2020**, 083C01 (2020).
- ⁸⁶⁷ [7] A. N. Ivanov, M. Pitschmann, and N. I. Troitskaya, Phys. Rev. D 88, 073002 (2013).
- ⁸⁶⁸ [8] T. Bhattacharya, et al., Phys. Rev. D 94, 054508 (2016).
- ⁸⁶⁹ [9] S. Gardner and C. Zhang, Phys. Rev. Lett. 86, 5666 (2001).
- ⁸⁷⁰ [10] D. Mund, et al., Phys. Rev. Lett. **110**, 172502 (2013).
- 871 [11] B. Märkisch, et al., Phys. Rev. Lett. 122, 242501 (2019).
- ⁸⁷² [12] M. A. Brown, et al., Phys. Rev. C 97, 035505 (2018).
- 873 [13] F. E. Wietfeldt and G. L. Greene, Rev. Mod. Phys. 83, 1173 (2011).
- ⁸⁷⁴ [14] J. C. Hardy and I. S. Towner, Phys. Rev. C **91**, 025501 (2015).
- ⁸⁷⁵ [15] C-Y. Seng, M. Gorchtein, H. H. Patel, and M. J. Ramsey-Musolf, Phys. Rev. Lett. **121**, 241804
 ⁸⁷⁶ (2018).
- ⁸⁷⁷ [16] C-Y. Seng, M. Gorchtein, H. H. Patel, and M. J. Ramsey-Musolf, Phys. Rev. D 100, 013001
 ⁸⁷⁸ (2019).
- 879 [17] A. Czarnecki, W. J. Marciano, and A. Sirlin, Phys. Rev. D, 100, 073008 (2019).
- 880 [18] C-Y. Seng, X. Feng, M. Gorchtein, and L.-C. Jin, Phys. Rev. D 101, 111301 (2020).
- ⁸⁸¹ [19] L. Hayen, arXiv:2010.07262 (2020).

- ⁸⁸² [20] V. K. Grigor'ev, A. P. Grishen, V. V. Vladimirskii, E. S. Nikolaevskii, and D. P. Zharkov,
 ⁸⁸³ Sov. J. Nucl. Phys. 6, 239 (1968).
- 884 [21] C. Stratowa, R. Dobrozemsky, and P. Weinzierl, Phys. Rev. D 18, 3970 (1978).
- 885 [22] J. Byrne *et al.*, J. Phys. G **28**, 1325 (2002).
- 886 [23] S. Balashov and Yu. Mostovoy, Russian Research Center Kurchatov Institute Preprint IAE-
- ⁸⁸⁷ 5718 /2, Moscow (1994).
- 888 [24] B. G. Yerozolimsky, et al., arXiv:nucl-ex/0401014 (2004).
- 889 [25] G. Darius, et al., Phys. Rev. Lett. 119, 042502 (2017).
- ⁸⁹⁰ [26] F. E. Wietfeldt, et al., Nucl. Instr. Meth. A611, 207 (2009).
- ⁸⁹¹ [27] B. Collett, et al., Rev. Sci. Instr. 88, 083503 (2017).
- ⁸⁹² [28] T. Hassan, et al., Nucl. Instr. Meth. A 867, 51 (2017).
- ⁸⁹³ [29] www.ncnr.nist.gov
- ⁸⁹⁴ [30] J. C. Cook, Rev. Sci. Instr. **80**, 023101 (2009).
- ⁸⁹⁵ [31] D. H. Wilkinson, Nucl. Instr. Meth. A **275**, 378 (1989).
- ⁸⁹⁶ [32] https://physics.nist.gov/PhysRefData/Star/Text/ESTAR.html
- ⁸⁹⁷ [33] B. C. Schafer, et al., Nucl. Instr. Meth. A 988, 1648662 (2021).
- ⁸⁹⁸ [34] M. Beck, et al., Phys. Rev. C **101**, 055506 (2020).
- ⁸⁹⁹ [35] P. Bopp, et al., Phys. Rev. Lett. 56, 919 (1986).
- 900 [36] B. G. Yerozolimsky, et al., Phys. Lett. B 412, 240 (1997).
- 901 [37] P. Liaud, et al., Nucl. Phys. A 612, 53 (1997).
- ⁹⁰² [38] Yu. Mostovoi, et al., Phys. Atom. Nucl. 64, 1955 (2001).
- 903 [39] A. Falkowski, M. González-Alonso, and O. Naviliat-Cuncic, arXiv:2010.13797v2 [hep-ph]
 904 (2020).
- 905 [40] J. Fry, et al., EPJ Web Conf. 219, 04002 (2019).