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Phys. Rev. C **101**, 044311 — Published 20 April 2020

DOI: [10.1103/PhysRevC.101.044311](https://doi.org/10.1103/PhysRevC.101.044311)

Shape evolution of neutron-rich $^{106,108,110}\text{Mo}$ isotopes in the triaxial degree of freedom

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(Dated: January 29, 2020)

The structure of ^{106}Mo , ^{108}Mo , and ^{110}Mo was investigated through β -delayed γ -ray spectroscopy at the RIKEN RI Beam Factory. New γ -ray transitions and levels are reported, including newly assigned 0_2^+ states in $^{108,110}\text{Mo}$. The β -delayed neutron-emission probabilities of ^{108}Nb and ^{110}Nb were determined by examining the γ rays of their respective daughter decays. Quadrupole deformations were obtained for $^{106,108,110}\text{Mo}$ from their 2_1^+ energies and lifetimes. The even-odd energy staggering in the 2_2^+ band was compared with typical patterns of the γ -vibrational band, rigid triaxial rotor, and γ -soft rotor. The very small even-odd staggering of ^{106}Mo , ^{108}Mo , and ^{110}Mo favors a γ -vibrational band assignment. The kinematic moment of inertia for the 2_2^+ band showed a trend similar to the ground-state band, which is expected for the γ -vibrational band. Beyond-mean-field calculations employing the constrained Hartree-Fock-Bogoliubov (HFB) + local quasiparticle-random-phase approximation (QRPA) method using the SLy5+T interaction reproduced the ground and 2_2^+ bands in ^{106}Mo and ^{108}Mo . The collective wave functions are consistent with the interpretation of the 2_2^+ band as the γ -vibrational band of the prolate shape. However, the staggering pattern observed in ^{110}Mo differs from the one suggested in the calculations which predict a γ -soft rotor. There was no experimental indication of the oblate shape or the γ -soft rotor predicted in heavier Mo isotopes.

The triaxial degree of freedom, γ , plays an important role in collective excitations of deformed even-even nuclei. While the first $J^\pi = 2^+$ state (2_1^+) is sensitive primarily to the quadrupole deformation parameter, β , the so-called γ band with a 2^+ band head is strongly related

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to triaxial motion [1]. In the case of axially-symmetric quadrupole deformation, a rotational band built on a γ -vibrational state constitutes the γ band. The energy of its band head is related to the softness of the vibrational motion in the γ direction. When the potential energy surface (PES) has a deep minimum between $\gamma = 0^\circ$ (prolate) and 60° (oblate), the nucleus takes on a static triaxial shape and rotates about all three axes of the intrinsic body. The rigid triaxial rotor model by Davydov *et al.* [2] predicts that the 2_2^+ state lies below the 4_1^+ state at the maximum triaxiality of $\gamma = 30^\circ$. Another model of the triaxial shape is the γ -unstable rotor by Wilets and Jean [3], where PES has a γ -independent valley at a given β . The γ -unstable model predicts degenerate 2_2^+ and 4_1^+ states. A transitional rotor between the γ -vibrational band and the γ -unstable rotor is the γ -soft rotor, of which the PES has a moderate path between prolate and oblate [4].

The neutron-rich Mo isotopes are good candidates to investigate shape evolution in the γ degree of freedom. Calculations using the liquid-drop or the finite-range liquid-drop model using particle number projection or Bardeen-Cooper-Schrieffer methods predict the coexistence of prolate and oblate shapes, a prolate-to-oblate shape transition at $N = 68$ or 70 , and triaxial ground states in ^{104}Mo , ^{106}Mo , and ^{108}Mo [5]. Hartree-Fock-Bogoliubov (HFB) calculations with the D1S-Gogny interaction [6] predict a gradual transition from γ -soft rotor in ^{102}Mo to oblate in ^{112}Mo . A calculation using the global Skyrme energy density functional UNEDF0 predicts triaxial ground-state deformation in $^{106,108}\text{Mo}$ [7]. Calculations of two quasi-particle states are used to investigate quasi-particle configurations near the proton and neutron Fermi surfaces[8].

From the lifetime measurement of the ground-state band in $^{100-108}\text{Mo}$ [9], the quadrupole deformation was indicated to reach a maximum at ^{106}Mo . More precise measurements are awaited to obtain a certain conclusion, since uncertainties of transitional quadrupole moments are larger than a change among isotopes. The measured 2_2^+ -state energy, $E(2_2^+)$, in the neutron-rich Mo isotopes decreases as mass number, A , increases. It becomes almost equal to $E(4_1^+)$ at $A = 108$ and drops below $E(4_1^+)$ at $A \geq 110$ [10–16]. The low-lying 2_2^+ state in the neutron-rich Mo isotopes has been interpreted in terms of the rigid triaxial shape [12], γ vibration [13, 14], and γ -soft rotor [15] based on the measured values of the energies of the 2_1^+ , 4_1^+ , and 2_2^+ states and the γ -decay branching ratio from 2_2^+ state. The interpretation of the 2_2^+ state attracts controversy due to its similarity between the three models, since the γ -vibrational state and γ -soft rotor have a finite root-mean-square value of γ as a result of a dynamic motion.

The energy staggering of the 2_2^+ band is a good signature to distinguish among the three models which describe axial asymmetry [1, 17]. The rigid-triaxial and γ -soft rotors show an energy staggering which deviates from the $J(J+1)$ dependence of the rigid axial rotor.

The staggering of the rigid triaxial rotor is opposite to that of the γ -soft rotor; for example, the 3_γ^+ state is close to the 2_γ^+ and 4_γ^+ states of the rigid triaxial and γ -soft rotors, respectively, where the γ subscript indicates the band member of the 2_2^+ state. On the other hand, the γ -vibrational band with a small γ oscillation has a small or negligible staggering since the shape is close to being axially symmetric.

Another signature of γ vibration is the existence of a two-phonon γ -vibrational band based on the $K = 4^+$ state. The $K = 4^+$ band lying below the pairing gap was identified in the $^{104,106,108}\text{Mo}$ isotopes with an energy ratio $E_{K=4}/E_{K=2} = 1.95, 2.02, \text{ and } 2.42$ for ^{104}Mo , ^{106}Mo , and ^{108}Mo , respectively, which are close to the harmonic-vibrator value of 2 [13, 14].

The second 0^+ state provides additional information on the nuclear shape, since its origin can derive from β vibration or a coexisting shape. The 0_2^+ states in the neutron-rich Mo isotopes are assigned up to $A = 106$ from β decay and (t,p) reaction studies [12, 18–20].

In the present study, the β -delayed γ rays of $^{106,108,110}\text{Mo}$ were observed under lower background conditions and/or with higher statistics than the previous investigations [12, 15, 19, 21]. The lifetimes of the 2_1^+ states were measured using a fast timing array of 18 $\text{LaBr}_3(\text{Ce})$ crystals, of which preliminary results are reported in Ref. [22]. Reliable branching ratios of the 2_2^+ states were determined. The 2_2^+ band in ^{110}Mo was extended from 5^+ to 7^+ . In ^{108}Mo and ^{110}Mo , 0_2^+ states are newly assigned. It is observed that the previous 0_2^+ assignment in ^{106}Mo [12] was incorrect. Values of quadrupole deformation and evidence for triaxial motion have been extracted from these measurements. The results are compared with beyond-mean-field calculations based on the five-dimensional collective Hamiltonian using the constrained HFB (CHFB) + local quasiparticle-random-phase approximation (LQRPA) approach.

II. EXPERIMENT

The experiment was performed at RI Beam Factory (RIBF), operated by RIKEN Nishina Center and CNS, University of Tokyo. The RI beam was produced by the in-flight fission reaction of a 345 MeV/u $^{238}\text{U}^{86+}$ beam impinging on a 3.0-mm thick beryllium target. The RI beam was separated by the BigRIPS fragment separator and transported through the ZeroDegree spectrometer [23, 24]. The particle identification (PID) was performed by determining the mass-to-charge ratio, A/Q , and the atomic number, Z [25].

The RI beam was implanted into the active stopper WAS3ABi (Wide-range Active Silicon Strip Stopper Array for Beta and ion implantation), which comprised five stacked Double-Sided Silicon Strip Detectors (DSSSDs) [26]. The RI hit position of one DSSSD was determined by selecting the fastest timing signal of x and y strips [27]. The implanted layer was determined by de-

TABLE I. The number of $^{106,108,110}\text{Zr}$ and $^{106,108,110}\text{Nb}$ ions implanted in WAS3ABi and their implantation rate.

Isotope	The number of implanted ions	Implantation rate (pps)
^{106}Zr	1.9×10^6	3.5
^{108}Zr	2.1×10^6	3.8
^{110}Zr	3.2×10^4	0.059
^{106}Nb	7.1×10^4	16
^{108}Nb	1.3×10^5	0.24
^{110}Nb	1.9×10^6	3.5

156 tecting the cross-talk signal induced to the DSSSD down-
157 stream of the implanted one [28].

158 The β particles emitted by the decay of the RI were
159 measured by WAS3ABi and two plastic scintillators with
160 2 mm thickness, placed upstream and downstream of
161 WAS3ABi. The timing signal of the plastic scintillator
162 was used for the high-time resolution detection of β par-
163 ticles. The β -particle hit pattern and energy deposition
164 in WAS3ABi and the plastic scintillators were used to
165 restrict position candidates of the β emitter [29]. The β
166 particle was associated with the implanted RI by using
167 the position and time differences between the RI and β
168 particle.

169 WAS3ABi was surrounded by the EUroball-RIKEN
170 Cluster Array (EURICA) [30] to detect γ rays emitted
171 from excited states populated by the β decay of im-
172 planted RIs. The systematic uncertainty of γ -ray en-
173 ergy was evaluated to be 0.15 keV from the residuals of
174 the energy calibration with standard γ -ray sources. The
175 γ -ray detection efficiency of EURICA was measured to
176 be 18.3% at 250 keV and 8.1% at 1 MeV. A system-
177 atic uncertainty of 5% was determined for the absolute
178 value from the uncertainty of the radioactivity of the γ -
179 ray sources. A fast-timing $\text{LaBr}_3(\text{Ce})$ array consisting
180 of eighteen $\phi 1.5'' \times 2''$ crystals was coupled to the EU-
181 RICA array to measure the lifetimes of low-lying excited
182 states in the nanosecond regime [31]. The Full-Width
183 Half Maximum (FWHM) of the time resolution of the
184 $\text{LaBr}_3(\text{Ce})$ array was evaluated to be 0.61 ns at 200 keV.
185 The γ -ray detection efficiency was 3.0(5)% and 0.7(2)%
186 at 250 keV and 1 MeV, respectively.

187 Excited states in $^{106,108,110}\text{Mo}$ populated in the beta
188 decay of $^{106,108,110}\text{Nb}$ were studied. The daughter decays
189 of Zr isotopes were also analyzed to increase statistics
190 and to search for β -decaying isomeric states. The num-
191 ber of implanted Nb and Zr isotopes are summarized in
192 Table I. Daughter-decay analysis provides evidence on
193 the existence of β -decaying isomeric states. For exam-
194 ple, in Ref. [32], the β - γ spectrum of ^{102}Zr was observed
195 through the β decay of ^{102}Y and the β -decay chain of
196 $^{102}\text{Sr} \rightarrow ^{102}\text{Y} \rightarrow ^{102}\text{Zr}$. Two different γ -ray transition pat-
197 terns revealed that ^{102}Y has a β -decaying isomeric state
198 and the β decay of the even-even ^{102}Sr isotope with the

200 spin-parity of 0^+ can only populate the β -decaying low
201 spin state in ^{102}Y . The same method was applied to the
202 $\text{Zr} \rightarrow \text{Nb} \rightarrow \text{Mo}$ β -decay chain in this work. For each β -
203 decay chain, $\text{Zr} \rightarrow \text{Nb} \rightarrow \text{Mo}$ or $\text{Nb} \rightarrow \text{Mo}$, the β -ion time
204 window was optimized to maximize the number of the
205 Nb-decay events and minimize the number of other de-
206 cays.

207 III. RESULTS

208 A. β decay to ^{106}Mo

209 The β -delayed γ -ray spectrum of ^{106}Mo obtained from
210 the β -decay chain $^{106}\text{Zr} \rightarrow ^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$ is shown in
211 Figs. 1 (a–b). The proposed level scheme of ^{106}Mo , illus-
212 trated in Fig. 2, was constructed through the use of γ -ray
213 coincidences, for example Figs. 1 (c–d), energy sums and
214 intensity balances. Nine new levels were identified and
215 a new transition from the 2_2^+ to 4_1^+ states was observed.
216 In the previous β - γ spectroscopic study [12], the ground
217 band was observed up to 6^+ , and the 2_2^+ and 4_3^+ bands
218 up to 4^+ . In the present study, γ rays from the 5^+ states
219 in the 2_2^+ and 4_3^+ bands were observed. These γ rays
220 are consistent with the results obtained from the spon-
221 taneous fission of ^{252}Cf [35–37]. The placement of the
222 784.6-keV and 1106.7-keV γ rays were reassigned from
223 those of Ref. [12] based on the following arguments. The
224 0_2^+ state was previously assigned at 956.6 keV based on
225 the 784.6-keV transition feeding only the 171.4-keV level.
226 However, the high statistics of the present study allowed
227 us to observe additional coincidences with the 784.6-keV
228 transition, which are shown in Fig. 1 (d). Based on this
229 information, the assignment of the 784.6-keV γ ray as the
230 transition between the 5_1^+ and 4_1^+ states is preferred. The
231 observation of the transition from 5_1^+ to 3_1^+ supports this
232 assignment. The previous assignment of the 1106.7-keV
233 γ ray was the transition between a 1279.9-keV state to
234 the 2_1^+ state [12], but it was reassigned to a known tran-
235 sition [34] from the 1816.9-keV state, since a coincidence
236 with 710.2 keV was observed. The half life of ^{106}Nb was
237 determined to be 1.10(5) s from the decay curve of the
238 171.4-keV γ ray for the $^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$ decay as shown in
239 Fig. 3 (a). The obtained half life was consistent with the
240 evaluated value of 1.02(5) s [34].

241 Table II summarizes the relative γ -ray intensity, I_γ ,
242 following the β decay from ^{106}Nb to ^{106}Mo from the two
243 decay chains, $^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$ and $^{106}\text{Zr} \rightarrow ^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$.
244 Since I_γ of the major peaks was consistent between both
245 decay chains, there was no evidence on the existence of a
246 second β -decaying state in ^{106}Nb . The absolute γ -ray in-
247 tensities per 100 β decays were determined from the data
248 of the $^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$ decay for the first time. Here, we
249 used the number of the detected β particles emitted from
250 the ^{106}Nb decay, which was determined from the decay-
251 curve integral of the parent component in the fitting func-
252 tion to the β -particle counts as a function of time. The
253 conversion factor from the relative to absolute γ -ray in-

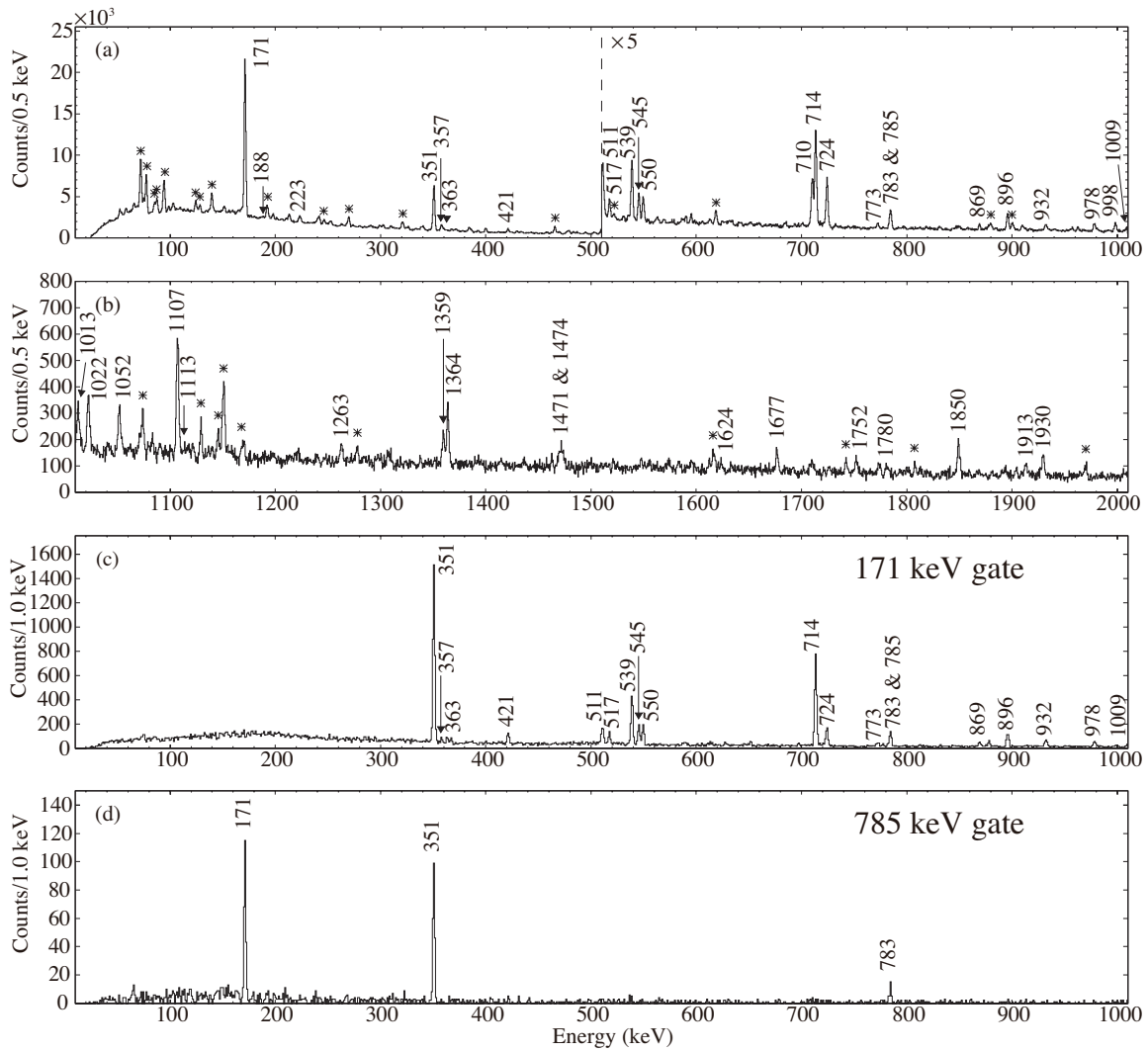


FIG. 1. (a–b) The β -delayed γ -ray spectrum of ^{106}Nb obtained from the β -decay chain $^{106}\text{Zr} \rightarrow ^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$. The range of the time window was set to be $180 \text{ ms} < t_{\text{ion}} - t_{\beta} < 2200 \text{ ms}$. The labeled peaks belong to ^{106}Mo . The identified background peaks are marked with asterisks. Other unknown peaks are mainly associated with parent ^{106}Zr decays. (c–d) The coincidence spectra gated on 171.4 keV and 784.6 keV.

256 tensities was obtained from the absolute intensity of the
 257 largest γ -ray peak at 171.4 keV in the $^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$
 258 decay. The relative systematic uncertainty of the absolute
 259 γ -ray detection efficiency was adopted into the uncer-
 260 tainty of the conversion factor as 0.696(38).

261 The β -decay intensities, I_{β} , to excited states, given in
 262 Table II, were determined by combining results obtained
 263 from the $^{106}\text{Zr} \rightarrow ^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$ and $^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$ decay
 264 chains so as to take into account small β -decay branches.
 265 The decay schemes and I_{γ} values were obtained from
 266 the $^{106}\text{Zr} \rightarrow ^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$ decay chain, which provided
 267 higher statistics. The total I_{β} of all γ -decaying excited
 268 states is given by summing the absolute transition in-
 269 tensities of excited states decaying to the ground state.

270 Two relevant transitions, $2_1^+ \rightarrow 0_1^+$ and $2_2^+ \rightarrow 0_1^+$, were
 271 observed. The sum of the absolute intensities of these two
 272 transitions was 92.2(51)%, which included contributions
 273 of possible undetected transitions, due to low intensities,
 274 through the 2_1^+ or 2_2^+ states. The remaining 7.8(51)%
 275 contribution is the sum of I_{β} to the ground state, and
 276 the β -delayed neutron emission probability, P_n . When a
 277 previously measured P_n of 4.5(3)% [34] is subtracted, the
 278 I_{β} value to the ground state is given as the upper limit
 279 $< 8.4\%$.

280 Table II summarizes the $\log ft$ value of each excited
 281 state calculated using $Q(\beta^-) = 9931(10) \text{ keV}$ from the
 282 atomic mass evaluation (AME2016) [33] and the calcula-
 283 tion tool of Ref. [38]. The $\log ft$ of the 6_1^+ state, 6.6(1),

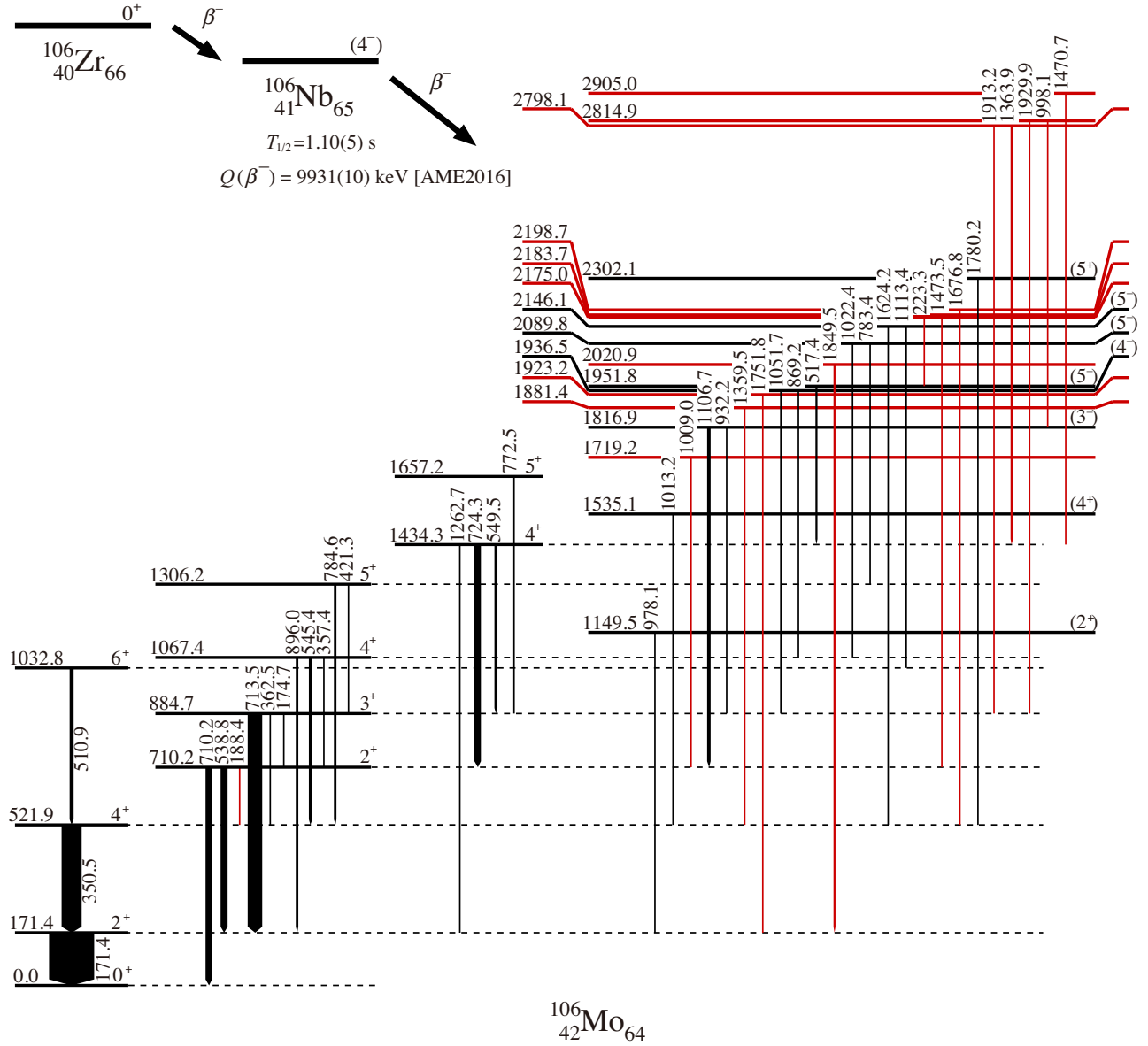


FIG. 2. The proposed level scheme of ^{106}Mo obtained from the β -decay chain $^{106}\text{Zr} \rightarrow ^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$. The $Q(\beta^-)$ of ^{106}Nb is taken from the atomic mass evaluation (AME2016: [33]). The arrow width is proportional to the relative intensity I_γ ($\text{Zr} \rightarrow \text{Mo}$, given in Table II). Red lines are the new levels and transitions. Spin-parities of the known states are taken from ENSDF [34].

TABLE II: The level energy, E_i , spin-parity, J^π , γ -ray energy, E_γ , relative γ -ray intensity, I_γ , β -decay intensity, I_β , and $\log ft$ of the excited states in ^{106}Mo . (Nb \rightarrow Mo) indicates the β decay from the implanted ^{106}Nb to ^{106}Mo . (Zr \rightarrow Mo) indicates the β decay to ^{106}Mo in the decay chain of the implanted ^{106}Zr , i.e. $^{106}\text{Zr} \rightarrow ^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$. (allowed/non-UF) indicates the calculation is for the allowed or non-unique forbidden transitions. (1UF) is for the first unique forbidden transition from 4^- to 2^+ or 6^+ states.

E_i (keV)	J^π	E_γ (keV)	I_γ^a (Nb \rightarrow Mo)	I_γ (Zr \rightarrow Mo)	I_β (%) ^b	$\log ft$ (allowed/non-UF)	$\log ft$ (1UF)
0.0	0^+				< 8.4		
171.4(2)	2^+	171.4(2)	100(2)	100.0(5)	7.3(8)	6.7(1)	9.1(1)
521.9(2)	4^+	350.5(2)	37.9(16)	43.8(5)	9.1(14)	6.5(1)	

TABLE II: (continued)

E_i (keV)	J^π	E_γ (keV)	I_γ^a (Nb→Mo)	I_γ (Zr→Mo)	I_β (%) ^b	log ft (allowed/non-UF)	log ft (1UF)
710.2(1)	2 ⁺	188.4(4)	2.9(7)	0.3(2)	2.8(6)	7.0(1)	9.3(1)
		538.8(2)	16.6(12)	15.6(3)			
		710.2(2)	14.4(15)	15.2(3)			
884.7(2)	3 ⁺	174.7(3)		1.0(4)	8.7(7)	6.5(1)	
		362.5(3)	1.7(7)	0.7(2)			
		713.5(2)	30.1(17)	31.9(4)			
1032.8(3)	6 ⁺	510.9(2)	5.3(12)	8.2(15)	5.5(11)	6.6(1)	8.9(1)
1067.4(1)	4 ⁺	357.4(2)	3.9(8)	2.1(2)	7.9(5)	6.5(1)	
		545.4(2)	5.3(10)	7.6(2)			
		896.0(2)	6.1(10)	6.1(2)			
1149.5(2)	(2 ⁺)	978.1(2)		2.3(2)	1.6(2)	7.1(1)	9.4(1)
1306.2(2)	5 ⁺	421.3(2)	3.1(7)	3.5(2)	5.4(8)	6.6(1)	
		784.6(2)	3.4(8)	5.5(7)			
		1434.3(1)	4 ⁺	549.5(2)			5.1(9)
724.3(2)	11.7(12)	14.0(3)					
1262.7(3)		1.4(2)					
1535.1(3)	(4 ⁺)	1013.2(2)		1.5(3)	1.0(2)	7.2(1)	
1657.2(3)	5 ⁺	772.5(2)		1.4(2)	1.0(1)	7.2(1)	
1719.2(2)		1009.0(2)		1.3(2)	0.9(1)	7.2(1)	
1816.9(2)	(3 ⁻)	932.2(2)	1.3(7)	2.0(2)	4.9(4)	6.5(1)	
		1106.7(2)	4.0(8)	7.4(3)			
		1881.4(3)		2.9(2)			2.0(2)
1923.2(2)		1.6(2)					
1751.8(2)		1.1(2)					
1936.5(2)	(4 ⁻)	869.2(2)		2.0(2)	3.5(3)	6.6(1)	
		1051.7(2)	2.9(2)	3.1(2)			
		1951.8(2)	(5 ⁻)	517.4(2)			6.2(9)
2020.9(2)		1849.5(2)	3.2(14)	4.1(3)			
2089.8(2)	(5 ⁻)	783.4(4)	2.6(11)	1.3(7)	2.9(3)	6.7(1)	
		1022.4(2)		2.5(2)			
2146.1(4)	(5 ⁻)	1113.4(5)		0.3(2)			0.5(2)
		1624.2(4)		0.4(2)			
2175.0(3)		223.3(2)		1.3(2)			
2183.7(4)		1473.5(3)		1.3(2)	0.9(1)	7.1(1)	
2198.7(3)		1676.8(2)		2.2(2)	1.5(2)	6.9(1)	
2302.1(3)	(5 ⁺)	1780.2(3)		1.4(2)	1.0(1)	7.1(1)	
2798.1(2)		1363.9(2)	6.3(9)	5.9(2)	5.2(3)	6.2(1)	
		1913.2(3)		1.5(1)			
		2814.9(2)		998.1(2)			2.3(1)
		1929.9(2)	2.7(2)				
2905.0(3)		1470.7(3)		1.7(2)			

^a The absolute intensity per 100 β -decays is 0.696(38) I_γ .^b Internal conversion coefficients, calculated using the BrIcc code [39], were adopted for three transitions with 171.4, 174.7, and 188.4 keV.

²⁸⁵ indicates an allowed transition with $\Delta J = 0$ or 1 and $\Delta\pi = 0$, or a first non-unique forbidden transition with $\Delta J = 0$ or 1 and $\Delta\pi = 1$ [40]. Three 2⁺ states have similar log ft values ranging from 6.7 to 7.1 which also in-
 ²⁸⁶
²⁸⁷
²⁸⁸
²⁸⁹ dicates allowed or first non-unique forbidden transitions. However, the transitions with $\Delta J \leq 1$ can not populate both the 2⁺ and 6⁺ states. Therefore, transitions with at least $\Delta J = 2$ are required for these states. For the
 ²⁹⁰
²⁹¹
²⁹²

293 unique forbidden transitions, the $\log ft$ values need to
 294 be calculated by taking into account the different energy
 295 dependence of the shape factor from that of the allowed
 296 decay [38, 41]. The $\log ft$ of the 6_1^+ state becomes 8.9(1)
 297 for the first unique forbidden transition with $\Delta J = 2$ and
 298 $\Delta\pi = 1$. This value is consistent with the typical range
 299 from 8 to 11 [40]. This indicates that the spin-parity of
 300 ^{106}Nb is 4^- . This assignment determines the transition
 301 type to other states. Since the β decay to the 2^+ states is
 302 also a first unique forbidden transition, the $\log ft$ values
 303 of the 2^+ states with 171.4, 710.2, and 1149.5 keV were
 304 recalculated as 9.1(1), 8.9(1), and 9.4(1), respectively.
 305 These values are consistent with the typical range of the
 306 first unique forbidden transition. The $\log ft$ values of
 307 the $3^-, 4^-,$ and 5^- states are consistent with the allowed
 308 transition with $\Delta J = 0$ or 1 and $\Delta\pi = 0$, and those of
 309 $3^+, 4^+,$ and 5^+ states are consistent with the first non-
 310 unique forbidden transition with $\Delta J = 0$ or 1 and $\Delta\pi =$
 311 1. Thus, providing further evidence that the spin-parity
 312 of ^{106}Nb is 4^- . The quasi-particle state configuration of
 313 ^{106}Nb is discussed in Sec. IV F.

B. β decay to ^{108}Mo

316 The β -delayed γ -ray spectrum of ^{108}Mo obtained
 317 from the $^{108}\text{Zr} \rightarrow ^{108}\text{Nb} \rightarrow ^{108}\text{Mo}$ decay chain is shown in
 318 Figs. 4 (a–b). The proposed level scheme illustrated
 319 in Fig. 5 was constructed through the use of γ -ray co-
 320 incidences, examples shown in Figs. 4 (c–d), energy
 321 sums, and intensity balances. In the previous β -decay
 322 study [21], the ground band was observed up to 4^+ and
 323 the 2_2^+ band was up to 3^+ . In this work, the 2_2^+ band was
 324 observed up to 4^+ , and the band head of the 4^+ band was
 325 observed at 1422.1 keV. Fifteen new levels were identified,
 326 of which the lowest at 893.4 keV was assigned to 0_2^+
 327 from the typical γ decay pattern of a low-lying 0^+ state,
 328 namely the observed 700.7-keV transition was measured
 329 to be in strong coincidence with the $2_1^+ \rightarrow 0_1^+$ transition,
 330 as shown in Fig. 4 (c), and without an observed γ decay
 331 to the 0_1^+ state. The spin-parity of the 1158.4-keV
 332 state was assigned to be 2^+ , and those of the 1404.8-,
 333 and 1727.6-keV states were to be 3 or 4^+ by assuming
 334 the transition type from those states is E1 or M1/E2.
 335 The half life of the ^{108}Nb decay was determined to be
 336 $T_{1/2} = 186(8)$ ms from the decay curve of the 192.8-keV
 337 γ ray, as shown in Fig. 3 (b), and is consistent with the
 338 evaluated value of 198(6) ms [34].

341 The I_γ values were determined for the two decay
 342 chains, $^{108}\text{Nb} \rightarrow ^{108}\text{Mo}$ and $^{108}\text{Zr} \rightarrow ^{108}\text{Nb} \rightarrow ^{108}\text{Mo}$, as
 343 summarized in Table III. The consistent I_γ values be-
 344 tween two decay chains indicate no β -decaying isomeric
 345 state in ^{108}Nb . The conversion factor from the relative
 346 to absolute γ -ray intensities was determined from the ab-
 347 solute 192.8-keV intensity in the $^{108}\text{Nb} \rightarrow ^{108}\text{Mo}$ decay.

348 The I_β values were determined from the absolute inten-
 349 sities and the decay scheme. As described in Sec. III A,
 350 the total I_β of the γ -decaying excited states in ^{108}Mo

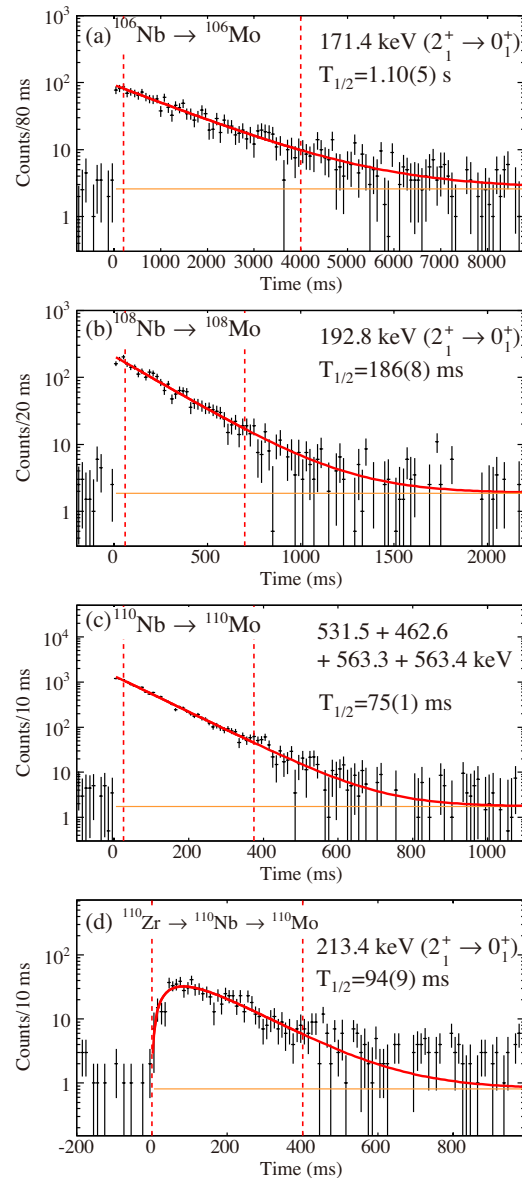


FIG. 3. The time spectra of β -delayed γ rays in the Mo isotopes. Dashed lines indicate the fitting region of the decay curve to determine the β -decay half life, $T_{1/2}$. Orange lines are the constant background, which was determined by fitting to the negative-time region. The β -delayed γ rays with 531.5, 462.6, 563.3, and 563.4 keV from the implanted ^{110}Nb were selected as the β decays of the high-spin state in ^{110}Nb .

351 was determined to be 62.8(33)% from the sum of abso-
 352 lute transition intensities of three transitions from the 2_1^+ ,
 353 2_2^+ , and 2_3^+ states to the ground state. The zero-neutron
 354 emission probability of the ^{108}Nb decay, P_{0n} , which is the
 355 probability decaying to ^{108}Mo without a delayed-neutron
 356 emission, was determined by using a new method de-
 357 scribed in Sec. III C as, $P_{0n} = 82(11)\%$. The difference
 358 of these two values gave the ground-state I_β of 19(12)%.

359 The I_γ values obtained in this work are inconsistent
 360 with the previous results [21] with the exception of the

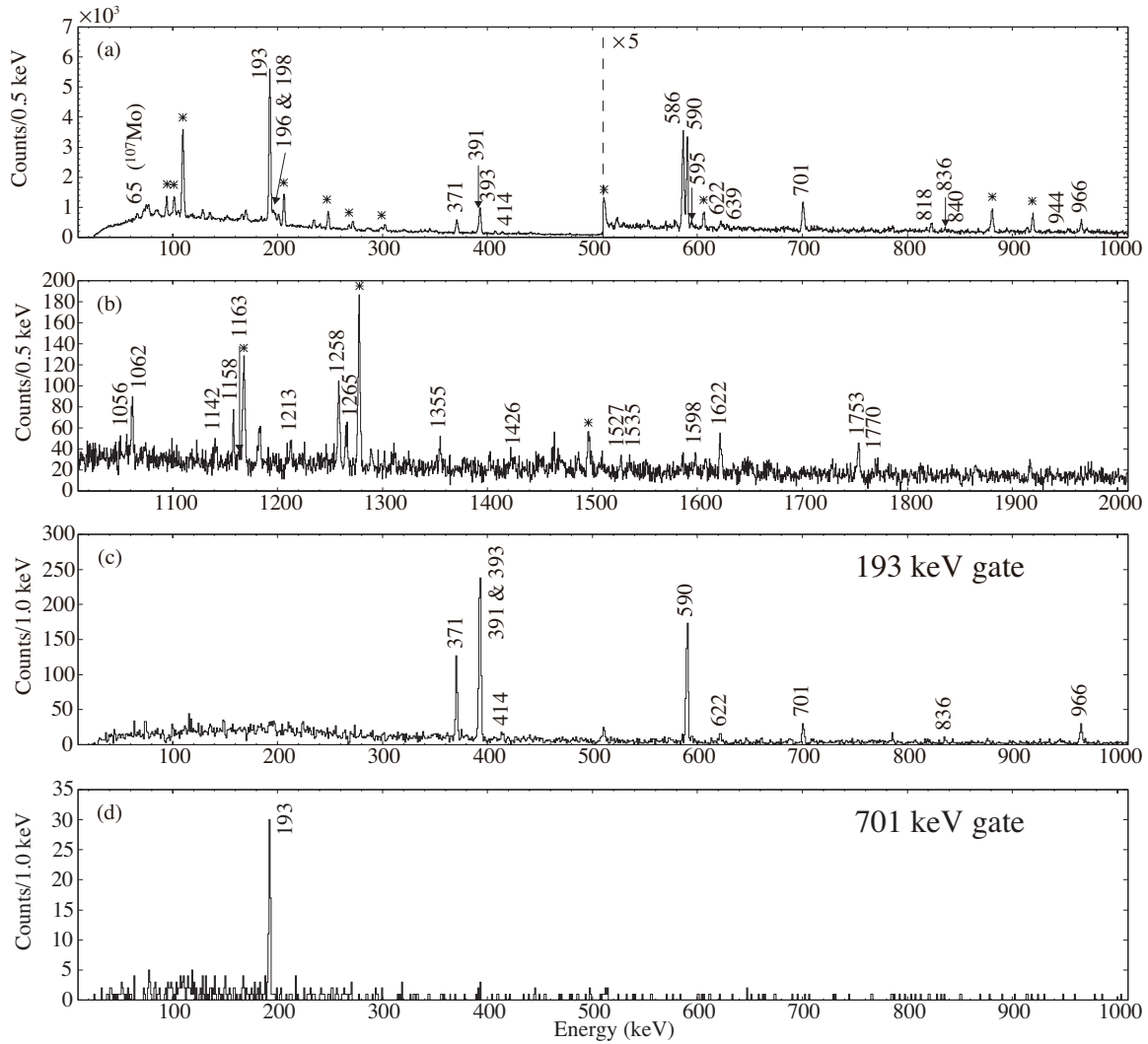


FIG. 4. (a–b) The β -delayed γ -ray spectrum of ^{108}Nb obtained from the β -decay chain $^{108}\text{Zr} \rightarrow ^{108}\text{Nb} \rightarrow ^{108}\text{Mo}$. The range of the time window was set to be $80 \text{ ms} < t_{\text{ion}} - t_{\beta} < 280 \text{ ms}$. The labeled peaks belong to ^{108}Mo . The identified background peaks are marked with asterisks. Other unknown peaks are mainly associated with parent ^{108}Zr decays. (c–d) The coincidence spectra gated on 192.8 keV and 700.7 keV.

361 371.1- and 393.1-keV γ rays. Notably the $I_{\gamma}(590.1 \text{ keV})$
 362 of 26.1(6)% was roughly half of that reported in Ref. [21],
 363 53%. As mentioned in Ref. [21], a large background in
 364 their γ -ray spectrum might be the cause of the inconsis-
 365 tency. The absolute intensity of the $2_1^+ \rightarrow 0_1^+$ transition
 366 was also roughly half of that reported in Ref. [21]. This
 367 may be due to a 50% uncertainty of the ^{108}Nb yield ex-
 368 trapolated as a function of the atomic number [21]. Al-
 369 though the uncertainty of the previous I_{β} was not eval-
 370 uated, the present $I_{\beta}(3_1^+)$ of 5.1(6)% is 1/10 of the re-
 371 ported 53% [21] owing to yield uncertainties and the pre-
 372 vious non-observation of the cascade transitions to the
 373 3_1^+ state.

374 The $\log ft$ values were determined from $T_{1/2}$, I_{β} , and
 375 $Q_{\beta} = 11210(12) \text{ keV}$ [33]. The $\log ft$ values of the 0_1^+

376 and 4_1^+ states were 5.8(3) and 6.4(1) and are too small
 377 for any transitions with $\Delta J \geq 2$ [40]. This is the same
 378 situation as for the ^{106}Nb decay. If the first unique for-
 379 bidden transition with $\Delta J = 2$ and $\Delta\pi = 1$ is considered
 380 for the transitions to these states, the spin-parity of the
 381 ^{108}Nb ground state is 2^- . The $\log ft$ values of the 0^+
 382 and 4^+ states were recalculated as the first unique for-
 383 bidden transition to be 8.2(3), 8.8(1), 8.7(1), 8.5(1), and
 384 9.2(1) for the ground state and the excited states at 563.8
 385 keV, 893.4 keV, 978.3 keV, and 1422.1 keV, respectively.
 386 These are within the typical range from 8 to 11 [40]. The
 387 $\log ft$ values of the 2^+ , 3^+ , and 3^- states indicate the
 388 allowed transition or the first non-unique forbidden tran-
 389 sition, and are consistent with the β decay from a 2^-
 state. The β decay to the 5^- state at 2161.8 keV is the

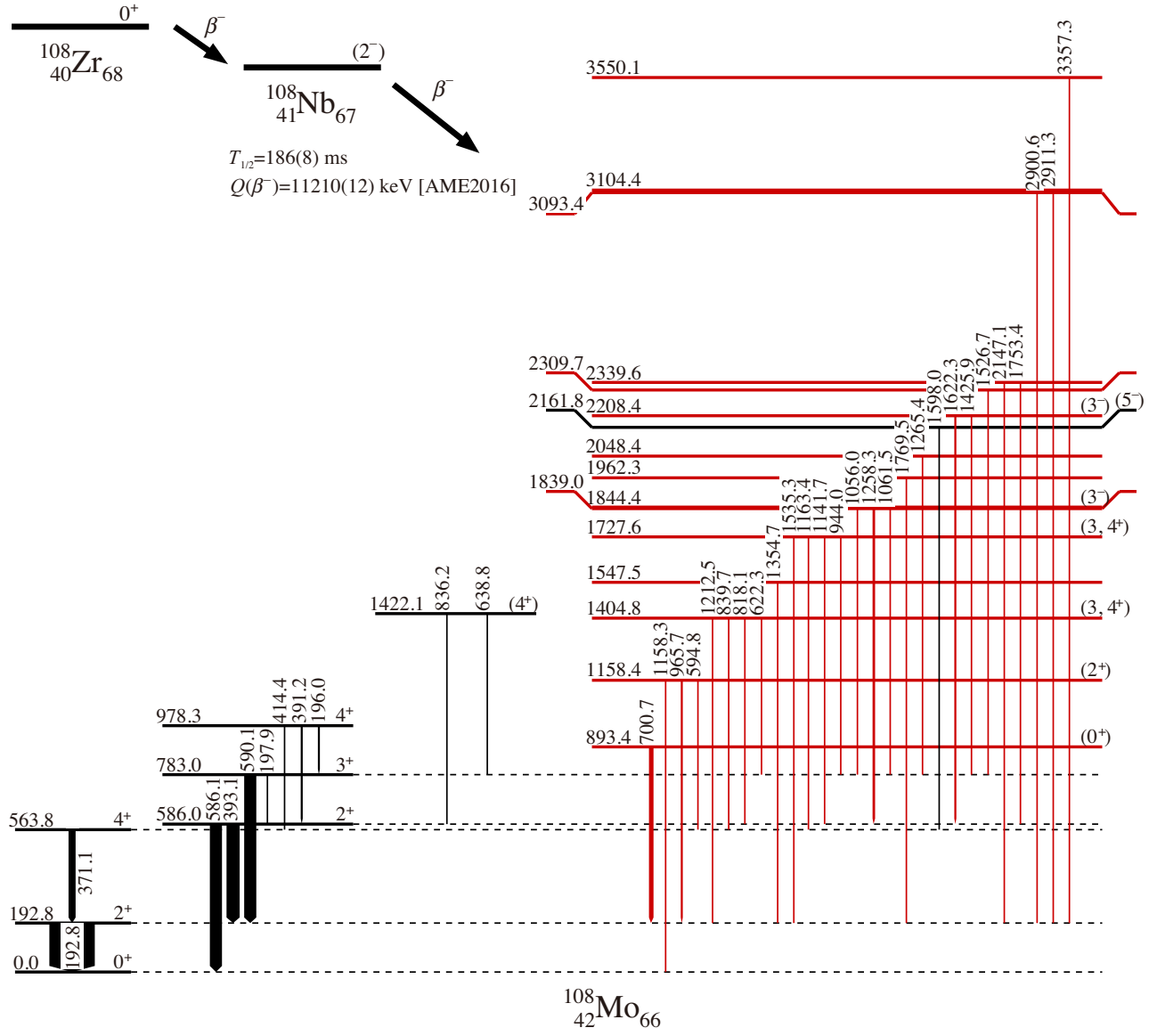


FIG. 5. The proposed level scheme of ^{108}Mo obtained from the β -decay chain $^{108}\text{Zr} \rightarrow ^{108}\text{Nb} \rightarrow ^{108}\text{Mo}$. Red lines are the new levels and transitions.

TABLE III: Same as Table II, but for ^{108}Mo . (1UF) is for the first unique forbidden transition from 2^- to 0^+ or 4^+ states. (2UF) is for the second unique forbidden transition from 2^- to 5^- states.

E_i (keV)	J^π	E_γ (keV)	I_γ^a (Nb \rightarrow Mo)	I_γ (Zr \rightarrow Mo)	I_β (%) ^b	logft (allowed/non-UF)	logft (1UF)	logft (2UF)
0.0	0^+				19(12)	5.8(3)	8.2(3)	
192.8(2)	2^+	192.8(2)	100(2)	100.0(9)	6.7(10)	6.2(1)		
563.8(2)	4^+	371.1(2)	18.2(10)	14.5(5)	3.7(6)	6.4(1)	8.8(1)	
586.0(1)	2^+	393.1(2)	28.3(13)	27.8(10)	13.2(12)	5.8(1)		
		586.1(2)	25.0(12)	26.4(7)				
783.0(2)	3^+	197.9(6)		3.4(1)	5.1(6)	6.2(1)		
		590.1(2)	27.4(12)	26.1(6)				
893.4(2)	(0^+)	700.7(2)	4.7(16)	9.7(5)	4.3(3)	6.3(1)	8.7(1)	

TABLE III: (continued)

E_i (keV)	J^π	E_γ (keV)	I_γ^a (Nb→Mo)	I_γ (Zr→Mo)	I_β (%) ^b	log ft (allowed/non-UF)	log ft (1UF)	log ft (2UF)
978.3(2)	4 ⁺	196.0(2)		5.0(1)	5.4(7)	6.1(1)	8.5(1)	
		391.2(3)	7.0(9)	4.5(14)				
		414.4(3)	2.1(5)	2.3(6)				
1158.4(1)	(2 ⁺)	594.8(3)	1.2(5)	1.5(4)	3.8(4)	6.3(1)		
		965.7(2)	4.2(7)	4.4(4)				
		1158.3(2)	3.2(6)	2.5(4)				
1404.8(2)	(3, 4 ⁺)	622.3(3)		1.7(4)	2.1(3)	6.5(1)		
		818.1(4)		0.8(3)				
		839.7(3)		0.7(3)				
		1212.5(3)		1.4(4)				
1422.1(2)	(4 ⁺)	638.8(4)	0.6(1)	0.5(3)	0.9(2)	6.8(1)	9.2(1)	
		836.2(3)		1.4(3)				
1547.5(3)		1354.7(2)		2.1(4)	0.9(2)	6.8(1)		
1727.6(2)	(3, 4 ⁺)	944.0(5)		0.4(3)	1.5(3)	6.5(1)		
		1141.7(3)		1.4(3)				
		1163.4(6)		0.5(5)				
		1535.3(4)		1.1(3)				
1839.0(5)		1056.0(4)		0.8(3)	0.4(1)	7.1(1)		
1844.4(2)	(3 ⁻)	1061.5(2)	2.2(1)	3.6(4)	4.1(4)	6.1(1)		
		1258.3(2)	7.5(6)	5.6(5)				
1962.3(2)		1769.5(2)		0.8(1)	0.4(1)	7.1(1)		
2048.4(3)		1265.4(2)	3.3(5)	3.1(4)	1.4(2)	6.5(1)		
2161.8(4)	(5 ⁻)	1598.0(3)		1.2(5)	0.5(2)	6.9(2)		11.6(2)
2208.4(2)	(3 ⁻)	1425.9(7)		1.1(3)	2.4(3)	6.2(1)		
		1622.3(2)		4.2(4)				
2309.7(3)		1526.7(3)		1.8(3)	0.8(1)	6.7(1)		
2339.6(2)		1753.4(3)		3.3(5)	2.8(3)	6.1(1)		
		2147.1(3)		3.0(4)				
3093.4(5)		2900.6(4)		1.6(4)	0.7(2)	6.6(1)		
3104.1(4)		2911.3(3)		2.3(5)	1.0(2)	6.4(1)		
3550.1(5)		3357.3(4)		1.6(6)	0.7(3)	6.4(2)		

^a The absolute intensity per 100 β -decays is $0.448(23)I_\gamma$.

^b Internal conversion coefficients, calculated using the BrIcc code [39], were adopted for three transitions with 192.8, 196.0, and 197.9 keV.

second unique forbidden transition with $\Delta J = 3$ and $\Delta\pi = 0$. The log ft value of the 5⁻ state was recalculated to be 11.6(2) and within the typical range from 10.6 to 18 for the second unique forbidden transition [40]. Therefore, the spin-parity of the ¹⁰⁸Nb was assigned to be 2⁻. The quasi-particle state configuration of ¹⁰⁸Nb is described in Sec. IV F.

C. Neutron-emission probability in ¹⁰⁸Nb β decay

The zero-neutron emission probability, P_{0n} , of the ¹⁰⁸Nb decay is given by the ratio $N_\beta(^{108}\text{Mo})/N_\beta(^{108}\text{Nb})$, where $N_\beta(^{108}\text{Mo})$ and $N_\beta(^{108}\text{Nb})$ are the integral of mea-

sured ¹⁰⁸Mo and ¹⁰⁸Nb decays after the ¹⁰⁸Nb implantation, respectively. The neutron emission probability P_n is given by

$$P_n = 1 - P_{0n} = \sum_{i \geq 1} P_{in}, \quad (1)$$

where i is the number of the emitted neutrons.

$N_\beta(^{108}\text{Nb})$ was determined to be $5.20(13) \times 10^4$ from a fit to the β -decay time curve obtained following the implantation of ¹⁰⁸Nb. The fit used the decay half-lives and neutron-emission probabilities of the parent ¹⁰⁸Nb, daughters ^{107,108}Mo, granddaughters ^{106,107,108}Tc and great granddaughters ^{107,108}Ru from the literature [34] except for ¹⁰⁸Nb where the half-life of 186(8) ms mea-

413 sured in this work was used. It was assumed that the 464
414 probability of the emission of two or more neutrons is
415 negligibly small so that $P_{1n} = 1 - P_{0n}$.

416 $N_\beta(^{108}\text{Mo})$ can be derived from the number of counts
417 of the 268.3-keV γ ray, $N_\gamma(268.3 \text{ keV})$, emitted from the
418 $^{108}\text{Mo} \rightarrow ^{108}\text{Tc}$ decay using the relation,

$$N_\gamma(268.3 \text{ keV}) = N_\beta(^{108}\text{Mo})\varepsilon_\gamma(268.3 \text{ keV}) \times I_{\gamma,\text{abs}}(268.3 \text{ keV}), \quad (2)$$

419 where $\varepsilon_\gamma(268.3 \text{ keV})$ is the γ -ray detection efficiency,
420 which is sensitive to the implantation position, and
421 $I_{\gamma,\text{abs}}(268.3 \text{ keV})$ is the absolute intensity of 268.3 keV
422 per one ^{108}Mo decay. In order to evaluate $N_\beta(^{108}\text{Mo})$,
423 we define the ratio,

$$R(268.3 \text{ keV}) = \frac{N_\gamma(268.3 \text{ keV})}{N_\beta(^{108}\text{Mo})}, \quad (3)$$

424 which should be the same for the $^{108}\text{Nb} \rightarrow ^{108}\text{Mo} \rightarrow$
425 ^{108}Tc and $^{108}\text{Mo} \rightarrow ^{108}\text{Tc}$ decays, if the position of
426 the ^{108}Nb and ^{108}Mo parent in WAS3ABi is the same.
427 To satisfy this requirement, we consider only events
428 where the implanted ion is ^{108}Nb . To obtain a value of
429 $R(268.3 \text{ keV})$ from the $^{108}\text{Mo} \rightarrow ^{108}\text{Tc}$ decay, we use the
430 detection time of the 192.8-keV γ ray emitted from the
431 2_1^+ state in ^{108}Mo as a time-zero of the decay of ^{108}Mo .
432 $N_\beta(^{108}\text{Mo})$ was then obtained from the β -decay time
433 curve using the same method as described for ^{108}Nb . The
434 number of ^{108}Tc 268.3-keV γ rays was obtained from the
435 γ -ray peak integral to give $R(268.3 \text{ keV}) = 0.0558(65)$.

436 To obtain a value of $N_\gamma(268.3 \text{ keV})$ for the $^{108}\text{Nb} \rightarrow$
437 $^{108}\text{Mo} \rightarrow ^{108}\text{Tc}$ decay, a time gate of 400–3000 ms after
438 the ^{108}Nb implantation in WAS3ABi was applied
439 to optimize the γ rays emitted from the ^{108}Mo decay.
440 This yielded a 268.3-keV peak containing 1695(43)
441 counts. The expected number of 268.3-keV γ rays observed
442 without time restriction is evaluated as $N_\gamma(268.3 \text{ keV}) =$
443 $2380(140)$, which, using Eq. (3), equates to
444 $N_\beta(^{108}\text{Mo}) = 42700(5600)$.

445 By using the relation, $P_{0n} = \frac{N_\beta(^{108}\text{Mo})}{N_\beta(^{108}\text{Nb})}$, we obtain
446 $P_{0n} = 82(11)\%$, giving $P_n = 18(11)\%$. Observation of
447 the known 65.4-keV γ ray [42] from the isomeric state
448 in ^{107}Mo in Fig. 4 (a) provides a direct evidence of the
449 β -delayed neutron emission of ^{108}Nb . The absolute γ -ray
450 intensity of the 65.4-keV γ ray corresponds to a minimum
451 P_{1n} of 8.1(7)%, which includes the contribution of the internal
452 conversion for the E2 transition. It is reasonable
453 that this is less than $P_n = 18(11)\%$, given above, as there
454 exist unobserved one- or multi-neutron emission channels.
455 The minimum value reported here is larger than a
456 previously reported P_n value of 6.2(5)% [43] and equal
457 to 8(2)% of Ref. [44]. The previous P_n values were derived
458 from measurements of β -delayed neutrons with ^3He
459 ionization chamber tubes [43], or a combination of ^3He
460 and B_3F proportional gas-counter tubes [44]. Neutron-
461 detection efficiencies of these configurations, which have
462 a possible energy dependence, could have been affected
463 by unknown β -delayed neutron energy distributions.

D. β decay to ^{110}Mo

465 The β -delayed γ -ray spectrum of ^{110}Mo obtained from
466 the β decay of ^{110}Nb is shown in Figs. 6 (a–b), and
467 the coincidence spectrum of the $2_1^+ \rightarrow 0_1^+$ transition is
468 shown in Fig. 6 (c). The proposed level scheme is shown
469 in Fig. 7. In the previous works of the ^{110}Nb β decay and
470 the ^{248}Cm spontaneous fission decay [15, 45], the ground
471 band up to 10^+ and the 2_2^+ band up to 5^+ were reported.
472 In the present work, thirty new levels are identified and
473 the 2_2^+ band is extended up to its 7^+ state. A new band
474 based on a 1243.8-keV state was observed and from its
475 interband transitions to the 2_2^+ band, a spin-parity of 4^+
476 was assigned to its band head. The spin-parities of the
477 band members with 1520.1 keV and 1796.2 keV were assigned
478 as 5^+ and 6^+ , respectively. A state at 1042.2 keV
479 was measured based on the observation of a 828.8-keV γ
480 ray coincident only with the 213.4-keV γ ray, as shown in
481 Fig. 6 (d). Direct γ decay from the 1042.2-keV state to
482 the ground state was not observed. Based on this typical
483 γ -decay pattern of a low-lying 0^+ state, the 1042.2-keV
484 state was assigned to 0^+ . The I_γ values are summarized
485 in Table IV.

486 The β -delayed γ -ray spectrum of ^{110}Mo obtained from
487 the $^{110}\text{Zr} \rightarrow ^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$ decay chain is shown in
488 Fig. 6 (e). Only five excited states were observed, which
489 were the 2^+ and 4^+ states in the ground band, the 2^+
490 and 3^+ states in the 2_2^+ band, and the 0_2^+ state. This
491 β -decay feeding pattern and the I_γ values, given in Table
492 V, are different from those of the $^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$
493 decay. These differences indicate the existence of two β -
494 decaying states in ^{110}Nb . Since the spin-parity of the
495 even-even nucleus ^{110}Zr is 0^+ , it is expected that the
496 low-spin states in ^{110}Nb are populated by the β decay of
497 ^{110}Zr . This expectation is consistent with the β -decay
498 feeding pattern to the lower-spin states in ^{110}Mo by the
499 $^{110}\text{Zr} \rightarrow ^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$ decay chain. On the other hand,
500 the $^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$ decay has contributions of the low-
501 and high-spin states in ^{110}Nb because the in-flight fission
502 reaction populates both states.

E. Extraction of β -decay properties for low- and high-spin states in ^{110}Nb

503 Beta-decay properties, namely $T_{1/2}$, relative and absolute
504 γ -ray intensities, I_β , and $\log ft$, need to be determined
505 separately for the low- and high-spin states in ^{110}Nb . To
506 evaluate $T_{1/2}$ for the high-spin state, the γ rays with
507 462.6, 531.5, 563.3, and 563.4 keV from the 5_1^+ , 6_1^+ , or
508 6_2^+ states were used as they are emitted only in the β
509 decay of the high-spin state. The half-life of the high-spin
510 state in ^{110}Nb was determined to be 75(1) ms from the sum
511 of the decay curves of these four γ rays using the data of
512 the $^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$ decay as shown in Fig. 3 (c). The
513 213.4-keV γ ray obtained in the $^{110}\text{Zr} \rightarrow ^{110}\text{Nb} \rightarrow$
514 ^{110}Mo decay chain was used for the half-life measurement
515 of the low-spin state in ^{110}Nb . The decay

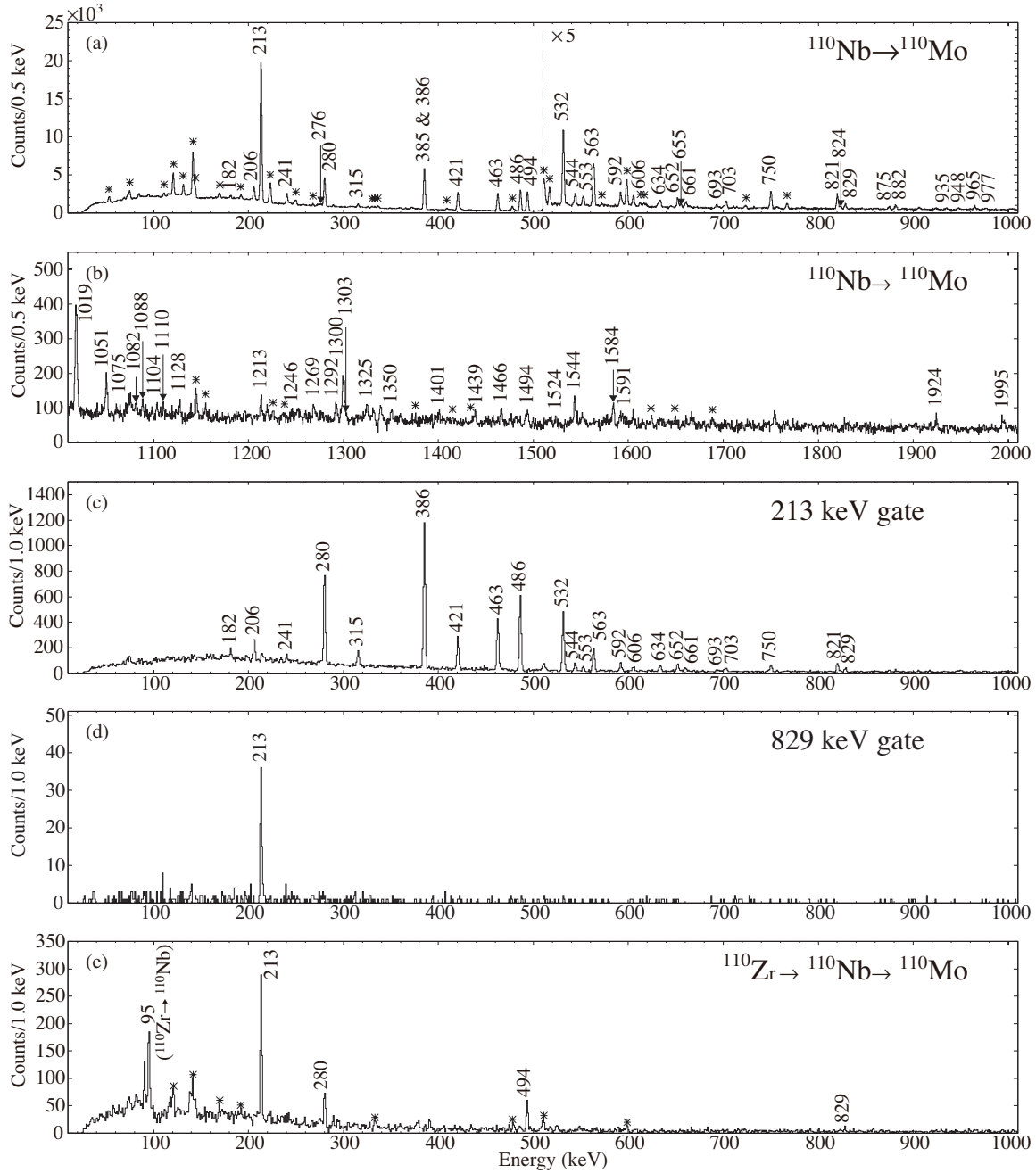


FIG. 6. (a–b) The β -delayed γ -ray spectrum of the implanted ^{110}Nb . The time window after the implantation of ^{110}Nb was set to be less than 400 ms. The labeled peaks belong to ^{110}Mo . The identified background peaks are marked with asterisks. (c–d) The coincidence spectra gated on 213.4 keV and 828.8 keV. (e) The β -delayed γ -ray spectrum obtained from the β -decay chain $^{110}\text{Zr} \rightarrow ^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$, where $\Delta t_{\beta\text{-ion}}$ from 30 to 250 ms was selected.

520 curve shown in Fig. 3 (d) shows the typical shape of a
 521 daughter populated by the decay of a parent. The half-
 522 life of the low-spin state in ^{110}Nb was determined to be
 523 94(9) ms by considering the daughter-decay component
 524 and the constant background. The half-life of ^{110}Zr , used
 525 in the fitting, was determined to be 37.7(31) ms from the
 526 decay curve of the 90.5- and 95-keV γ rays associated
 527 with the ^{110}Zr decay. The half life of previous measure-

528 ments was determined without any consideration of the
 529 second β -decaying state in ^{110}Nb . The previous values
 530 of 82(4) ms [34] and 82(2) ms [46] appear to be a reason-
 531 able average of the presently reported low- and high-spin
 532 states.

533 The absolute γ -ray intensities for the low-spin state in
 534 ^{110}Nb were determined as follows. The β decay of ^{110}Nb
 which followed the emission of a 95-keV γ ray from the

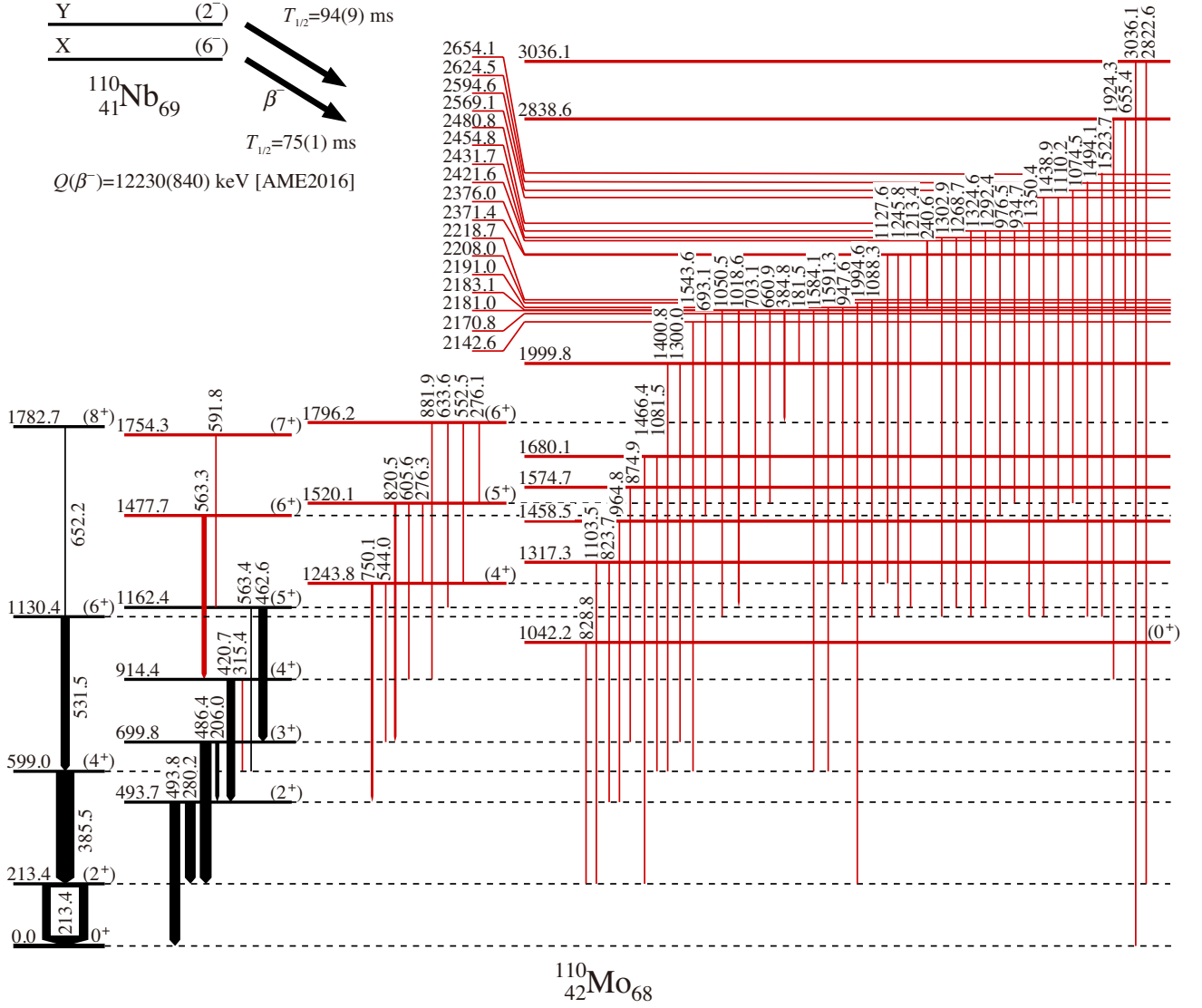


FIG. 7. The proposed level scheme of ^{110}Mo obtained from the β -decay of ^{110}Nb isotopes implanted into WAS3ABi. Red lines are the new levels and transitions.

TABLE IV: Same as Table II, but for the ^{110}Mo results obtained from the β decay of the implanted ^{110}Nb . (high) indicates the β decay of the high-spin state in ^{110}Nb . The low-spin contribution was subtracted by combining with the results in Table V and the assumption that the 0⁺ states at 0 and 1042.2 keV are populated only from the low-spin β decay. (1UF) is for the first unique forbidden transition from 6⁻ to 4⁺ or 8⁺ states.

E_i (keV)	J^π	E_γ (keV)	I_γ^a (Nb→Mo)	I_γ^b (high)	$I_\beta(\%)^c$ (high)	logft (high) (allowed/non-UF)	logft (high) (1UF)
0.0	0 ⁺				0		
213.4(2)	(2 ⁺)	213.4(2)	100.0(5)	100(11)	<1.5		
493.7(1)	(2 ⁺)	280.2(2)	23.5(4)	21.6(33)	-5.4(45)		
		493.8(2)	23.1(3)	18.9(38)			
599.0(2)	(4 ⁺)	385.5(2)	39.0(7)	52.7(14)	6.2(16)	5.9(2)	8.5(3)
699.8(1)	(3 ⁺)	206.0(2)	8.5(2)	11.3(3) ^e	1.5(6)	6.5(2)	
		486.4(2)	26.2(3)	34.9(8)			

TABLE IV: (continued)

E_i (keV)	J^π	E_γ (keV)	I_γ^a (Nb→Mo)	I_γ^b (high)	$I_\beta(\%)^c$ (high)	log ft (high) (allowed/non-UF)	log ft (high) (1UF)
914.4(2)	(4 ⁺)	420.7(2)	18.8(3)	27.0(4)	4.8(15)	6.0(2)	8.5(3)
		315.4(2)	2.9(2)	4.2(3)			
1042.2(2)	(0 ⁺)	828.8(2)	1.8(1)	0	0		
1130.4(3)	(6 ⁺)	531.5(2)	19.7(3)	28.3(4)	8.2(20)	5.7(2)	
1162.4(2)	(5 ⁺)	462.6(2)	19.7(3)	28.3(4)	6.5(17)	5.8(2)	
		563.4(3)	1.8(4)	2.6(6)			
1243.8(1)	(4 ⁺)	544.0(2)	2.9(2)	4.2(3)	3.5(9)	6.1(2)	8.5(3)
		750.1(2)	5.9(2)	8.5(3)			
1317.3(2)		823.7(2)	1.3(1)	1.9(1)	1.4(3)	6.5(2)	
		1103.5(3)	0.5(1)	0.7(1)			
1458.5(2)		964.8(2)	1.1(1)	1.6(1)	0.5(2)	6.9(2)	
1477.7(2)	(6 ⁺)	563.3(2)	10.0(10)	14.4(14)	4.8(14)	5.9(2)	
1520.1(2)	(5 ⁺)	276.3(3)	0.3(4)	0.4(6)	3.8(11)	6.0(2)	
		605.6(2)	2.9(2)	4.2(3)			
		820.5(2)	4.9(2)	7.0(3)			
1574.7(3)		874.9(3)	0.9(1)	1.3(1)	0.7(2)	6.7(2)	
1680.1(2)		1081.5(3)	0.4(1)	0.6(1)	0.9(2)	6.6(2)	
		1466.4(3)	0.8(1)	1.2(1)			
1754.3(3)	(7 ⁺)	591.8(2)	3.3(3)	4.7(4)	2.5(7)	6.1(2)	
1782.7(3)	(8 ⁺)	652.2(2)	2.8(2)	4.0(3)	2.2(5)	6.2(2)	8.6(3)
1796.2(1)	(6 ⁺)	276.1(3)	0.8(4)	1.2(6)	1.7(7)	6.3(2)	
		552.5(2)	2.7(2)	3.9(3)			
		633.6(2)	2.1(2)	3.0(3)			
		881.9(2)	1.6(1)	2.3(1)			
		1300.0(2)	2.3(2)	3.3(3)	0.5(3)		6.8(3)
1999.8(2)		1400.8(4)	0.3(1)	0.4(1)			
		1543.6(2)	1.6(2)	2.3(3)	1.2(3)	6.4(2)	
2142.6(3)		693.1(2)	0.9(1)	1.3(1)	0.7(2)	6.6(2)	
2170.8(3)		181.5(2)	1.9(2)	2.7(3)	10.1(25)	5.4(2)	
2181.0(1)		384.8(2)	5.0(6)	7.2(9)			
		660.9(2)	1.4(1)	2.0(1)			
		703.1(2)	2.4(1)	3.5(1)			
		1018.6(2)	5.0(2)	7.2(3)			
		1050.5(2)	1.6(1)	2.3(1)			
2183.1(3)		1584.1(2)	1.4(2)	2.0(3)	0.4(2)	6.8(3)	
2191.0(3)		947.6(3)	0.6(1)	0.9(1)	1.0(3)	6.4(2)	
		1591.3(4)	0.7(2)	1.0(3)			
2208.0(4)		1994.6(3)	0.8(1)	1.2(1)	0.6(2)	6.6(2)	
2218.7(4)		1088.3(3)	0.5(1)	0.7(1)	0.4(1)	6.8(2)	
2371.4(4)		1127.6(3)	0.6(1)	0.9(1)	0.5(1)	6.7(2)	
2376.0(3)		1213.4(3)	0.9(1)	1.3(1)	0.9(2)	6.4(2)	
		1245.8(3)	0.3(1)	0.5(1)			
2421.6(2)		240.6(2)	4.2(7)	6.0(10)	3.2(9)	5.9(2)	
2431.7(3)		1268.7(3)	0.7(1)	1.0(1)	0.8(2)	6.5(2)	
		1302.9(6)	0.4(1)	0.6(1)			
2454.8(2)		934.7(3)	0.5(1)	0.7(1)	2.0(5)	6.1(2)	

TABLE IV: (continued)

E_i (keV)	J^π	E_γ (keV)	I_γ^a (Nb→Mo)	I_γ^b (high)	$I_\beta(\%)^c$ (high)	log ft (high) (allowed/non-UF)	log ft (high) (1UF)
		976.5(3)	0.4(1)	0.6(1)			
		1292.4(2)	1.0(1)	1.4(1)			
		1324.6(3)	0.7(1)	1.0(1)			
2480.8(4)		1350.4(3)	0.7(1)	1.1(1)	0.5(2)	6.7(3)	
2569.1(3)		1110.2(3)	0.4(1)	0.6(1)	0.8(2)	6.5(2)	
		1438.9(3)	0.6(1)	0.9(1)			
2594.6(5)		1074.5(5)	0.4(1)	0.6(1)	0.3(1)	6.9(2)	
2624.5(4)		1494.1(3)	0.9(3)	1.3(4)	0.7(3)	6.5(3)	
2654.1(4)		1523.7(3)	0.6(1)	0.9(1)	0.5(1)	6.6(2)	
2838.6(2)		655.4(2)	0.9(1)	1.3(1)	1.4(4)	6.2(2)	
		1924.3(3)	0.9(2)	1.3(3)			
3036.1(2)		2822.6(3)	1.1(1)	1.6(1)	2.1(5)	5.9(2)	
		3036.1(3)	1.6(2)	2.3(3)			

^a The absolute intensity per 100 β -decays is $0.492(25)I_\gamma$.

^b The absolute intensity per 100 β -decays is $0.54(19)I_\gamma$.

^c Internal conversion coefficients [39] were adopted for two transitions with 213.4 and 206.0 keV.

^e Branching ratio of the 206.0- and 486.4-keV transitions and I_γ (486.4 keV) in Table V were used to subtract the low-spin β decay contribution.

536 decay of ^{110}Zr was analyzed using the observation of the
537 95-keV γ ray as time zero. The observation of the 213.4-
538 , 280.2-, and 493.8-keV γ rays shows that the low-spin
539 state in ^{110}Nb is selected by the gate on the 95-keV γ ray.
540 The ratio of the number of the measured β decays and
541 213.4-keV γ rays was determined from this subsequent β -
542 decay analysis. The conversion factor from I_γ to absolute
543 intensity was determined to be $0.41(14)$ using the 213.4-
544 keV γ ray.

545 The I_γ values corresponding to the high-spin state
546 were determined by subtracting the low-spin contribu-
547 tion from the results given in Table V under the assump-
548 tion that the ground and second 0^+ states are directly
549 populated only by the low-spin β decay. The I_β values
550 for low- and high-spin β decays were determined and are
551 summarized in Tables IV and V.

552 The I_β value of the ^{110}Mo ground state corresponding
553 to the low-spin state and P_n values corresponding to the
554 low- and high-spin states were determined by combining
555 the following five equations. First, the P_n value has a
556 relation to $I_\beta(E_i)$ for the γ -decaying states at the energy
557 E_i and $I_\beta(0)$ for the ground state as,

$$\sum I_\beta^L(E_i) + I_\beta^L(0) + P_n^L = 100\%, \quad (4)$$

$$\sum I_\beta^H(E_i) + P_n^H = 100\%, \quad (5)$$

558 where \sum represents the sum over all excited states de-
559 caying to the ground state and the superscripts L and H
560 represent the low- and high-spin states in ^{110}Nb , respec-
561 tively. The $\sum I_\beta^L(E_i)$ value was evaluated as $58(20)\%$
562 by the sum of the two absolute transition intensities of

563 213.4 and 493.8 keV, which decay directly to the ground
564 state. The conversion-electron coefficients were taken
565 into account. This sum includes unobserved small I_β
566 contributions with cascade transitions through the 2_1^+
567 and 2_2^+ states. The same method was applied to the β -
568 decay results of the implanted ^{110}Nb . The contribution of
569 the 3036.1-keV transition was also added. The obtained
570 value, $\sum I_\beta^{L+H}(E_i) = 65.2(33)$, includes the contribution
571 of both the low- and high-spin states. The superscript
572 L+H refers to the β decay of the implanted ^{110}Nb . The
573 $\sum I_\beta^H(E_i)$ value was described by using the fraction r of
574 the low-spin state in the implanted ^{110}Nb as,

$$\sum I_\beta^{L+H}(E_i) = r \sum I_\beta^L(E_i) + (1-r) \sum I_\beta^H(E_i). \quad (6)$$

575 From the assumption that the 828.8-keV γ ray is emitted
576 only from the β decay of the low-spin state, r was given
577 as,

$$r = \frac{I_{\gamma,\text{abs}}^{L+H}(828.8 \text{ keV})}{I_{\gamma,\text{abs}}^L(828.8 \text{ keV})} = 0.36(15), \quad (7)$$

578 where $I_{\gamma,\text{abs}}(828.8 \text{ keV})$ is the absolute intensity of the
579 828.8-keV γ ray.

580 From the data of the $^{110}\text{Nb} \rightarrow ^{110}\text{Mo} \rightarrow ^{110}\text{Tc}$ decay
581 chain, the P_{0n}^{L+H} value can be determined following the
582 procedure described in Sec. III C. It is given by

$$1 - P_{0n}^{L+H} = rP_n^L + (1-r)P_n^H, \quad (8)$$

583 Here, only the differences from Sec. III C are de-
584 scribed. The 213.4-keV γ ray was used for the iden-
585 tification of the $^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$ decay. The number

TABLE V. Same as Table II, but for the ^{110}Mo results obtained from the β -decay chain $^{110}\text{Zr} \rightarrow ^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$, where the low-spin state in ^{110}Nb is populated by the β decay of the 0^+ ground state in ^{110}Zr . (1UF) is for the first unique forbidden transition from 2^- to 0^+ or 4^+ states.

E_i (keV)	J^π	E_γ (keV) (low)	I_γ^a (low)	I_β (%) (low)	$\log ft$ (low) (allowd/non-UF)	$\log ft$ (low) (UF)
0.0	0^+			47(26)	5.2(3)	7.8(4)
213.4	(2^+)	213.4	100(4)	25.0(88)	5.5(2)	
493.7	(2^+)	280.2	28.0(24)	25.0(87)	5.4(2)	
		493.8	33.0(27)			
599.0	(4^+)	385.5	7.0(13)	2.9(11)	6.4(2)	8.9(3)
699.8	(3^+)	486.4	6.0(4)	2.5(9)	6.4(2)	
1042.2	(0^+)	828.8	6.0(15)	2.5(10)	6.3(2)	8.8(3)

^a The absolute intensity per 100 β decays is $0.41(14)I_\gamma$.

of the ^{110}Mo β decay was obtained using the 121.0-keV γ ray emitted from ^{110}Tc . From $R(121.0 \text{ keV}) = 0.0375(16)$, $N_\gamma(121.0 \text{ keV}) = 2.279(44) \times 10^4$, and $N_\beta(^{110}\text{Nb}) = 7.39(7) \times 10^5$, $P_{0n}^{\text{L+H}} = 82(4)\%$ and $P_n^{\text{L+H}} = 18(4)\%$ were determined.

Based on the above values and Eqs. (4–8), the remaining values were determined as $P_n^{\text{L}} = -5(41)\%$, $P_n^{\text{H}} = 31(15)\%$, $I_\beta^{\text{L}}(0) = 47(26)\%$, and $\Sigma I_\beta^{\text{H}}(E_i) = 69(15)\%$. Since the P_n^{L} value must be positive, an upper limit is given as $P_n^{\text{L}} < 36\%$. The large uncertainties were propagated mainly from the uncertainty of $I_{\gamma,\text{abs}}^{\text{L}}$ (828.8 keV). The separate P_n determination of the low- and high-spin states was made for the first time in the ^{110}Nb β decay. The previous $P_n^{\text{L+H}}$ value of $40(8)\%$ [43] is larger than the present result. In the previous work, ^{110}Nb was produced by bombarding a U target with a 50 MeV H_2^+ beam. The low-spin fraction r may be different due to the different production reaction and energy.

The $\log ft$ values were determined from the half-lives, I_β and $Q_\beta = 12230(840) \text{ keV}$ [33] for the low- and high-spin states, (as summarized in Tables IV and V), respectively. The excitation energy in ^{110}Nb was not taken into account, which would be negligible in comparison with its Q_β .

First, the spin-parity of the low-spin state in ^{110}Nb is discussed. Positive-parity states with spins ranging from 0 to 4 are populated by the β decay of the low-spin ^{110}Nb . Because this decay pattern and the $\log ft$ values are similar to the ^{108}Nb decay, the spin-parity of the low-spin ^{110}Nb is assigned to be 2^- . The $\log ft$ values of 0^+ and 4^+ states were recalculated as the first unique forbidden transition to be 7.8(4), 8.8(3), and 8.9(3) for 0_1^+ , 0_2^+ , and 4_1^+ , respectively. These are consistent with the typical range from 8 to 11 [40].

For the β decay from the high-spin state, it is impossible to interpret the $\log ft$ values of both the 3^+ and 8^+ states, even if the first unique forbidden transition is considered. Because the I_β to the 3^+ state, 1.5(6), is smaller than the other states, missing feedings from

higher excited states may cause a significant deviation from the actual $\log ft$. On the other hand, it is reasonable that the 8^+ state, which is the largest spin among the measured states, is directly populated. Therefore, the 3^+ state is considered to be mainly fed from the higher excited states. The $\log ft$ values of the 4^+ , 5^+ , 6^+ , 7^+ , and 8^+ states are in the range from 5.7 to 6.3. This case is similar to the situation above. When the spin-parity of the high-spin state in ^{110}Nb is 6^- , the transitions to 4^+ or 8^+ states become the first unique forbidden transition. The recalculated $\log ft$ values, 8.5(3), 8.5(3), 8.5(3) and 8.6(3) for the 4_1^+ , 4_2^+ , 4_3^+ , and 8_1^+ states, respectively, are consistent with the typical range. For the other positive parity states, the $\log ft$ values are consistent with the first non-unique forbidden transitions from the 6^- state. As a result, the spin-parity of the high-spin state is assigned to be 6^- .

F. Lifetime measurement of 2_1^+ states in $^{106,108,110}\text{Mo}$

The mean lifetimes, τ , of the 2_1^+ states in $^{106,108,110}\text{Mo}$ were measured from the time between the observation of a β particle in a plastic scintillation detector and a γ ray corresponding to the $2_1^+ \rightarrow 0_1^+$ transition in the $\text{LaBr}_3(\text{Ce})$ detector array. Figure 8 shows the time-difference distributions for the three nuclei and Fig. 9 shows the corresponding γ -ray spectra with the regions used to make the time spectra highlighted in gray. The time spectra show a clear single exponential decay on a very low background. The γ -ray spectra in Fig. 9 do not show any evidence for delayed feeding of the 2_1^+ state from higher-lying states and indeed, the lifetime of the 4_1^+ state in ^{108}Mo was recently measured as $\tau = 29.7_{-9.1}^{+11.3}$ ps [9]. Its effect can be ignored, since the lifetime is one order of magnitude smaller than the time resolution of 0.61 ns at 200 keV. The lifetimes of the 2_1^+ states were determined from fitting the slope with a single ex-

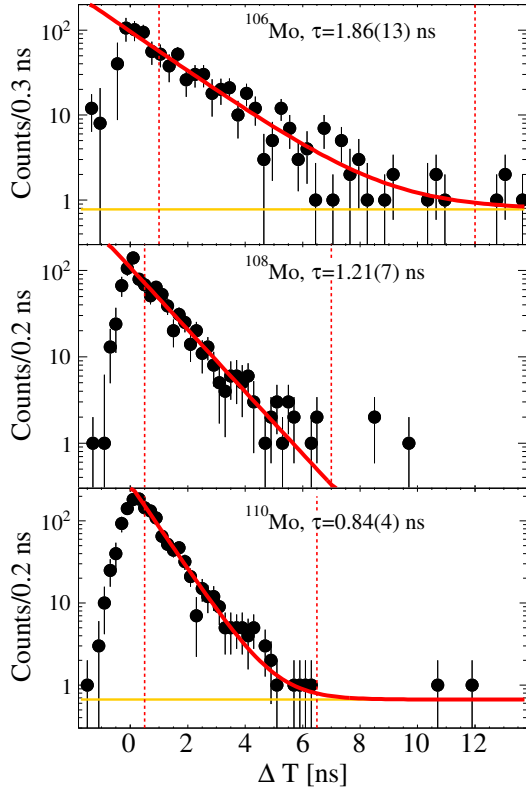


FIG. 8. The time spectra of $2_1^+ \rightarrow 0_1^+$ γ -ray transition in ^{106}Mo , ^{108}Mo , and ^{110}Mo . ΔT is the time from β -particle detection by the plastic scintillator to γ -ray detection by the $\text{LaBr}_3(\text{Ce})$ array. The solid red lines are the best-fit curves using an exponential function and fixed constant background to the region indicated by the dashed red lines. The constant backgrounds, shown by the orange lines, were determined by fitting the region of $15 < \Delta T < 25$ ns, $10 < \Delta T < 25$ ns, and $8 < \Delta T < 25$ ns for ^{106}Mo , ^{108}Mo , and ^{110}Mo , respectively.

661 ponential function and a constant background, yielding
 662 $\tau = 1.86(13)$, $1.21(7)$, and $0.84(4)$ ns for ^{106}Mo , ^{108}Mo ,
 663 and ^{110}Mo , respectively. The previously reported results
 664 for ^{106}Mo are $0.54(8)$ [47, 48], $1.08(22)$ [49], $1.73(24)$ [50],
 665 and $1.93(14)$ ns [51]. The present lifetime ($\tau = 1.86(13)$
 666 ns) is consistent with the values in Refs. [50, 51]. The
 667 result of $\tau = 1.21(7)$ ns for ^{108}Mo is consistent with the
 668 previously reported value of $0.72(43)$ ns [21] but pro-
 669 vides a smaller uncertainty. The measurement for ^{110}Mo
 670 was made for the first time. The systematic trend of
 671 $B(E2; 2_1^+ \rightarrow 0_1^+)$ values in the Mo isotopes is shown in
 672 Fig. 10. The present results with small uncertainties
 673 show that the $B(E2)$ value is nearly unchanged between
 674 the neutron numbers $N = 62$ and 66 , and drops slightly
 675 at $N = 68$.

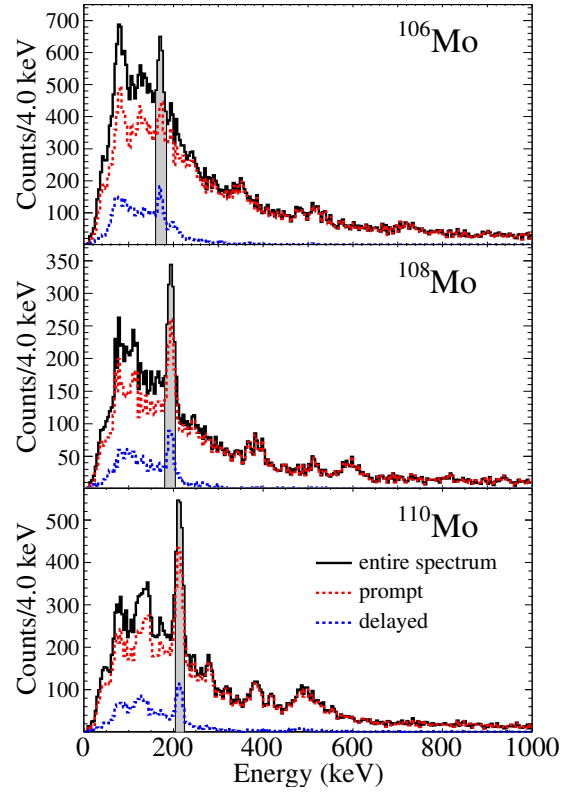


FIG. 9. The γ -ray energy spectra of the $\text{LaBr}_3(\text{Ce})$ array. The energy region used to make the time spectra of Fig. 8 are highlighted with gray. The prompt, $|\Delta T| < 1$ ns, and delayed, $\Delta T > 1$ ns, components are shown by the red and blue dotted lines, respectively.

IV. DISCUSSION

A. Quadrupole deformation of ground state in $^{106,108,110}\text{Mo}$

679 The ground-state band is described as the rotational
 680 motion of a deformed nucleus. The quadrupole deforma-
 681 tion parameter β was obtained from the $B(E2; 2_1^+ \rightarrow 0_1^+)$
 682 values using the formula given in the review paper [48]
 683 as $0.349(13)$, $0.327(10)$, and $0.305(7)$ for ^{106}Mo , ^{108}Mo ,
 684 and ^{110}Mo , respectively. Figure 11 shows the neutron-
 685 number dependence of β for Mo and Zr isotopes. While
 686 the Zr isotopes have a clear peak structure at $N = 64$
 687 and reach $\beta = 0.46(1)$, the Mo isotopes have almost con-
 688 stant $\beta \sim 0.32$ between $N = 60$ and 68 . A comparison
 689 with microscopic calculations is described in Sec. IV E.
 690

B. Triaxial motion in 2_2^+ band

692 The low-lying 2_2^+ state is a signature of a softness
 693 against γ vibration, a γ -unstable rotor, or a rigid triaxial
 694 rotor. The three models are distinguished by means of

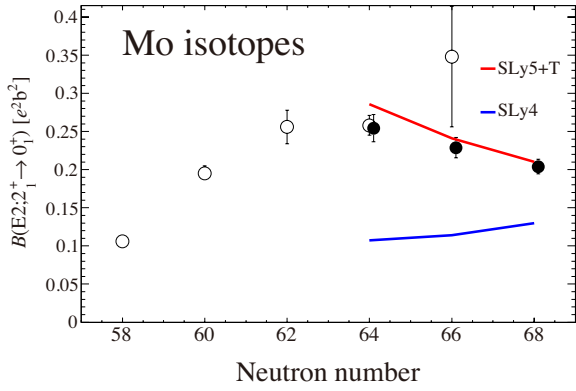


FIG. 10. Experimental and theoretical $B(E2; 2_1^+ \rightarrow 0_1^+)$ values of the even-even Mo isotopes. The experimental values were calculated by the use of the relation in Ref. [52]. The open circles are taken from Ref. [48]. The theoretical values were calculated using the five-dimensional collective Hamiltonian with the pairing-plus-quadrupole interaction parameters determined from the two kinds of the Skyrme-interaction parameters (SLy5+T and SLy4).

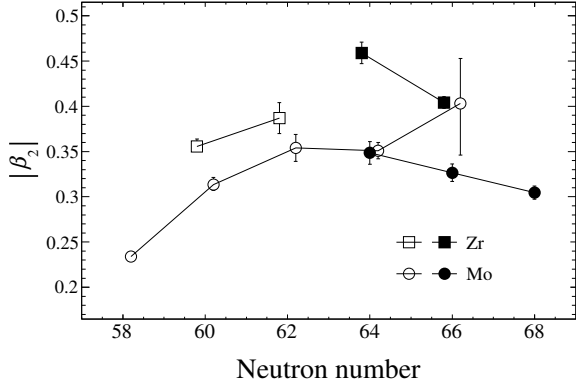


FIG. 11. Quadrupole deformation parameter β for Zr (square) and Mo (circle) isotopes. Filled circles are the present results for the Mo isotopes. Filled squares for the Zr isotopes are the results from the same data set [53], but the values were recalculated from $B(E2; 2_1^+ \rightarrow 0_1^+)$ by using the formula given in the review paper [48]. Open circles and squares are taken from the review paper [48] and a later work [54].

the energy staggering of the 2_2^+ band [1]:

$$\frac{E_s(J)}{E(2_1^+)} = \frac{\Delta E_J - \Delta E_{J-1}}{E(2_1^+)}, \quad (9)$$

where $\Delta E_J = E_\gamma(J) - E_\gamma(J-1)$, and $E_\gamma(J)$ is the energy of the 2_2^+ band member with the spin J . The $E_s(4)/E(2_1^+)$ value of the γ -vibrational band is close to $1/3$, which is given by the $J(J+1) - K^2$ rule if the rotational energies are described approximately as the axially-symmetric rigid rotor. At maximum triaxiality ($\gamma = 30^\circ$) of a rigid-triaxial rotor in the Davydov model, it becomes $5/3$ [2]. Another extreme case of γ -unstable nuclei in the Wilets-Jean model [3] yields -2 . Figure

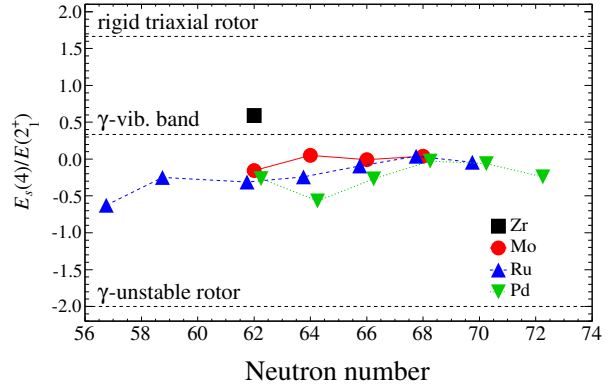


FIG. 12. The $E_s(4)/E(2_1^+)$ ratio around neutron-rich $A = 110$. The black-dashed lines represent the ideal values of three models; rigid-triaxial rotor, γ -unstable rotor, and γ -vibrational band. Filled square, circles, triangles and inverted triangles represent Zr, Mo, Ru, and Pd isotopes, respectively.

12 shows the $E_s(4)/E(2_1^+)$ ratio around the neutron-rich $A = 110$ region. The Mo, Ru, and Pd isotopes have similar values in the range from -0.5 to $+0.1$, which is below the $1/3$ of the γ vibrational band. A larger value of ^{102}Zr than other isotopes suggests that ^{102}Zr has the steeper

potential towards the γ direction. Figure 13 shows the $E_s(J)/E(2_1^+)$ ratio as a function of J for the Mo, Ru, and Pd isotopes. The difference among the isotopes is more apparent than in Fig. 12. The J -dependence of $E_s(J)/E(2_1^+)$ is shown to have a relation to the triaxial motion from the calculation using the Bohr Hamiltonian with a γ -dependent potential [4]. While the γ -vibrational band shows a flat pattern, the γ -soft and the rigid triaxial rotors show a staggering pattern with low values at even and odd J , respectively. The flat pattern of the $^{106,108,110}\text{Mo}$ isotopes indicates that the excitation energies are explained by the rotational bands built on a γ -vibrational 2_2^+ state with the axially-symmetric deformed shape and quantum number $K = 2$. On the other hand, the staggering pattern of the Pd isotopes with $N \leq 66$ indicates a γ -soft rotor. The Ru isotopes show an intermediate behavior. The staggering pattern of the Pd isotopes suddenly disappears at $N = 68$. Especially at $J \geq 6$, a slight staggering in the opposite direction is observed. It is observed that the three isotopes with $N = 68$ show a similar staggering pattern to each other. This staggering is enhanced for ^{112}Ru . The staggering pattern at $N = 68$ might indicate the onset of a very weak triaxial shape and might show a significant neutron contribution to make a shallow potential minimum at a finite γ .

For the γ -vibrational band, the kinematic moment of inertia (MoI) is expected to be similar to that of the ground band. Figure 14 shows the kinematic MoI of the ground and 2_2^+ bands up to $J = 10$. The newly discovered levels in the $K = 2$ band of ^{110}Mo extended the kinematic MoI up to $J = 7$. The similar evolution of the kinematic MoI between these two bands supports the interpretation

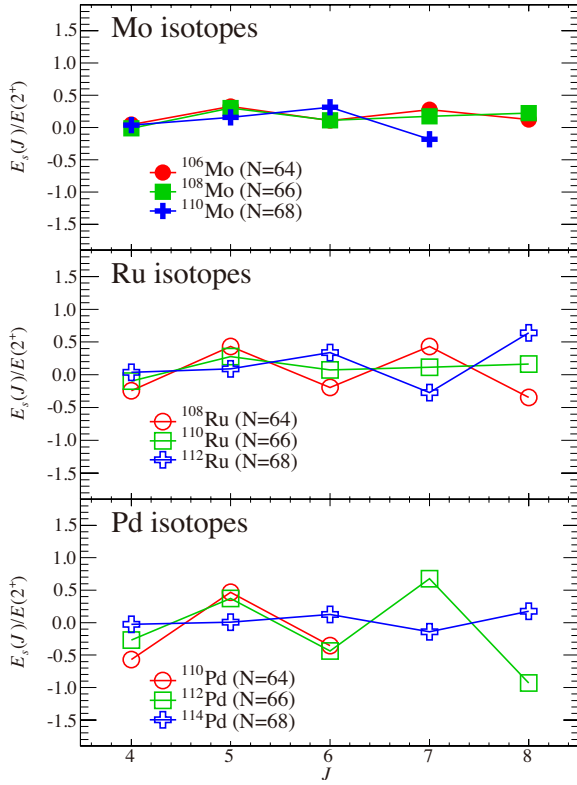


FIG. 13. The staggering pattern of $E_s(J)/E(2_1^+)$. The flat pattern indicates the γ -vibrational band, while the staggering pattern with low values at even and odd J indicates the γ -soft and rigid triaxial rotor, respectively, [4].

TABLE VI. The experimental and theoretical $B(E2)$ ratios. The M1/E2 mixing ratio of $\delta = 6.2_{-0.8}^{+1.0}$ [56] was used for ^{106}Mo . A pure E2 transition was assumed for ^{108}Mo and ^{110}Mo . The theoretical calculation using the SLy5+T interaction is given.

	Alaga	^{106}Mo	^{108}Mo	^{110}Mo
$B(E2; 2_2^+ \rightarrow 2_1^+)$		4.5(6)	8.3(6)	17.3(4)
$B(E2; 2_2^+ \rightarrow 0_1^+)_{\text{exp.}}$				
$B(E2; 2_2^+ \rightarrow 2_1^+)$	1.43	2.0	4.9	14.0
$B(E2; 2_2^+ \rightarrow 0_1^+)_{\text{th.}}$				

of a γ -vibrational band.

The ratio $B(E2; 2_2^+ \rightarrow 2_1^+)/B(E2; 2_2^+ \rightarrow 0_1^+)$ provides additional information about the 2_2^+ band. The $B(E2)$ ratio is given as 1.43 by the Alaga rule [55], where the rotational and vibrational motions for the axially-symmetric shape are well decoupled. The experimental $B(E2)$ ratios shown in Table VI are clearly larger than the Alaga value. For the γ -vibrational band, the enhancement can be explained by the rotation-vibration coupling model which introduces the Coriolis mixing between two bands with $\Delta K = 2$ [1]. In Sec. IV E, the $B(E2)$ ratio is compared with beyond-mean-field calculations.

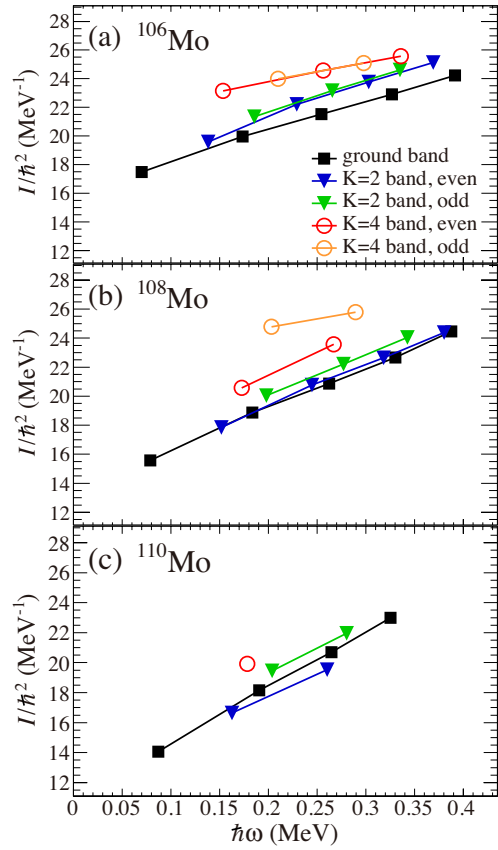


FIG. 14. The kinematic moment of inertia for the ground band (black line with filled squares), $K^\pi = 2^+$ band (blue line with filled triangles for even J and green line for odd J), and $K^\pi = 4^+$ band (red line with open circles for even J and orange line for odd J) in (a) ^{106}Mo , (b) ^{108}Mo , and (c) ^{110}Mo .

C. Candidate of two-phonon γ band

The $K^\pi = 4^+$ band in ^{110}Mo has the lowest band-head energy of 1244 keV among the neutron-rich Mo isotopes. A potential two-quasiparticle state with $K^\pi = 4^+$ would appear around or above the pairing gap. However, the observed energy is well below $2\Delta_p \sim 3.4$ MeV and $2\Delta_n \sim 2.5$ MeV for the proton and neutron pairs, respectively, which are calculated from the atomic mass evaluation AME2016 [33]. A $K^\pi = 4^+$ band, decaying to the γ band, is known in many neighboring nuclei, such as $^{104,106,108}\text{Mo}$, and $^{108,110,112,114,116}\text{Ru}$ [34, 57]. The systematical observations of the $K^\pi = 4^+$ state indicate that the $K^\pi = 4^+$ band head is a collective excitation rather than a two quasiparticle state.

The $K^\pi = 4^+$ band in ^{106}Mo has been discussed in the context of a two-phonon γ vibration [13]. The ratio of the lowest $K^\pi = 4^+$ and 2^+ band-head energies is 2.02, which is close to the 2.0 value for a harmonic vibrator. The reduced transition probabilities of the interband transition between $K^\pi = 2^+$ and 4^+ bands were compared with those between $K^\pi = 0^+$ and 2^+ bands,

and were consistent with the relation of the one-phonon and two-phonon excitations. The ratio of the band-head energies changes gradually as 1.95, 2.02, 2.43, and 2.52 for ^{104}Mo , ^{106}Mo , ^{108}Mo , and ^{110}Mo , respectively. The kinematic MoI of the $K^\pi = 4^+$ band shown in Fig. 14 has similar values to those of the ground-state and γ bands. Thus, the newly discovered $K^\pi = 4^+$ band in ^{110}Mo was assigned as a candidate of the two-phonon γ vibrational band.

D. Second 0^+ state

The energies of the 0_2^+ state, 893.4 and 1042.2 keV for ^{108}Mo and ^{110}Mo , respectively, are low enough to indicate a β -vibrational state or shape coexistence rather than two-quasiparticle states, since they are well below the pairing gaps, $2\Delta_p$ and $2\Delta_n$, given in Sec. IV C. The energies are similar to those of other Mo isotopes, which range from 695 keV to 886 keV between ^{98}Mo and ^{104}Mo , respectively [34].

The 1158.4-keV 2^+ state in ^{108}Mo has a similar decay pattern to the 2_3^+ state in $^{106,108,110}\text{Ru}$ isotopes [34]. The 2_3^+ state in the Ru isotopes decays also to the 0_2^+ state. Although the corresponding γ -ray transition from 1158.4-keV state to 0_2^+ state in ^{108}Mo was not observed due to the lack of the sensitivity for $I_\gamma < 0.5\%$, the energy difference, $E(2_3^+) - E(0_2^+) = 265$ keV, is similar to the cases of 402, 273, and 260 keV for $^{106,108,110}\text{Ru}$ [34], respectively. Based on these systematic trends, the 1158.4-keV state in ^{108}Mo was tentatively assigned as the member of the 0_2^+ band.

The 0_2^+ states of $^{108,110}\text{Mo}$ will be discussed by comparing with predictions in Sec. IV E.

E. Comparison with 5D collective Hamiltonian calculation with microscopic approach

Five-dimensional collective Hamiltonian calculations were performed for the low-lying states in $^{106,108,110}\text{Mo}$. The PES and the kinetic terms (vibrational and rotational masses) were microscopically calculated using the CHFB+LQRPA approach using pairing-plus-quadrupole (P+Q) interactions whose parameters, such as spherical single-particle energies in the two-major harmonic oscillator shell model space and interaction strengths, were fitted to the mean-field results obtained with two kinds of Skyrme interactions, SLy5+T or SLy4 (see Refs. [58–60] for details). The Schrödinger equation in the collective space was solved to obtain the energies and the collective wave functions of the ground and excited states. The PESs and the collective wave functions squared are shown in Fig. 15 for SLy5+T and Fig. 16 for SLy4. The two kinds of theoretical excitation energies are compared with the experimental ones in Fig. 17. The PESs show a strong dependence on the effective interaction used. The calculation with the SLy5+T interaction predicts a pro-

late shape with $\beta \sim 0.35$ and $\gamma = 0^\circ$, while the SLy4 interaction predicts an oblate shape with $\beta \sim 0.2$ and $\gamma = 60^\circ$. For the comparison with the experimental results, the $B(E2; 2_1^+ \rightarrow 0_1^+)$ value was used instead of β . The $B(E2; 2_1^+ \rightarrow 0_1^+)$ values were calculated by adopting the effective charges, $e_\pi = 1.5e$, and $e_\nu = 0.5e$, for the two major-shell single-particle model space as shown in Fig. 10. The theoretical values with SLy5+T are roughly double those with SLy4 and agree well with the experimental ones. The energy of 2_1^+ state for the rotational band, which has a strong correlation to $B(E2)$ [52], is an observable closely related to β . The energies of the ground-state band are well reproduced by the calculations with SLy5+T, as shown in Fig. 17. The good agreement with the theoretical values using the SLy5+T interaction indicates that the ground state in $^{106,108,110}\text{Mo}$ has a prolate shape. The $B(E2)$ values for SLy5+T shows an increase at $N = 64$, while the experimental ones are rather constant. The PES of ^{106}Mo has a gentle slope toward $\beta \sim 0.45$, which may increase β compared with ^{108}Mo . Because the largest β was observed at $N = 64$ in the Zr isotopes [53] and the energy of the 2_1^+ state becomes minimum at $N = 64$ for both isotopes [61], the soft potential toward the large β might be consistent with the experimental results. But a less-soft potential would be necessary for a better agreement.

The energies of the 2_2^+ band in ^{106}Mo are well reproduced by the calculation with SLy5+T. The wave functions of 2_γ^+ and 3_γ^+ are localized on a finite γ value, reflecting the dynamical triaxial deformation induced by the γ vibration of the prolate shape. While the band-head energy in ^{108}Mo is overestimated, the excitation energies measured with respect to the 2_2^+ state are well reproduced and the wave functions show the γ vibration expected from the experimental odd-even staggering. Thus, the calculations for ^{106}Mo and ^{108}Mo are consistent with the interpretation in Sec. IV B, that is, the rotational band of the γ vibrational state. On the other hand, the calculated 2_2^+ band in ^{110}Mo shows considerable energy staggering. The 3_γ^+ and 5_γ^+ states converge toward the 4_γ^+ and 6_γ^+ states, respectively. The degeneracy of these states is predicted in the γ -unstable model. The wave function of 2_γ^+ is prolonged in the γ direction as expected in the γ -unstable model. It is caused by the flatness of the PES between $\gamma = 20^\circ$ and 60° . Conversely, the experimental results indicate γ vibration in the stiffer potential. It is noticed that the calculated wave function of the 3_γ^+ state is similar to those of the lighter Mo isotopes and indicates γ vibration. The characteristics of the wave functions with higher spins change depending on if the spin is even or odd. This is also noticed in the calculations with SLy4. It is suggested that the energy staggering with the close degeneracy of $E(3_\gamma)$ and $E(4_\gamma)$ might depend not only on the prolonged wave function toward the γ direction, but also on the difference between the even and odd spins. The odd-spin states cannot mix with the $K^\pi = 0^+$ component, since the odd-spin states are not allowed in the $K^\pi = 0^+$ band. This means that the ex-

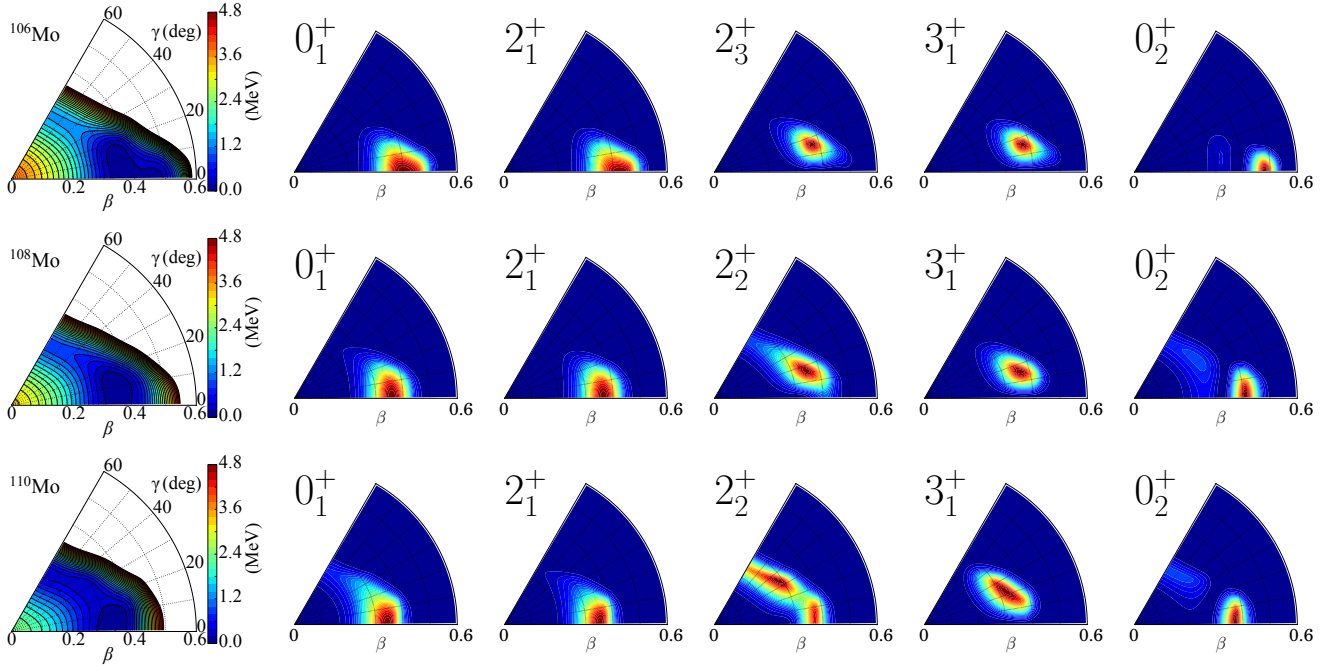


FIG. 15. The potential-energy surface and the collective-wave functions squared (with a factor of β^4) of low-lying states in ^{106}Mo , ^{108}Mo , and ^{110}Mo . The pairing-plus-quadrupole interaction and spherical single-particle energies used in the CHFB+LQRPA calculations were fitted to the mean-field results obtained with the SLy5+T interaction.

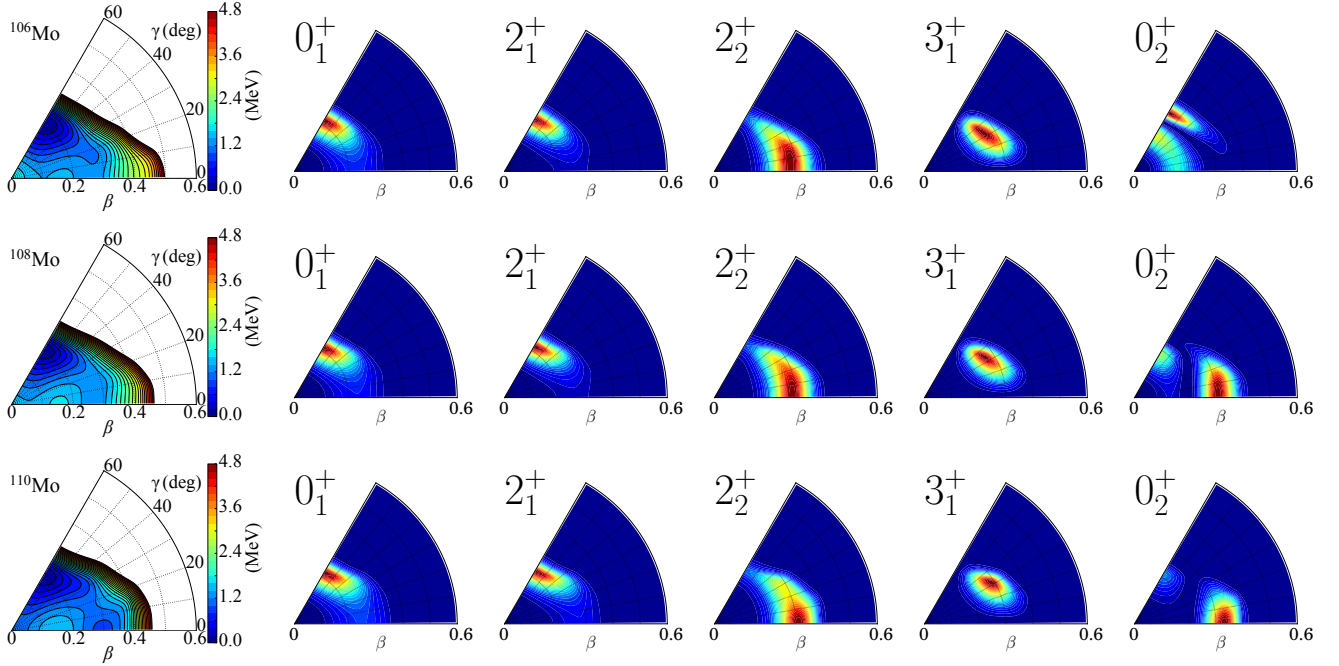


FIG. 16. Same as Fig. 15, but with the SLy4 interaction.

893 cited even-spin states (e.g. 4_2^+) are more influenced by
 894 the mixing with $K^\pi = 0^+$ bands, which are built on the
 895 ground state, shape coexistence, shape fluctuation in the
 896 β direction around $\gamma = 0^\circ$, and any low-lying $K^\pi = 0^+$
 897 states. The odd-spin states are not very sensitive to them

898 at all. This will result in a qualitative difference between
 899 the even- and odd-spin states, and energy staggering that
 900 deviates from the ideal γ -band energy.

901 The quadrupole collective Hamiltonian approach can
 902 predict a two-phonon γ vibrational band with $K^\pi = 4^+$,

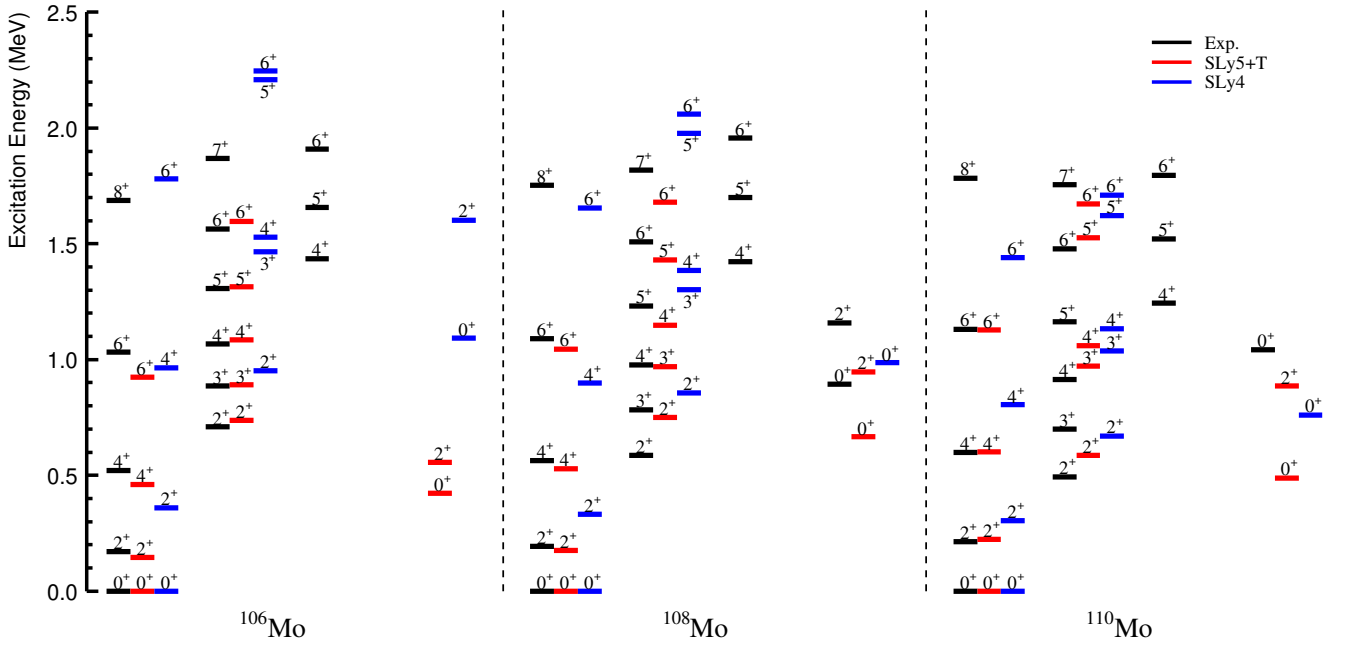


FIG. 17. The experimental and theoretical energies of the low-lying excited states in ^{106}Mo , ^{108}Mo , and ^{110}Mo . Black lines present the experimental results, and red and blue lines present the results from the theoretical calculations using SLy5+T and SLy4, respectively.

903 but not two quasiparticle states because it does not
 904 include the quasiparticle degrees of freedom explicitly. As
 905 discussed in Sec. IV C, the observed $K^\pi = 4^+$ band is
 906 most likely built on a collective excitation. However, the
 907 $K^\pi = 4^+$ band was not predicted by the calculations. An
 908 ideal two-phonon γ vibrational state has a wave function
 909 localized around the prolate minimum. To have a local-
 910 ized two-phonon $K^\pi = 4^+$ vibrational state, which has
 911 a larger vibrational energy than that of a one-phonon
 912 state, generally the PES along the γ direction has to be
 913 deep enough to prevent oblate admixtures. If this is not
 914 satisfied, the corresponding two-phonon state will mix
 915 with the oblate shape and lose its two-phonon charac-
 916 ter. The potential barriers in the γ direction from the
 917 potential minimum, shown in Fig. 15, are shallow. By
 918 increasing in energy by 1 MeV or so from the prolate
 919 potential minimum, the other side of the axial symme-
 920 try at $\gamma = 60^\circ$ (oblate) is reached. Further theoretical
 921 investigations are necessary to reproduce these collective
 922 excitations. One of the important improvements for the
 923 5D collective model is to use effective interactions such
 924 as modern Skyrme energy density functionals instead of
 925 the P+Q Hamiltonian [62].

926 The squared wave functions of the 0_2^+ state in
 927 $^{106,108,110}\text{Mo}$ with SLy5+T indicate β vibrational mo-
 928 tion. On the other hand, the calculation with SLy4 indi-
 929 cates the possibility of shape coexistence of prolate and
 930 oblate shapes. Since the energy difference between the
 931 0_2^+ and 2_3^+ states in ^{108}Mo is consistent with the predic-
 932 tion with SLy5+T, the 0_2^+ state in ^{108}Mo is suggested to
 933 be a β vibrational state. There is no experimental in-

934 formation providing a favored origin for the 0_2^+ state in
 935 ^{110}Mo . Additional experimental and theoretical works
 936 are awaited for further discussions.

937 F. Structure of parent nuclei $^{106,108,110}\text{Nb}$

938 *Configuration of ^{106}Nb :* The spin-parity of the β -
 939 decaying state in ^{106}Nb was assigned to be 4^- , and
 940 there were no experimental indications of the existence
 941 of a second β -decaying state. From the prompt γ -
 942 ray spectroscopy of the ^{252}Cf spontaneous fission [63],
 943 the spin-parity of the ground state in ^{106}Nb was as-
 944 signed as 1^- . Owing to the relatively strong popula-
 945 tion of high-spin states in ^{106}Mo and the fact that no
 946 known γ rays of ^{106}Nb are observed following the de-
 947 cay of ^{106}Zr , it is likely that the β -decaying state of
 948 ^{106}Nb is not the 1^- ground state. The configuration
 949 of $\pi 3/2^- [301] \otimes \nu 5/2^+ [413]$ with $K^\pi = 1^-$ was pro-
 950 posed for the ground state [63]. In the Nilsson dia-
 951 gram [64], these quasiparticle states are predicted for
 952 the prolate shape with $\beta \sim +0.35$ measured in ^{106}Mo .
 953 The Gallagher-Moszkowski (GM) rule [65] predicts that
 954 the state with the antiparallel spin-coupling becomes a
 955 higher-lying state. Therefore, the observed β -decaying
 956 state was assigned to be a high-spin $K^\pi = 4^-$ isomeric
 957 state of the GM partner in the $\pi 3/2^- [301] \otimes \nu 5/2^+ [413]$
 958 configuration.

959 *Configuration of ^{108}Nb :* The spin-parity of the ^{108}Nb
 960 ground-state was assigned to be 2^- , and there was no
 961 evidence of a β -decaying isomeric state. The single-

TABLE VII. Candidates of the quasiparticle-state configurations of two β -decaying states in ^{110}Nb . Four quasiparticle states are selected from the Nilsson diagram [64] and the quasiparticle level in the Woods-Saxon potential [66] for each nucleon. The left and right values show the spin-parity of the parallel- and antiparallel-spin coupling, respectively. The parallel-spin coupling state becomes lower-lying state [65]. The spins of the assigned configurations for the low and high-spin states are written in bold text.

	$\pi 1/2^+[431]$	$\pi 5/2^+[422]$	$\pi 5/2^-[303]$	$\pi 3/2^-[301]$
$\nu 5/2^+[402]$	$2^+/3^+$	$5^+/0^+$	$0^-/5^-$	$4^-/1^-$
$\nu 1/2^+[411]$	$1^+/0^+$	$2^+/3^+$	$3^-/2^-$	$1^-/2^-$
$\nu 7/2^-[523]$	$3^-/4^-$	$6^-/1^-$	$1^+/6^+$	$5^+/2^+$
$\nu 1/2^-[541]$	$1^-/0^-$	$2^-/3^-$	$3^+/2^+$	$1^+/2^+$

proton and neutron levels in the deformed nucleus were calculated according to the Nilsson diagram [64] and by using the Woods-Saxon potential [66]. A major difference of the level orderings between these two is the negative parity states of the protons. Candidates of the valence proton and neutron configurations were selected based on these two predictions. These are, $\pi 1/2^+[431]$, $\pi 5/2^+[422]$, $\pi 5/2^-[303]$, and $\pi 3/2^-[301]$ for the proton configuration, and $\nu 1/2^+[411]$, $\nu 5/2^+[413]$, and $\nu 1/2^-[541]$ for the neutron configuration at around $\beta = +0.33$ for ^{108}Mo . The spin-parity of the $\pi 5/2^-[303] \otimes \nu 1/2^+[411]$ configuration is 2^- and 3^- with the antiparallel- and parallel-spin couplings, respectively. The lower-lying state is the 3^- state based on the GM rule. The 2^- state would not form a β -decaying isomeric state because of a fast M1 transition to the 3^- state. Thus, the expected β -decaying state is not the 2^- state, but the 3^- state. The 2^- state of the $\pi 3/2^-[301] \otimes \nu 1/2^+[411]$ configuration is also antiparallel-spin coupled, therefore the 1^- state with the parallel-spin coupling would be the β -decaying state. The $\pi 5/2^+[422] \otimes \nu 1/2^-[541]$ configuration can generate a β -decaying 2^- state with the parallel-spin coupling. The 3^- state with the antiparallel-spin coupling will decay to the 2^- state by a M1 transition. Therefore, the ground state of ^{108}Nb was assigned to be the 2^- state with the $\pi 5/2^+[422] \otimes \nu 1/2^-[541]$ configuration.

Configuration of ^{110}Nb : Two β -decaying states were observed. The spin-parities were assigned to be 2^- and 6^- . The quasiparticle states are selected from the Nilsson diagram [64] at around $\beta = +0.305$ for ^{110}Mo or the single particle levels in the Woods-Saxon potential [66] as $\pi 1/2^+[431]$, $\pi 5/2^+[422]$, $\pi 5/2^-[303]$, and $\pi 3/2^-[301]$ for the proton, and $\nu 5/2^-[402]$, $\nu 1/2^+[411]$, $\nu 7/2^-[523]$, and $\nu 1/2^-[541]$ for the neutron. The spin-parities of the configuration coupled with these quasiparticle states are summarized in Table VII.

The 6^- state is only generated by the parallel-spin coupling of the $\pi 5/2^+[422] \otimes \nu 7/2^-[523]$ configuration. The anti-parallel spin coupled 1^- state of this configuration, which has a higher energy based on the GM rule, would

not be a β -decaying state, because it can decay to the β -decaying 2^- state by an M1 transition. For the low-spin 2^- state, there are three candidates as given in Table VII. Since the spin difference between the GM pair is 1 for all three candidates, the lower energy state with the parallel spin becomes the β -decaying state. Thus, the parallel spin-coupling state of the $\pi 5/2^+[422] \otimes \nu 1/2^-[541]$ configuration was assigned to the β -decaying 2^- state.

The difference between the assigned configurations of the two β -decaying states is the neutron quasiparticle state. It is indicated that the $\nu 7/2^-[523]$ and $\nu 1/2^-[541]$ states are near the Fermi surface and close to each other. There was no experimental evidence to select the ground state from these two states.

Comparison between Nilsson diagram and single-particle levels in Woods-Saxon potential: The assigned configurations of ^{106}Nb , ^{108}Nb , and ^{110}Nb are consistent with the Nilsson diagram given in Ref. [64]. On the other hand, the $\pi 5/2^+[422]$ state in the Woods-Saxon potential is located below $Z = 40$ [66], even though it is used in the configuration of ^{108}Nb and ^{110}Nb . From comparison with the Nilsson diagram, it is suggested that the $\pi 3/2^-[301]$ state in the Woods-Saxon potential may need to lower in energy so as to cross the $\pi 5/2^+[422]$ state at $\beta \sim 0.3$.

V. SUMMARY

The delayed γ rays emitted from the β decays of $^{106,108,110}\text{Nb}$ were observed to investigate the shape evolution of $^{106,108,110}\text{Mo}$. The neutron-emission probability, P_n , of ^{108}Nb and ^{110}Nb was determined from the β -delayed γ rays emitted from the daughter nuclei with the same mass number. The daughter decays of $^{106,108,110}\text{Zr}$ were used to search for β -decaying isomeric states in the Nb isotopes and to increase the statistics of the γ rays from ^{106}Mo and ^{108}Mo . Two β -decaying states with low and high spins were found in the ^{110}Nb β decay. Although the ground state in ^{110}Nb was not assigned from these two candidates, the decay properties, including P_n , were separately determined for each state.

The lifetime of the 2_1^+ state in the Mo isotopes was measured by using the fast timing LaBr₃(Ce) array. The quadrupole deformation parameter was obtained from the energy and lifetime of the 2_1^+ state. The deformation is almost unchanged with $\beta \sim 0.33$ from the neutron number $N = 62$ to 66 and slightly decreases to 0.305(7) at $N = 68$. The even-odd energy staggering of the 2_2^+ band was evaluated using $E_s(J)/E(2_1^+)$ as a function of the spin J . The staggering of the ^{106}Mo , ^{108}Mo , and ^{110}Mo isotopes shows the pattern of the γ -vibrational band. The comparison of kinematic moment of inertia between the ground and 2_2^+ bands supports the interpretation as the γ -vibrational band. A candidate of the two-phonon γ vibrational band was found well below the proton and neutron pairing gaps also in the ^{110}Mo iso-

1059 tope.

1060 The ground, γ , and two-phonon γ bands were com-
1061 pared to beyond-mean-field calculations. The ground-
1062 band energies and $B(E2)$ of the 2_1^+ state were reproduced
1063 by the calculation with the SLy5+T interaction. The γ
1064 band of ^{106}Mo was also reproduced very well. The com-
1065 parison indicates that the shape is prolate with axial sym-
1066 metry. However, the even-odd staggering of the γ band
1067 in ^{110}Mo was not reproduced. The predicted potential
1068 might be too shallow toward the triaxial deformation es-
1069 pecially for ^{110}Mo . This may also be the reason why no
1070 two-phonon γ bands exist in the theoretical results.

1071 The 893.4- and 1042.2-keV states in ^{108}Mo and ^{110}Mo
1072 were assigned as the second 0^+ states, respectively. On
1073 the other hand, the transition from the second 0^+ state
1074 previously reported in the β -decay to ^{106}Mo was shown
1075 to be the known $5_1^+ \rightarrow 4_1^+$ transition. The compari-
1076 son with the beyond-mean-field calculation indicates a
1077 β -vibrational character for the 0_2^+ state in ^{108}Mo .

1078 The $\log ft$ values were reasonably understood only
1079 when the first unique forbidden transition was intro-
1080 duced. It gave the strong constraint for the spin-parity
1081 assignment of the parent nuclei. The quasiparticle con-
1082 figurations of the parent nuclei were assigned by referring
1083 the Nilsson diagram for the prolate shape.

1084 It is interesting to investigate whether the disagree-
1085 ment between the experiment and prediction for ^{110}Mo
1086 is enhanced at heavier Mo isotopes or not. The low-lying
1087 2_1^+ , 4_1^+ , and 2_2^+ states are known in ^{112}Mo [16]. In order
1088 to study the triaxial motion, measurements of the higher
1089 spin states in the 2_2^+ band are awaited.

ACKNOWLEDGEMENTS

We would like to express our gratitude to the
RIKEN Nishina Center accelerator staff for provid-
ing a stable and high intensity ^{238}U primary beam.
This work was supported by JSPS KAKENHI Grants
Nos. 24740188, 25247045, 26800117, and 16K17680,
NRF Grant No. 2016K1A3A7A09005575, STFC Grant
Nos. ST/J000132/1, ST/J000051/1 and ST/K502431/1,
DOE Grant No. DE-FG02-91ER-40609, and Span-
ish Ministerio de Ciencia e Innovación under Contracts
No. FPA2009-13377-C02 and No. FPA2011-29854-C04.
P.H.R. acknowledges support from the UK National Mea-
surement Office (NMO). P.-A.S. was financed by JSPS
Grant No. 23 01752 and the RIKEN Foreign Postdoc-
toral Researcher Program. We acknowledge the EU-
ROBALL Owners Committee for the loan of germa-
nium detectors and the PreSpec Collaboration for the
readout electronics of the cluster detectors. NH ac-
knowledges the JSPS-NSFC Bilateral Program for the
Joint Research Project on "Nuclear mass and life for un-
ravelling mysteries of r-process." Numerical calculations
were performed in part using the COMA (PACS-IX) and
Oakforest-PACS provided by Multidisciplinary Coopera-
tive Research Program in Center for Computational Sci-
ences, University of Tsukuba.

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