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Magnetic borophenes from evolutionary search

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A computational methodology based on *ab initio* evolutionary algorithms and the spin-polarized density functional theory was developed to predict two-dimensional (2D) magnetic materials. Its application to a model system borophene reveals an unexpected rich magnetism and polymorphism. A metastable borophene with nonzero thickness is an antiferromagnetic (AFM) semiconductor from first-principles calculations, which can be further tuned into a half metal by finite electron doping. In this borophene, the buckling and coupling among three atomic layers are not only responsible for magnetism, but also result in an out-of-plane negative Poisson's ratios under uniaxial tension, making it the first elemental material possessing auxetic and magnetic properties simultaneously.

I. INTRODUCTION

Two-dimensional (2D) magnetic materials have attracted huge interest owing to their potential applications in spintronics and data storage.^{1–12} The ultimate thinness changes the physical properties dramatically compared to the corresponding bulk materials. Although a number of 2D magnetic materials have been proposed theoretically, 9^{-14} few of them were synthesized experimentally. Recent experimental studies found that 2D forms of CrI₃ and Cr₂Ge₂Te₆ can inherit the ferromagnetic (FM) orders at low temperatures from their bulk forms.^{1,2} Strikingly, even for paramagnetic (PM) bulk material, i.e., VSe₂, its monolayer form shows an unexpected strong room-temperature ferromagnetism on van der Waals substrates.³ Stimulated by these exiting experimental reports, 56 new magnetically ordered monolayer structures were predicted from highthroughput computation to be exfoliable from known magnetic bulk materials.⁴ However, discovering new 2D magnetic materials beyond exfoliation from the parent bulk compounds is still governed by trial and error approaches. Among the light element-based 2D materials, graphene is not magnetic,¹⁵ but may be a promising material for spintronics by optimizing defects, substrate, or adsorbing hydrogen atoms.^{16–19} Boron, with only three valence electrons, is electron deficient, resulting in the formation of multicenter B-B bonds and rich polymorphism with great chemical complexity in borophenes.^{20–31} Various borophenes have been successfully synthesized on Ag, Cu, or Al substrates under ultrahigh-vacuum conditions. $^{32-36}$ The atomically thin borophenes display remarkable properties, such as the emergence of superconductivity, massless Dirac fermions, superior transport and mechanical properties.²⁰⁻³⁶ However, the phase diagram of borophene remains largely unexplored due to lack of efficient structure prediction method. With the goal of uncovering more 2D mateials with superior magnetic properties besides magnetic doping that have been experimentally confirmed as one of simple and efficient methods,²⁹⁻³¹ we developed a new strategy based on evolutionary structure prediction and explored the magnetic borophenes in a systematic manner.

II. METHOD

To search for the stable 2D magnetic structures, we further developed a new computational scheme based on the *ab initio* evolutionary algorithm $USPEX^{37-40}$ combined with the spin-polarized density functional theory (DFT). The initial structures are randomly produced with assigned layer group symmetry and user-defined thickness. They are assumed to have either FM, AFM, or nonmagnetic (NM) order. The corresponding values of magnetic moments are then set as 1 for low spin (LS), 4 for high spin state (HS) with the signs (+ or -) depending on FM or AFM, while 0 for NM. The ratio of different structures (NM, FM-LS, FM-HS, AFM-LS, AFM-HS, FM-LSHS, and AFM-LSHS) is also a user defined input.⁴¹ The sum of all ratio numbers is 1, which also determines the distribution of the random numbers. The structures with odd number of atoms are supposed to have FM order



FIG. 1. (color online) (a) Energy evolution for 2D CrI₃ system during the magnetic evolutionary searching. All of structures are magnetic and the inset shows the most stable structure of P3m1-CrI₃. (b) Energy distribution of borophenes from the magnetic evolutionary searching.

automatically. For the evolutionary search, either the relaxed energy or the total magnetic moment was used as a criterion (*fitness* function) for parent structures selection to generate new structures by various evolutionary operators, such as random structure generator, heredity and mutations (including lattice constants and coordination). The optimized individual magnetic momentums are saved for further data processing by new operators of spin heredity or spin mutations, which enhance the spin structural diversity significantly. For an intrinsic magnetic system, e.g., CrI₃, the total energy was selected as the criterion to find the most thermodynamically stable structure. By contrast, for the nonmagnetic system, e.g., borophene, there are several alternative ways to be considered: (I) If the energy was selected as the criterion, the target is to find the lowest-energy structure associated with a few magnetic phases since boron is an intrinsic NM element. (II) While the total magnetic moment was chosen, the target is to find a structure with the largest magnetic moment. Hence lots of metastable



FIG. 2. (color online) (a) and (b) Top and side views of 19 - P6/mmm borophene. The partial bonds among three layers are removed for clarity. Three inequivalent atomic positions (B1, B2, and B3) of NM structure are labelled. The dotted red, blue and black lines indicate the lattices of NM, striped-AFM, and non-collinear 120° AFM (ncl-AFM) structures, respectively. (c) and (d) striped-AFM and ncl-AFM, the pink arrows indicate the relative directions of their magnetic moments.

magnetic borophenes are obtained. However, the best one is difficult to be synthesized because of its relative higher energy. (III) To find a suitable magnetic lowerenergy structure, the fitness can take account of both energy and magnetic moment by using the equation of $fitness = (E_{tot} - a|spin|)/n$. Here E_{tot} , |spin|, and n are the total energy, total magnetic moment, and number of atoms for the whole system, the coefficient of a is a constant with the unit of eV/μ_B . Our magnetic structure searching for borophene adopted the last method, and it works well with a default a value of 2. For each relaxed structure, we sum over the (absolute) values of the magnetic moments for all atoms ($\sum M_i$ and $\sum |M_i|$). If $\sum |M_i|$ is close to zero (< $0.03 \times N_{atoms}$, where N_{atoms} is the number of magnetic atoms), we assign it to be NM; otherwise, the structure would be either AFM ($|\sum M_i| <$



FIG. 3. (color online) Band structures of 19 - P6/mmm borophene with (a) ncl-AFM, (b) NM, (c) striped-AFM, (d) FM structures. (e) The atomic orbital resolved band structures of striped-AFM 19 - P6/mmm borophene. Two flat bands dominated by the p_z orbitals primarily originate from one type of B1 atoms. The highest valence band with majority spin is colored in pink, and the lowest conduction band with minority spin is colored in dark blue. (f) These two flat bands mainly originate from the other magnetic B1 atoms of striped-AFM state, but their spin electrons behave oppositely.

 $0.25 \times N_{atoms}$) or FM ($|\sum M_i| \ge 0.25 \times N_{atoms}$). We also assign the structure to be LS {if max($|M_i|$) < 1.5} or HS {min($|M_i|$) > 1.5}. Otherwise, the structure would be labelled as a hybrid HSLS. We limited our structural search within an unit cell of 5-20 atoms with a vacuum of 20 Å. Structure relaxations and total energy calculations were performed with the projector-augmented wave⁴² (PAW) method as implemented in the VASP package,⁴³ and the exchange-correlation energy was computed within the generalized gradient approximation (GGA) with the functional of Perdew, Burke, and Ernzerhof (PBE).⁴⁴ The plane-wave cutoff energy of 600 eV and uniform Γ centered k-points grids with the resolution of $2\pi \times 0.025$ $Å^{-1}$ were used. The convergence for terminating the electronic self-consistency cycle and the force criterion for structure relaxation were set at 10^{-6} eV and 10^{-2} eV/Å. The charge doping is simulated by varying the total number of electrons in the unit cell, with a compensated jellium background of opposite charge to maintain neutrality. Phonon dispersion curves were calculated by the supercell method (the $2 \times 2 \times 1$ supercell for NM, FM and AFM states) using the PHONOPY package⁴⁵ with the energy convergence of 10^{-7} eV.



FIG. 4. (color online) (a) and (b) Top and side views of spin charge density of striped-AFM 19 - P6/mmm borophene. The majority-spin charge density is colored in red, while the minority-spin charge density is colored in blue. The dotted lines indicate the rectangular lattice of striped-AFM structure. (c) and (d) Top and side views of ELF of FM 19 - P6/mmm borophene. The unpaired electrons are labeled as number 1 in c and d.

III. RESULTS AND DISCUSSION

To test the reliability and accuracy of this new method, we first investigated 2D CrI₃ system. As shown in Fig. 1a, our calculations demonstrated that the most stable structure has ferromagnetic order and P31m symmetry, and its lattice constants and magnetization (3 μ_B per Cr atom) are in good agreement with the experimental results.² Compared with high-throughput computational screening,^{4,13,14} this search uncovered many new metastable magnetic structures which do not have analogous known parent bulk materials in the database, suggesting that our search is not biased by the database and thus offers a more complete sampling of the configurational space. We then applied this method to borophene. Both magnetic and nonmagnetic borophenes are unveiled in Fig. 1b. Fewer than 300 magnetic borophenes were predicted among 3500 structures in total, after the removal of duplicate structures which were found more than once in the search. We also note that magnetic calculations may be numerically sensitive to the choice of computational parameters, and magnetism of some planar monolavers may disappear in more converged calculations because high density of states (DOS) at the Fermi level can be lowered by structural distortion. Since elemental boron prefers NM state, all magnetic borophenes are metastable phases with respect to its ground-state structure. It is impractical to check the ground state (NM, FM, or AFM) for all magnetic structures because we only focus on several low-energy structures in which ferromagnetism persists, as they are more likely to be synthesized on a suitably chosen substrate. The most stable magnetic structure contains 19 atoms per unit cell (Fig. 2) and is designated as 19 - P6/mmm borophenes according to its symmetry. For 19-P6/mmm borophene



FIG. 5. (color online) (a) Band structure of FM 19 - P6/mmm borophene with the electron doping concentration of $1.2 \times 10^{14} \ cm^{-2}$. (b) Band structure with the electron doping concentration of $4.8 \times 10^{13} \ cm^{-2}$. (c) The variation of relative energy difference between FM and striped-AFM phases by finite electron doping. (d) Phonon dispersion curve of FM 19 - P6/mmm borophene with the doping concentration of 0.02 electrons per atom.

with NM order (NM 19 - P6/mmm borophene), the lattice parameters are a = b = 6.033 Å, and c = 19.97 Å. Three inequivalent atomic positions are B1 (0.0,0.0,0.5), B2 (0.362,0.181,0.5), and B3 (0.576,0.153,0.434), which form triatomic 2.64 Å thick layers (see Figs. 2a and 2b). The middle layer, through which a mirror plane passes, consists of isolated hexagonal B₇ clusters (meanwhile, leading to large empty spaces, see Fig. 2a), while the top and bottom layers, are composed of triangular units, and they connect together to form dodecagonal vacancies on top of the B₇ clusters, which forms particular symmetric voided structure.

The calculated total energies for the 19 - P6/mmmborophene with striped-AFM (Fig. 2c), non-collinear 120° AFM order (ncl-AFM, see Figs. 2a and 2d), FM, and NM states are about -6.162, -6.162, -6.161, and -6.152 eV/atom, which are higher in energies than previously synthesized 2-Pmmn (-6.19 eV/atom), $^{32}\chi_3$ (-6.24 eV/atom),³⁴ β_{12} (-6.23 eV/atom),³⁴ and α -sheet structures (-6.28 eV/atom),²⁰ but are lower in energy than graphene-like borophene (-5.42 eV/atom),³⁵ indicating that 19 - P6/mmm borophene is a metastable structure with the ground-state AFM order. There is only one magnetic atom per unit cell of FM 19 - P6/mmmborophene (Fig. 2a), which is located at the center of B_7 clusters (B1 atoms). The local magnetic moment of each B1 atom is about 1.0 μ_B . The geometry of B1 atoms forms a magnetic triangular lattice and thus many configurations include FM, striped-AFM and ncl-AFM orders are considered (Fig. 2). The calculations show that ncl-AFM phase, which are considerably, by 2.2 meV per



FIG. 6. (color online) Striped-AFM 19-P6/mmm borophene under strain. (a) Calculated total energy vs. strain relation. (b) The Poisson's ratios as a function of uniaxial deformation of striped-AFM structure along x direction. (c) Poisson's ratios as a function of uniaxial deformation of AFM structure along y direction. (d) The lengths of specific B2-B3 bonds as a function of uniaxial tensile strain. The inset shows the x-bonds and y-bonds, which are colored in red and blue respectively.

19 atoms, and 24.5 meV per 19 atoms, lower in energy than those of striped-AFM and FM orders. Therefore, ncl-AFM borophene is the ground-state structure, which is an indirect semiconductor with bandgap of 0.54 eV (Fig. 3a). Moreover, by mapping the DFT energy difference to the classical spin model, the nearest-neighbor exchange parameter J_1 is estimated to be -5.45 meV and the next nearest-neighbor exchange parameter J_2 is ~ -0.14 meV. J_1 is much bigger than J_2 , indicating that 19 - P6/mmm borophene has a ground-state ncl-AFM structure, which is dominated by the AFM J_1 in the triangular lattice. However, under minor electron doping, ncl-AFM phase is less stable than striped-AFM and FM phases, and there is even an AFM-FM transition when doping concentration is higher than ~ 0.006 electrons per atom $(3.6 \times 10^{13} \ cm^{-2})$. Hence the ncl-AFM structure will not be discussed further in subsequent discussions for the doped cases.

Electronic band structure calculations show that NM 19 - P6/mmm borophene is metallic (Fig. 3b). In contrast, striped-AFM and FM 19 - P6/mmm borophenes are semiconductors with an indirect bandgap of 0.41 eV and a direct bandgap of 0.18 eV, respectively (Figs. 3c and 3d). The electronic stability, in terms of DOS at the Fermi level with the order of NM metal < FM or AFM semiconductor, is consistent with the energetic stability. To explore the physical origin of magnetism in striped-AFM borophene, we analyzed the atomic orbital-



FIG. 7. The energy difference of striped-AFM, ncl-AFM refer to FM phases as a function of biaxial tensile (negative) or compressive strain (positive).

resolved band structures as shown in Figs. 3e and 3f. In Fig. 3e, two flat bands around the Fermi level are primarily contributed by the p_z orbitals of magnetic B1 atoms. Between them, one flat band with majority spin is colored in pink, while the other with minority spin is colored in dark blue. Interestingly, there also exist two more flat bands in Fig. 3f, which mainly originate from the other B1 atoms, but their spin characters are opposite. That is, two highest valence bands or two lowest conduction bands (flat bands) with opposite spin electrons are offseted each other (Figs. 3e and 3f) and thus, the whole structure exhibits AFM order. As mentioned above, these flat bands are dominated by the unpaired electrons $(p_z \text{ orbitals})$, which can be confirmed by the spin charge density distribution (Figs. 4a and 4b). Large bubble-like spin density maxima are localized on top of B1 atoms (center of B_7 clusters). These bubbles represent the majority-spin (colored in red) and minority-spin electrons (colored in blue) and have the same size and shape due to mirror symmetry. The special arrangement of spin densities among B1 atoms in the plane are responsible for striped-AFM order. In addition, the electron localization function (ELF) of FM 19 - P6/mmmborophene in Figs. 4c and 4d shows that each B1 atom has an unpaired electron, and consequently has a local magnetic moment of 1 μ_B .

FM 19 – P6/mmm borophene is a direct narrow-gap semiconductor. As see in Fig. 3d, the lowest conduction band with minority spin is very close to the Fermi level along Γ -X and Γ -Y directions, while the conduction band with majority spin is relatively far from the Fermi level. Obviously, it may be tuned from the FM semiconductor to a FM half metal by shifting the Fermi level upward a little, which can be realized by electron doping. Note that a charge doping of 10^{15} cm⁻² had already been experimentally achieved in some 2D materials by a gate-voltage.⁴⁶ For the electron doping concentration of $0.02 \ (1.2 \times 10^{14} \ cm^{-2})$ and $0.008 \ (4.8 \times 10^{13} \ cm^{-2})$ electrons per atom (Figs. 5a and 5b), the bands in the majority and minority spin channels are separated, suggesting intrinsic ferromagnetism. Most importantly, minority spin channels are completely polarized, indicating that 19 - P6/mmm borophene is a half-metal whose majority spin electrons behave like semiconductor, while minority spin electrons display metallic conduction. All of these suggest that this structure may have significant potential applications in spintronics. Figure 5c shows the variation of relative energy difference between FM and striped-AFM phases via the electron doping concentration from 0 to $1.2 \times 10^{14} \ cm^{-2}$. Actually, the 19 - P6/mmmborophene is a ground-state FM half metal above the concentration of 0.006 electrons per atom. We also calculated the phonon dispersion curves with finite electron doping. The absence of imaginary frequencies in the phonon spectrum (Fig. 5d) is suggesting that the structure remains dynamically stable upon doping. Note that the rectangular 19-P6/mmm borophene has a large unit cell and the excess electrons are dominantly distributed on the magnetic B1 atoms in both FM and striped-AFM states, the weak spurious electrostatic interaction can be cancelled out, so the energy differences between the charged FM and striped-AFM states are correct.⁴⁷

Because of the strong covalent B-B networks, borophenes are usually expected to be hard 2D materials, e.g., the in-plane Youngs modulus of 2 - Pmmnborophene (398 GPa·nm along the a axis), potentially rivals graphene (the hardest 2D material) at 340 GPa·nm.^{32,48} It is natural to study the mechanical properties of 19 - P6/mmm borophene with different magnetic states. With its reconstructed rectangular lattice, using the standard Voigt notation, the elastic strain energy per unit area can be expressed as⁴⁹ U_{ϵ} $= (1/2)C_{11}\epsilon_{xx}^2 + (1/2)C_{22}\epsilon_{yy}^2 + C_{12}\epsilon_{xx}\epsilon_{yy} + 2C_{66}\epsilon_{xy}^2,$ where C₁₁, C₂₂, C₁₂, and C₆₆ are the elastic constants, corresponding to second partial derivatives of the energy with respect to strain. The in-plane Young's modulus and Poisson's ratio can be derived from the elastic constants as: $\mathbf{E}_x = (\mathbf{C}_{11}\mathbf{C}_{22}-\mathbf{C}_{12}\mathbf{C}_{21})/\mathbf{C}_{22}, \ \mathbf{E}_y = (\mathbf{C}_{11}\mathbf{C}_{22}-\mathbf{C}_{12}\mathbf{C}_{21})/\mathbf{C}_{22}$ $C_{12}C_{21})/C_{11}$, $\nu_{xy} = C_{21}/C_{22}$, and $\nu_{yx} = C_{12}/C_{11}$. The calculated C_{11} , C_{22} , C_{12} , and C_{66} for striped-AFM 19 - P6/mmm borophene are 227, 227, 143, and 42 GPa·nm, so the Youngs modulus is equal to $E_x = E_y$ = 137 GPa·nm, and the corresponding Poisson's ratio is equal to 0.63 (Fig. 6a), which are much softer than previously reported structures due to its large empty spaces among three layers.^{32,50} In sharp contrast to the positive in-plane Poisson's ratio ($\nu_{xy} = \nu_{yx} = 0.63$), 19 - P6/mmm borophene, regardless of its magnetic order, possesses an unexpected out-of-plane negative Poisson's ratios (NPR) when tensile strain was applied in the x (parallel to the a axis) and y (parallel to b axis) directions. As shown in Figs. 6b and 6c, the out-of-plane strains ϵ_z of striped-AFM 19-P6/mmm borophene have the linear relationship with ϵ_x and ϵ_y , respectively. When

it was compressed, the data were fitted to the function of y = -0.119(-0.269)x in the x (y) direction. Since the out-of-plane Poisson's ratio⁵¹ is defined as ν_{zx} = $-\partial \epsilon_z/\partial \epsilon_x$ or $\nu_{zy} = -\partial \epsilon_z/\partial \epsilon_y$, these results represent positive Poisson's ratios in both directions. While for tension, the data were fitted to the function of y =0.381(0.162)x, so they are $\nu_{zx} = -0.381$ and $\nu_{zy} = -0.162$, showing NPR effect on the contrary, which are different from those of phosphorene or borophane (NPR for both tension and compression only either in the y or in the x direction).^{52,53} The length of specific B2-B3 bonds (named as x-bonds, colored in red, see Fig. 6d) increases under tensile strain along the x direction, so does for the other specific B2-B3 bonds (named as y-bonds, colored in blue, see Fig. 6d) along the y direction. The slope of x-bonds is more than that of y-bonds, implying that xbonds elongate faster than y-bonds upon stretching and resulting in $|\nu_{zx}| > |\nu_{zy}|$. Owing to very similar lattice constants among AFM, FM, and NM states, the ν_{zx} and ν_{zu} of NM (FM) 19 – P6/mmm borophene are -0.416 (-0.379) and -0.194 (-0.167) by using the same methods. Therefore, such exotic buckling bonding configurations are responsible for the NPR effect (see the inset of Fig. 6d). At last, the energy difference of striped-AFM, ncl-AFM refer to the FM phases as a function of biaxial tensile (negative strain) or compressive strain (positive strain) was plotted in Fig. 7. It showed that the striped-AFM structure is the most stable phase among different states between the range of 1% and 3%, while the ncl-AFM structure is the most stable one under biaxial tensile strain.

IV. CONCLUSION

In conclusion, we developed and performed a systematic evolutionary search for stable magnetic borophenes and identified that 19 - P6/mmm borophene is a stable striped-AFM semiconductor, which not only can be further tuned into a half metal, but also has intrinsic outof-plane negative Poisson's ratios. The 19 - P6/mmmborophene may be grown on suitable substrates of metals or transition-metal borides.⁵⁴ If the magnetic borophenes can be realized from experiments, the outstanding properties make it a promising candidate in spintronics and nanoelectromechanical devices simultaneously.

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