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Dirac nodal lines and flat-band surface state in the functional oxide RuO₂

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The efficiency and stability of RuO₂ in electro-catalysis has made this material a subject of intense fundamental and industrial interest. The surface functionality is rooted in its electronic and magnetic properties – determined by a complex interplay of lattice-, spin-rotational, and time-reversal symmetries, as well as the competition between Coulomb- and kinetic energies. This interplay was predicted to produce a network of Dirac nodal lines (DNL), where the valence- and conduction bands touch along continuous lines in momentum space. Here we uncover direct evidence for three DNLs in RuO₂ by angle resolved photoemission spectroscopy (ARPES). These DNLs give rise to a flat-band surface state (FBSS) that is readily tuned by the electrostatic environment, and that presents an intriguing platform for exotic correlation phenomena. Our findings support high spin-Hall conductivities and bulk magnetism in RuO₂, and are likely related to its catalytic properties.

Introduction.—Ruthenium dioxide is a functional semimetal of wide industrial use, in part stemming from its remarkable electronic/ionic conduction properties and favorable thermal and chemical stability¹. RuO₂ is corrosion resistant and its diffusion properties are beneficial for pH and dissolved oxygen sensing electrodes, as e.g. employed in water quality monitoring sensors². Further, due to particularly high Coulombic efficiencies and good mass transport properties, nanoporous RuO₂ is a prototype conversion material in metal oxide lithium-ion battery electrodes³ with high charge storage capacity (supercapacitors)⁴.

The interest in RuO₂ stems also from its efficiency in electro-catalytic processes⁵ – especially in the electrochemical reduction of CO₂ to methanol⁶ and in the industrial recycling of chlorine from HCl (Deacon process)⁷. The RuO₂ (110) surface, in particular, is among the highest performing anodes for the oxygen evolution reaction in photo-electrochemical water splitting and electrolysis⁸. Such qualities can be related to specific properties of the Fermi surface: First principle calculations based on density functional theory (DFT) claim magnetic moments on the RuO₂ surface to be responsible for low overpotentials in the evolution reaction of ground-state magnetic (triplet) oxygen from nonmagnetic water, resulting in high catalytic efficiencies⁹. Such local magnetic moments are confirmed by neutron scattering experiments. and attributed to a spin density wave instability driven by a particularly large density of states at nested 'hot spots' in the Fermi surface¹⁰. These in turn are believed to be the direct consequence of the non-symmorphic symmetry of the rutile RuO₂ crystal structure^{11,12}, establishing an intimate link between the fundamental properties and the surface functionality.

Dirac nodal lines in RuO_2 .—The significance of non-symmorphicity in RuO₂ was recently discussed within the framework of topology and relativistic Dirac physics¹³. Symmetry considerations in conjunction with DFT predicted a network of two types of Dirac nodal lines $(DNL)^{14-23}$, where the valence- and conduction bands touch close to the Fermi level along continuous lines in momentum space: (A) First, time reversaland inversion symmetry in unison with a mirror symmetry protect a band crossing within the (110) and ($\overline{1}10$) planes. This produces a network of 4-fold degenerate $(2 \times \text{spin and } 2 \times \text{orbital})$ and topologically nontrivial DNLs (DNL1)¹³, outlined by blue lines in the Brillouin zone (BZ) of Fig. 1 (a). (B) The second type of DNL in RuO₂ is topologically trivial and protected by a non-symmorphic glide mirror symmetry¹³. In brief, the RuO₂ lattice is a bipartite composition of two sub-lattices with different RuO₆ octahedral orientation that are related by a fractional lattice translation of half a body diagonal and a reflection about the (100) plane. The consequent band-folding gives rise to two sets of bands, producing – in conjunction with time reversal symmetry - fourfold degenerate DNL2s along the $k_x = \pi/a$ and $k_y = \pi/a$ boundary planes of the primitive BZ^{22,24}. In the presence of spin-orbit coupling (SOC) the DNL1s are gapped, which was predicted to result in high spin-Hall conductivities 13 , similar as in IrO_2^{25} . The DNL2s however remain strictly symmetry protected along the XM and MA lines in the BZ (green lines in Fig. 1 a) 13,26 .

This scenario is confirmed by our state-of-the-art ARPES experiments on the (110) surface of slightly n-type, Ir doped RuO₂ (see the Supplemental Material S4²⁷

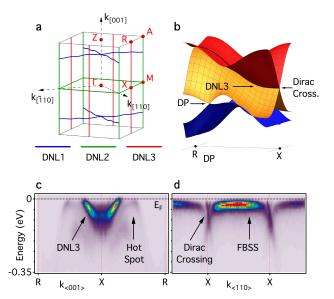


FIG. 1. Dirac nodal lines (DNLs) in RuO₂. a, Brillouin Zone of RuO₂, summarizing the calculated k-space trajectories of the three DNLs. b, DFT band-structure model of RuO₂, showing the 4-fold band crossing of DNL3 along XR, and a Dirac point at DP. c, ARPES map along XR outlining DNL3 and the 'hot spot' states. d, Perpendicular ARPES map, showing the Dirac crossing that forms DNL3, as well as the FBSS.

as well as Refs. 28 and 29), and presents a rare observation of relativistic Dirac Fermions in a functional oxide of genuine industrial use. Even more fascinating, we find evidence for an additional, unexpected DNL3 of type (B) along XR, producing a continuous Dirac crossing at the Fermi level (Fig. 1), and remaining surprisingly intact despite considerable SOC. This DNL3 serves as an anchor line for a non-dispersive FBSS (Fig. 1 d), the analogue of the theoretically predicted drumhead surface state 14,19,30. Its diverging density of states can give rise to novel exotic phenomena such as surface superconductivity³¹, long-range Coulomb interaction³² or graphene-like Landau levels³³, and is likely involved in surface catalytic processes. Finally, we reveal the nested 'hot spot' features in the Fermi surface (Fig. 1 c) that are held responsible for the spin density wave scenario of magnetism in RuO₂¹⁰, and a postulated pillar of its catalytic efficiency⁹.

ARPES in the XR plane.—Our comprehensive ARPES results in Fig. 2 substantiate these claims. Panel (a) shows a Fermi surface taken with $h\nu=69$ eV photon energy and probes the RuO_2 BZ along a (110) plane containing the X and the R high symmetry points (see Fig. 2 c and the Supplemental Material $S3^{27}$). We observe four main spectral contributions, marked in panel (a) and summarized in the schematics of panel (b). (I) First, and most importantly, we observe double arc structures centered at the X points. These represent the two

branches of the Dirac crossing that forms DNL3. The arcs extend towards the zone center, and form a faint onion-dome. (II) Second, we find intense spectral features labeled DP. These are the intersection points of DNL1 with the XR momentum plane, as outlined in panel (c). (III) Third, intense 'hot streaks' mark the projections of DNL1 onto the XR plane. Their intersection with the XR BZ boundary line marks the 'hot spot' features in the Fermi surface, claimed responsible for the magnetic instability in ${\rm RuO_2^{10}}$. (IV) Last, we identify two prominent arcs spanning in between adjacent DNL3s, the signature of the FBSS.

(I)—Let us first discuss the unexpected DNL3 along XR: Fig. 2 (d) shows horizontal band structure cuts for five selected momenta $k_{(001)}$ (outlined in b), revealing the evolution of the Dirac crossing from X towards R. From $k_{(001)} = 0$ (d₁) to ~ 0.25 Å⁻¹ (d₅), the crossing point moves towards lower binding energies (black arrows), and eventually passes the Fermi level at $k_{(001)} \sim 0.28 \text{ Å}^{-1}$. Our DFT calculation in panel (e) $^{34-36}$ reproduces the Dirac crossing in (d₁) astonishingly well, but locates it 0.56 eV above the experimental value of $\sim -0.1 \text{ eV}$, a striking deficit of our simplified DFT approach. The corresponding 3D band structure model of Fig. 1 (b) correctly produces the continuous 4-fold band crossing of DNL3 along XR. The degeneracy however is supposed to be lifted by SOC as seen in Fig. 2 (f). As the degeneracy is strictly symmetry protected along the XM line¹³, the SOC induced splitting effect is weak in the vicinity of the X point and remains unresolved by our ARPES experiment.

(II)—The features labeled DP in Fig. 2 (a) represent the intersection points of DNL1 with the (110) momentum plane, highlighted in panel (c). Both ARPES and DFT reveal the corresponding Dirac crossing in panel (g), but the SOC induced gap remains again unresolved. As with DNL3, theory locates the crossing point about 0.15 eV above the experimental value of -10 meV.

(III)—Fig. 2 (h) shows ARPES cuts along $k_{(001)}$, taken at representative momenta $k_{\langle 110 \rangle}$ as outlined in (b). Next to the features forming the onion-dome, we observe the continuous evolution of the Dirac states at DP in (h₁) towards a band with a hole-like parabolic band maximum at the 'hot spots' in (h_5) , as correctly predicted by DFT (blue in panel i). This evolution is smooth and responsible for the intense 'hot streaks' in the Fermi surface of panel 2 (a), the projection of DNL1 onto the XR momentum plane (see panel c and the Supplemental Material S4²⁷). The nesting of these parallel 'hot streaks' along commensurate nesting vectors, as well as their simultaneous electron- and hole-like character, favors potential Fermi surface instabilities such as spin- or charge density waves. In addition, the intersections of these 'hot streaks' with the XR BZ boundary lines, i.e. the 'hot spots', are symmetry protected by the non-symmorphic glide plane of RuO₂. The 4-fold degeneracy of these bands is thus lifted only by SOC (panel i), and/or by a magnetic spin density wave instability – the claimed origin of magnetic

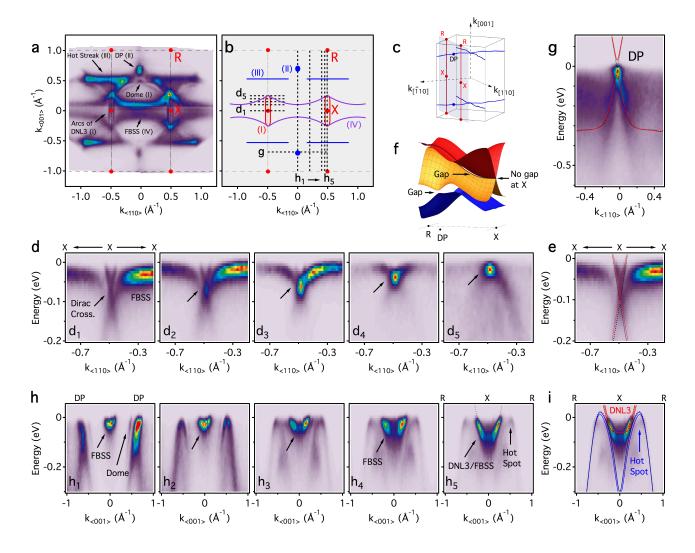


FIG. 2. **ARPES in the XR plane. a**, ARPES Fermi surface measured with 69 eV photons. We mark the high symmetry points (red), the BZ boundaries (black dashed), as well as prominent spectral features (black arrows). **b**, Schematic summary of the Fermi surface in (a). Black dotted lines indicate the position of ARPES cuts in panels (d), (g) and (h). **c**, The RuO2 BZ, focusing on the (110) measurement plane containing the X and R high symmetry points, and its intersection with DNL1 at DP. **d**, Energy dispersion along $k_{\langle 110 \rangle}$, showing the evolution of the Dirac crossing and the FBSS with $k_{\langle 001 \rangle} = 0$ (d₁); =0.1 (d₂); =0.15 (d₃); =0.2 (d₄); =0.25 (d₅). **e**, Shifted (see text) DFT (black dotted) and DFT+SOC (red solid) calculations, compared to the ARPES data of (d₁). **f**, DFT+SOC band-structure model of RuO₂. In comparison to Fig. 1 (b), SOC gaps DNL3 and the DP, but the 4-fold band crossing at X is strictly symmetry protected. **g**, ARPES close up of the Dirac crossing at DP, compared to shifted (see text) DFT (black dotted) and DFT+SOC (red solid) calculations. **h**, Energy dispersion along $k_{\langle 001 \rangle}$ and the evolution of the FBSS with $k_{\langle 110 \rangle} = 0$ (h₁); =0.2 (h₂); =0.4 (h₃); =0.45 (h₄); =0.495 (h₅). Along XR (h₅), the FBSS merges with rDNL3. **i**, Shifted (see text) DFT (black dotted) and DFT+SOC (red solid) calculations, compared to the ARPES data of (h₅). 'Hot spot' bands associated with a Fermi surface instability in Ref. ¹⁰ are shown in blue and did not require an energy correction.

moments in RuO_2^{10} .

(IV)—Last, we return to Fig. 2 (d) and note that these panels also trace the energy dispersion of the FBSS along $k_{\langle 110 \rangle}$, as well as its anchoring in the Dirac crossing. Its photon energy independence (see Supplemental Material S4²⁷), as well as the fact that the bulk DFT description in panel (e) misses this state, clearly demonstrates its surface character. Far away from X, the FBSS remains non-

dispersively flat at ~ -30 meV, but takes a sharp, holelike downward bend to merge with the Dirac crossing at the BZ boundary XR. The ARPES cuts in Fig. 2 (h) present the perpendicular dispersion of the FBSS at the BZ center (h₁), and trace its evolution with $k_{\langle 110 \rangle}$ (h₂₋₄) as it integrates into the DNL3 in (h₅). Along XR (h₅), DNL3 and the FBSS produce an electron-like parabolic dispersion (black dotted line), with a ~ 0.1 eV band bot-

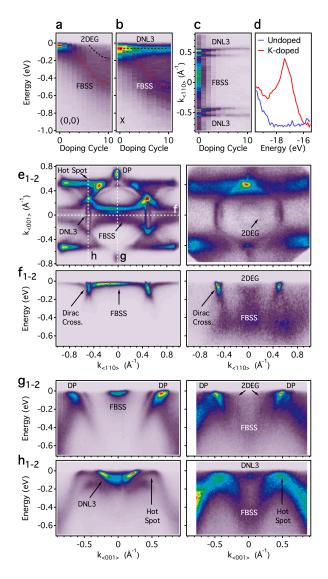


FIG. 3. **Doping evolution of the FBSS. a**, EDC at $(k_{\langle 110\rangle}, k_{\langle 001\rangle}) = (0,0)$, **b**, EDC at $(k_{\langle 110\rangle}, k_{\langle 001\rangle}) = (0.495,0)$ Å⁻¹ (X), and **c**, MDC at $k_{\langle 001\rangle} = 0$, all measured in situ with 69 eV photons as a function of potassium deposition. **d**, K 1s core level measurements before (1) and after deposition (2). **e**, Fermi surfaces and **f-h**, ARPES band structures along paths indicated in (e₁), before (1) and after (2) K-deposition.

tom and $m^* \sim 2.5 m_e$ effective mass, well mimicked by the DFT bands (red) in panel (i). The simultaneous electronand hole character, as well as the diverging density of states of the FBSS, are clear hallmarks of a saddle-point van Hove singularity.

Doping evolution of the FBSS.—The spanning and anchoring of the FBSS in between adjacent DNL3s, as well as its flat energy dispersion, suggest this state to represent the analogue of the drumhead surface state predicted in systems with closed contour DNLs^{14,30}. To test its robustness, we deposit potassium at the surface while

monitoring the ARPES response in situ. An overview of the results is presented in Fig. 3. Panels (a) and (b) show the continuous doping evolution of energy distribution curves (EDC) at $(k_{\langle 110 \rangle}, k_{\langle 001 \rangle}) = (0,0)$ and at the X point, respectively. With increasing electron doping, the FBSS considerably broadens and disperses to ~ -0.43 eV (red dashed in Fig. 3 a,b). The states associated with DNL3 populate only slightly (black dashed in Fig. 3 b), producing the Fermi surface bifurcation in the momentum distribution curve (MDC) of panel (c).

Panel (d) shows the K 1s core level peak, panels (e-h) show the ARPES data before and after potassium deposition, respectively. With respect to the pre-deposition Fermi surface in (e₁), the post-deposition Fermi surface (e₂) reveals overall broader and fuzzier spectral weight. However, whereas the bulk derived spectral contributions related to DNL3 (I), DP (II), and the 'hot spot' states (III) remain intact, the FBSS disappears and gives way to the faint circular contours of a gas of itinerant surface electrons (2DEG). The dispersion of the FBSS along $k_{(110)}$ (white dashed line marked 'f' in e_1) before and after deposition is shown in panels (f_1) and (f_2) , respectively. Dropping to higher binding energy, the FBSS produces broad but robust spectral weight at ~ -0.43 eV, while the 2DEG forms a broad parabolic line shape close to E_F . The drop of the FBSS is reproduced in panels (g) along $k_{(001)}$ (marked 'g' in e_1). The bulk band derived Dirac crossing at DP however stays remarkably intact. In panels (h), the 'hot spot' states gain overall spectral weight with respect to DNL3, seemingly connect to the FBSS, and form a continuous M-shaped like band contour along $k_{\langle 001 \rangle}$ (marked 'h' in e_1).

The sensitive response of the FBSS to surface doping indicates a significant loss of coherence in response to changes in the electrostatic environment. While the potassium induced surface disorder plays only a minor role, we believe this effect to result from augmented scattering of the FBSS with quasi-particles from the metallic bulk of ${\rm RuO_2}^{30}$. Indeed, such scattering is greatly enhanced for van Hove singularities, which enhance the Coulomb interaction and correlation of the surface electrons³². Thus, even in the presence of relatively weak perturbations, we may expect exotic symmetry broken states such as surface magnetism³⁰, surface superconductivity³¹, or graphene-like Landau levels³³, whose experimental exploration we leave for a further study.

Finally, it is intriguing to speculate why the additional DNL3 escaped earlier DFT and symmetry investigations¹³. For one, we note that DFT of pure and Ir doped RuO₂ consistently misses the correct binding energy of the relevant bands by significant values (at X: 0.56 eV; at DP: 0.15 eV; see also the Supplemental Material S5²⁷), and consequently out of reach of the Fermi level. This is a consequence of the oversimplified DFT description of the correlated Ru 4d manifold in RuO₂. Unlike in 5d rutile oxides like IrO₂^{37,38}, the common neglect of correlation effects in 4d transition metal com-

pounds is hence not entirely justified. Further, SOC is expected to split the DNL3s along XR, an effect that we found to be weak and beyond the resolving power of our experiment. This is in remarkable analogy to the well studied system graphene, a predicted quantum spin Hall insulator³⁹, which in view of low SOC presents itself – like RuO_2 – as a de facto Dirac semi-metal⁴⁰.

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