



CHORUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

NMR study of optically hyperpolarized phosphorus donor nuclei in silicon

P. Gumann, H. Haas, S. Sheldon, L. Zhu, R. Deshpande, T. Alexander, M. L. W. Thewalt, D. G. Cory, and C. Ramanathan

Phys. Rev. B **98**, 180405 — Published 16 November 2018

DOI: [10.1103/PhysRevB.98.180405](https://doi.org/10.1103/PhysRevB.98.180405)

NMR study of optically hyperpolarized phosphorus donor nuclei in silicon

P. Gumann,^{1,2,3,*} H. Haas,^{2,3,†} S. Sheldon,^{1,2} L. Zhu,⁴ R. Deshpande,^{2,3}
T. Alexander,^{2,3,‡} M.L.W. Thewalt,⁵ D.G. Cory,^{2,6,7} and C. Ramanathan^{4,§}

¹IBM T.J. Watson Research Center, Yorktown Heights, NY 10598 USA

²Institute for Quantum Computing, University of Waterloo, Waterloo, Ontario N2L 3G1 Canada

³Department of Physics and Astronomy, University of Waterloo, Waterloo, Ontario N2L 3G1 Canada

⁴Department of Physics and Astronomy, Dartmouth College, Hanover, NH 03755 USA

⁵Department of Physics, Simon Fraser University, Burnaby, British Columbia V5A 1S6 Canada

⁶Department of Chemistry, University of Waterloo, Waterloo, Ontario N2L 3G1 Canada

⁷Perimeter Institute for Theoretical Physics, Waterloo, Ontario N2L 2Y5 Canada

(Dated: October 8, 2018)

We use above-bandgap optical excitation, via a 1047 nm laser, to hyperpolarize the ^{31}P spins in low-doped ($N_D = 6 \times 10^{15} \text{ cm}^{-3}$) natural abundance silicon at 4.2 K and 6.7 T, and inductively detect the resulting NMR signal. The 30 kHz spectral linewidth observed is dramatically larger than the 600 Hz linewidth observed from a ^{28}Si -enriched silicon crystal. We show that the broadening is consistent with previous ENDOR results showing discrete isotope mass effect contributions to the donor hyperfine coupling. A secondary source of broadening is likely due to variations in the local strain, induced by the random distribution of different isotopes in natural silicon. The nuclear spin T_1 and the build-up time for the optically-induced ^{31}P hyperpolarization in the natural abundance silicon sample were observed to be 178 ± 47 s and 69 ± 6 s respectively, significantly shorter than the values previously measured in ^{28}Si -enriched samples under the same conditions. We measured the T_1 and hyperpolarization build-up time for the ^{31}P signal in natural abundance silicon at 9.4 T to be 54 ± 31 s and 13 ± 2 s respectively. The shorter build-up and nuclear spin T_1 times at high field are likely due to the shorter electron-spin T_1 , which drives nuclear spin relaxation via non-secular hyperfine interactions. At 6.7 T, the phosphorus nuclear spin T_2 was 16.7 ± 1.6 ms at 4.2 K, a factor of 4 shorter than in ^{28}Si -enriched crystals. This was observed to shorten to 1.9 ± 0.4 ms in the presence of the infrared laser.

Phosphorus-doped silicon (Si:P) is a technologically important material in quantum applications^{1–5}, as the donor spins have some of the longest coherence times observed for any solid-state spin system^{6,7}. The growth of isotopically-enriched ^{28}Si crystals, where local magnetic field fluctuations due to the ^{29}Si are eliminated, has enabled dramatically longer electronic⁷ and nuclear⁸ donor spin coherence times.

Natural silicon consists of 3 isotopes: ^{28}Si , ^{29}Si and ^{30}Si , whose relative abundances are 92.23%, 4.67% and 3.1% respectively. While ^{29}Si is a spin-1/2 nucleus, ^{28}Si and ^{30}Si are spin-0 nuclei. In addition to suppressing spin-induced magnetic field noise, isotope engineering of silicon — originally enabled by the Avogadro Project⁹ — has improved our understanding of silicon physics. Photoluminescence^{10,11} and ESR^{12–14} experiments on boron-doped ^{28}Si and natural silicon have shown that the random distribution of silicon isotopes causes local changes to the valence band in the vicinity of the boron acceptor. The broad EPR lines observed at low doping concentrations in natural silicon were attributed to a distribution of local strain fields induced by the random spatial distribution of different isotopes¹⁴. For shallow group-V donor states, changes in the electron-nuclear hyperfine interaction have been observed with electron-nuclear double resonance (ENDOR) to correlate with the host crystal isotope mass distribution¹⁵, though the microscopic mechanisms underlying this effect are still unclear.

Directly studying the spin properties of phosphorus nu-

clei at low donor concentrations has been a challenge. Given the low sensitivity of NMR measurements, direct inductive detection of phosphorus nuclear spins in silicon has previously only been possible at very high doping concentrations ($\sim 10^{18} \text{ cm}^{-3}$)^{16,17}. We recently demonstrated a direct inductive readout of the phosphorus NMR signal from an isotopically-enriched, ^{28}Si -sample with a ^{31}P donor concentration in the range of 10^{15} cm^{-3} , following hyperpolarization with a non-resonant infrared laser¹⁸. The inductively detected NMR data complemented results from optically¹⁹ and electrically⁸ detected experiments on ^{31}P at similar dopant concentrations. Here, we utilize optical hyperpolarization and direct inductive readout to characterize the properties of ^{31}P spins in a natural silicon crystal, and contrast the results with data from ^{28}Si -enriched samples.

Figure 1 shows the normalized NMR spectra obtained from ^{28}Si (red) and natural silicon (blue) samples. The spectrum from the ^{28}Si sample was recorded with 16 averages, and an optical hyperpolarization time of 400 s, whereas the spectrum from the natural silicon sample was acquired with 256 averages, with an optical hyperpolarization time of 250 s. Both spectra were obtained using a commercial Bruker Avance NMR Spectrometer at 6.7 T and 4.2 ± 0.3 K. Under these conditions, the thermal electron spin polarization is 79 %. We probed the nuclear spins in the lower electron spin manifold, with a transition at 174 MHz, where the thermal nuclear spin polarization is 0.1 %. The length of the $\pi/2$ pulse used was 2.5 μs . The optical excitation was performed with a

150 mW, 1047 nm, above-bandgap laser, with a linearly polarized beam of 9 mm effective size. The (indirect) bandgap in silicon is 1.17 eV which corresponds to an optical wavelength of 1059 nm²⁵. The penetration depth for 1047 nm light in silicon at cryogenic temperatures is a few centimetres which allowed the excitation of bulk phosphorus donors throughout the sample²⁶.

Similar sized ²⁸Si and natural silicon samples, measuring $2 \times 2 \times 8$ mm³, were mounted in a strain-free configuration. The ²⁸Si sample was a dislocation-free crystal²⁴ with a phosphorus donor concentration of 1.5×10^{15} cm⁻³, while the natural silicon sample was a float-zone grown commercial silicon sample (Topsil) with a phosphorus donor concentration of 6×10^{15} cm⁻³. The boron concentration in both samples was less than 1.0×10^{14} cm⁻³. Both samples were etched in HF/HNO₃ before the experiments. We also confirmed the same natural silicon linewidth after annealing and etching another separate sample cut from the same crystal. In each case, the samples were placed in a silver plated copper, *RF*-coil, connected to a resonant, low temperature *LC*-circuit. Home-built NMR probes were then immersed into commercial, liquid helium dewars with a set of optical, sapphire windows located at the bottom of each dewar, and aligned with the main B_0 magnetic field of both magnets.

The ³¹P-spectra from the ²⁸Si-enriched sample is observed to have a linewidth of 600 Hz, while the linewidth of the natural silicon crystal is substantially broader, about 30 kHz. Such considerable changes have previously been observed in ESR-detected ENDOR spectra of Si:P samples with varying silicon isotopic concentration. In order to understand the difference in the observed linewidths, it is useful to consider the effective Hamiltonian for an isolated phosphorus donor impurity at high magnetic field:

$$\mathcal{H} = -\gamma_n B_z I_z - \gamma_e B_z S_z + \frac{2\pi}{\hbar} A S_z I_z + \mathcal{H}_n^d,$$

where $\gamma_n/2\pi = 17.23$ MHz/T and $\gamma_e/2\pi = -28.024$ GHz/T are the nuclear and electron gyromagnetic ratios, $A = 117.5$ MHz is the nominal strength of the isotropic hyperfine interaction, and \mathcal{H}_n^d represents the magnetic dipolar coupling between the phosphorus nucleus and other electronic and nuclear spins in the system. At high field the eigenstates are almost exactly given by the product states $|\uparrow_e \uparrow_n\rangle$, $|\uparrow_e \downarrow_n\rangle$, $|\downarrow_e \uparrow_n\rangle$, $|\downarrow_e \downarrow_n\rangle$ ²⁰. The resonance frequency for a nuclear spin transition is given by $\gamma_n B_z \pm \pi A$, corresponding to frequencies of 174.08 MHz and 56.58 MHz respectively. As noted above, the experiments shown here were performed on the larger 174.08 MHz transition, which corresponds to the $|\downarrow_e\rangle$ manifold. At our temperature and field values a thermalized electron spin occupies the $|\downarrow_e\rangle$ state 90% of the time. At low doping concentrations, the largest contribution to \mathcal{H}_n^d in natural silicon is the phosphorus-silicon dipolar coupling, which we estimate to be on the order of 200 Hz in a natural abundance crystal – about twice the strength of the observed silicon-silicon dipolar linewidth

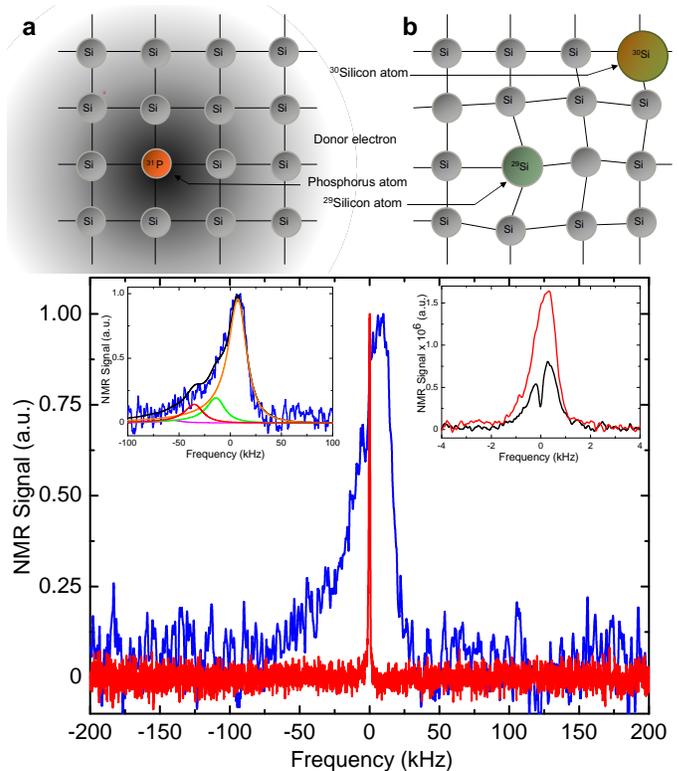


FIG. 1. Schematic representation of (a) a uniform ²⁸Si-enriched crystal, and (b) a natural silicon lattice containing ²⁸Si, ²⁹Si and ³⁰Si atoms. The 2 nm Bohr radius of the shallow ³¹P donor electron extends over a large number of silicon lattice sites. The main plot below shows normalized ³¹P NMR spectra from ²⁸Si (red) and natural silicon (blue) samples, measured at 6.7 T and 4.2 K. A 1 kHz exponential line broadening has been applied to the spectrum from the natural silicon sample and a 100 Hz line broadening to the spectrum from the ²⁸Si sample. The left inset shows a comparison of the observed NMR spectrum for natural silicon (shown in blue) and a simulation of the lineshape (shown in black) expected from the mass effect model¹⁵. The inset also shows the 4 largest relative contributions from $M_{NN} \approx 28$ (orange), $M_{NN} \approx 28.25$ (green), $M_{NN} \approx 28.5$ (pink), and $M_{NN} \approx 28.75$ (red). The right inset shows the result of an NMR hole-burning experiment on the ²⁸Si sample, with a 10 s long saturation pulse using a weak 3 Hz Rabi frequency, indicating the inhomogeneous nature of the spectral line. The width of the spectral hole is about 200 Hz.

in natural silicon²¹. This is insufficient to explain the observed broadening.

It is apparent that any variation in the hyperfine strength A will cause a shift in the observed NMR line. The hyperfine interaction strength A is given by

$$A = \frac{2}{3} \frac{\mu_0}{\hbar} \gamma_e \gamma_n |\psi(0)|^2$$

where $\psi(0)$ is the magnitude of the electronic wavefunction at the ³¹P nucleus²⁰. Isotope variations can result in both local symmetry breaking²² as well as change the effective mass of the electron, resulting in changes to $\psi(0)$

and the hyperfine interaction strength. In previous EN-DOR experiments on a series of crystals with different silicon isotopic compositions, the observed spectra were seen to strongly correlate with the isotopic composition of the host lattice¹⁵. Though they were unable to provide a complete microscopic understanding of the phenomena, two distinct effects were observed: a discrete dependence on the isotopic composition, and a residual continuous broadening. For the discrete dependence the authors extracted the following relation for the variation of hyperfine interaction strength(s) with isotopic composition:¹⁵

$$A = A_{28} + \alpha_{\text{NN}} (M_{\text{NN}} - M_{28}) + \alpha_{\text{bulk}} (M_{\text{bulk}} - M_{28}),$$

where A_{28} is the ^{31}P hyperfine interaction in a ^{28}Si -enriched lattice, M_{NN} is the average mass of the four nearest-neighbor silicon isotopes, M_{28} is the mass of ^{28}Si and M_{bulk} is the average bulk isotopic mass.

For the ^{28}Si samples, there should be little to no variation in A , as observed in the experiment. The nuclear spin T_2 for the ^{31}P in ^{28}Si has been measured to be 56 ms ¹⁸, suggesting that most of the 600 Hz broadening arises from local magnetic field inhomogeneities. The right inset shows the result of an NMR hole-burning experiment with a 10 s long saturation pulse using a weak 3 Hz Rabi frequency. The width of the spectral hole is about 200 Hz. It should be noted that the relative intensities for the two spectra in this inset are arbitrary as the experimental parameters, such as polarization time and sampling periods were optimized independently for each spectra.

The left inset to Figure 1 shows a comparison of the observed NMR spectrum for natural silicon (shown in blue) and a simulation of the lineshape (shown in black) expected from this model. Zero and first order phase corrections to the experimental data were adjusted to yield the best fit to the model lineshapes. The natural silicon spectrum was also shifted by -1 kHz to optimize the fit. This shift is consistent with small frequency shifts that we observe for the ^{28}Si -enriched sample spectra between different experimental runs, which happen due to changes in sample positioning. The model uses the experimentally measured¹⁵ parameters $\alpha_{\text{NN}} = -170 \text{ kHz/u}$ and $\alpha_{\text{bulk}} = 117 \text{ kHz/u}$, and the isotopic masses in natural silicon to find the peak centers. Each peak is convolved with the same anisotropic Lorentzian lineshape function⁴¹ used by Sekiguchi *et al.*¹⁵, with a linewidth of 22.45 kHz and asymmetry parameter 3.2×10^{-5} .

There are 9 possible values for M_{NN} starting from $M_{\text{NN}} = M_{28} = 27.9769265325 \text{ u}$ ⁴², and increasing in steps of 0.25 u to $M_{\text{NN}} \approx 30 \text{ u}$. The inset also shows the 4 largest relative contributions from $M_{\text{NN}} \approx 28$ (orange), $M_{\text{NN}} \approx 28.25$ (green), $M_{\text{NN}} \approx 28.5$ (pink), and $M_{\text{NN}} \approx 28.75$ (red). There is good agreement for both the center of the line with respect to the ^{28}Si data, and the width of the spectrum.

The residual broadening captured by the anisotropic Lorentzian lines is most likely due to strain-induced hyperfine changes due to the random isotope distribution,

which were originally studied by Wilson and Feher²², and recently re-explored by Mansir *et al.*²³ The random distribution of different isotopes has been observed to result in a broad distribution of strain fields in boron-doped silicon ESR studies¹⁴.

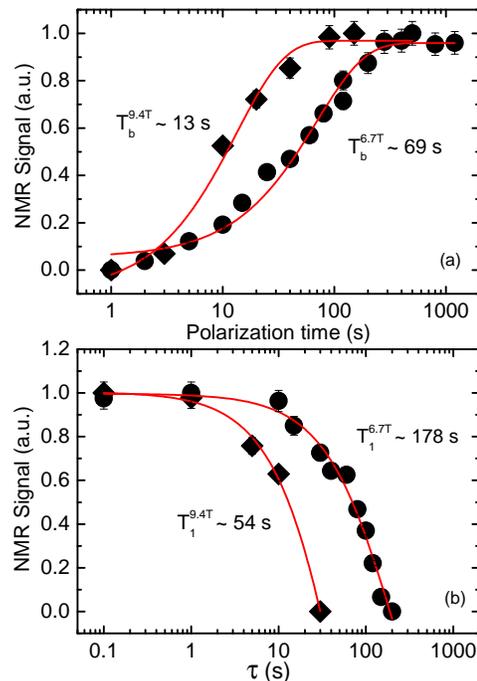


FIG. 2. (a) Build-up of the hyperpolarized ^{31}P signal at 9.4 T (black diamonds) and 6.7 T (black circles) in natural silicon as a function of illumination time (τ) using a 1047 nm laser. The normalized data were fit to the function: $1 - \exp(-\tau/T_b)$, to find the characteristic build-up times $T_b^{9.4T} = 13 \pm 2 \text{ s}$, and $T_b^{6.7T} = 69 \pm 6 \text{ s}$. (b) Decay of the optically hyperpolarized ^{31}P signal in natural silicon at 9.4 T (black diamonds) and 6.7 T (black circles), yielding T_1 relaxation times of $T_1^{9.4T} = 54 \text{ s}$ and $T_1^{6.7T} = 178 \text{ s}$ respectively. For both subplots, the maximum signal at the two magnetic fields has been normalized to have a value of one since our experiments did not provide the magnitude of spin polarization.

We also compared the properties of the optically-induced ^{31}P NMR signal at two different magnetic fields, 6.7 T and 9.4 T. At 9.4 T and 4.2 K the equilibrium electron spin polarizations is 91%. The NMR experiments were once again performed on the larger 220.7 MHz transition which has a thermal equilibrium polarization of 0.13%. The experiments at 9.4 T used 3 different pieces from the natural silicon crystal, while the build-up and relaxation experiments at 6.7 T used two pieces from the same crystal. A similar broad NMR line was observed at 9.4 T (data not shown).

Figure 2(a) shows the build-up of the ^{31}P -spin polarization accomplished by illuminating the sample with a lower power 100 mW, 1047 nm laser. The build-up curves of the optical hyperpolarization were measured by increasing the laser excitation time (or polarization time), from 1 s to 16 minutes for the 6.7 T data set,

and from 1 s to 100 s for the 9.4 T results. We were able to fit the build-up curves using a single exponential with characteristic times of 13 ± 2 s at 9.4 T and 69 ± 6 s at 6.7 T fields. The thermal equilibrium polarization could not be measured, making it difficult to directly quantify either the sign or the magnitude of the nuclear spin polarization. Previous ESR measurements have reported a negative nuclear spin polarization following optical hyperpolarization^{18,27}.

Figure 2(b) shows the results of T_1 relaxation measurements at the two fields. The data were recorded using a 200 s laser polarization pulse, followed by a delay time τ , during which the laser was turned off, and a $\pi/2$ -readout pulse. Both data sets are fit with a single exponential decay, yielding $T_1^{6.7T} = 178 \pm 47$ s and $T_1^{9.4T} = 54 \pm 31$ s. The observed build-up times also depend on the optical coupling of the light to the sample in a given experiment, which could vary depending on laser alignment and sample positioning.

The observed build up and relaxation times for the natural silicon samples are significantly shorter than the 577 s build-up time and 712 s ^{31}P nuclear T_1 relaxation time measured at 6.7 T and 4.2 K for the ^{28}Si -enriched sample¹⁸. While the phosphorus concentration in the natural silicon samples is about 4 times higher, it is known that for donor concentrations below 10^{16} cm^{-3} , the electron spin T_1 is independent of donor concentration,^{33,37} at least at a magnetic field of around 0.3 T. At low fields ^{28}Si isotopic enrichment does not appear to change the electron spin T_1 times either³³. However, it has also been demonstrated²⁸ that matching the larger hyperfine-shifted phosphorus Larmor frequency to the ^{29}Si Larmor frequency (at 2.8 T) induces an efficient resonant spin polarization transfer from ^{31}P to ^{29}Si nuclei. In our experiment the smaller 56.58 MHz hyperfine shifted ^{31}P resonance is only 50 kHz shifted from the ^{29}Si Larmor frequency. Given the relatively short T_1 of the donor electrons (10s of ms), the ^{31}P nuclear spin transition is near resonant with the ^{29}Si spins for about 10% of the time, when the donor is in this higher excited manifold, potentially shortening the nuclear spin T_1 . Isotopic variations could also modify the phonon spectrum, which could be important in the optical hyperpolarization process.

The shorter build-up and nuclear T_1 times at high field are likely due to the shorter electron-spin T_1 at high field, which in turn, drives nuclear spin relaxation via non-secular hyperfine interactions³⁴. The direct electron spin-phonon relaxation process is expected to scale with temperature and field as $T_1^{-1} \propto B^5 \coth\left(\frac{\hbar\gamma B}{k_B T}\right)$. At 4.2 K, we expect $\hbar\gamma B \ll k_B T$, and $T_1^{-1} \propto B^4 T$.²⁹⁻³² In the presence of light, the electron T_1 is known to be further shortened by up to two orders of magnitude driven by the creation of non-thermal resonant phonons, photoionization and photoneutralization due to exciton capture processes^{35,36}, exchange interaction with photocarriers³⁷ and trapping and re-emission of electrons³⁸, with T_1 mea-

sured to be on the order of 2 ms in the presence of light and almost 20 ms in the dark at 8.56 T^{38,40}.

Figure 3 shows the results of spin-echo experiments performed to measure the coherence time of the ^{31}P nuclear spins, following 200 s of laser irradiation. The higher-power 150 mW 1047 nm laser was used for the optical excitation here. We measured the signal decay with the laser off and on, and fit the data to a single exponential decay to obtain nuclear spin T_2 values of 16.7 ms and 1.9 ms for the two cases respectively, very close to the electronic T_1 values measured previously at high fields^{38,40}. In the absence of light the Hahn-echo T_2 in natural silicon is about a factor of 4 shorter than the 56 ms T_2 observed with ^{28}Si , due to the presence of the magnetically-active ^{29}Si spins and potentially because of the higher dopant concentration which reduces the electron T_1 , and consequently the nuclear spin T_2 . The order of magnitude change in T_2 (16.7 ms to 1.9 ms) measured in the presence of light is likely due to the rapid modulation of the electron spins when the light is on, which results in local field fluctuations.

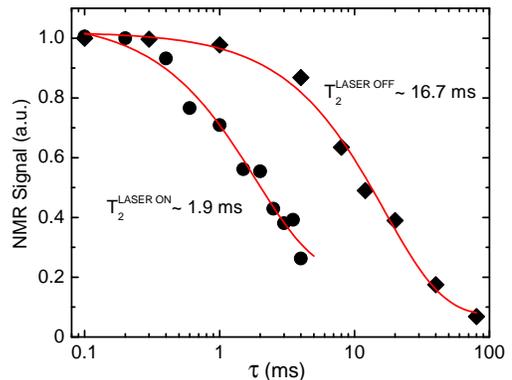


FIG. 3. ^{31}P nuclear spin coherence time, T_2 , in natural silicon measured with the Hahn echo at 4.2 K temperature, 6.7 T field. For the black circles the laser was kept ON during acquisition, $T_2 = 1.9 \pm 0.4$ ms while for the black diamonds the laser was turned OFF during the acquisition, $T_2 = 16.7 \pm 1.6$ ms. All data were measured with Hahn echo, with 150 s of optical polarization provided by a 1047 nm, and 150 mW, above-gap laser.

Non-resonant optical hyperpolarization of donor nuclei provides an important new tool to probe their local magnetic environment, allowing us to measure isotope mass effects and strain-induced broadening due to the random distribution of isotopes in natural silicon. We found that both the build-up time for the optical hyperpolarization and the nuclear-spin T_1 for natural silicon are dramatically shorter than for ^{28}Si at 6.7 T. In our experiments the 56.58 MHz hyperfine shifted ^{31}P resonance lies only 50 kHz away from the ^{29}Si Larmor frequency and could therefore be yielding a shortened T_1 .

This work was undertaken thanks in part to funding from the the Canada First Research Excellence Fund (CFREF). Further support was provided by the

Canada First Research Excellence Fund (CFREF), the Natural Sciences and Engineering Research Council of Canada (NSERC), the Canada Excellence Research Chairs (CERC) Program, the Canadian Institute for Ad-

vanced Research (CIFAR), the province of Ontario and Industry Canada. L.Z and C.R acknowledge support from the NSF under Grant No. CHE-1410504.

P.G and H.H contributed equally to this work.

-
- * gumann@us.ibm.com
† hhaas@uwaterloo.ca
‡ Now at IBM Q
§ chandrasekhar.ramanathan@dartmouth.edu
- ¹ B. E. Kane, *Nature* **393**, 133 (1998).
 - ² T. D. Ladd, J. R. Goldman, F. Yamaguchi, Y. Yamamoto, E. Abe and K.M. Itoh, *Phys. Rev. Lett.* **89**, 017901 (2002).
 - ³ A. R. Stegner, C. Boehme, H. Huebl, M. Stutzmann, K. Lips, M. S. Brandt, *Nature Physics*, **2**, 835?838 (2006).
 - ⁴ A. Laucht, J. T. Muhonen, F. A. Mohiyaddin, R. Kalra, J. P. Dehollain, S. Freer, F. E. Hudson, M. Veldhorst, R. Rahman, G. Klimeck, and K.M. Itoh, *Science Advances* **1**, e1500022 (2015).
 - ⁵ C. C. Lo, M. Urdampilleta, P. Ross, M. F. Gonzalez-Zalba, J. Mansir, S. A. Lyon, M. L. W. Thewalt, J. J. L. Morton, *Nature Materials*, **14** 490 (2015).
 - ⁶ A. M. Tyryshkin, J. J. L. Morton, S. C. Benjamin, A. Ardavan, G. A. D. Briggs, J. W. Ager, and S. A. Lyon, *J. Phys.: Condens. Matter* **18**, S783 (2006).
 - ⁷ A. M. Tyryshkin, S. Tojo, J. J. L. Morton, H. Riemann, N. V. Abrosimov, P. Becker, H. J. Pohl, T. Schenkel, M. L. Thewalt, K. M. Itoh, and S. A. Lyon, *Nature Materials*, **11**, 143 (2012).
 - ⁸ K. Saeedi, S. Simmons, J. Z. Salvail, P. Dluhy, H. Riemann, N. V. Abrosimov, P. Becker, H. J. Pohl, J. J. L. Morton, M. L. Thewalt, *Science*, **342**, 830 (2013).
 - ⁹ B. Andreas, Y. Azuma, G. Bartl, P. Becker, H. Bettin, M. Borys, I. Busch, M. Gray, P. Fuchs, K. Fujii, H. Fujimoto, E. Kessler, M. Krumrey, U. Kuetgens, N. Kuramoto, G. Mana, P. Manson, E. Massa, S. Mizushima, A. Nicolaus, A. Picard, A. Pramann, O. Rienitz, D. Schiel, S. Valkiers, A. Waseda, *Phys. Rev. Lett.* **106**, 030801 (2011).
 - ¹⁰ D. Karaiskaj, M. L. W. Thewalt, T. Ruf, M. Cardona, and M. Konuma, *Phys. Rev. Lett.* **89**, 016401 2002.
 - ¹¹ D. Karaiskaj, G. Kirczenow, M. L. W. Thewalt, R. Buczko, and M. Cardona, *Phys. Rev. Lett.* **90**, 016404 2003.
 - ¹² H. Tezuka, A. R. Stegner, A. M. Tyryshkin, S. Shankar, M. L. W. Thewalt, S. A. Lyon, K. M. Itoh, and M. S. Brandt, *Phys. Rev. B* **81**, 161203 (2010).
 - ¹³ A. R. Stegner, H. Tezuka, T. Andlauer, M. Stutzmann, M. L. W. Thewalt, M. S. Brandt, and K. M. Itoh, *Phys. Rev. B* **82**, 115213 (2010).
 - ¹⁴ A. R. Stegner, H. Tezuka, H. Riemann, N. V. Abrosimov, P. Becker, H.-J. Pohl, M. L. W. Thewalt, K. M. Itoh, and M. S. Brandt, *Applied Physics Letters* **99**, 032101 (2011).
 - ¹⁵ T. Sekiguchi, A.M. Tyryshkin, S. Tojo, E. Abe, R. Mori, H. Riemann, N.V. Abrosimov, P. Becker, H.-J. Pohl, J.W. Ager, E.E. Haller, M.L.W. Thewalt, J.J.L. Morton, S.A. Lyon, and K.M. Itoh, *Phys. Rev. B* **90**, 121203 (2014).
 - ¹⁶ H. Alloul and P. Dellouve, *Phys. Rev. Lett.* **59**, 587 (1987).
 - ¹⁷ M. Jeong, M. Song, T. Ueno, T. Mizusaki, A. Matsubara, and S. Lee, *J. Phys.:Conference Series* **150**, 042078 (2009).
 - ¹⁸ P. Gumann, O. Patange, C. Ramanathan, H. Haas, O. Moussa, M. L. W. Thewalt, H. Riemann, N.V. Abrosimov, P. Becker, H. J. Pohl, K.M. Itoh, D.G. Cory, *Phys. Rev. Lett.* **113**, 267604 (2014).
 - ¹⁹ M. Steger, T. Sekiguchi, A. Yang, K. Saeedi, M. E. Hayden, M. L. W. Thewalt, K. M. Itoh, H. Riemann, N. V. Abrosimov, P. Becker, and H.-J. Pohl, *J. Appl. Phys.* **109**, 102411 (2011).
 - ²⁰ A. Schweiger and G. Jeschke, *Principles of Pulse Electron Paramagnetic Resonance*, Oxford University Press, New York (2001).
 - ²¹ B. Christensen and J. C. Price, *Phys. Rev. B* **95**, 134417 (2017).
 - ²² D. K. Wilson and G. Feher, *Phys. Rev.* **124**, 1068 (1961).
 - ²³ J. Mansir, P. Conti, Z. Zeng, J. J. Pla, P. Bertet, M. W. Swift, C. G. Van de Walle, M. L. W. Thewalt, B. Sklenard, Y. M. Niquet, and J. J. L. Morton, *Phys. Rev. Lett.* **120**, 167701 (2018).
 - ²⁴ P. Becker, H.J. Pohl, H. Riemann, and N. Abrosimov, *Physica Status Solidi (a)* **207**, 49 (2010).
 - ²⁵ W. Bludau, A. Onton, and W. Heinke, *J. Appl. Phys.* **45**, 1846 (1974).
 - ²⁶ G. G. MacFarlane *et al.* , *J. Phys. Chem. Solids* **8**, 388 (1959).
 - ²⁷ D. R. McCamey, J. van Tol, G. W. Morley, C. Boehme, *Phys. Rev. Lett.* **102**, 027601 (2009).
 - ²⁸ P. Dluhy, J. Z. Salvail, K. Saeedi, M. L. W. Thewalt, and S. Simmons, *Phys. Rev. B* **91**, 195206 (2015).
 - ²⁹ A. Honig and E. Stupp, *Phys. Rev. Lett.* **1**, 275 (1958).
 - ³⁰ A. Honig and E. Stupp, *Phys. Rev.* **117**, 69 (1960).
 - ³¹ H. Hasegawa, *Phys. Rev.* **118**, 1523 (1960).
 - ³² L. M. Roth, *Phys. Rev.* **118**, 1534 (1960).
 - ³³ A. M. Tyryshkin, S. A. Lyon, A. V. Astashkin, A. M. Rait-simring, *Phys. Rev. B* **68**, 350 (2003).
 - ³⁴ D. Pines, J. Bardeen, and C.P. Slichter, *Phys. Rev.* **106**, 489 (1957).
 - ³⁵ J. R. Haynes, *Phys. Rev. Lett.* **4**, 361 (1960).
 - ³⁶ M. L. W. Thewalt, *Can. J. Phys.* **55**, 1463 (1977).
 - ³⁷ G. Feher and E. A. Gere, *Phys. Rev.* **114**, 1245 (1959).
 - ³⁸ G.W. Morley, D. R. McCamey, H. A. Seipel, L-C. Brunel, J. Van Tol, and C. Boehme, *Phys. Rev. Lett.* **101**, 207602 (2008).
 - ³⁹ D. R. McCamey, J. Van Tol, G. W. Morley, and C. Boehme, *Science* **330**, 1652 (2010).
 - ⁴⁰ D. R. McCamey, C. Boehme, G. W. Morley, J. van Tol, *Phys. Rev. B* **85**, 073201 (2012).
 - ⁴¹ A. L. Stancik and E. B. Brauns, *Vib. Spectrosc.* **47**, 66-69 (2008).
 - ⁴² G. Audi, A. H. Wapstra, C. Thibault, *Nuc. Phys. A*, **729**, 337-676 (2003)