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Phys. Rev. B **98**, 155128 — Published 16 October 2018

DOI: [10.1103/PhysRevB.98.155128](https://doi.org/10.1103/PhysRevB.98.155128)

Sr₃Ir₂O₇F₂: Topochemical conversion of a relativistic Mott state into a spin-orbit driven band insulator

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The topochemical transformation of single crystals of Sr₃Ir₂O₇ into Sr₃Ir₂O₇F₂ is reported via fluorine insertion. Characterization of the newly formed Sr₃Ir₂O₇F₂ phase shows a nearly complete oxidation of Ir⁴⁺ cations into Ir⁵⁺ that in turn drives the system from an antiferromagnetic Mott insulator with a half-filled $J_{eff} = 1/2$ band into a nonmagnetic $J = 0$ band insulator. First principles calculations reveal a remarkably flat insertion energy that locally drives the fluorination process to completion. Band structure calculations support the formation of a band insulator whose charge gap relies on the strong spin-orbit coupling inherent to the Ir metal ions of this compound.

PACS numbers:

I. INTRODUCTION

Topochemical transformations have long been harnessed to control the properties of a broad array of quantum materials. Post growth transformations of bulk single crystals are often utilized to achieve a number of unconventional electronic states ranging from quantum spin liquids¹ to charge density waves² to superconductivity³. The power of this approach is its utility in modifying the properties of an existing crystal framework to realize ground states and properties^{4,5} otherwise precluded from conventional synthetic methods⁶.

One area of interest is the potential of exploring new electronic states in spin-orbit assisted Mott materials. These are systems where the interplay between strong crystal field energies, spin-orbit coupling, and on-site Coulomb interactions cooperate to stabilize a Mott insulating state comprised of spin-orbit entangled electrons⁷. Control over carrier concentrations⁸ and dimensionality/bandwidth⁹ in these systems are key to realizing many of the new states predicted^{10–12}; however these degrees of freedom are often constrained by the solubility limits of conventional dopants and the structural stabilities of the host lattices¹³.

Modifying the host lattices of these unusual spin-orbit Mott insulators via topochemical transformations has recently shown promise. Chemical reactions driving postgrowth transformations have stabilized spin liquid formation^{1,14}, unconventional metallic phases,¹⁵ as well as new magnetic phases¹⁶. However, utilizing similar techniques to control the Ir valence and lattice dimensionality of the $n = 1$ and $n = 2$ members of the Ruddlesden-Popper (R.P.) series of strontium iridates Sr_{*n*+1}Ir_{*n*}O_{3*n*+1}, the seminal examples of spin-orbit assisted Mott states, remains notably unexplored.

The development of novel routes of controlling the electronic states and lattice architectures of R.P. strontium

iridates is of interest for a variety of reasons. For instance, doping holes into Sr_{*n*+1}Ir_{*n*}O_{3*n*+1} is a proposed route to realizing unconventional superconductivity¹⁷ and controlling the relative spacing between IrO₆ planes is a potential mechanism for controlling their unusual magnetic ground states.¹⁸ Trivial alloying of these systems to explore these effects has proven severely limited by solubility bounds¹⁹ as well as disorder effects associated with perturbing the IrO₆ planes^{20,21}. To this end, an appealing alternate approach of controlling the dimensionality and valence of Sr_{*n*+1}Ir_{*n*}O_{3*n*+1} compounds is through postgrowth reaction with fluorine gas. Prior studies of bilayer ($n = 2$) 3*d* and 4*d* transition metal oxide R.P. phases⁶ demonstrate a common instability of this structure to the incorporation of F[−] anions and suggest that similar techniques may be leveraged within their 5*d* cousins.

Here we report the fluorine-driven transformation of Sr₃Ir₂O₇ crystals into Sr₃Ir₂O₇F₂, which in turn raises the valence of Ir ions in the lattice from Ir⁴⁺ to Ir⁵⁺ and drives the system from an antiferromagnetic $J_{eff} = 1/2$ Mott state into a nonmagnetic $J = 0$ spin-orbit driven band insulator. Soft postgrowth reaction of Sr₃Ir₂O₇ crystals in a low temperature fluorine environment drives a rapid expansion of the unit cell's long-axis (by $\approx 16\%$) as F[−] ions intercalate within the SrO rocksalt layers of the structure. The reaction diffuses to completion (incorporating two F atoms per formula unit) throughout the bulk of the crystal due to a low insertion energy and shallow chemical potential gradient with increasing F content. Experimental data combined with first principles calculations characterize the resulting Sr₃Ir₂O₇F₂ state as a highly distorted spin-orbit driven insulator, and our combined results demonstrate Sr₃Ir₂O₇F_{*x*} as a unique material that can be driven from a $J_{eff} = 1/2$ into a $J = 0$ spin-orbit entangled ground state.

II. EXPERIMENTAL DETAILS

A. Crystal growth

Single crystals of $\text{Sr}_3\text{Ir}_2\text{O}_7$ were grown via a halide flux growth technique similar to earlier reports^{8,22}. Starting powders of SrCO_3 , IrO_2 , and SrCl_2 were mixed in a 1:1:15 molar ratio and placed inside of a platinum crucible with a lid. The mixture was then reacted at 1300 °C for 5 hours and slowly cooled to 850 °C over 125 hours. Plate-like single crystals (typical size $1 \times 1 \times 0.3$ mm) were then removed from the flux by etching the resulting boule with deionized water.

B. Fluorination of $\text{Sr}_3\text{Ir}_2\text{O}_7$

Once single crystals were extracted from the boule, their phase purity was verified with x-ray diffraction measurements, and crystals were then loaded into an alumina boat and buried within CuF_2 powder. The crucible was placed inside of a tube furnace under argon gas flow and heated to 250 °C over the course of 30 minutes. This temperature was then held for 2 hours and the reaction was stopped by quenching the crucible in air. For reaction times substantially less than this, crystals were found to be mixed phase containing both the $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ and $\text{Sr}_3\text{Ir}_2\text{O}_7$ structures, and for reaction times appreciably greater than this, samples began to show local decomposition into SrF_2 . We note here that similar fluorination could be achieved via reaction in sealed quartz ampoules containing XeF_2 , indicating that the F insertion process is driven via exposure to F_2 gas and not a more complicated process of anion exchange involving direct contact with the CuF_2 .

C. Neutron and x-ray diffraction measurements

Neutron diffraction measurements were performed on the HB3A diffractometer at the High Flux Isotope Reactor at Oak Ridge National Laboratory. A Si-220 monochromator (1.546 Å) was utilized and a 2D Anger camera detector collected the scattering intensity. All data were corrected for neutron absorption through WinGX²³ and refined via the FullProf software package²⁴. The minimum neutron transmission was 0.7085 for the (0 0 4) reflection and the maximum neutron transmission was 0.82662 for (2 0 0) reflection with an average transmission of 0.78414. X-ray powder diffraction data were collected on powder samples comprised of crushed crystals and were collected on an Panalytical Empyrean Powder Diffractometer with a Cu source. Single crystal x-ray data were collected on a Kappa Apex II Diffractometer with a Mo source ($\lambda = 0.71073$ Å).

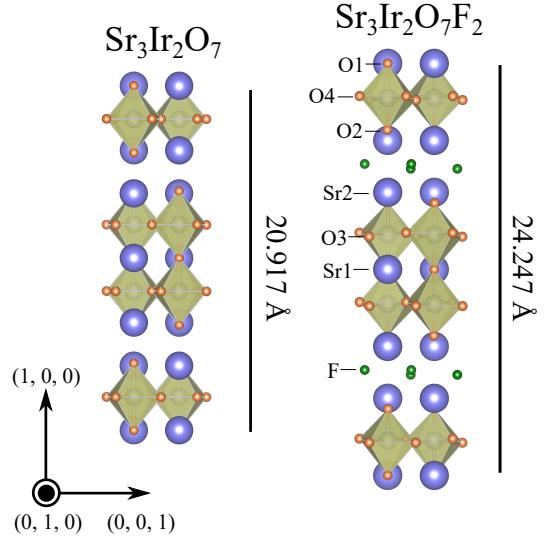


FIG. 1: Illustration of the crystallographic unit cells of $\text{Sr}_3\text{Ir}_2\text{O}_7$ and $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$. IrO_6 octahedra are shaded and purple spheres denote Sr atoms. Green spheres denote the positions of intercalated F^- anions. The long axis of the parent monoclinic unit cell expands by 16% upon incorporation of two F atoms per formula unit into the crystal matrix.

D. Charge transport/magnetization

Charge transport measurements were performed in a Quantum Design Physical Property Measurement System (DynaCool PPMS) with an AC resistance bridge. Crystals were mounted in a four wire configuration and silver paint used to create contacts. Transport data were collected with current flowing within the bc -plane. Magnetization measurements were performed within a SQUID-based Quantum Design Magnetic Property Measurement System (MPMS3), and crystals were mounted on a quartz paddle with a small drop of varnish. Magnetization data were collected with the field applied within the bc -plane.

E. Optical conductivity measurements

Optical reflectivity measurements were also performed to characterize the electronic structure of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$. The bc -plane reflectivity spectra $R(\omega)$ was measured in the energy region between 5 meV and 1 eV by using an in-situ overcoating technique²⁵. The complex dielectric constant between 0.74 eV and 5 eV was obtained by using a spectroscopic ellipsometer, and the complex optical conductivity $\sigma(\omega) = \sigma_1(\omega) + i\sigma_2(\omega)$ was determined via a Kramers-Kronig analysis²⁶.

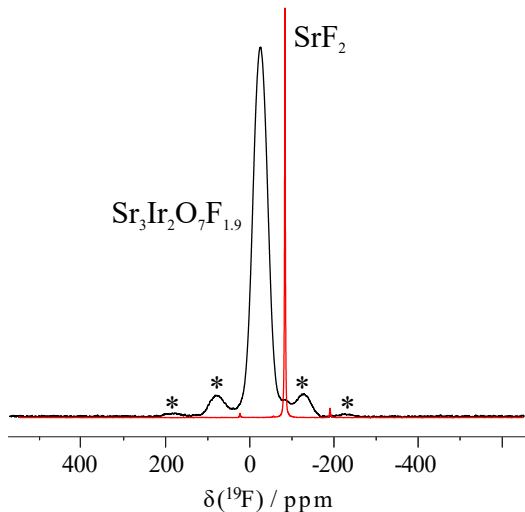


FIG. 2: ^{19}F spin echo NMR spectra illustrating a dominant F environment with a chemical shift of $\delta = 25.1$ ppm in a measurement of crushed $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ crystals. Asterisks denote spinning sidebands associated with this peak. A weak secondary signal is observed at $\delta = 88$ ppm beneath the centerband and the sideband of the primary site, which matches the shift expected for a SrF_2 -like F environment. The black line denotes data for $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ and the red line denotes data for the reference SrF_2 .

F. X-ray Absorption Measurements

X-ray absorption spectroscopy (XAS) measurements were performed at Beamline A2 at CHESS. Crushed single crystals were prepared on three layers of Kapton tape, with an average sample thickness corresponding to nearly two absorption lengths. Measurements were collected at the Ir L_2 ($2p_{1/2} \rightarrow 5d$) and L_3 ($2p_{3/2} \rightarrow 5d$) absorption edges. The energy of the incident x-ray beam was selected using a double-crystal diamond (1, 1, 1) monochromator. XAS measurements were performed at room temperature in transmission geometry to directly measure the linear x-ray attenuation coefficient, $\mu(E)$, using a series of three ion chambers. The sample was mounted between the first two, and IrO_2 powder was mounted between the last two ion chambers as a reference to ensure the energy calibration did not drift.

G. NMR measurements

^{19}F NMR data were acquired at room temperature on a Bruker Advance 500 MHz (11.7 T) wide-bore NMR spectrometer and at a Larmor frequency of -470.6 MHz. The data were obtained under 50 kHz magic angle spinning (MAS) using a 1.3 mm double-resonance probe. ^{19}F chemical shifts were referenced against lithium fluoride ($\delta = -204$ ppm). The spin echo spectra were acquired on SrF_2 and $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_x$ samples using a 90° RF pulse of 2.0 μs and a 180° RF pulse of 4.0 μs at 76.3 W. Recycle de-

lays of 200 s and 12 s were used for SrF_2 and $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_x$ samples, respectively. A ^{19}F probe background spin echo spectrum, acquired under the same conditions as the spin echo spectrum of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_x$ samples but on an empty 1.3 mm rotor, revealed no significant background signal. Lineshape analysis was carried out using the SOLA lineshape simulation package within the Bruker Topspin software.

H. DFT modeling

Theoretical results utilized density functional theory (DFT) within the *Vienna Ab-initio Simulation Package* (VASP)²⁷, using the projector-augmented-wave method²⁸ and the Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional²⁹. Spin-orbit coupling was included via the non-collinear spinor method implemented in VASP. The DFT+ U ³⁰ method was used to take into account correlation effects, and the U value is chosen to be 1.6 eV, based on constrained random-phase-approximation calculations from Ref. 31. This value was previously found to give a good description of the band structure and other electronic properties of Sr-327³².

III. RESULTS AND DISCUSSION

A. Structural analysis

Following reaction of $\text{Sr}_3\text{Ir}_2\text{O}_7$ crystals within a bed of CuF_2 powder, the reacted crystals were initially ground into a powder and checked with x-ray diffraction to explore whether the reaction spanned the bulk of the crystals. Powder data collected from crushed crystals refined with a Le Bail fit to a global structure in space group $C2/c$ with $a = 24.2068(1)$, $b = 5.45033(8)$, $c = 5.50633(7)$, $\alpha = 90$, $\beta = 90.032(1)$, $\gamma = 90$. This is consistent with the large a -axis expansion expected for the transformation from $\text{Sr}_3\text{Ir}_2\text{O}_7$ into $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ depicted in Fig. 1. Notably, the crushed crystals reacted under optimized conditions provide a powder with one unique a -axis lattice parameter, indicating a diffusion of F throughout the bulk of the crystals and with no unreacted $\text{Sr}_3\text{Ir}_2\text{O}_7$ remaining.

To further parameterize the insertion of fluorine, quantitative ^{19}F NMR spectra were collected on a SrF_2 standard and on a collection of crushed $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_x$ single crystals to determine the F stoichiometry of the material. NMR spectra are plotted in Fig. 2 and reveal one major F environment with a chemical shift of $\delta = 25.1$ ppm, consistent with the F ions inserted between the interstitial Sr atoms; however a weak secondary peak is also apparent between the centerband and first sideband of the primary F environment. The position of this minor F resonance matches with the chemical shift $\delta = 88$ ppm expected for a SrF_2 -like local environment³³. For samples more aggressively fluorinated (longer exposure

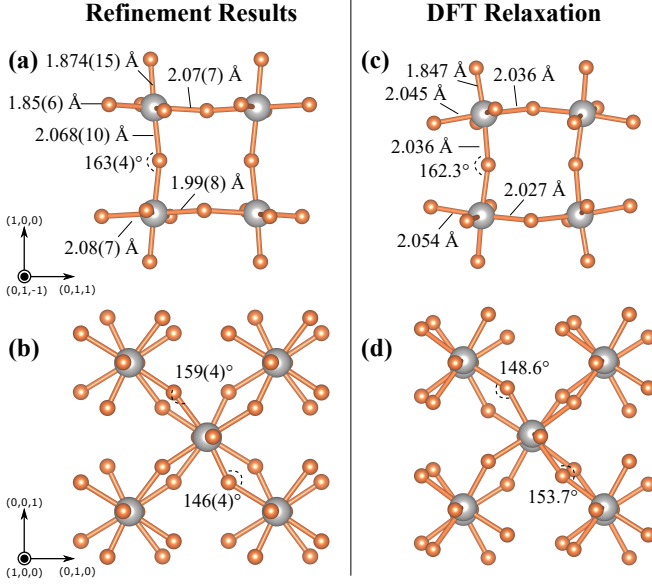


FIG. 3: Illustration of the IrO_6 octahedra, Ir-O bond lengths, and Ir-O-Ir bond angles determined via (a),(b) x-ray/neutron diffraction and (c),(d) DFT structural relaxation calculations.

times), the small secondary resonance grows in relative intensity and reflects an eventual decomposition of the sample under prolonged exposure to fluorine.

Under the optimized conditions reported here, the average fluorine content of the crushed crystals is measured to be $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_{1.9}$ and the secondary SrF_2 -like environment was too weak to be reliably quantified (ie. $< \approx 3\%$ molar fraction). This small secondary peak could arise from either a slight overexposure to F_2 gas or from residual contamination of CuF_2 on the surface of one of the crystals crushed for analysis. Given this uncertainty and the inability to perform NMR measurements on the volume of a single small crystal, we will reference the compound as $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ for the purposes of this paper. As will be shown later, this is supported by DFT calculations which demonstrate that the fully intercalated compound containing two F atoms per formula unit is the most stable, and any F deficiencies averaged across of crystal likely arise from phase separated $\text{Sr}_3\text{Ir}_2\text{O}_7$ regions.

A single $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ crystal was also measured with a combination of single crystal x-ray and neutron diffraction, and the structure was refined in the same twinned $C2/c$ unit cell as the parent $\text{Sr}_3\text{Ir}_2\text{O}_7$ material.³⁴ As the crystal volumes are small and the mosaics of crystals are broadened following F insertion, the neutron data were collected with the high flux neutron wavelength (1.546 Å) that limits the accessible reciprocal space for precisely determining the atomic displacement parameters. The neutron data was therefore analyzed in two ways: (1) by applying a constraint fixing the Sr and Ir positions to those determined initially via the x-ray data and (2) by allowing all atomic positions to refine freely. Atomic positions determined via the two methods were consistent

TABLE I: Table of atom positions determined at 298 K using single crystal neutron and x-ray diffraction data within space group $C2/c$. Isotropic thermal parameters are listed in units of 10^{-3} \AA^2 . While isotropic thermal parameters were refined for x-ray data, neutron data were used to refine the atomic positions with constrained atomic displacements due to the limited accessible reciprocal space with 1.546 Å. These parameters were fixed at $3.8 \times 10^{-3} \text{ \AA}^2$ for Ir and Sr sites and $6.33 \times 10^{-3} \text{ \AA}^2$ for O and F sites for neutron refinement. Fit results yielded weighted $R_{F2} = 0.074$, $\chi^2 = 0.776$ for x-ray data and weighted $R_{F2} = 0.078$, $\chi^2 = 3.07$ for neutron data.

Atom	site	x_{xray}	y_{xray}	z_{xray}	U_{iso}
Ir	8f	0.58430(3)	0.7653(8)	0.7501(3)	5.2(3)
Sr1	4e	0.50000	0.225(2)	0.75000	10.1(12)
Sr2	8f	0.68705(9)	0.7790(15)	0.2503(6)	11.3(9)
O1	4e	0.50000	0.708(12)	0.75000	16(11)
O2	8f	0.6611(6)	0.803(6)	0.754(4)	5(6)
O3	8f	0.0890(13)	0.410(13)	0.447(10)	31(11)
O4	8f	0.0794(11)	0.962(14)	0.551(10)	23(8)
F	8f	0.2558(12)	0.505(8)	0.003(12)	16(4)

Atom	site	$x_{neutron}$	$y_{neutron}$	$z_{neutron}$	U_{iso}
Ir	8f	0.5872(8)	0.768(13)	0.741(7)	3.8
Sr1	4e	0.50000	0.210(15)	0.7500	3.8
Sr2	8f	0.6871(10)	0.755(16)	0.243(12)	3.8
O1	4e	0.50000	0.72(2)	0.75000	6.33
O2	8f	0.658(2)	0.800(14)	0.740(18)	6.33
O3	8f	0.0699(15)	0.488(13)	0.533(16)	6.33
O4	8f	0.088(2)	0.933(13)	0.589(15)	6.33
F	8f	0.252(8)	0.509(9)	0.00000	6.33

within error and the unconstrained refinement yielded better weighted R_{F2} and χ^2 fit parameters. While neutron diffraction is sensitive to the scattering from both O and F atoms, there is minimal scattering contrast in the coherent neutron cross sections between them. Hence, F atoms were assumed to only occupy the same interstitial sites within the SrO planes as those identified in previous studies of $\text{Sr}_3\text{Ru}_2\text{O}_7\text{F}_2$ ³⁵; an assumption consistent with NMR data identifying a single F environment and the known expansion of the a -axis upon F insertion.

Metal-oxygen and metal-fluorine bond lengths and bond angles determined via neutron diffraction agreed within error with the those of x-ray measurements, and the atomic positions are summarized in Table 1. The x-ray refined structure is shown in Fig. 3 with the local oxygen octahedral environments and Ir-O-Ir bond angles are labeled. The data reveal highly distorted IrO_6 octahedra with apical O sites closest to the F anions substantially compressed toward the Ir positions. The spacing of Ir sites between the planes of a bilayer remains unchanged upon F insertion (4.0880(15) Å for $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$, 4.084(2) Å for $\text{Sr}_3\text{Ir}_2\text{O}_7$), consistent with a model of F incorporated only in the planes between bilayers.

A key difference between the parent material and the fluorinated compound is in the local iridium environments, where a strong deviation away from local cubic symmetry arises. This can be parameterized via a distortion parameter for $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ of $\Delta_d = \frac{1}{6} \sum_{n=1,6} [(d_n -$

$d_{avg})/d_{avg}]^2 = 0.014$ where d_n is summed over individual Ir-O bond lengths and d_{avg} is the average Ir-O bond length. Once F is inserted, this Δ_d becomes over an order of magnitude larger than the $\Delta_d = 0.00066$ of the parent compound³⁴ and presages a departure from the cubic limit.

The experimentally determined structure for $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ was further compared with a relaxed unit cell determined via DFT and plotted in Fig. 3. The local IrO_6 octahedral environments in the theoretical and experimental structures agree reasonably well with one another, where the apical Ir-O2 bond length contracts and the Ir-O1-Ir interlayer bond angle is substantially distorted away from 180° . The expected positions of the F ions and the phasing of the octahedral distortions also mirror one another, and the modified long-axis lattice parameter $a_{exp} = 24.24690 \text{ \AA}$ determined via single crystal x-ray measurements is close to the predicted value $a_{exp} = 24.42624 \text{ \AA}$. However, the DFT structure also predicts a larger orthorhombicity $b_{DFT} = 5.46711 \text{ \AA}$ and $c_{DFT} = 5.70697 \text{ \AA}$ than that observed experimentally $b_{exp} = 5.45539 \text{ \AA}$ and $c_{exp} = 5.48889 \text{ \AA}$, and notable differences appear between the measured and calculated values for the in-plane Ir-O3 bond length. While twinning effects and disorder in the average structure of the crystal may account for some discrepancies, differences in the experimental b and c lattice parameters of the order predicted by DFT were not observed in either our x-ray or neutron diffraction measurements.

B. Electronic Properties of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$

Electron transport and magnetization measurements were performed on single crystals of both $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ and $\text{Sr}_3\text{Ir}_2\text{O}_7$ in order to characterize the evolution of the electronic ground state as the iridium valence is shifted from Ir^{4+} to Ir^{5+} . Temperature dependent resistivity data with current flowing within the basal bc -plane are plotted in Fig. 4 (a). The F intercalated system remains an insulator, and comparison with the resistivity of the crystal prior to fluorination shows that the room temperature resistivity increases by over two orders of magnitude. This implies an enhanced charge gap, and the weak divergence of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$'s resistivity upon cooling likely stems from in-gap impurity states due to disorder within the crystal introduced during the fluorination process. Resistivity data did not fit to standard Arrhenius or variable-range hopping forms of transport.

Exploring the gap structure further, optical conductivity measurements are plotted in Fig. 4 (b). In $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$, a charge gap appears with a slow build up of conductivity with a broad peak centered at 1.5 eV (labeled peak A) and a second, higher energy, feature at 2.5 eV. In comparing the optical conductivity data with unfluorinated $\text{Sr}_3\text{Ir}_2\text{O}_7$, the lower energy transitions between the lower and upper Hubbard bands of the

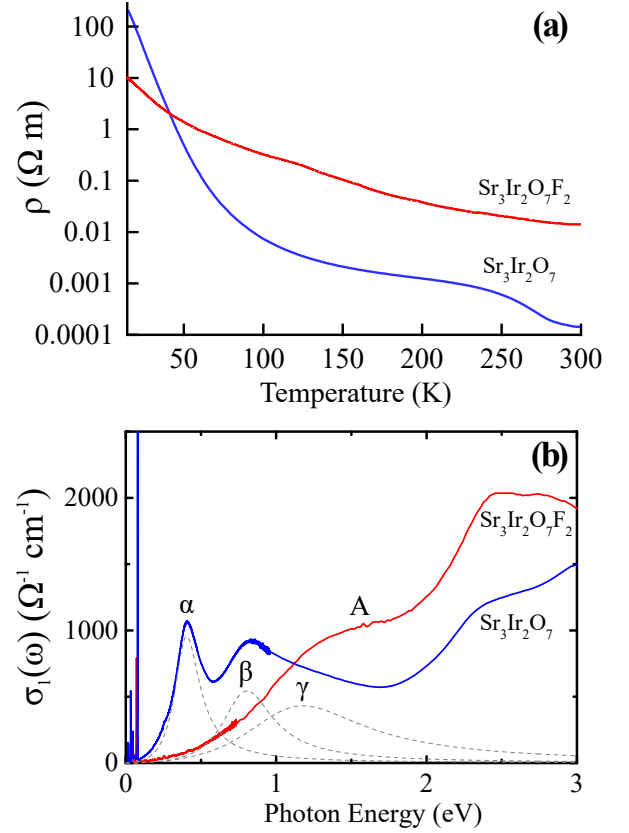


FIG. 4: (a) DC charge transport measured as a function of temperature for both $\text{Sr}_3\text{Ir}_2\text{O}_7$ and $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$. (b) Optical conductivity measured at room temperature for both $\text{Sr}_3\text{Ir}_2\text{O}_7$ and $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$. α , β , and γ transitions are the expected transitions for the $J_{eff} = 1/2$ Mott state of $\text{Sr}_3\text{Ir}_2\text{O}_7$ as described in the text, and the “A” peak is labeled as the dominant excitation in $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$.

$J_{eff} = 1/2$ manifold (α) and the transitions from the $J_{eff} = 3/2$ band into the upper Hubbard band (β and γ) are suppressed. Instead, the F-intercalation seemingly drives the formation of a larger gap within the t_{2g} manifold while the higher energy spectral features for $E > 2$ eV are similar between the two compounds.

Naively, in the single-ion limit, the formation of a $J = 0$ state should have excited states with a first excited triplet $J = 1$ band and a higher $J = 2$ energy level. The splitting of these states should be on the order of $\lambda \approx 0.2 \text{ eV}$ and $3\lambda \approx 0.6 \text{ eV}$ respectively, assuming a value for the spin-orbit coupling strength $\xi = 0.4 \text{ eV}$ where $\lambda = \frac{\xi}{2S}$.⁷ The band picture is considerably more complex, where the system's departure from the ideal limit of a cubic crystal field at Ir-sites as well as intermixing of oxygen states in the valence and conduction bands requires careful modeling. Furthermore, the optical conductivity spectrum of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ revealing the single inherently broad “A” peak is subject to selection rules of intersite hopping terms, which can potentially mask any lower energy bands.

At a minimum, the optical data demonstrate the formation of a band insulating phase as the system transitions from an $5d^5$ into a $5d^4$ valence state. To test whether or not this insulating state is reflective of a $J = 0$ ground state whose character is primarily driven via the strong spin-orbit coupling inherent to the Ir^{5+} cations, x-ray absorption measurements (XAS) were performed. XAS data collected at the Ir L_3 and L_2 absorption edges are plotted in Fig. 5 (a) and illustrate an L_3/L_2 branching ratio of 6.2 ± 0.7 —an enhanced value consistent with the addition of holes and of strong spin-orbit effects in the electronic structure of this material^{36,37}. Using the average number of six $5d$ holes, this value can be converted to a measurement of $\langle L \cdot S \rangle = 3.5 \pm 0.3 [\hbar^2]$.³⁶ This value is again comparable to those observed in spin-orbit driven $J_{\text{eff}} = 1/2$ Mott insulating iridates and suggests that the distortion of the IrO_6 octahedra in $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ is insufficient to appreciably broaden the bandwidth by mixing the spin-orbit split t_{2g} bands (or alternatively by quenching the orbital moment of the t_{2g} manifold entirely). As a result, the electronic ground state is consistent with the $J = 0$ state expected from a low-spin d^4 valence in a cubic crystal field.

Magnetization measurements collected on a single crystal are plotted in Fig. 5 (b). Naively, a $J = 0$ ground state should exhibit only a weak Van Vleck paramagnetic response with quenched local moments. Our magnetization measurements are consistent with this expectation with the addition of a weak Curie-Weiss term that appears at low temperature. The data were fit to the form $\chi(T) = \frac{C}{T - \Theta_W} + \chi_0$ with values $\chi_0 = 1.329 \times 10^{-7} \frac{\mu_B}{\text{Oe Ir}}$ and a Curie constant $C = 9.227 \times 10^{-7} \frac{\mu_B \text{K}}{\text{Oe Ir}}$ yielding an effective moment of $0.203 \pm 0.002 \mu_B$ and Weiss temperature $\Theta_W = -2.5 \pm 0.3 \text{ K}$. This weak local moment response is commonly observed in Ir^{5+} octahedrally coordinated compounds^{38,39} and often arises from a dilute concentration of magnetic impurities, such as local Ir^{4+} $J_{\text{eff}} = 1/2$ moments. This is consistent with the majority of local moments being quenched within the $J = 0$ state that forms in the low spin d^4 manifold.

Assuming $1.73 \mu_B$ per $J_{\text{eff}} = 1/2$ impurity moment in the sample, the measured μ_{eff} would imply a 1.4% concentration of remaining $J_{\text{eff}} = 1/2$ moments. To further verify this, the field dependence of the magnetization was measured at 2 K and the $M(H)$ data are plotted in the inset of Fig. 5 (b). These data are well fit by the Brillouin function expected for isolated $J_{\text{eff}} = 1/2$ moments with a weak linear slope ($7.5 \times 10^{-4} \frac{\mu_B}{\text{kOe}}$) arising from the temperature independent Van Vleck and background contributions. The saturation value for the Brillouin function fit is found to be $0.014 \pm 0.004 \mu_B \text{ Ir}^{-1}$, in excellent agreement with the Curie-Weiss response expected to arise from a 1.4% concentration of $J = 1/2$ impurity moments.

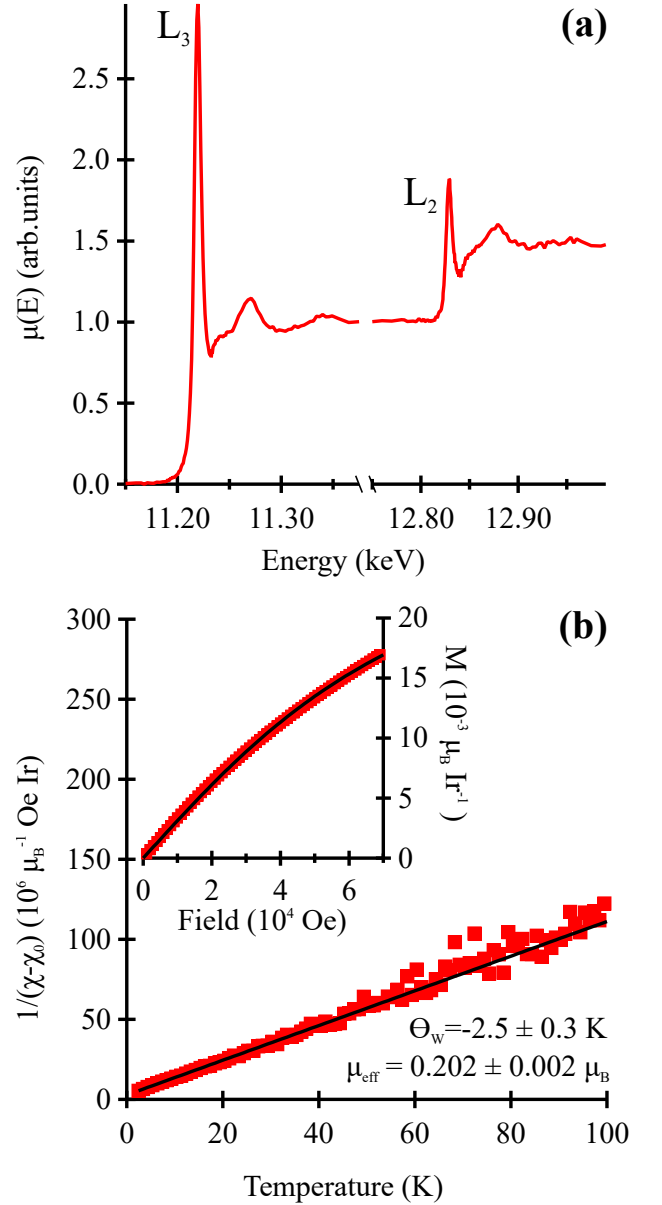


FIG. 5: (a) X-ray absorption data showing the measured $\mu(E)$ at both the Ir L_3 and L_2 absorption edges. (b) Inverse susceptibility $(\chi - \chi_0)^{-1}$ plotted as a function of temperature. The temperature independent term in the susceptibility χ_0 (comprised of the Van Vleck paramagnetic and background terms) has been removed to isolate the local moment response. The resulting Curie-Weiss fit is shown as the black line through the data with values detailed in the text. The inset shows field dependence of the magnetization collected at 2 K. The solid line is a fit to a $J = 1/2$ Brillouin function with a weak linear background as described in the text.

C. *Ab initio* modeling of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$

The formation of the $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ structure was explored via calculations of partially-fluorinated structures in DFT calculations. Intermediate levels of fluorination

were calculated by adding single fluorine atoms to the Sr-327 unit cell: from 0 (unfluorinated $\text{Sr}_3\text{Ir}_2\text{O}_7$) to 8 (fully fluorinated $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$). All symmetry-inequivalent sites were tested for each F atom added, and the structure was then fully relaxed (starting based on a linear interpolation of the two relaxed endpoints, $\text{Sr}_3\text{Ir}_2\text{O}_7$ and $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$). The fluorine site leading to the lowest energy after relaxation was chosen, and that site was kept occupied as further atoms were added. This allows for the absorption energy for n fluorine atoms within the $\text{Sr}_3\text{Ir}_2\text{O}_7$ matrix to be determined as follows:

$$E_{\text{Abs}}(n) = E_{\text{tot}}[(\text{Sr-327})_4\text{F}_n] - 4E_{\text{tot}}[\text{Sr-327}] - n\mu_{\text{F}}. \quad (1)$$

The chemical potential of fluorine (referenced to fluorine gas in the dilute limit) was then determined to be $\mu_{\text{F}} = -0.797$ eV based on the vapor pressure of CuF_2 at 200 °C,⁴⁰ assuming total dissociation into F_2 gas. This also allows the calculation of the “insertion energy” of F, the energy change upon adding one additional fluorine atom to the unit cell:

$$E_{\text{Ins}}(n) = E_{\text{Abs}}(n) - E_{\text{Abs}}(n-1). \quad (2)$$

These quantities are shown as a function of $x = n/4$, the number of fluorine atoms per formula unit, in Figure 6. These results show that fluorine incorporation is strongly exothermic up to $x = 2$, but moderately endothermic for higher x . This agrees with the rapid, low temperature fluorination observed in experiments and explains why the system rapidly runs to complete fluorination $x = 2$. Partial fluorination inevitably results in samples with regions of $x = 2$ and $x = 0$ concentrations, and potential annealing in the absence of a F source may allow for further staging behavior to occur.

Electronic structure calculations were also performed to investigate the band structure of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$. The Brillouin zone was sampled using a $1 \times 4 \times 4$ Γ -centered grid—only a single \mathbf{k} -point point is needed in the k_z direction because of the size of the long-axis lattice parameter and the quasi-2D nature of the material. Using $U = 1.6$ eV, the resulting band structure is plotted in Figure 7. The 0.40 eV gap is indirect between the conduction-band minimum (CBM), located 19% along X- Γ , and the valence-band maximum (VBM), located 50% along X- Γ . The VBM state has 53% Ir d character and 42% O p character, while the CBM has 61% Ir d character and 36% O p character. If the U term is removed from the calculation, the system remains gapped, confirming the band insulating character. Additionally, the valence band is comprised of comparable weights of t_{2g} orbitals, consistent with the formation of a spin-orbit entangled $J = 0$ valence state. However, the DFT model further predicts substantial spectral weight arising from e_g orbitals within the valence band. This does not conform to a simple picture of low spin d^4 electrons isolated in a spin-orbit quenched t_{2g} multiplet, and instead suggests that the route to the $J = 0$ ground state is more complex than a conventional $L \cdot S$ -coupling scheme.

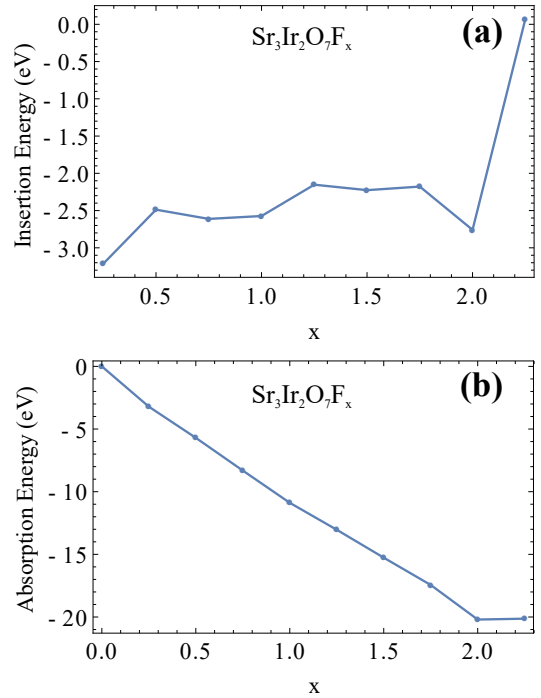


FIG. 6: (a) Fluorine absorption energy (Eq. 1) and (b) insertion energy (Eq. 2) of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_x$. This shows that fluorine incorporation will proceed spontaneously until $x = 2$, in agreement with the synthesis results.

Finally, the band structure was also computed in the absence of spin-orbit coupling (results not shown). Without spin-orbit coupling there is no gap, and the Fermi level crosses Ir d states in the minority spin channel. These results reveal a band insulator whose charge gap is reliant on the strong spin-orbit coupling inherent to Ir cations in the system.

D. Discussion

While topochemical transformations of R.P. phases via F insertion have been explored for a number of transition metal oxides, iridates are rather underexplored. One obstacle has been the difficulty of preparing phase pure powder specimens of $\text{Sr}_3\text{Ir}_2\text{O}_7$ —powder can only be stabilized under high pressure conditions⁴¹ and, even then, powder often includes Sr_2IrO_4 and SrIrO_3 impurities. As a remedy, our results show that insertion of F anions can be directly realized within single crystals of $\text{Sr}_3\text{Ir}_2\text{O}_7$ where the reaction proceeds under relatively soft conditions (250 °C for 2 hours).

The insertion of F into $\text{Sr}_3\text{Ir}_2\text{O}_7$ parallels previous reactions of powders with dissociated CuF_2 in bilayer R.P. oxides such as $\text{La}_3\text{Ni}_2\text{O}_7$ ⁵, $\text{Sr}_3\text{Ru}_2\text{O}_7$ ³⁵, as well as in alloyed variants with mixed transition metal sites such as $\text{Sr}_3(\text{Mn}_{0.5}\text{Ru}_{0.5})_2\text{O}_7$ ⁴². The shallow slope of the insertion energy in $\text{Sr}_3\text{Ir}_2\text{O}_7$ locally drives the complete transformation of $\text{Sr}_3\text{Ir}_2\text{O}_7$ into $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ such that crys-

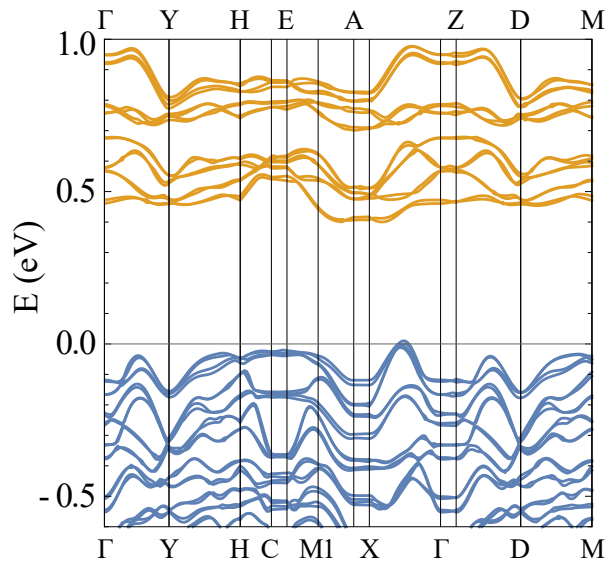


FIG. 7: Band structure of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ (cell defined such that the z-axis is aligned out of the iridium oxide planes). Occupied valence bands are shown in blue, and unoccupied conduction bands are shown in orange.

tals reacted for shorter periods of time are comprised of local patches of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ and $\text{Sr}_3\text{Ir}_2\text{O}_7$. Due to the large interface energy of these two phases within a single crystal, further staging behavior such as an intermediate $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}$ phase may be realizable if the initial F loading and postgrowth annealing procedures are optimized.

NMR measurements reveal that F insertion into $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ generates only a single local F environment, albeit one with substantial broadening. The main contribution to the NMR linewidth is likely due to residual homonuclear dipolar coupling interactions between the F spins in the layer, even under fast (50 kHz) magic angle spinning of the sample during data acquisition. Yet, we cannot exclude that local disorder also contributes to a lesser extent to the linewidth of the ^{19}F resonance.

The single resonant frequency attributed to $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ is consistent with F insertion only within the SrO rocksalt layers of the crystal matrix, and there is no indication of the partial anion exchange of F with apical O sites closest to F layers previously observed in $\text{Sr}_3(\text{Ti}_{0.5}\text{Ru}_{0.5})_2\text{O}_6\text{F}_2$ ⁴² and $\text{Sr}_3\text{Fe}_2\text{O}_6\text{F}_2$ ⁴³. Scattering data further support this claim with the bond valence sums (BVS)⁴⁴ of the nominal F site totaling 1.16 for x-ray data and 1.19 for the neutron data assuming F occupation versus 1.56 when assuming O occupation. The BVS of the nominal F sites assuming F occupation is also consistent other $n = 2$ R.P. systems where F is known to insert between bilayers,^{35,45} and the average Sr-F bond length of 2.47 Å is close to the 2.511 Å bond length of SrF_2 ⁴⁶.

Within the iridium-oxygen bilayers, the insertion of F affects an increased distortion of the IrO_6 octahedra and a commensurate increase in the bond valence sum of Ir

cations from 4.18 in $\text{Sr}_3\text{Ir}_2\text{O}_7$ to 5.09 in $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$. This is consistent with the oxidation state of Ir being raised from Ir^{4+} to Ir^{5+} and the near complete intercalation of two F anions per formula unit. The addition of F anions above and below the IrO_6 bilayers also drives a large contraction of the outermost apical Ir-O2 bond lengths from 2.022(2) Å in $\text{Sr}_3\text{Ir}_2\text{O}_7$ to 1.87(1) Å in $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$. This is consistent with other F intercalated bilayer systems that do not undergo anion exchange³⁵. While the overall extent of the bilayer blocks along the long-axis (distance between neighboring O2 sites along a) is shortened due to the compression of the Ir-O2 bond lengths, the distance between Ir atoms is unaffected due to the accompanying overall expansion of the a -axis.

The change in Ir-O bond lengths and the increased distortion of the IrO_6 octahedra observed in scattering data are consistent with DFT calculations of the relaxed structure; however more precise comparisons of changes in the Ir-O-Ir bond angles upon F insertion are prohibited by the large uncertainties inherent to the single crystal neutron diffraction data. This uncertainty is largely driven by a broadened crystal mosaic created by the F insertion process. Upon F insertion, the crystal mosaic (defined by the full width at half maximum scattering intensity distribution of crystallites) increases from $< 0.5^\circ$ to $\approx 3^\circ$ in the larger (several mg) crystals suitable for neutron diffraction measurements. DFT calculations show that the origin of the charge gap is predicated on the inclusion of spin-orbit coupling in the model, and spin-orbit coupling effects on the electronic ground state are further confirmed by XAS measurements that reveal a strongly enhanced branching ratio at the Ir L_3 and L_2 absorption edges. This is consistent with the formation of a $J = 0$ ground state within the low spin $5d^4$ valence electrons, despite the strong deviation of the local crystal field from perfect cubic symmetry. A number of other octahedrally coordinated Ir^{5+} systems have also been observed to manifest a $J = 0$ ground state in lattice geometries varying from corner sharing double perovskites⁴⁷ to edge-sharing honeycomb lattices³⁸ to isolated octahedra.³⁹

The lack of an appreciable local moment in the low field magnetization of $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ and, more specifically, the absence of fluctuation-driven magnetic order is notable. There is considerable interest in investigating the possibility of a spin-orbital liquid state^{48,49} as well as other unconventional magnetic states⁵⁰ in strongly spin-orbit coupled d^4 $J = 0$ spin systems. The conversion of $\text{Sr}_3\text{Ir}_2\text{O}_7$, a system thought inherently close to a dimer instability^{51,52}, into $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ is a test case for exploring the presence of these electronic phases. $\text{Sr}_3\text{Ir}_2\text{O}_7$ itself also lacks a high temperature Curie-Weiss response above its antiferromagnetic ordering temperature, and any rare, phase separated regions of $\text{Sr}_3\text{Ir}_2\text{O}_7$ within the crystal naively should not yield a measurable local moment. Instead the measured $\mu_{\text{eff}} \approx 0.2 \mu_B$ reflects a dilute concentration of impurity moments likely arising from another defect mechanism such as a low concentra-

tion of oxygen vacancies.

IV. CONCLUSIONS

We have demonstrated that single crystals of the $J_{eff} = 1/2$ Mott insulator $\text{Sr}_3\text{Ir}_2\text{O}_7$ can be converted into the $J = 0$ band insulator $\text{Sr}_3\text{Ir}_2\text{O}_7\text{F}_2$ via the insertion of fluorine into the crystal matrix. Reaction of crystals embedded within CuF_2 powder proceeds rapidly and converts the entirety of Ir^{4+} cations into Ir^{5+} with negligible anion exchange observed. F atoms insert within the SrO interstitial planes between the bilayers of the lattice, resulting in a strong perturbation to the IrO_6 octahedral environments away from an ideal cubic symmetry. Despite this distortion, x-ray absorption measurements and first principles calculations are consistent with the formation of a spin-orbit entangled $J = 0$ electronic ground state that possesses a charge gap reliant on the strong spin-orbit coupling inherent to the Ir cations.

V. ACKNOWLEDGMENTS

This work was supported primarily by ARO Award W911NF-16-1-0361 (S.D.W., C.P., Z. P.). M. W. S. was supported by the MRSEC Program of the National Science Foundation under Award No. DMR-1121053. The MRL Shared Experimental Facilities are supported by the MRSEC Program of the NSF under Award No. DMR 1720256; a member of the NSF-funded Materials Research Facilities Network. The work at HYU was supported by Basic Science Research Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Science, ICT and Future Planning (Grant No. 2017R1A2B4009413). The work at ORNL's HFIR was sponsored by the Scientific User Facilities Division, Office of Science, Basic Energy Sciences, U.S. Department of Energy. Research conducted at CHESS is supported by the NSF under award DMR-1332208.

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